Introduction to multi-messenger astrophysics

Mauricio Bustamante

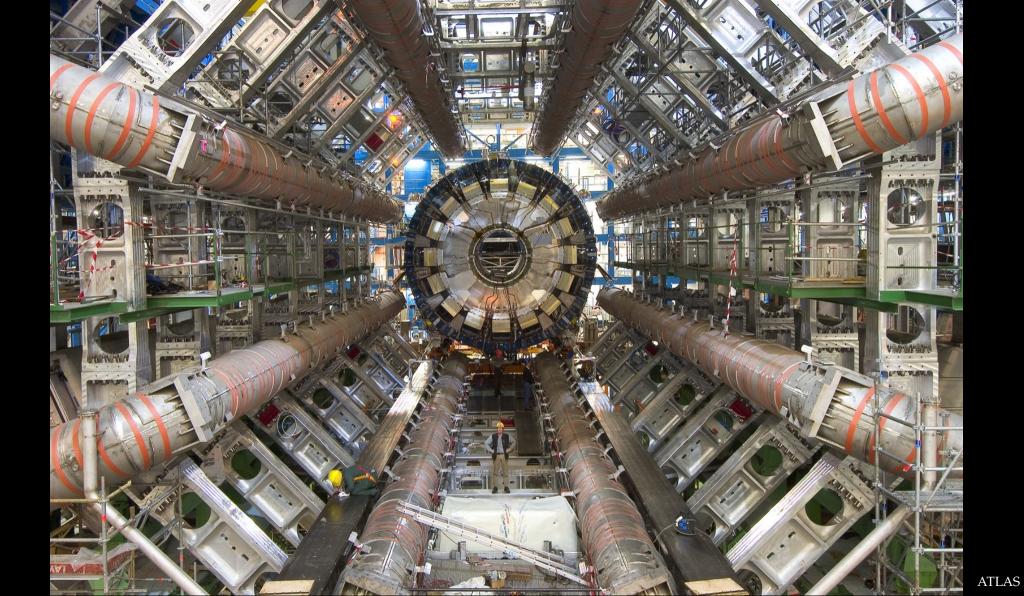
Niels Bohr Institute, University of Copenhagen

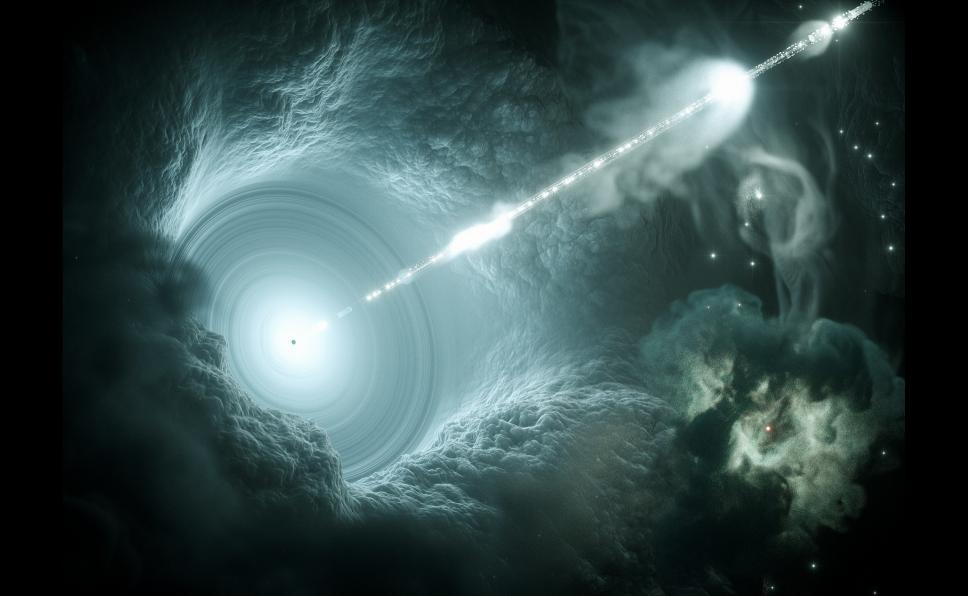
Spåtind 2025 Skeikampen, Norway, January 02-07, 2025

