

# The flavor composition of high-energy cosmic neutrinos

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Niels Bohr Institute, University of Copenhagen

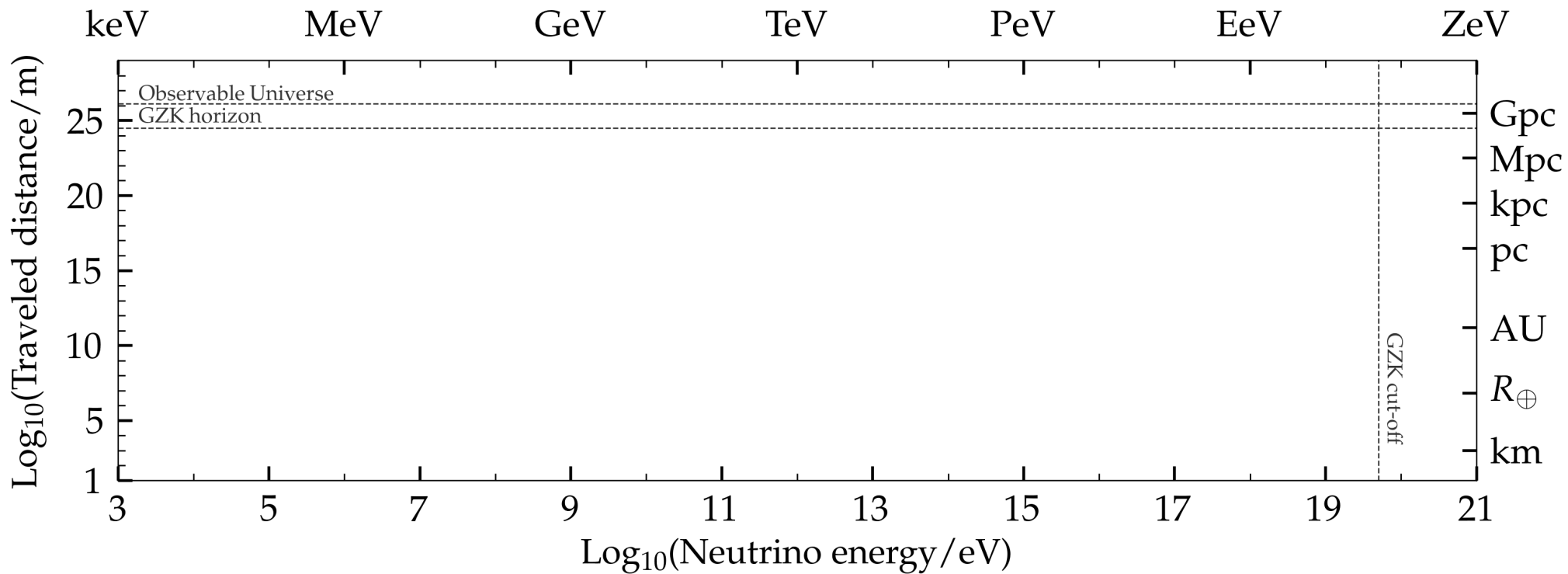
Neutrinos from Home  
December 02–05 , 2025

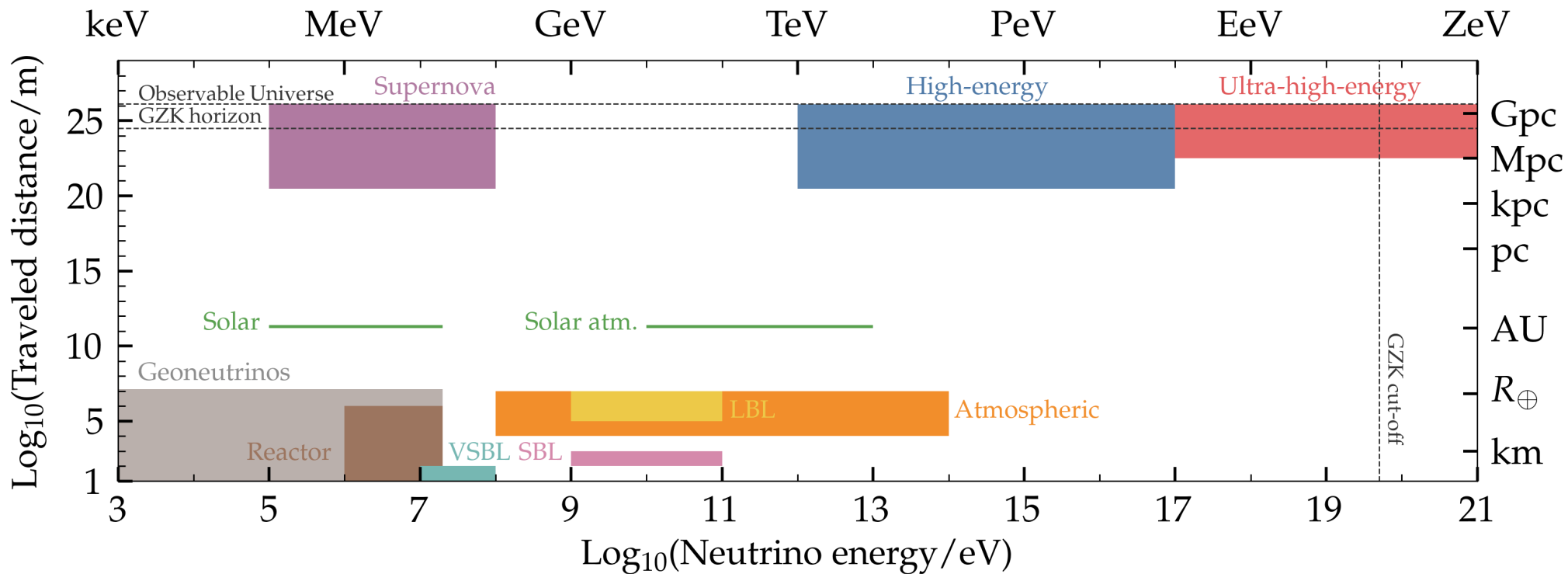
UNIVERSITY OF  
COPENHAGEN



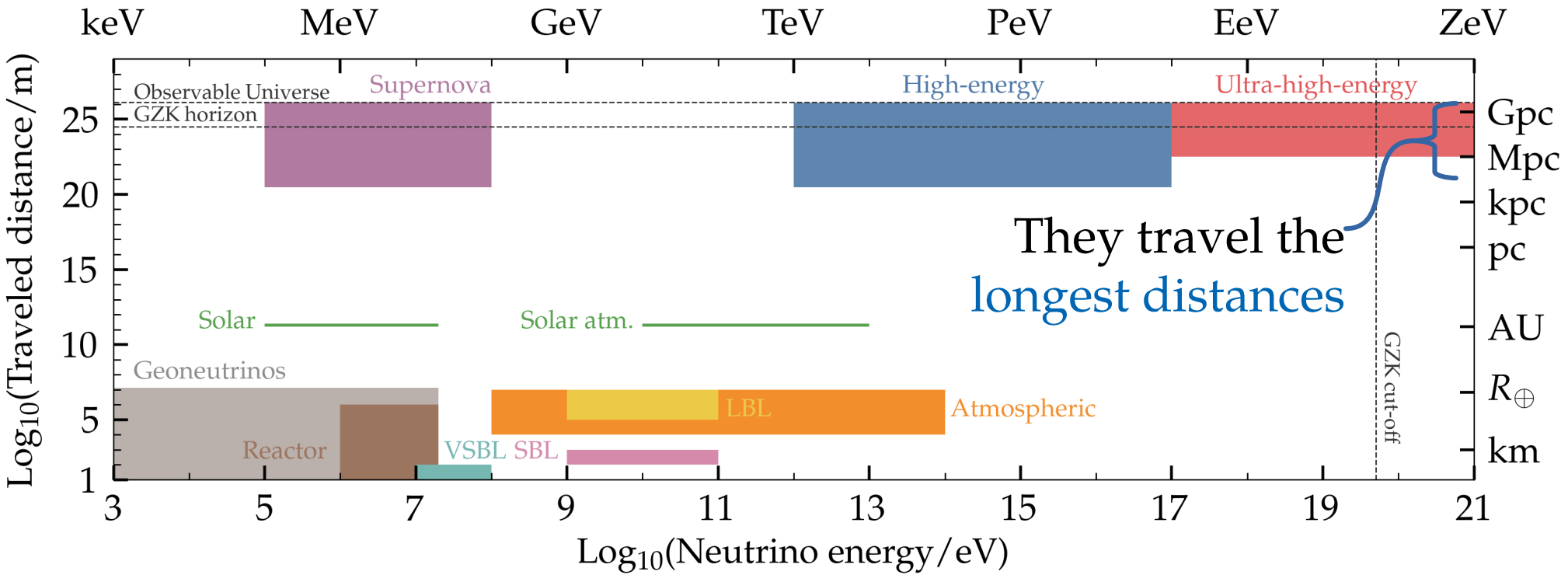
VILLUM FONDEN



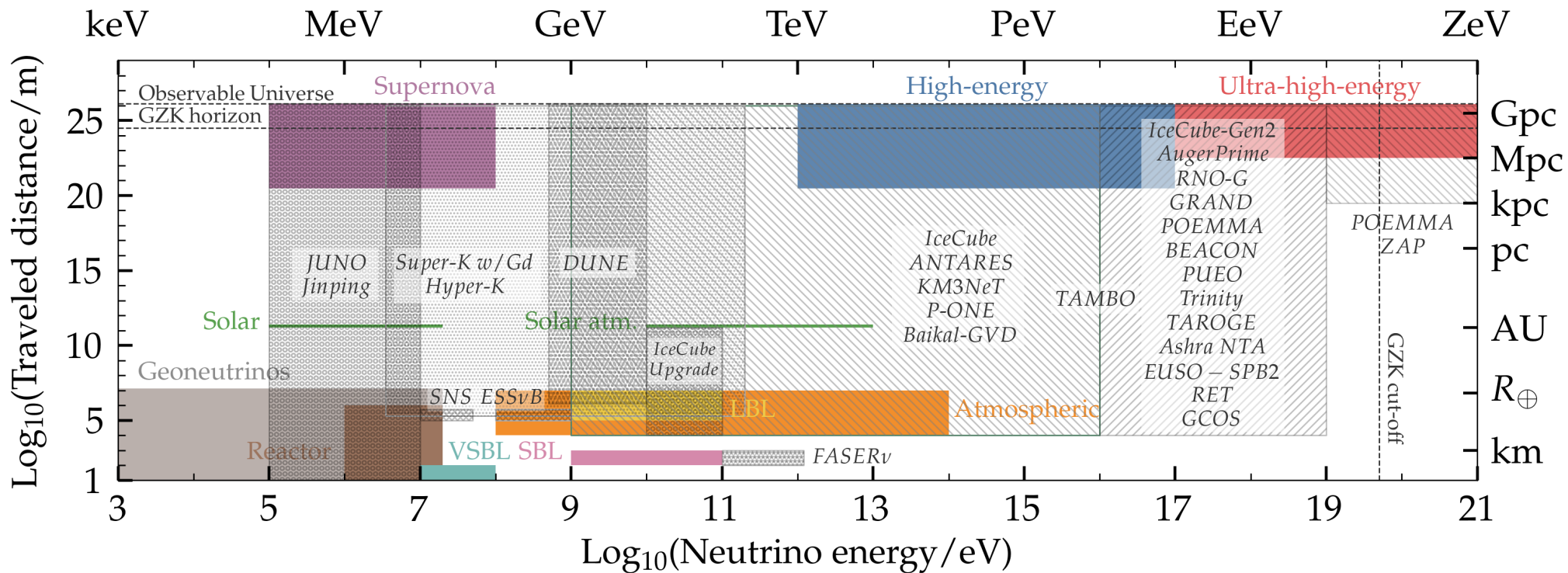


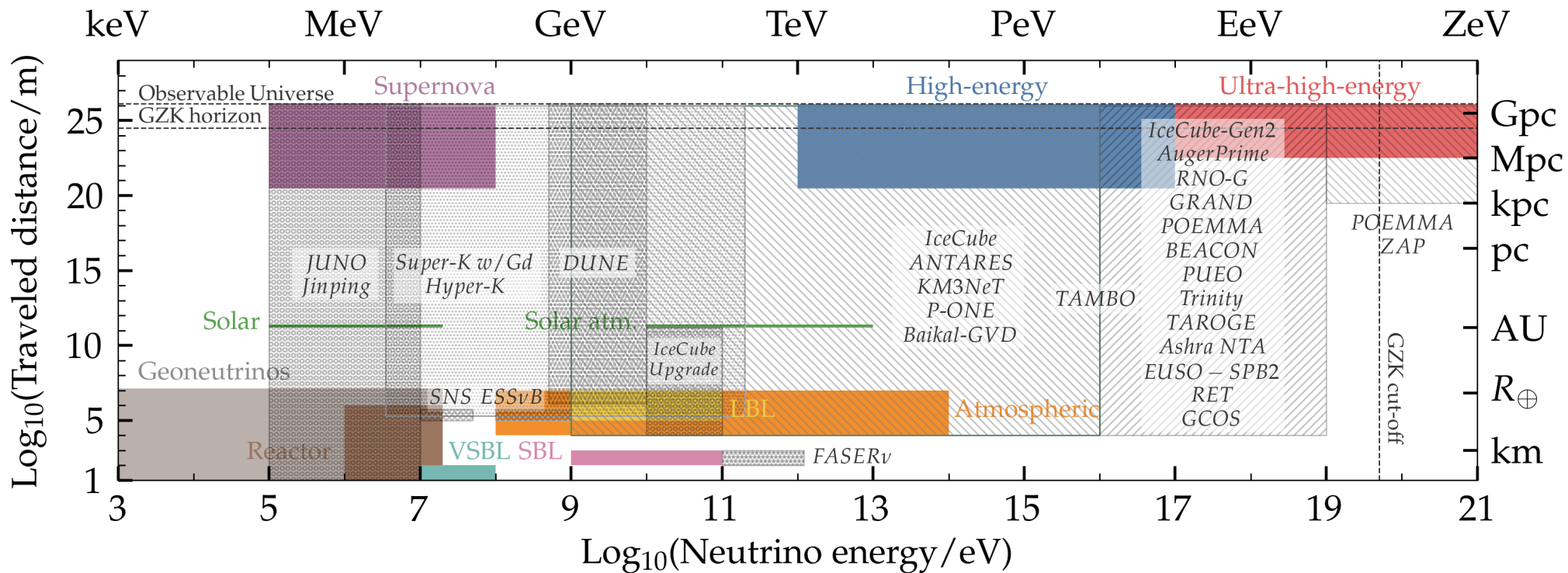


They have the **highest energies**



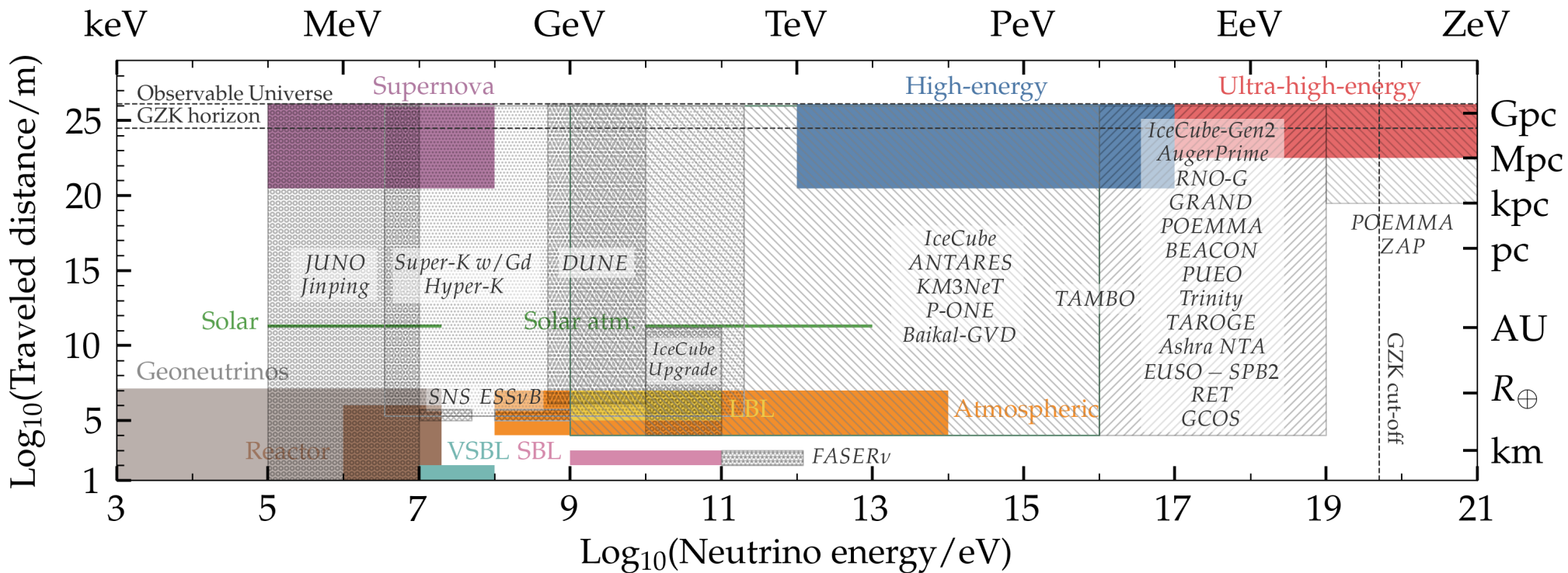
They travel the **longest distances**





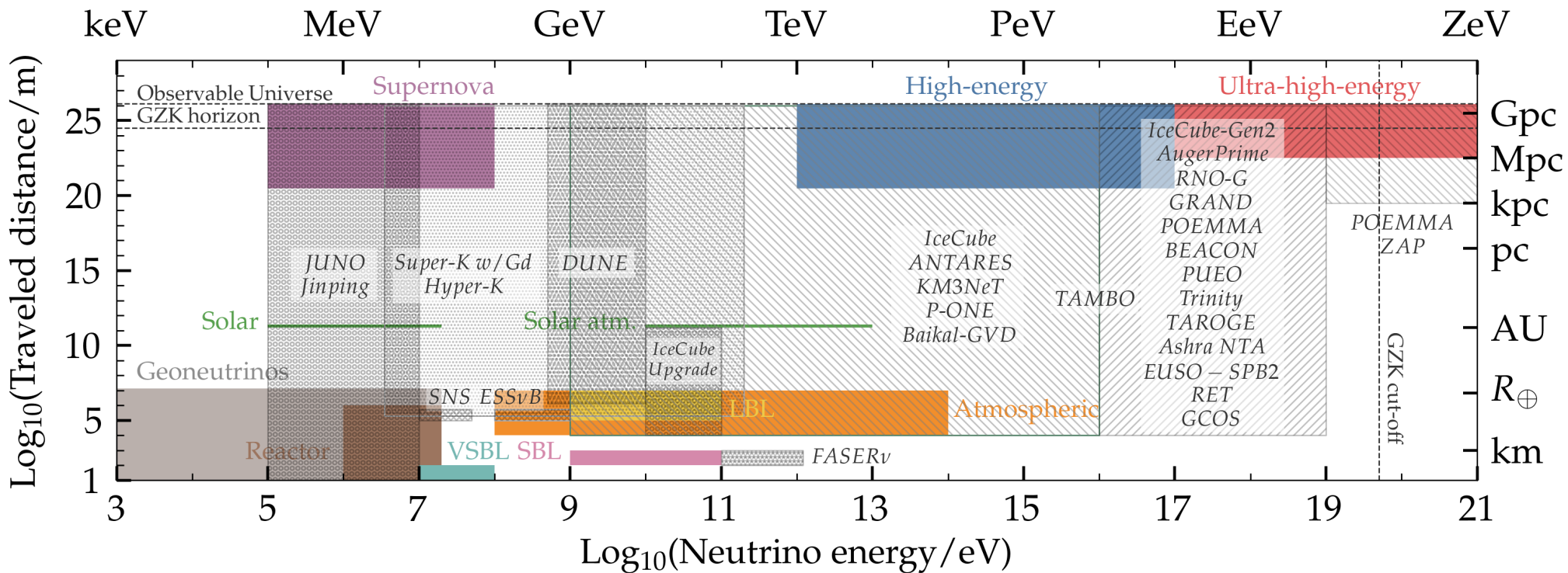
Synergies with lower energies

Discovered in 2013  
by IceCube



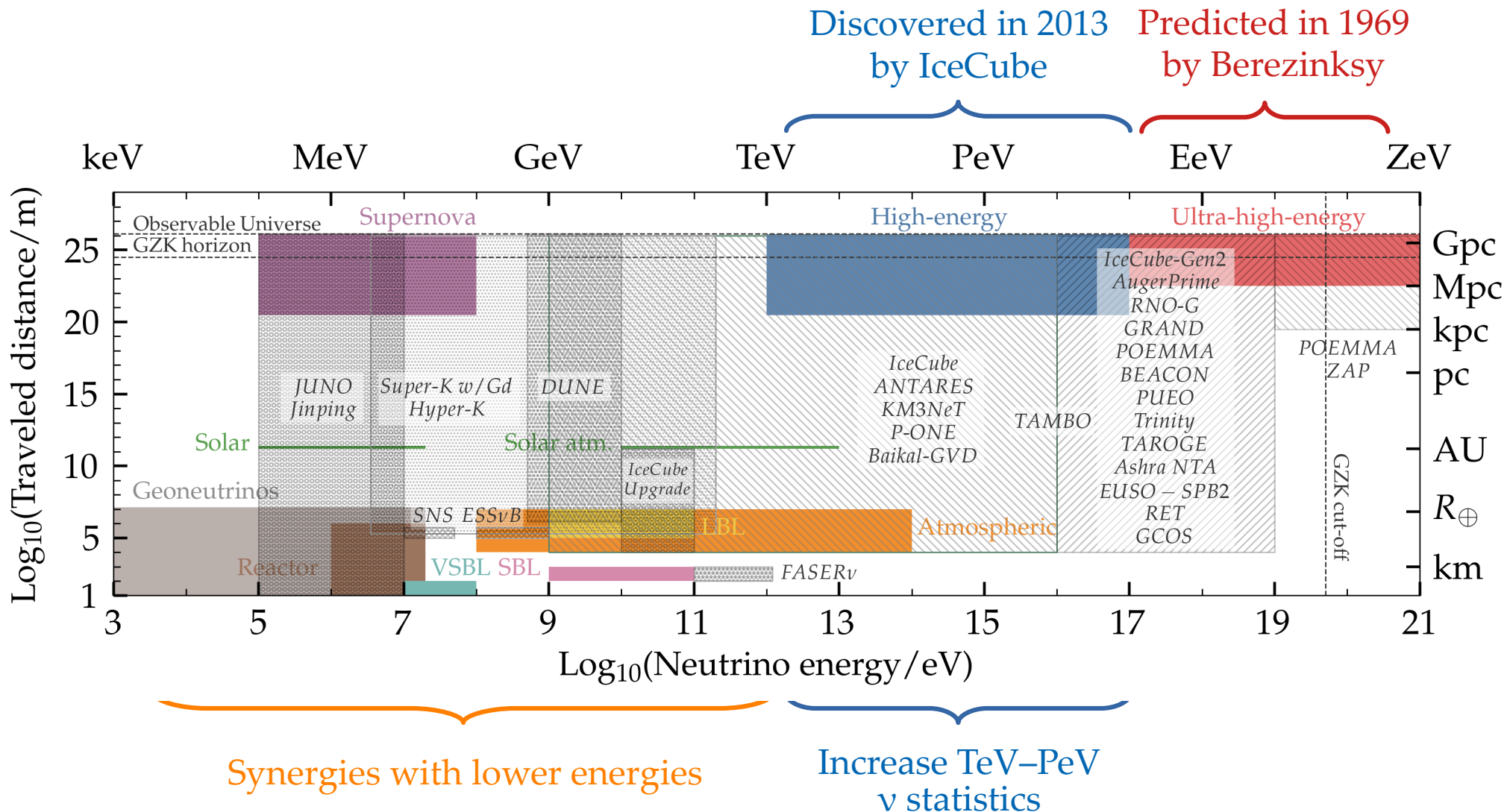
Synergies with lower energies

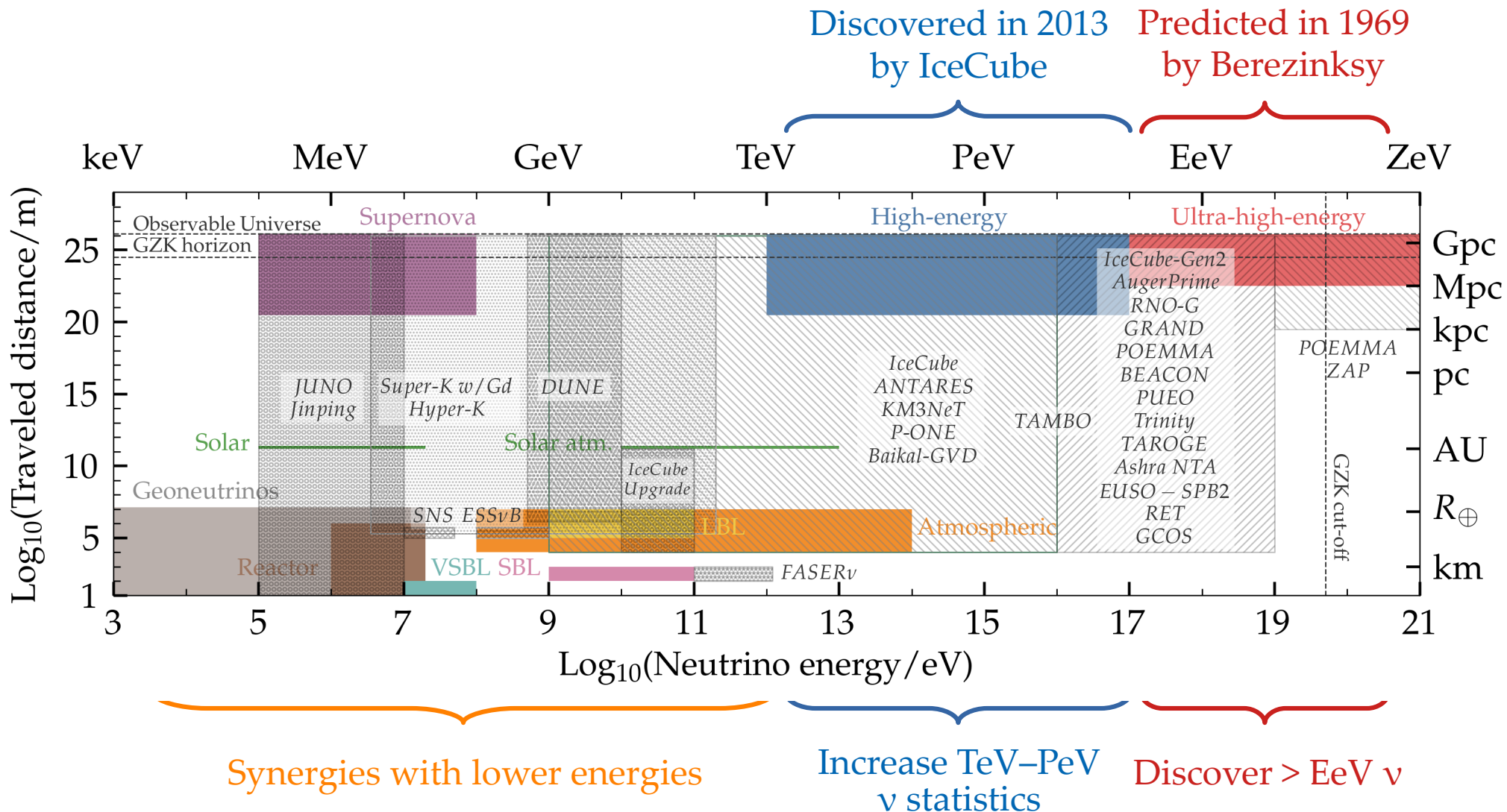
Discovered in 2013  
by IceCube



Synergies with lower energies

Increase TeV–PeV  
ν statistics



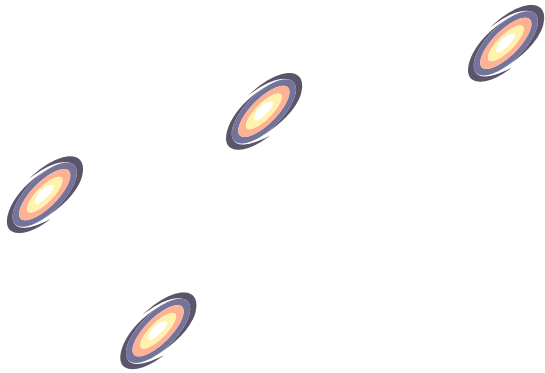


Redshift



$z = 0$

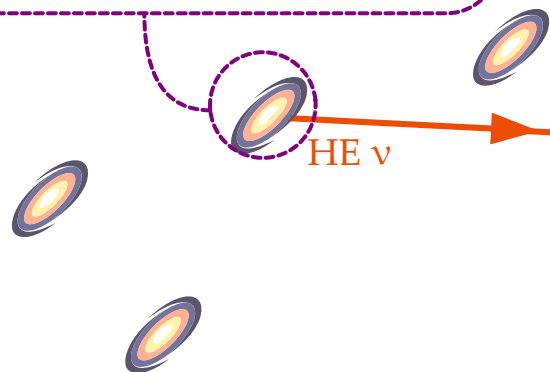
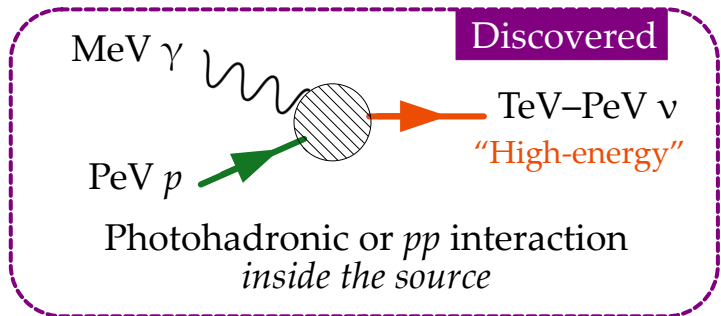
*Note:  $\nu$  sources can be steady-state or transient*



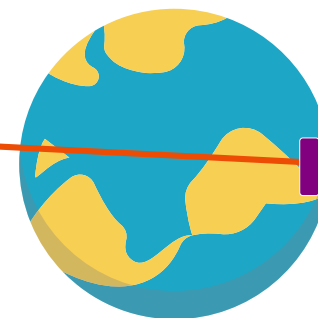
Redshift ←

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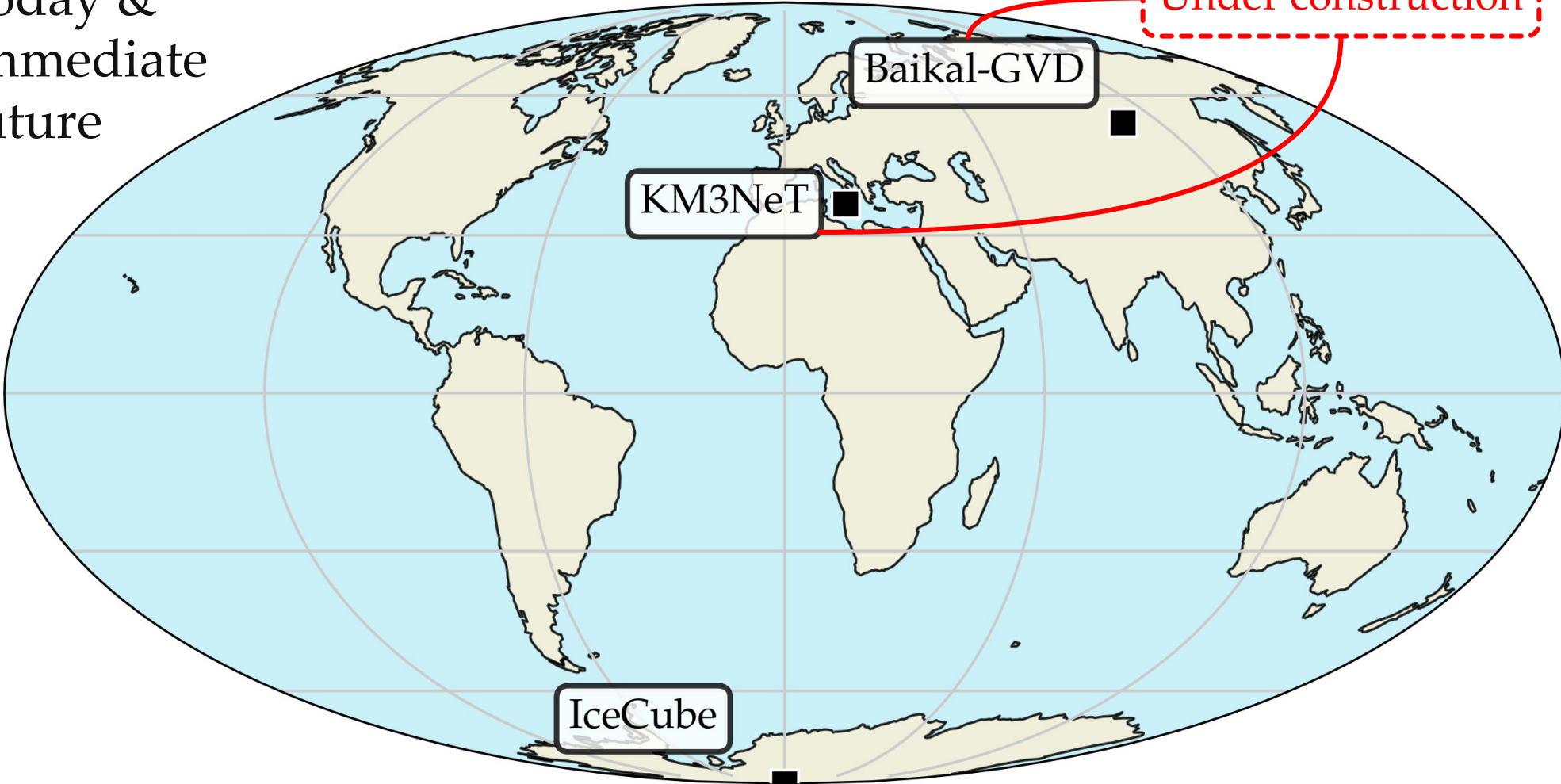


$\nu$  propagation  
inside the Earth



$\nu$  detection

Today &  
immediate  
future



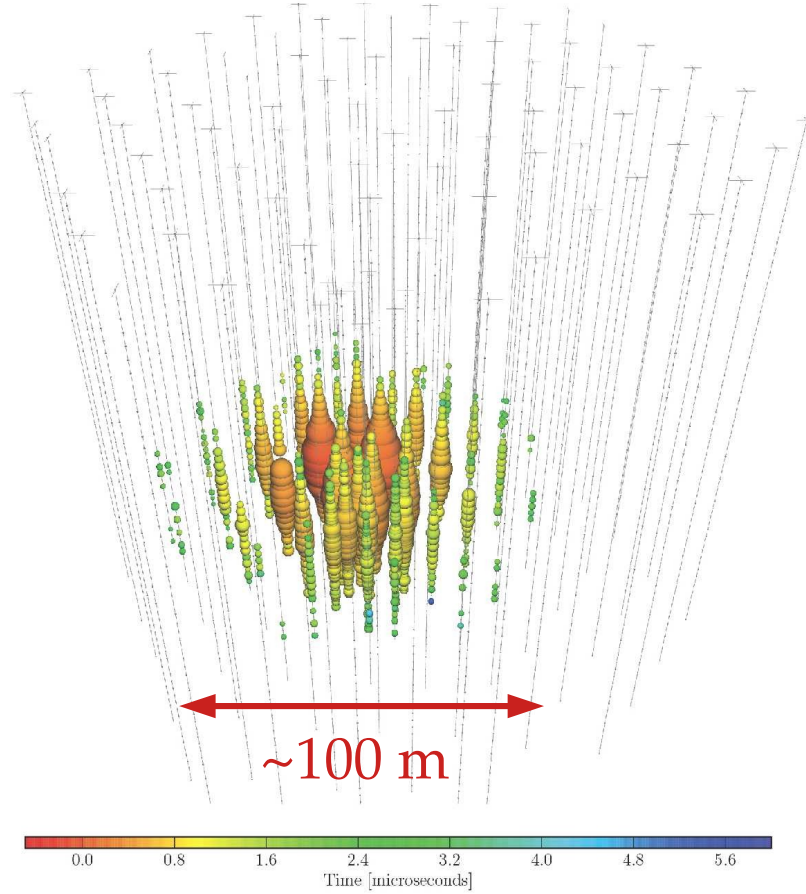
Under construction

Baikal-GVD

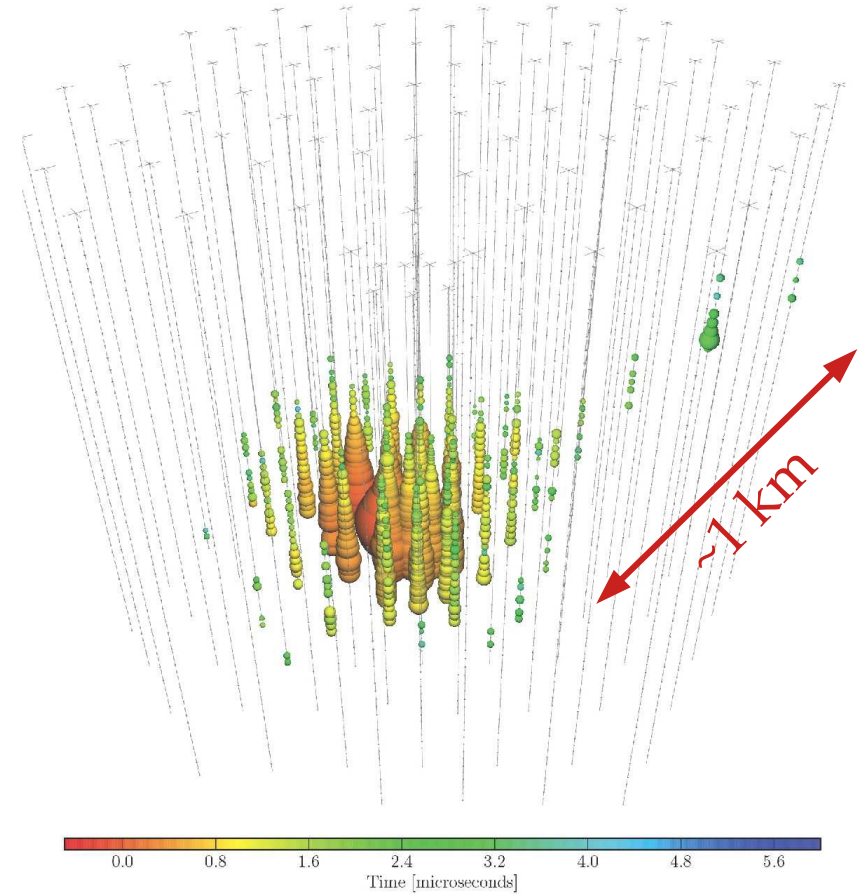
KM3NeT

IceCube

# Shower (mainly from $\nu_e$ and $\nu_\tau$ )

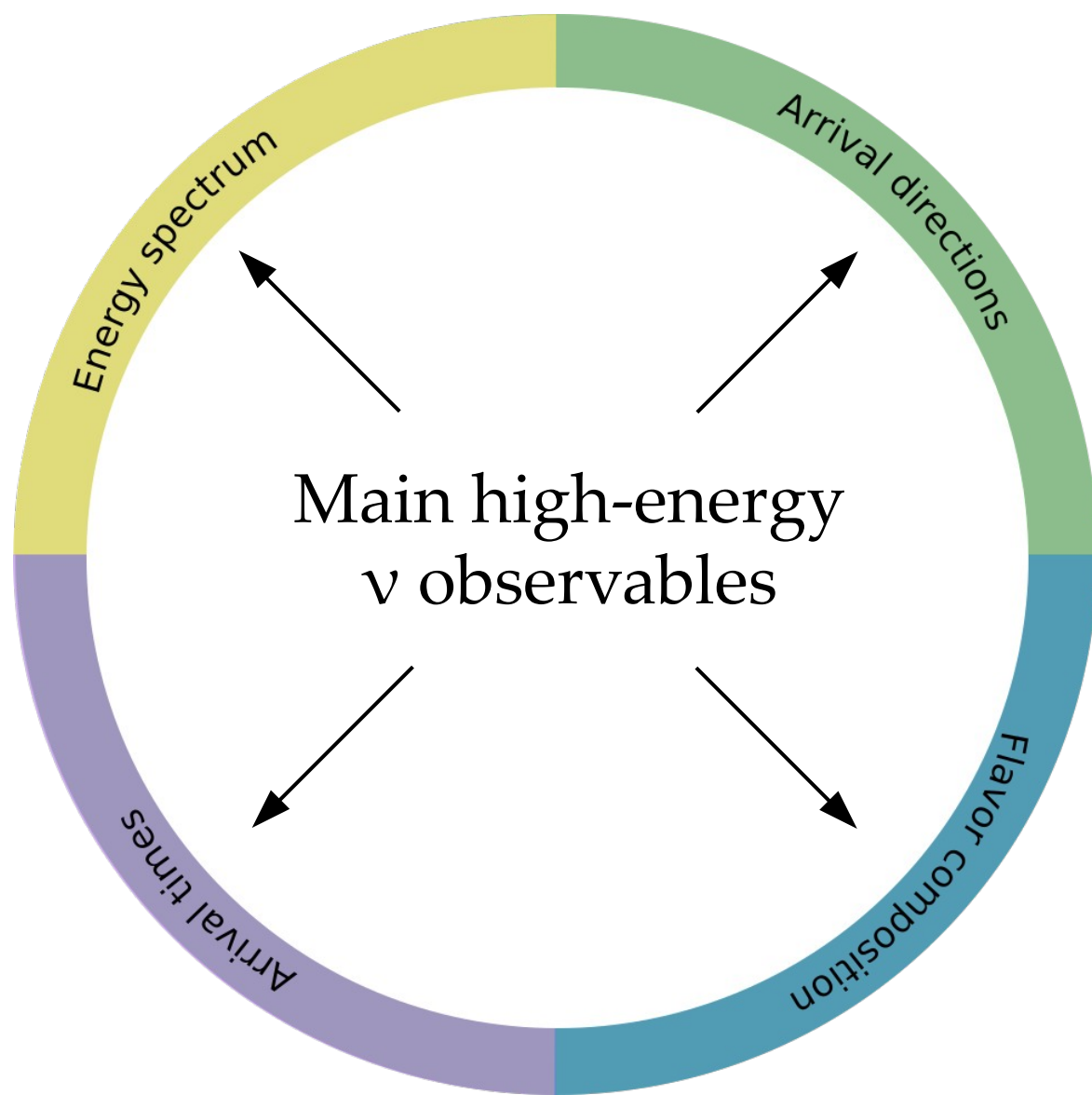


# Track (mainly from $\nu_\mu$ )



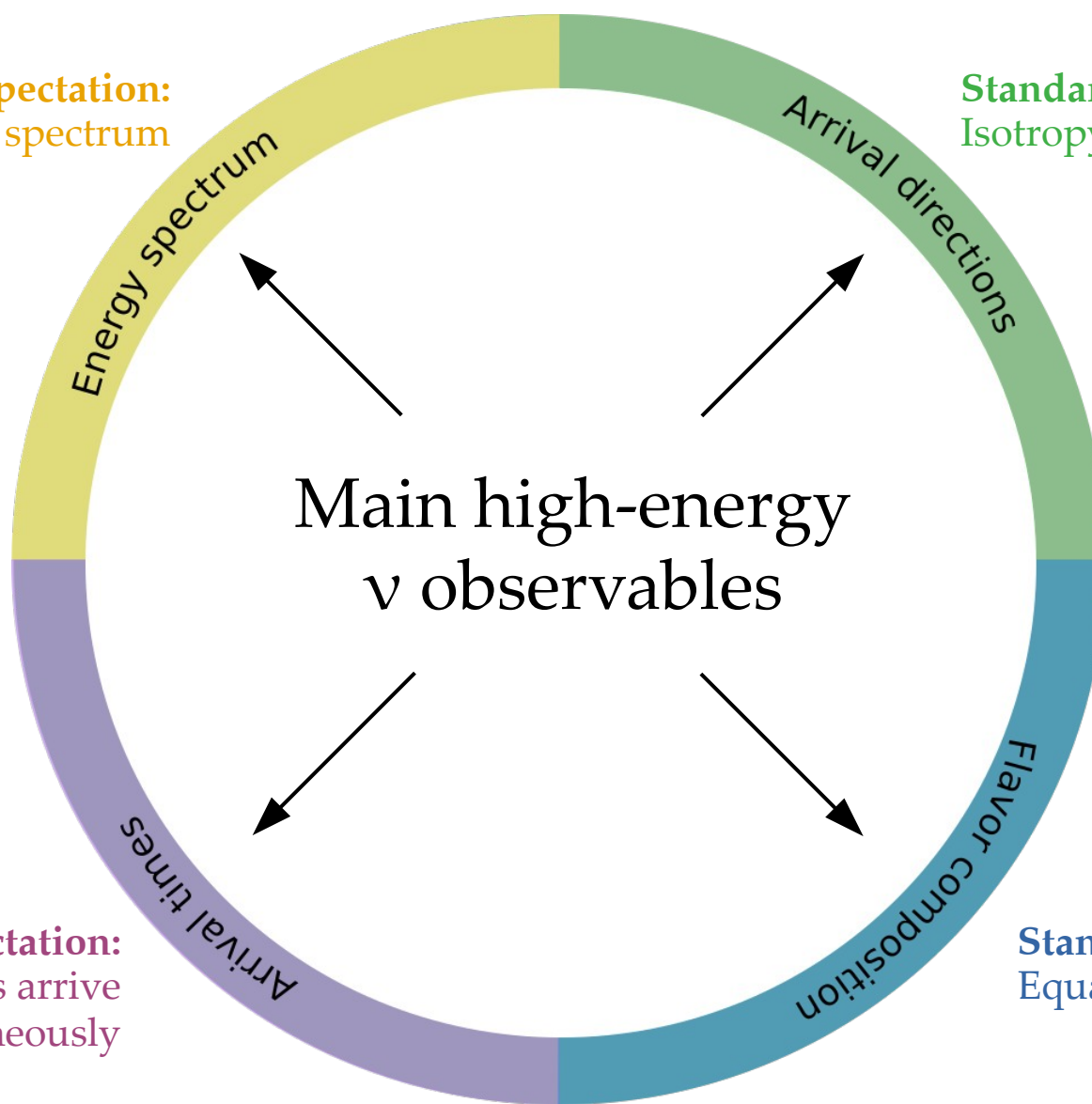
Poor angular resolution:  $< 5^\circ$

Angular resolution:  $< 1^\circ$



**Standard expectation:**  
Power-law energy spectrum

**Standard expectation:**  
Isotropy (for diffuse flux)



**Standard expectation:**  
Equal number of  $\nu_e, \nu_\mu, \nu_\tau$

**Standard expectation:**  
 $\nu$  and  $\gamma$  from transients arrive simultaneously

**Standard expectation:**  
Power-law energy spectrum

Energy spectrum

**Standard expectation:**  
Isotropy (for diffuse flux)

Arrival directions

**Standard expectation:**  
Equal number of  $\nu_e$ ,  $\nu_\mu$ ,  $\nu_\tau$

Flavor composition

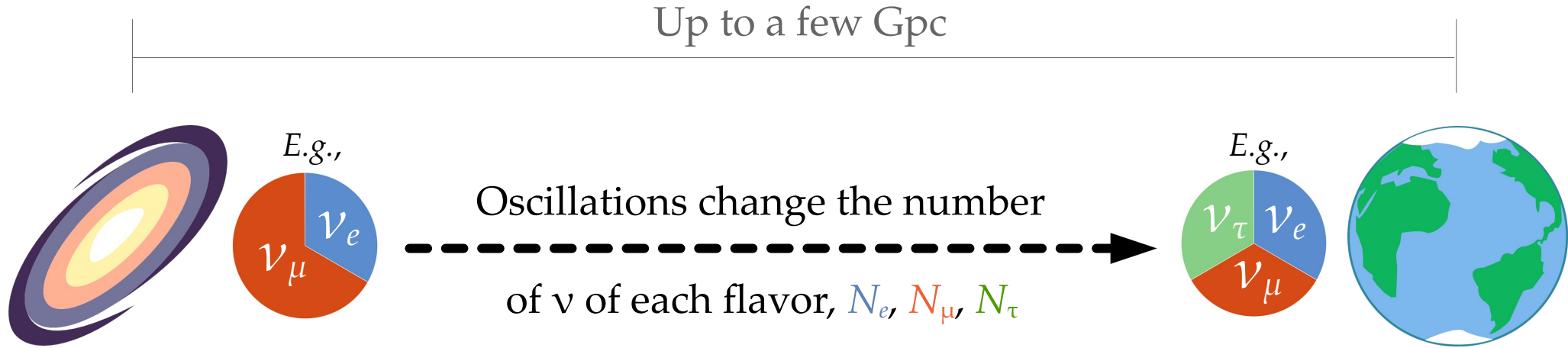
**Standard expectation:**  
 $\nu$  and  $\gamma$  from transients arrive  
simultaneously

Arrival times

# Predicting the flavor composition at Earth

Astrophysical sources

Earth



Different production mechanisms yield different flavor ratios:

$$(f_{e,S}, f_{\mu,S}, f_{\tau,S}) \equiv (N_{e,S}, N_{\mu,S}, N_{\tau,S})/N_{\text{tot}}$$

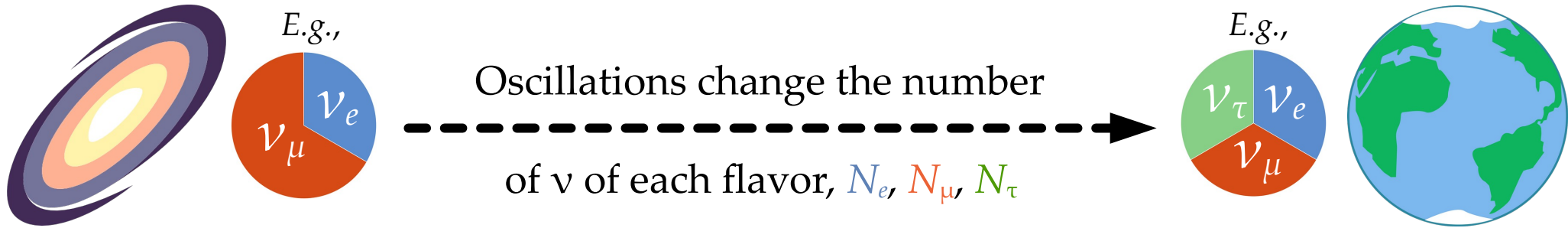
Flavor ratios at Earth ( $\alpha = e, \mu, \tau$ ):

$$f_{\alpha,\oplus} = \sum_{\beta=e,\mu,\tau} P_{\nu_\beta \rightarrow \nu_\alpha} f_{\beta,S}$$

Astrophysical sources

Earth

Up to a few Gpc



Different production mechanisms yield different flavor ratios:

$$(f_{e,S}, f_{\mu,S}, f_{\tau,S}) \equiv (N_{e,S}, N_{\mu,S}, N_{\tau,S})/N_{\text{tot}}$$

Flavor ratios at Earth ( $\alpha = e, \mu, \tau$ ):

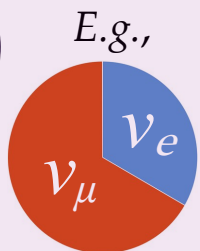
$$f_{\alpha,\oplus} = \sum_{\beta=e,\mu,\tau} P_{\nu_\beta \rightarrow \nu_\alpha} f_{\beta,S}$$

Standard oscillations  
or  
new physics

*From sources to Earth:* we learn what to expect when measuring  $f_{\alpha,\oplus}$



Sources



$(f_{e,S}, f_{\mu,S}, f_{\tau,S})$

Oscillations



$(\theta_{12}, \theta_{23}, \theta_{13}, \delta_{CP})$

Earth



$(f_{e,\oplus}, f_{\mu,\oplus}, f_{\tau,\oplus})$

One likely TeV–PeV  $\nu$  production scenario:

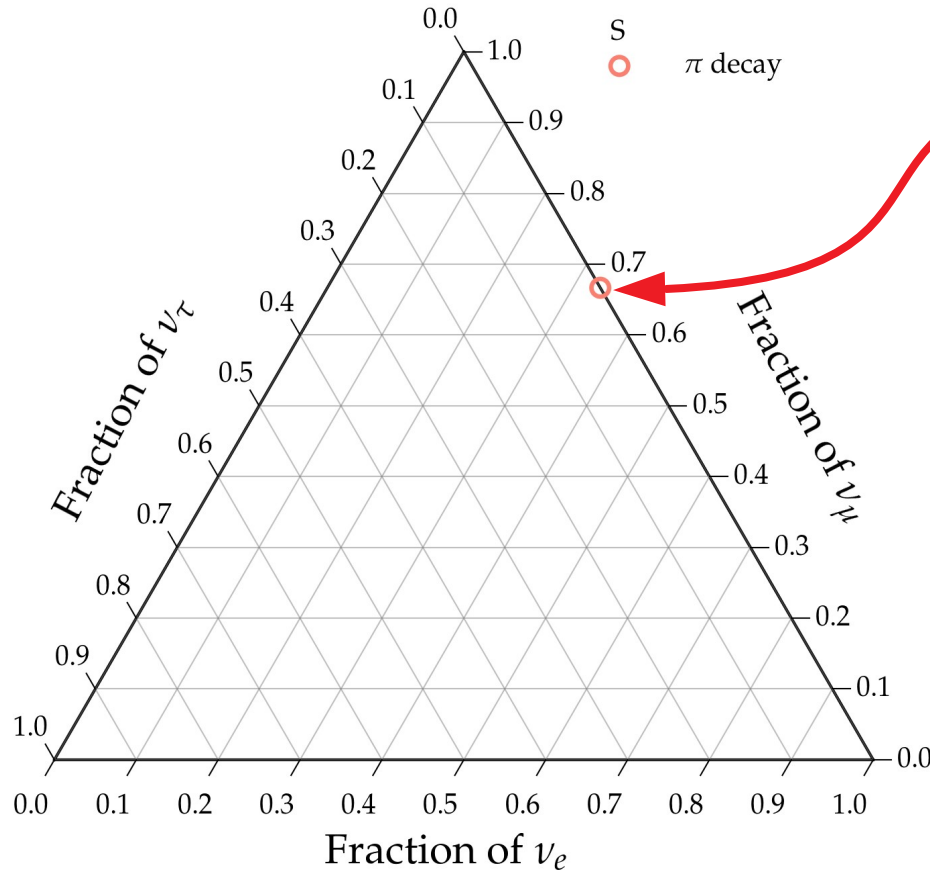
$$p + \gamma \rightarrow \pi^+ \rightarrow \mu^+ + \nu_\mu \quad \text{followed by} \quad \mu^+ \rightarrow e^+ + \nu_e + \bar{\nu}_\mu$$

Full  $\pi$  decay chain

$$(1/3:2/3:0)_S$$

*Note:*  $\nu$  and  $\bar{\nu}$  are (so far) indistinguishable  
in neutrino telescopes

One likely TeV–PeV  $\nu$  production scenario:

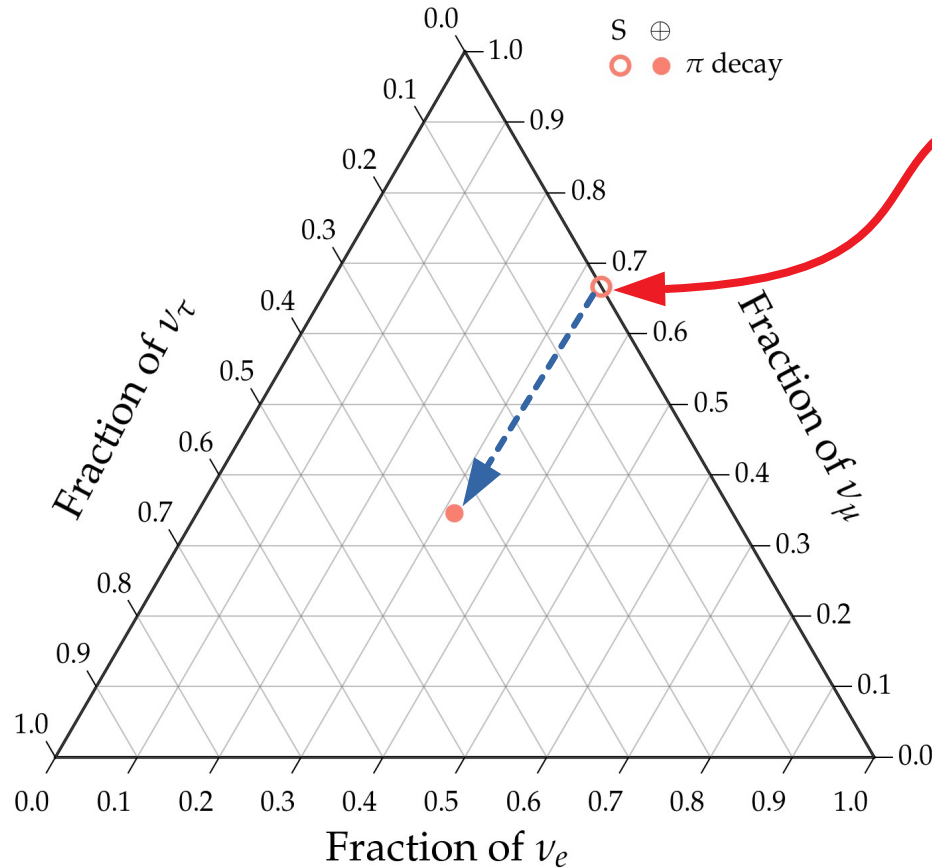


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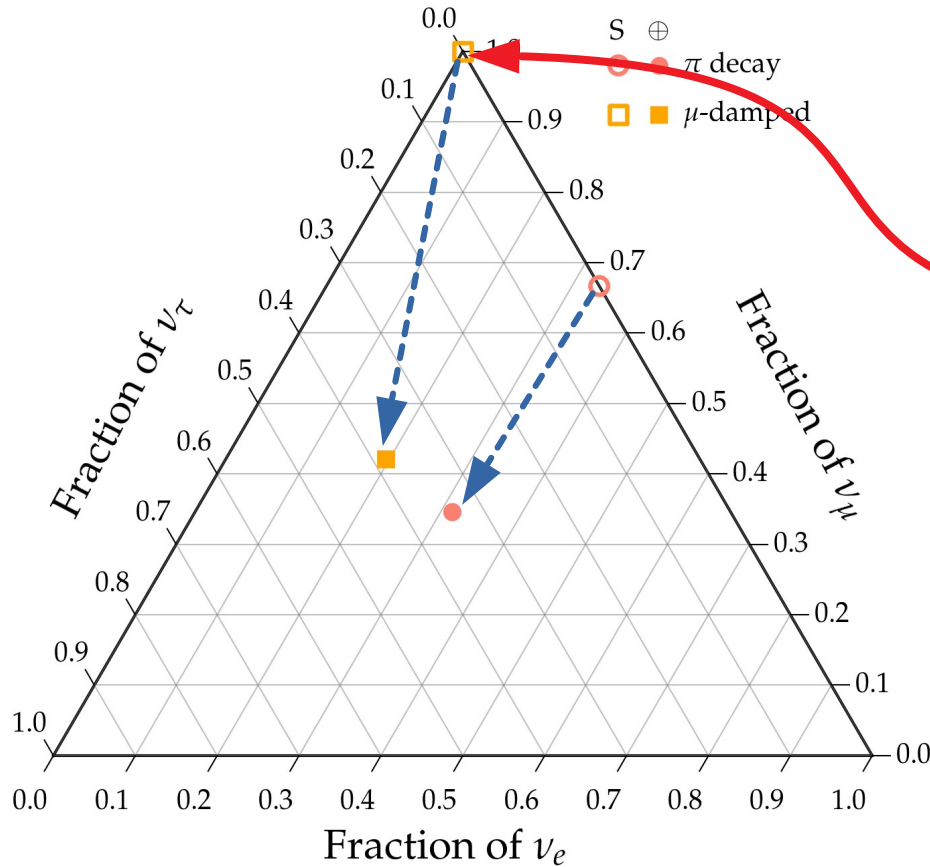


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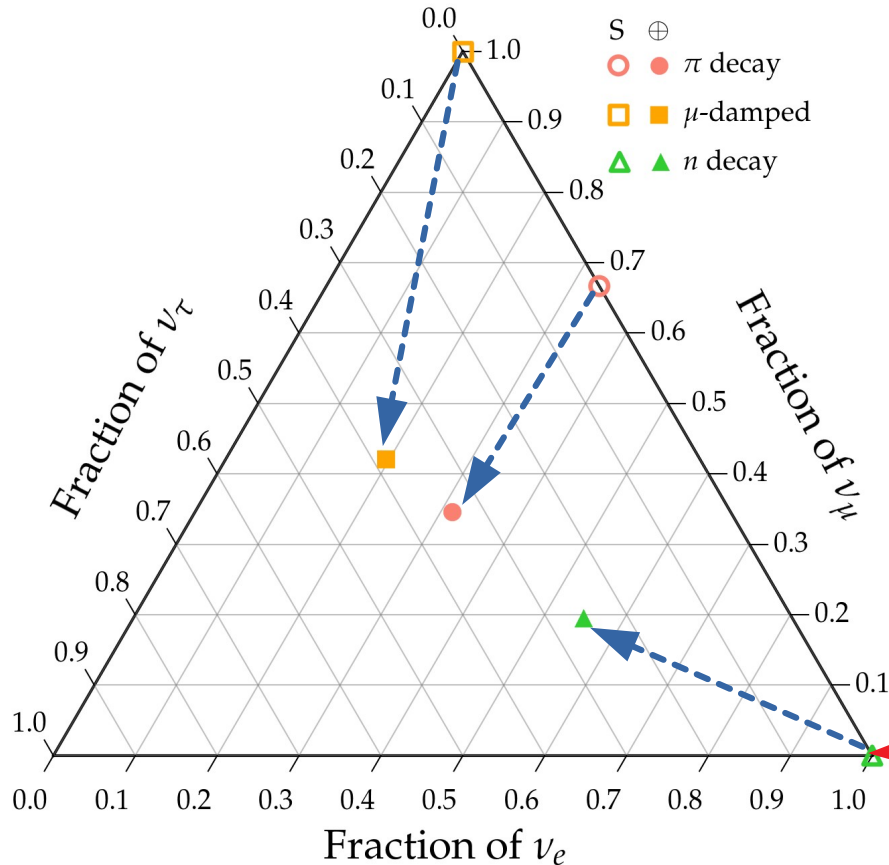
$(1/3:2/3:0)_S$

Muon damped

$(0:1:0)_S$

Note:  $\nu$  and  $\bar{\nu}$  are (so far) indistinguishable in neutrino telescopes

# One likely TeV–PeV $\nu$ production scenario:



Full  $\pi$  decay chain

$(1/3:2/3:0)_S$

Muon damped

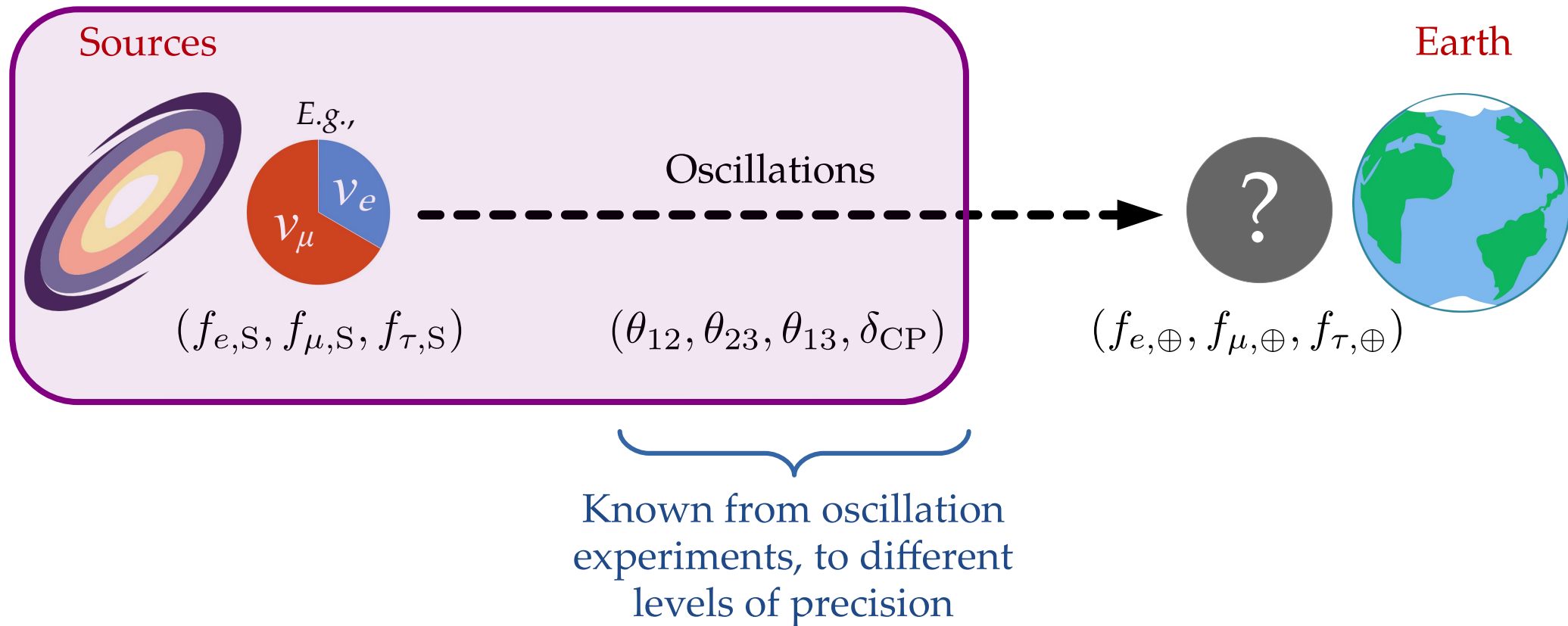
$(0:1:0)_S$

Neutron decay

$(1:0:0)_S$

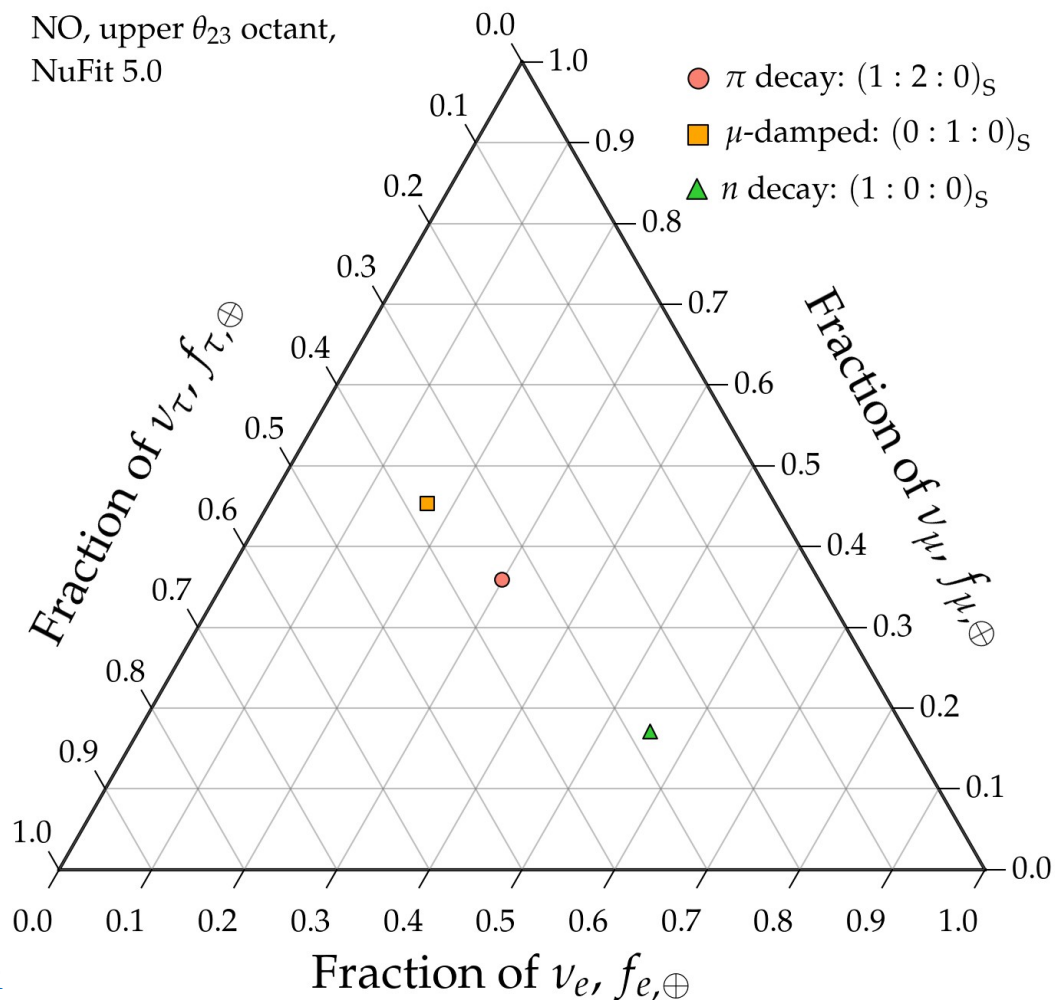
Note:  $\nu$  and  $\bar{\nu}$  are (so far) indistinguishable in neutrino telescopes

*From sources to Earth:* we learn what to expect when measuring  $f_{\alpha,\oplus}$