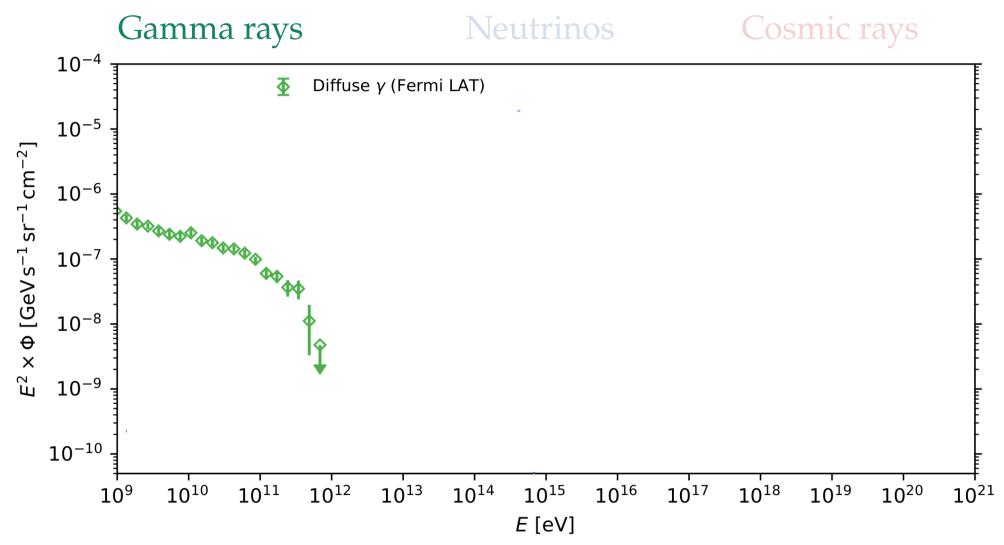


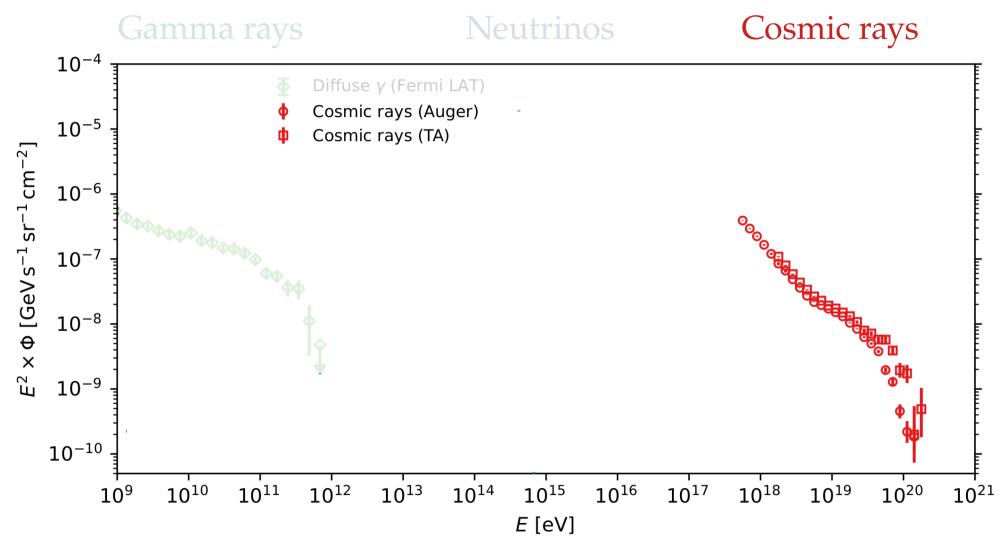
VILLUM FONDEN

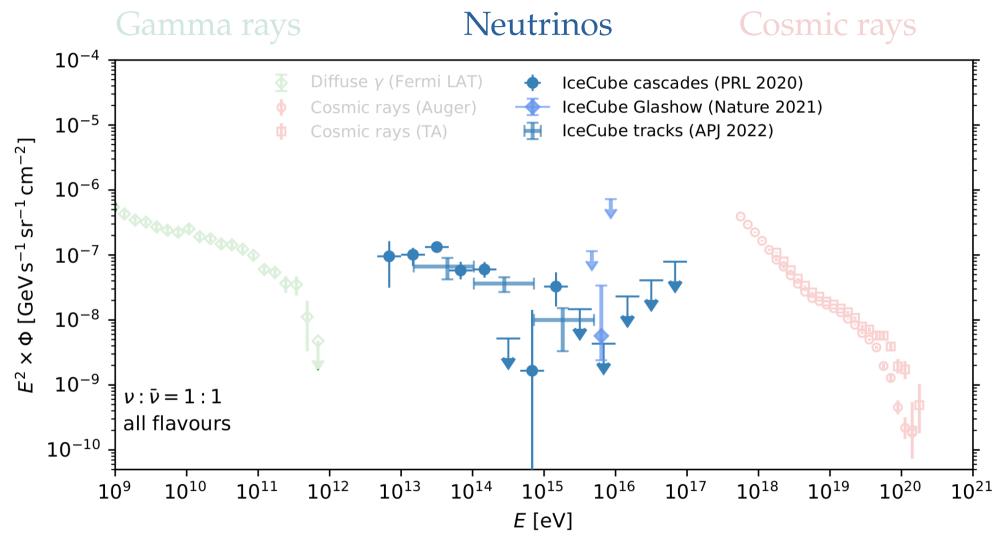


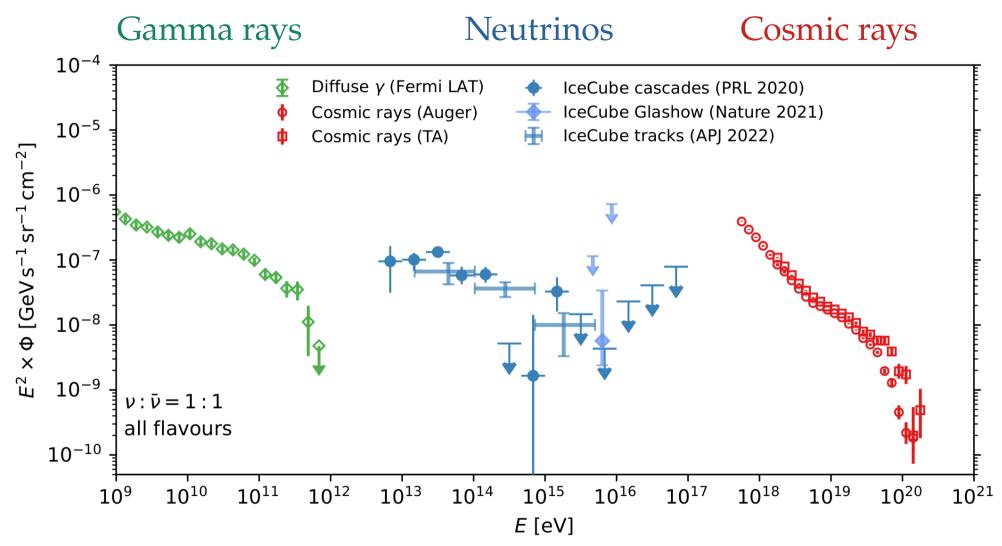