# Theoretically palatable regions: today

NO, upper  $\theta_{23}$  octant,  
NuFit 5.0



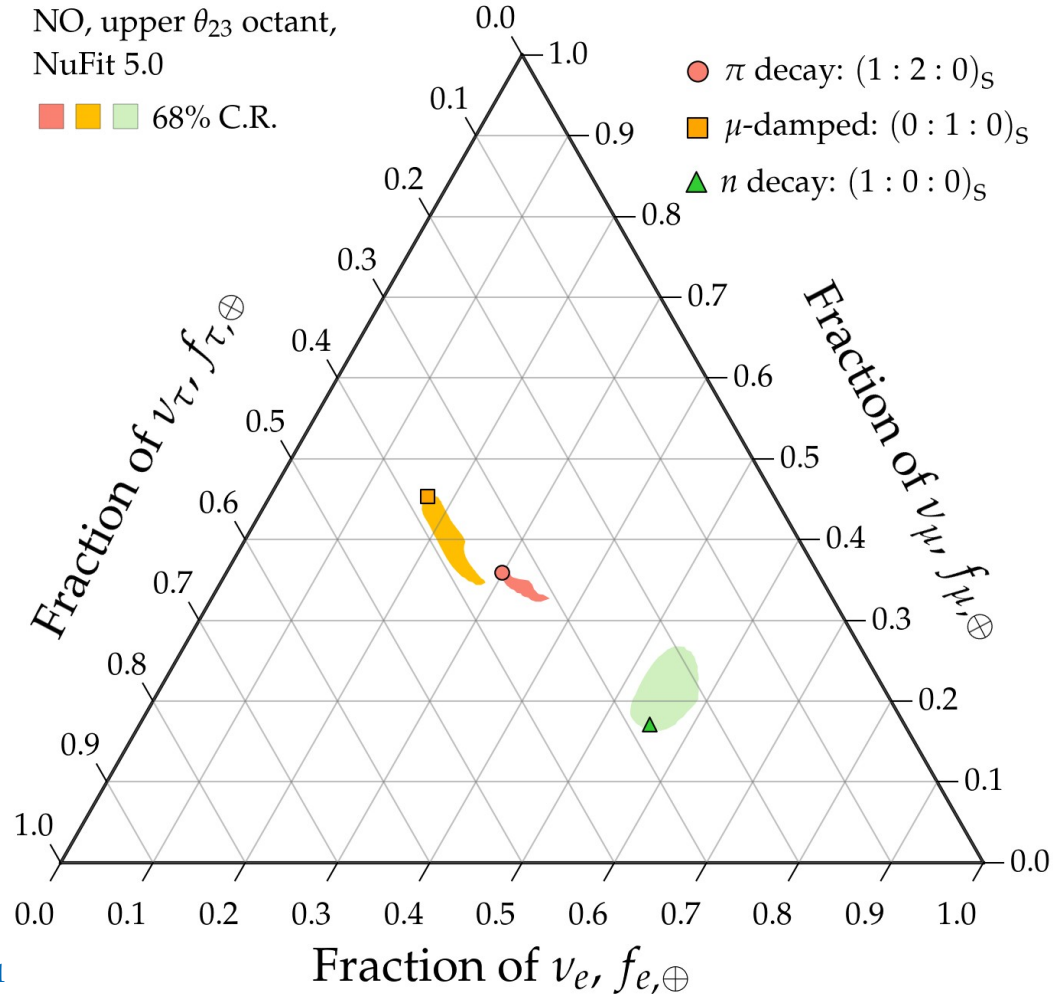
Note:

All plots shown are for normal neutrino mass ordering (NO); inverted ordering looks similar

Song, Li, Argüelles, MB, Vincent, JCAP 2021

See also: MB, Beacom, Winter, PRL 2015

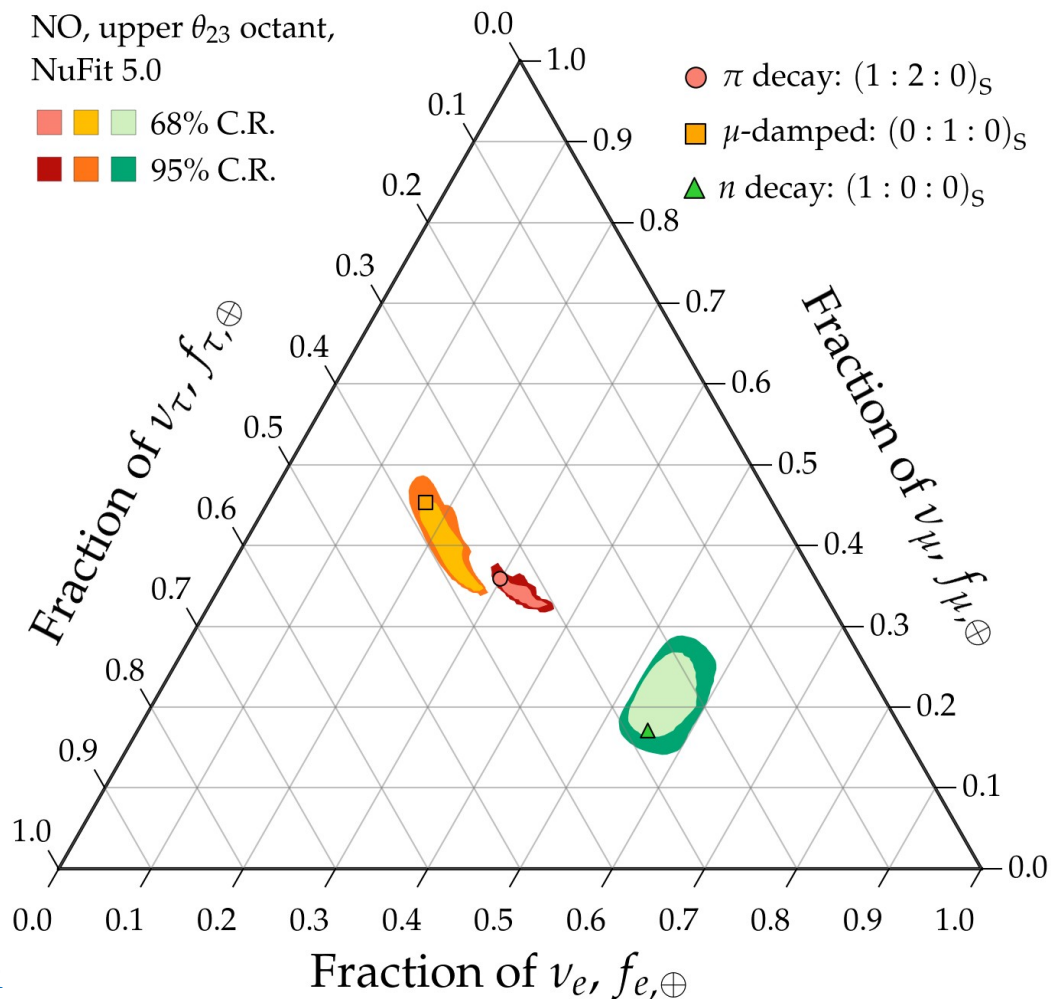
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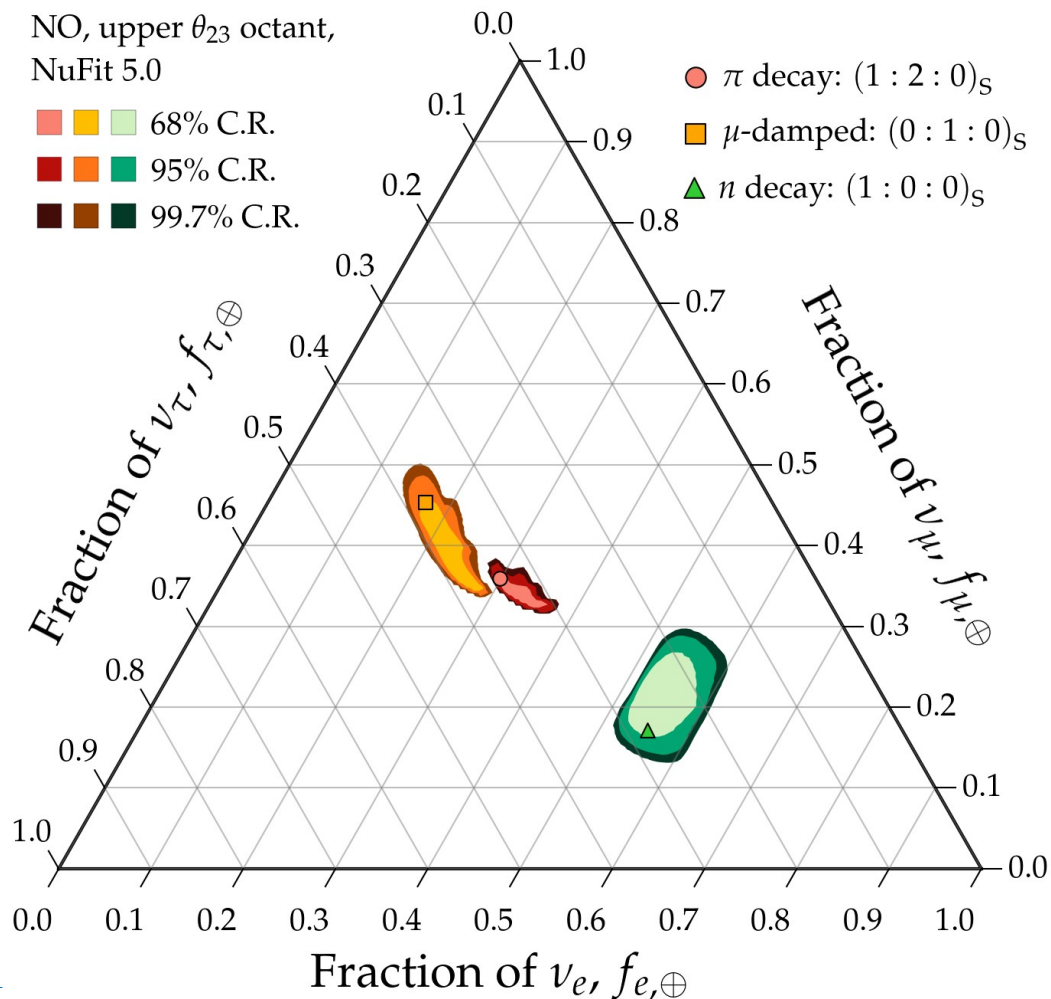
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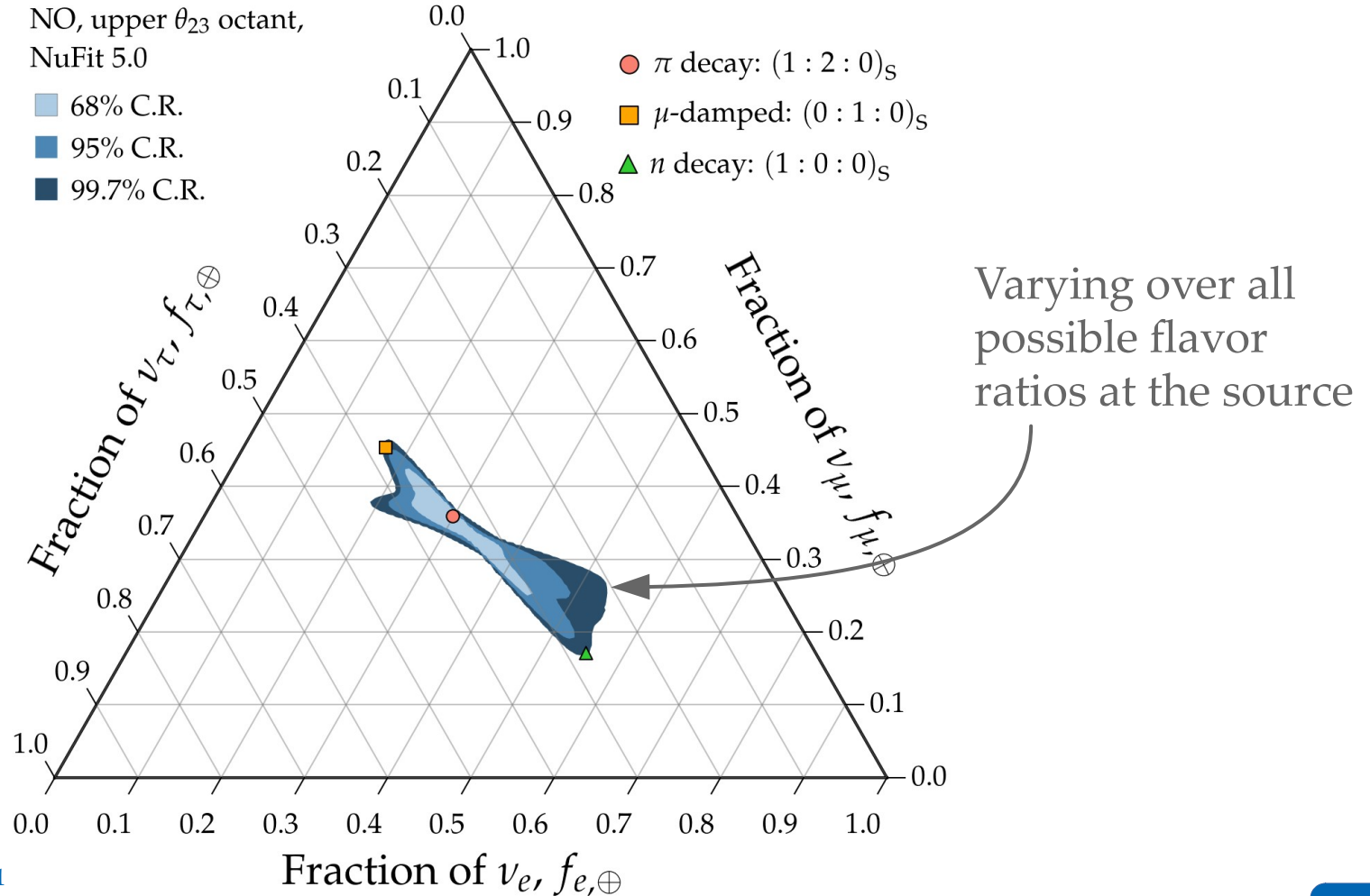
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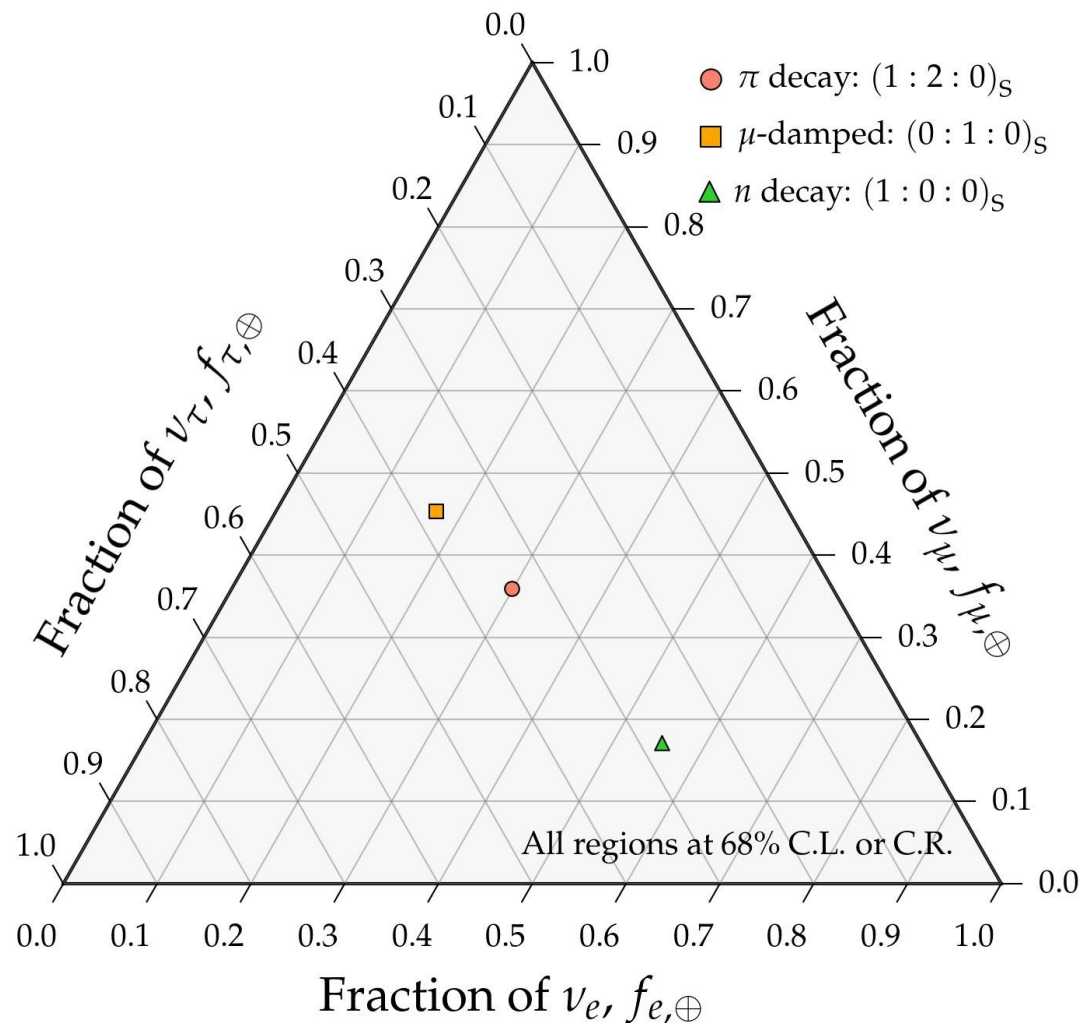
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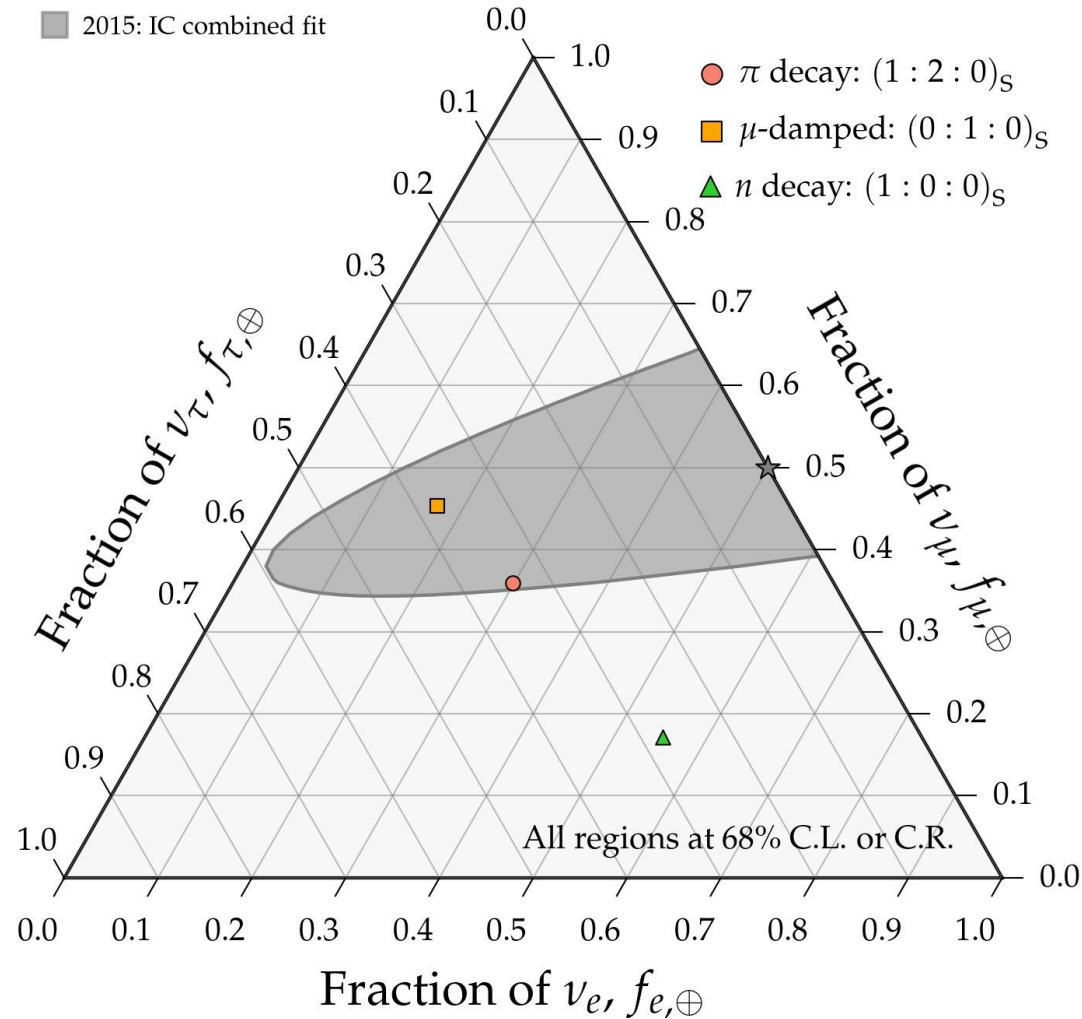
*Note:*  
All plots shown are for normal neutrino mass ordering (NO); inverted ordering looks similar

# Measuring the flavor composition

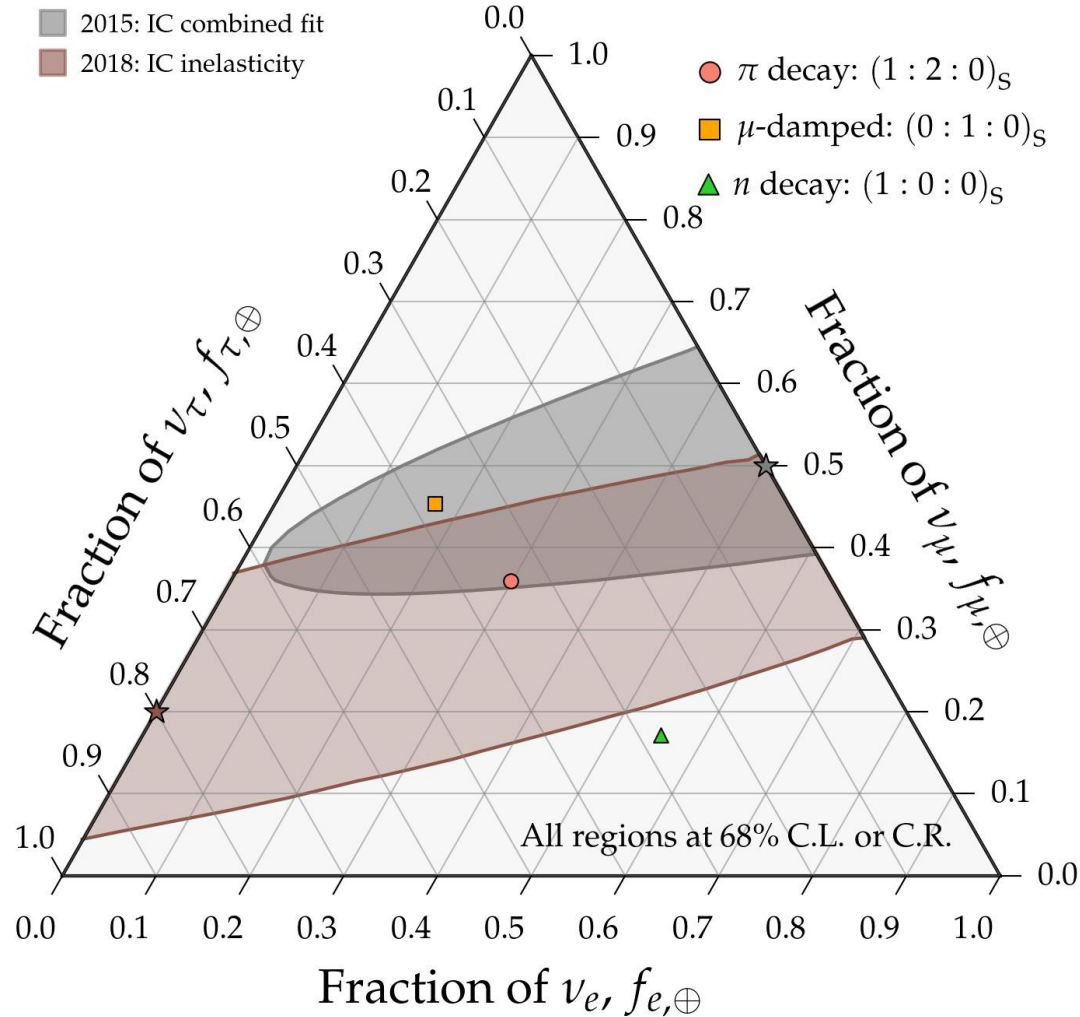
# Measuring flavor composition 2015–2025



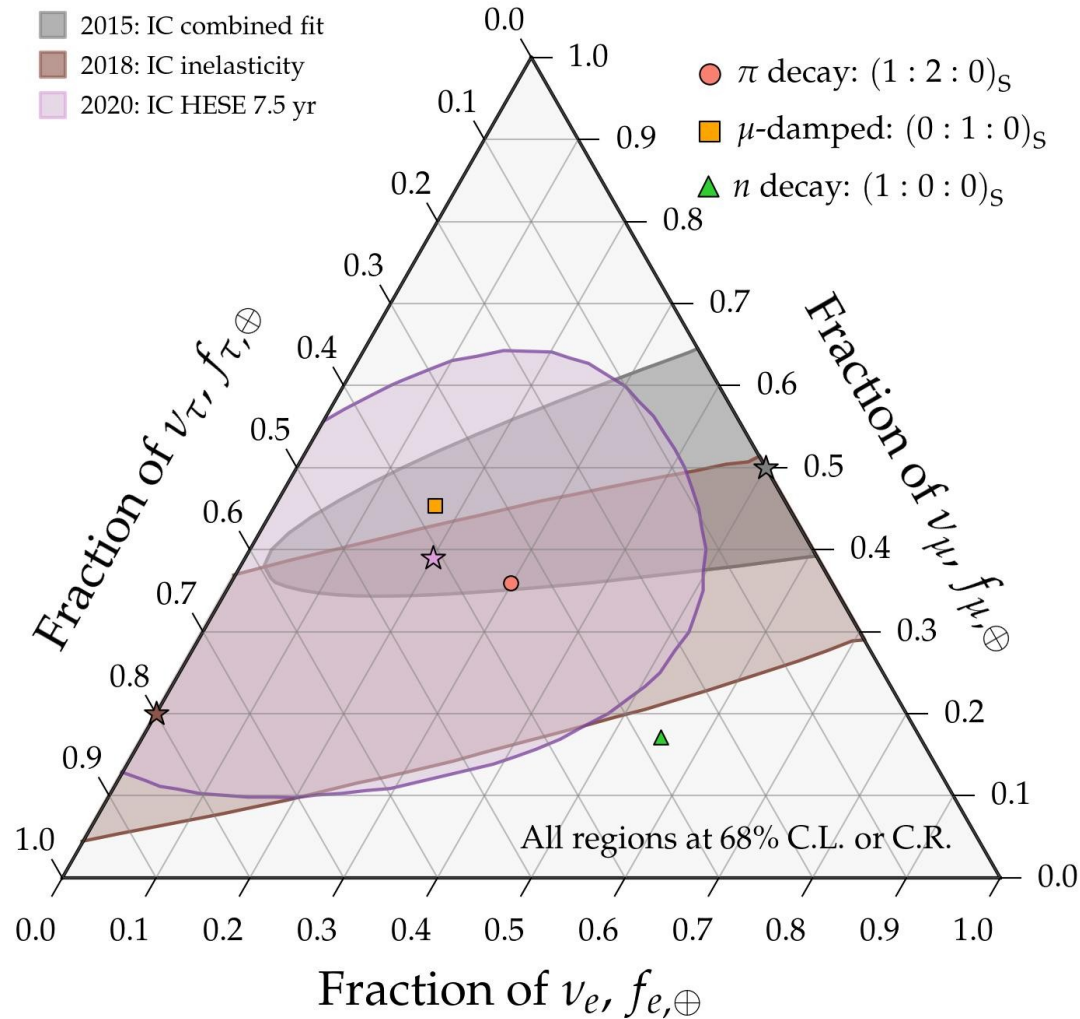
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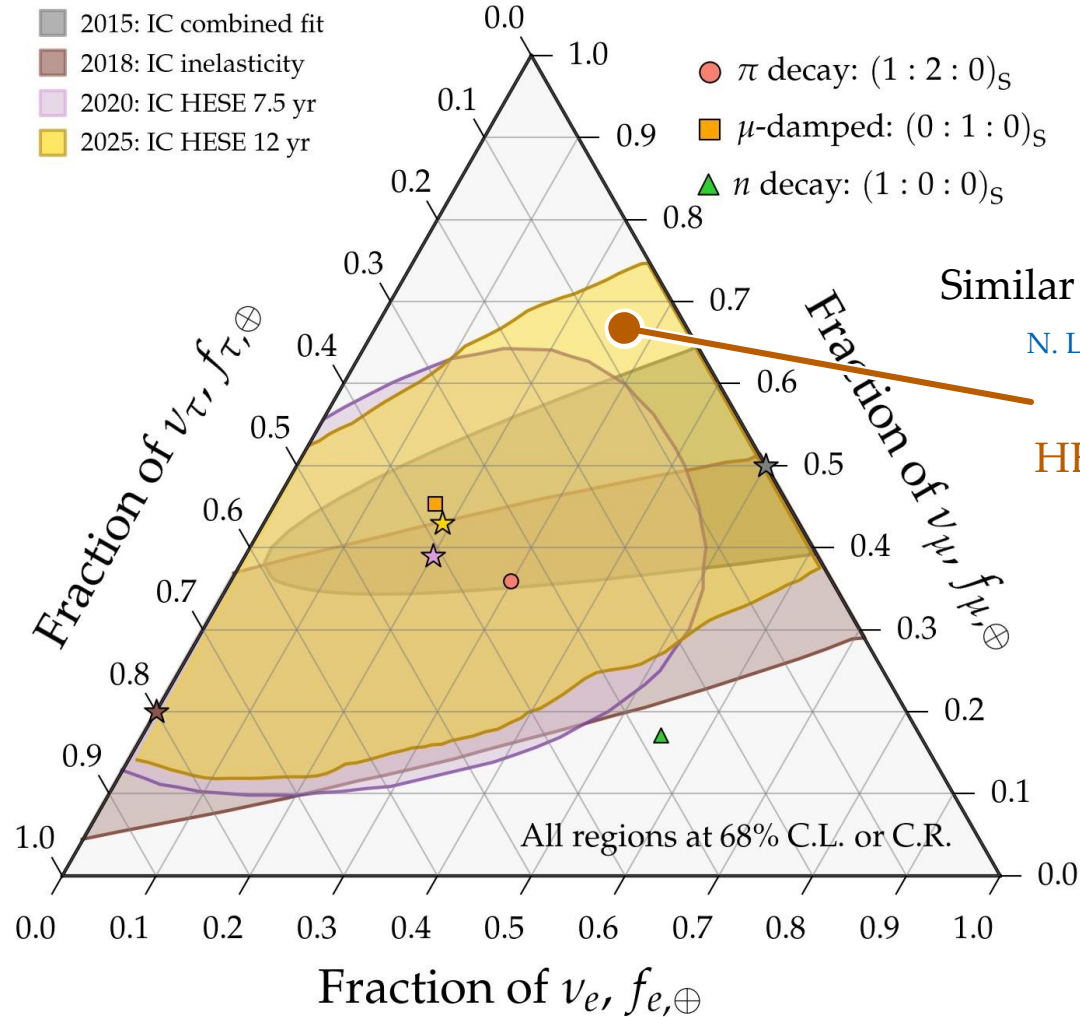
# Measuring flavor composition 2015–2025



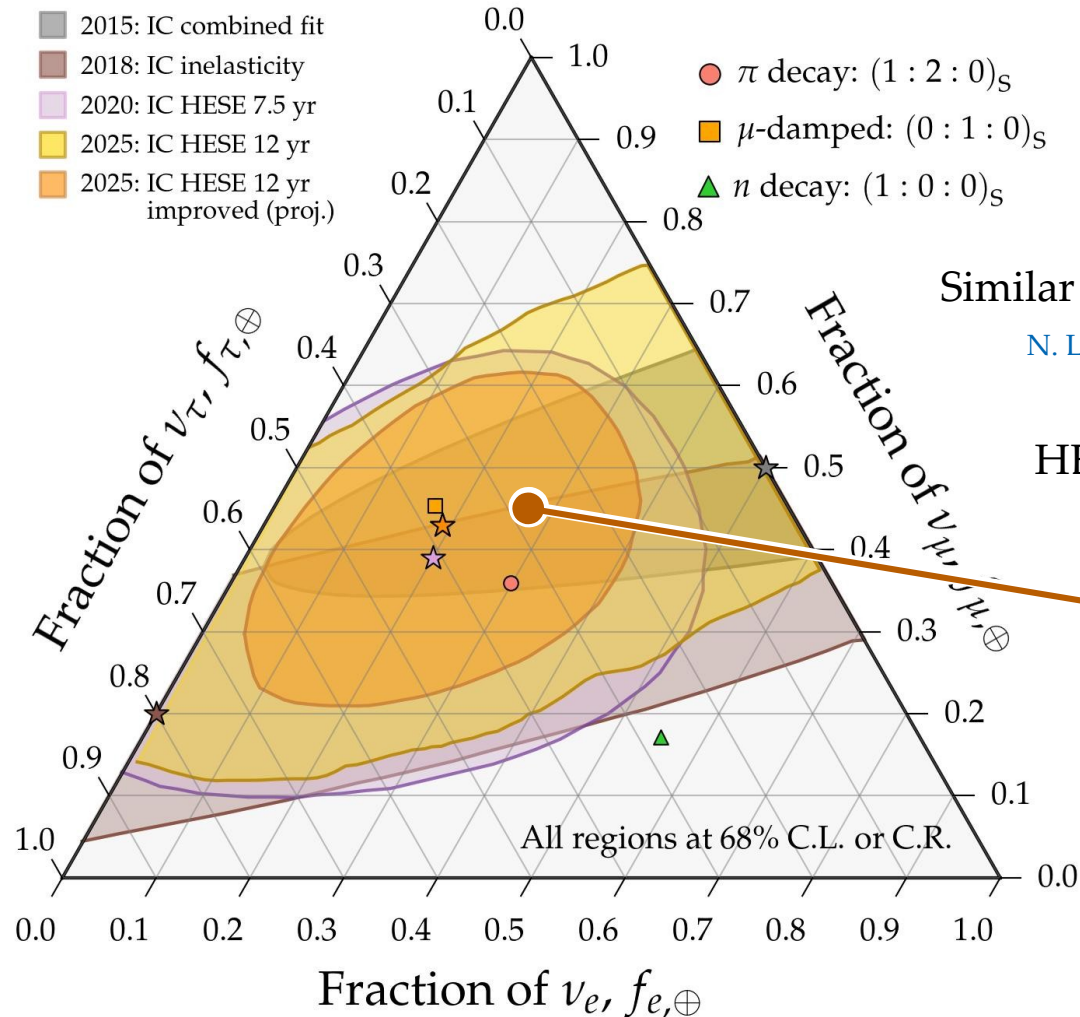
# Measuring flavor composition 2015–2025



# Measuring flavor composition 2015–2025



# Measuring flavor composition 2015–2025



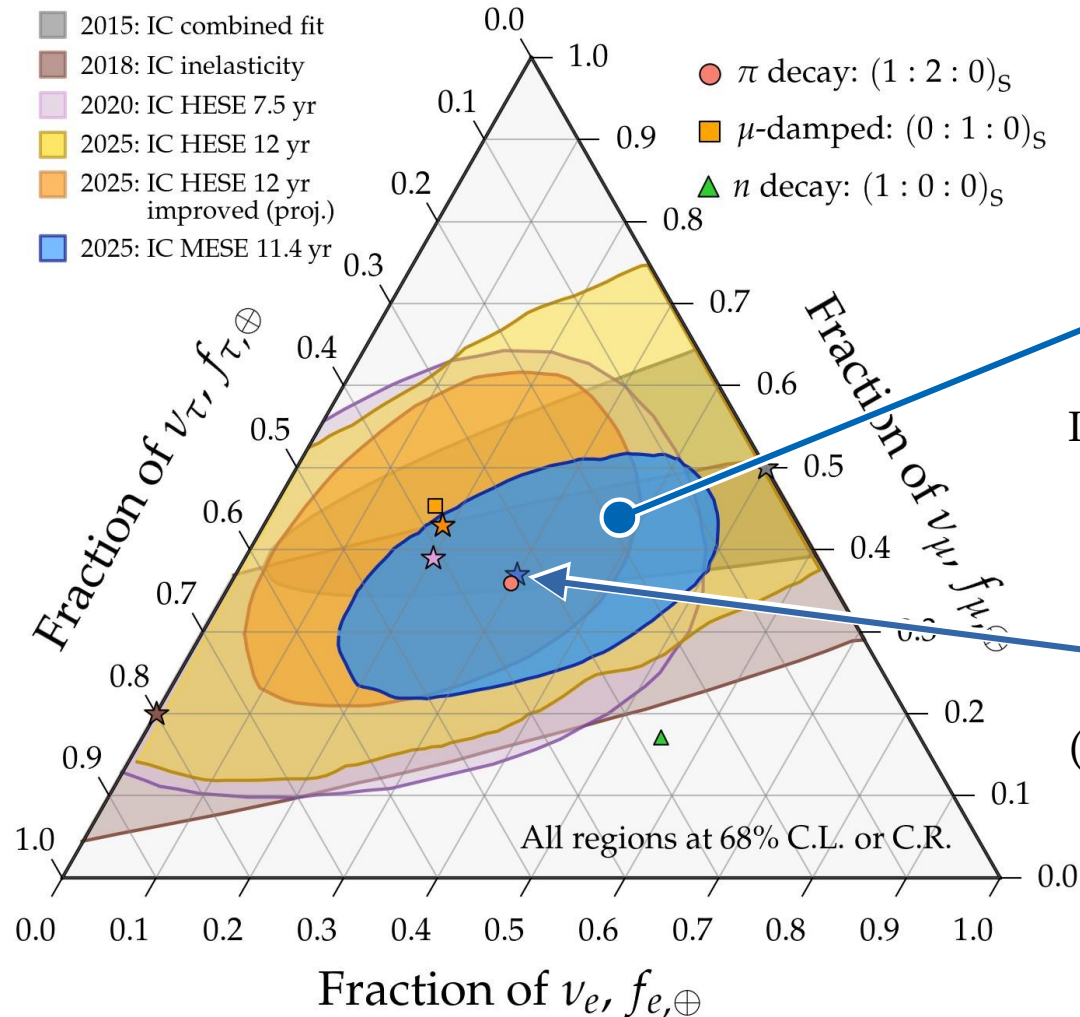
Similar likelihood as with 7.5 yr

N. Lad, T. J. van Eeden, M. Ackermann  
PoS(ICRC2025)1198

HESE ( $> 60$  TeV) are scarce  
( $\sim 100$  events in 12 yr)

Improve via a neural network that uses the energy asymmetry of the two bangs and the direction

# Measuring flavor composition 2015–2025



MESE events ( $> 1$  TeV) are more abundant

Includes classification of  $\nu_\tau$

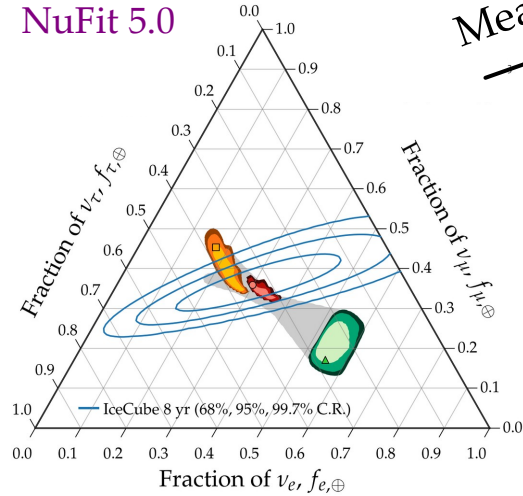
First time all flavors are nonzero at 68% C.L.

Best fit very close to nominal expectation of (1:1:1) from production via pion decay

# How knowing the mixing parameters better helps

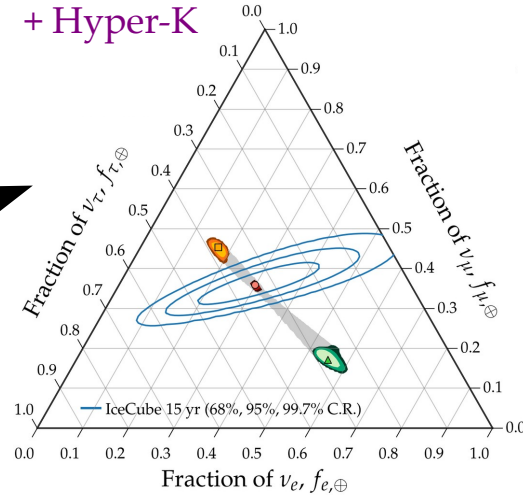
2020

NuFit 5.0

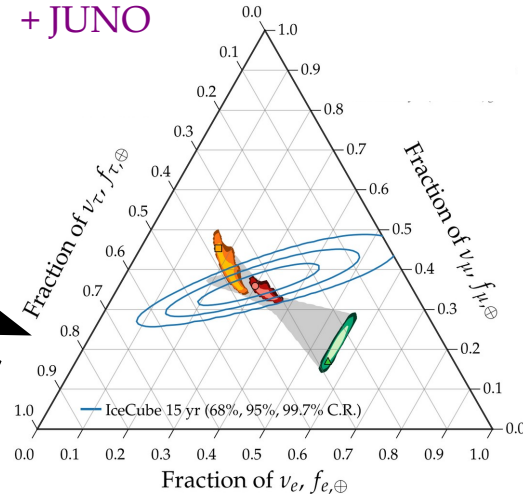


Measure  $\theta_{23}$  better

+ Hyper-K



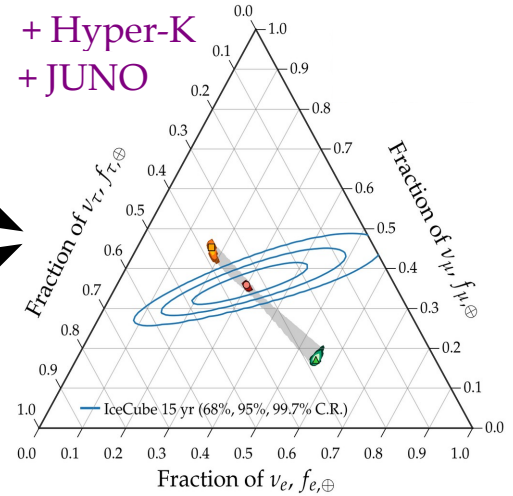
+ JUNO



Measure  $\theta_{12}$  better

~2030

+ Hyper-K  
+ JUNO

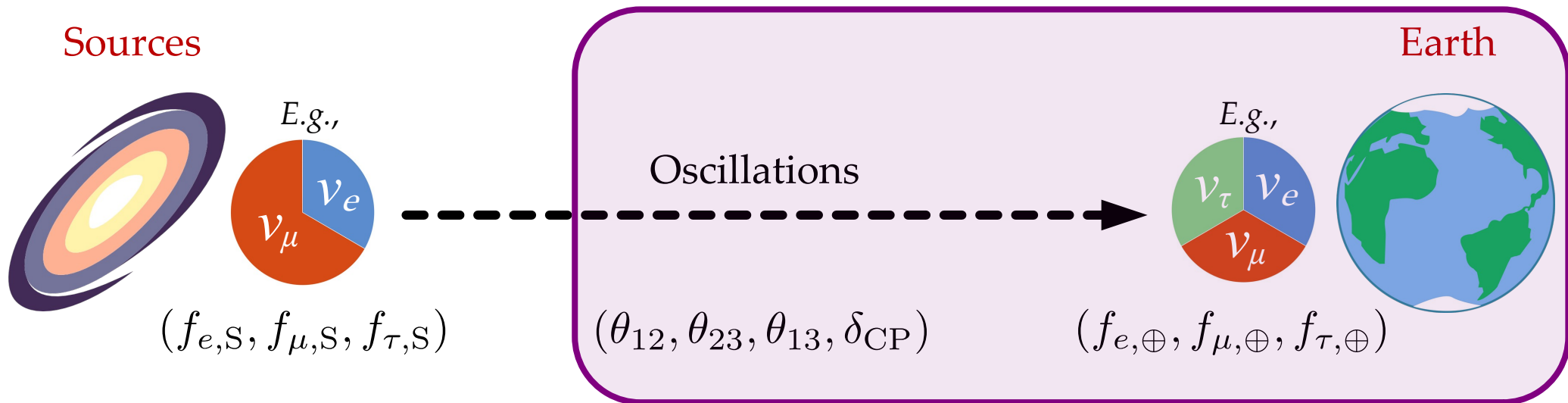


In our results:  
JUNO + Hyper-K + DUNE

Marginal improvement til 2040

Back to the sources

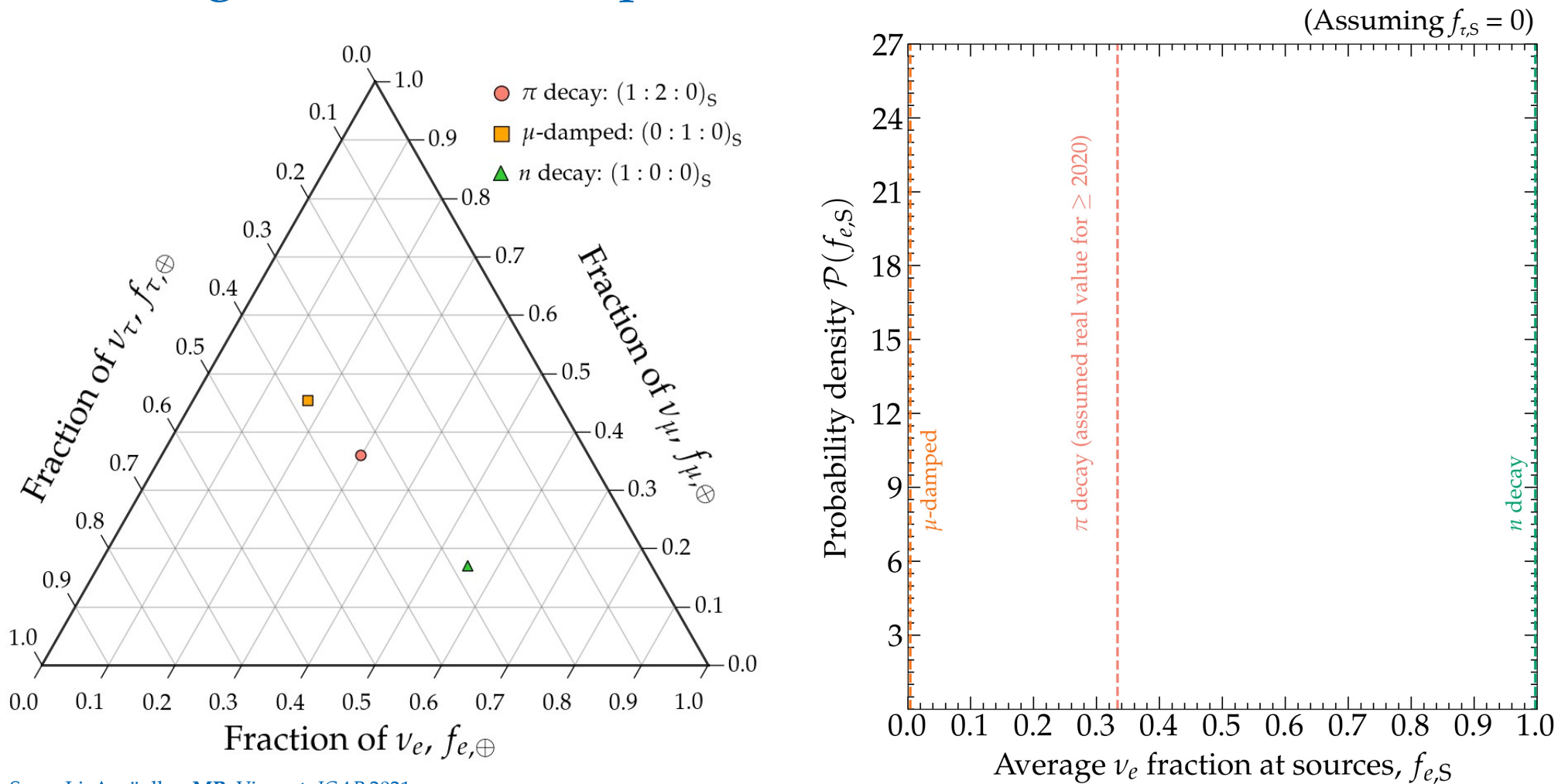
*From sources to Earth:* we learn what to expect when measuring  $f_{\alpha,\oplus}$



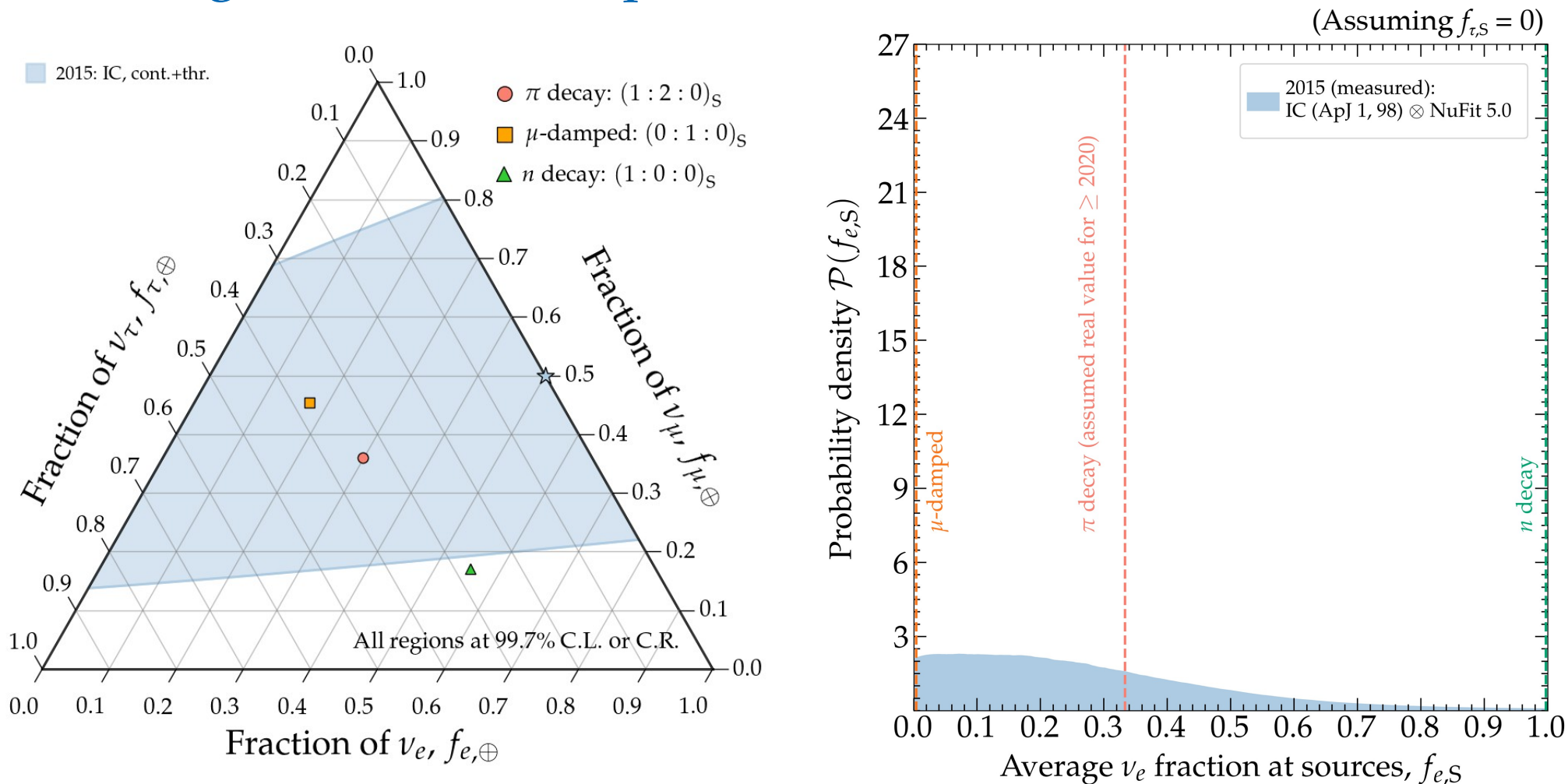
*From Earth to sources:* we let the data teach us about  $f_{\alpha,S}$

# Inferring the flavor composition at the sources

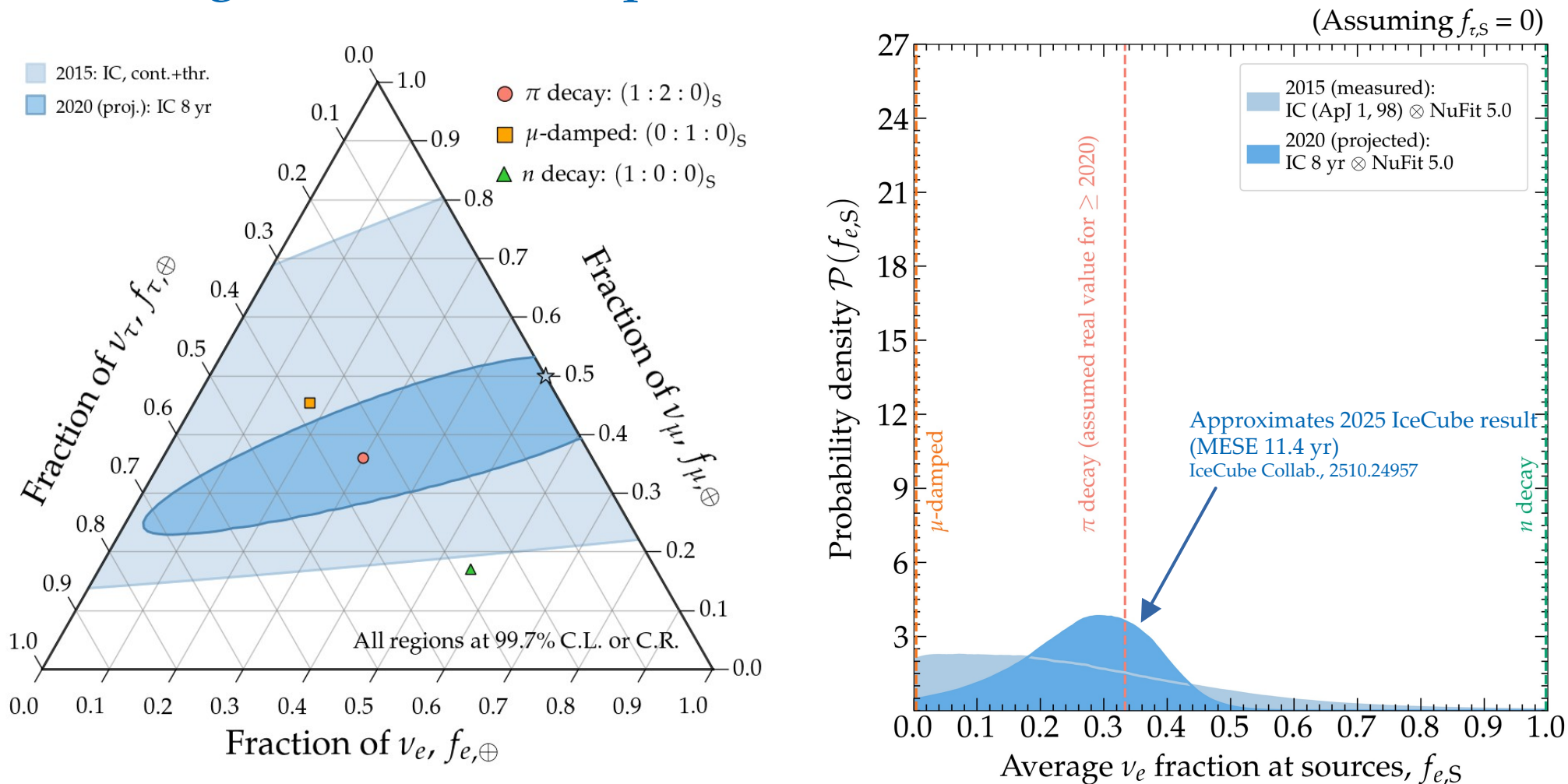
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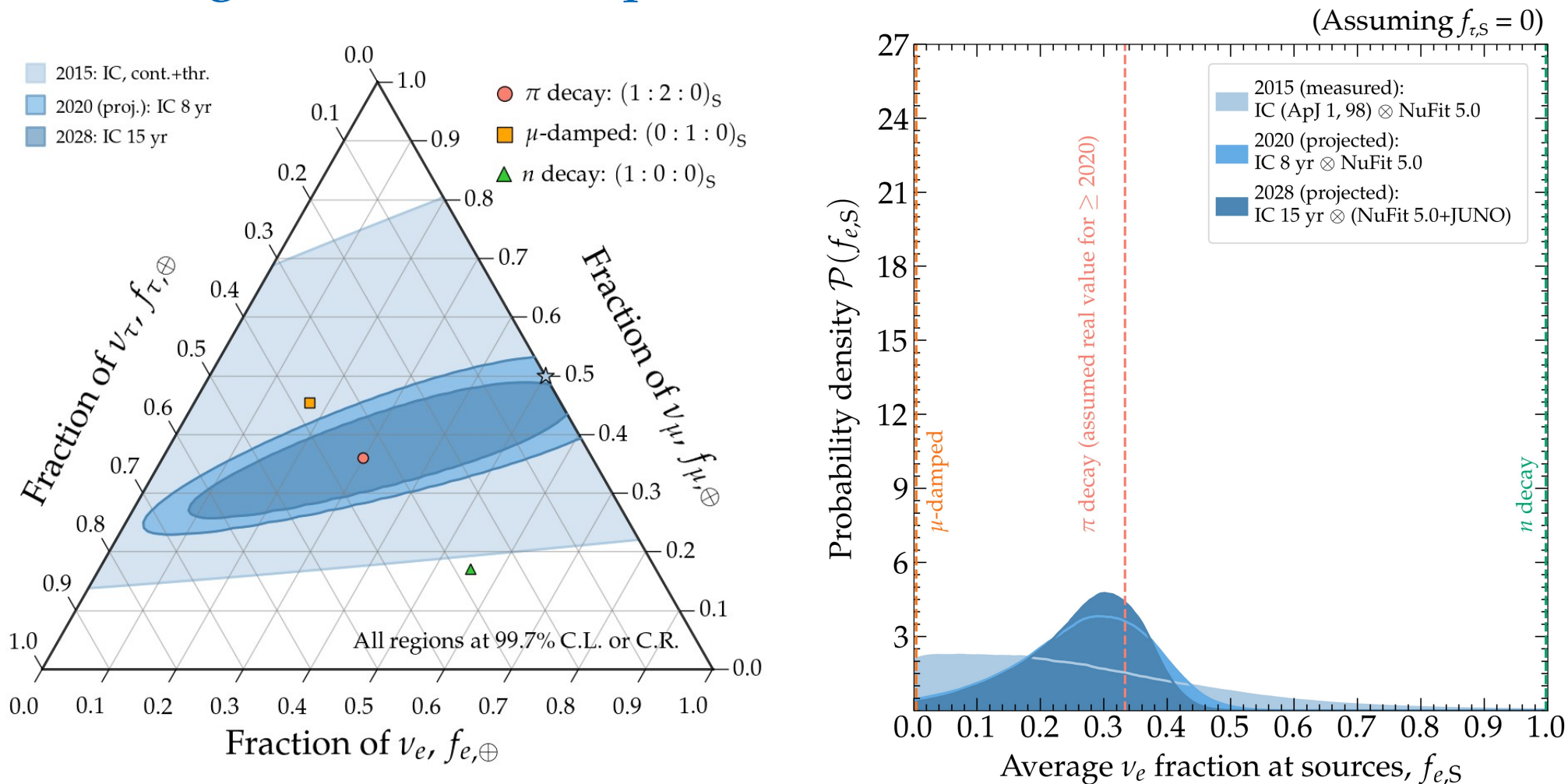
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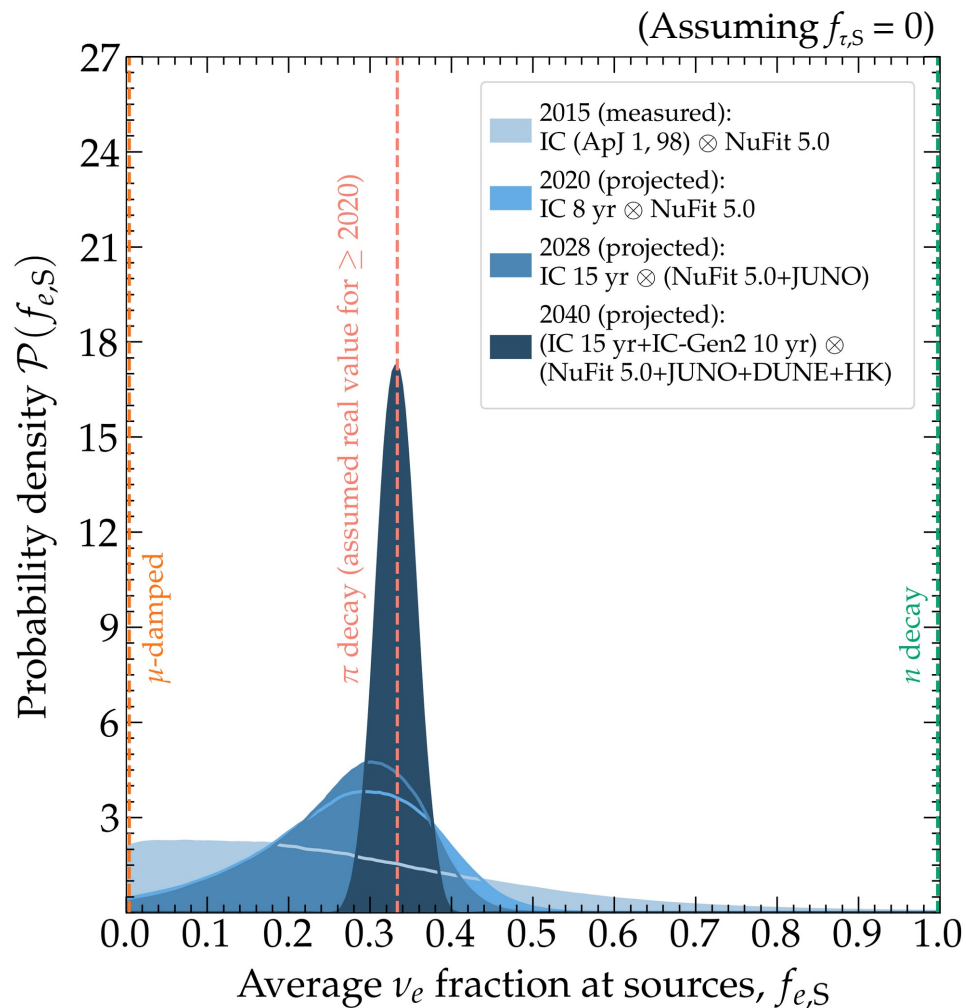
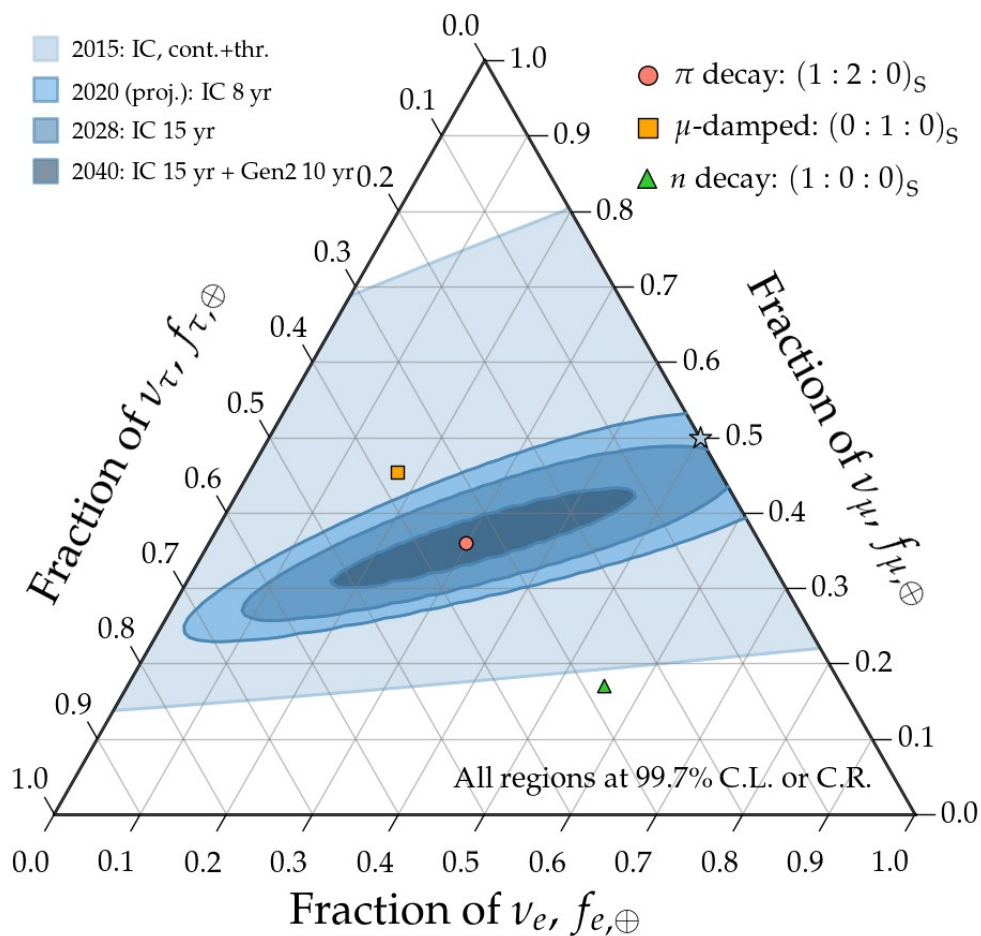
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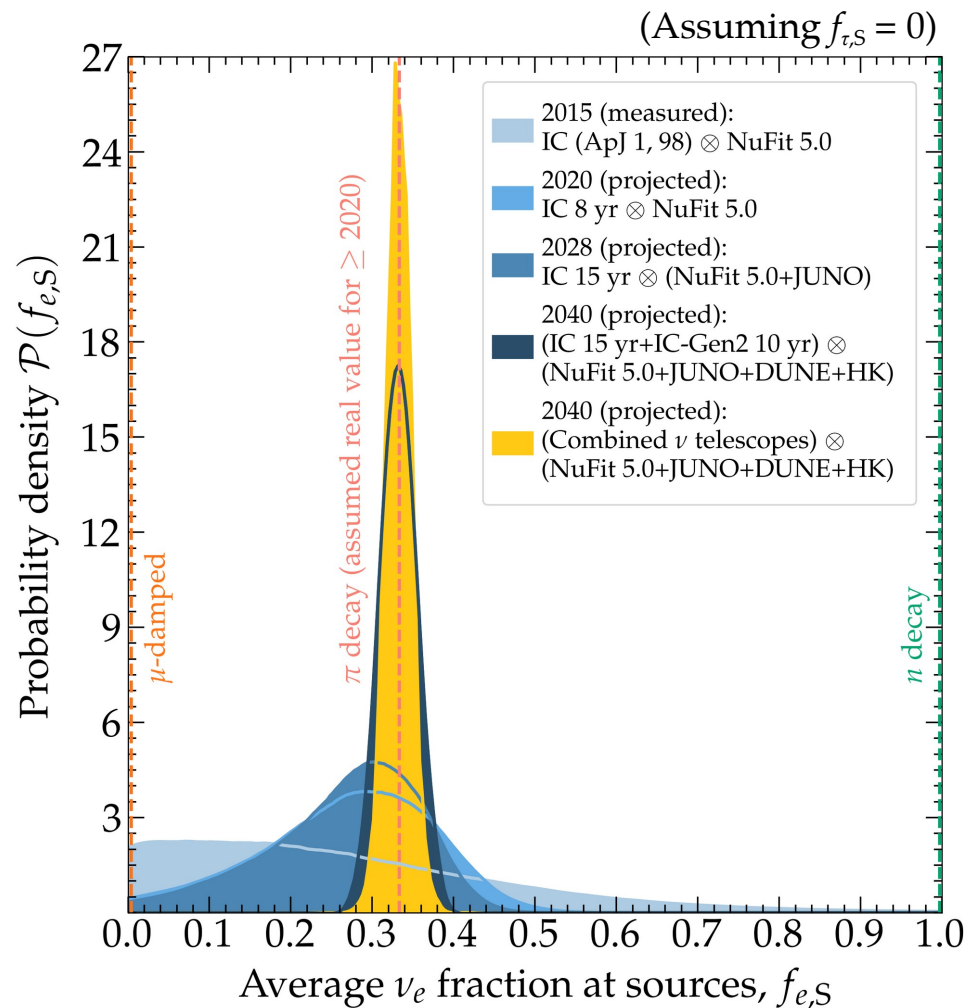
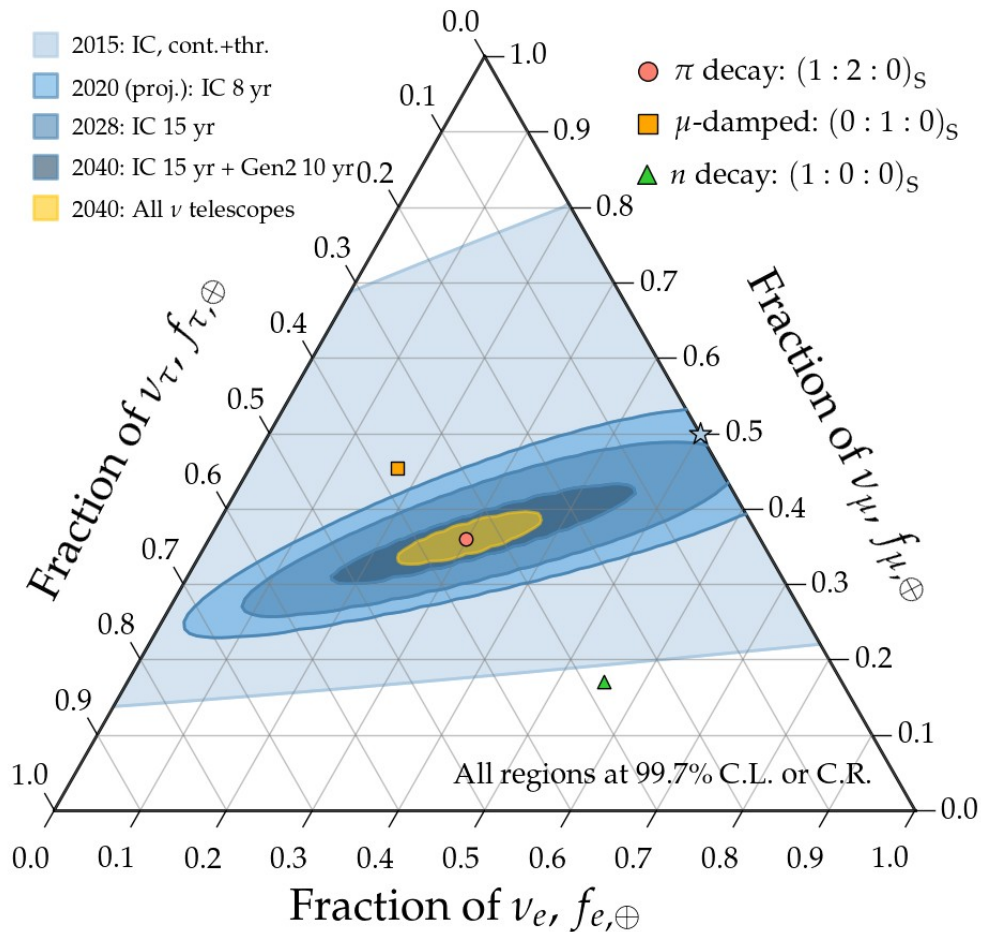
# Inferring the flavor composition at the sources