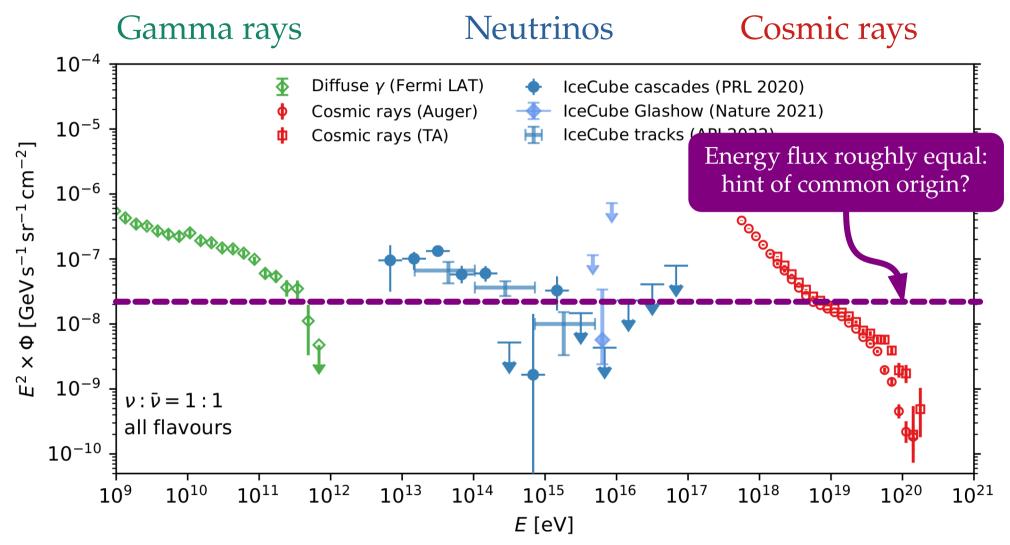




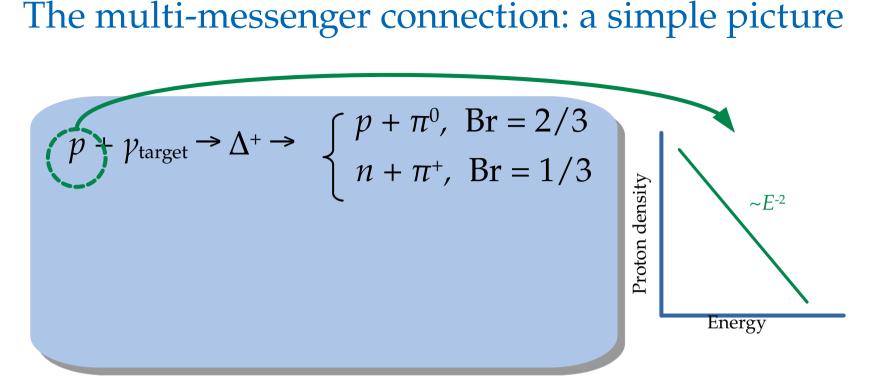


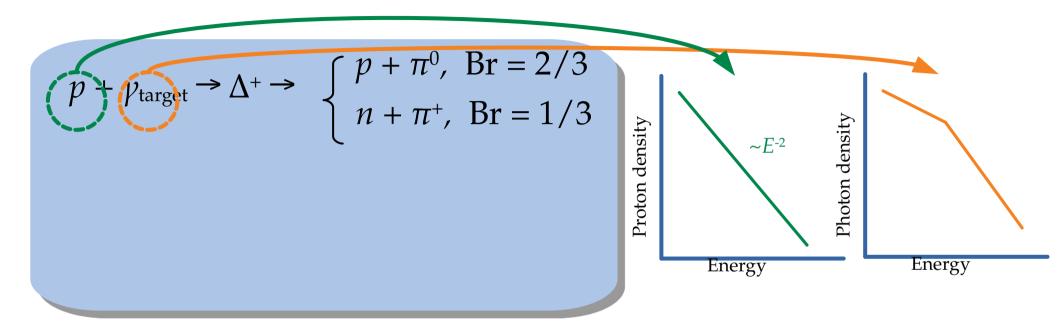


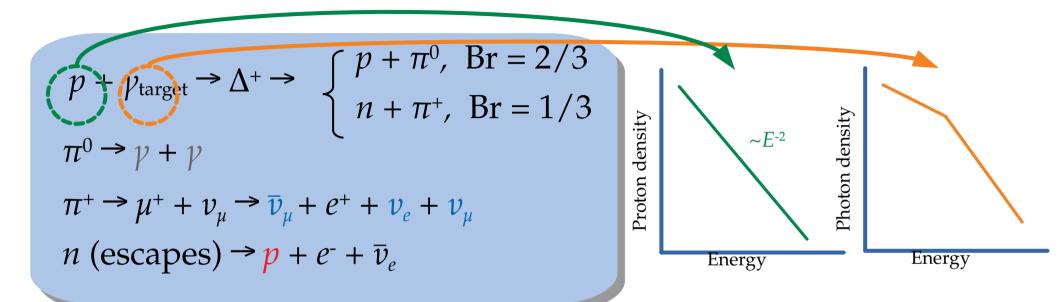




$$p + p_{\text{target}} \rightarrow \Delta^{+} \rightarrow \begin{cases} p + \pi^{0}, \text{ Br} = 2/3\\ n + \pi^{+}, \text{ Br} = 1/3 \end{cases}$$





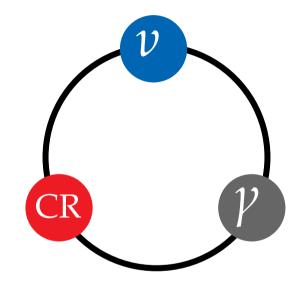


$$p + \gamma_{\text{target}} \rightarrow \Delta^{+} \rightarrow \begin{cases} p + \pi^{0}, & \text{Br} = 2/3 \\ n + \pi^{+}, & \text{Br} = 1/3 \end{cases}$$

$$\pi^{0} \rightarrow \gamma + \gamma$$

$$\pi^{+} \rightarrow \mu^{+} + \nu_{\mu} \rightarrow \bar{\nu}_{\mu} + e^{+} + \nu_{e} + \nu_{\mu}$$

$$n \text{ (escapes)} \rightarrow p + e^{-} + \bar{\nu}_{e}$$



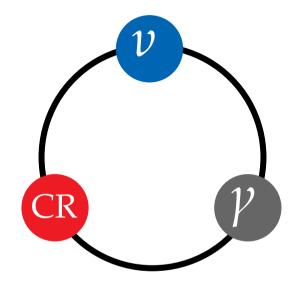
Neutrino energy = Proton energy / 20 Gamma-ray energy = Proton energy / 10

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1 PeV 20 PeV Neutrino energy = Proton energy / 20

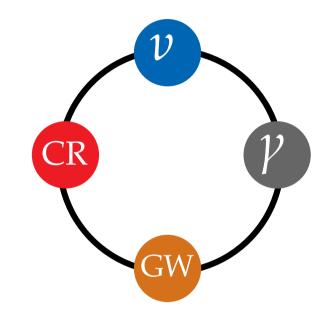
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1 PeV 20 PeV