# Inferring the flavor composition at the sources

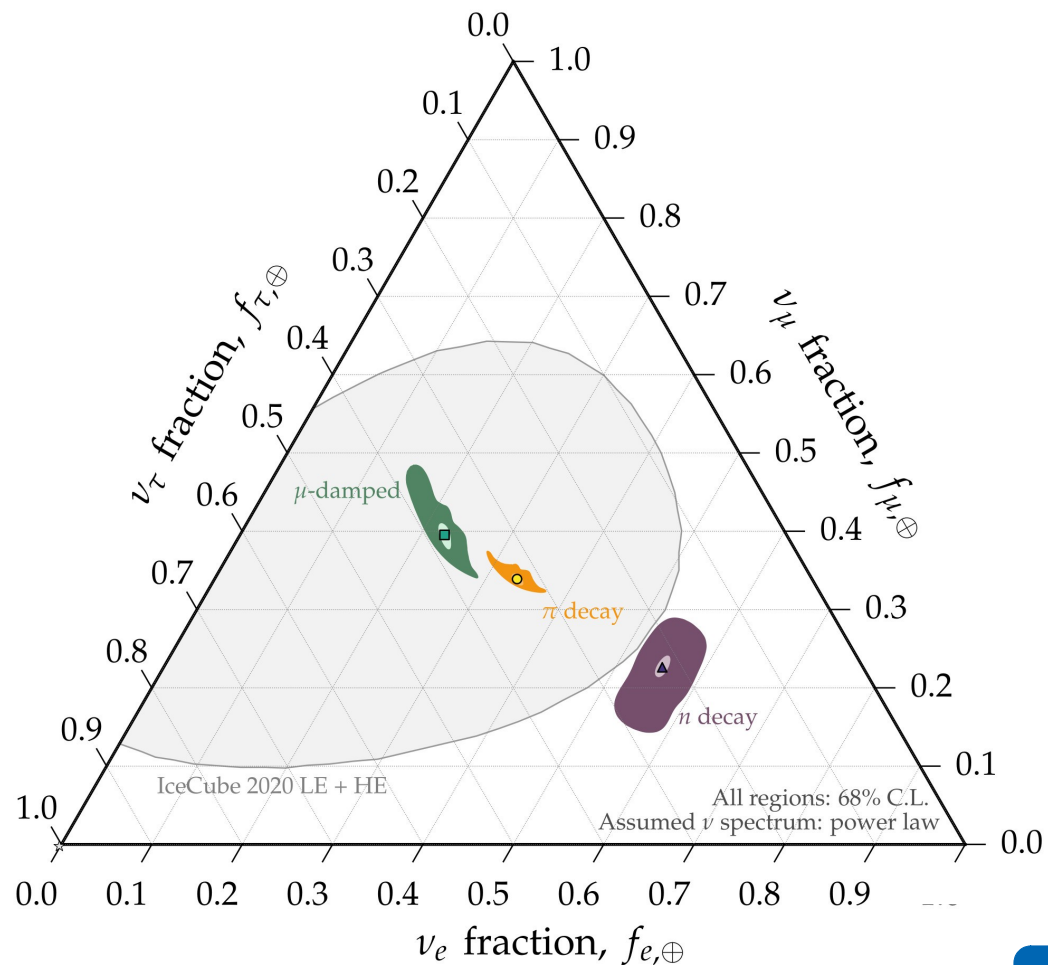


# Inferring the flavor composition at the sources



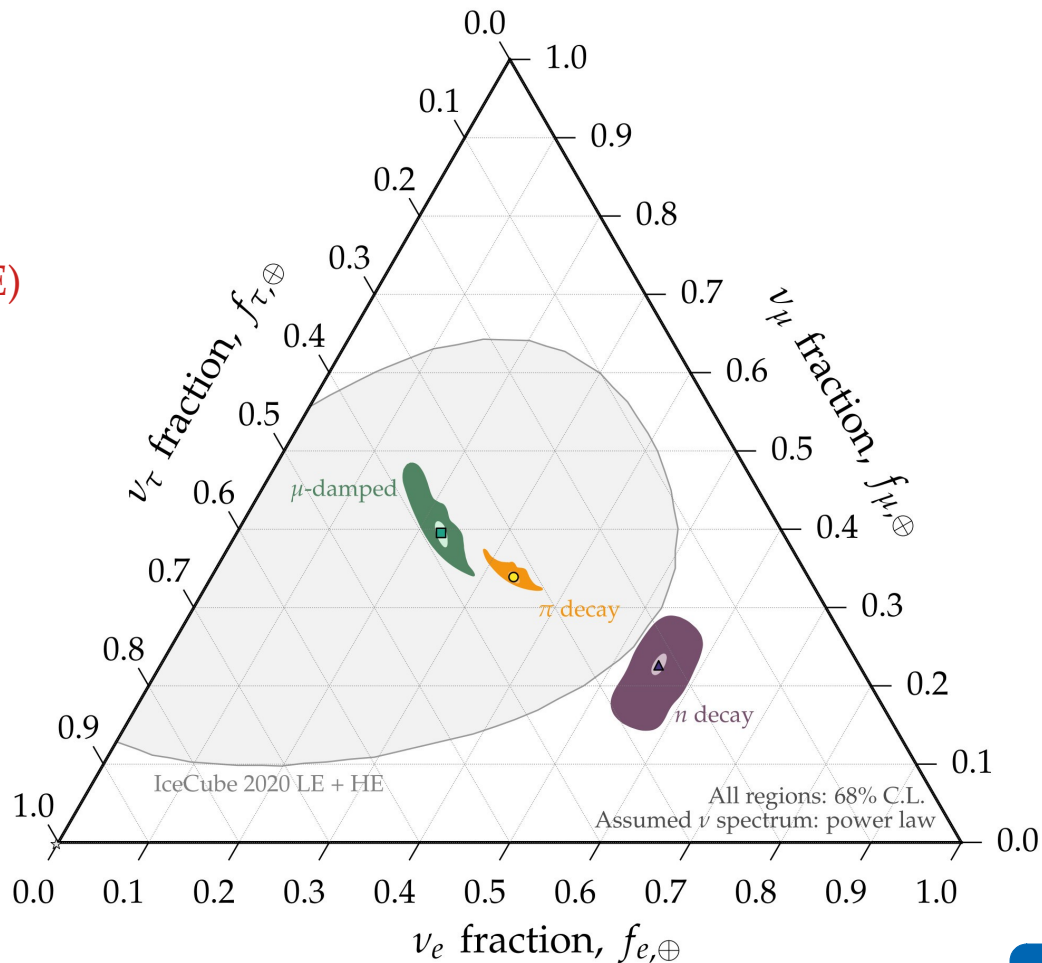
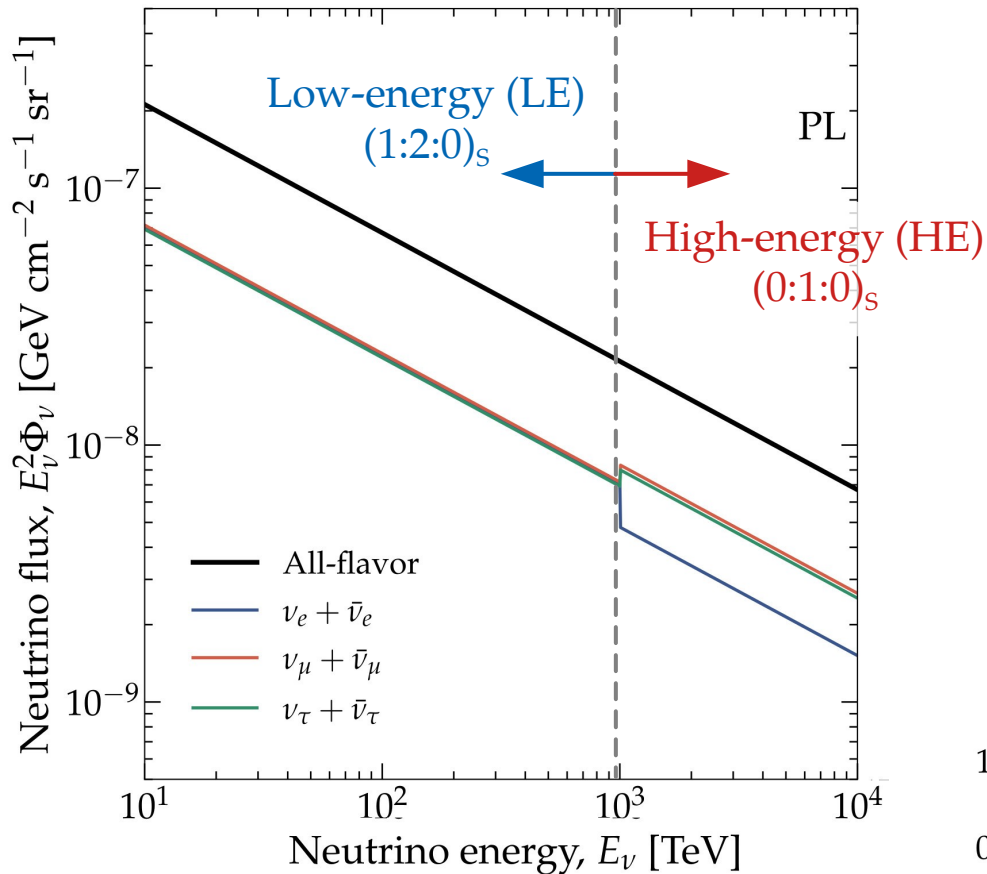
# Energy-dependent flavor composition

# Flavor composition: measuring the energy dependence



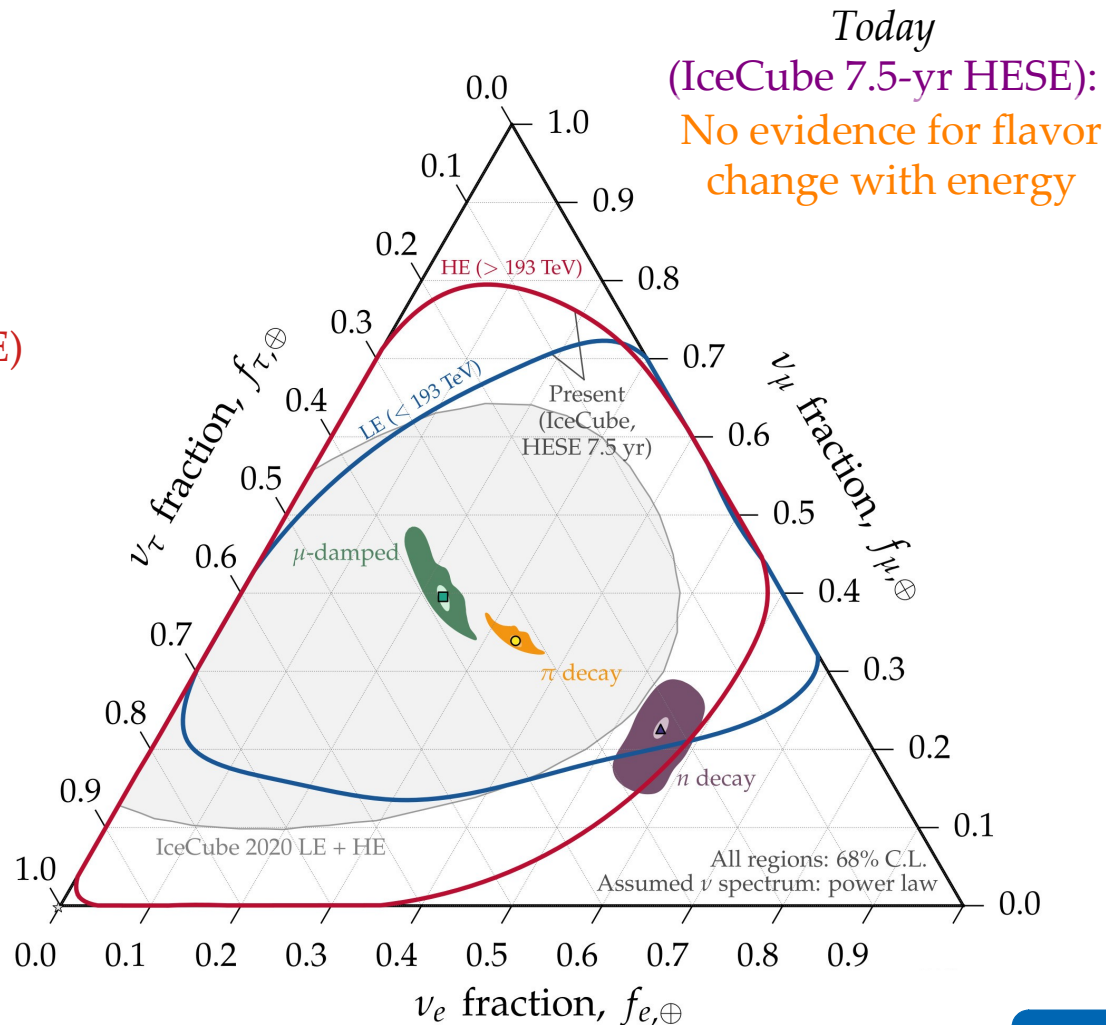
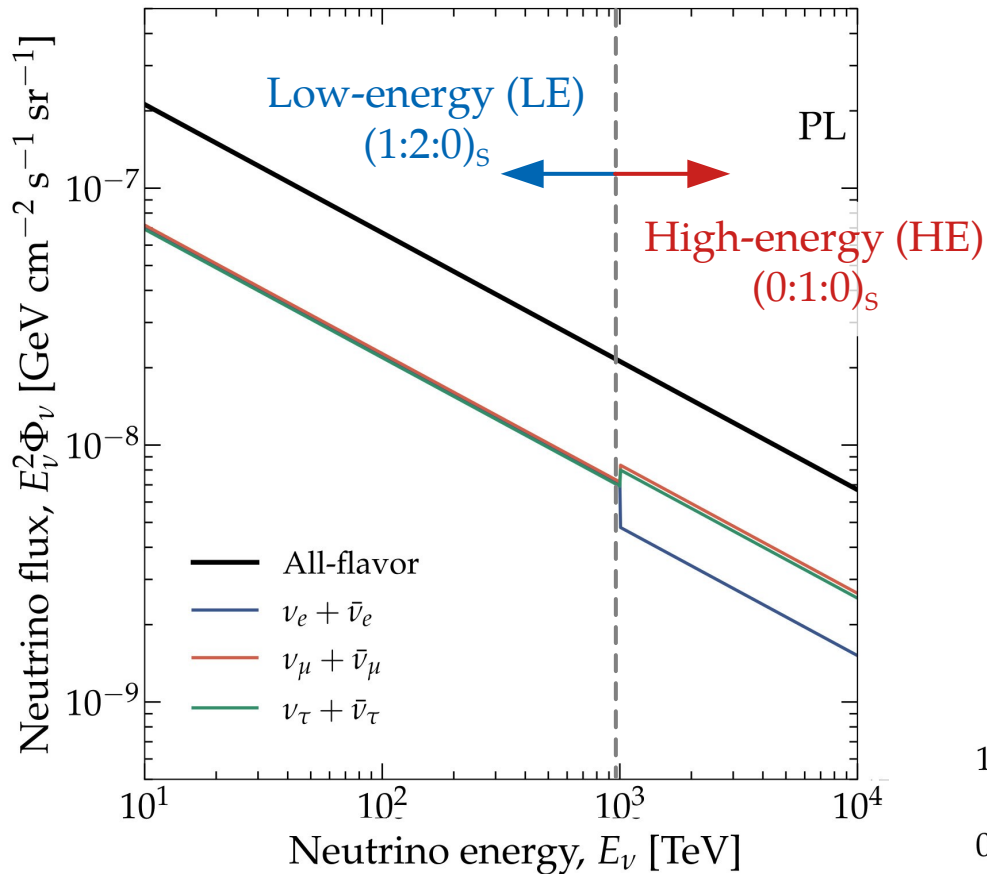
# Flavor composition: measuring the energy dependence

## Power-law (PL) diffuse $\nu$ flux



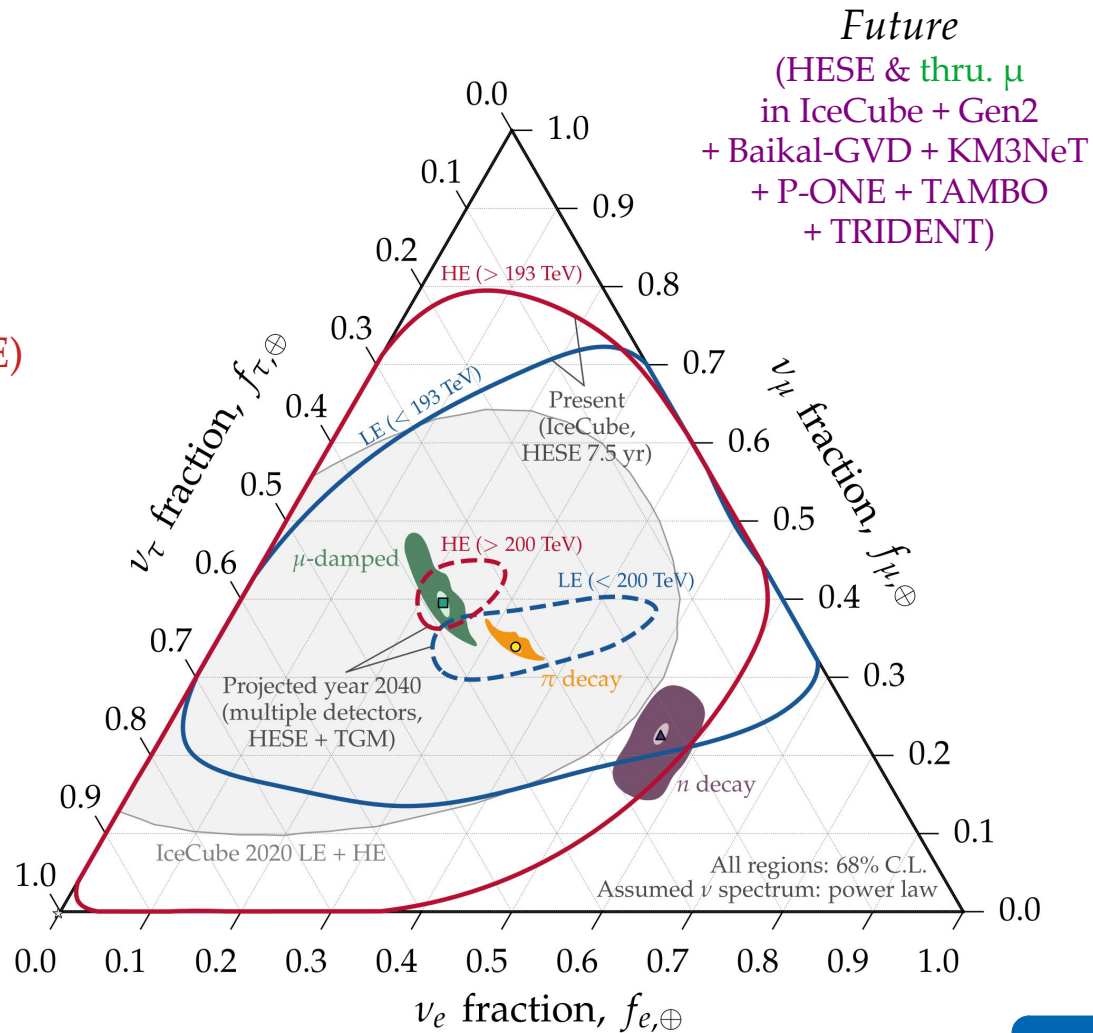
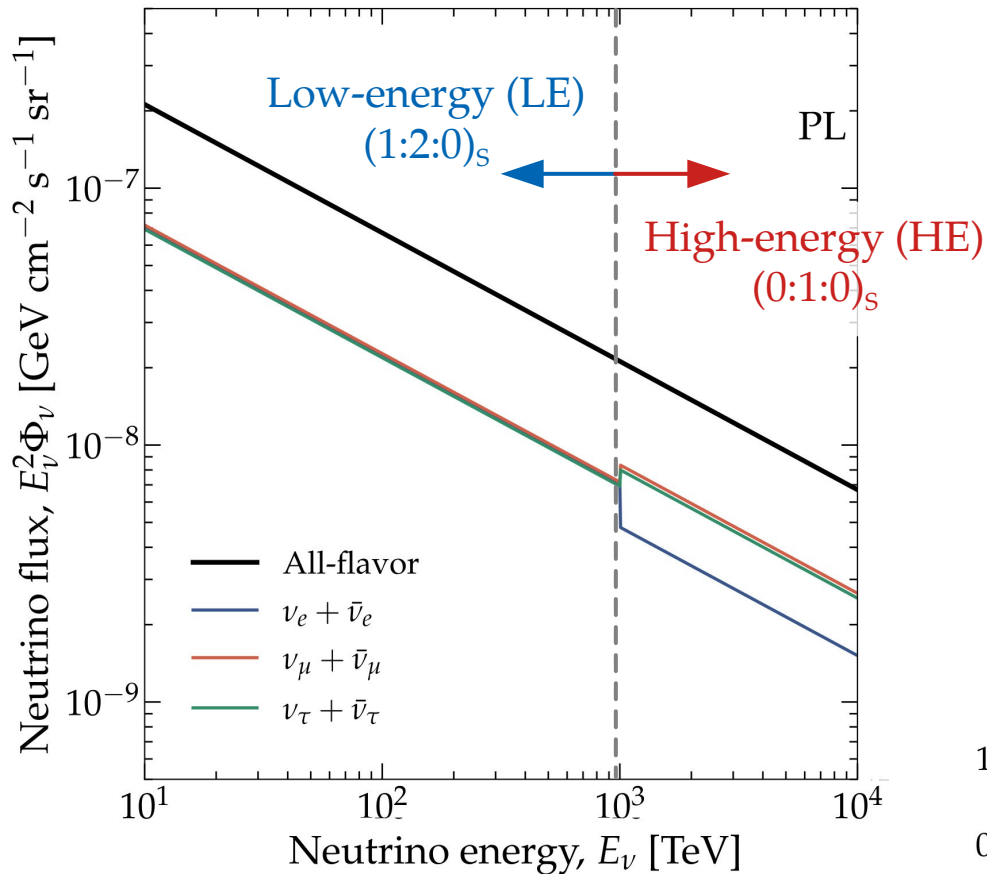
# Flavor composition: measuring the energy dependence

Power-law (PL) diffuse  $\nu$  flux



# Flavor composition: measuring the energy dependence

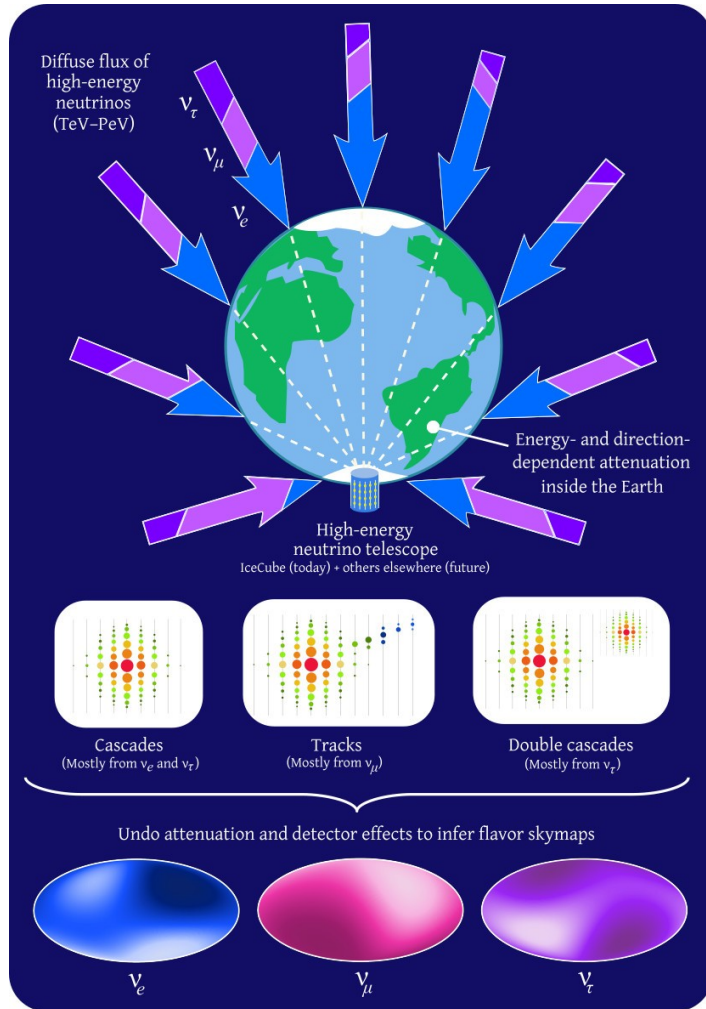
Power-law (PL) diffuse  $\nu$  flux



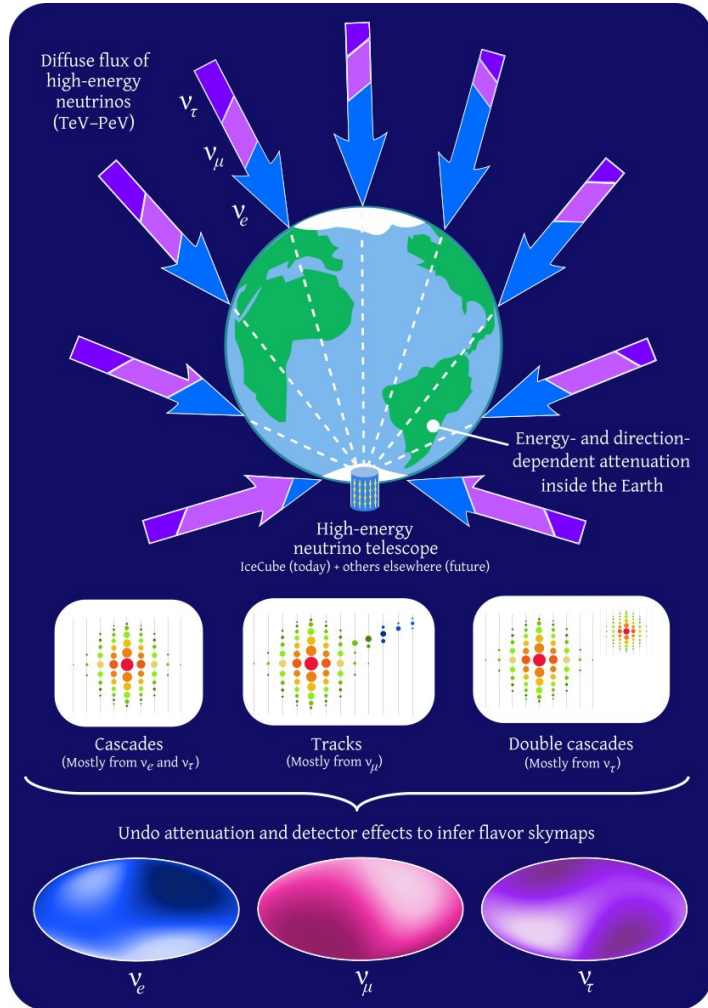
# Direction-dependent flavor composition

# Flavor anisotropy in the high-energy neutrino sky

*Does the high-energy sky shine equally brightly  
In neutrinos of all flavors?*

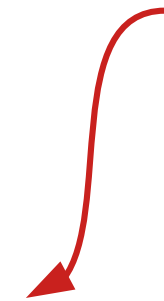


# Flavor anisotropy in the high-energy neutrino sky

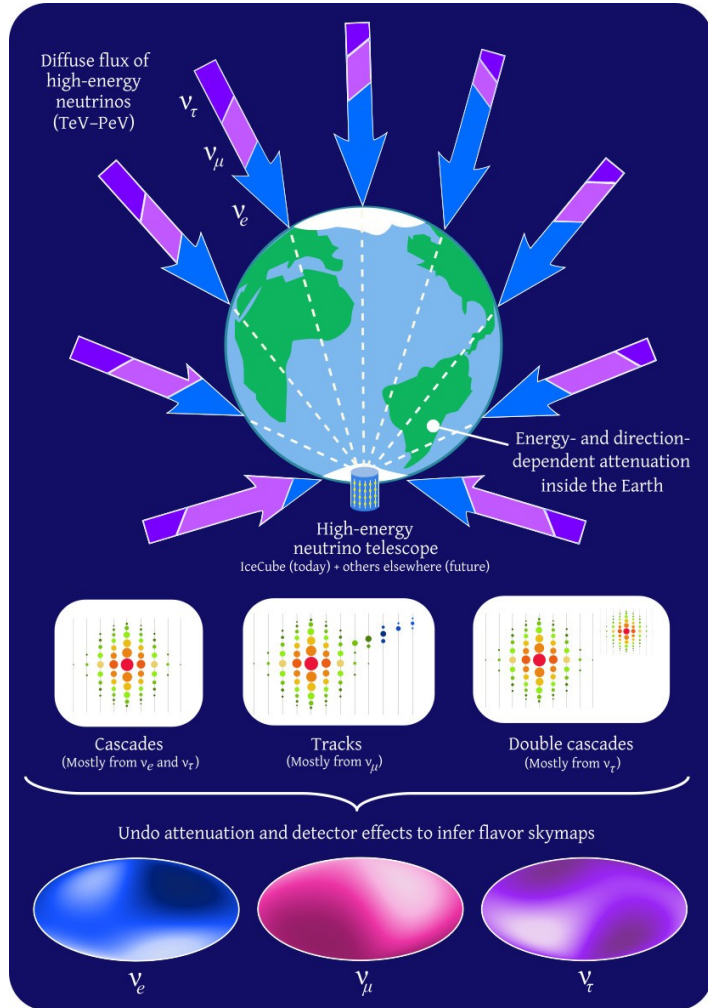


*Does the high-energy sky shine equally brightly  
In neutrinos of all flavors?*

From the angular distribution of detected events in neutrino telescopes (HESE cascades, tracks, double cascades) ...



# Flavor anisotropy in the high-energy neutrino sky

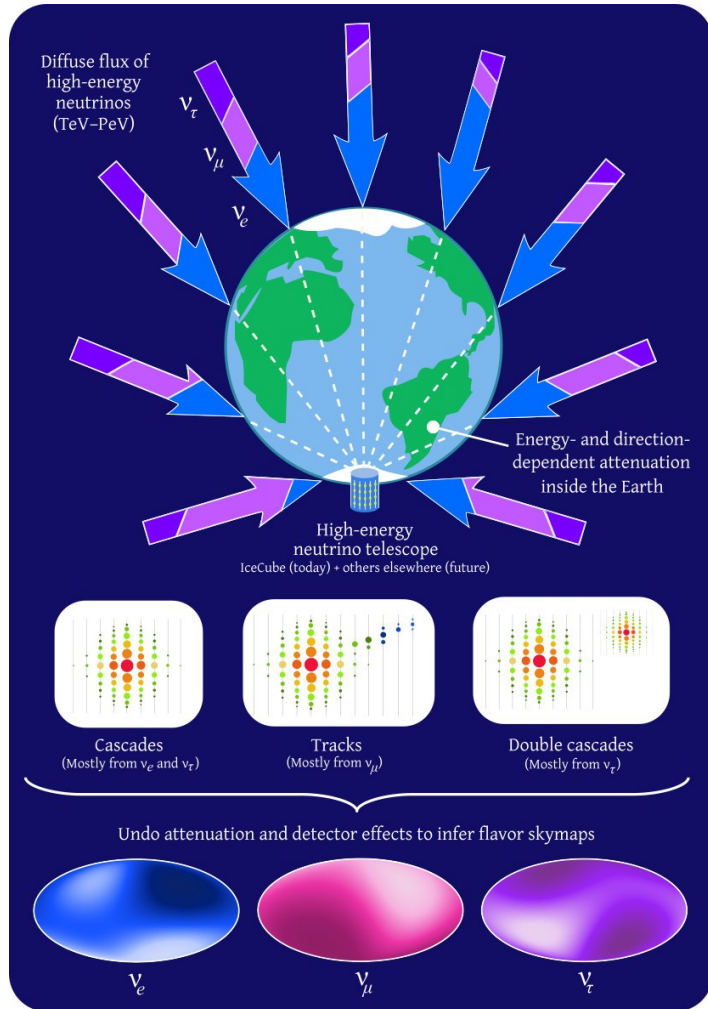


*Does the high-energy sky shine equally brightly  
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From the angular distribution of detected events in neutrino telescopes (HESE cascades, tracks, double cascades) ...

... we infer the directional dependence of the diffuse fluxes of  $\nu_e$ ,  $\nu_\mu$ ,  $\nu_\tau$

# Flavor anisotropy in the high-energy neutrino sky



*Does the high-energy sky shine equally brightly  
In neutrinos of all flavors?*

*From the angular distribution of detected  
events in neutrino telescopes  
(HESE cascades, tracks, double cascades) ...*

*How? Undo detection effects  
(use public IceCube  
HESE Monte Carlo)*

*... we infer the directional dependence of  
the diffuse fluxes of  $\nu_e$ ,  $\nu_\mu$ ,  $\nu_\tau$*

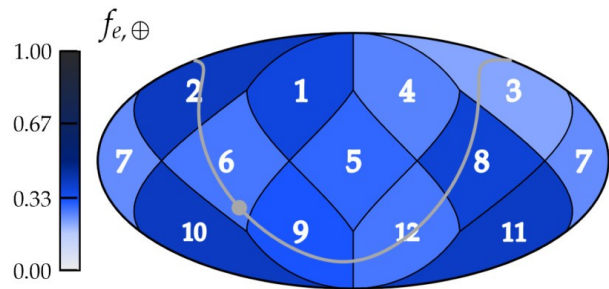
Directional high-energy astrophysical neutrino flavor composition: IceCube HESE (7.5 yr)

Real, public data

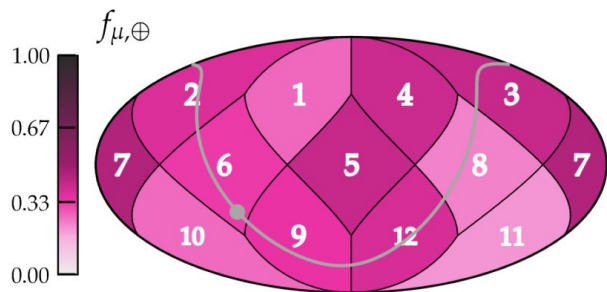
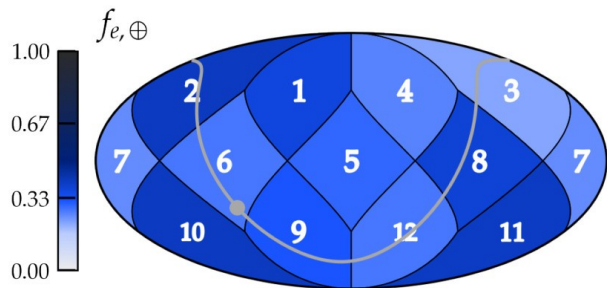


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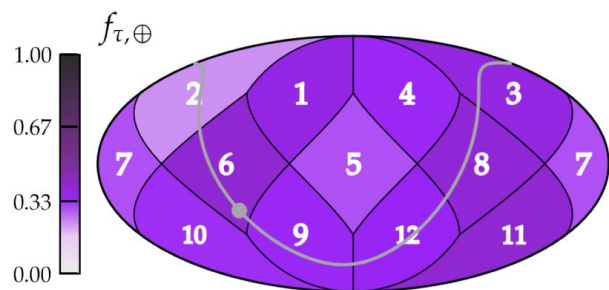
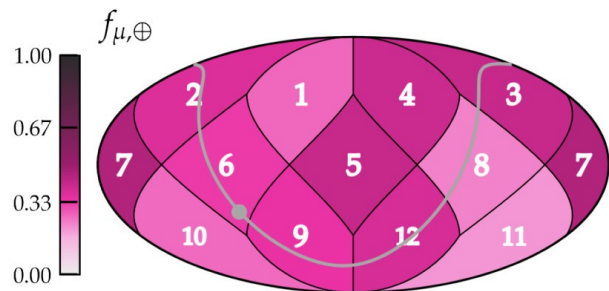
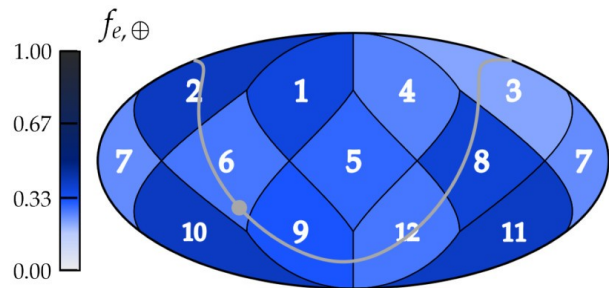
# Directional high-energy astrophysical neutrino flavor composition: IceCube HESE (7.5 yr)



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Equatorial

Telalovic, MB, JCAP 2025

# Directional high-energy astrophysical neutrino flavor composition: IceCube HESE (7.5 yr)

This work:

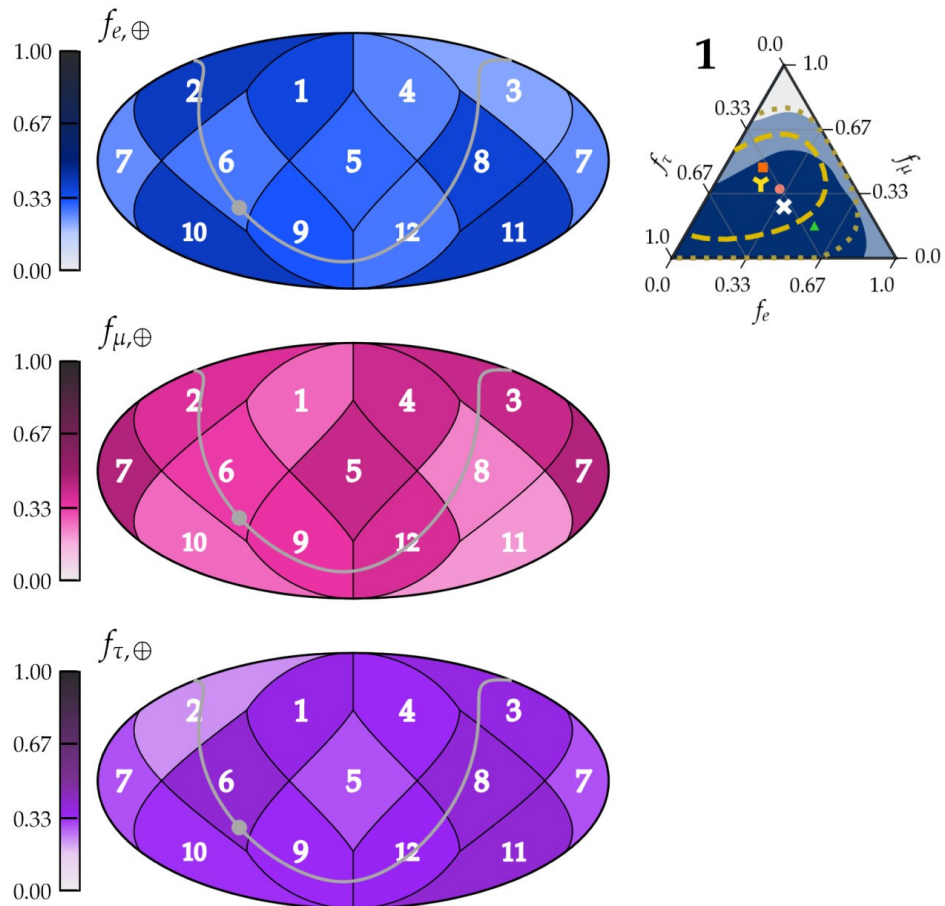
⊗ Best fit ■ 1σ ■ 2σ □ 3σ

IceCube 2020 all-sky:

⊕ Best fit - - 1σ ··· 2σ

Benchmarks:

●  $\pi^\pm$  decay: (1:2:0)<sub>S</sub> ■  $\mu$ -damped: (0:1:0)<sub>S</sub> ▲  $n$  decay: (1:0:0)<sub>S</sub>



Equatorial

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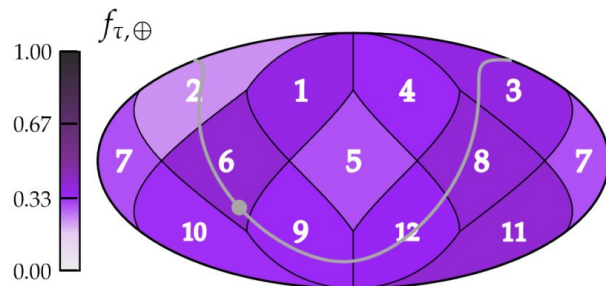
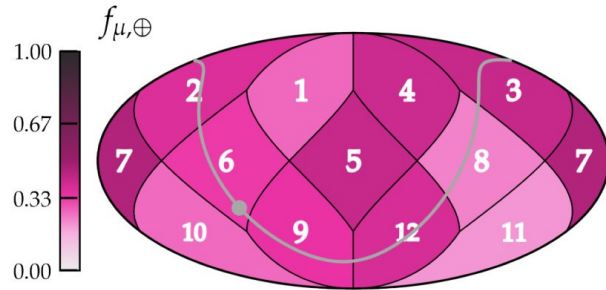
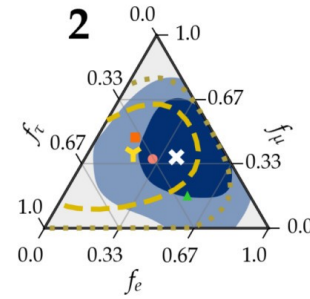
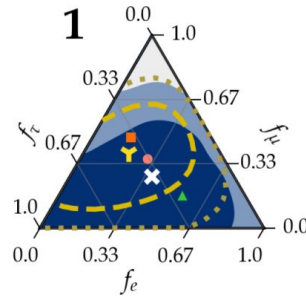
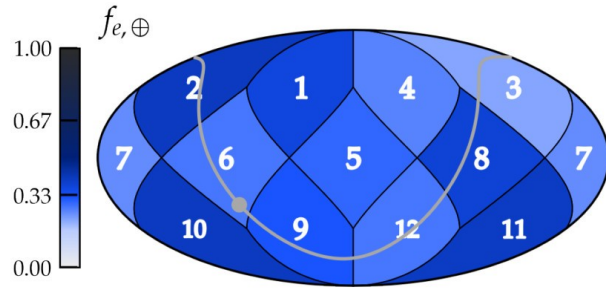
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Benchmarks:

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Equatorial

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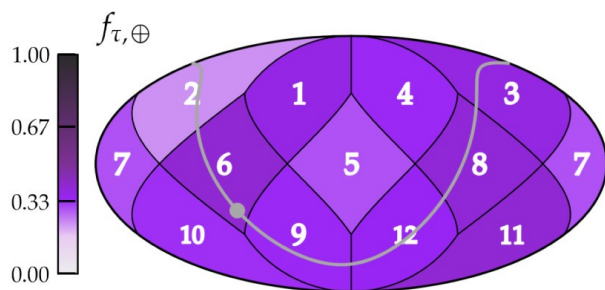
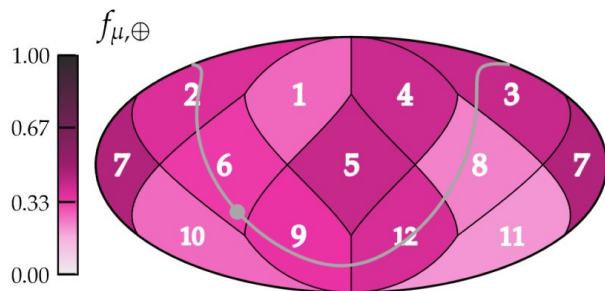
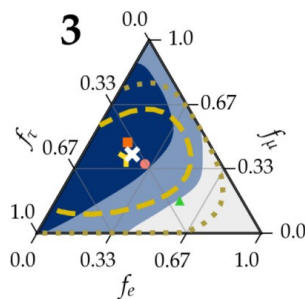
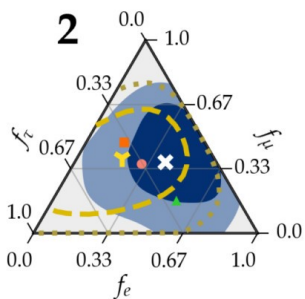
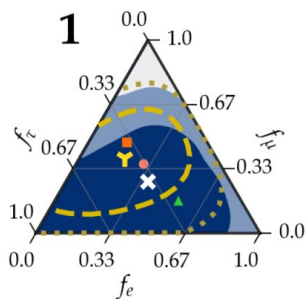
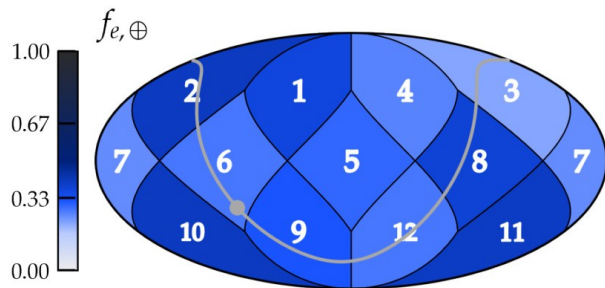
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IceCube 2020 all-sky:

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Benchmarks:

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Equatorial

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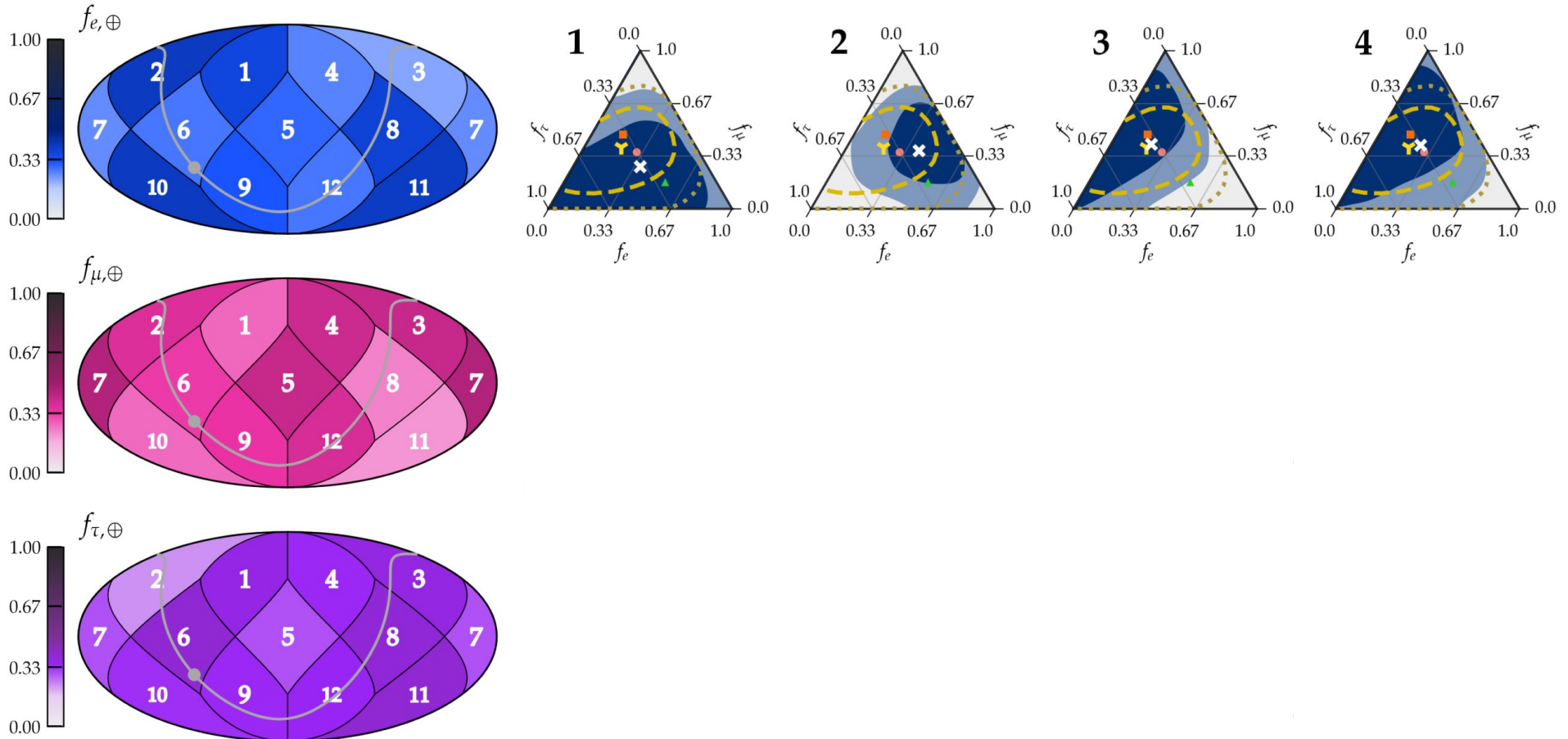
⊗ Best fit   ■ 1σ   ■ 2σ   □ 3σ

IceCube 2020 all-sky:

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Equatorial

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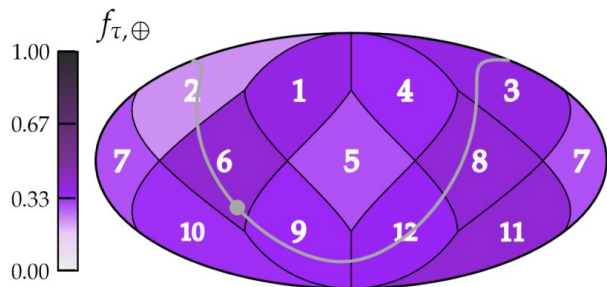
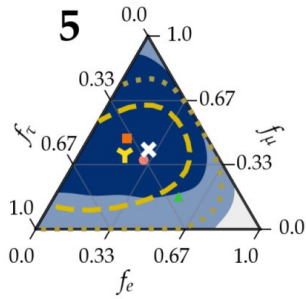
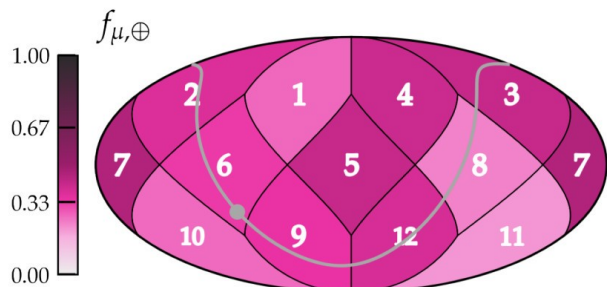
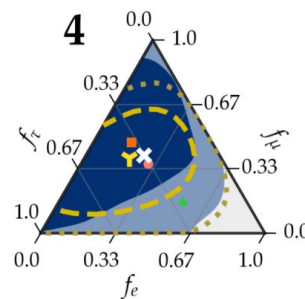
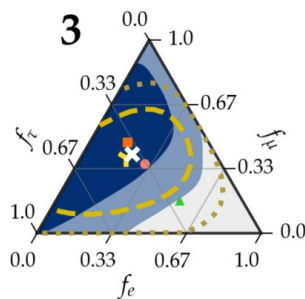
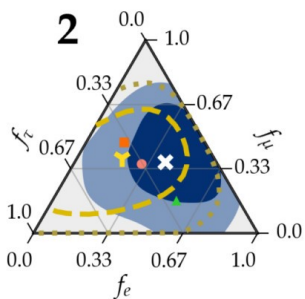
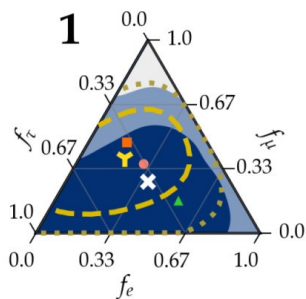
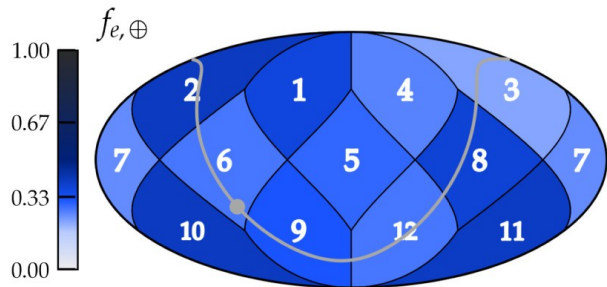
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Benchmarks:

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Equatorial

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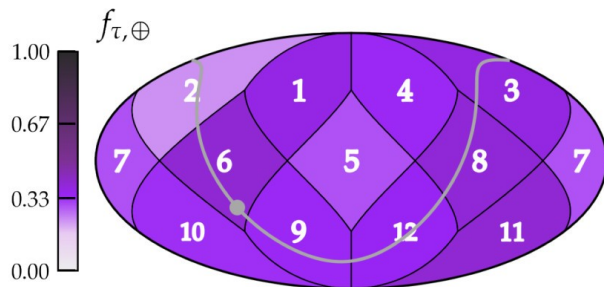
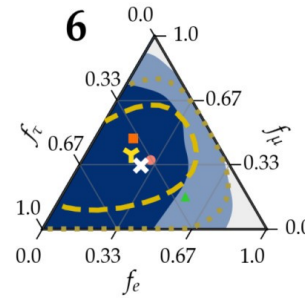
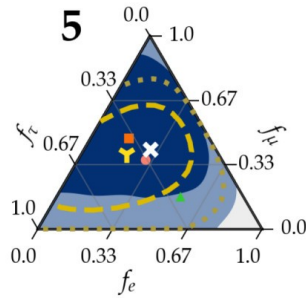
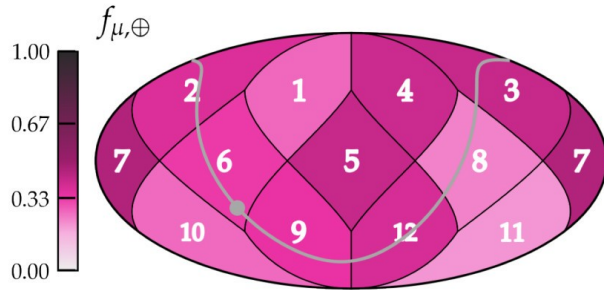
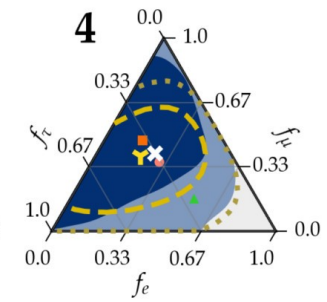
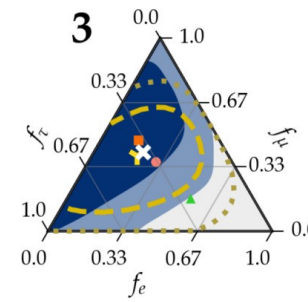
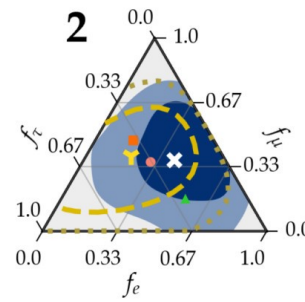
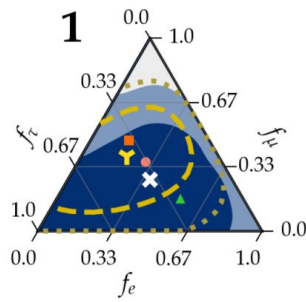
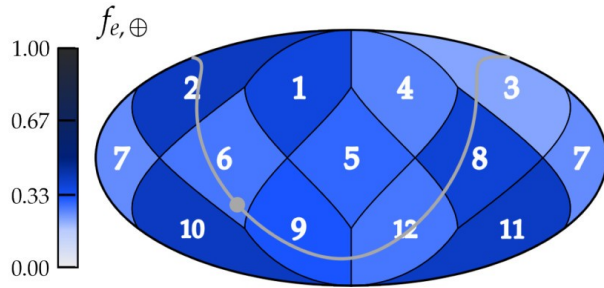
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IceCube 2020 all-sky:

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Benchmarks:

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Equatorial

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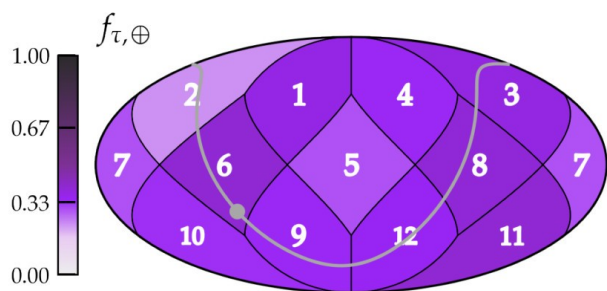
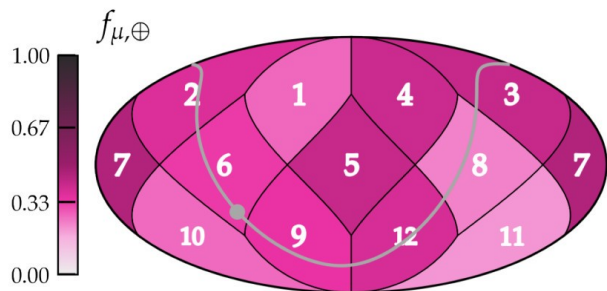
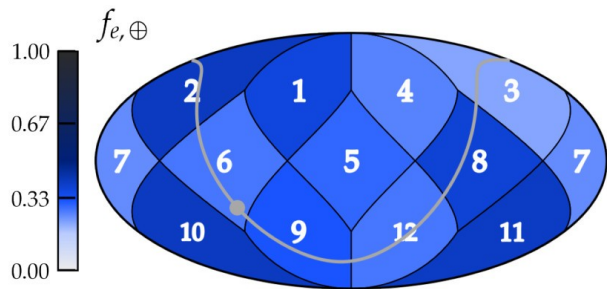
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IceCube 2020 all-sky:

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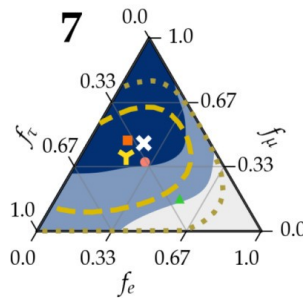
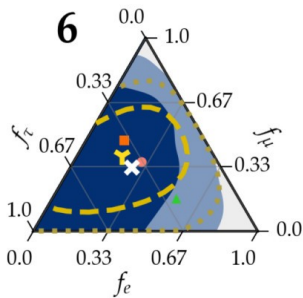
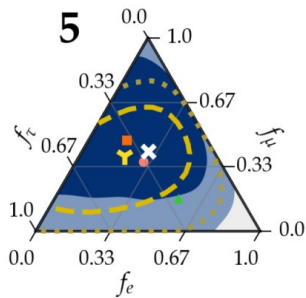
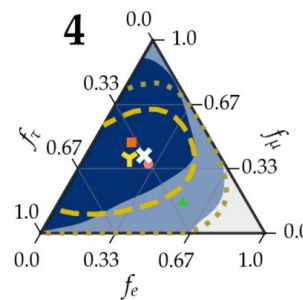
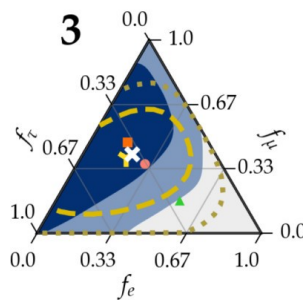
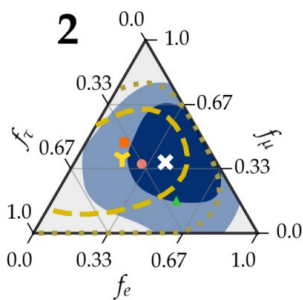
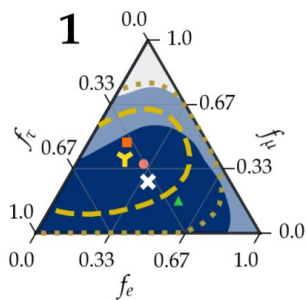
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Equatorial

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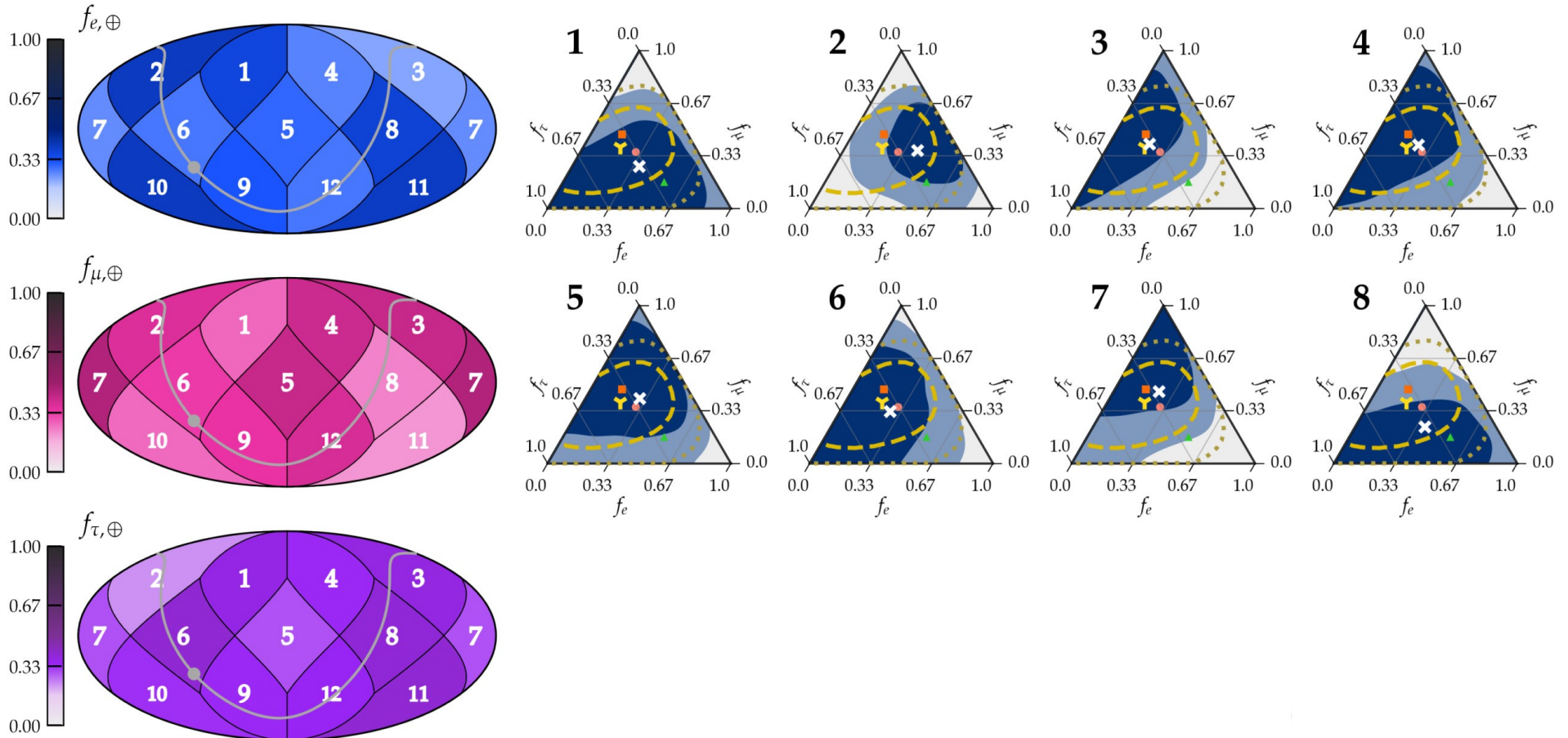
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IceCube 2020 all-sky:

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Benchmarks:

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Equatorial

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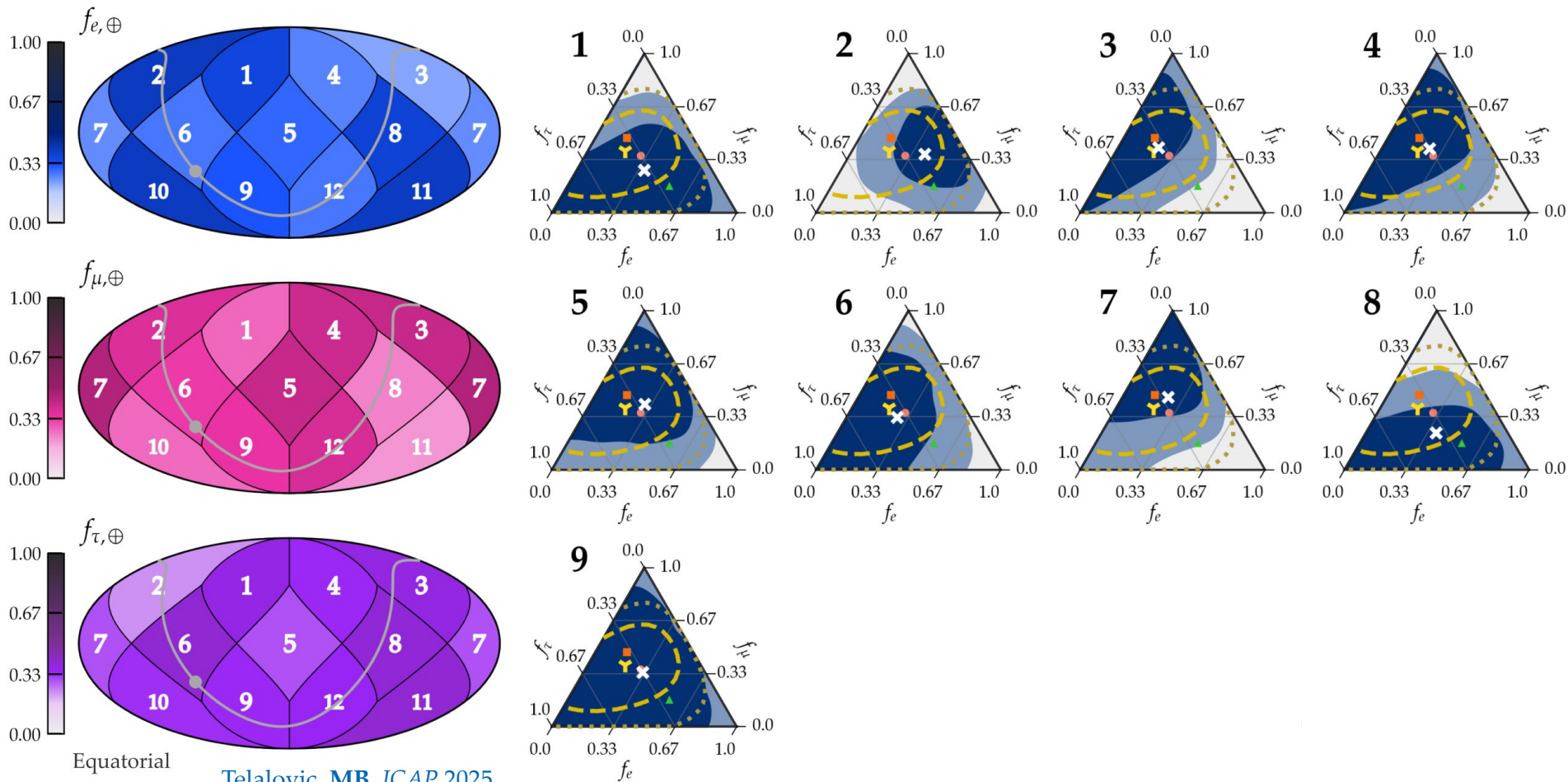
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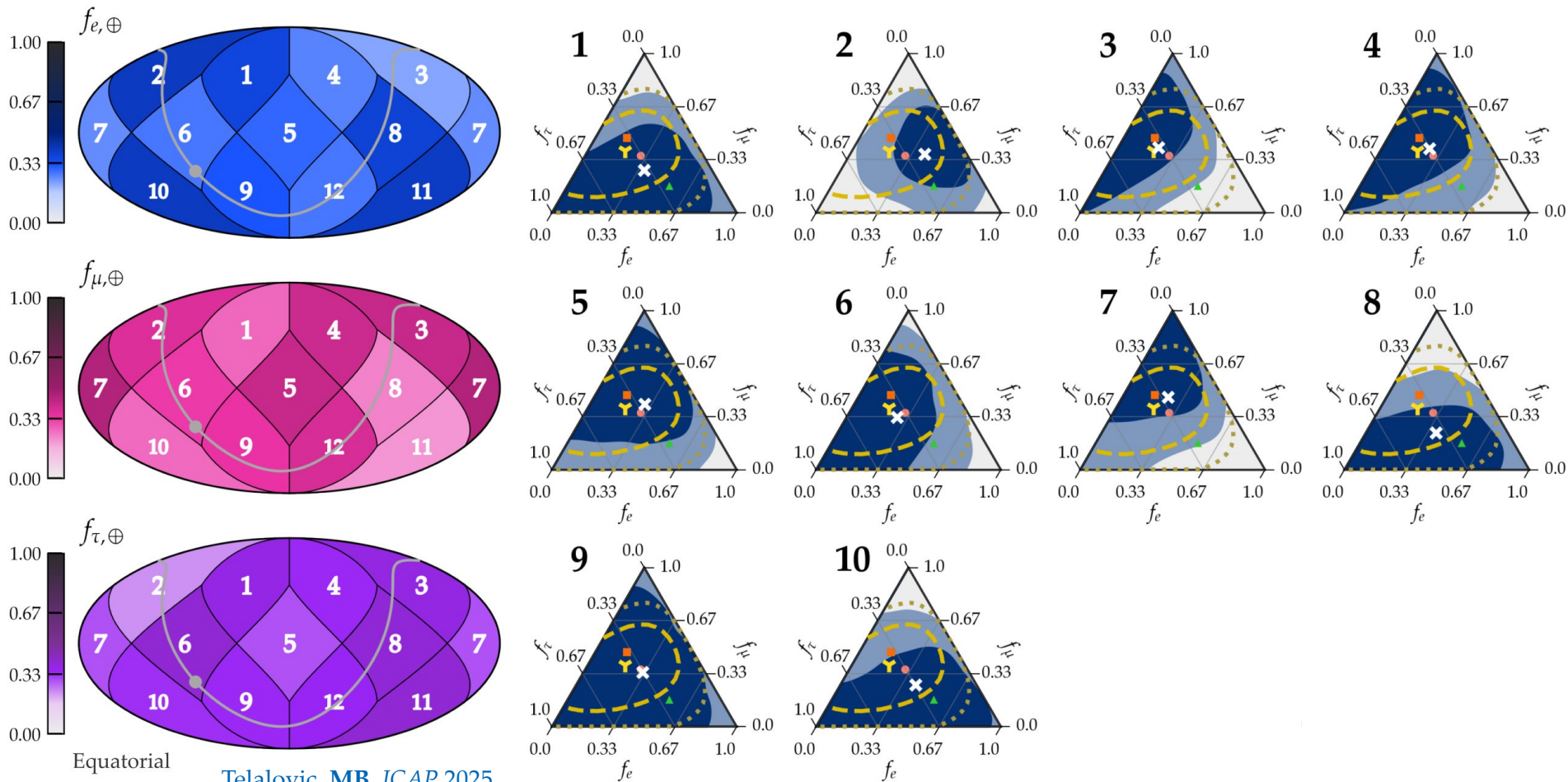
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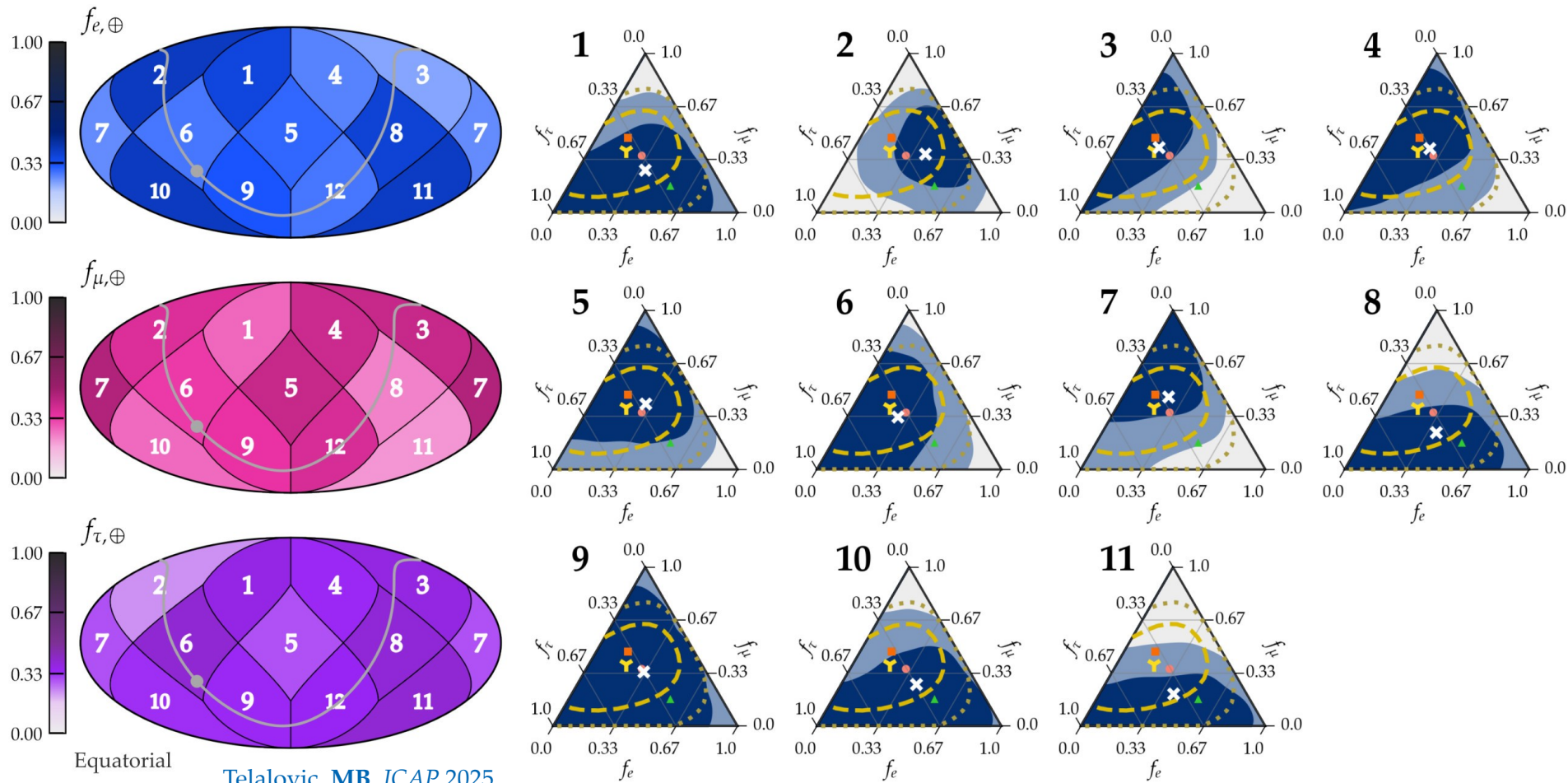
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Equatorial