Neutrino energy = Proton energy / 20 Gamma-ray energy = Proton energy / 10













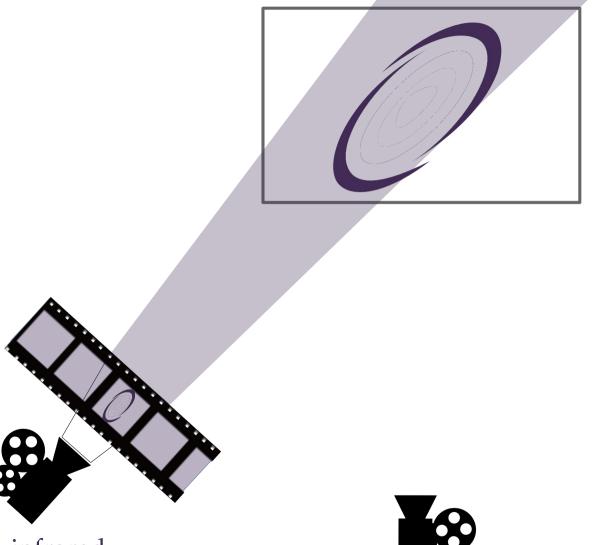








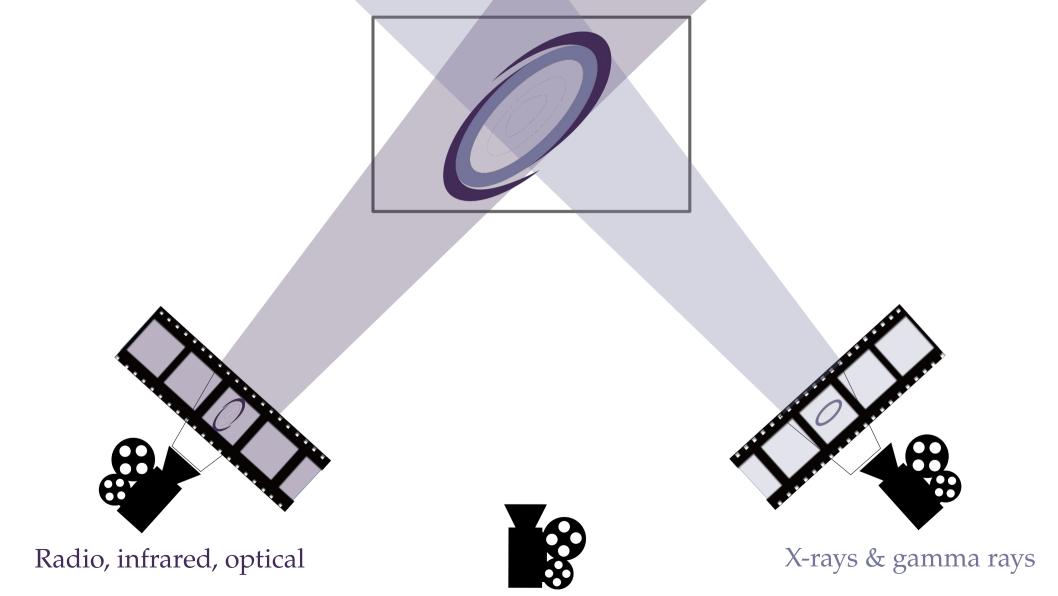


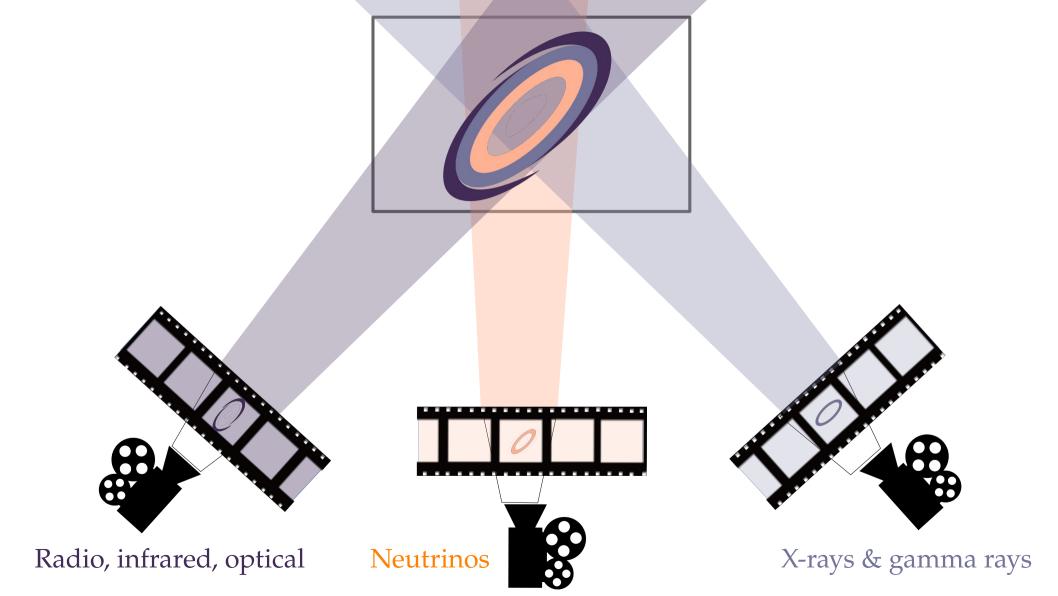












Gravitational waves Radio, infrared, optical X-rays & gamma rays Neutrinos

Gamma rays

Neutrinos

UHE cosmic rays

Gamma rays Neutrinos UHE cosmic rays
Point back at sources Yes Yes No

	Gamma rays	Neutrinos	UHE cosmic rays
Point back at sources	Yes	Yes	No
Size of horizon	10 kpc (at PeV)	Size of the Universe	100 Mpc (> 40 EeV)

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Energy degradation	Severe	Tiny	Severe

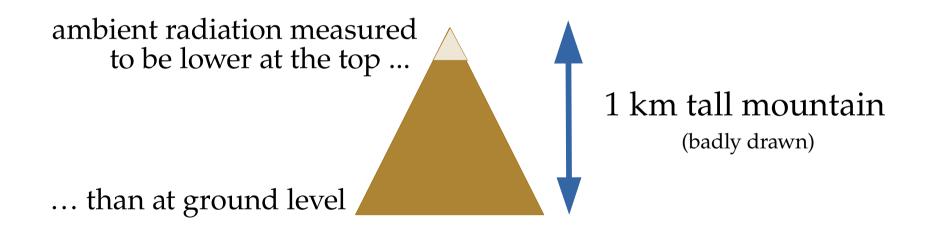
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Point back at sources	Yes	Yes	No
Size of horizon	10 kpc (at PeV)	Size of the Universe	100 Mpc (> 40 EeV)
Energy degradation	Severe	Tiny	Severe
Relative ease to detect	Easy	Hard	Easy

Ultra-high-energy cosmic rays

Cosmic rays discovered

The state at the beginning of the 20th century:

- (1) ambient radiation was already known to exist
- (2) believed to be mainly coming from the ground