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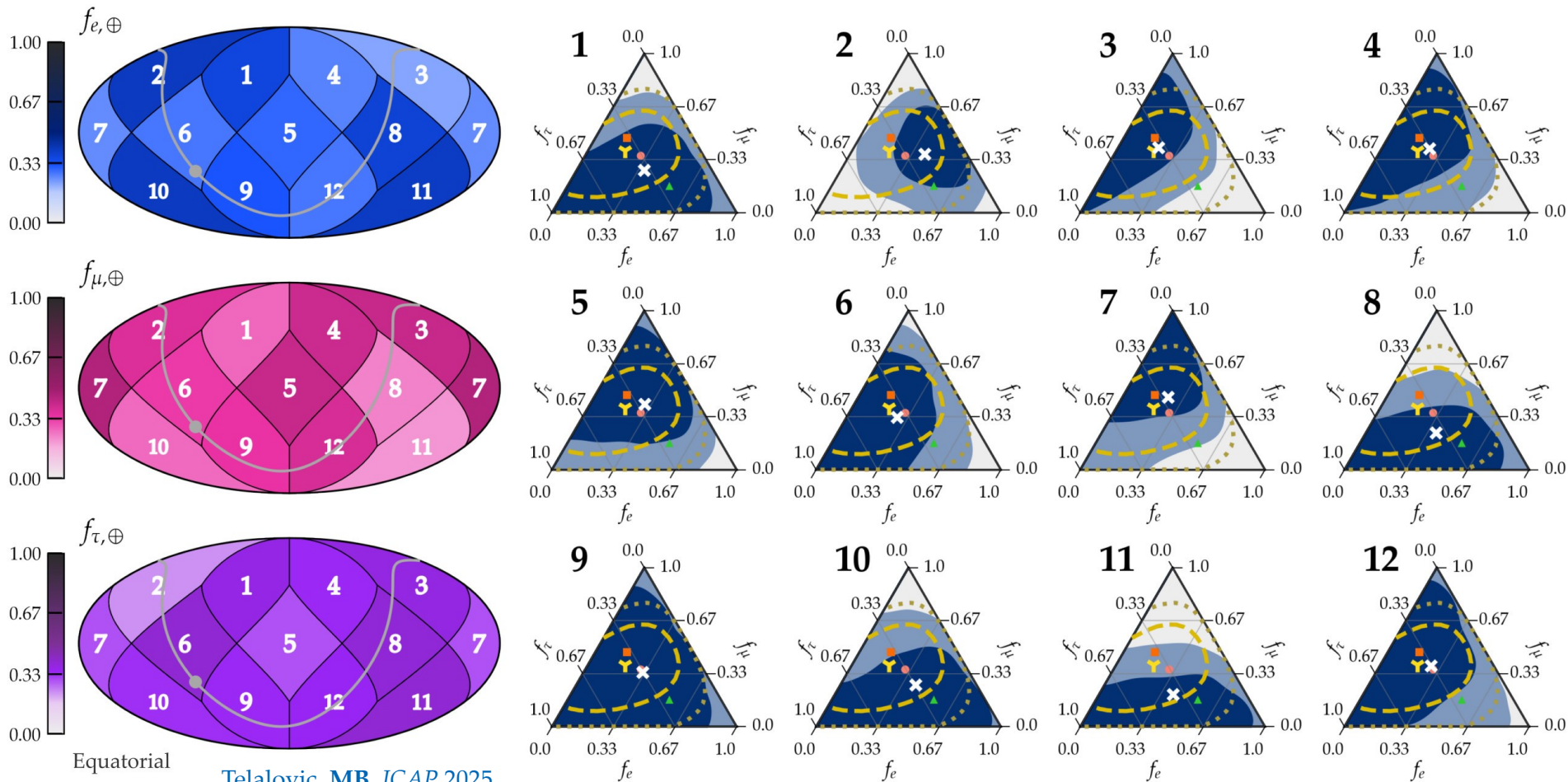
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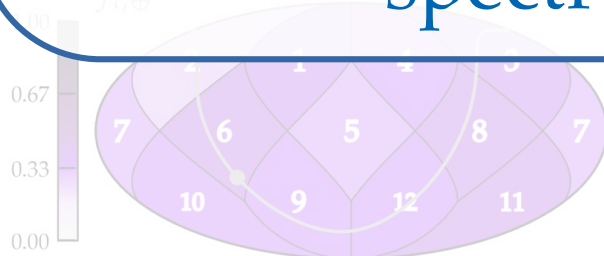
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There is no sign of flavor anisotropy  
in present-day IceCube data  
(Bayes factor is  $\sim 1$ )

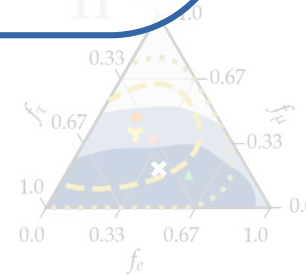
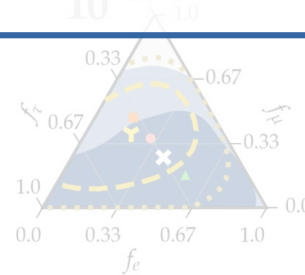
We place the first constraints on  
the flavor neutrino angular power  
spectrum *à la* CMB



Work led by  
Bernanda  
Telalovic



Telalovic, MB, 2310.15224



# New physics in the flavor composition

# Fundamental physics with high-energy cosmic neutrinos

Numerous new  $\nu$  physics effects grow as  $\sim \kappa_n \cdot E^n \cdot L$

So we can probe  $\kappa_n \sim 4 \cdot 10^{-47} (E/\text{PeV})^{-n} (L/\text{Gpc})^{-1} \text{PeV}^{1-n}$

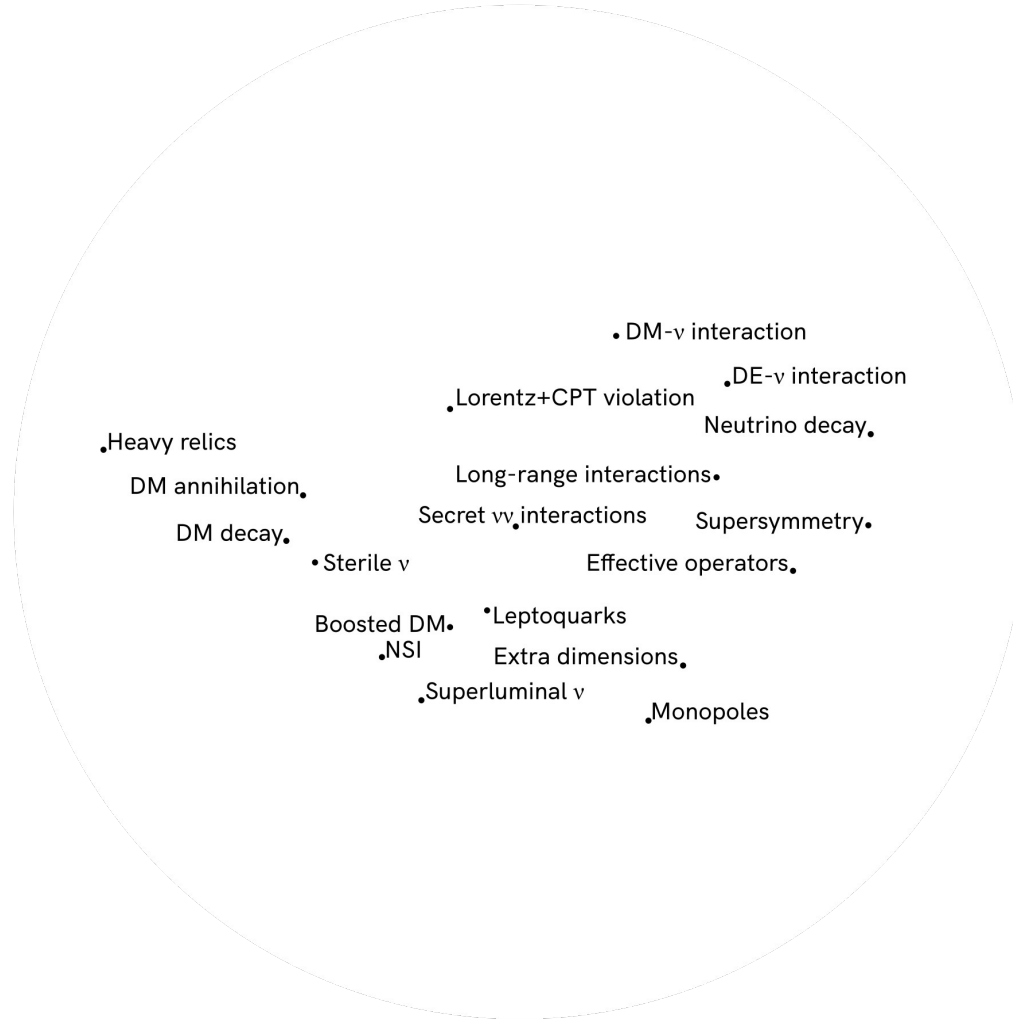
Improvement over limits using atmospheric  $\nu$ :  $\kappa_0 < 10^{-29} \text{PeV}$ ,  $\kappa_1 < 10^{-33}$

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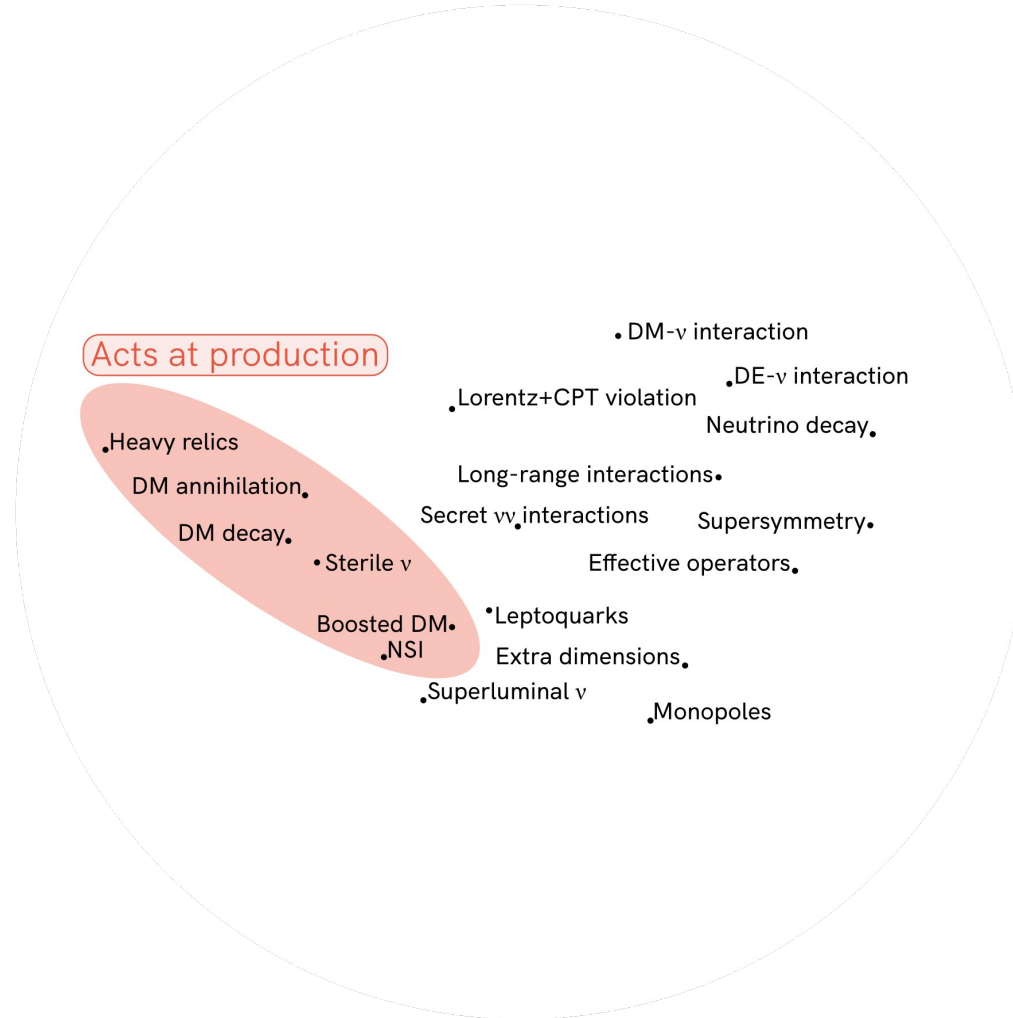
Numerous new  $\nu$  physics effects grow as  $\sim \kappa_n \cdot E^n \cdot L$  } *E.g.,*  
 $n = -1$ : neutrino decay  
 $n = 0$ : CPT-odd Lorentz violation  
 $n = +1$ : CPT-even Lorentz violation

So we can probe  $\kappa_n \sim 4 \cdot 10^{-47} (E/\text{PeV})^{-n} (L/\text{Gpc})^{-1} \text{PeV}^{1-n}$

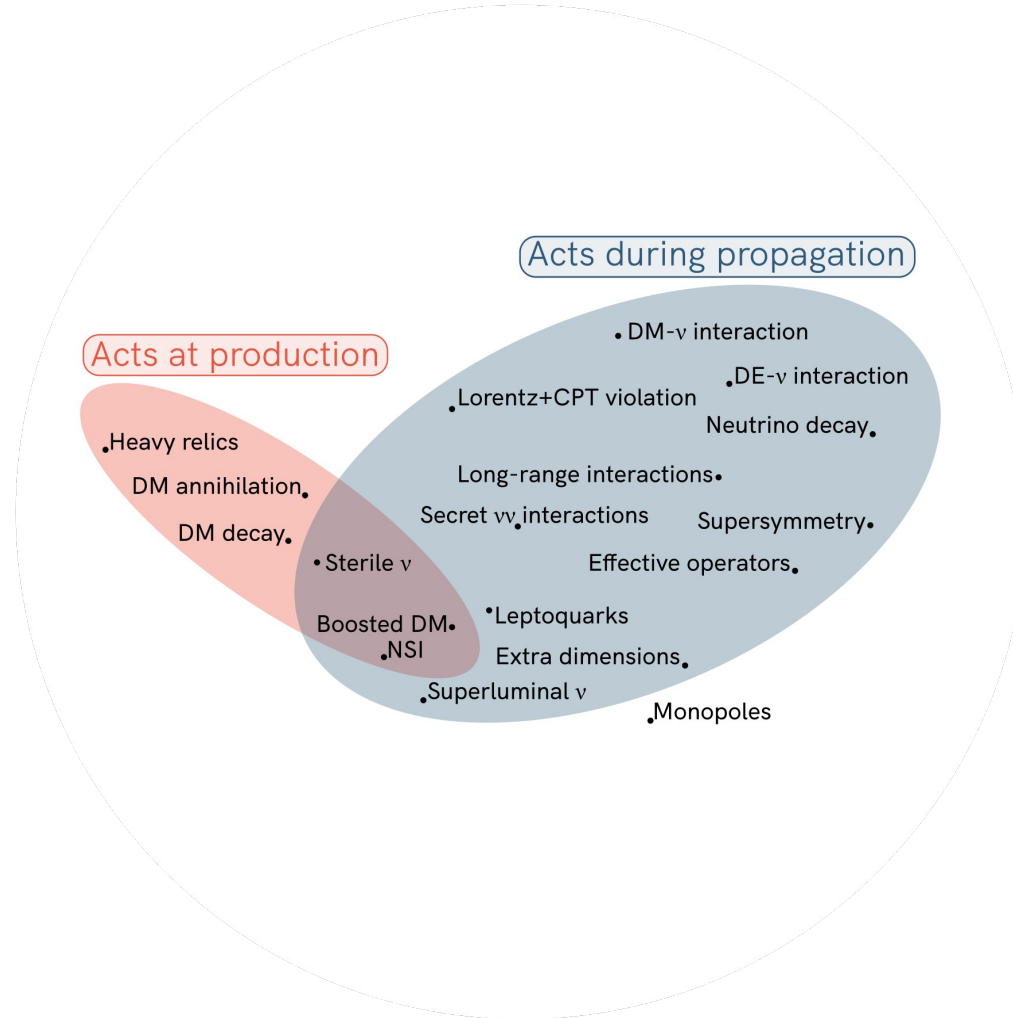
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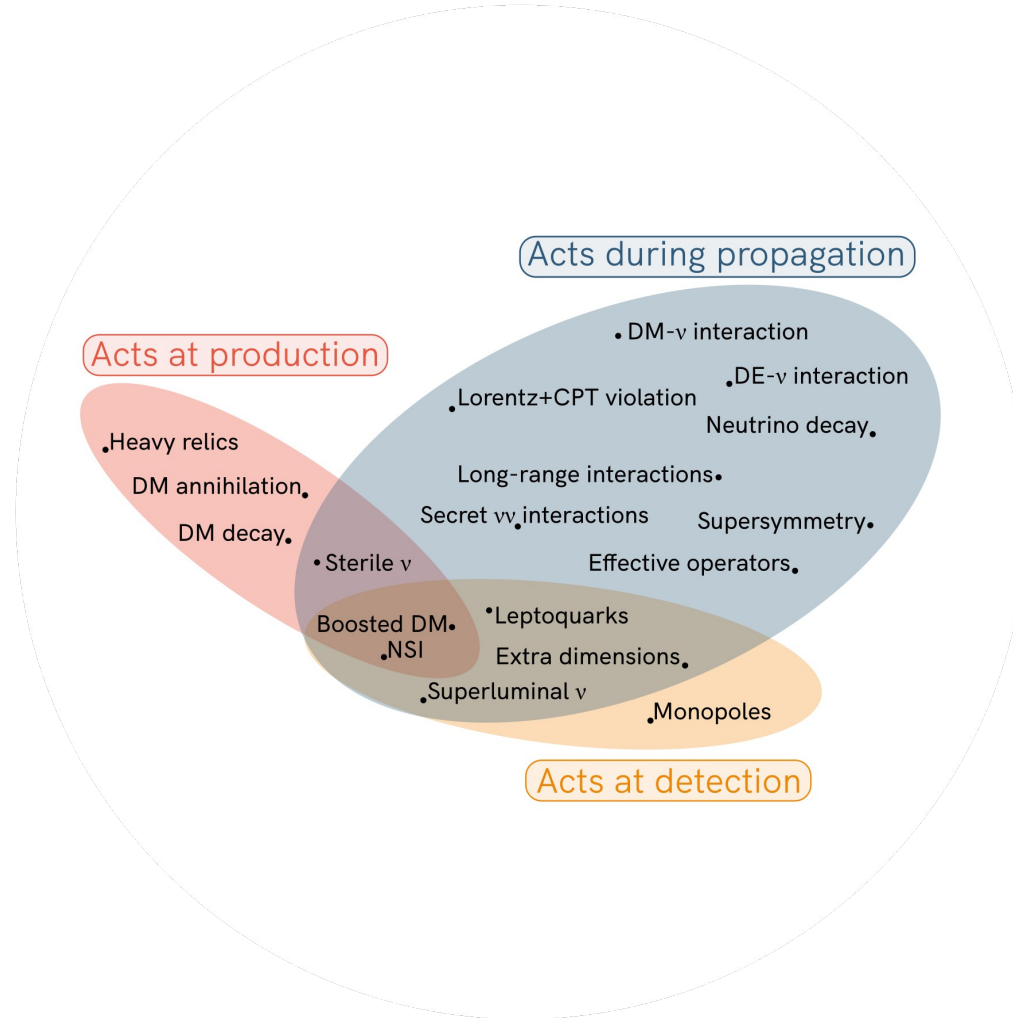
*Note: Not an exhaustive list*



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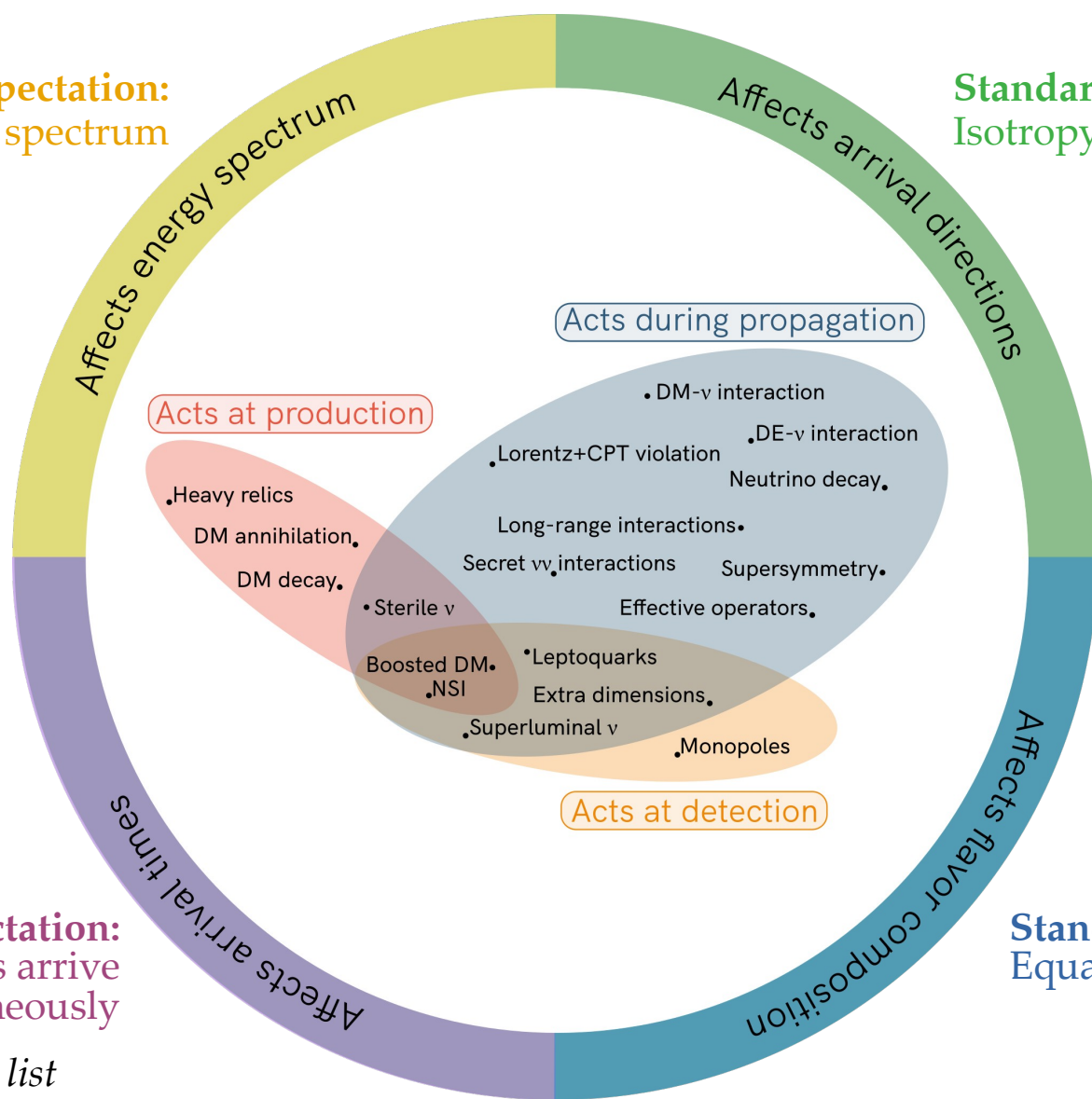
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**Standard expectation:**  
Power-law energy spectrum

**Standard expectation:**  
Isotropy (for diffuse flux)



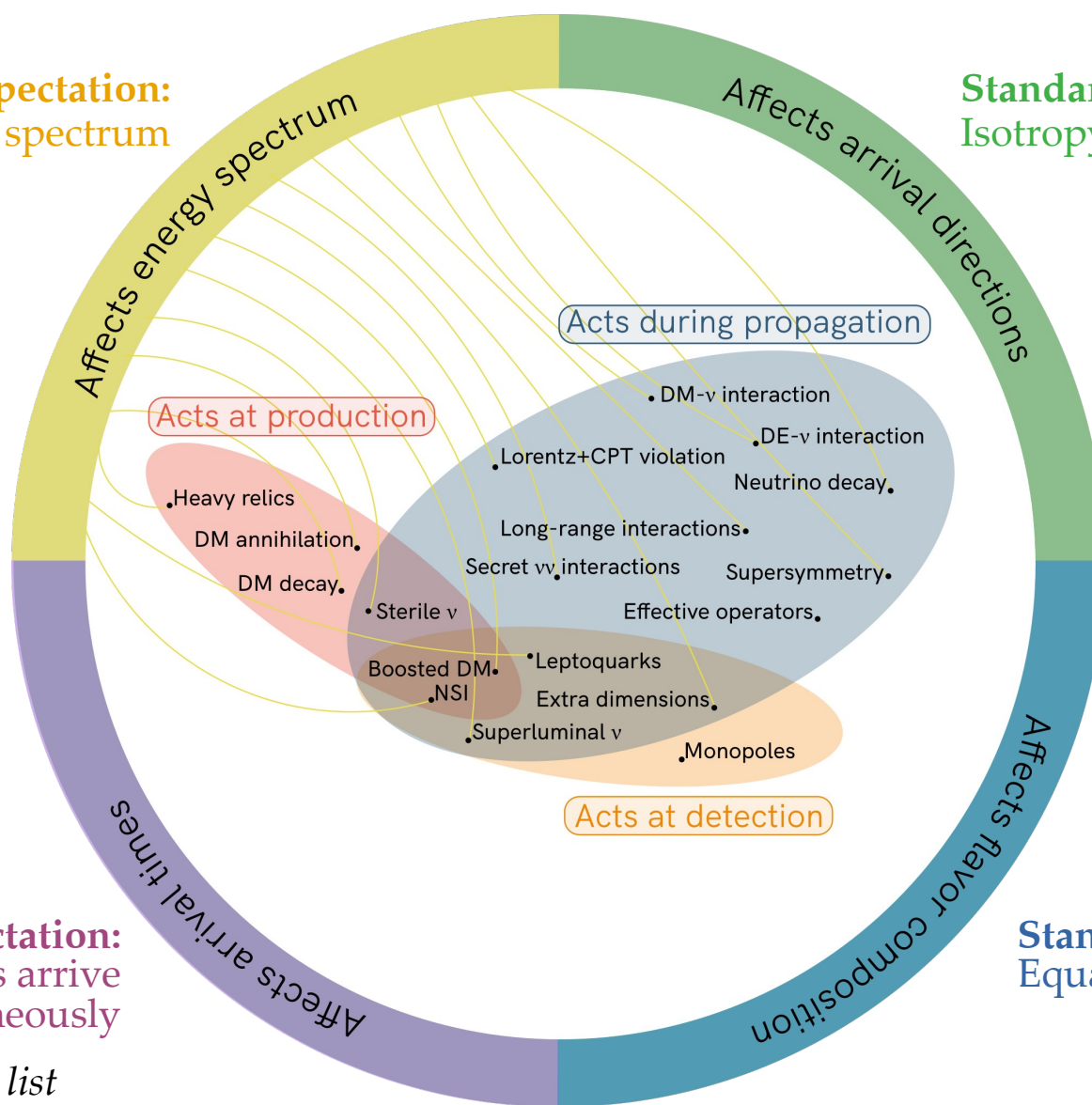
**Standard expectation:**  
Equal number of  $\nu_e, \nu_\mu, \nu_\tau$

**Standard expectation:**  
 $\nu$  and  $\gamma$  from transients arrive simultaneously

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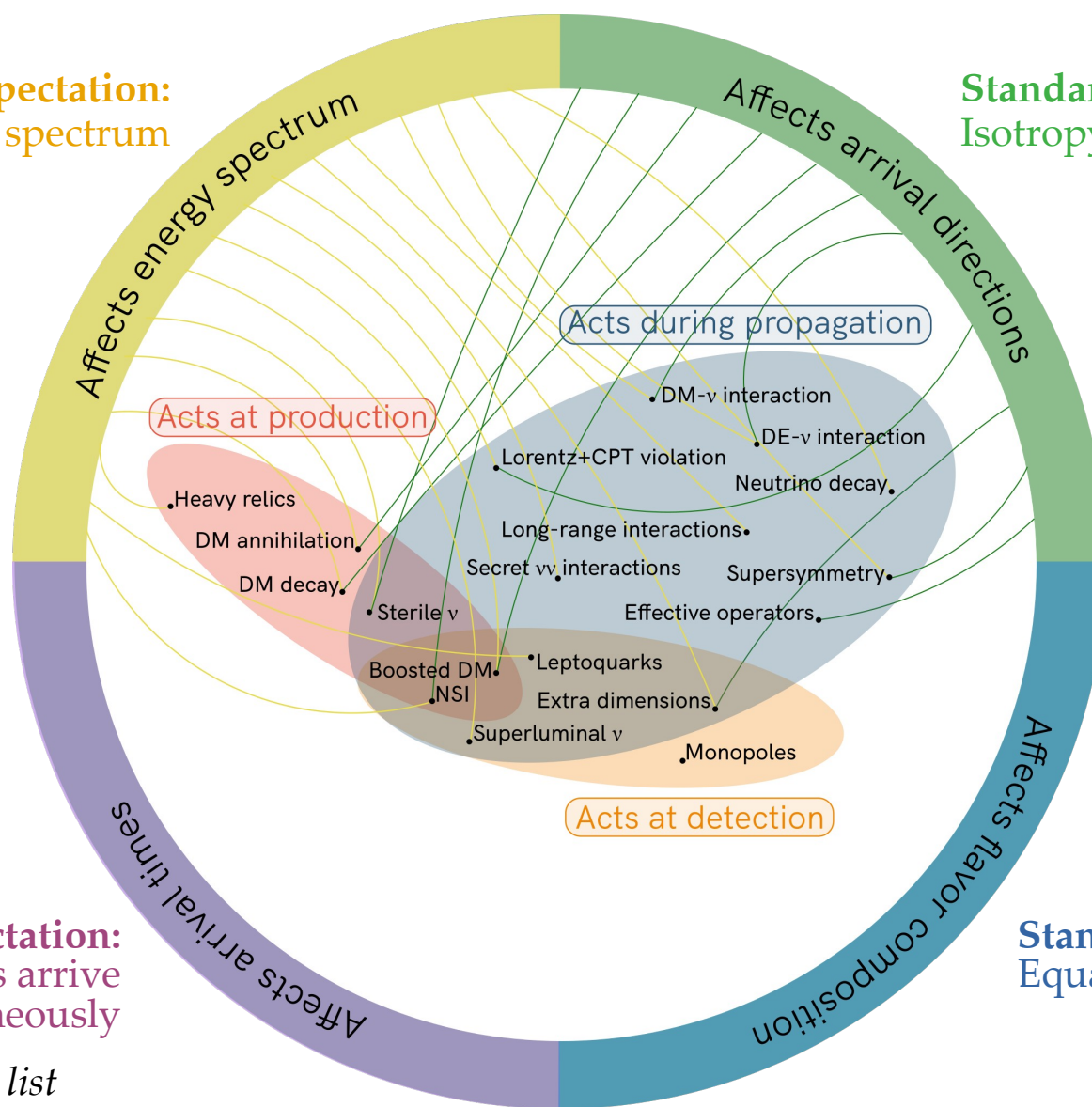
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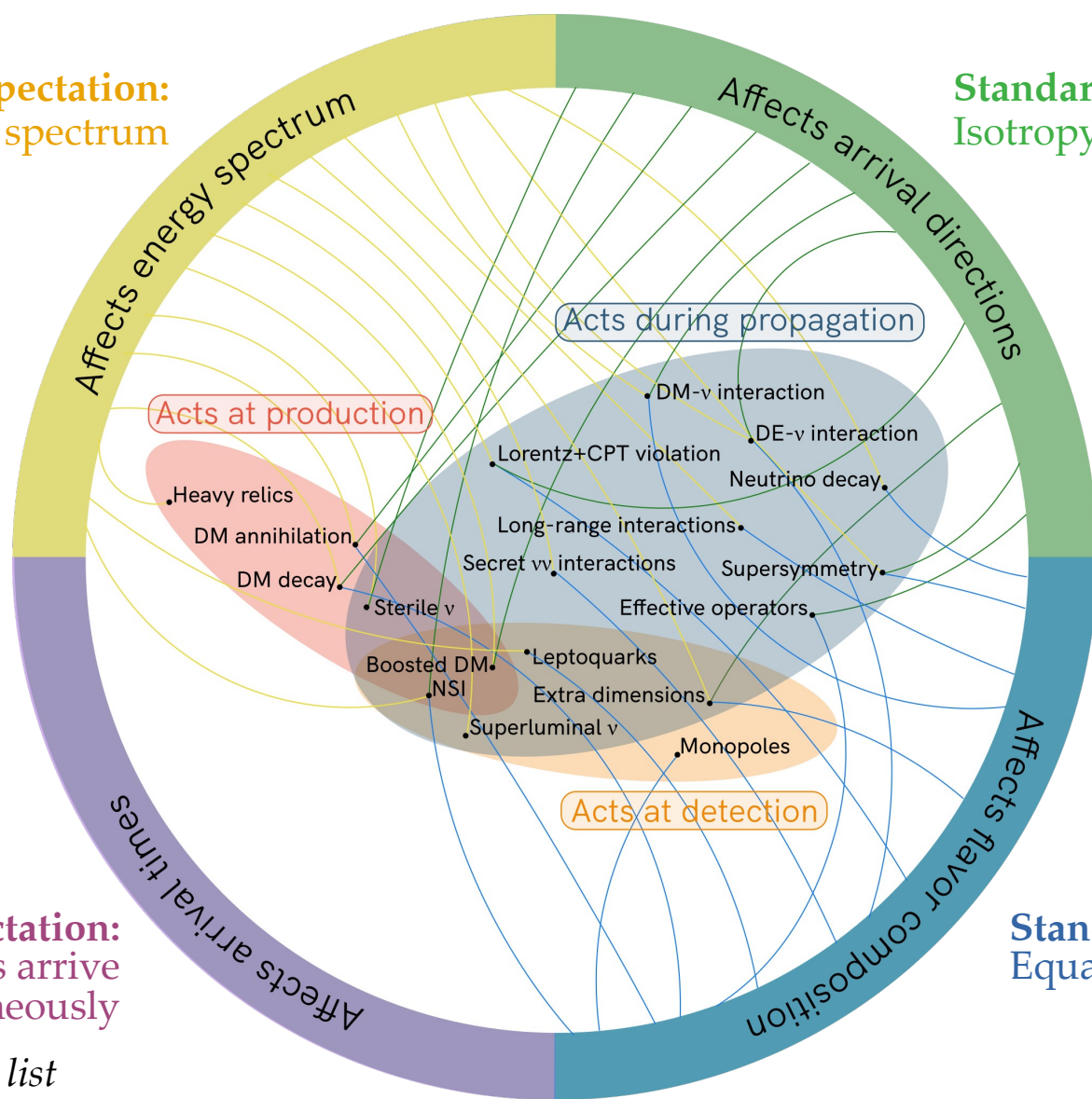
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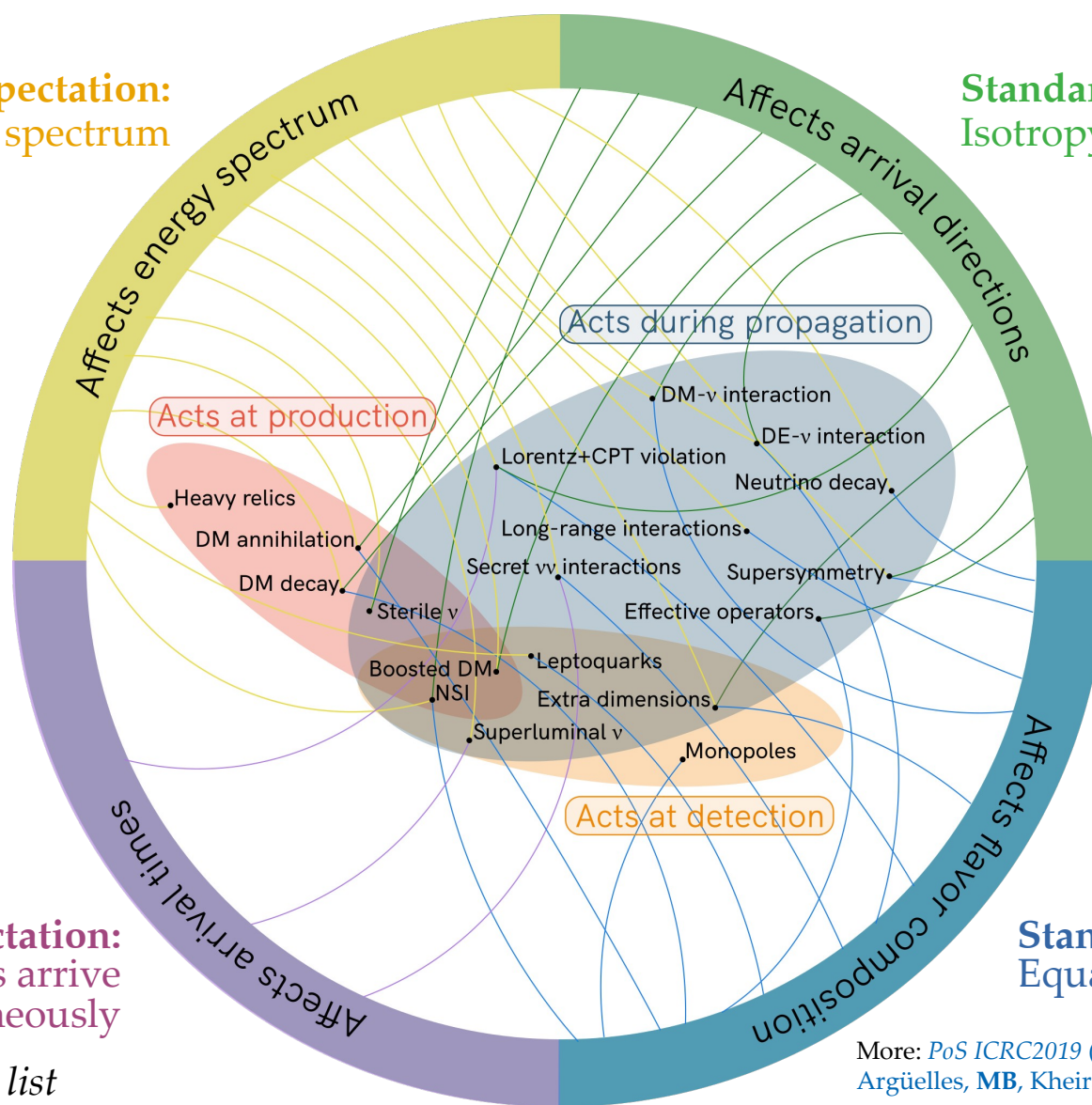
**Standard expectation:**  
 $\nu$  and  $\gamma$  from transients arrive  
simultaneously

**Standard expectation:**  
Equal number of  $\nu_e, \nu_\mu, \nu_\tau$

*Note: Not an exhaustive list*

**Standard expectation:**  
Power-law energy spectrum

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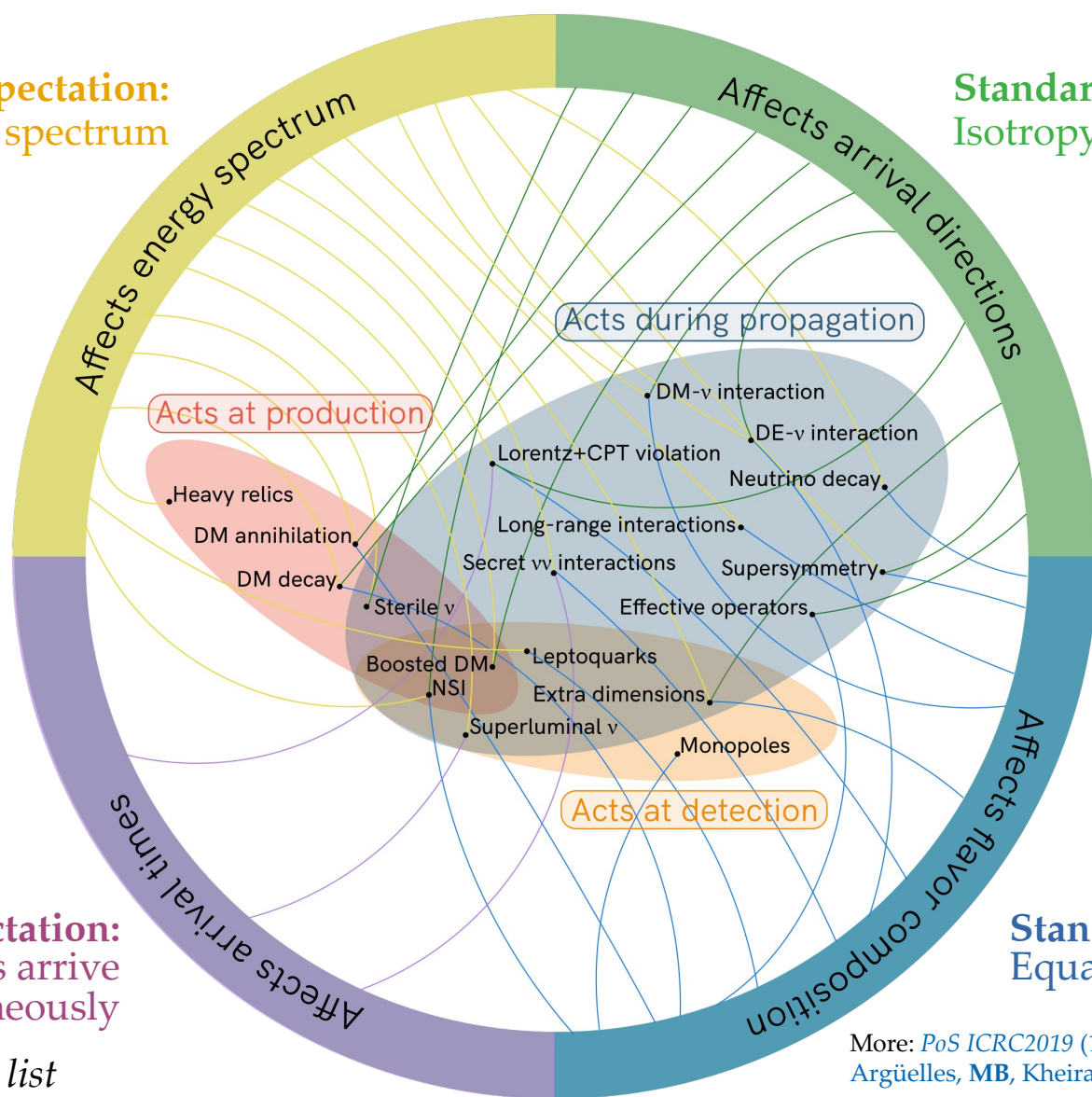
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More: *PoS ICRC2019 (1907.08690)*  
Argüelles, MB, Kheirandish, Palomares-Ruiz, Salvadó, Vincent

Standard expectation:  
Power-law energy spectrum

Standard expectation:  
Isotropy (for diffuse flux)

Affects energy spectrum

Affects arrival directions

Acts during propagation

Acts at production

### Reviews:

Ahlers, Helbing, De los Heros, *EPJC* 2018

Argüelles, MB, Kheirandish, Palomares-Ruiz, Salvadó, Vincent, *ICRC* 2019 [1907.08690]

Ackermann, Ahlers, Anchordoqui, MB, et al., *Astro2020 Decadal Survey* [1903.04333]

Affects arrival times

Affects flavor composition

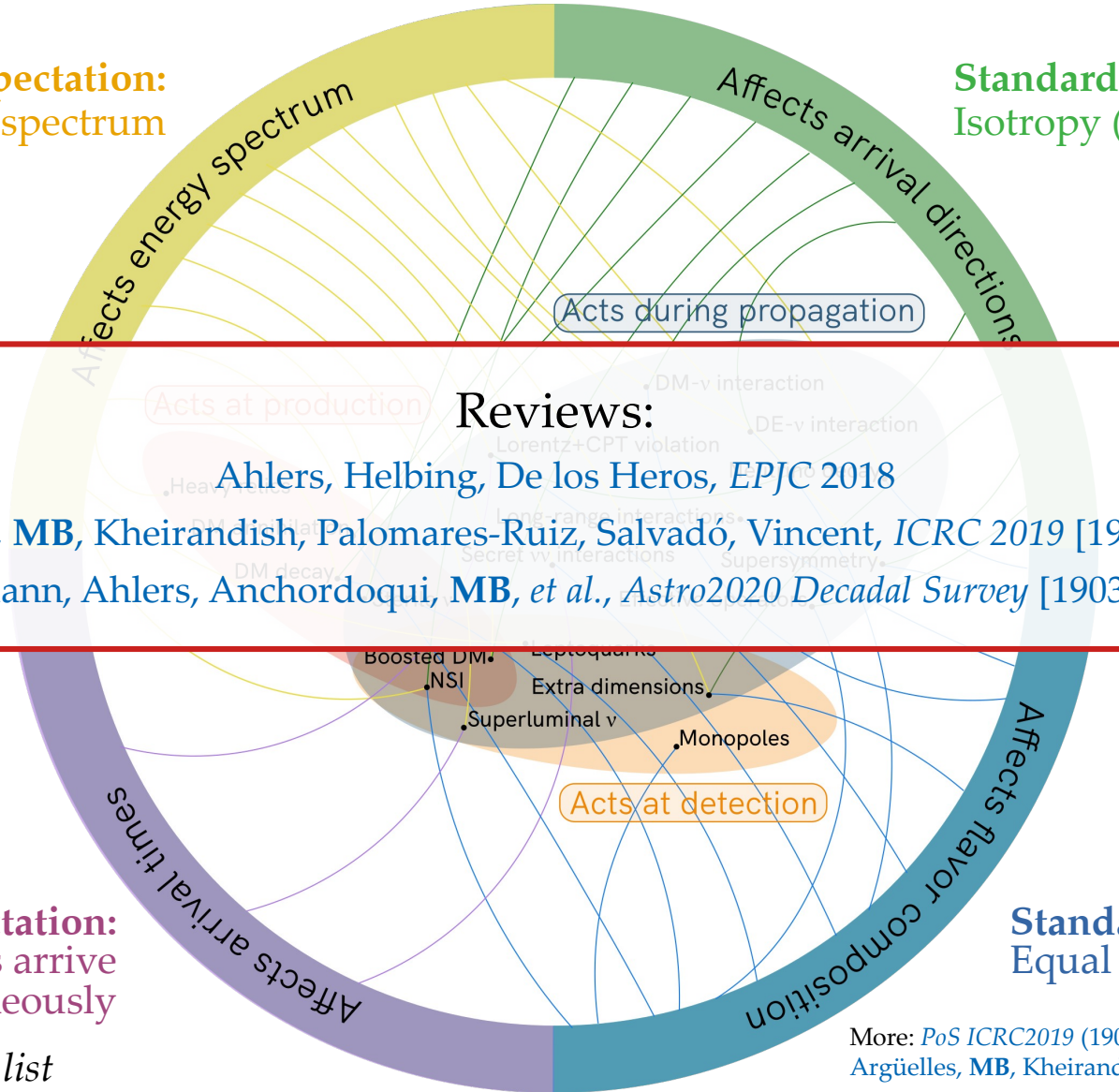
Acts at detection

Standard expectation:  
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simultaneously

Standard expectation:  
Equal number of  $\nu_e, \nu_\mu, \nu_\tau$

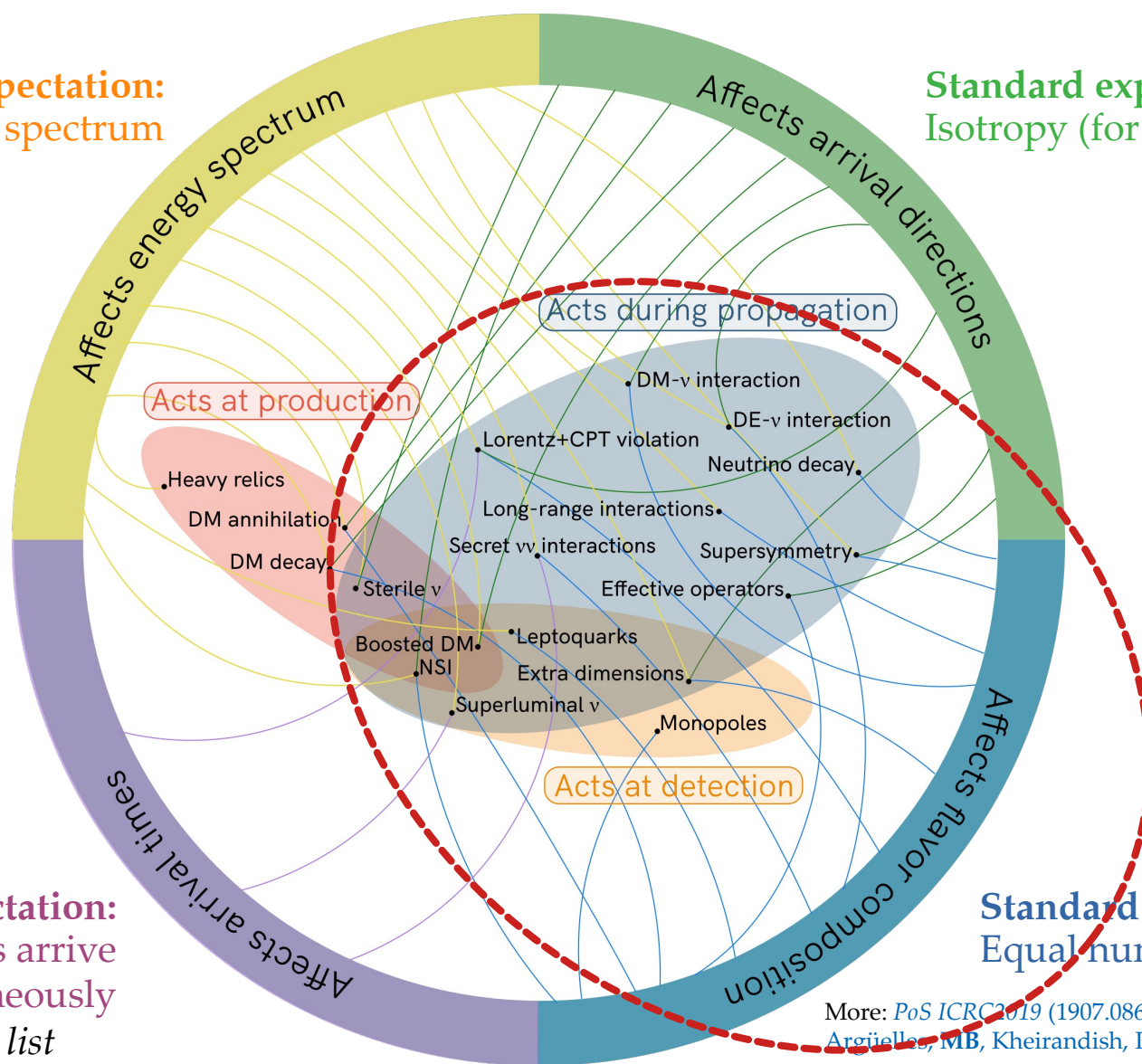
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# New physics in flavor composition

Use the flavor sensitivity to test new physics:

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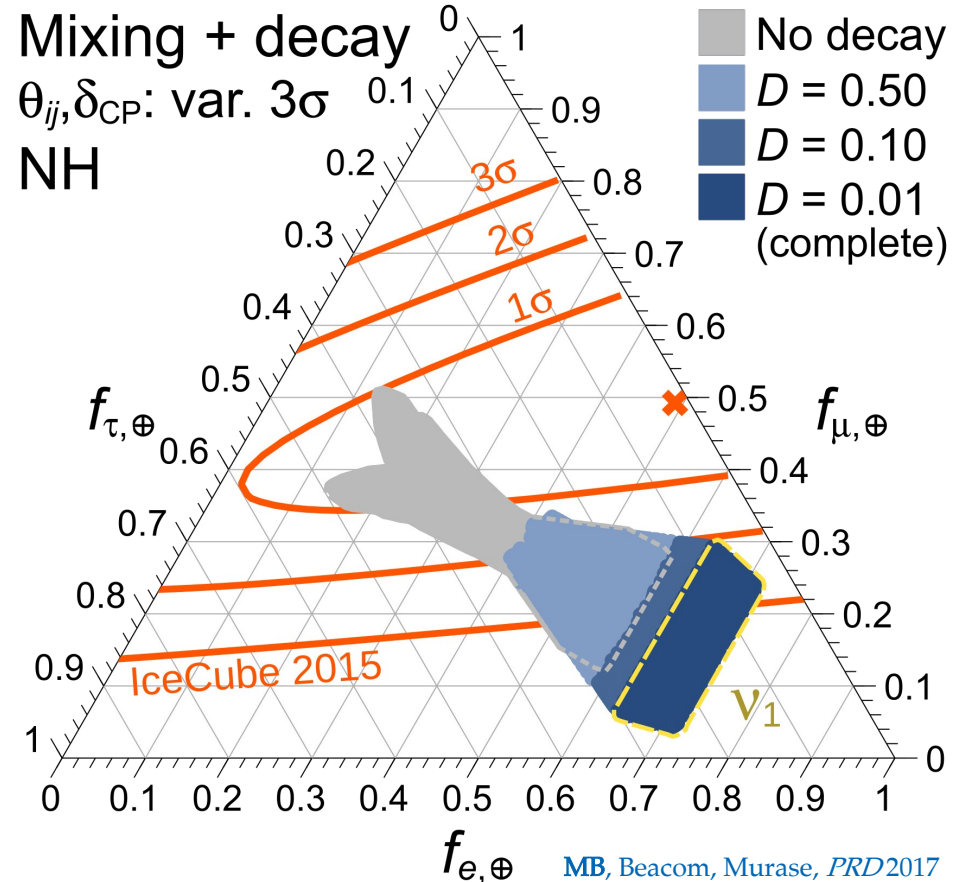
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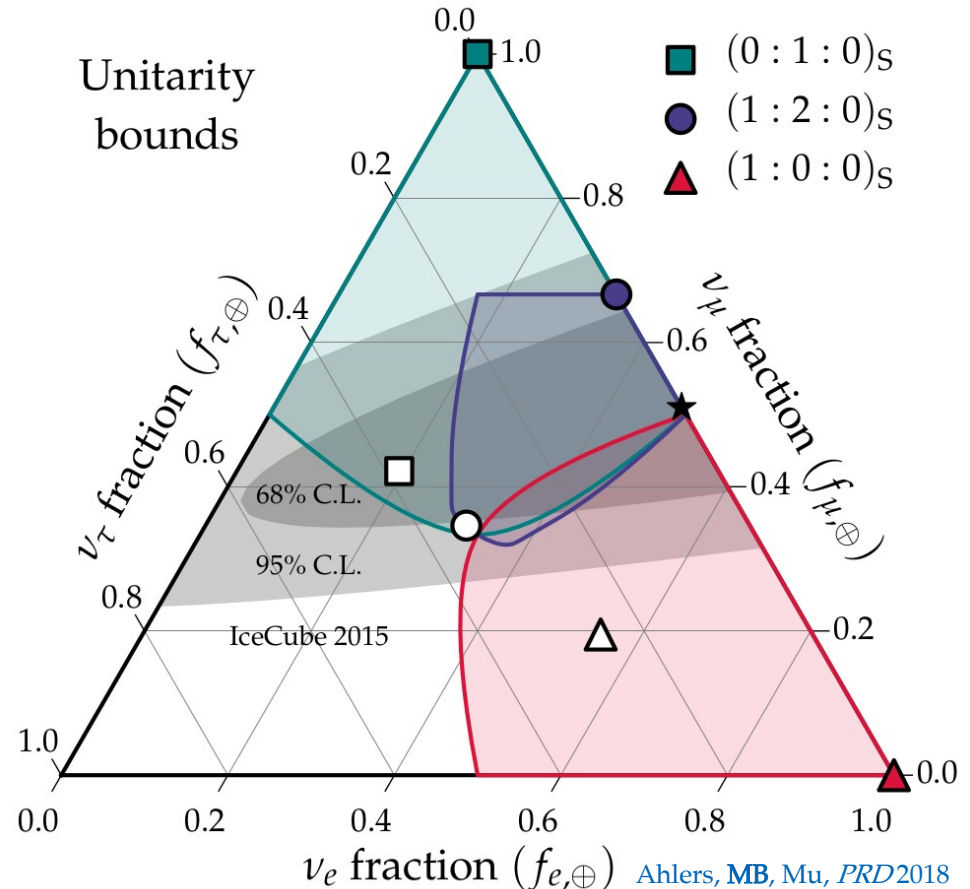
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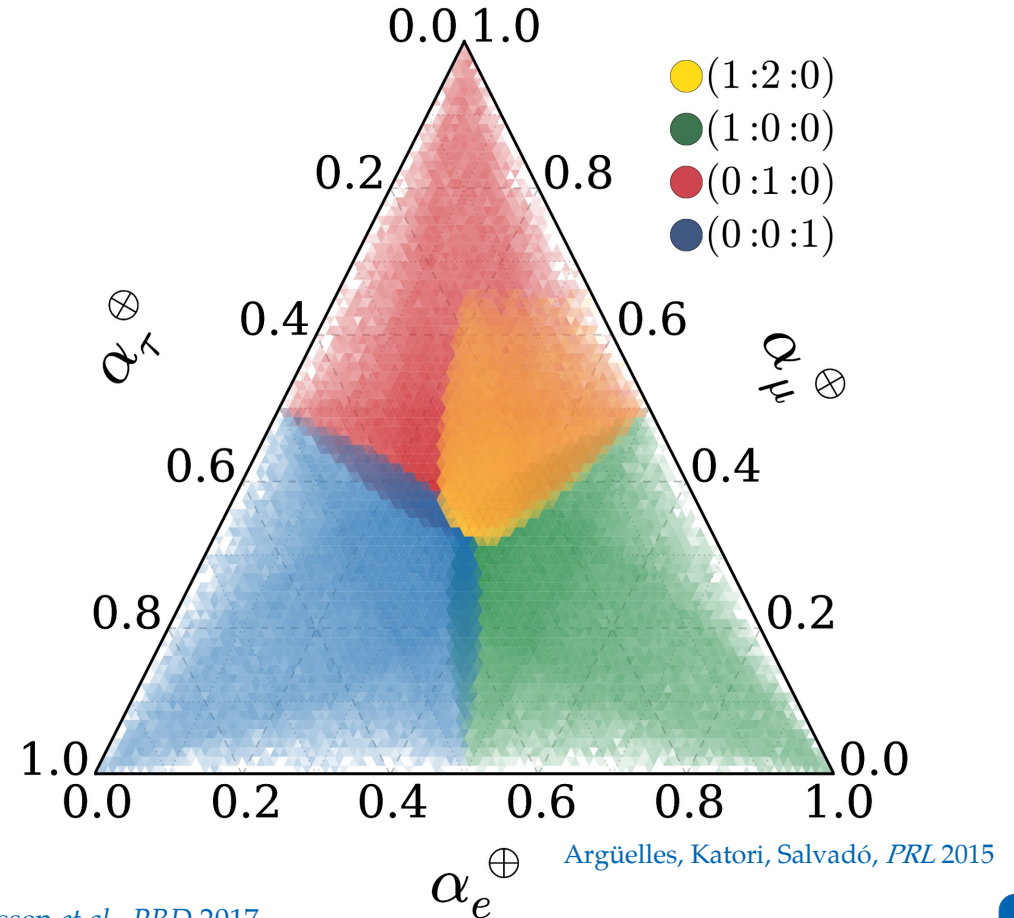
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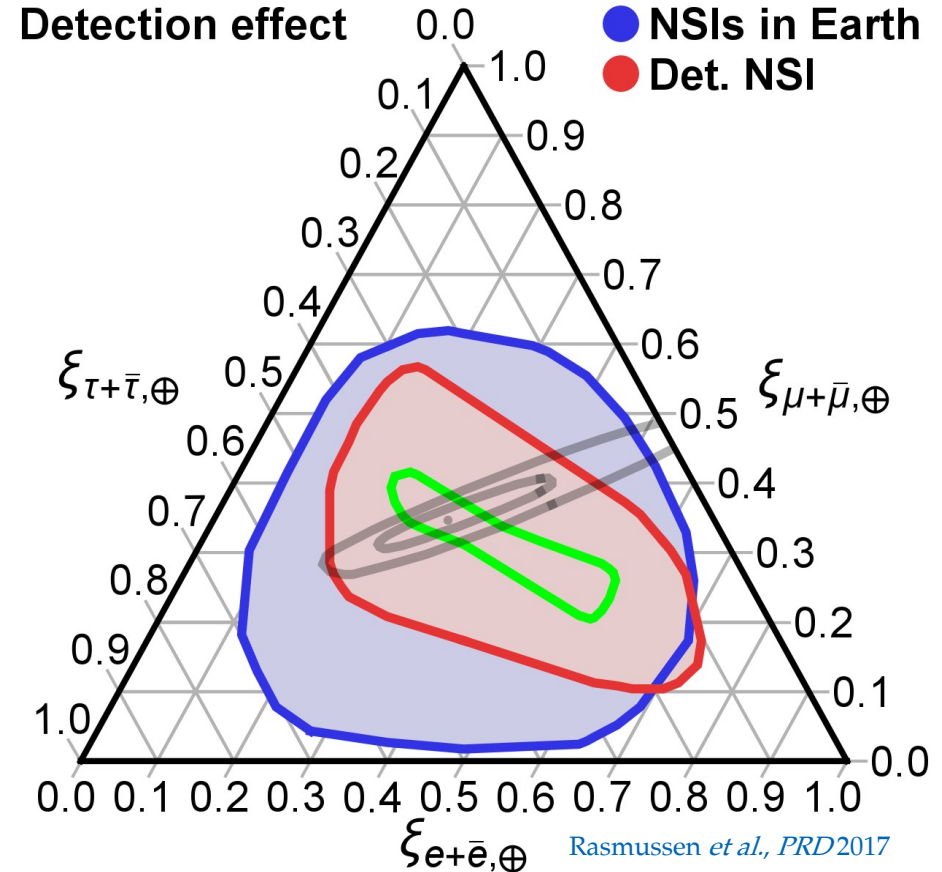
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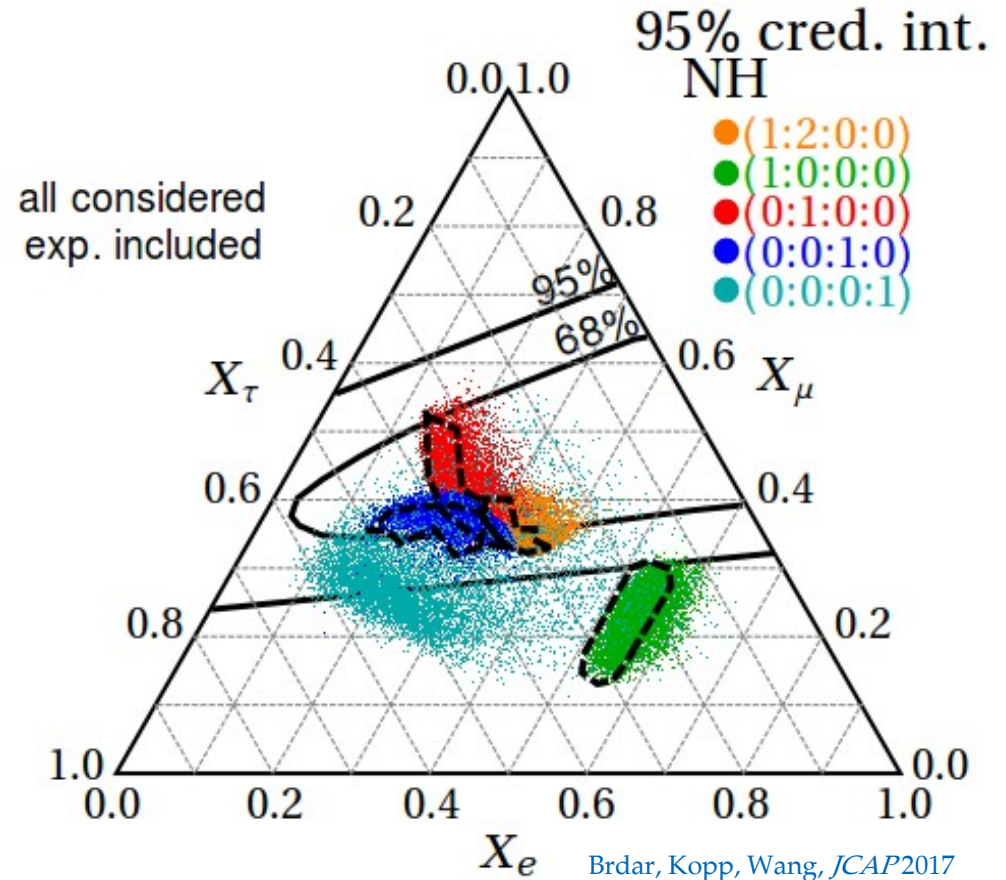
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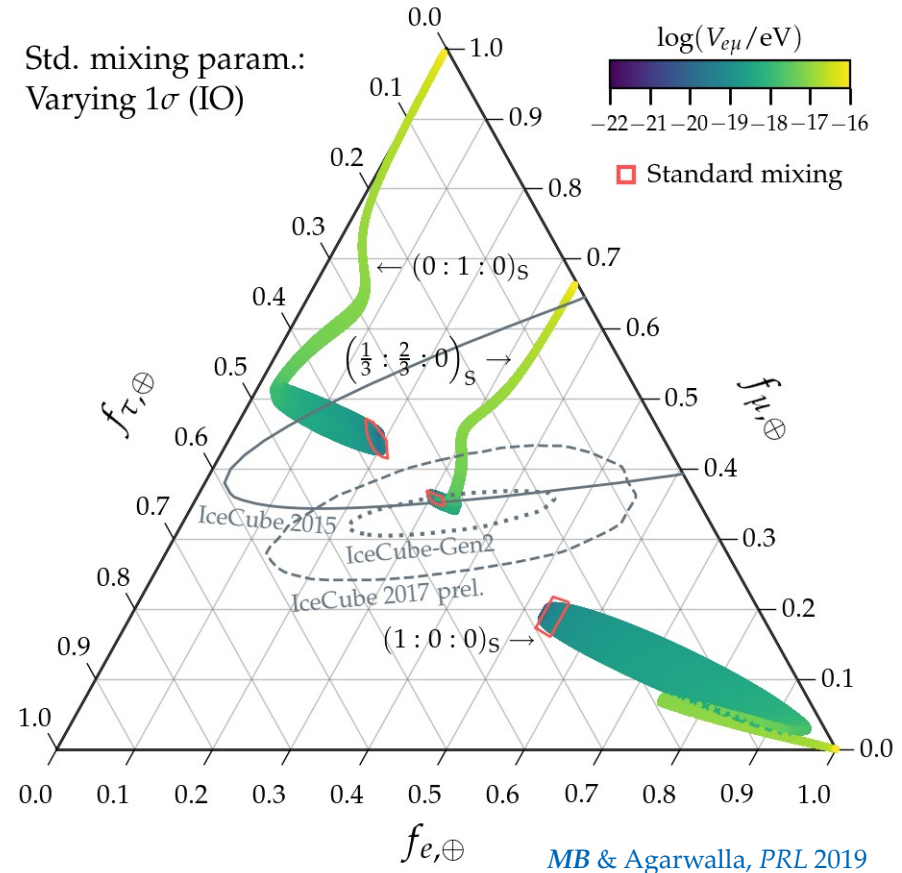
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## ► Long-range $e\nu$ interactions

[*MB* & Agarwalla, *PRL* 2019]

Reviews:

Argüelles *et al.* (inc. *MB*), *EPJC* 2023; Mehta & Winter, *JCAP* 2011; Rasmussen *et al.*, *PRD* 2017



An example:  
Lorentz violation

Flavor-dependent  
interactions  
between neutrinos  
and a fundamental  
Lorentz-violating tensor




Standard oscillations:

$$H_{\text{std}} = \frac{1}{2E} U_{\text{PMNS}}^\dagger \text{diag}(0, \Delta m_{21}^2, \Delta m_{31}^2) U_{\text{PMNS}}$$

Lorentz-violating interactions (Standard Model Extension):

*Kostelecky, Mewes, PRD 2004*

$$H_{\text{new}} = \sum_{n \geq 0} \left( \frac{E}{\Lambda_n} \right)^n U_n^\dagger (\mathcal{O}_{n,1}, \mathcal{O}_{n,2}, \mathcal{O}_{n,3}) U_n$$


$U_n$  has the same shape as  $U_{\text{PMNS}}$ ,  
but its entries are a priori undetermined

Total Hamiltonian:

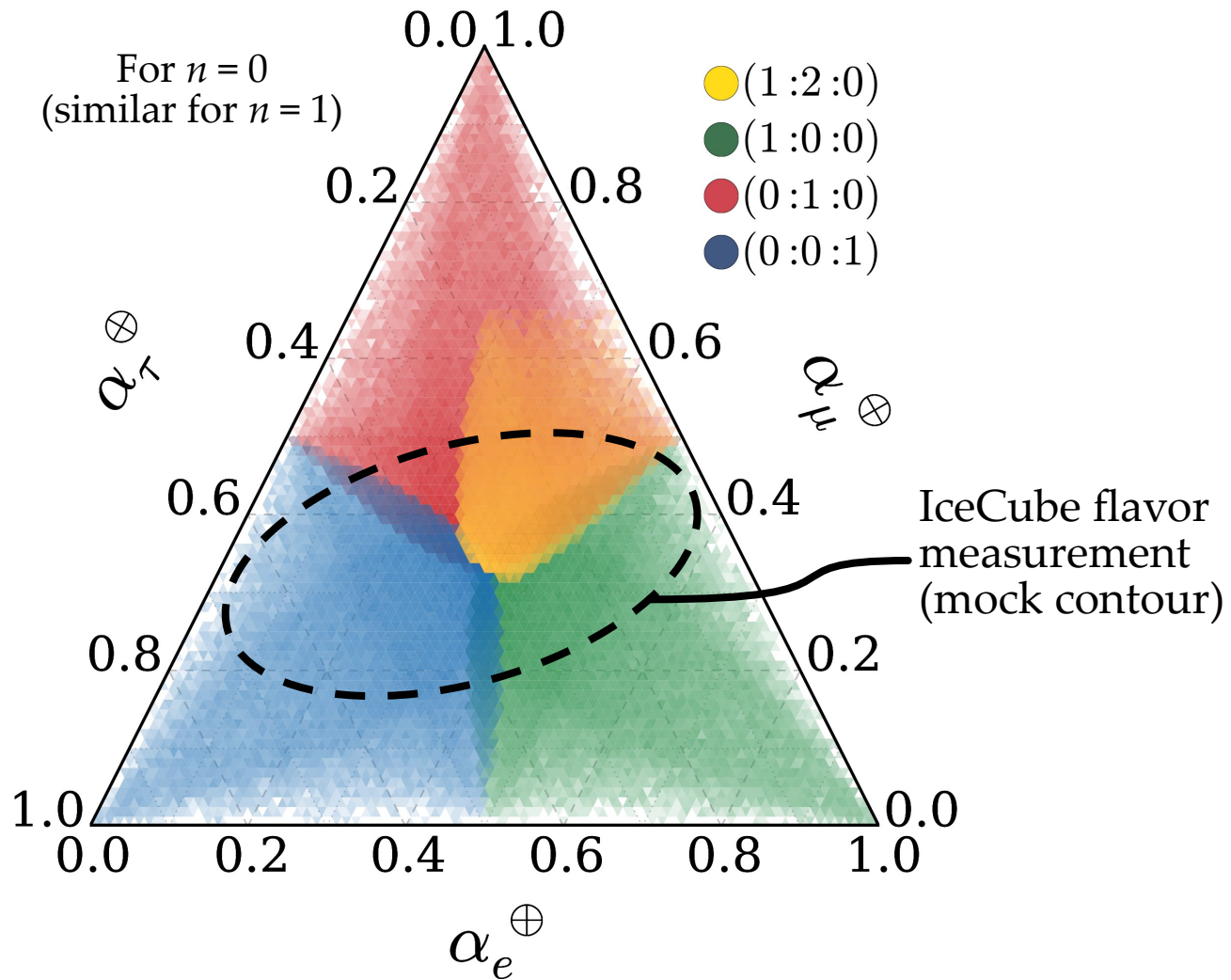
$$H_{\text{tot}} = H_{\text{std}} + H_{\text{new}}$$

The flavor-transition probabilities are calculated as before

$$P_{\alpha\beta} = \sum_{i=1}^3 |(\mathbf{U}_{\text{tot}})_{\alpha i}|^2 |(\mathbf{U}_{\text{tot}})_{\beta i}|^2 ,$$

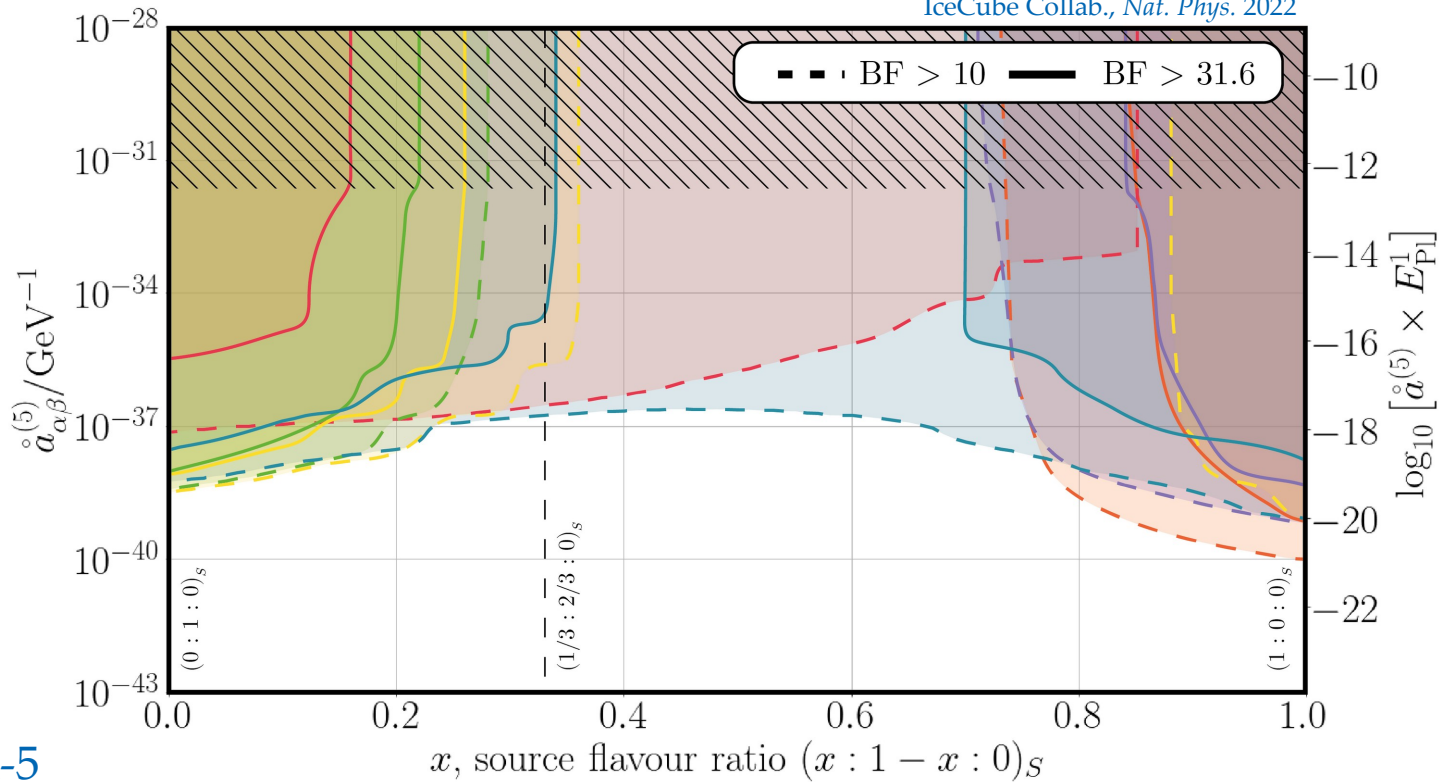
Depends on standard & new parameters

but now the lepton mixing matrix,  $\mathbf{U}_{\text{tot}}$ , is the one that diagonalizes  $H_{\text{tot}}$

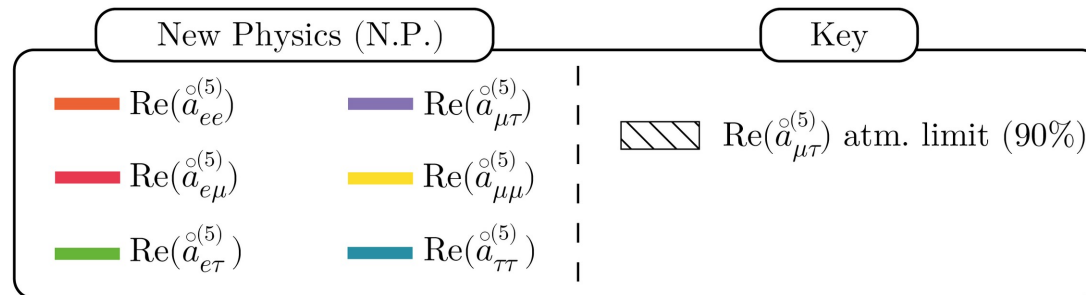


Argüelles, Katori, Salvadó, *PRL* 2015

See also Ahlers, **MB**, Mu, *PRD* 2018; Rasmussen *et al.*, *PRD* 2017; **MB**, Beacom, Winter *PRL* 2015;  
**MB**, Gago, Peña-Garay *JCAP* 2010; Bazo, **MB**, Gago, Miranda *IJMPA* 2009; + many others



Dimension-5  
CPT-odd  
isotropic  
Lorentz-invariance  
-violating  
coefficient



How it started

How it's going

10-20 years from now



How it started

How it's going

10–20 years from now

First predictions of high-energy cosmic  $\nu$



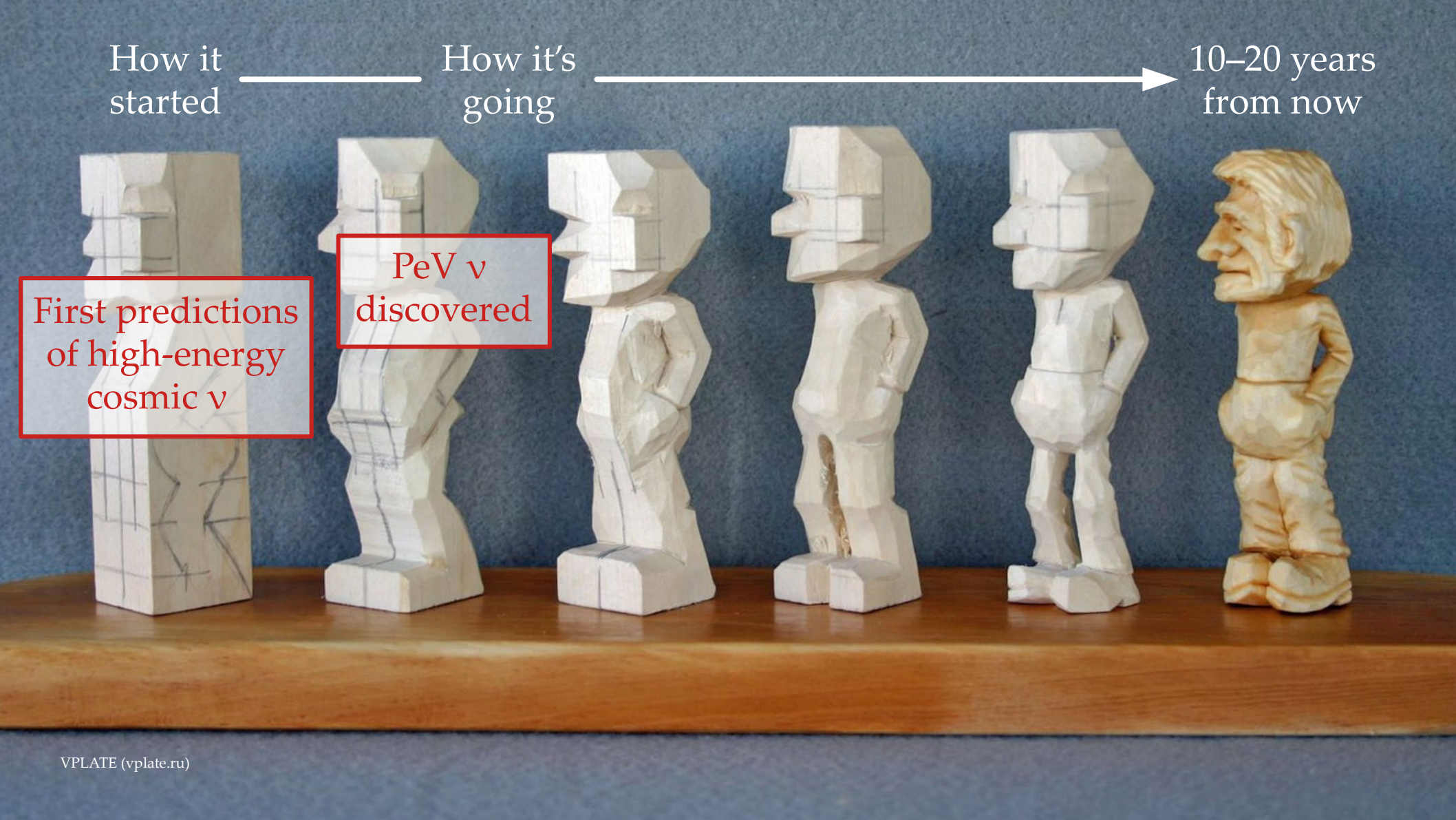
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Hints of sources  
First tests of  $\nu$  physics

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Precision tests with PeV  $\nu$   
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How it started

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10–20 years from now

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How do we get there?

EeV  $\nu$  discovered  
Precision tests with PeV  $\nu$   
First tests with EeV  $\nu$

Thanks!

Backup slides

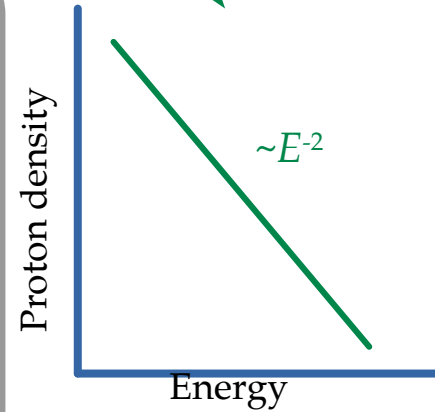
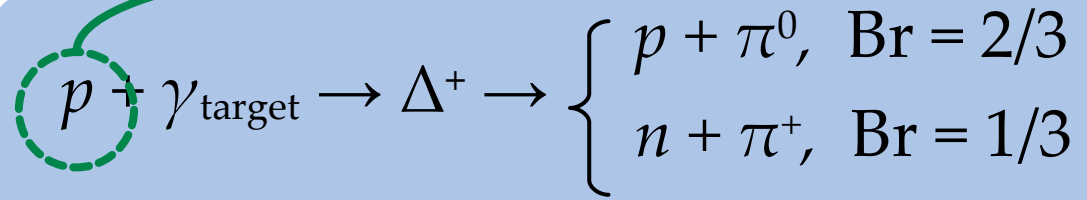
# The multi-messenger connection: a simple picture

(or  $p + p$ )

$$p + \gamma_{\text{target}} \rightarrow \Delta^+ \rightarrow \begin{cases} p + \pi^0, & \text{Br} = 2/3 \\ n + \pi^+, & \text{Br} = 1/3 \end{cases}$$

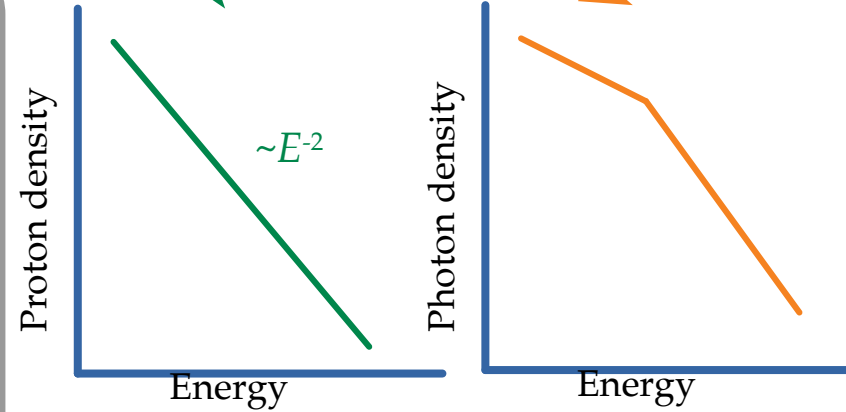
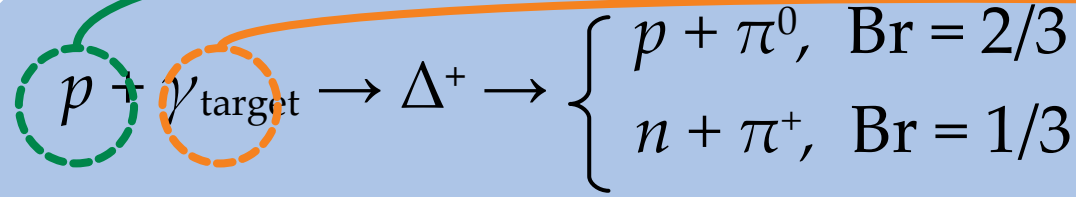
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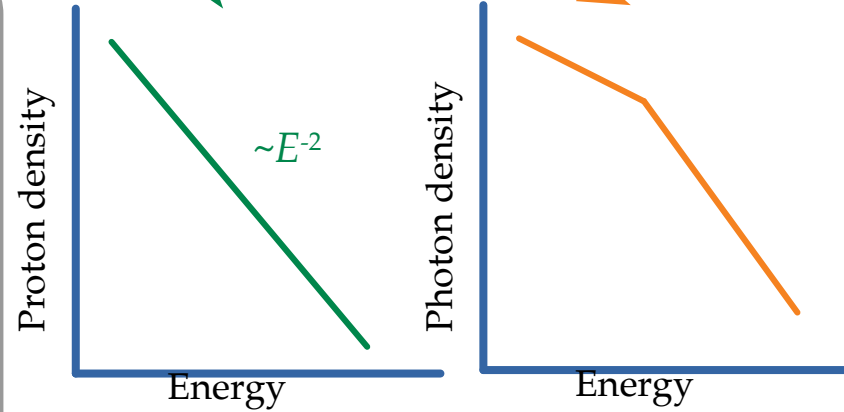
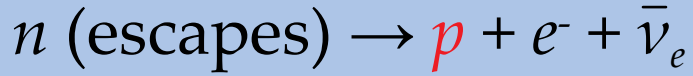
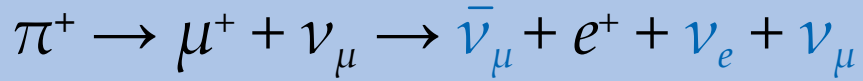
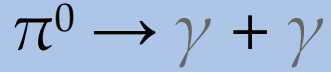
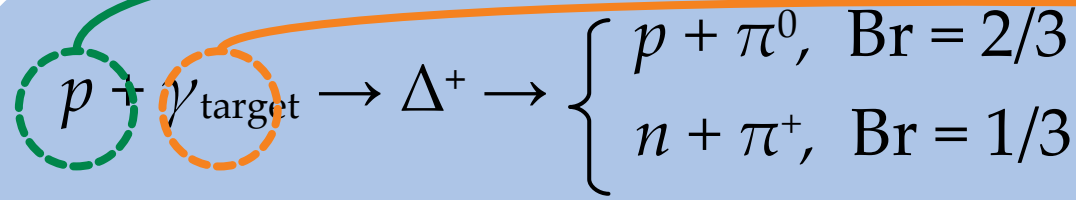
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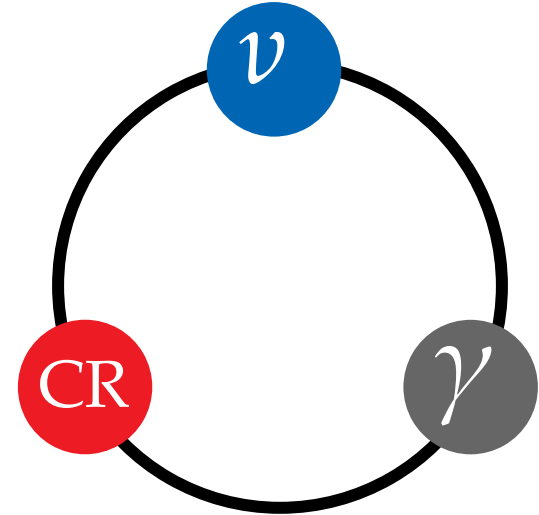
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Neutrino energy = Proton energy / 20

Gamma-ray energy = Proton energy / 10

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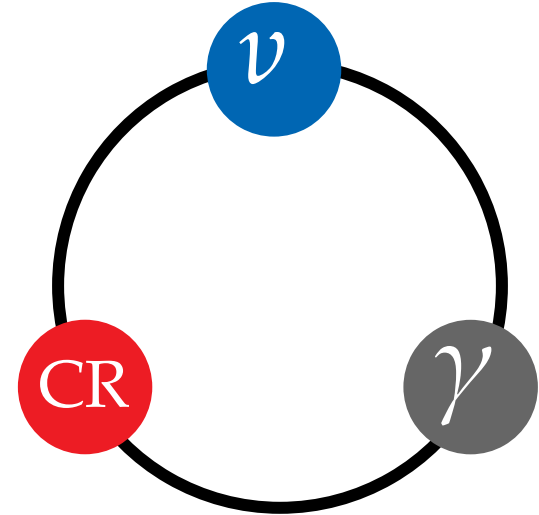
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1 PeV

20 PeV

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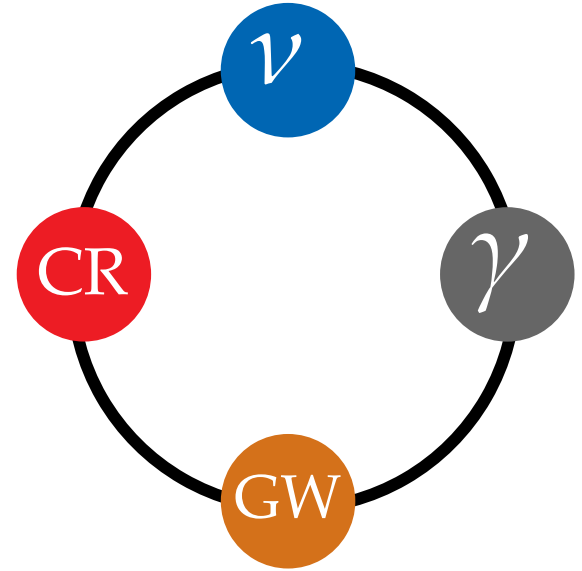
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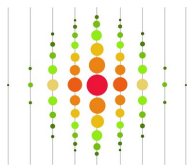
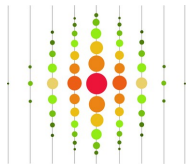
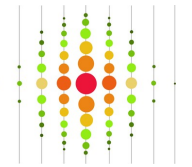
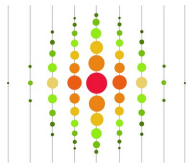

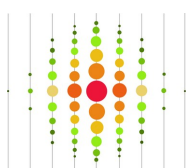
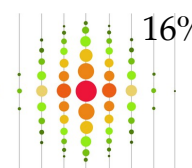
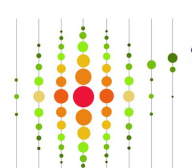
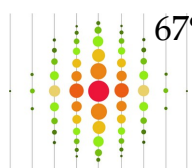
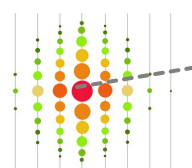


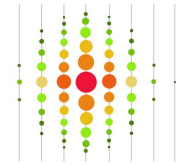
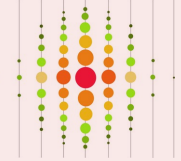
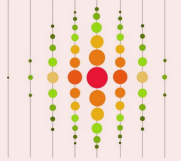

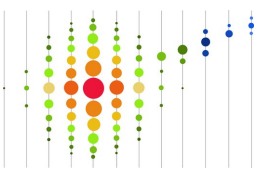

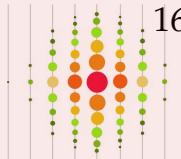
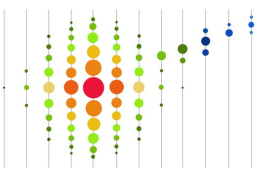

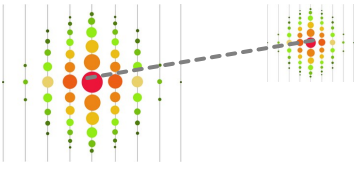
1 PeV

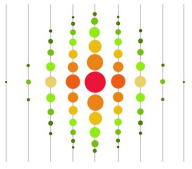
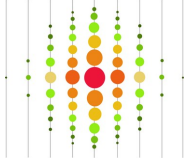
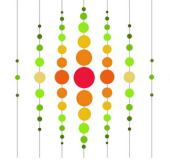
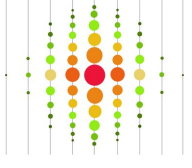
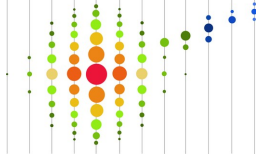
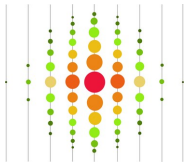
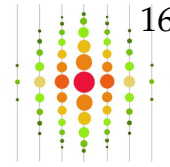

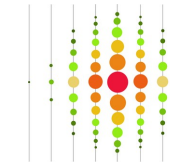
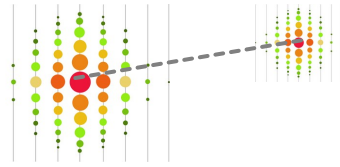
20 PeV

Neutrino energy = Proton energy / 20

Gamma-ray energy = Proton energy / 10

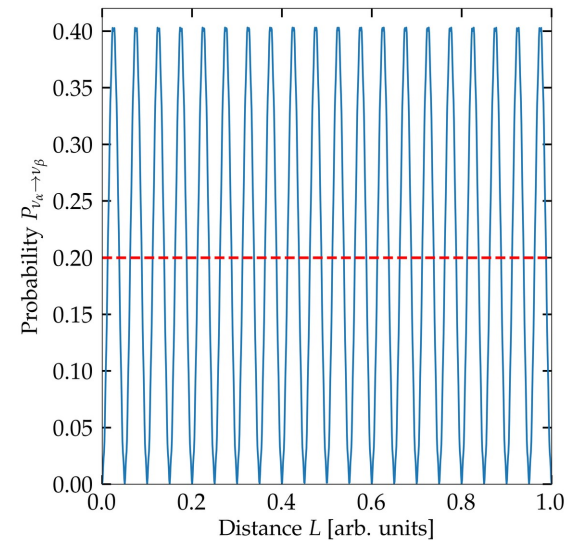
$\nu_x + \bar{\nu}_x$ $\text{NC}$	 <p>Hadronic <math>X</math> shower</p>				
$\nu_e + \bar{\nu}_e$ $\text{CC}$	 <p>Hadronic <math>X</math> shower</p>	+  <p>E.m. shower</p>	<div style="border: 2px solid green; padding: 10px; width: fit-content; margin: auto;"> <math>\nu_\mu</math>: easy to identify the outgoing track         </div>		
$\nu_\mu + \bar{\nu}_\mu$ $\text{CC}$	 <p>Hadronic <math>X</math> shower</p>	+ <div style="border: 2px solid green; border-radius: 15px; padding: 10px; width: fit-content; margin: auto;">  <p>Track</p> </div>			
$\nu_\tau + \bar{\nu}_\tau$ $\text{CC}$	 <p>Hadronic <math>X</math> shower</p>	+  <p>E.m. shower</p>	or  <p>Track</p>	or  <p>Hadronic shower</p>	or  <p>Double pulse/bang</p>

$\nu_x + \bar{\nu}_x$ NC	 <p>Hadronic <math>\chi</math> shower</p>
$\nu_e + \bar{\nu}_e$ CC	<div style="display: flex; align-items: center;"> <div style="border: 2px solid red; padding: 5px; margin-right: 10px;">  <p>Hadronic <math>\chi</math> shower</p> </div> <div style="margin: 0 10px;">+</div> <div style="border: 2px solid red; padding: 5px; margin-right: 10px;">  <p>E.m. shower</p> </div> <div style="border: 2px solid red; padding: 10px; margin-left: 10px;"> <math>\nu_e</math> and <math>\nu_\tau</math>: difficult to distinguish, both make showers         </div> </div>
$\nu_\mu + \bar{\nu}_\mu$ CC	<div style="display: flex; align-items: center;"> <div style="margin-right: 10px;">  <p>Hadronic <math>\chi</math> shower</p> </div> <div style="margin: 0 10px;">+</div> <div style="margin-right: 10px;">  <p>Track</p> </div> </div>
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$\nu_x + \bar{\nu}_x$ NC	 <p>Hadronic <math>\chi</math> shower</p>			
$\nu_e + \bar{\nu}_e$ CC	 <p>Hadronic <math>\chi</math> shower</p>	+  <p>E.m. shower</p>	<div style="border: 2px solid blue; padding: 5px; display: inline-block;">         The occasional track (weakly) breaks the <math>\nu_e / \nu_\tau</math> degeneracy       </div>	
$\nu_\mu + \bar{\nu}_\mu$ CC	 <p>Hadronic <math>\chi</math> shower</p>	+  <p>Track</p>		
$\nu_\tau + \bar{\nu}_\tau$ CC	 <p>Hadronic <math>\chi</math> shower</p>	+  <p>E.m. shower</p>	or <div style="border: 2px solid blue; border-radius: 15px; padding: 5px; display: inline-block;">  <p>Track</p> </div>	or  <p>Hadronic shower</p> or  <p>Double pulse/bang</p>

Full 3ν oscillation probability:

$$P_{\alpha\beta}(E, L) = \delta_{\alpha\beta} - 4 \sum_{i>j} \operatorname{Re}(U_{\alpha i}^* U_{\beta i} U_{\alpha j} U_{\beta j}^*) \sin^2 \left( \frac{\Delta m_{ij}^2 L}{4E} \right) + 2 \sum_{i>j} \operatorname{Im}(U_{\alpha i}^* U_{\beta i} U_{\alpha j} U_{\beta j}^*) \sin \left( \frac{\Delta m_{ij}^2 L}{2E} \right)$$



Oscillation length for 1-TeV  $\nu$ :  $2\pi \times 2E/\Delta m^2 \sim 0.1$  pc

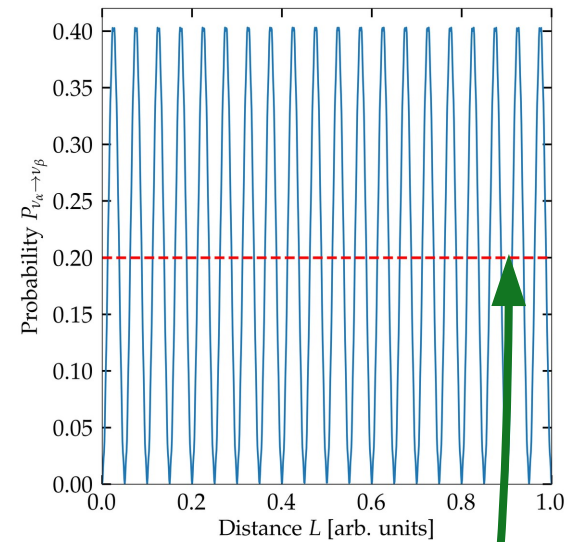
- $\sim 8\%$  of the way to Proxima Centauri
- $\ll$  Distance to Galactic Center (8 kpc)
- $\ll$  Distance to Andromeda (1 Mpc)
- $\ll$  Cosmological distances (few Gpc)

We cannot resolve oscillations, so we use instead the average probability:

$$P_{\alpha\beta} = \sum_{i=1}^3 |U_{\alpha i}|^2 |U_{\beta i}|^2$$

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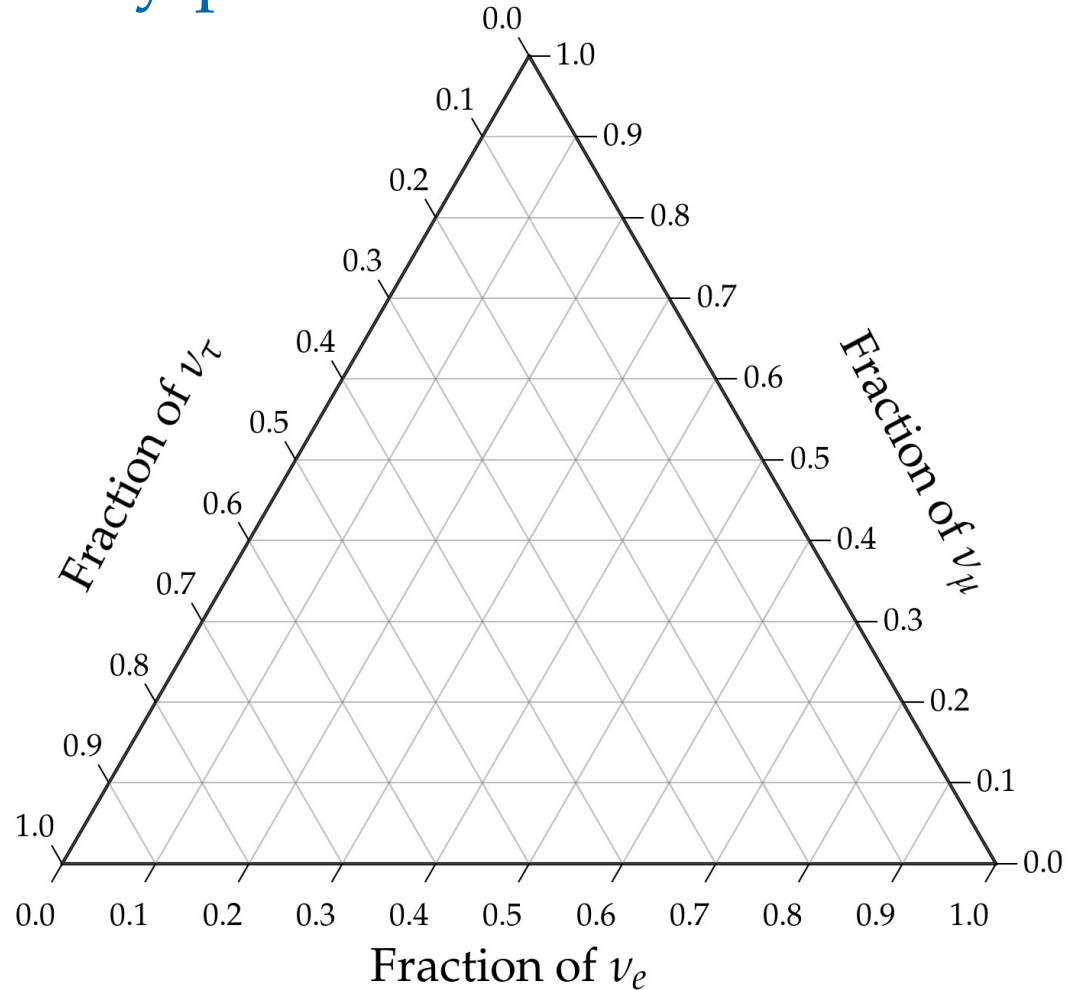
# Quick aside: how to read a ternary plot

Assumes underlying unitarity –  
sum of projections on each axis is 1

How to read it:

Follow the tilt of the tick marks

Always in this order:  $(f_e, f_\mu, f_\tau)$



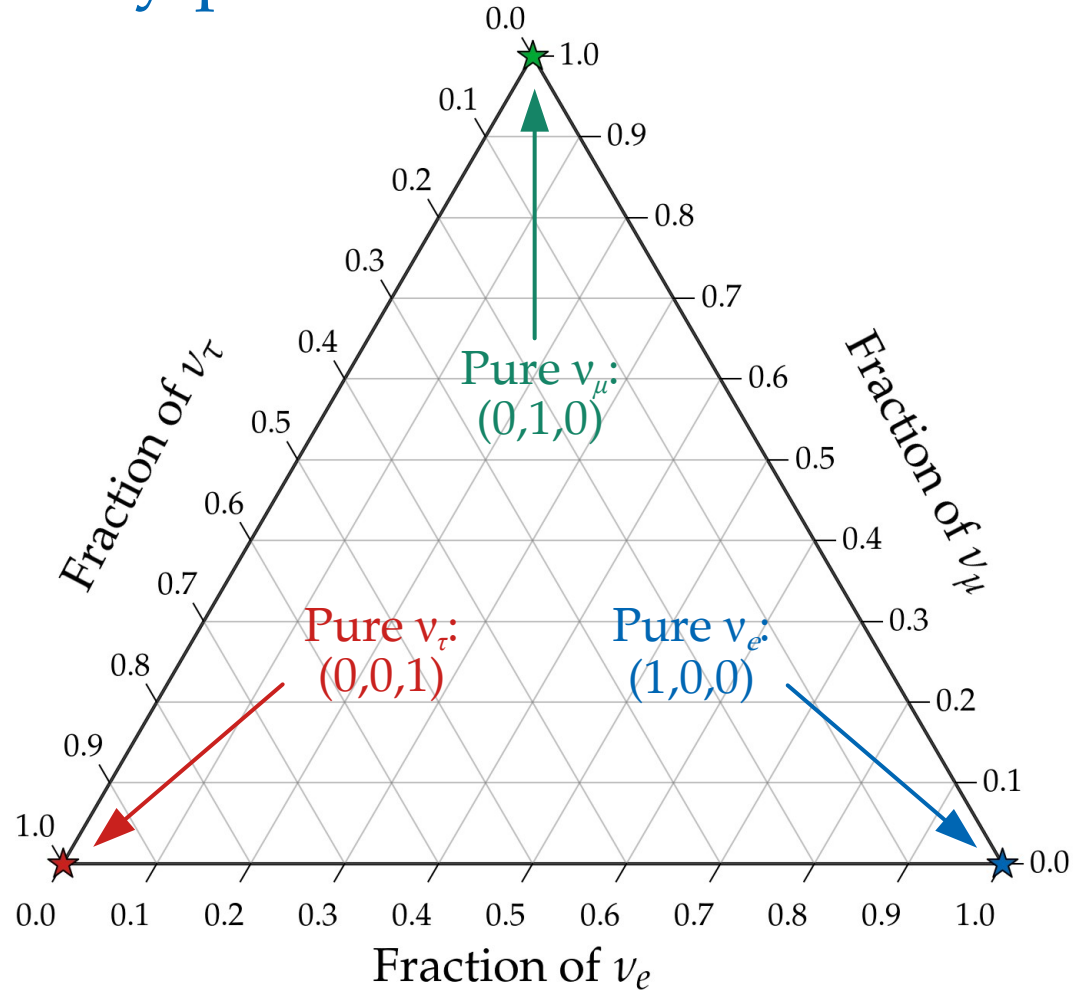
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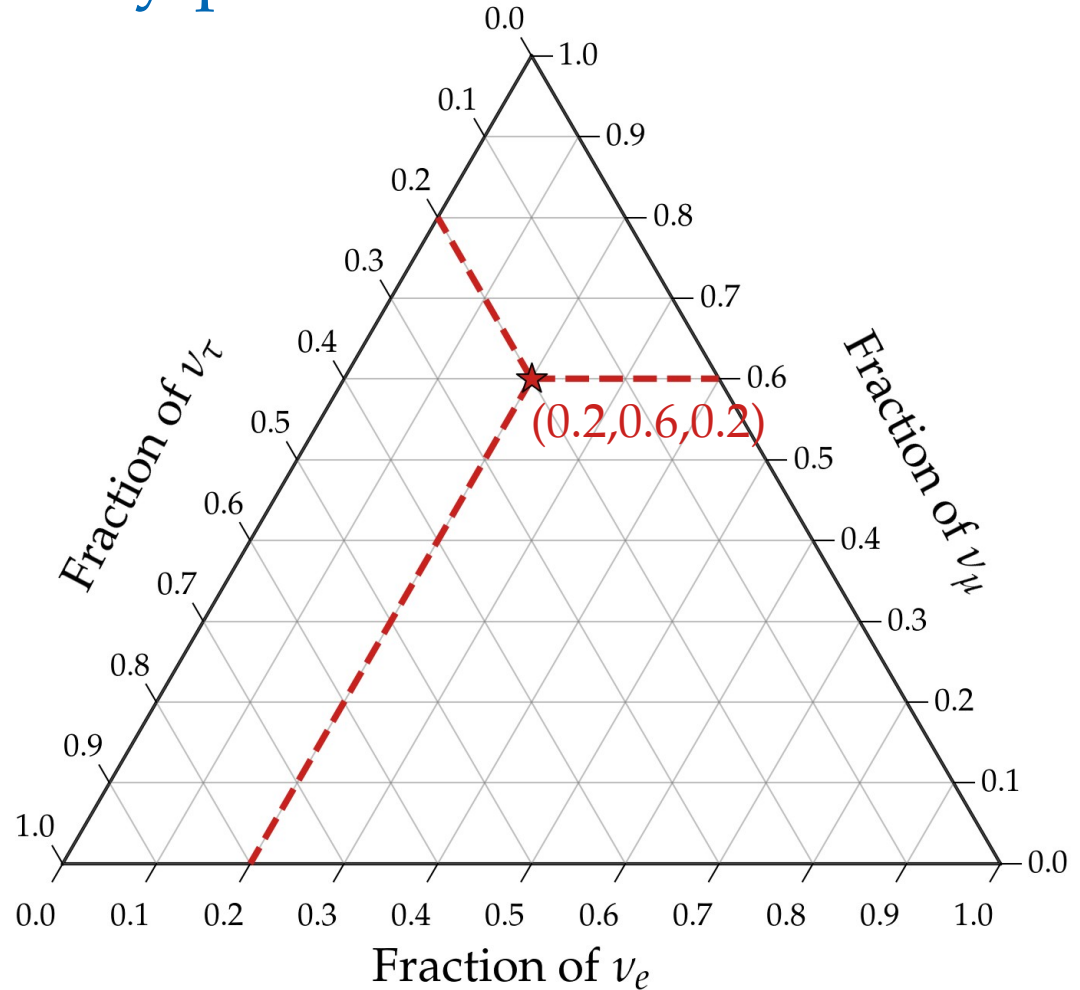
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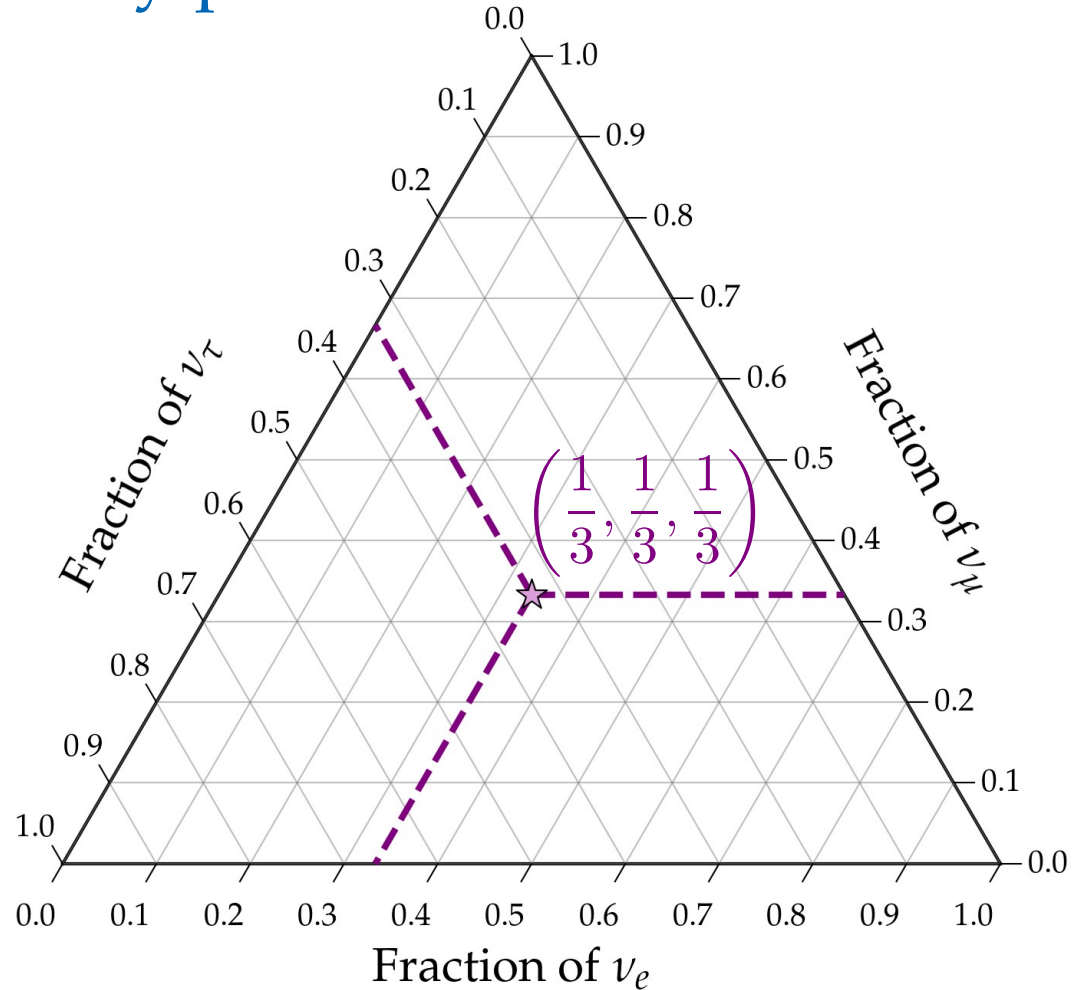
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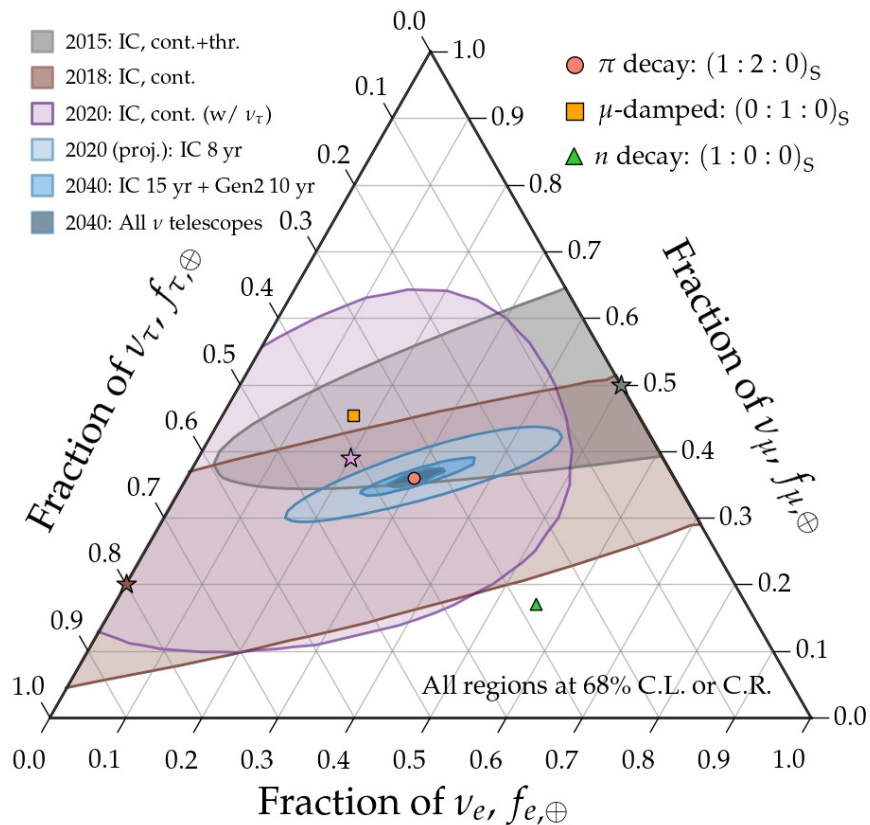
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# Inferring the flavor composition at the sources

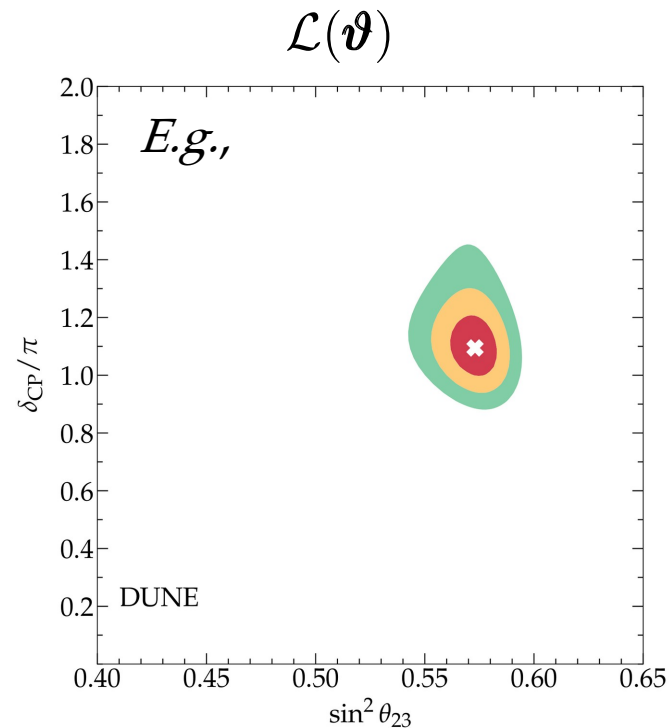
## Ingredient #1:

Flavor ratios measured at Earth,  
 $(f_{e,\oplus}, f_{\mu,\oplus}, f_{\tau,\oplus})$



## Ingredient #2:

Probability density of mixing  
 parameters  $(\theta_{12}, \theta_{23}, \theta_{13}, \delta_{CP})$



# Inferring the flavor composition at the sources

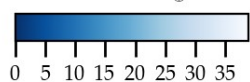
## Ingredient #1:

Flavor ratios measured at Earth,

$$(f_{e,\oplus}, f_{\mu,\oplus}, f_{\tau,\oplus})$$

$$\mathcal{P}_{\text{exp}}(f_{\alpha,\oplus})$$

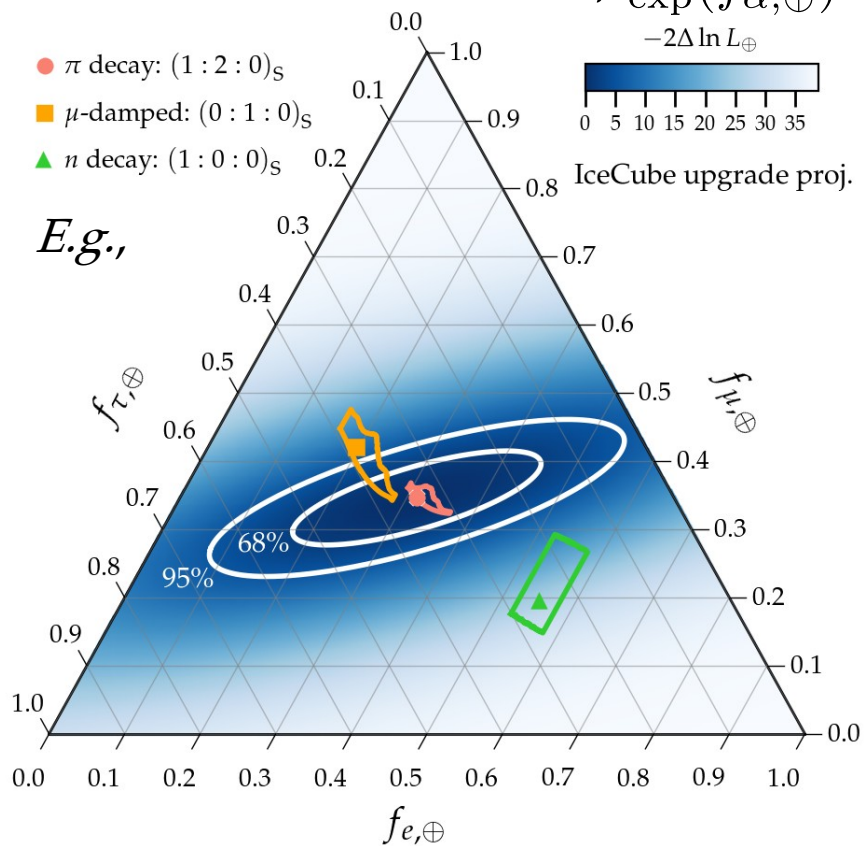
$$-2\Delta \ln L_{\oplus}$$



IceCube upgrade proj.

- $\pi$  decay:  $(1:2:0)_S$
- $\mu$ -damped:  $(0:1:0)_S$
- ▲  $n$  decay:  $(1:0:0)_S$

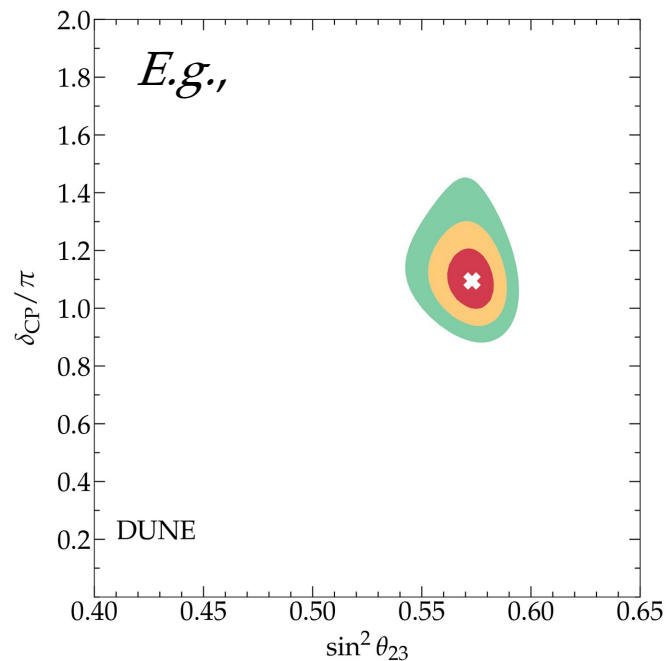
*E.g.,*



## Ingredient #2:

Probability density of mixing parameters  $(\theta_{12}, \theta_{23}, \theta_{13}, \delta_{\text{CP}})$

$$\mathcal{L}(\vartheta)$$



**Standard expectation:**  
Power-law energy spectrum

Energy spectrum

**Standard expectation:**  
Isotropy (for diffuse flux)

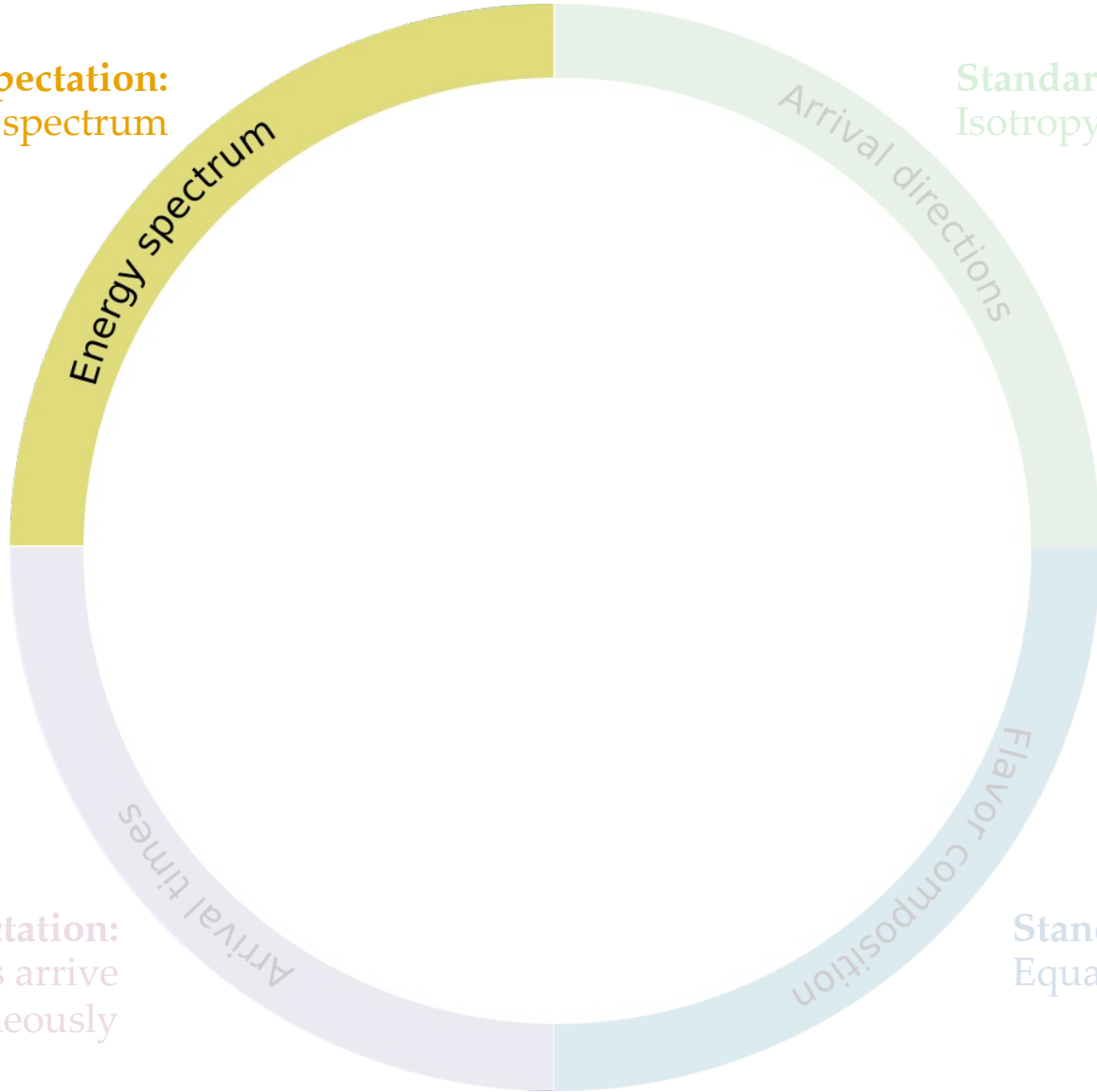
Arrival directions

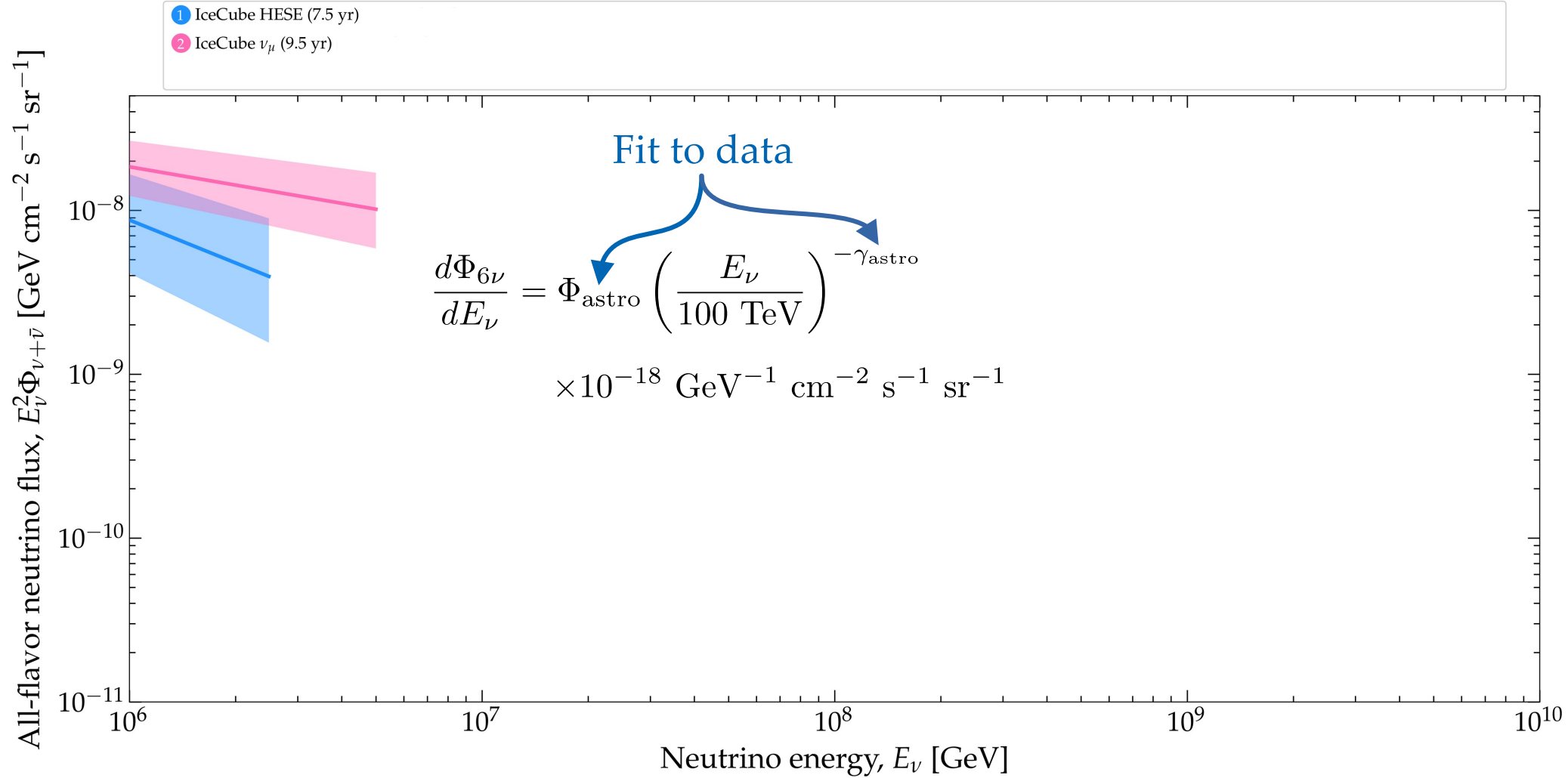
**Standard expectation:**  
Equal number of  $\nu_e$ ,  $\nu_\mu$ ,  $\nu_\tau$

Flavor composition

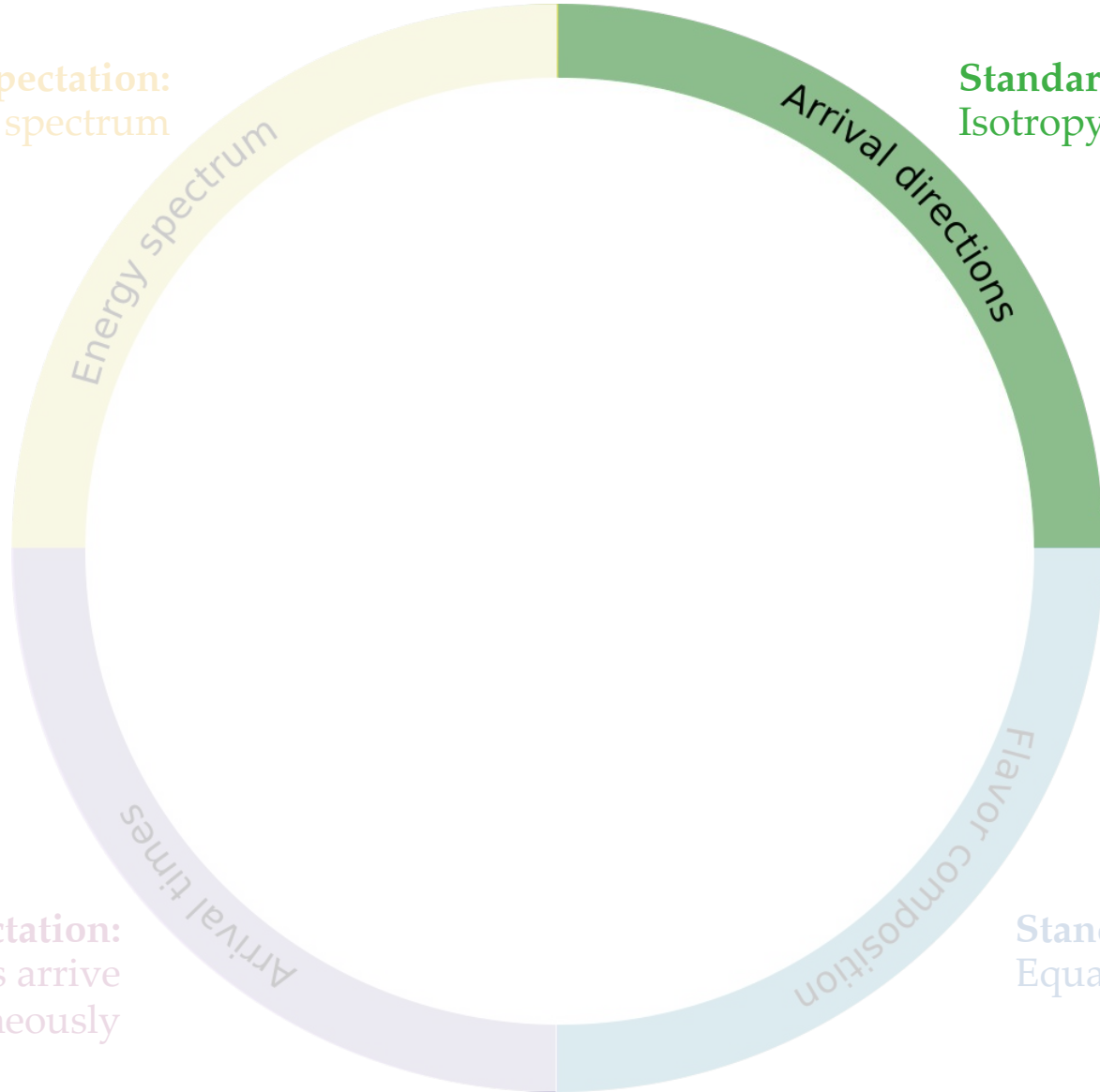
**Standard expectation:**  
 $\nu$  and  $\gamma$  from transients arrive  
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Arrival times





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Power-law energy spectrum



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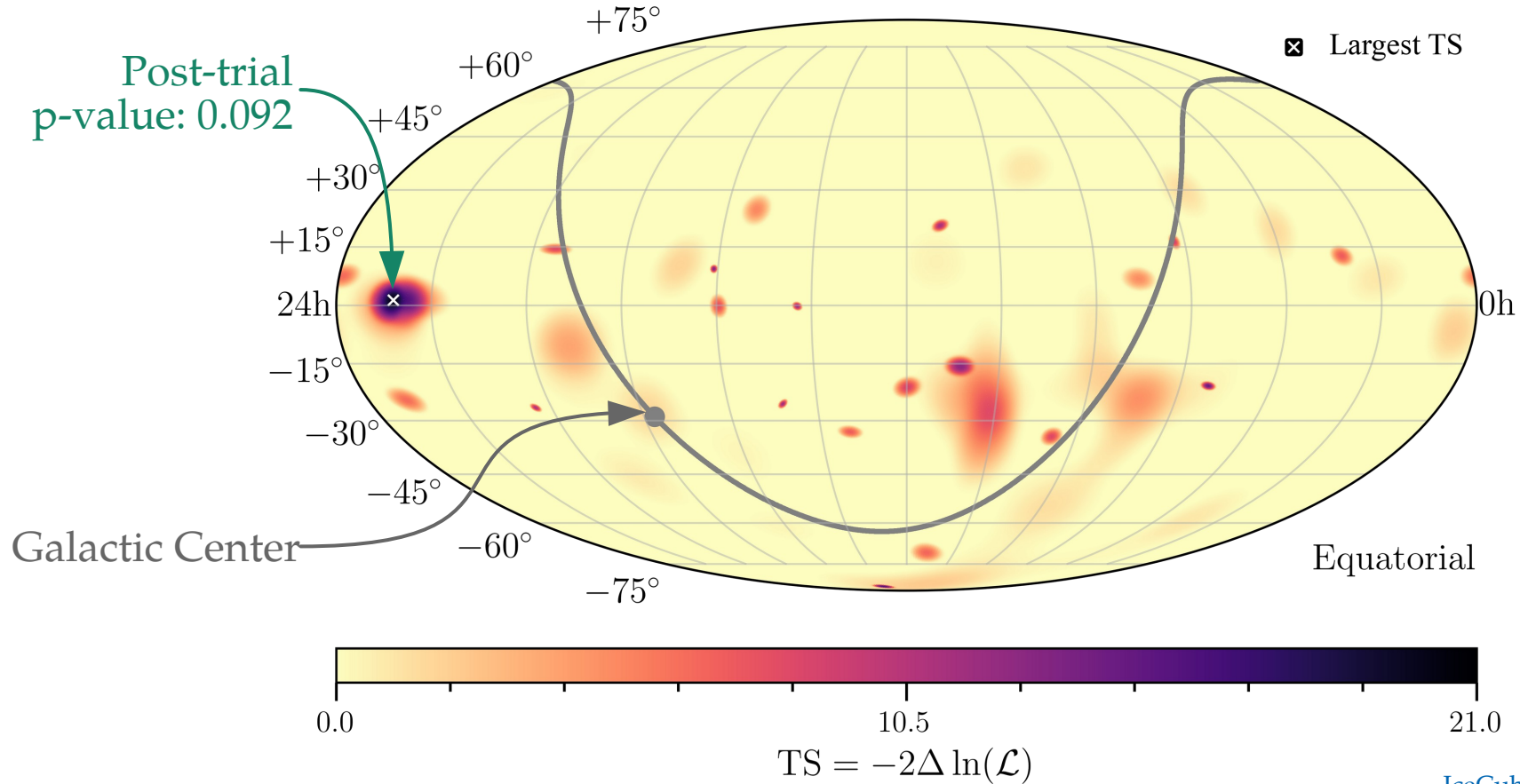
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simultaneously

**Standard expectation:**  
Equal number of  $\nu_e$ ,  $\nu_\mu$ ,  $\nu_\tau$

# Arrival directions (7.5 yr)

No significant excess in the neutrino sky map:



**Standard expectation:**  
Power-law energy spectrum

Energy spectrum

**Standard expectation:**  
Isotropy (for diffuse flux)

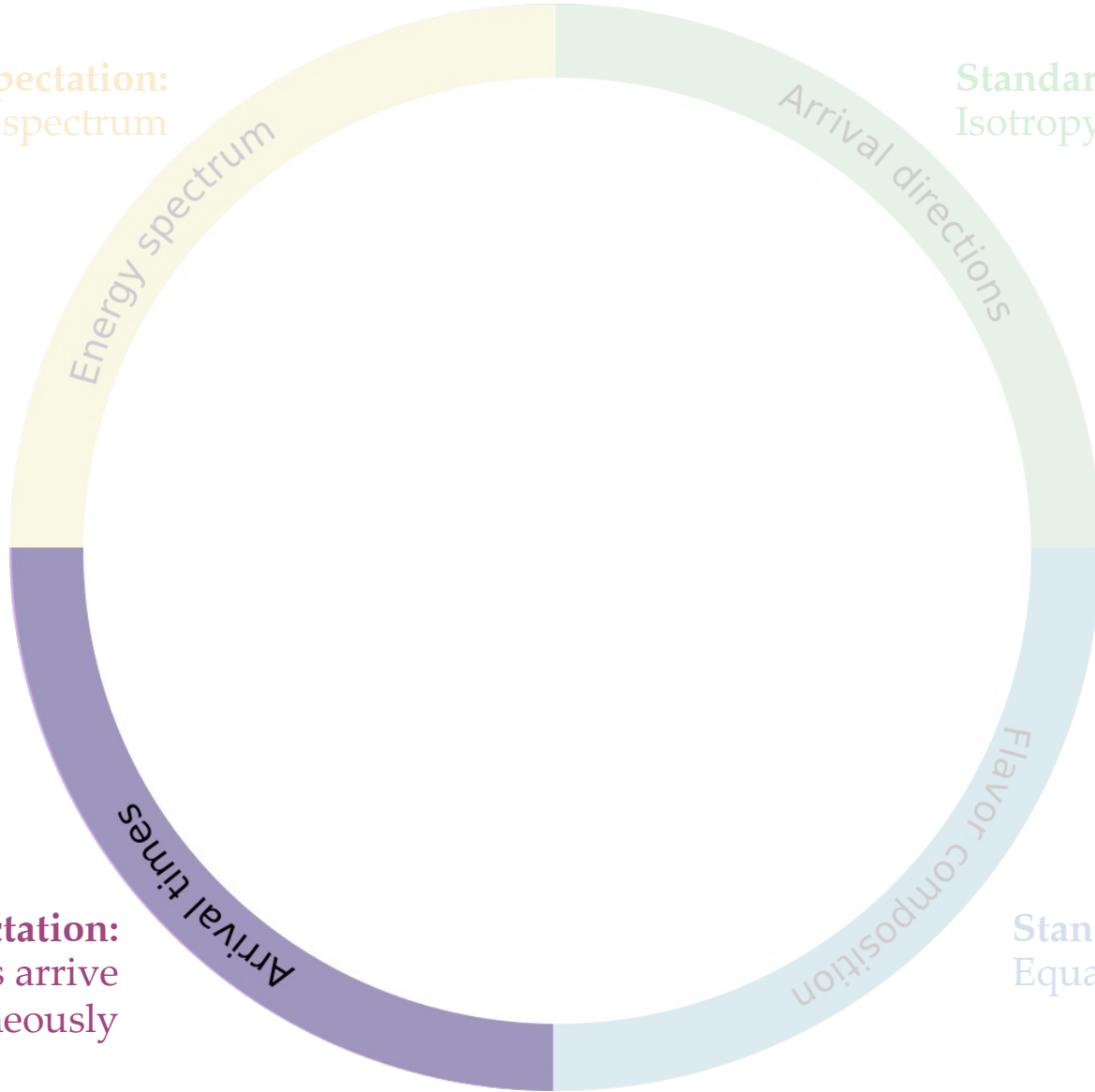
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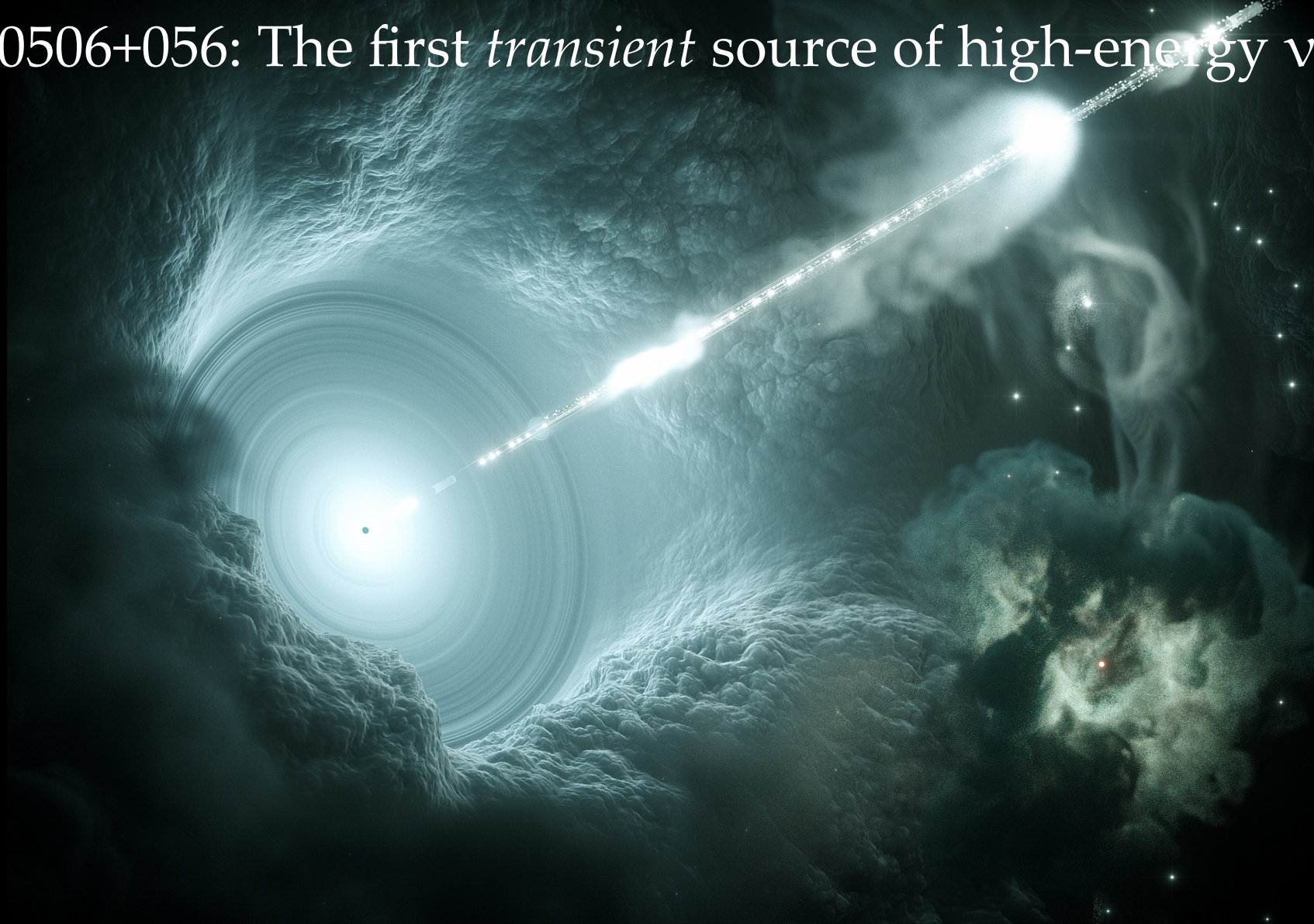
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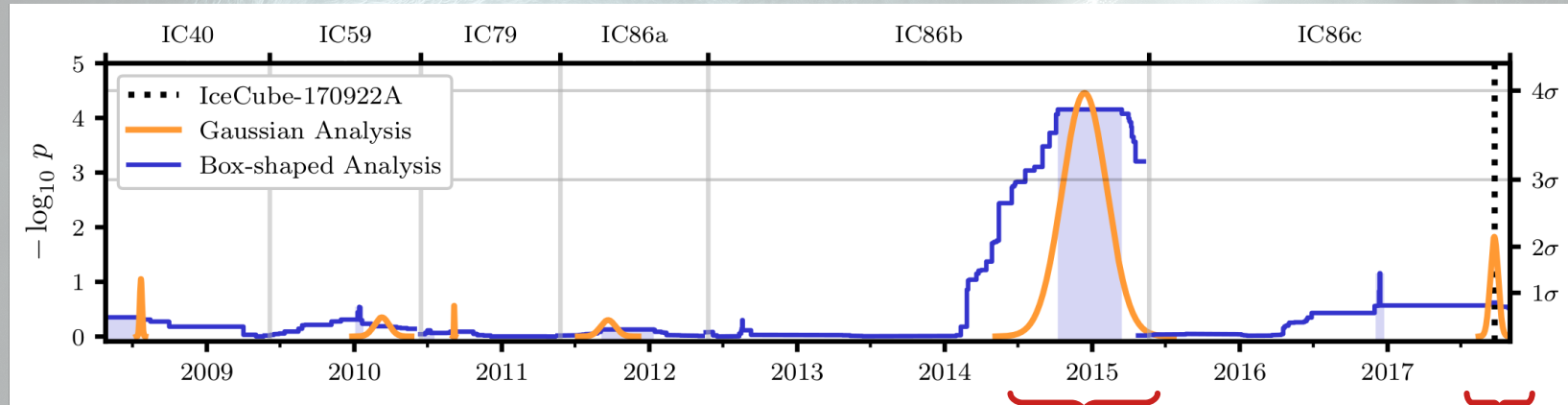
TXS 0506+056: The first *transient* source of high-energy  $\nu$



# TXS 0506+056: The first *transient* source of high-energy $\nu$

## Blazar TXS 0506+056:

IceCube, *Science* 2018



After re-analysis (2101.09836),  
significance dropped  
from  $p=7 \times 10^{-5}$  to  $p=8 \times 10^{-3}$

2014–2015:  $13 \pm 5$   $\nu$  flare, no X-ray flare  
 $3.5\sigma$  significance of correlation (post-trial)

2017: one 290-TeV  $\nu$  + X-ray flare  
 $1.4\sigma$  significance of correlation

Combined (pre-trial):  $4.1\sigma$



# Evidence for BSM

Evidence for BSM

Evidence for SM

$$\text{Bayes factor} = \frac{\text{Evidence for BSM}}{\text{Evidence for SM}}$$

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If  $B \ll 1$ : SM is favored

If  $B \gg 1$ : BSM is favored

If  $B \sim 1$ : No preference

$$\text{Bayes factor} = \frac{\text{Evidence for BSM}}{\text{Evidence for SM}}$$

Bayes factor =  $\frac{\text{Evidence for BSM}}{\text{Evidence for SM}}$

$$\mathcal{Z}_{\text{SM}} = \int \mathcal{L}(\theta_{\text{SM}}, \theta_{\text{astro}}, \theta_{\text{det}}) \pi(\theta_{\text{SM}}, \theta_{\text{astro}}, \theta_{\text{det}}) d\theta_{\text{SM}} d\theta_{\text{astro}} d\theta_{\text{det}}$$

Account for **particle-physics** + **astrophysical** + **detector** uncertainties

Bayes factor =  $\frac{\text{Evidence for BSM}}{\text{Evidence for SM}}$

$$\mathcal{Z}_{\text{SM}} = \int \overbrace{\mathcal{L}(\theta_{\text{SM}}, \theta_{\text{astro}}, \theta_{\text{det}})}^{\text{Likelihood}} \overbrace{\pi(\theta_{\text{SM}}, \theta_{\text{astro}}, \theta_{\text{det}})}^{\text{Prior}} d\theta_{\text{SM}} d\theta_{\text{astro}} d\theta_{\text{det}}$$

Account for **particle-physics** + **astrophysical** + **detector** uncertainties

$$\mathcal{Z}_{\text{BSM}} = \int \mathcal{L}(\theta_{\text{SM}}, \theta_{\text{astro}}, \theta_{\text{det}}, \theta_{\text{BSM}}) \pi(\theta_{\text{SM}}, \theta_{\text{astro}}, \theta_{\text{det}}, \theta_{\text{BSM}}) \times d\theta_{\text{SM}} d\theta_{\text{astro}} d\theta_{\text{det}} d\theta_{\text{BSM}}$$

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Account for **particle-physics** + **astrophysical** + **detector** uncertainties

# Neutrino decay

# Are neutrinos forever?

▶ In the Standard Model (vSM), neutrinos are essentially stable ( $\tau > 10^{36}$  yr):

▶ One-photon decay ( $\nu_i \rightarrow \nu_j + \gamma$ ):  $\tau > 10^{36} (m_i/\text{eV})^{-5}$  yr

▶ Two-photon decay ( $\nu_i \rightarrow \nu_j + \gamma + \gamma$ ):  $\tau > 10^{57} (m_i/\text{eV})^{-9}$  yr

▶ Three-neutrino decay ( $\nu_i \rightarrow \nu_j + \nu_k + \bar{\nu}_k$ ):  $\tau > 10^{55} (m_i/\text{eV})^{-5}$  yr

» Age of Universe  
(~ 14.5 Gyr)

▶ BSM decays may have significantly higher rates:  $\nu_i \rightarrow \nu_j + \varphi$

▶ We work in a model-independent way:

the nature of  $\varphi$  is unimportant if it is invisible to neutrino detectors

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» Age of Universe  
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► BSM decays may have significantly higher rates:  $\nu_i \rightarrow \nu_j + \phi$  — Nambu-Goldstone boson of a broken symmetry

► We work in a model-independent way:

the nature of  $\phi$  is unimportant if it is invisible to neutrino detectors

Astrophysical sources

Earth

$L \sim$  up to a few Gpc



Decay changes the number  
of each  $\nu$  mass eigenstate,  $N_1, N_2, N_3$



The flux of  $\nu_i$  is attenuated by  $\exp[- (L/E) \cdot (m_i/\tau_i)]$

$\underbrace{m_i}_{\text{Mass of } \nu_i} \underbrace{\tau_i}_{\text{Lifetime of } \nu_i}$

Astrophysical sources

Earth

$L \sim$  up to a few Gpc



Decay changes the number  
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Only sensitive to their ratio

The flux of  $\nu_i$  is attenuated by  $\exp[-(L/E) \cdot (m_i/\tau_i)]$

Mass of  $\nu_i$  Lifetime of  $\nu_i$

Astrophysical sources

Earth

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Decay changes the number  
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Lower- $E \nu$  are longer-lived...

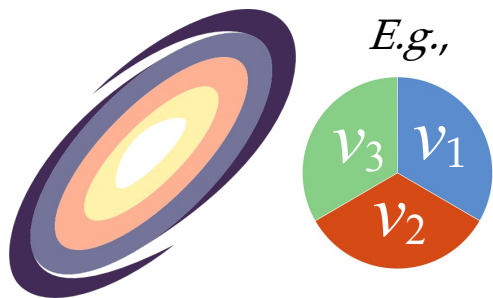
The flux of  $\nu_i$  is attenuated by  $\exp[-(L/E) \cdot (m_i/\tau_i)]$

... but  $\nu$  that travel longer  $L$  are more attenuated!

Astrophysical sources

Earth

$L \sim$  up to a few Gpc



# Astrophysical sources

# Earth

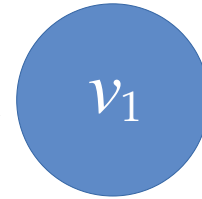
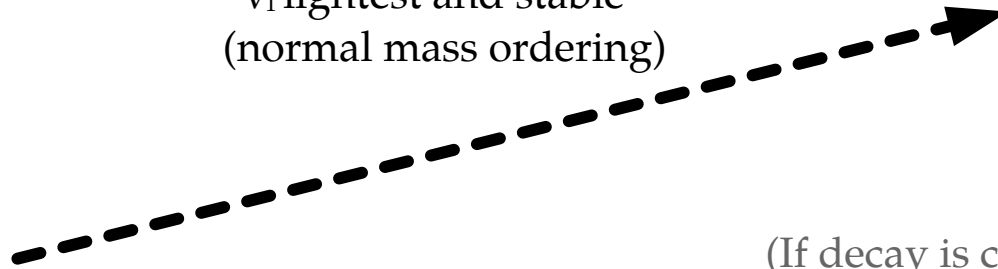
$L \sim$  up to a few Gpc

$$\nu_2, \nu_3 \rightarrow \nu_1$$

$\nu_1$  lightest and stable  
(normal mass ordering)



*E.g.,*



(If decay is complete)



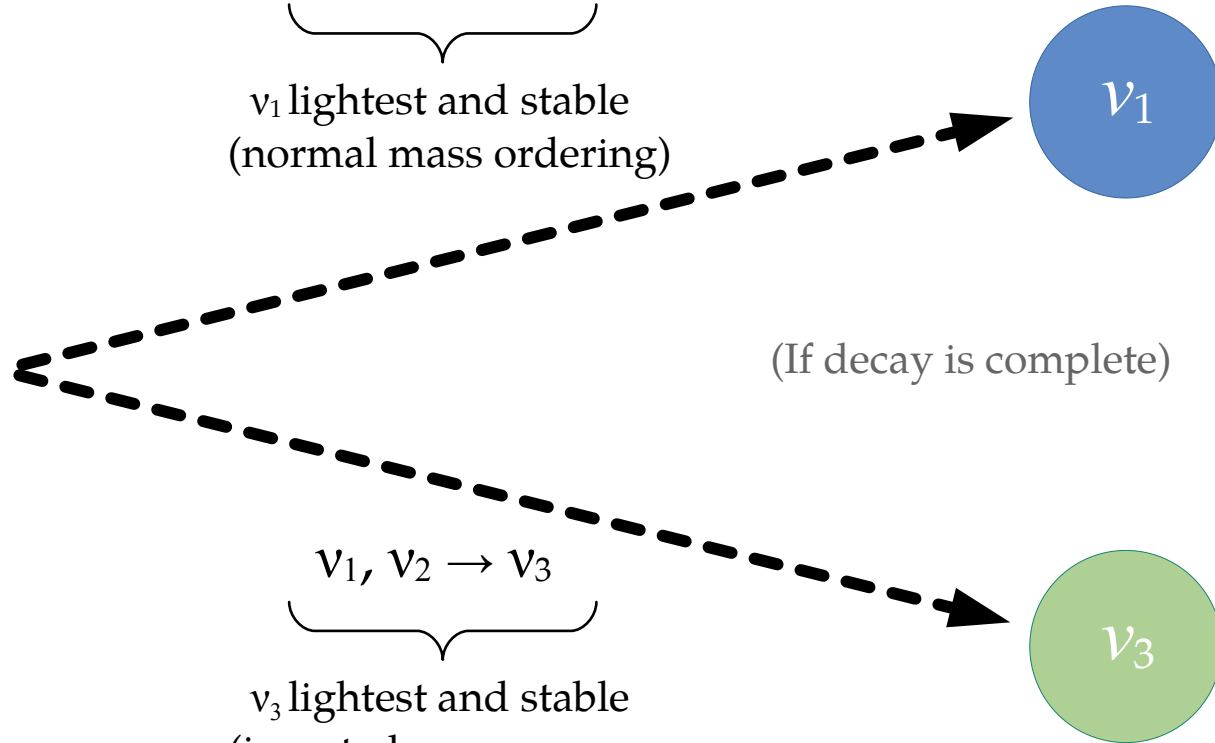
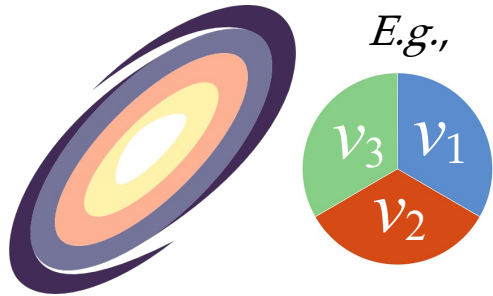
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# Earth

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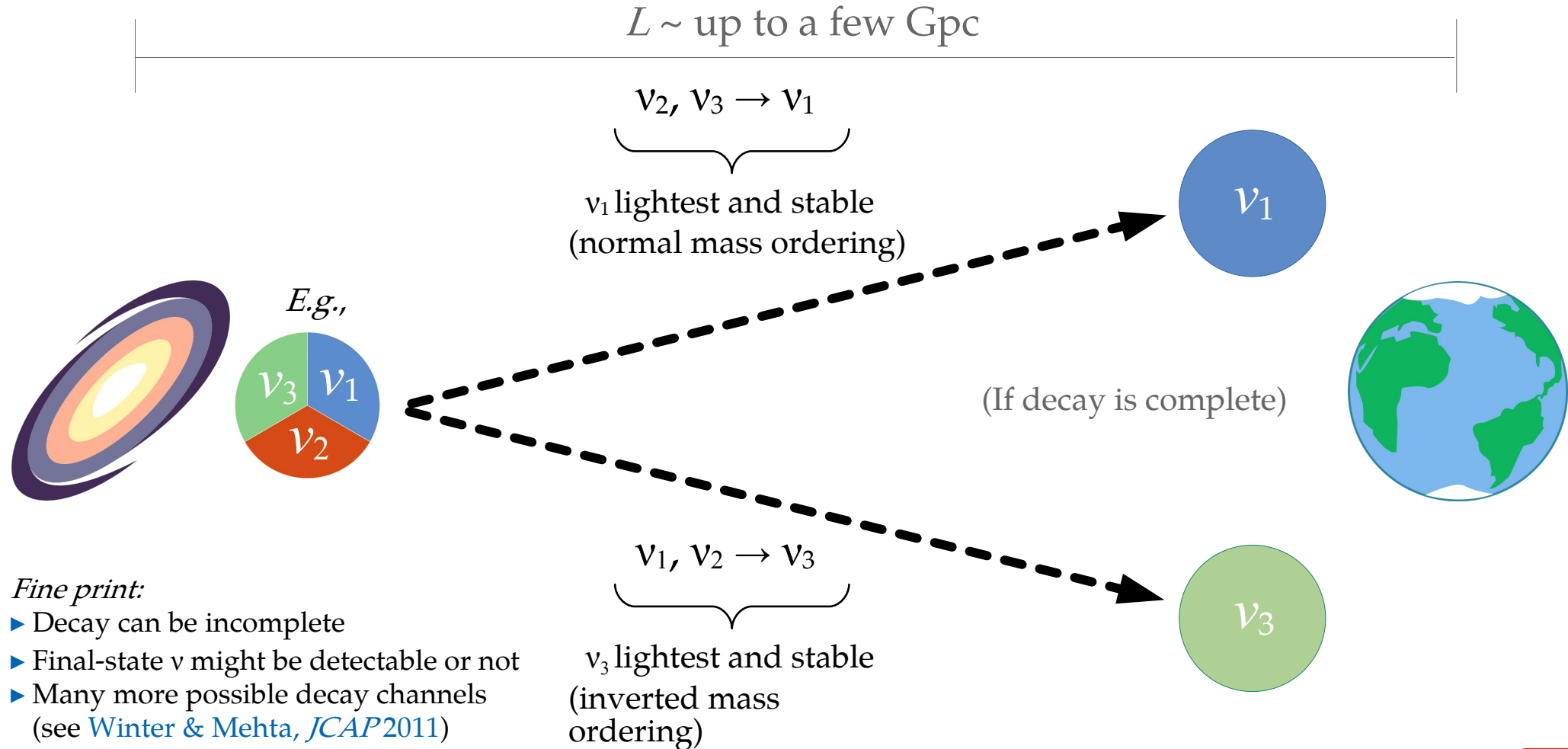
$$\nu_1, \nu_2 \rightarrow \nu_3$$

$\nu_3$  lightest and stable  
(inverted mass ordering)



# Astrophysical sources

Earth



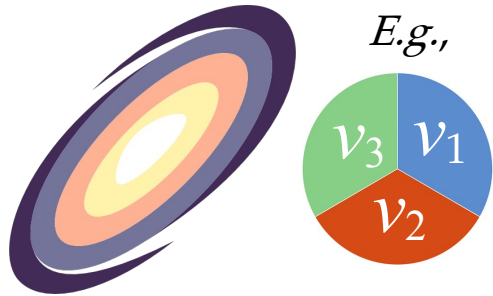
# Astrophysical sources

Earth

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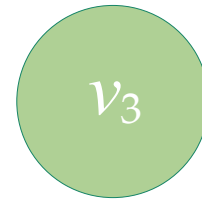
$\nu_1$  lightest and stable  
(normal mass ordering)



What does decay change?

$$\nu_1, \nu_2 \rightarrow \nu_3$$

$\nu_3$  lightest and stable  
(inverted mass ordering)

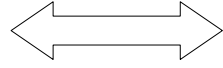


### Fine print:

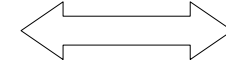
- ▶ Decay can be incomplete
- ▶ Final-state  $\nu$  might be detectable or not
- ▶ Many more possible decay channels (see Winter & Mehta, JCAP2011)

# What does neutrino decay change?

Flavor composition



Spectrum shape

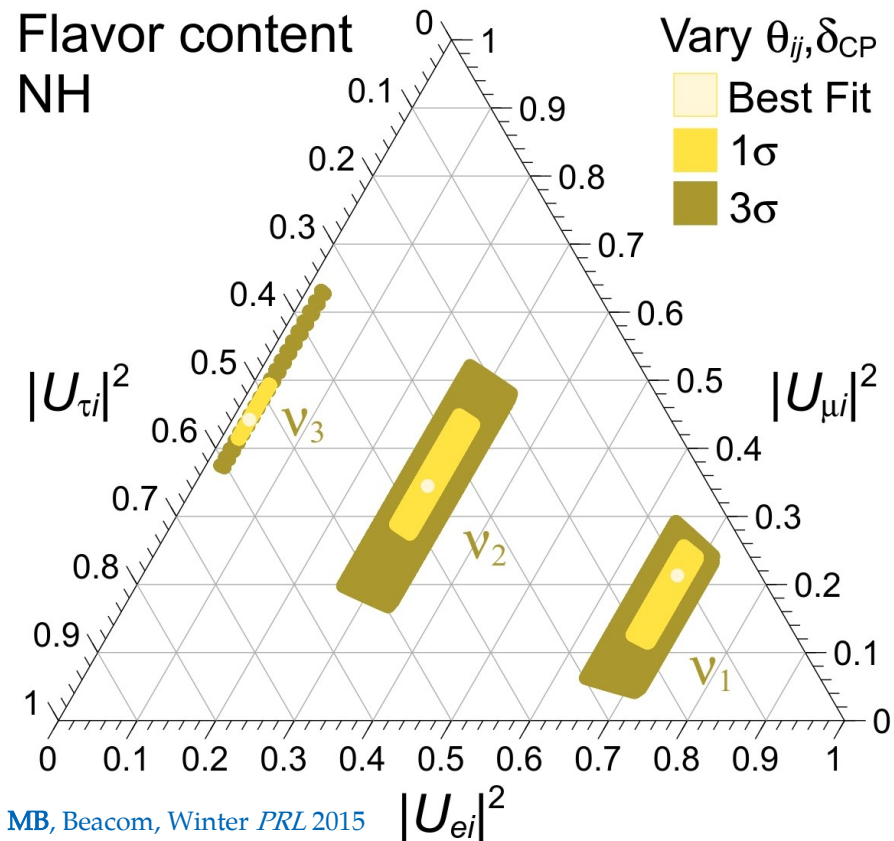
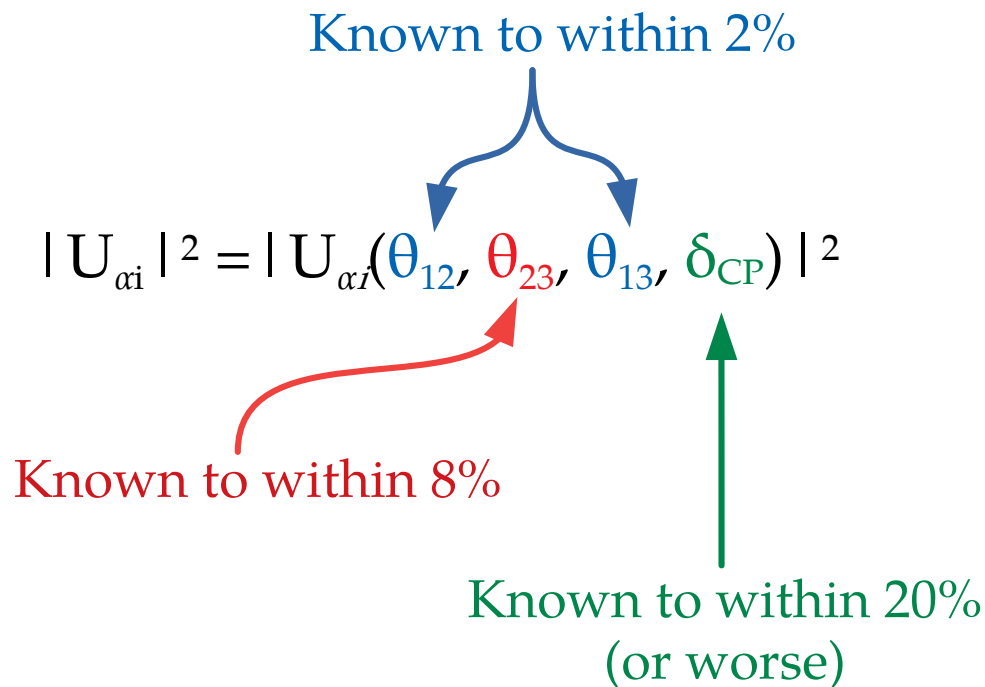


Event rate

# What does neutrino decay change?

Flavor composition  $\longleftrightarrow$  Spectrum shape  $\longleftrightarrow$  Event rate

Flavor content of mass eigenstates:



# What does neutrino decay change?

Flavor composition



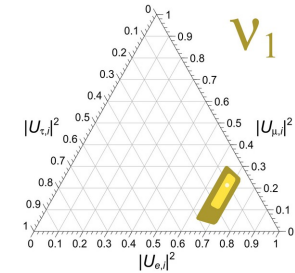
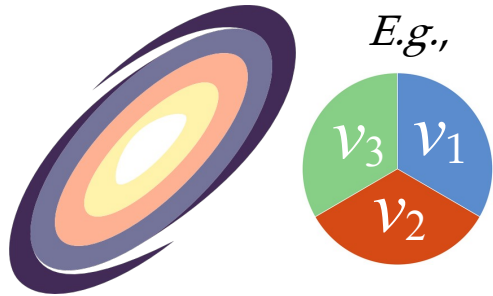
Spectrum shape



Event rate

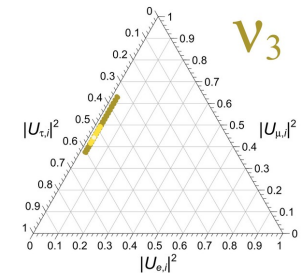
$$\nu_2, \nu_3 \rightarrow \nu_1$$

$\nu_1$  lightest and stable  
(normal mass ordering)



$$\nu_1, \nu_2 \rightarrow \nu_3$$

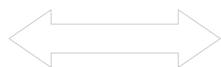
$\nu_3$  lightest and stable  
(inverted mass ordering)



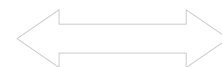
# What does neutrino decay change?

See also: Beacom *et al.*, *PRL* 2002 / Baerwald, MB, Winter, *JCAP* 2012 / MB, Beacom, Murase, *PRD* 2017 / Rasmussen *et al.*, *PRD* 2017 / Denton & Tamborra, *PRL* 2018 / Abdullahi & Denton, *PRD* 2020 / MB, 2004.06844

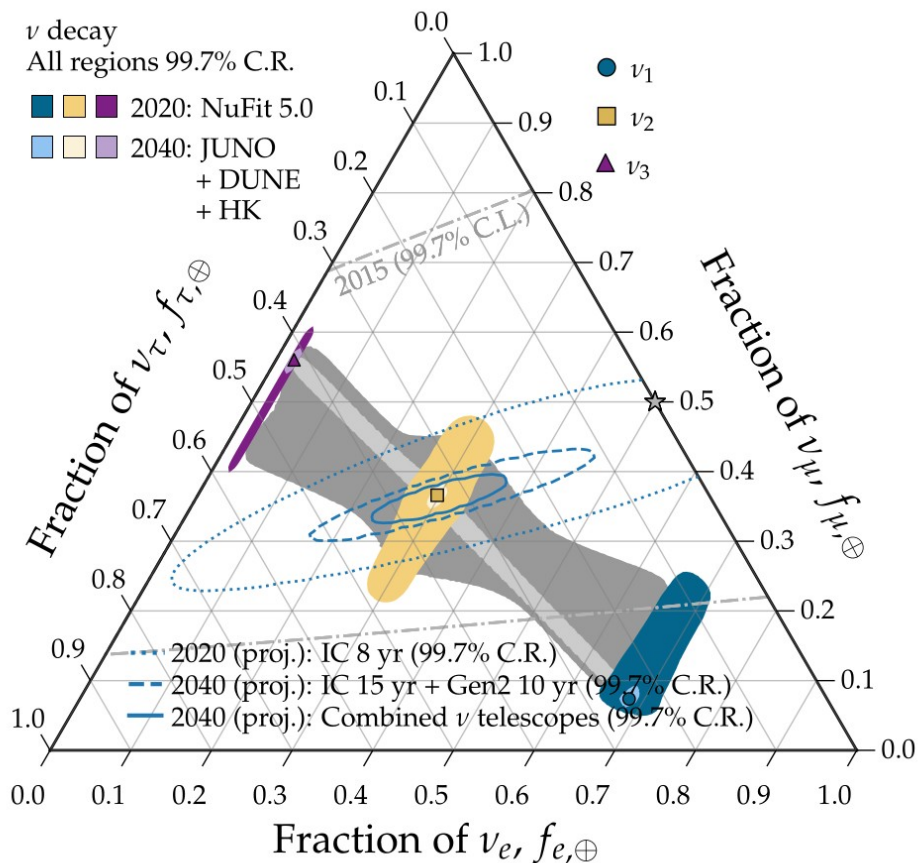
Flavor composition



Spectrum shape



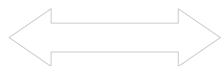
Event rate



# What does neutrino decay change?

See also: Beacom *et al.*, *PRL* 2002 / Baerwald, MB, Winter, *JCAP* 2012 / MB, Beacom, Murase, *PRD* 2017 / Rasmussen *et al.*, *PRD* 2017 / Denton & Tamborra, *PRL* 2018 / Abdullahi & Denton, *PRD* 2020 / MB, 2004.06844

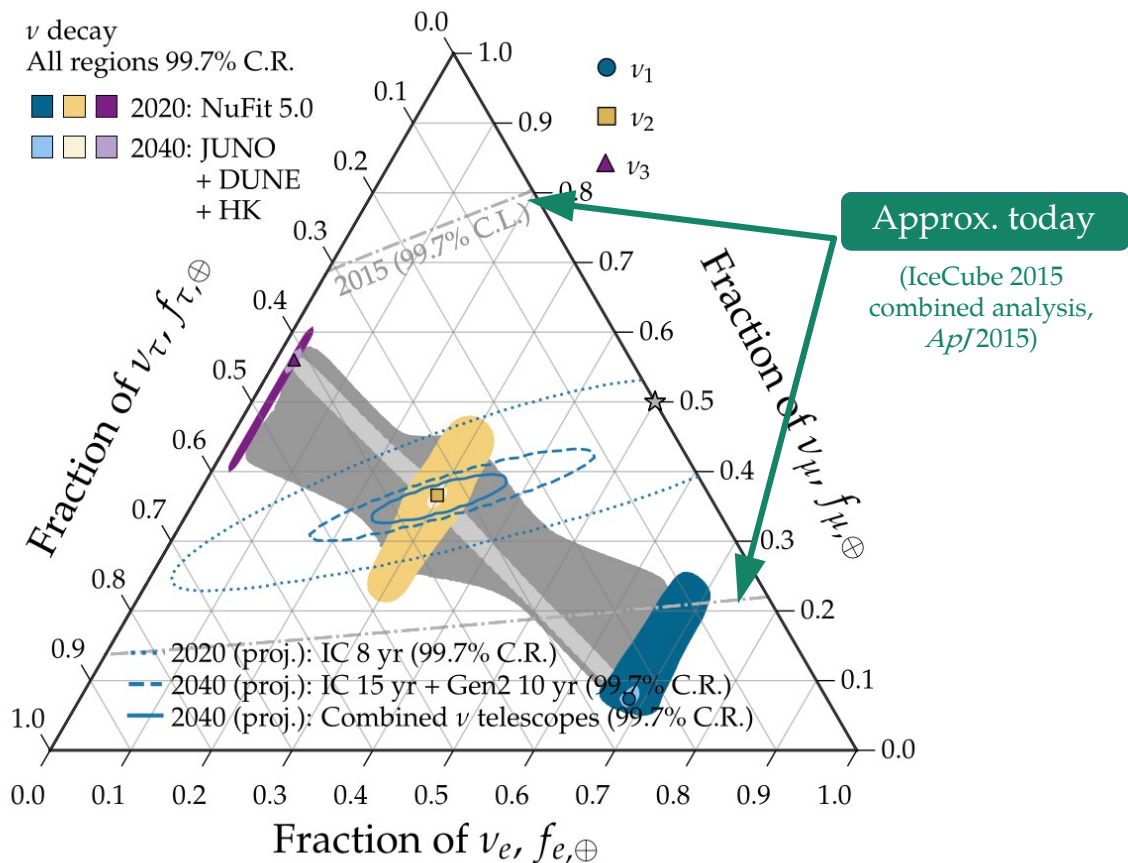
Flavor composition



Spectrum shape



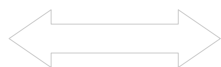
Event rate



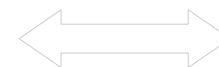
# What does neutrino decay change?

See also: Beacom *et al.*, *PRL* 2002 / Baerwald, MB, Winter, *JCAP* 2012 / MB, Beacom, Murase, *PRD* 2017 / Rasmussen *et al.*, *PRD* 2017 / Denton & Tamborra, *PRL* 2018 / Abdullahi & Denton, *PRD* 2020 / MB, 2004.06844

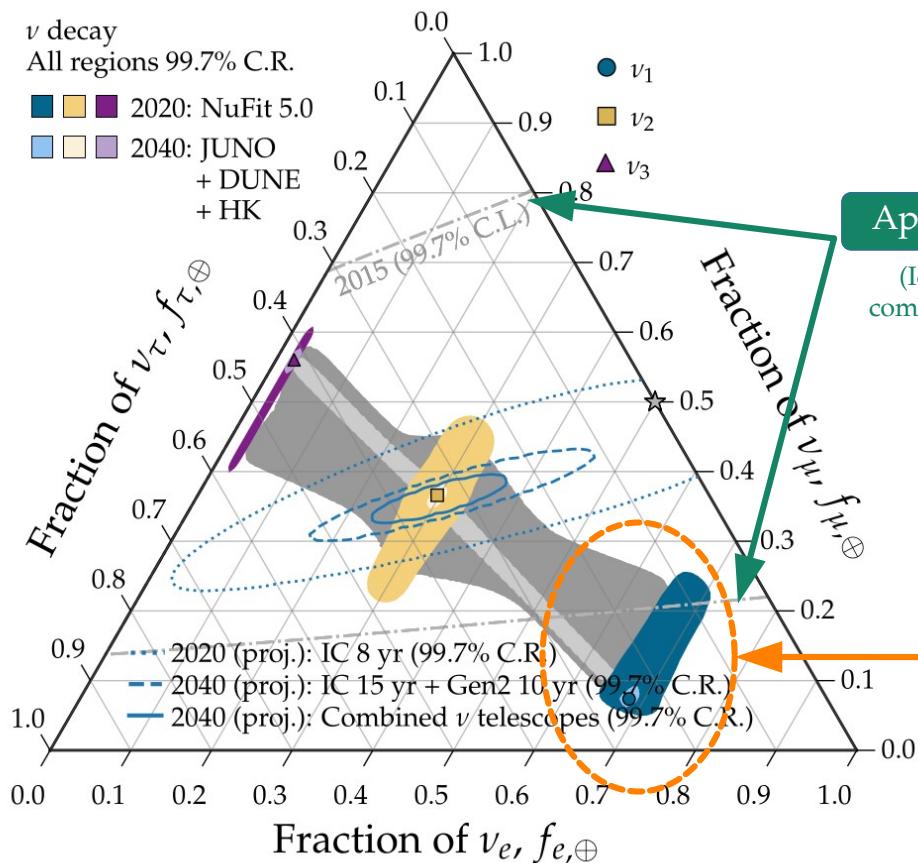
Flavor composition



Spectrum shape



Event rate

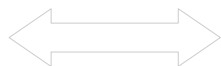


Complete decay into  $\nu_1$  disfavored by 2015 IceCube flavor measurement

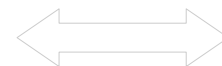
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See also: Beacom *et al.*, *PRL* 2002 / Baerwald, MB, Winter, *JCAP* 2012 / MB, Beacom, Murase, *PRD* 2017 / Rasmussen *et al.*, *PRD* 2017 / Denton & Tamborra, *PRL* 2018 / Abdullahi & Denton, *PRD* 2020 / MB, 2004.06844

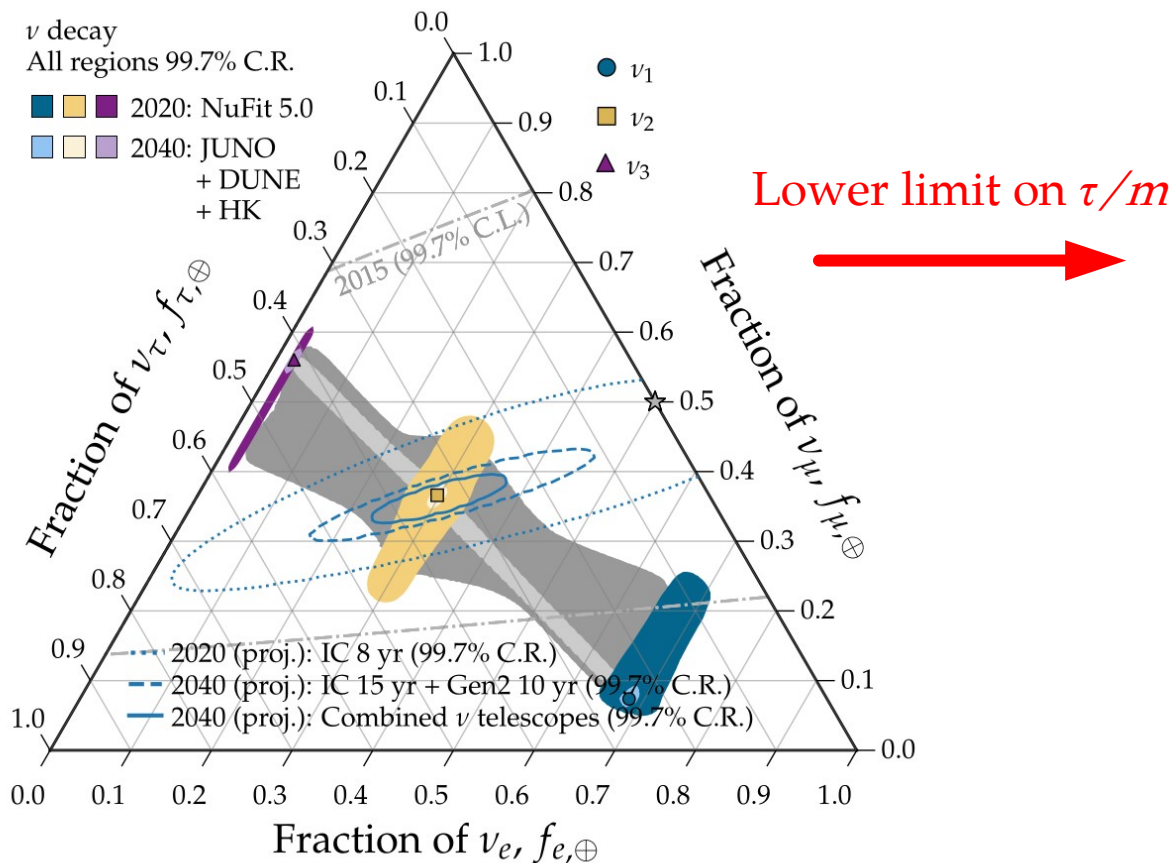
Flavor composition



Spectrum shape



Event rate



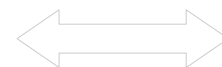
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See also: Beacom *et al.*, *PRL* 2002 / Baerwald, MB, Winter, *JCAP* 2012 / MB, Beacom, Murase, *PRD* 2017 / Rasmussen *et al.*, *PRD* 2017 / Denton & Tamborra, *PRL* 2018 / Abdullahi & Denton, *PRD* 2020 / MB, 2004.06844

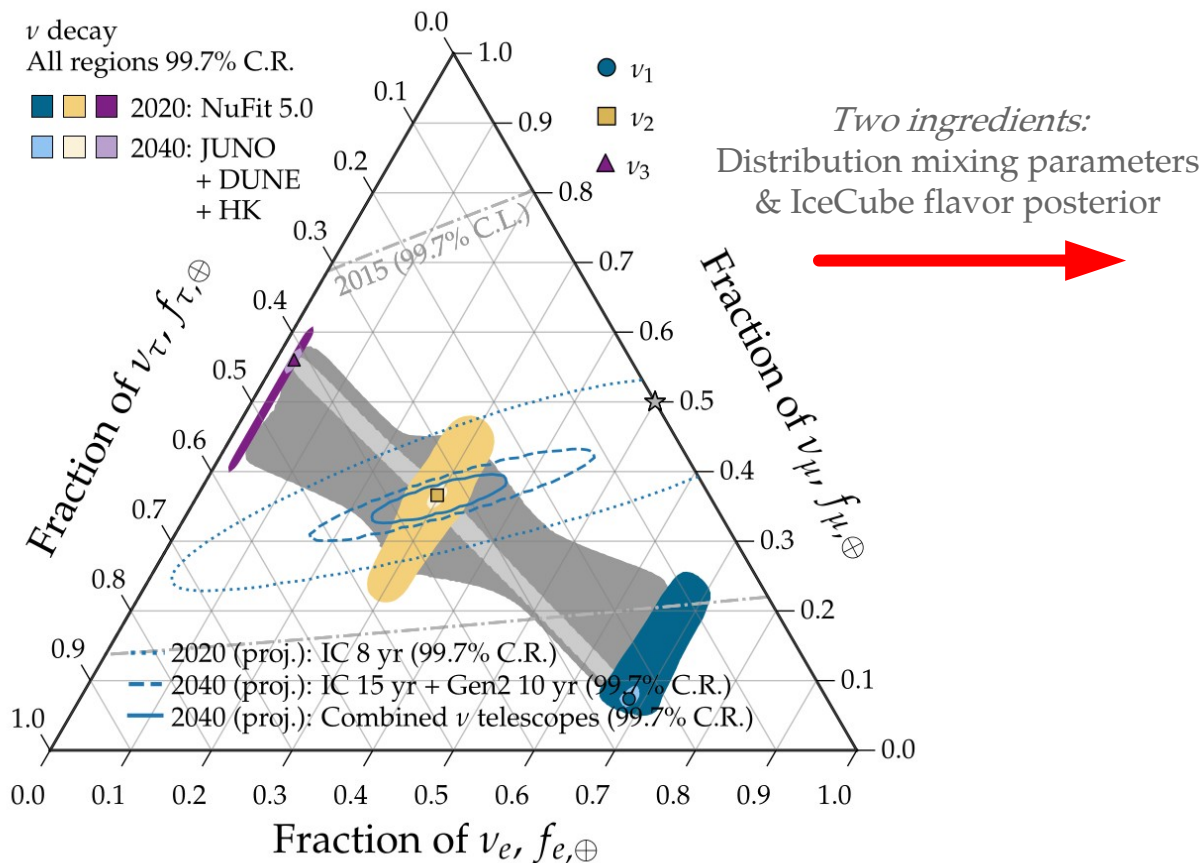
Flavor composition



Spectrum shape



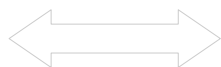
Event rate



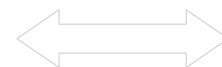
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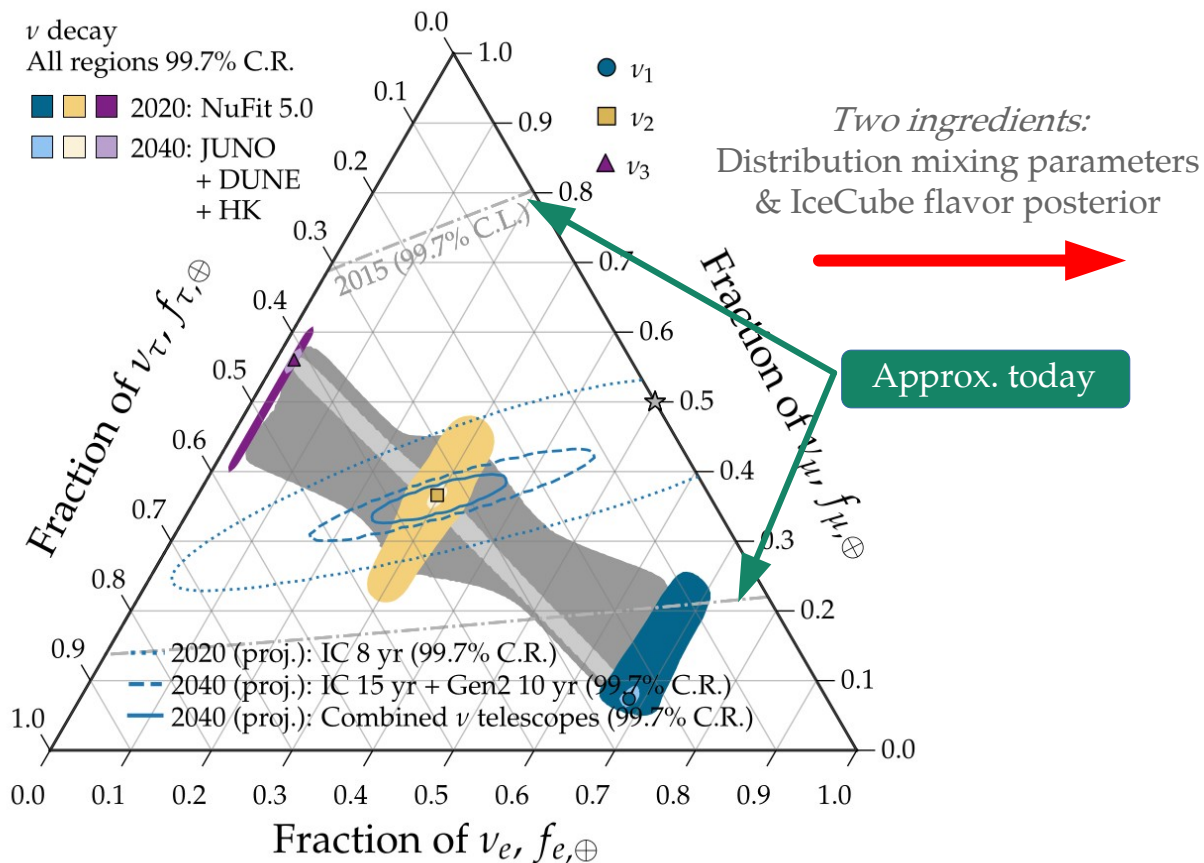
Flavor composition



Spectrum shape



Event rate



# What does neutrino decay change?

See also: Beacom *et al.*, *PRL* 2002 / Baerwald, **MB**, Winter, *JCAP*2012 / **MB**, Beacom, Murase, *PRD*2017 / Rasmussen *et al.*, *PRD*2017 / Denton & Tamborra, *PRL* 2018 / Abdullahi & Denton, *PRD*2020 / **MB**, 2004.06844

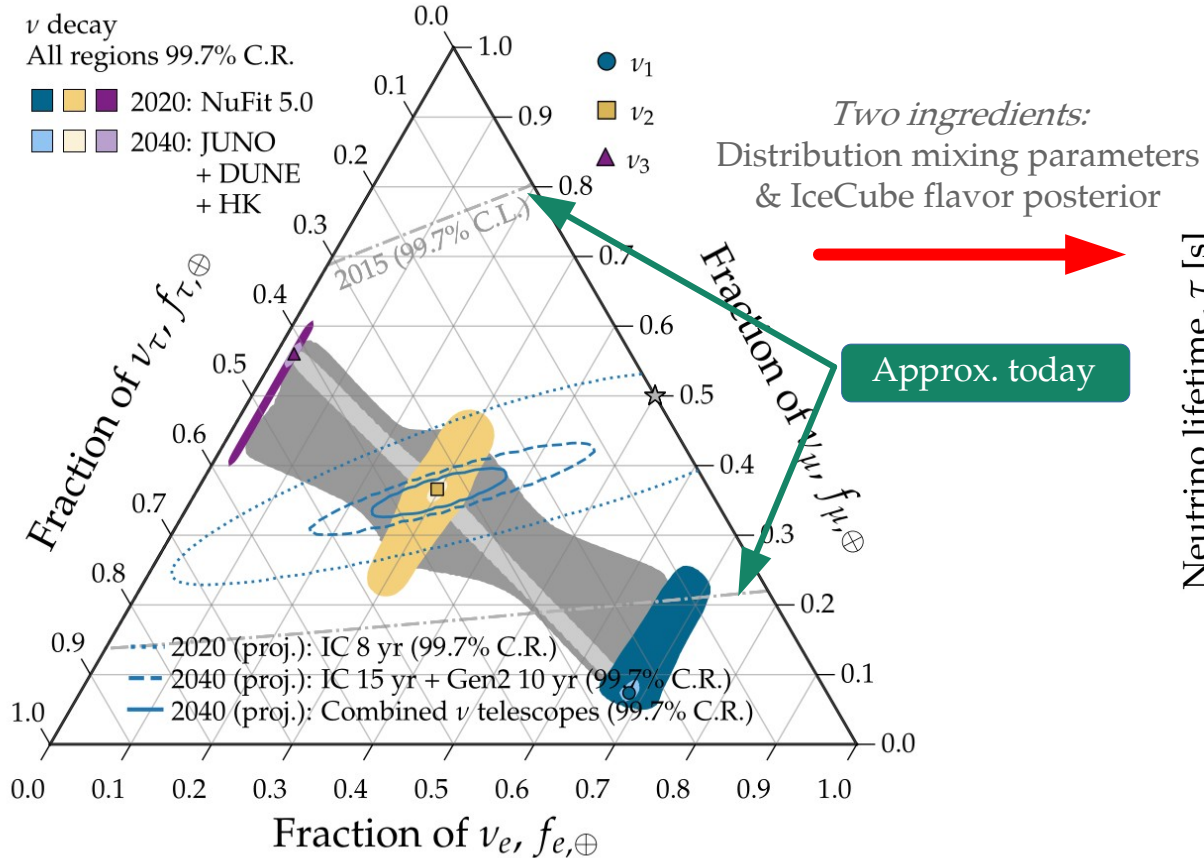
Flavor composition



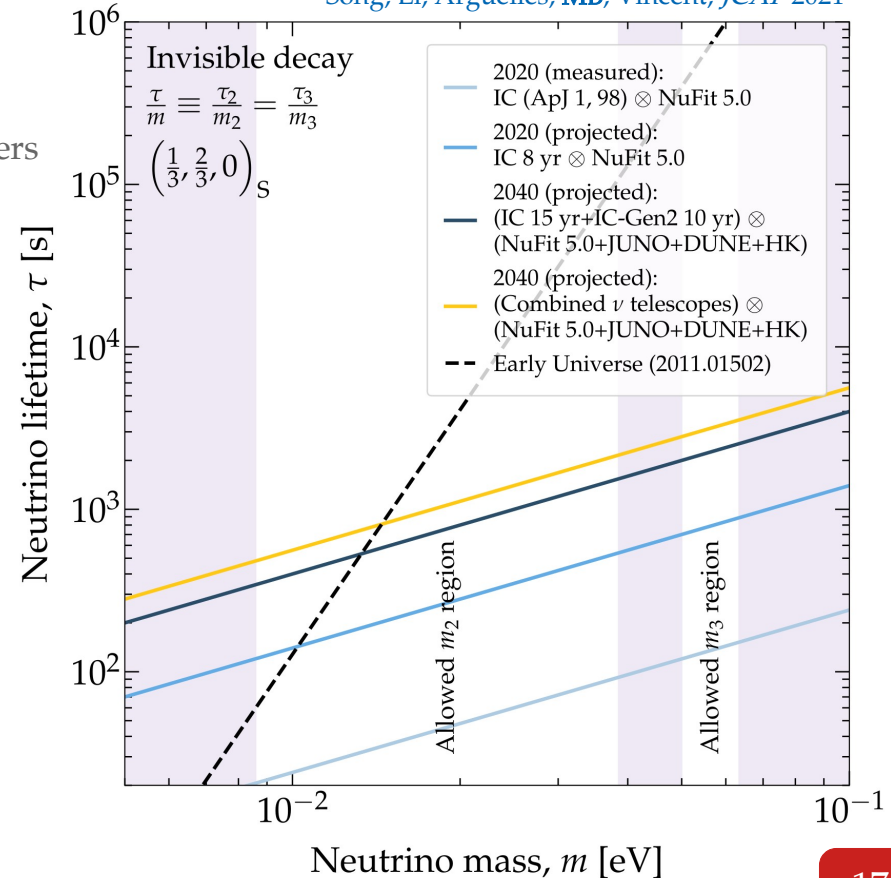
Spectrum shape



Event rate



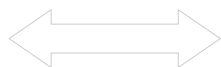
Song, Li, Argüelles, **MB**, Vincent, *JCAP*2021



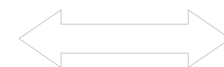
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See also: Beacom *et al.*, *PRL* 2002 / Baerwald, **MB**, Winter, *JCAP*2012 / **MB**, Beacom, Murase, *PRD*2017 / Rasmussen *et al.*, *PRD*2017 / Denton & Tamborra, *PRL* 2018 / Abdullahi & Denton, *PRD*2020 / **MB**, 2004.06844

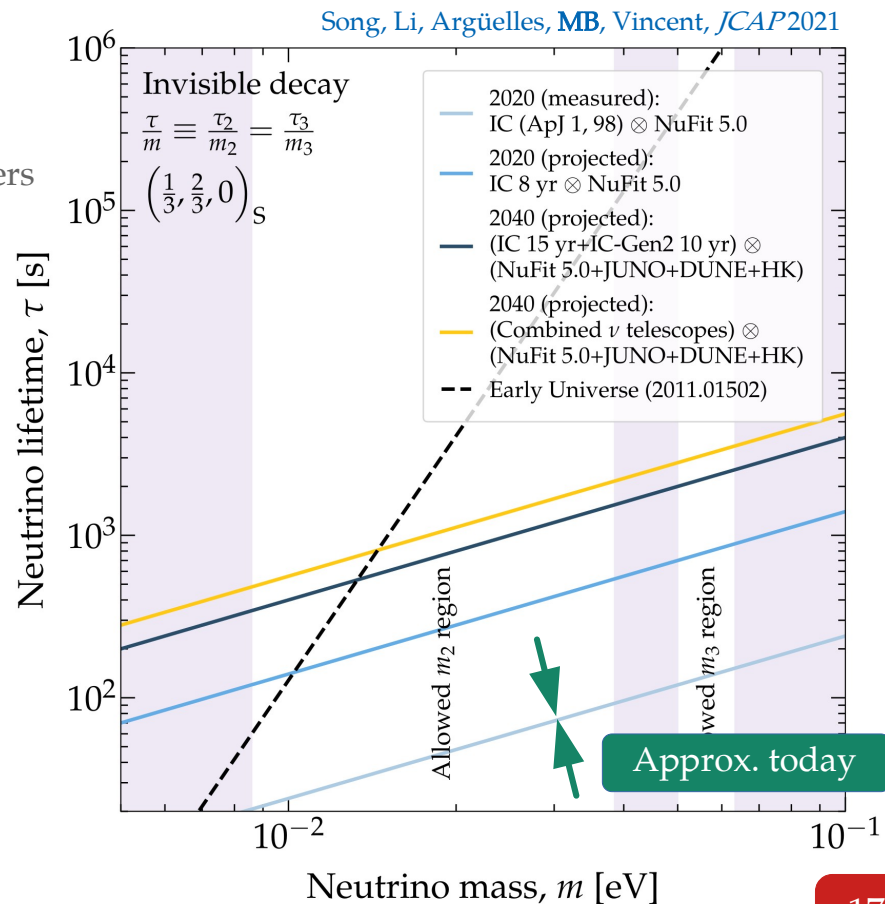
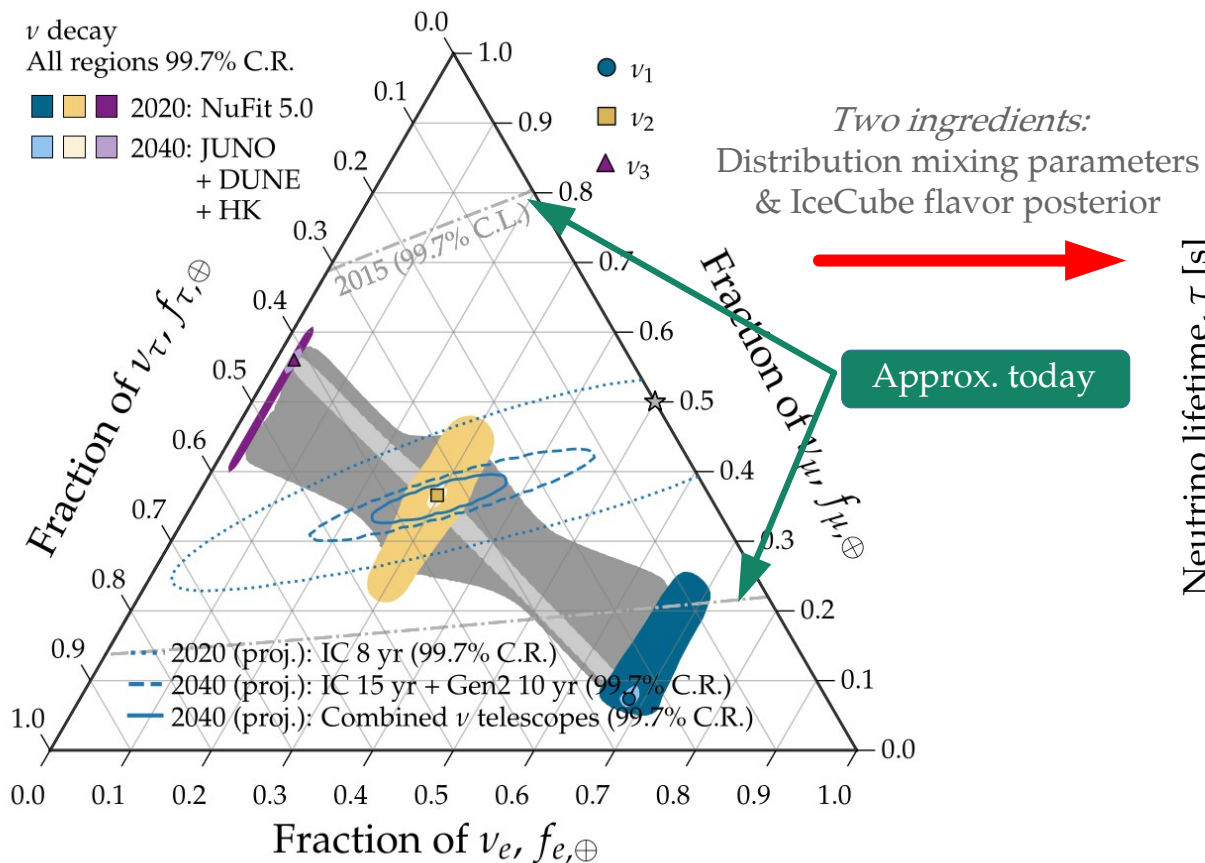
Flavor composition



Spectrum shape



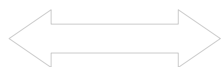
Event rate



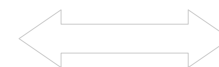
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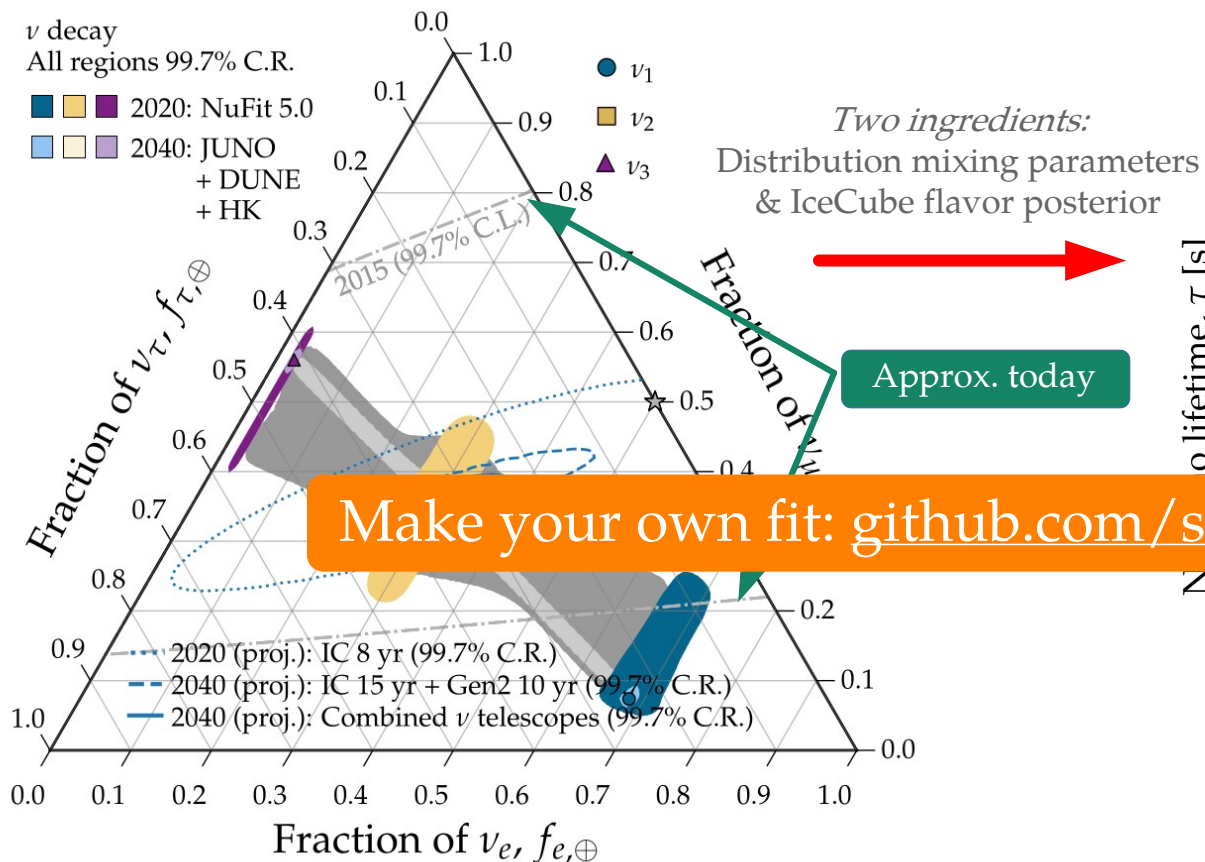
Flavor composition



Spectrum shape

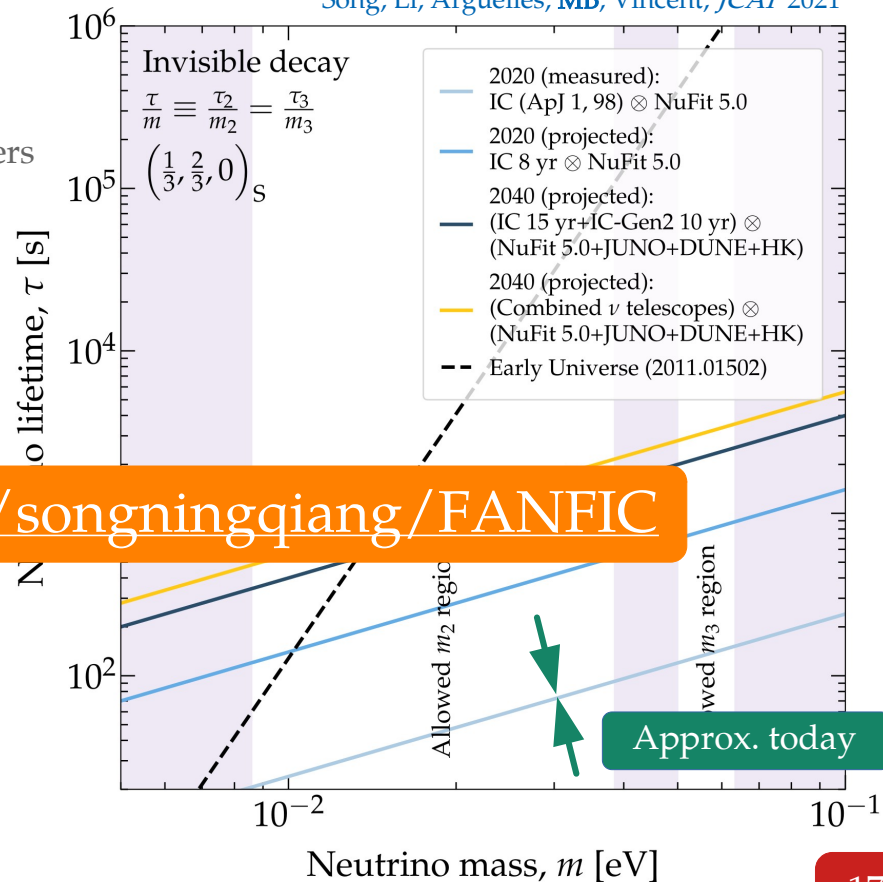


Event rate



Make your own fit: [github.com/songningqiang/FANFIC](https://github.com/songningqiang/FANFIC)

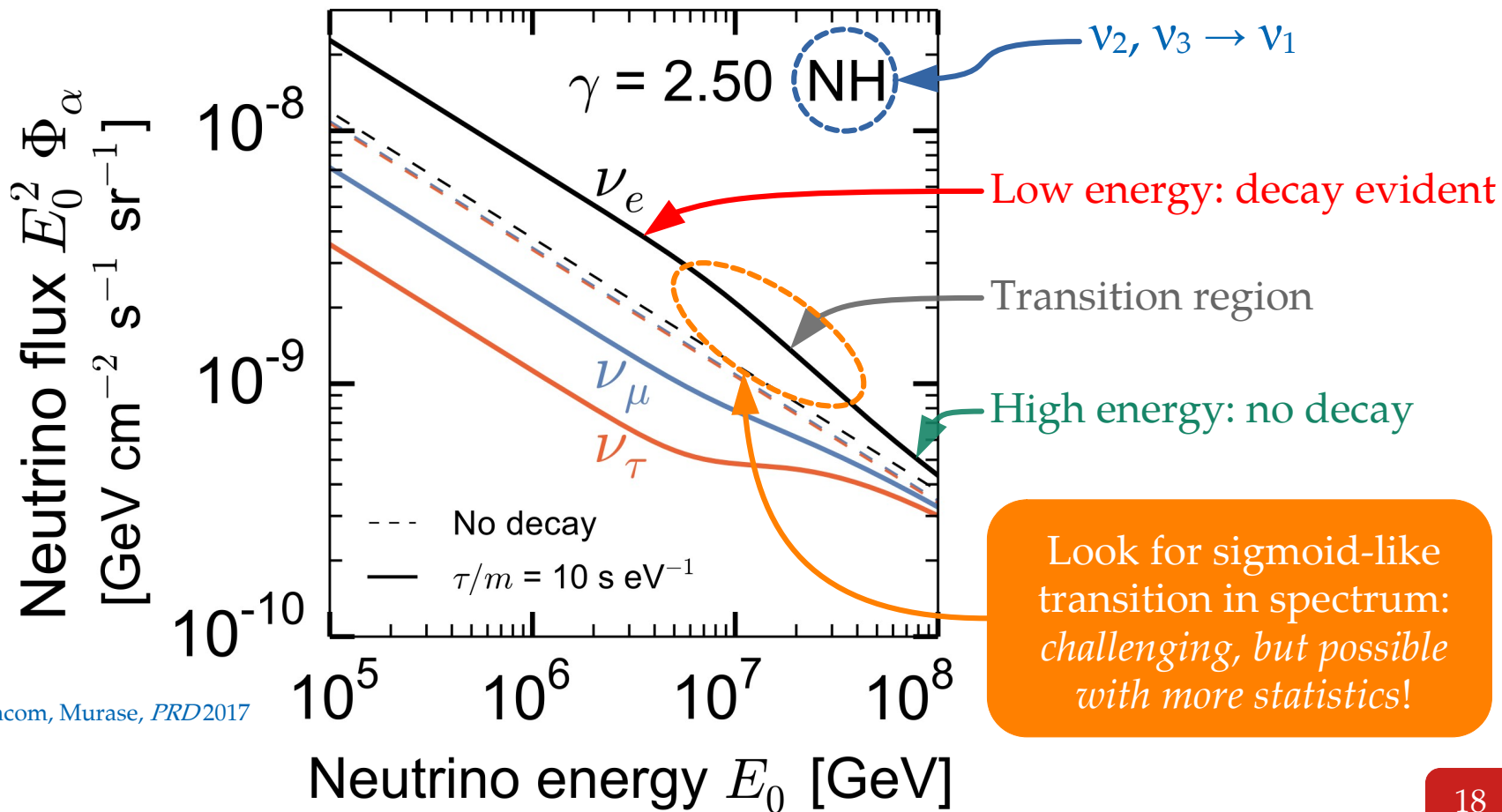
Song, Li, Argüelles, MB, Vincent, *JCAP* 2021



# What does neutrino decay change?

See also: Beacom *et al.*, *PRL* 2002 / Baerwald, MB, Winter, *JCAP*2012 / Rasmussen *et al.*, *PRD*2017 / Denton & Tamborra, *PRL* 2018 / Abdullahi & Denton, *PRD*2020 / MB, 2004.06844 / Song, Li, Argüelles, MB, Vincent, *JCAP*2020

Flavor composition  $\longleftrightarrow$  Spectrum shape  $\longleftrightarrow$  Event rate

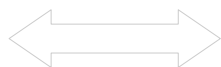


MB, Beacom, Murase, *PRD*2017

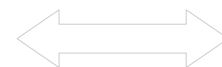
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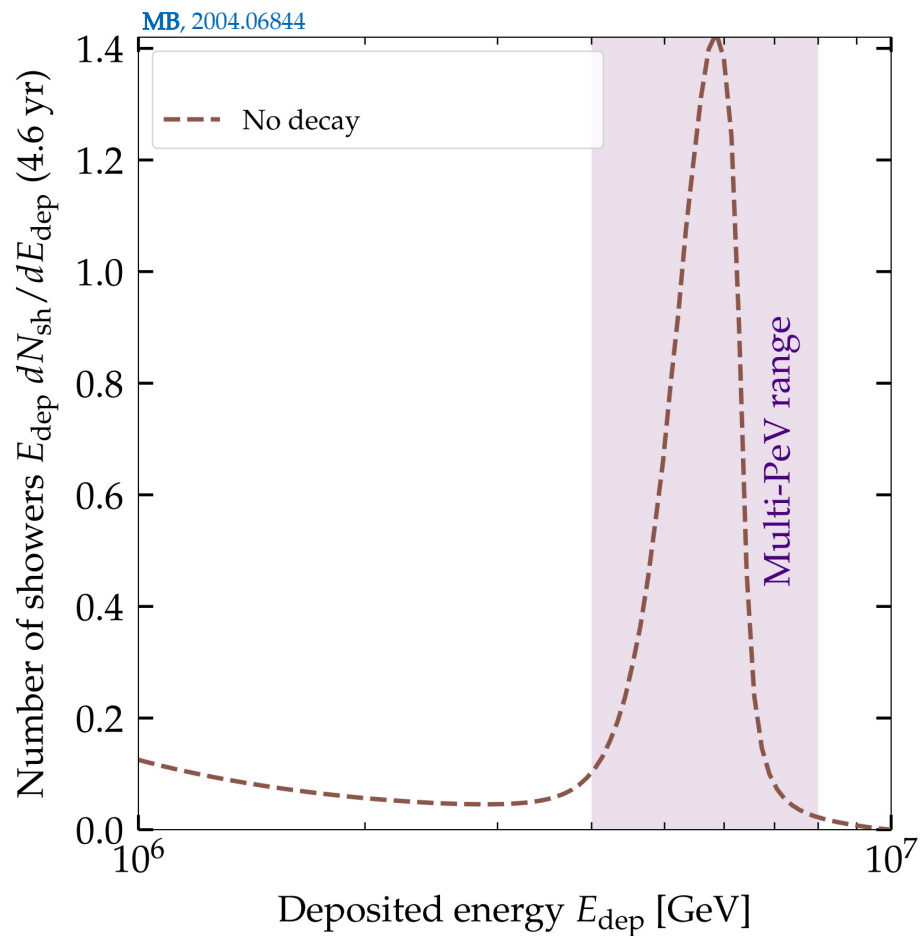
Flavor composition



Spectrum shape



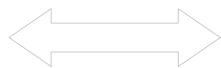
Event rate



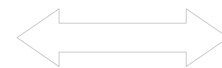
# What does neutrino decay change?

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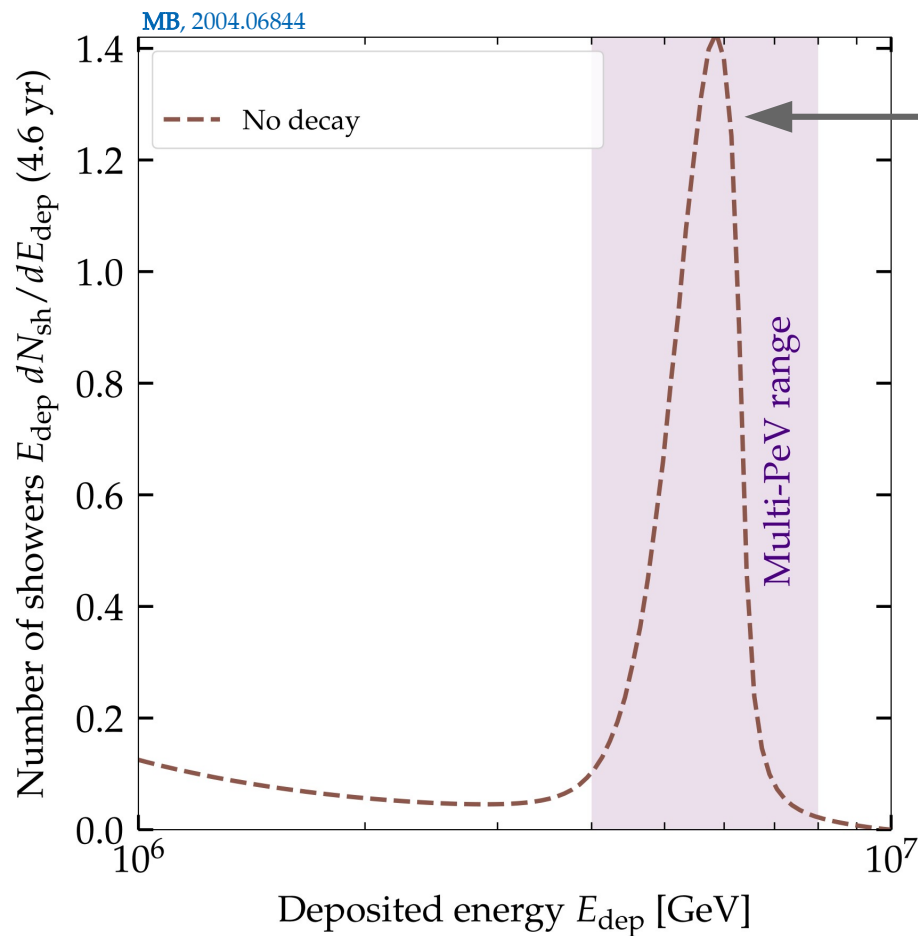
Flavor composition



Spectrum shape



Event rate



Glashow resonance (GR):

$\bar{\nu}_e + e \rightarrow W \rightarrow \text{hadrons} \rightarrow \text{shower}$

# What does neutrino decay change?

See also: Beacom *et al.*, *PRL* 2002 / Baerwald, MB, Winter, *JCAP* 2012 / MB, Beacom, Murase, *PRD* 2017 / Rasmussen *et al.*, *PRD* 2017 / Denton & Tamborra, *PRL* 2018 / Abdullahi & Denton, *PRD* 2020 / Song, Li, Argüelles, MB, Vincent, *JCAP* 2020

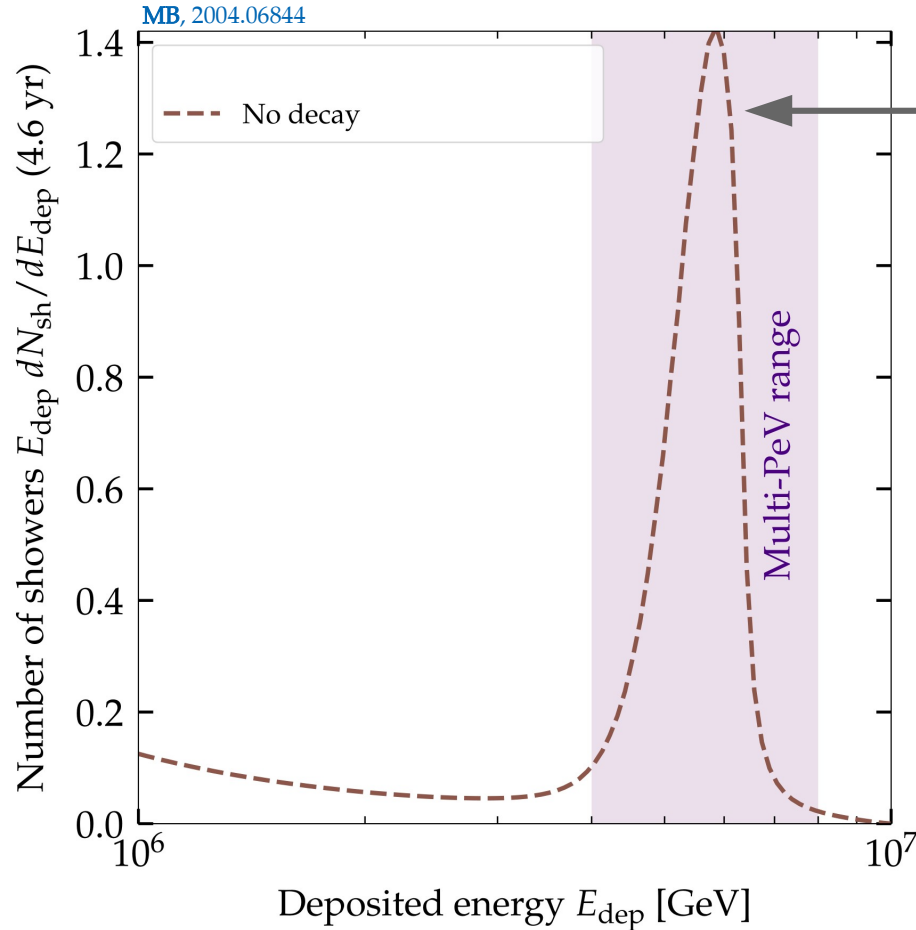
Flavor composition



Spectrum shape



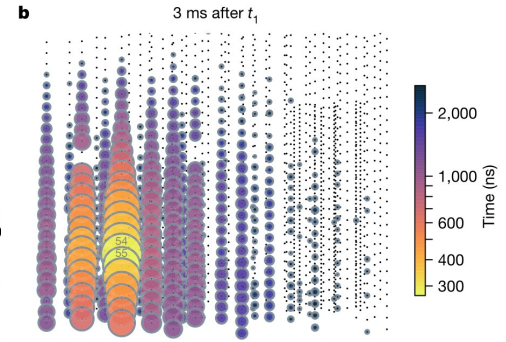
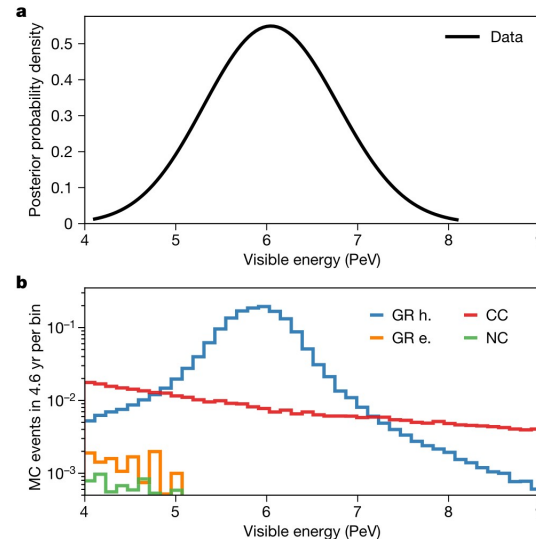
Event rate



Glashow resonance (GR):

$$\bar{\nu}_e + e \rightarrow W \rightarrow \text{hadrons} \rightarrow \text{shower}$$

IceCube has seen one GR candidate in 4.6 years:

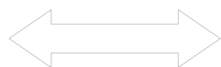


IceCube Collab., *Nature* 2021

# What does neutrino decay change?

See also: Beacom *et al.*, *PRL* 2002 / Baerwald, MB, Winter, *JCAP*2012 / MB, Beacom, Murase, *PRD*2017 / Rasmussen *et al.*, *PRD*2017 / Denton & Tamborra, *PRL* 2018 / Abdullahi & Denton, *PRD*2020 / Song, Li, Argüelles, MB, Vincent, *JCAP*2020

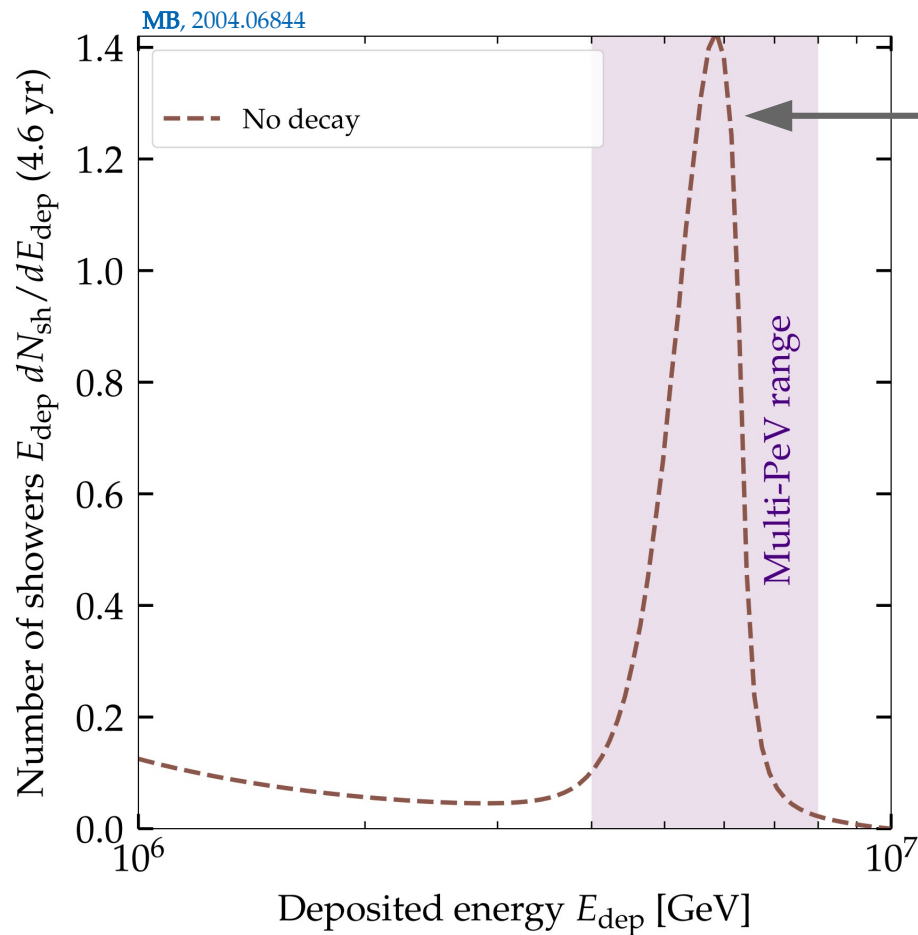
Flavor composition



Spectrum shape



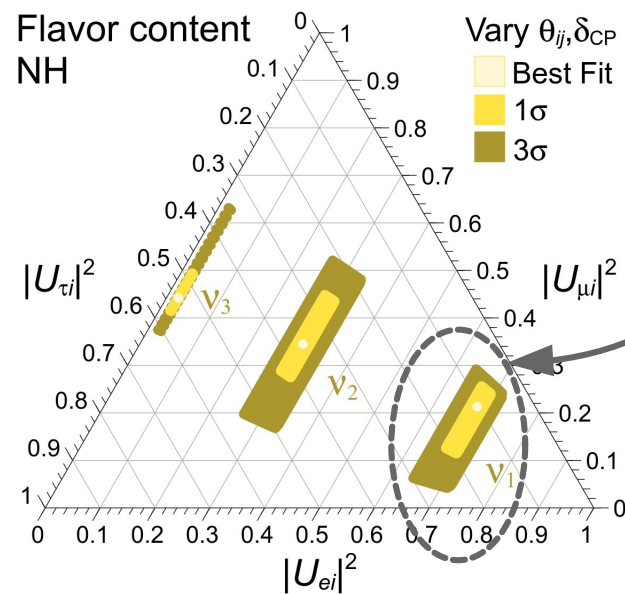
Event rate



Glashow resonance (GR):

$$\bar{\nu}_e + e \rightarrow W \rightarrow \text{hadrons} \rightarrow \text{shower}$$

$\nu_1$  is the mass eigenstate with the most  $e$  flavor



# What does neutrino decay change?

See also: Beacom *et al.*, *PRL* 2002 / Baerwald, MB, Winter, *JCAP*2012 / MB, Beacom, Murase, *PRD*2017 / Rasmussen *et al.*, *PRD*2017 / Denton & Tamborra, *PRL* 2018 / Abdullahi & Denton, *PRD*2020 / Song, Li, Argüelles, MB, Vincent, *JCAP*2020

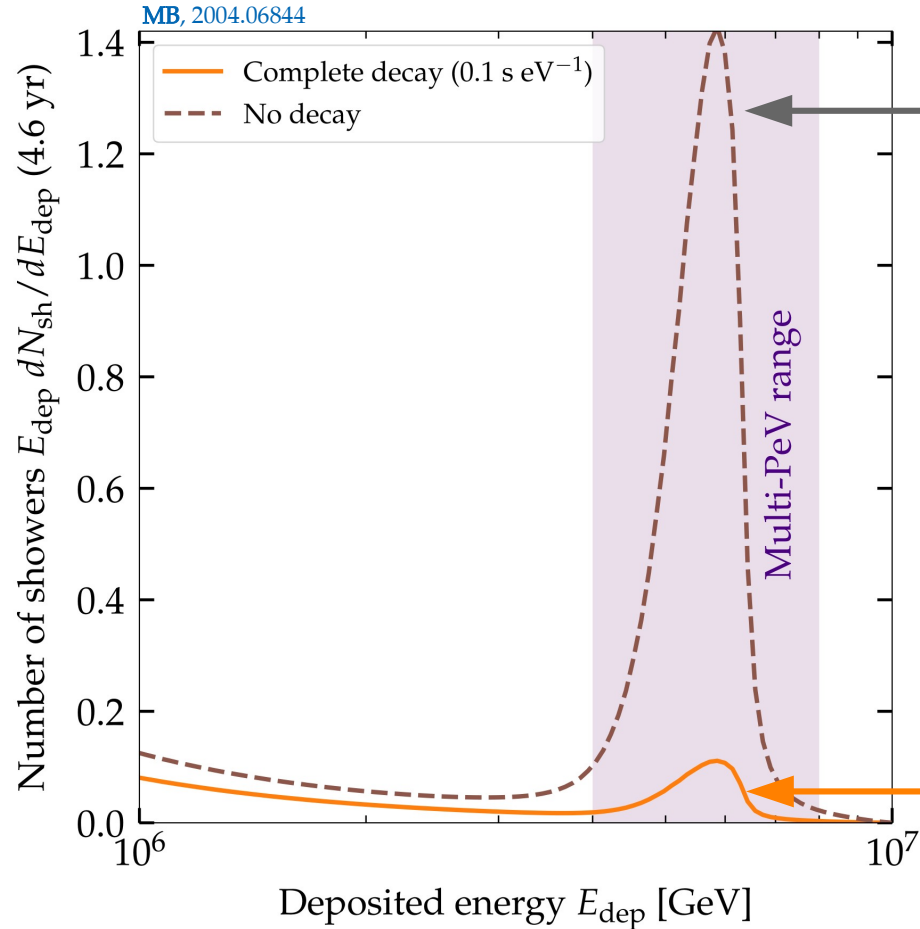
Flavor composition



Spectrum shape



Event rate



Glashow resonance (GR):

$$\bar{\nu}_e + e \rightarrow W \rightarrow \text{hadrons} \rightarrow \text{shower}$$

If  $\bar{\nu}_1$  had decayed en route to Earth, there would not have been  $\bar{\nu}_e$  left to trigger a GR

# What does neutrino decay change?

See also: Beacom *et al.*, *PRL* 2002 / Baerwald, MB, Winter, *JCAP*2012 / MB, Beacom, Murase, *PRD*2017 / Rasmussen *et al.*, *PRD*2017 / Denton & Tamborra, *PRL* 2018 / Abdullahi & Denton, *PRD*2020 / Song, Li, Argüelles, MB, Vincent, *JCAP*2020

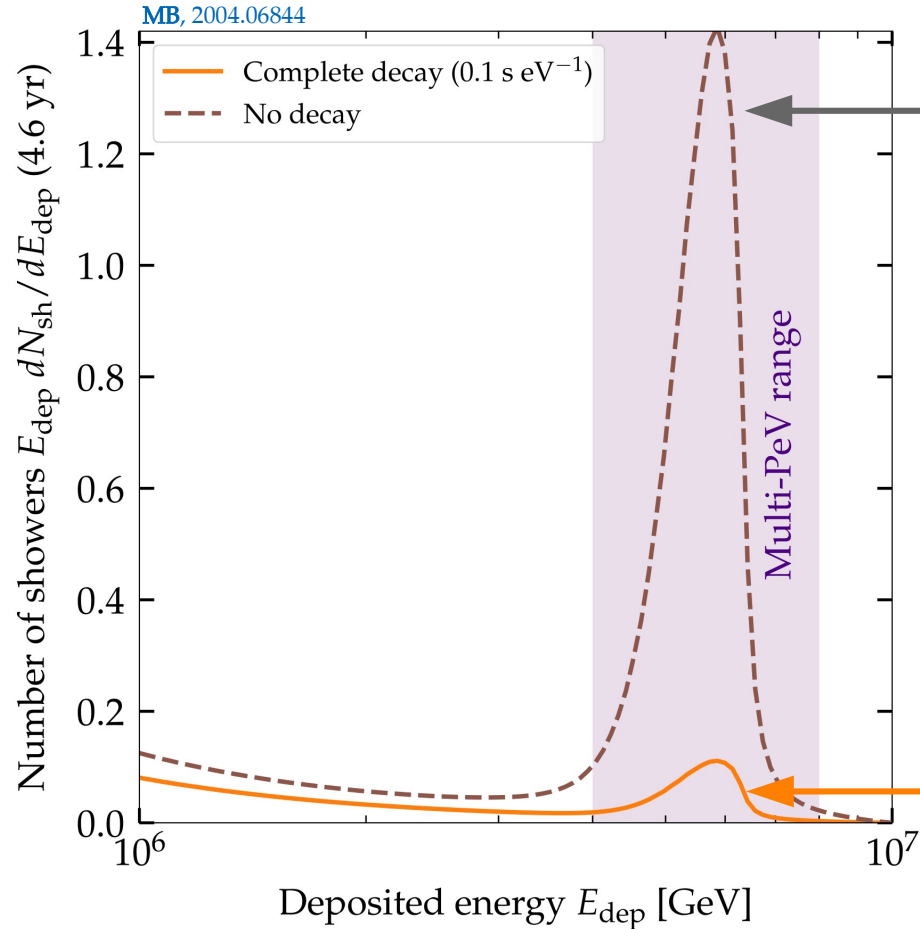
Flavor composition



Spectrum shape



Event rate



Glashow resonance (GR):

$$\bar{\nu}_e + e \rightarrow W \rightarrow \text{hadrons} \rightarrow \text{shower}$$

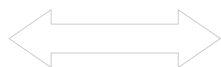
So by having observed 1 GR event we can place a *lower* limit on the lifetime of  $\bar{\nu}_1$  ( $= \nu_1$ )

If  $\bar{\nu}_1$  had decayed en route to Earth, there would not have been  $\bar{\nu}_e$  left to trigger a GR

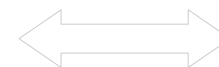
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Flavor composition

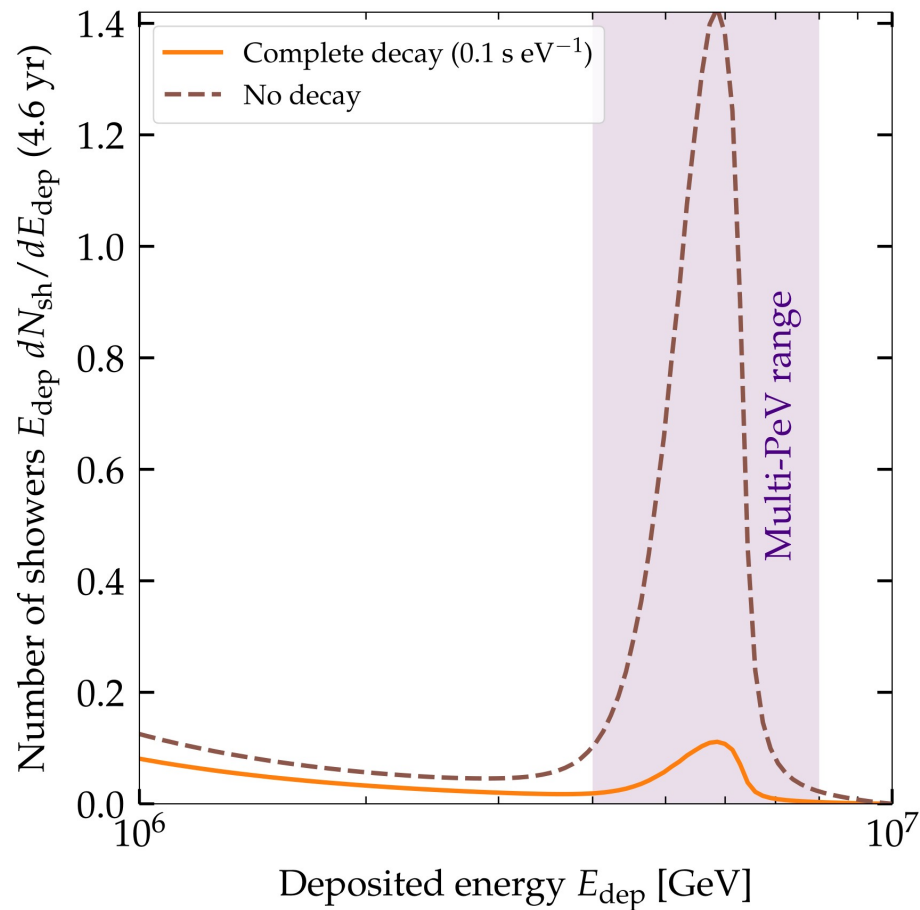


Spectrum shape



Event rate

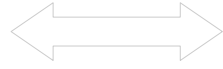
**MB**, 2004.06844



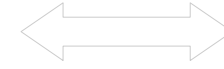
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See also: Beacom *et al.*, *PRL* 2002 / Baerwald, MB, Winter, *JCAP*2012 / MB, Beacom, Murase, *PRD*2017 / Rasmussen *et al.*, *PRD*2017 / Denton & Tamborra, *PRL* 2018 / Abdullahi & Denton, *PRD*2020 / Song, Li, Argüelles, MB, Vincent, *JCAP*2020

Flavor composition

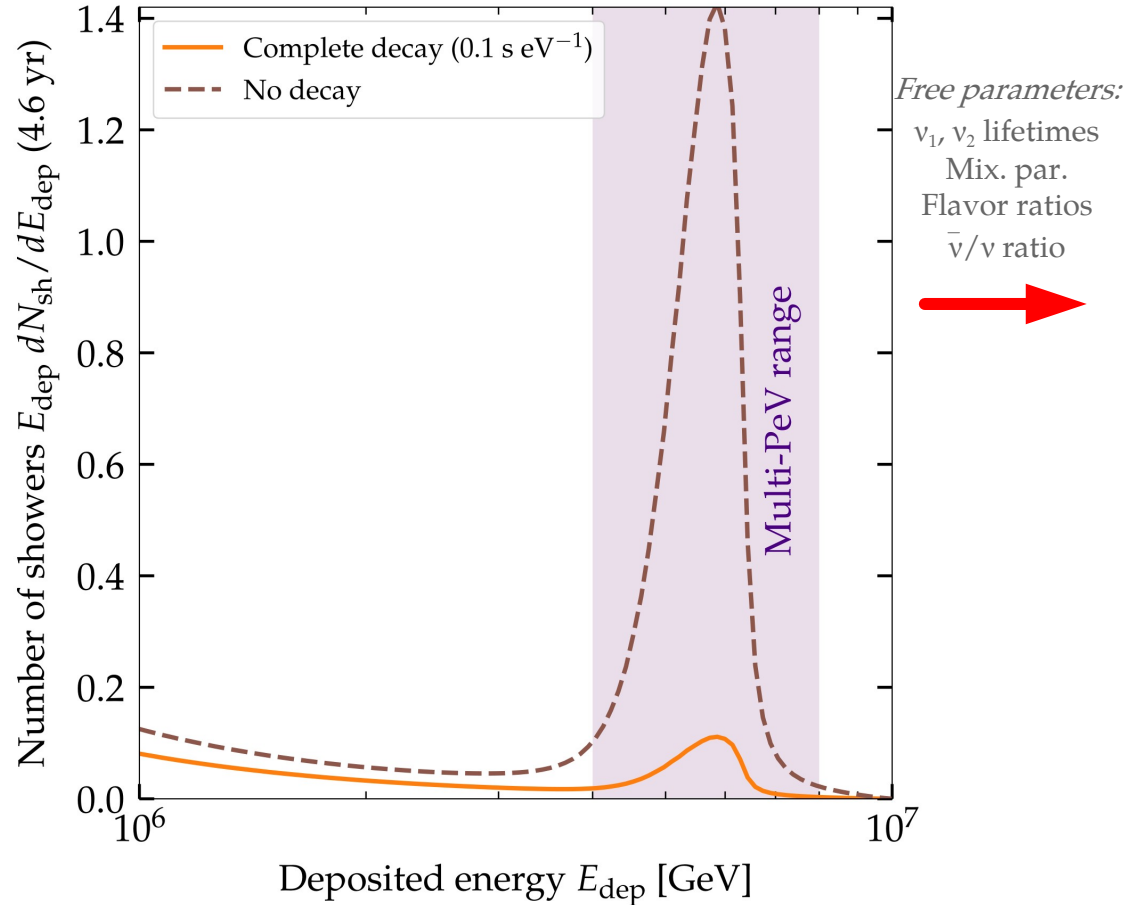


Spectrum shape



Event rate

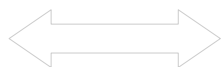
MB, 2004.06844



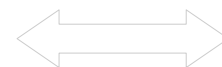
# What does neutrino decay change?

See also: Beacom *et al.*, *PRL* 2002 / Baerwald, MB, Winter, *JCAP* 2012 / MB, Beacom, Murase, *PRD* 2017 / Rasmussen *et al.*, *PRD* 2017 / Denton & Tamborra, *PRL* 2018 / Abdullahi & Denton, *PRD* 2020 / Song, Li, Argüelles, MB, Vincent, *JCAP* 2020

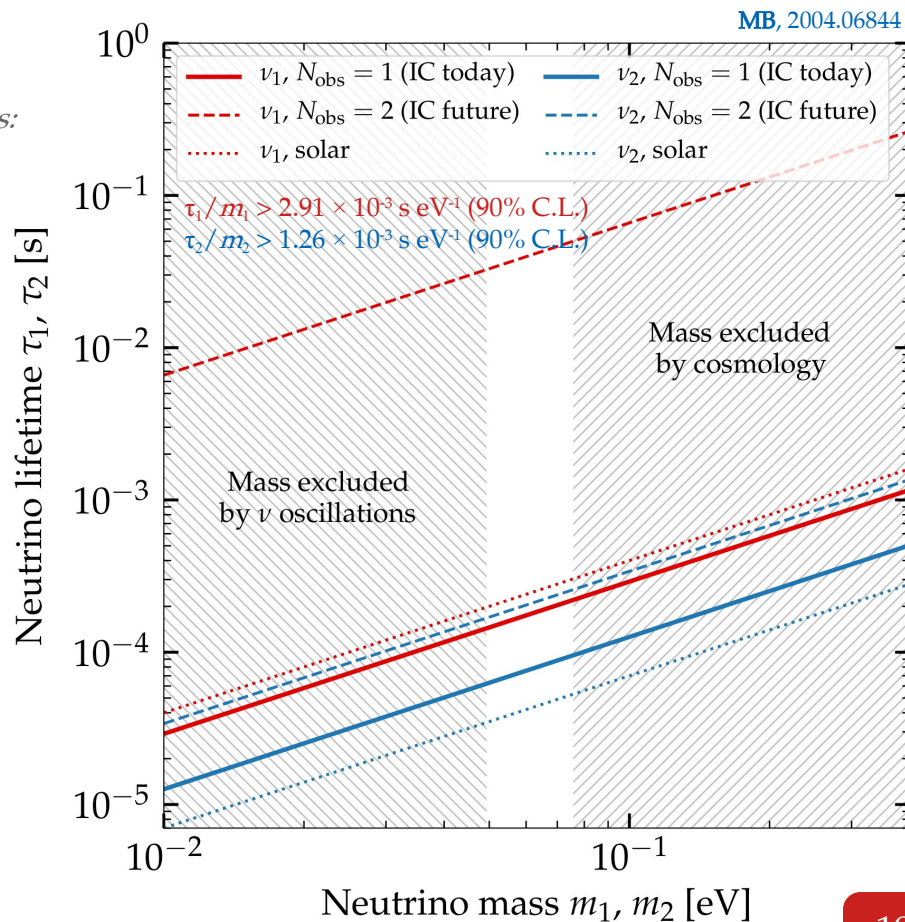
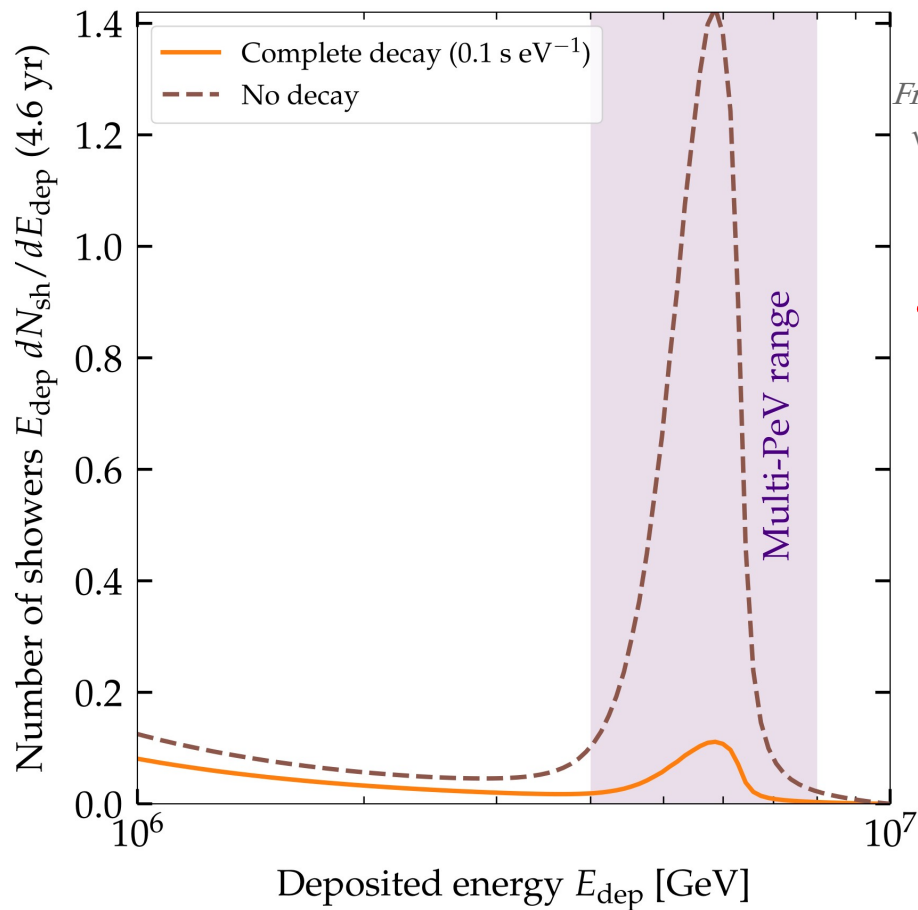
Flavor composition



Spectrum shape



Event rate



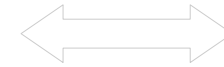
# What does neutrino decay change?

See also: Beacom *et al.*, *PRL* 2002 / Baerwald, MB, Winter, *JCAP*2012 / MB, Beacom, Murase, *PRD*2017/ Rasmussen *et al.*, *PRD*2017 / Denton & Tamborra, *PRL* 2018 / Abdullahi & Denton, *PRD*2020 / Song, Li, Argüelles, MB, Vincent, *JCAP*2020

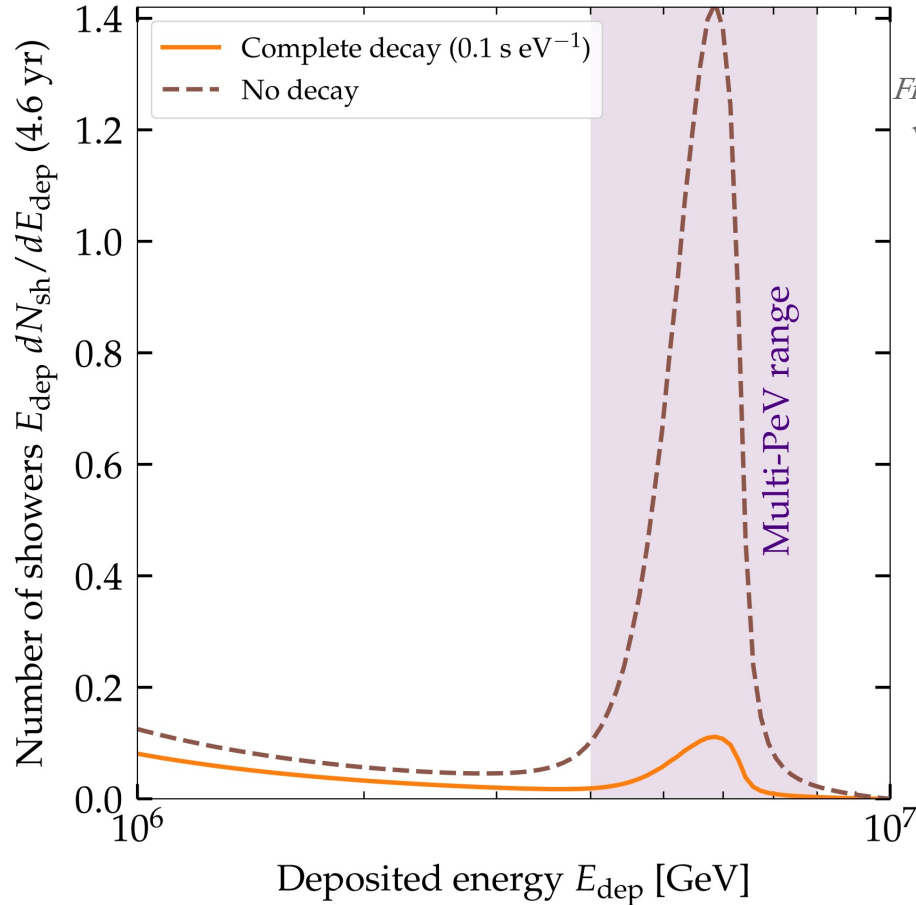
Flavor composition



Spectrum shape

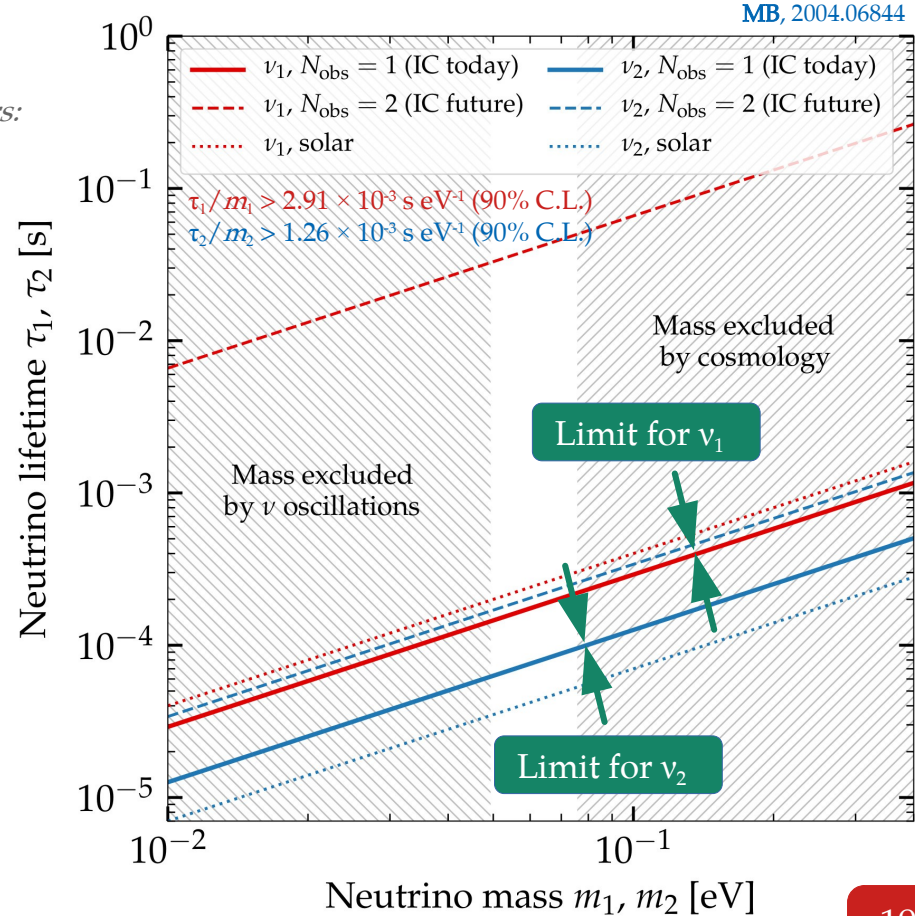


Event rate

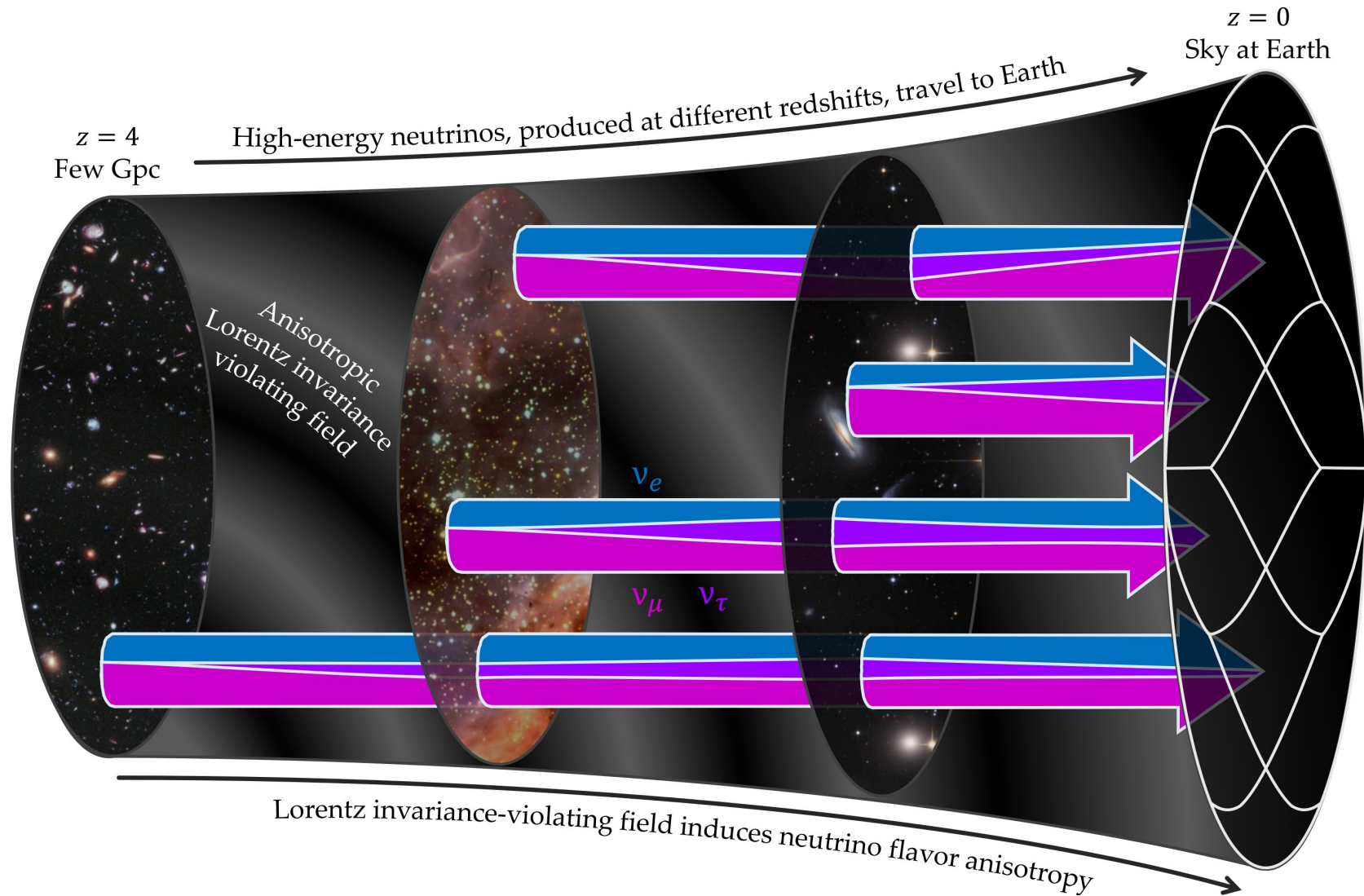


Free parameters:

- $\nu_1, \nu_2$  lifetimes
- Mix. par.
- Flavor ratios
- $\bar{\nu}/\nu$  ratio



# Direction-dependent flavor composition



Anisotropic Lorentz-invariance violation makes the flavor sky anisotropic:

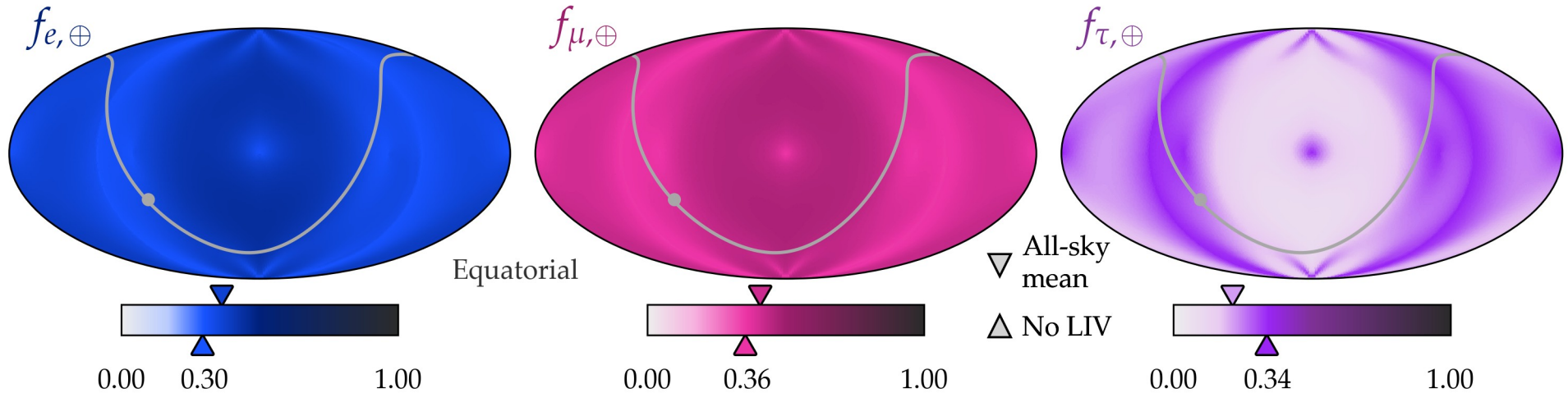
$$H_{\text{tot}} = H_{\text{vac}} + \sum_{d=2}^{\infty} H_{\text{LIV}}^{(d)} = H_{\text{vac}} + E^{d-3} \sum_{\ell=0}^{d-1} \sum_{m=-\ell}^{\ell} Y_{\ell}^m(\hat{\mathbf{p}}) (a_{\text{eff}}^{(d)})_{\ell m}^{\alpha\beta}$$

Neutrino oscillation probability becomes direction-dependent 

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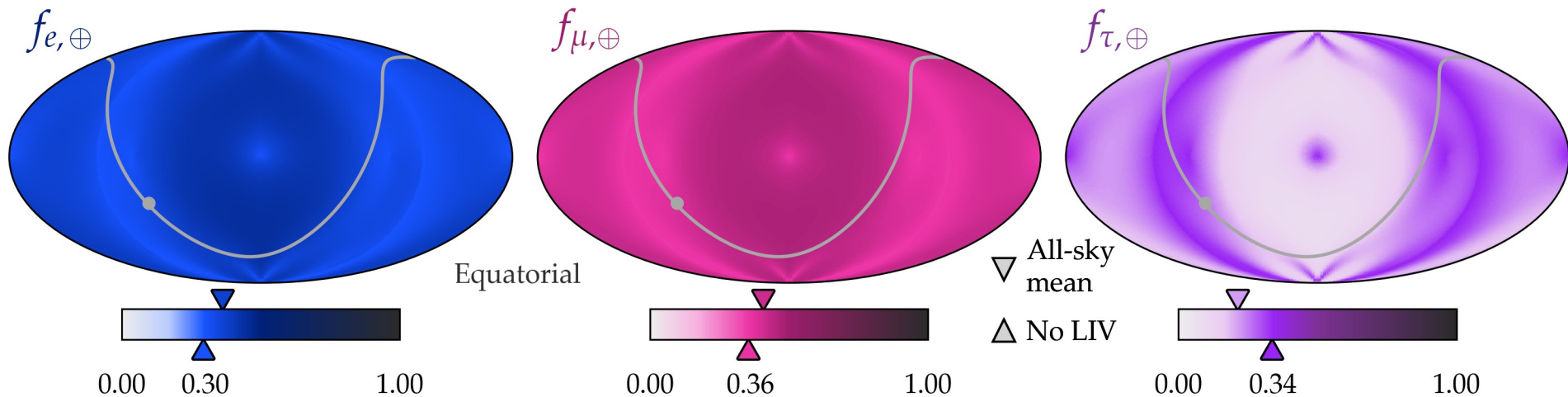
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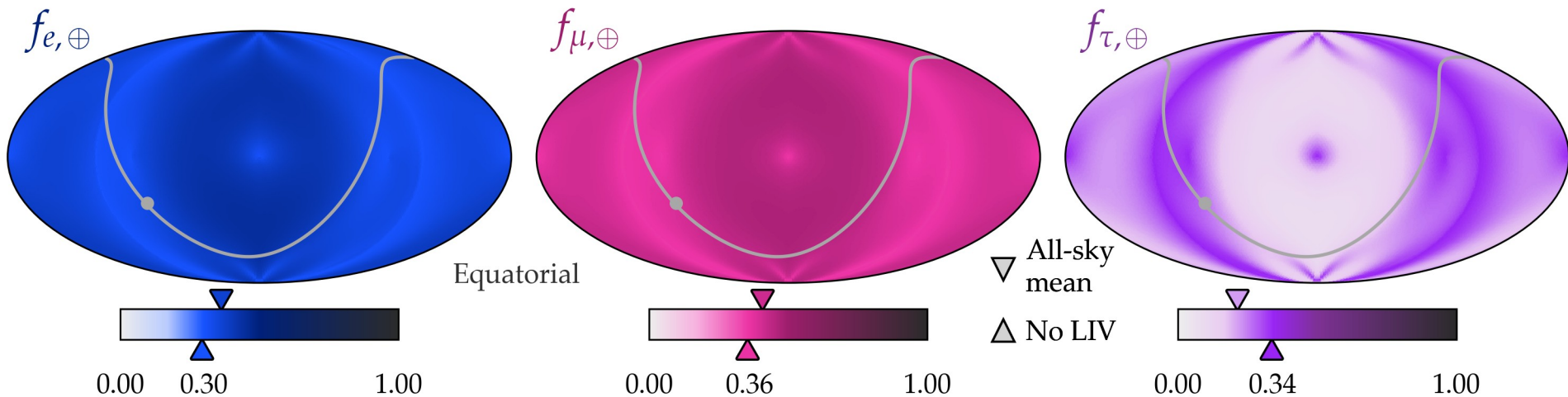
Upper limits from accelerator  $\nu$  (MINOS):  $< 10^{-20} - 10^{-15} \text{ GeV}^{-1}$

For dimension-5 CPT-odd LIV coefficient

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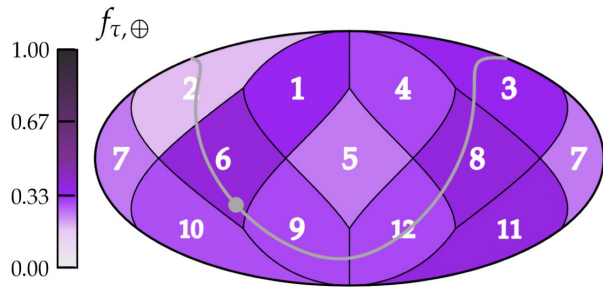
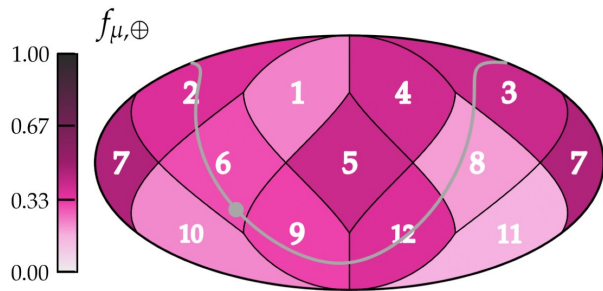
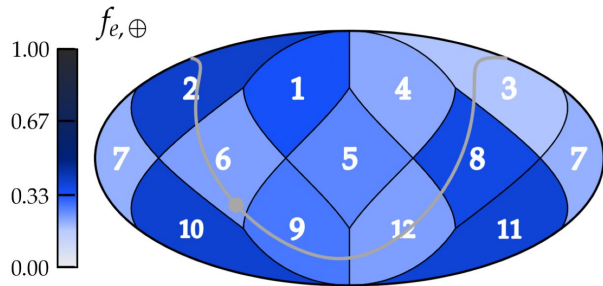
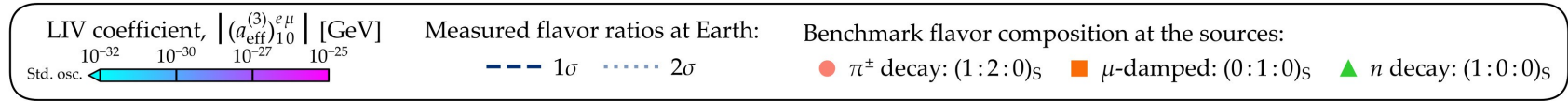


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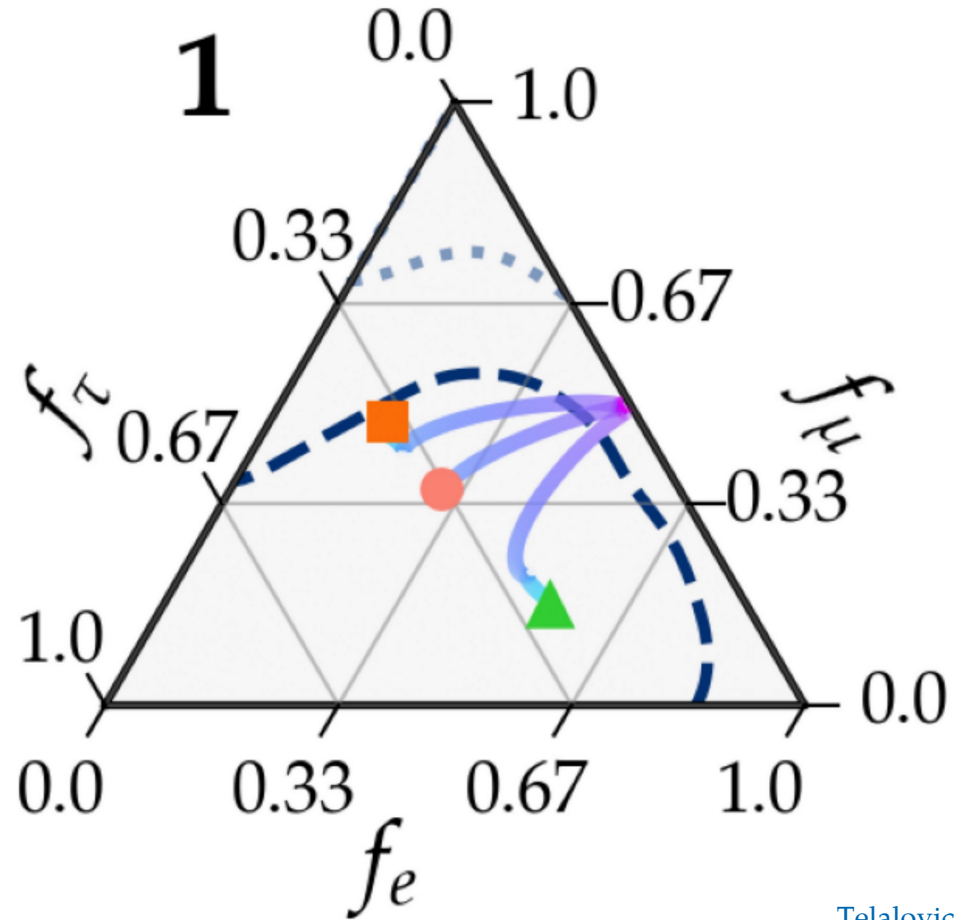
Upper limits from 7.5-year HESE:  $< 10^{-34} \text{ GeV}^{-1}$

For dimension-5  
CPT-odd LIV coefficient

# Lorentz-violating high-energy neutrino flavor anisotropy (IceCube HESE 7.5 years)

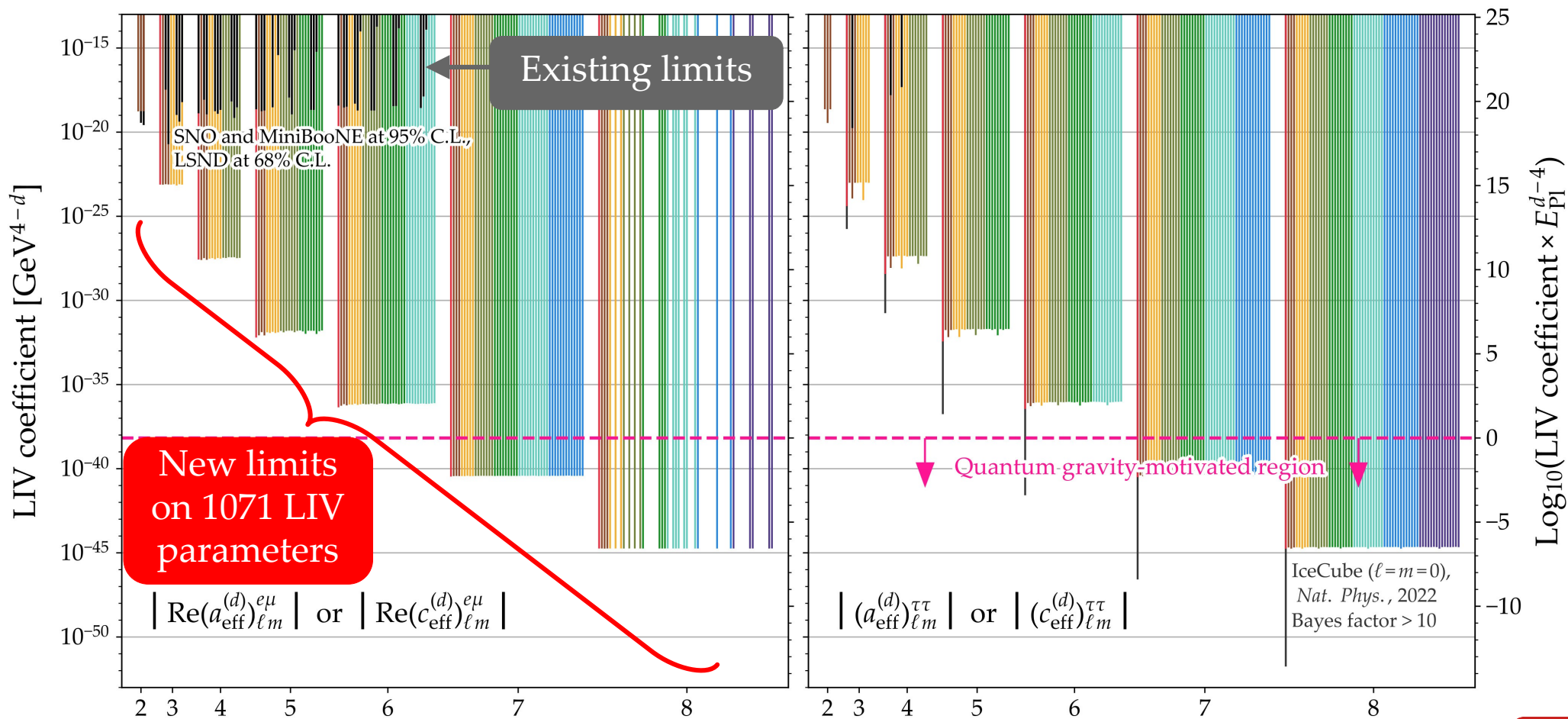


Equatorial





Disfavored at 95% C.L. from flavor isotropy (this work, using IceCube 7.5-year HESE)



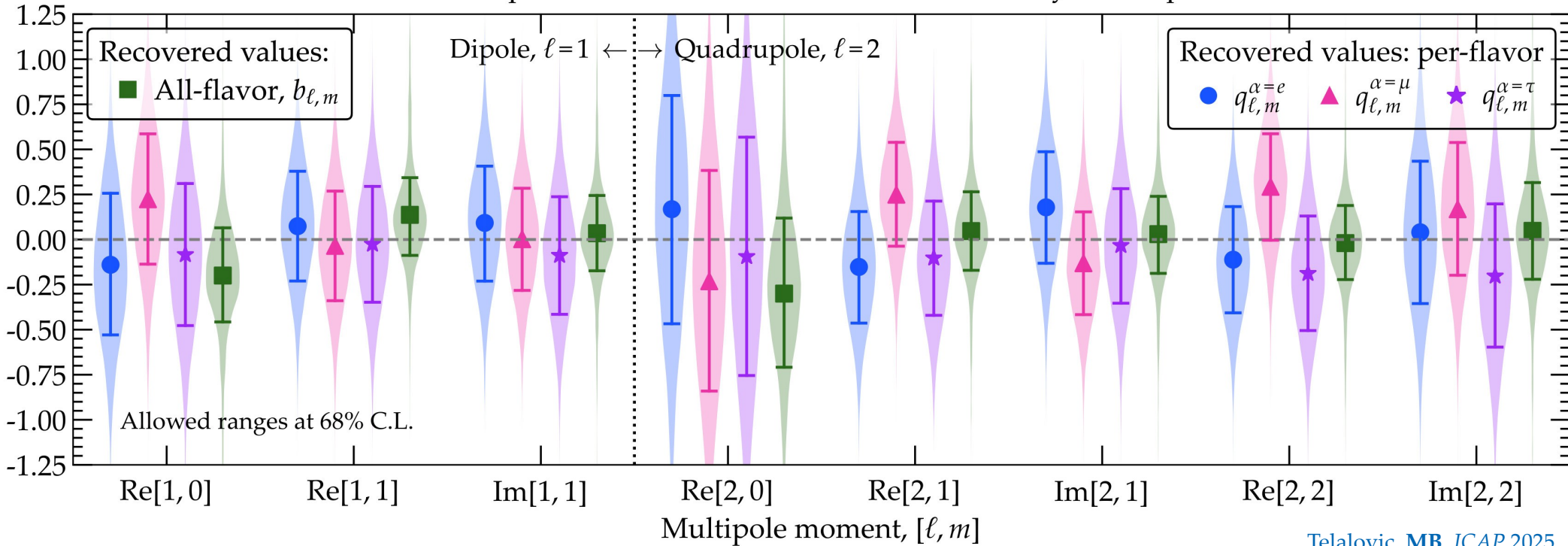
# Flavor dipoles and quadrupoles in the sky?

Flavor-dependent multipole expansion

Isotropic flux

$$\Phi_{\nu\alpha}(E_\nu, \theta_z, \phi) = \Phi_0 \left( \frac{E_\nu}{100 \text{ TeV}} \right)^{-\gamma} \times \frac{1}{6} \left[ 1 + \sum_{\ell=1}^{\infty} \sum_{m=-\ell}^{\ell} q_{\ell,m}^\alpha Y_\ell^m(\theta_z, \phi) \right]$$

Multipole moments from the IceCube HESE 7.5-year sample



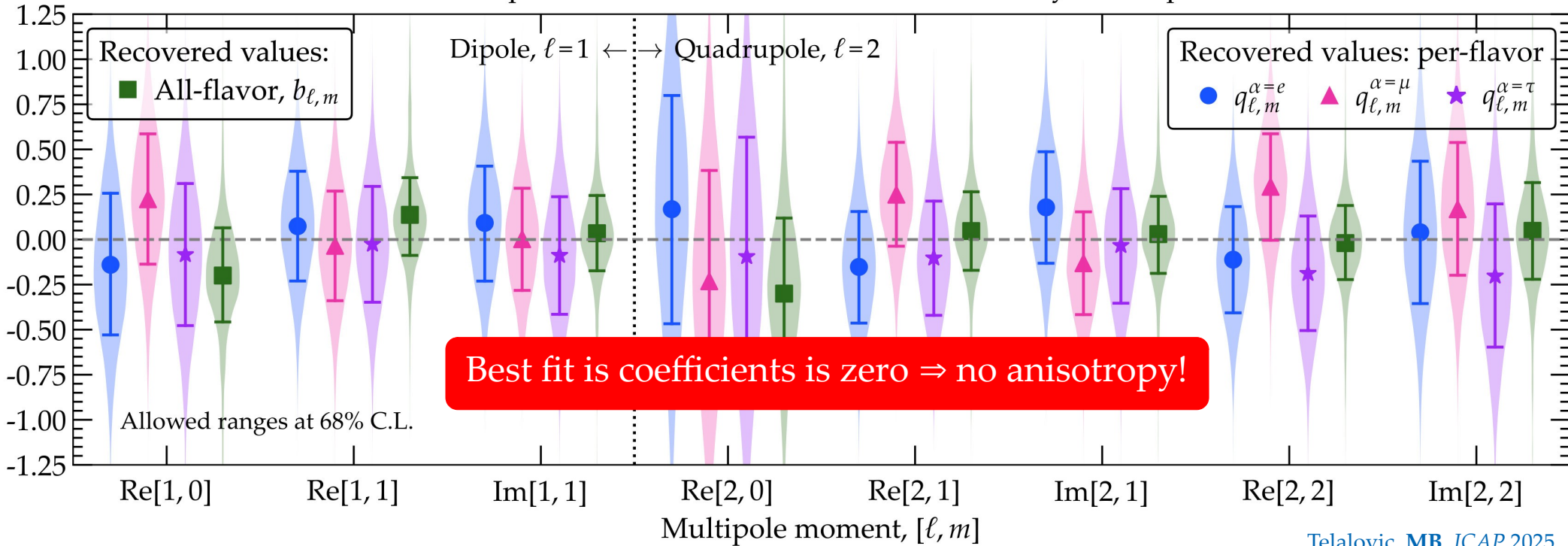
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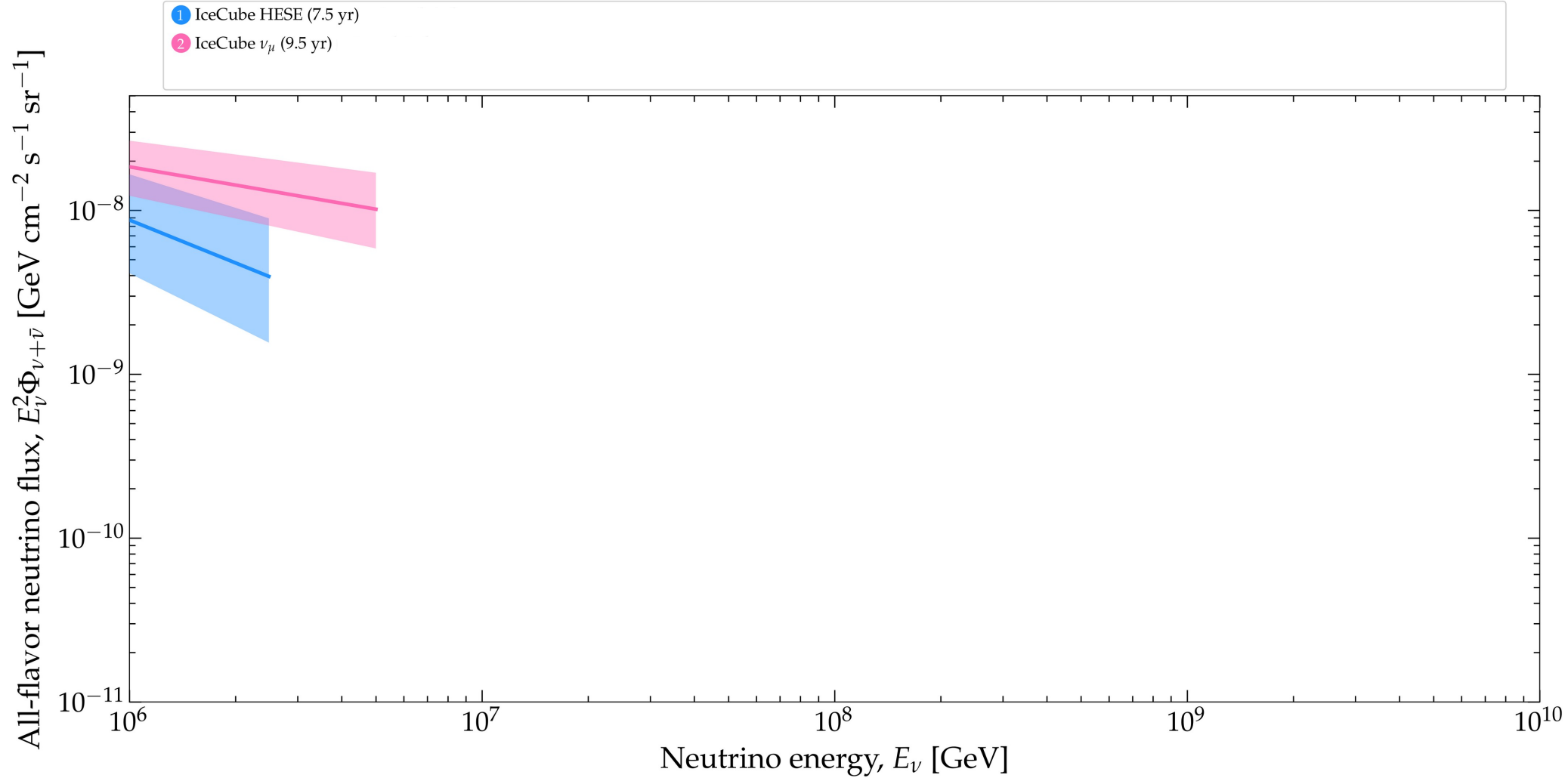
Isotropic flux

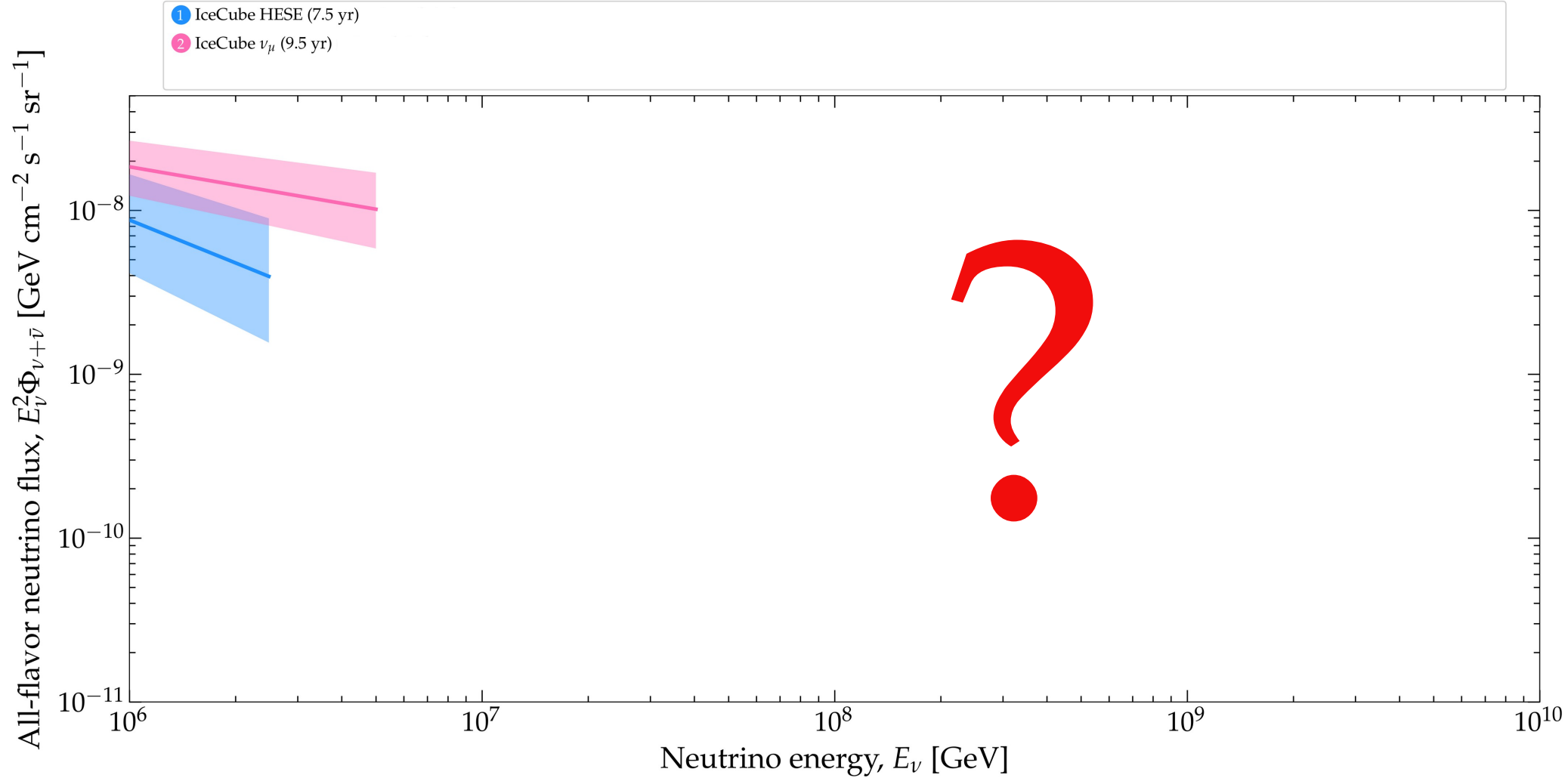
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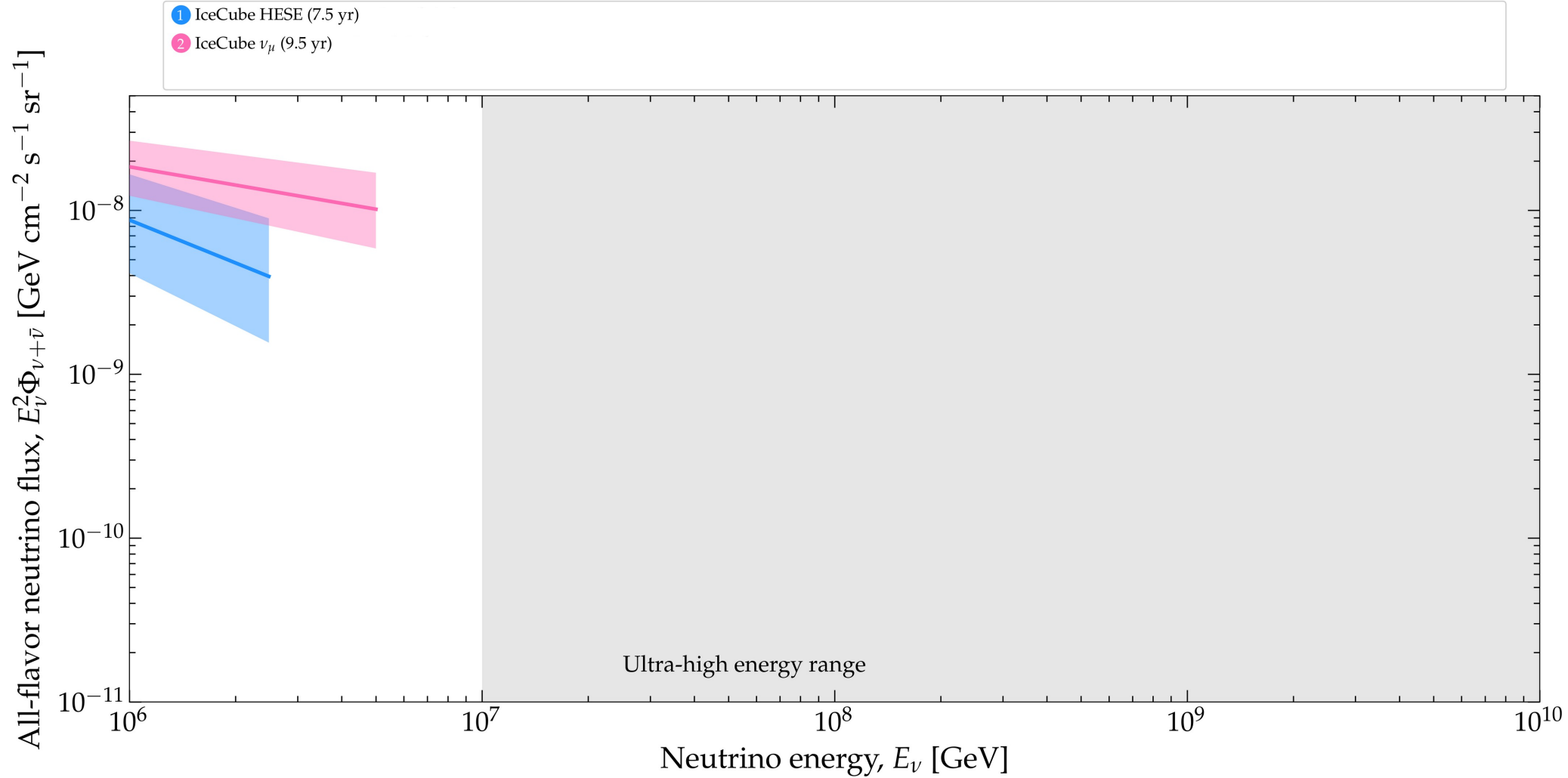
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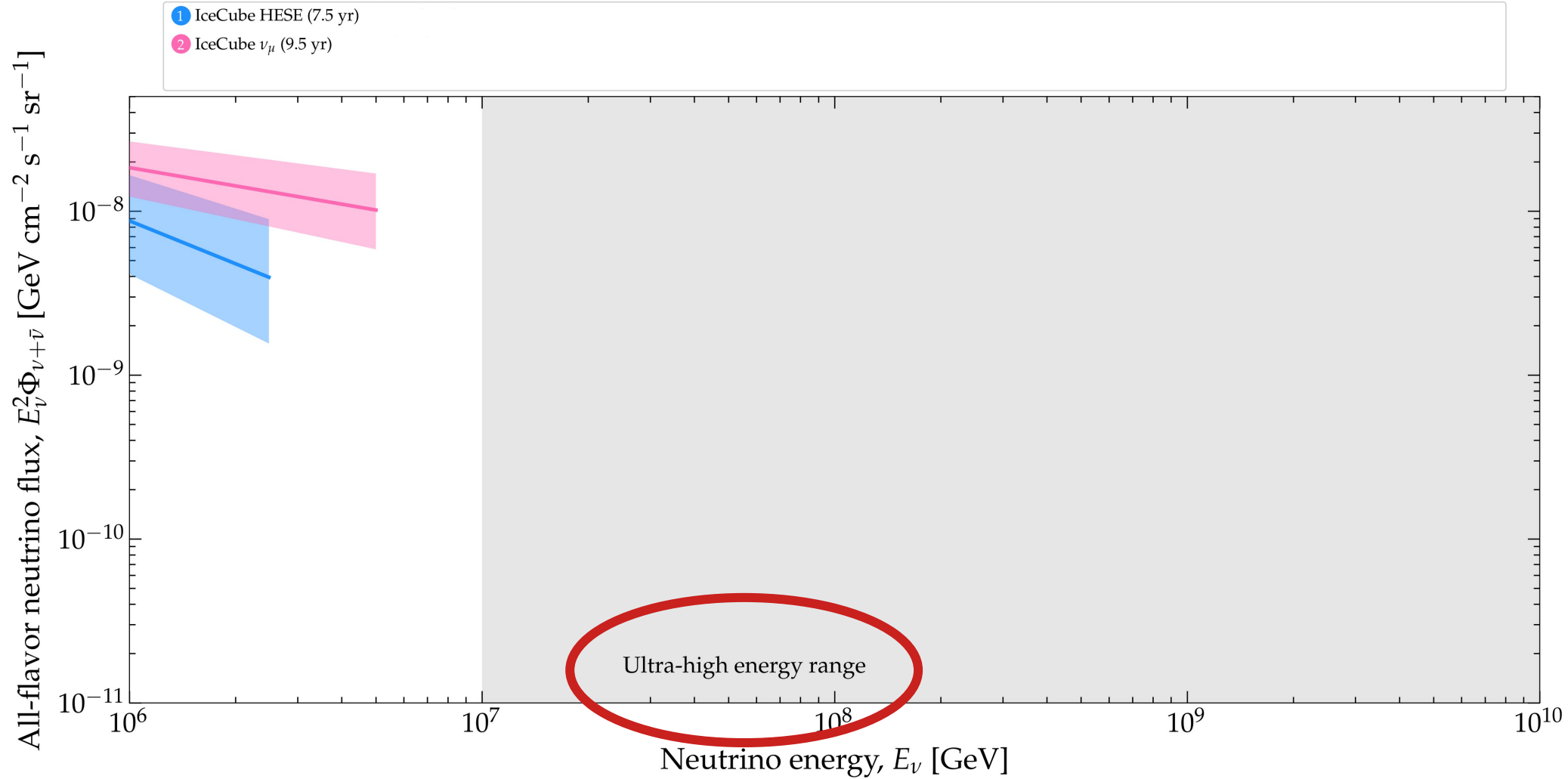


Flavor at ultra-high  
energies ( $> 100$  PeV)



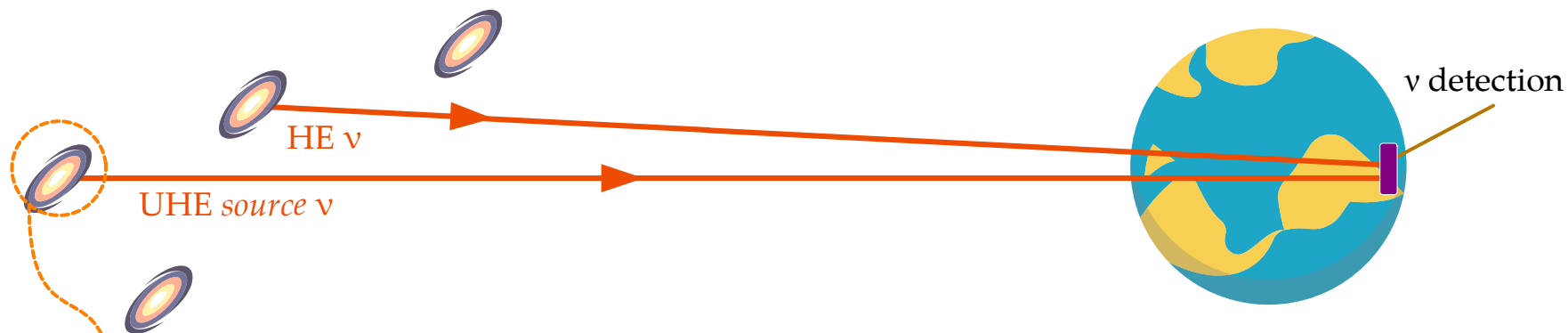






Redshift ←

$z = 0$



Undiscovered

$\text{meV } \gamma$

$\text{EeV } p$

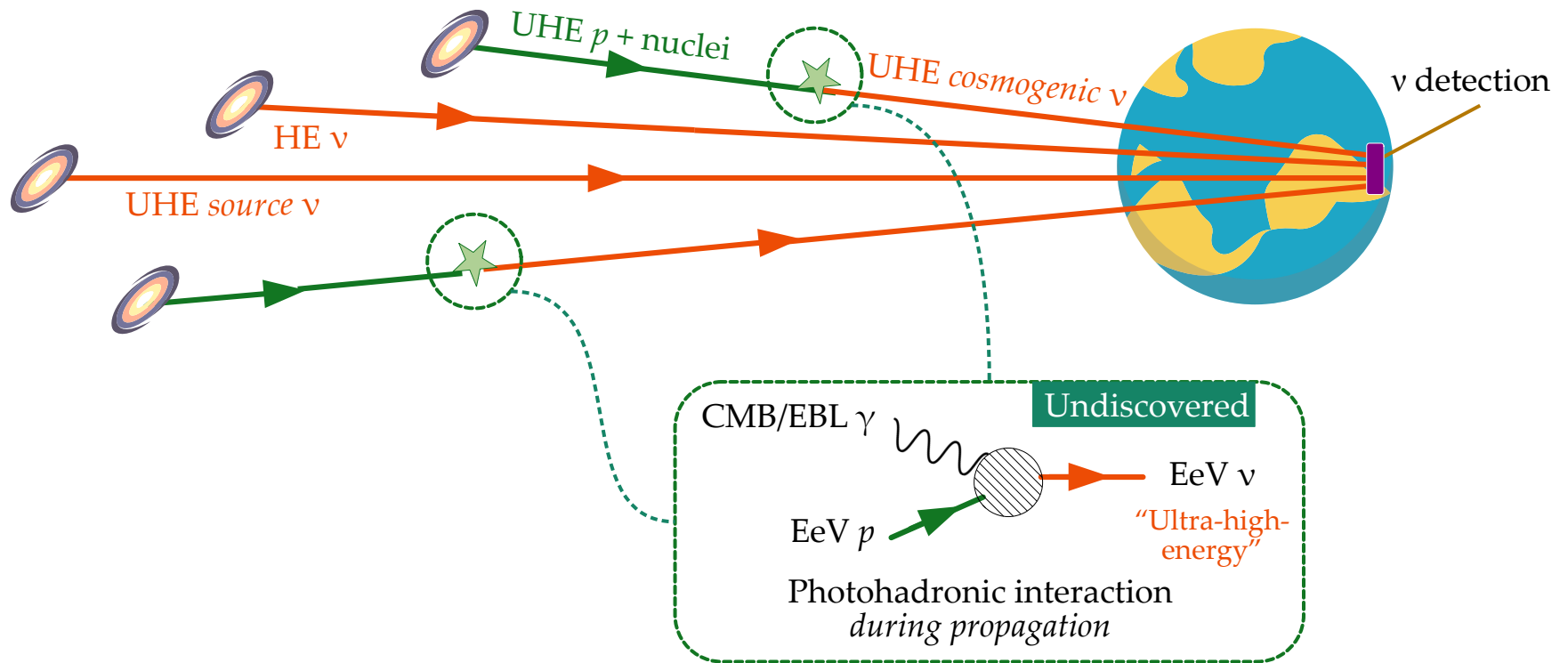
$\text{EeV } \nu$

"Ultra-high-energy"

Photohadronic or  $pp$  interaction  
inside the source

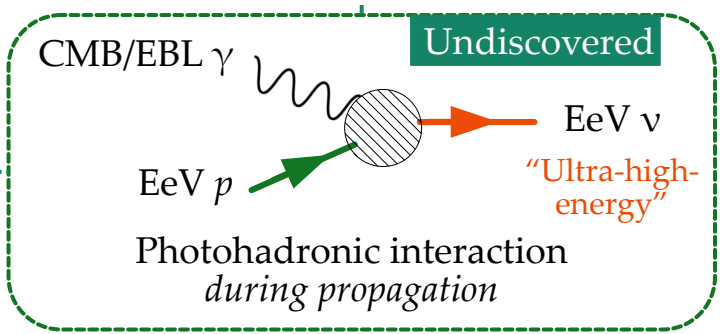
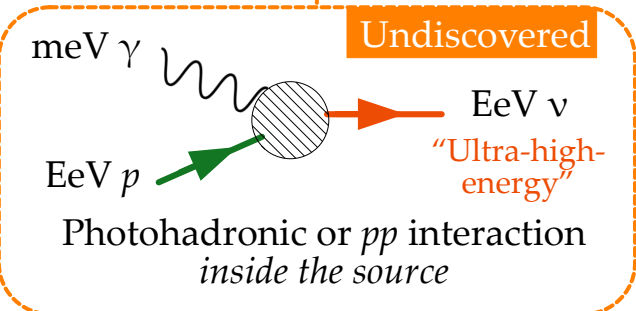
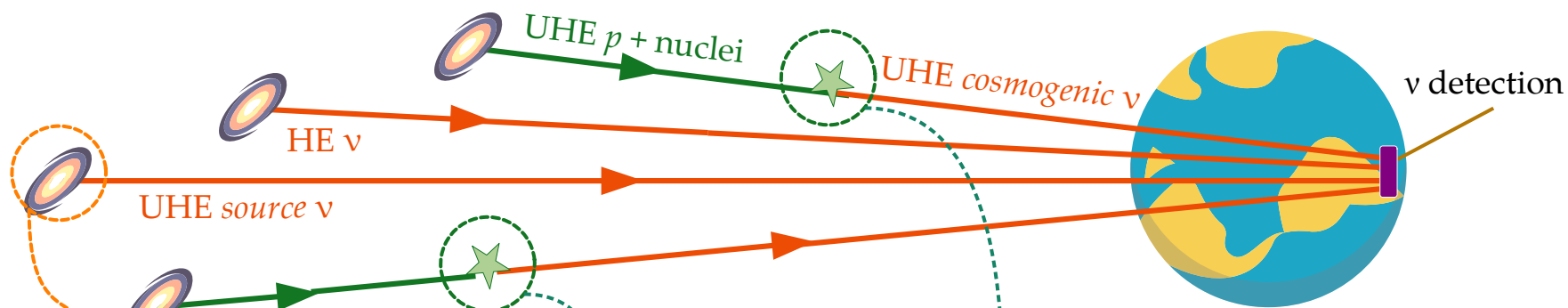
Redshift ←

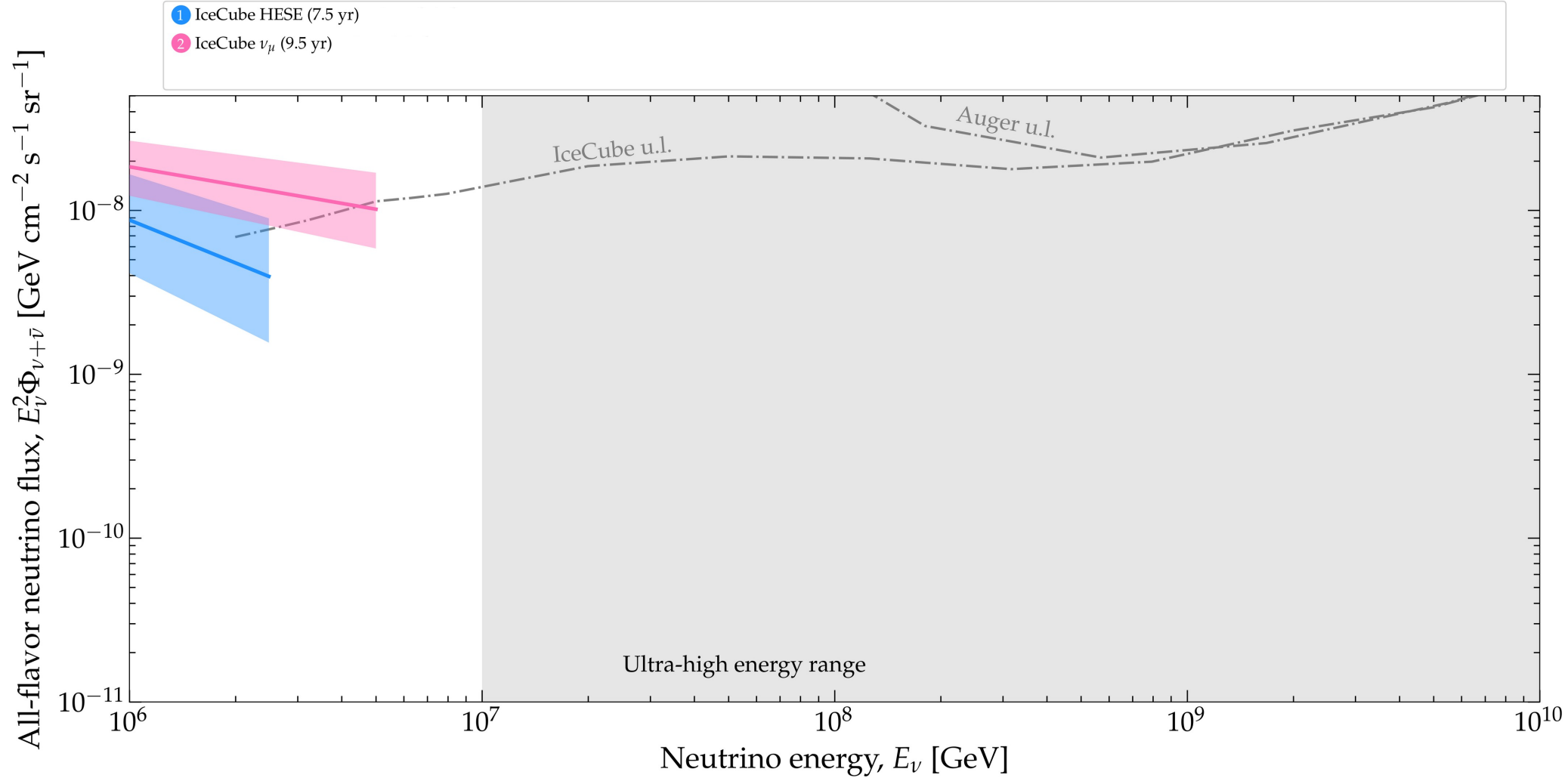
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Redshift ←

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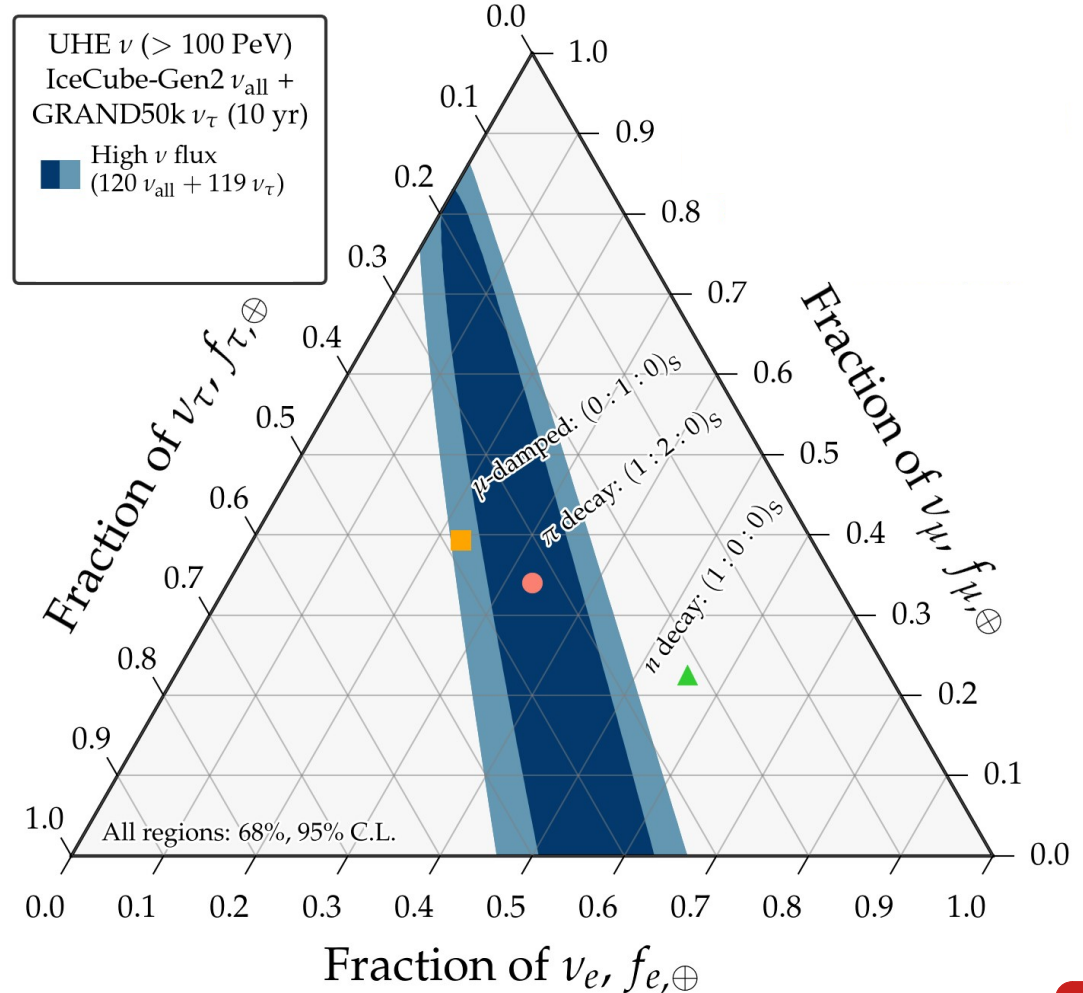




# Manufacturing UHE flavor sensitivity with two detectors

What if future UHE radio-detection neutrino telescopes cannot see flavor?

Then we combine two of detectors:

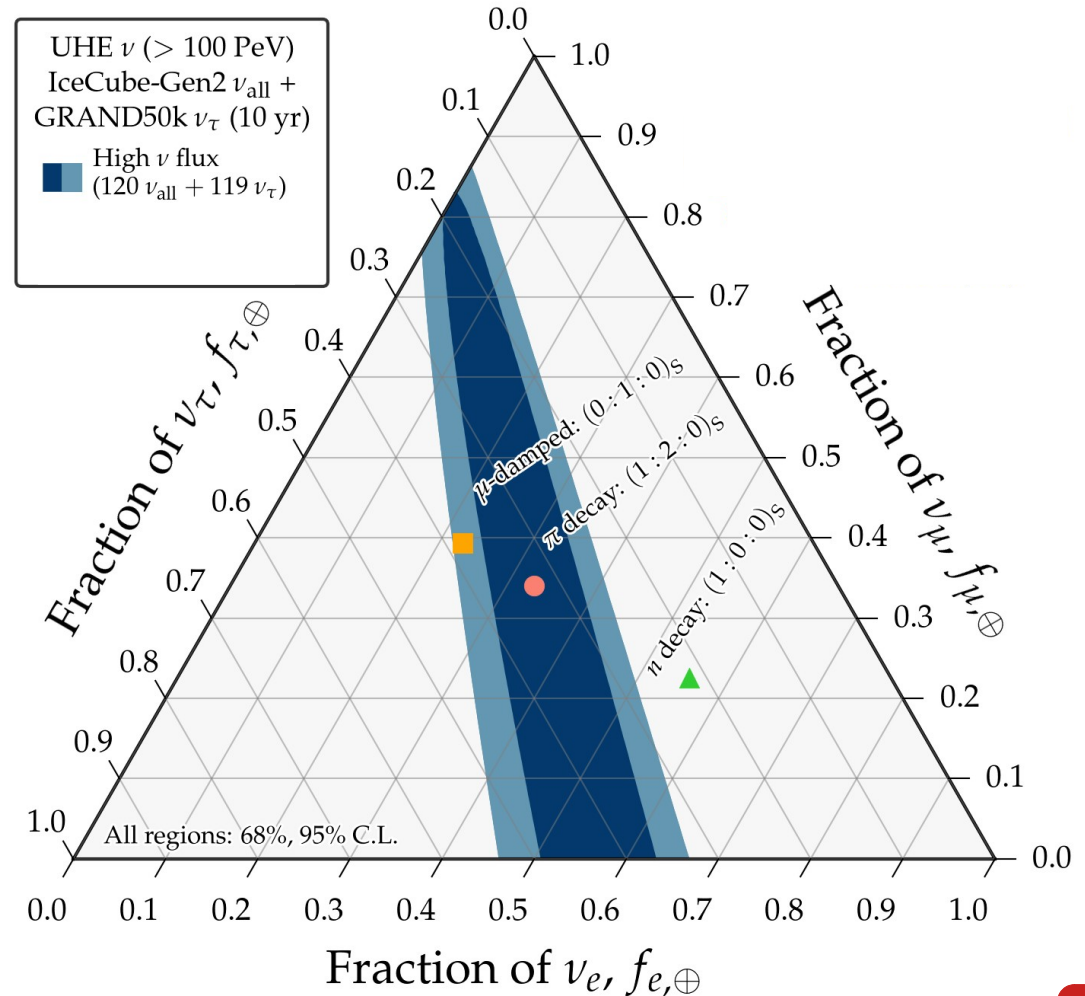


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indistinct detection of all flavors  
by IceCube-Gen2 (radio)



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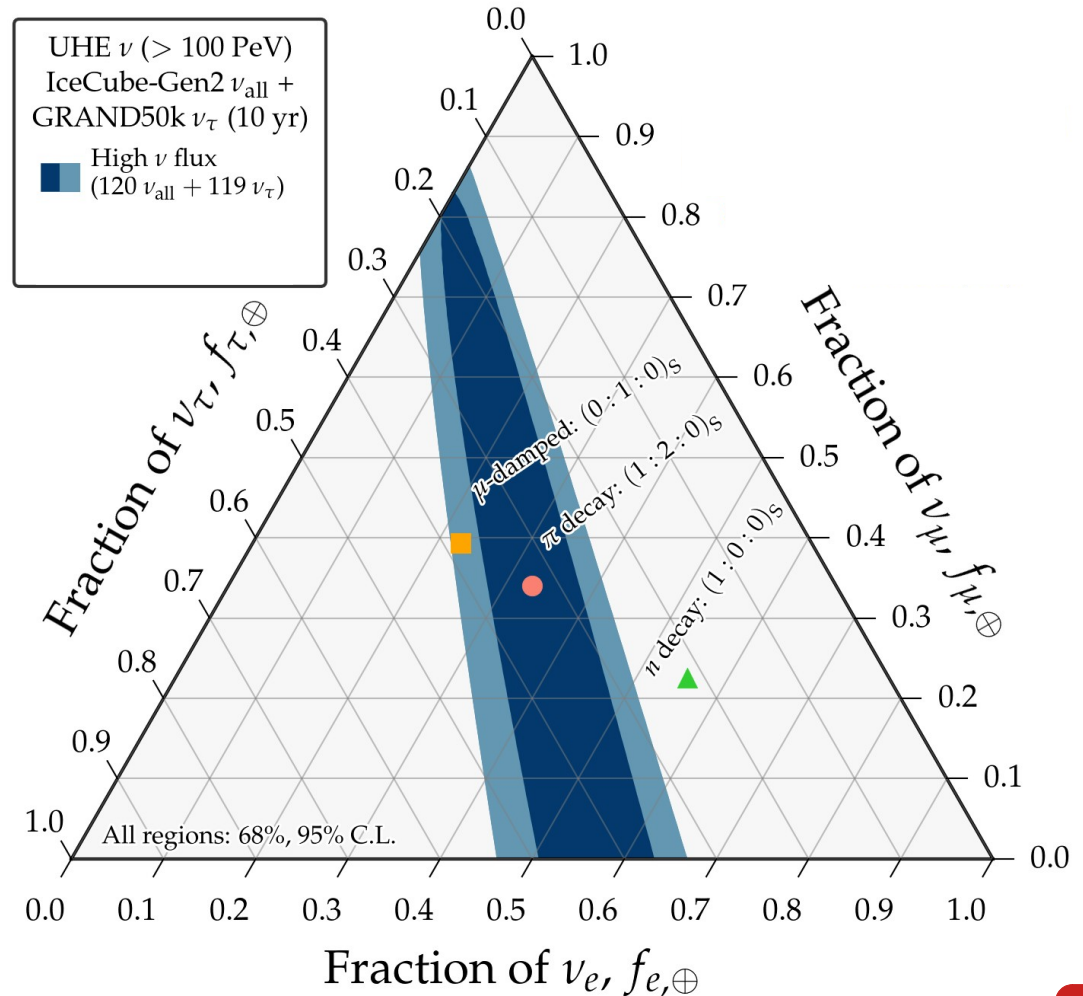
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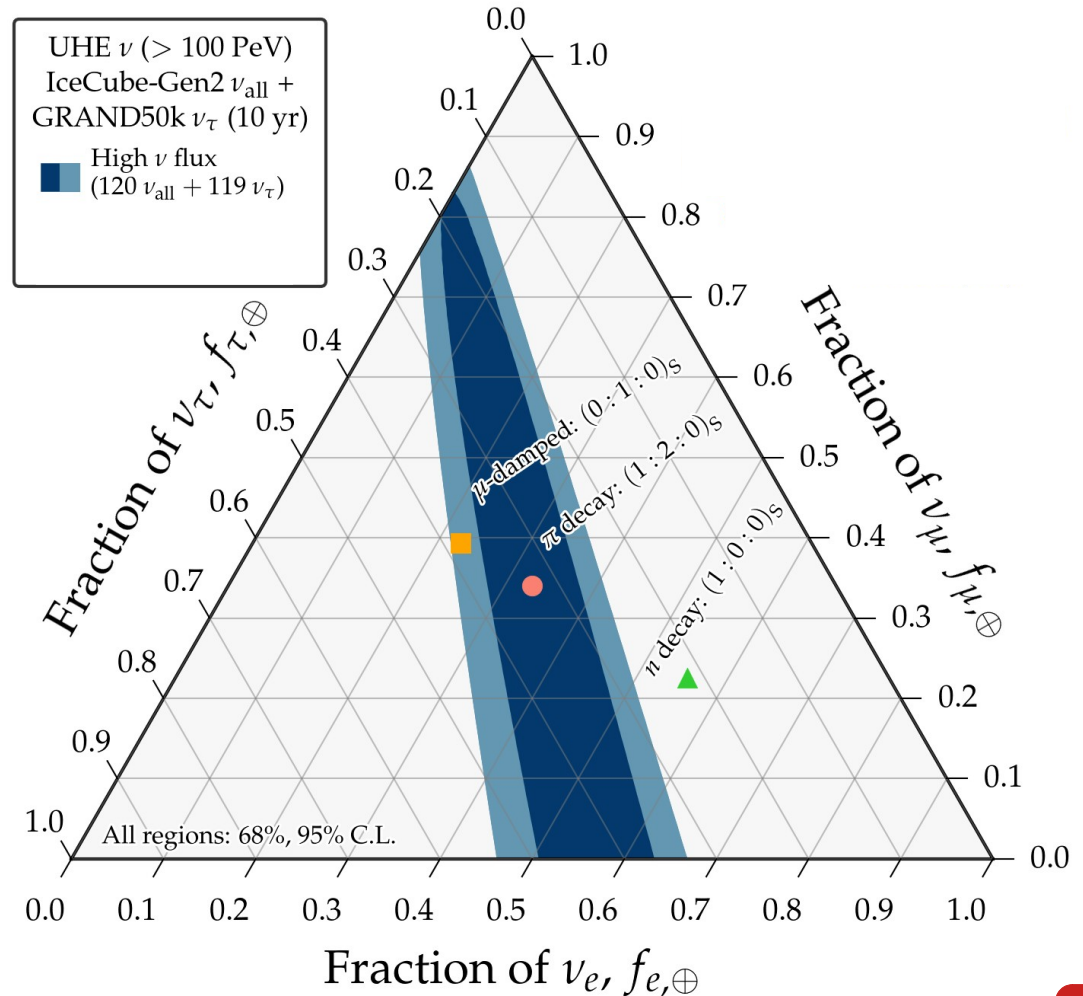
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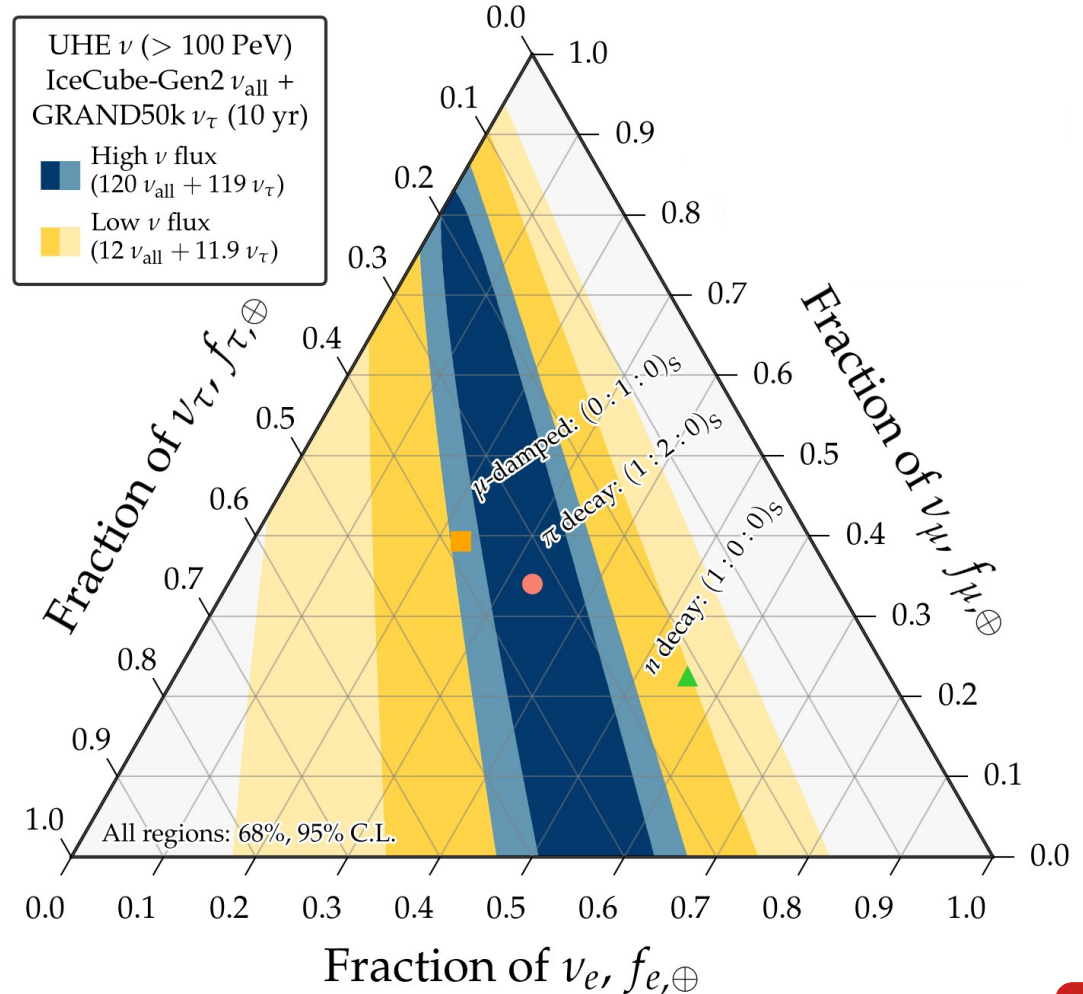
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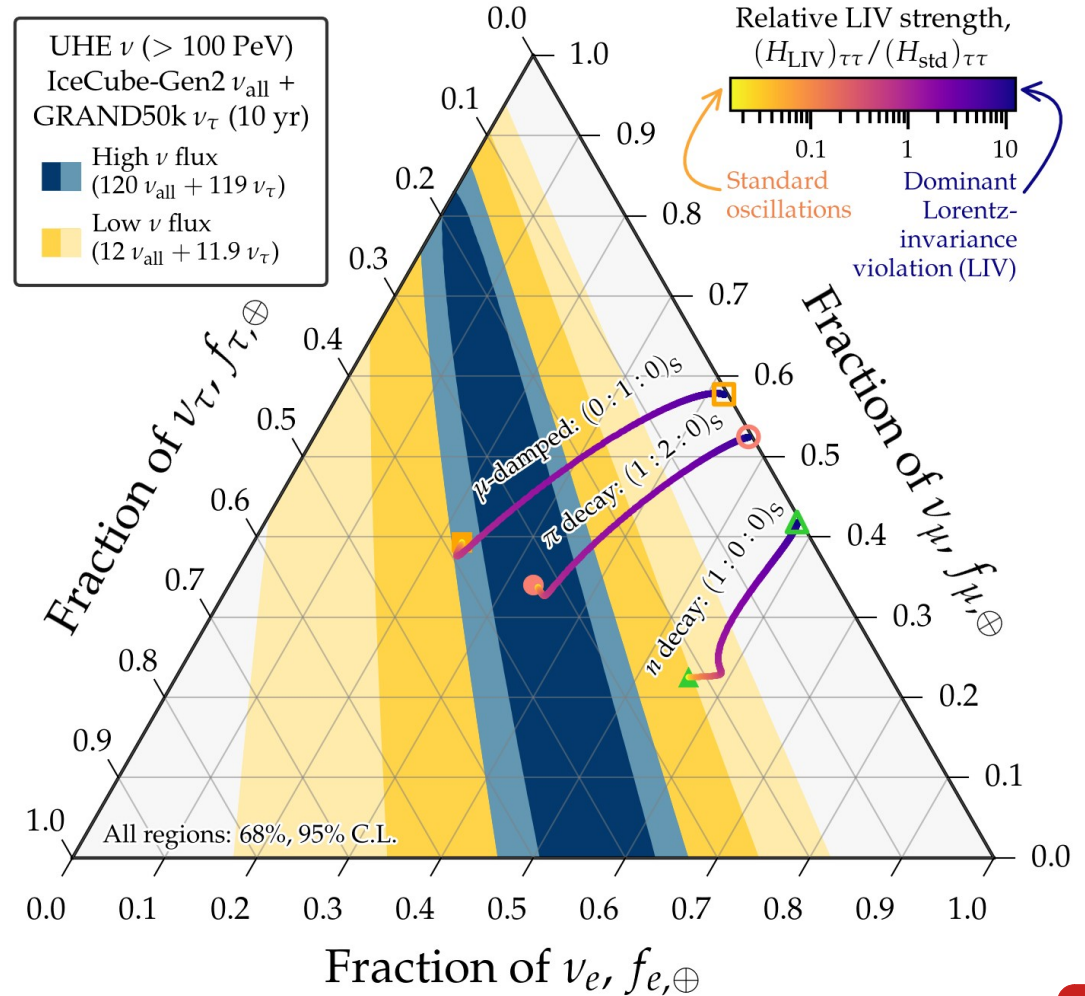
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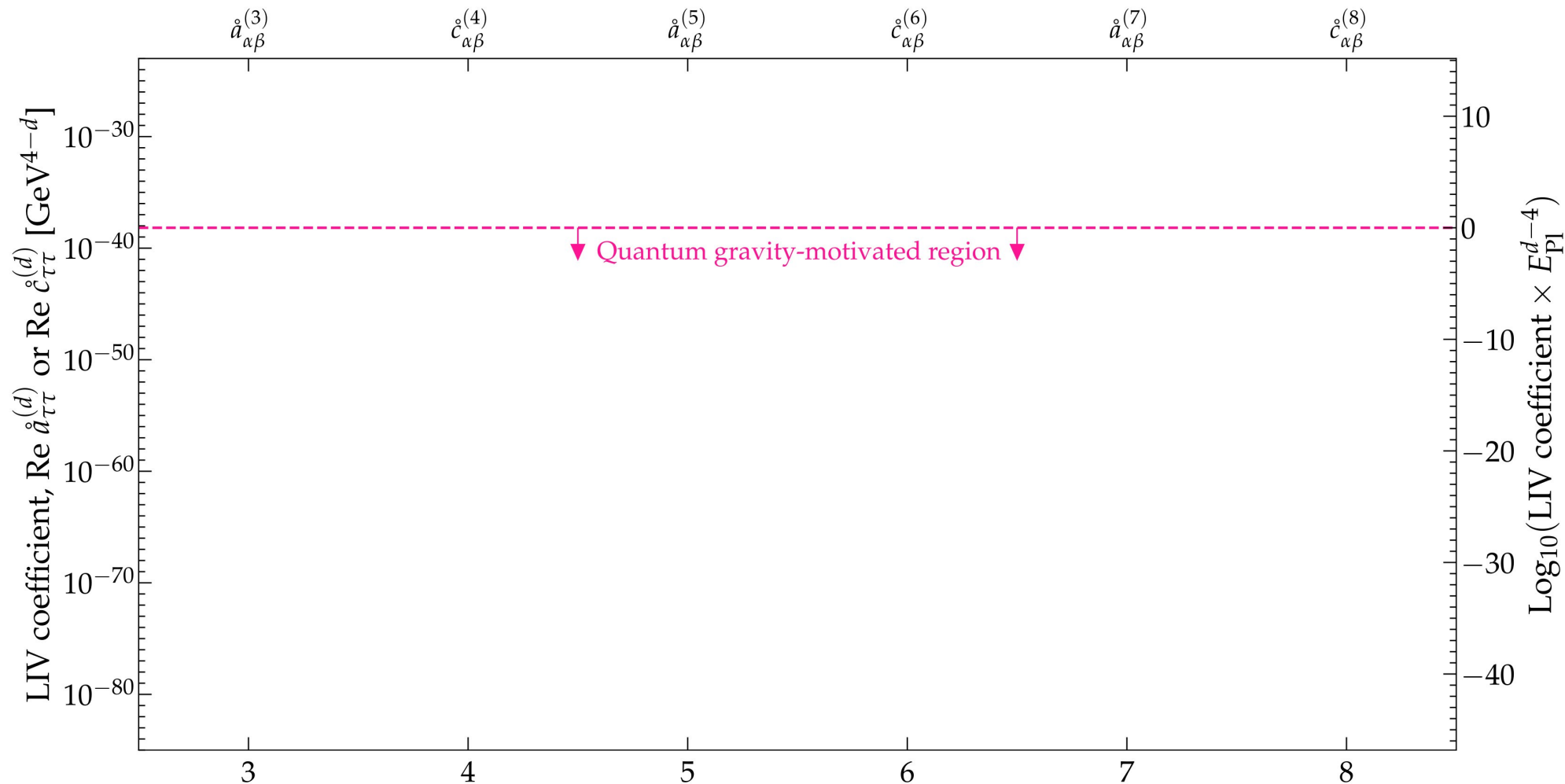
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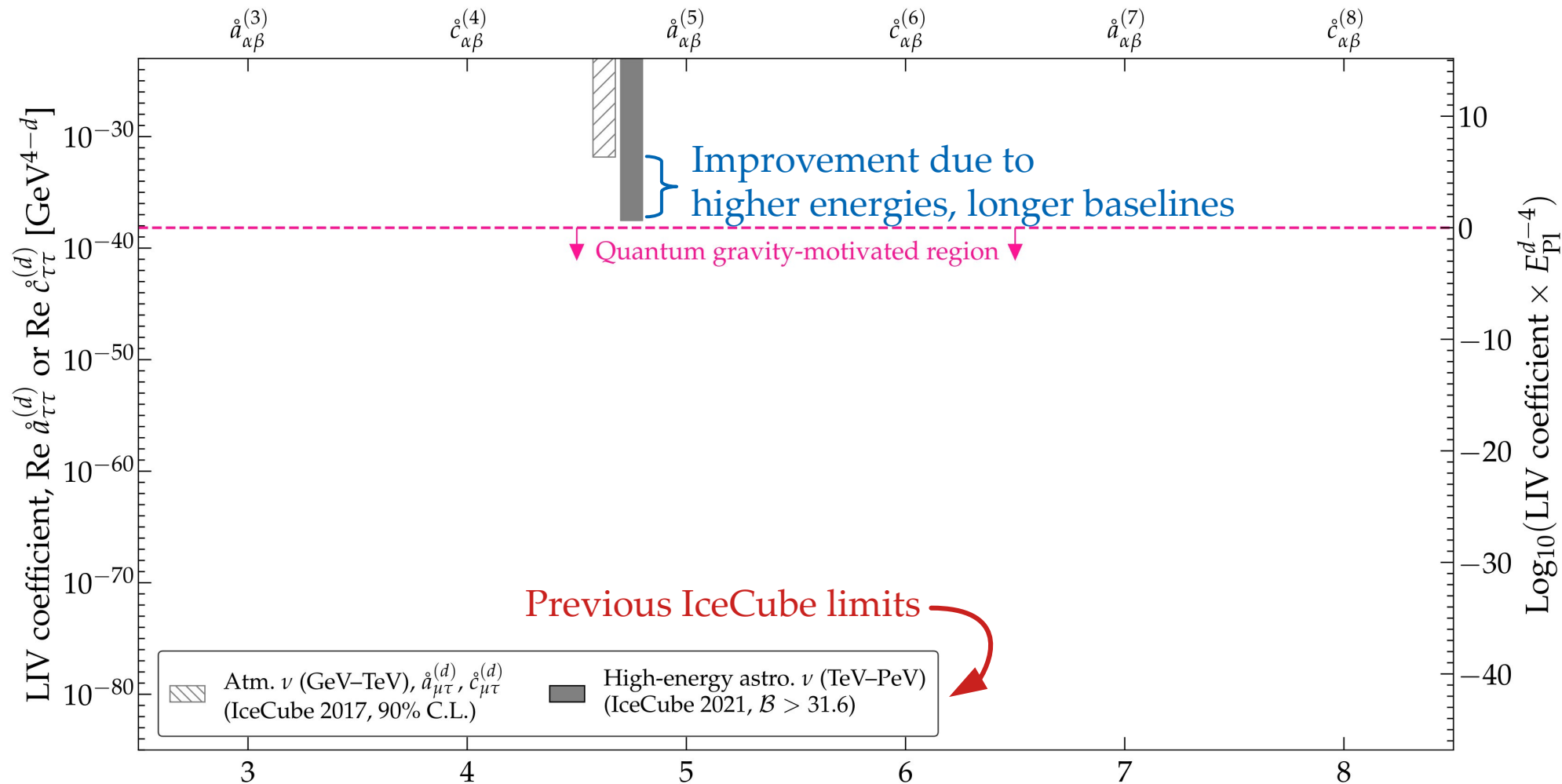
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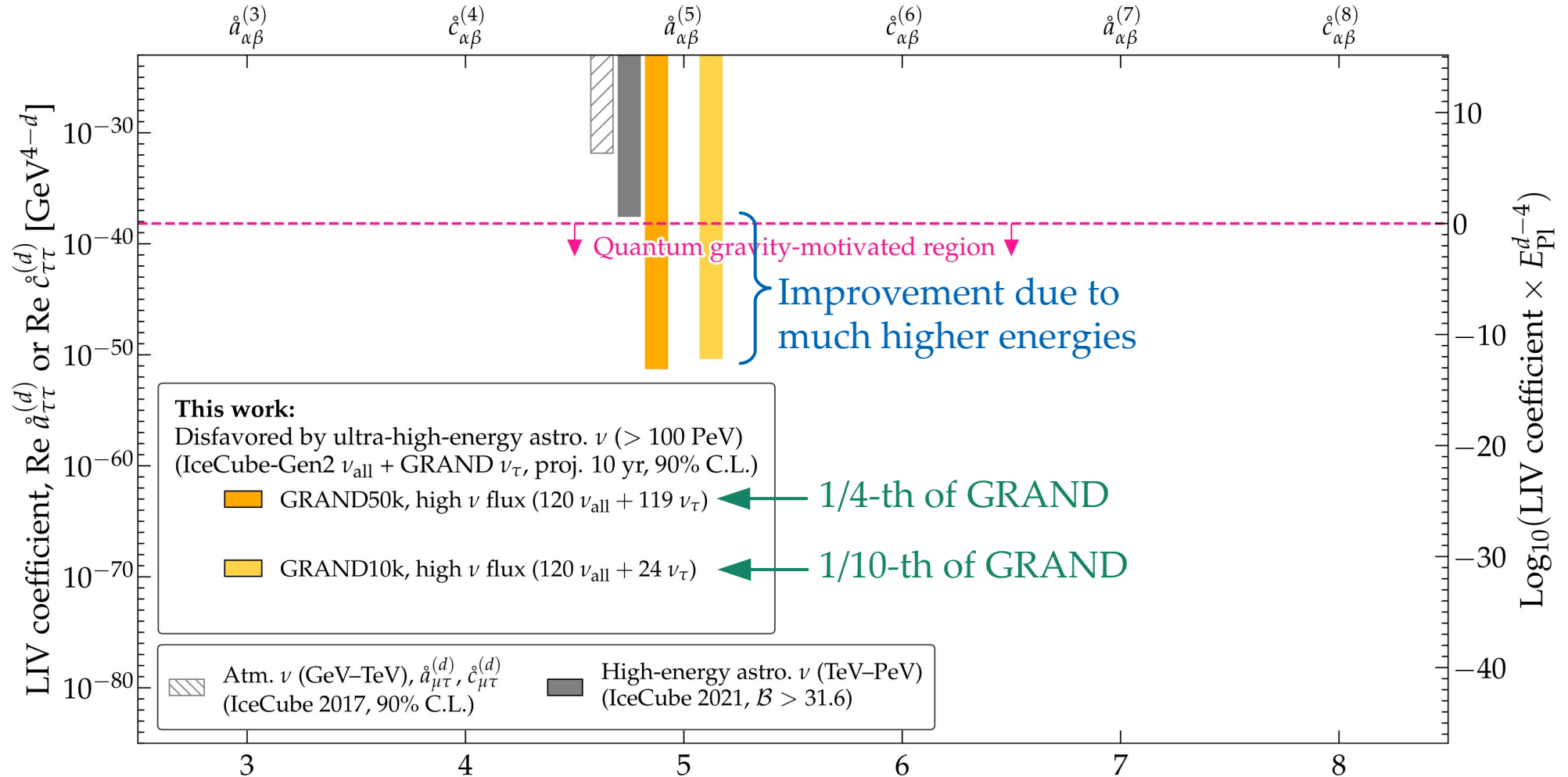
# Lorentz-invariance violation at ultra-high energies



# Lorentz-invariance violation at ultra-high energies

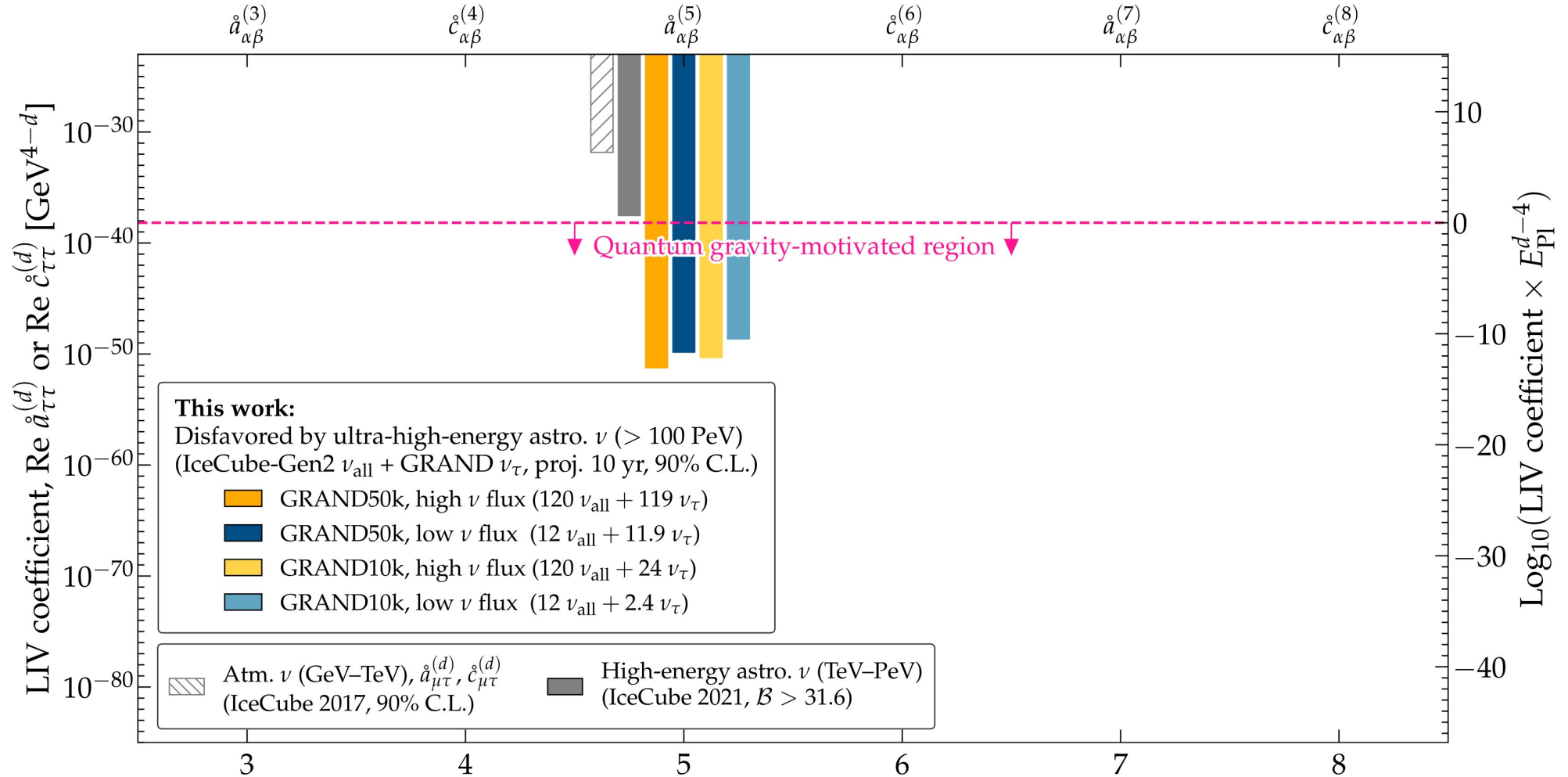


# Lorentz-invariance violation at ultra-high energies

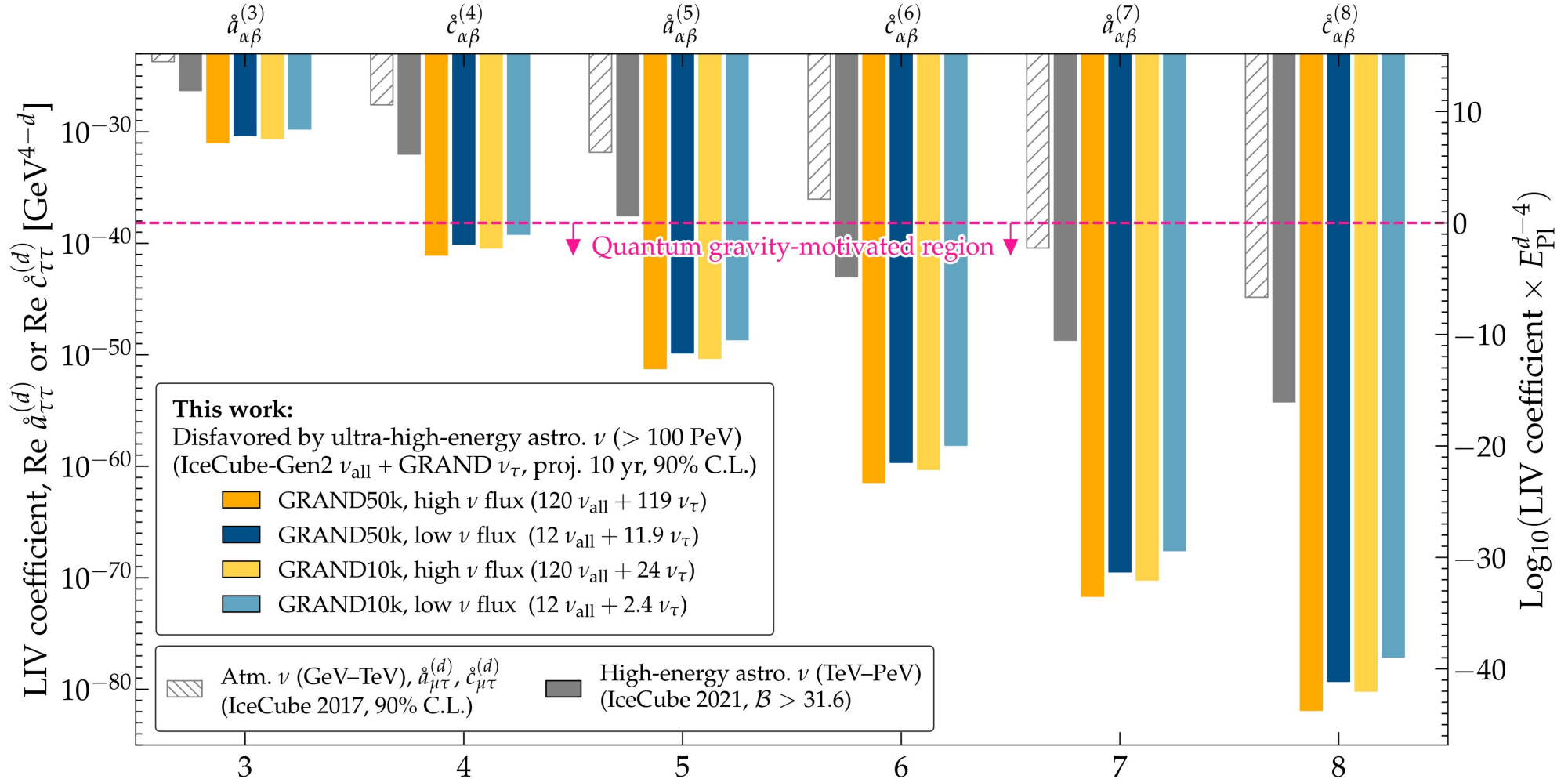


Dimension of Lorentz invariance-violation (LIV) operator,  $d$

# Lorentz-invariance violation at ultra-high energies

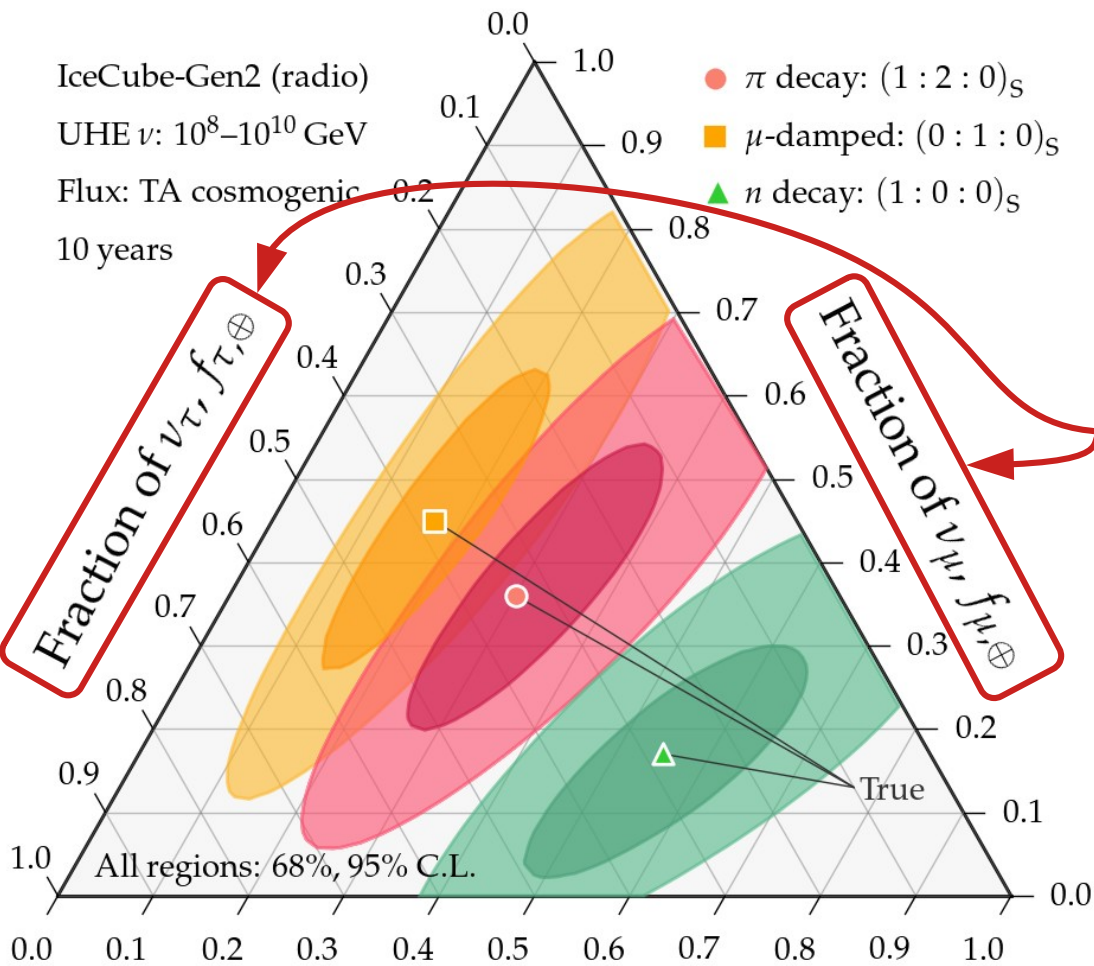


# Lorentz-invariance violation at ultra-high energies



# IceCube-Gen2 (radio) alone might measure flavor

Fraction of  $\nu_e$   
 Showers are elongated due to the LPM effect



Fraction of  $\nu_\mu + \nu_\tau$   
 Secondary muons and tauons create showers that hit >1 radio station

Fraction of  $\nu_e, f_{e, \oplus}$