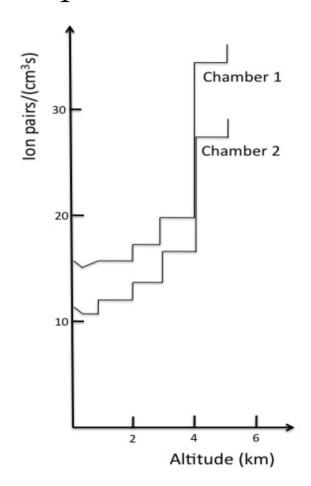


Problem: they had measured *only* up to ~1 km of altitude

Physics is a risky business

Victor Hess – 1911-1913, balloon flights up to 5.3 km





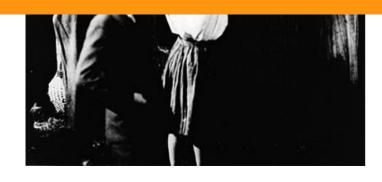
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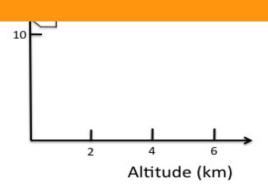
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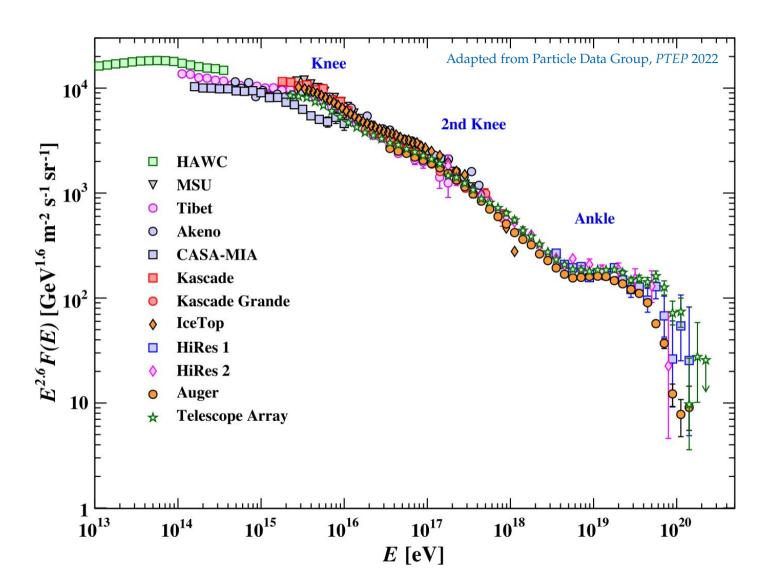
"Unknown penetrating radiation" = cosmic rays

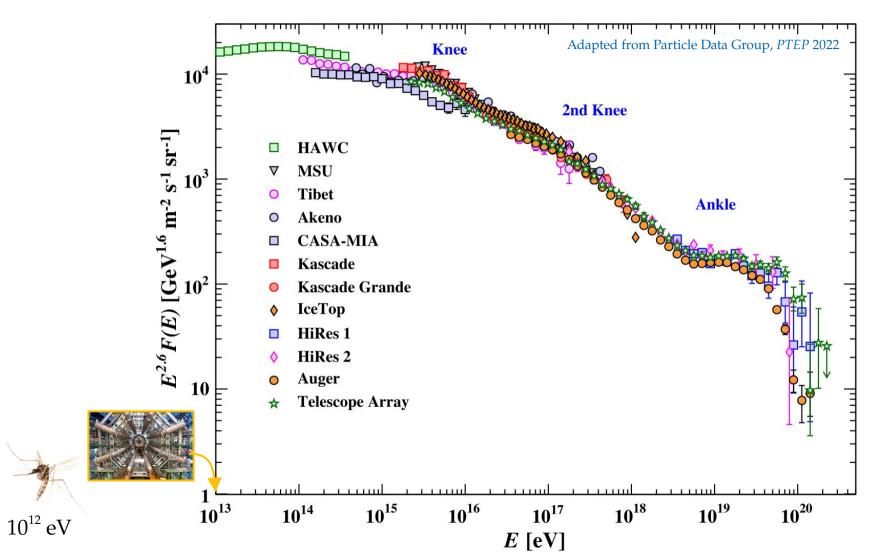
... and that's one way to get a Nobel Prize in Physics







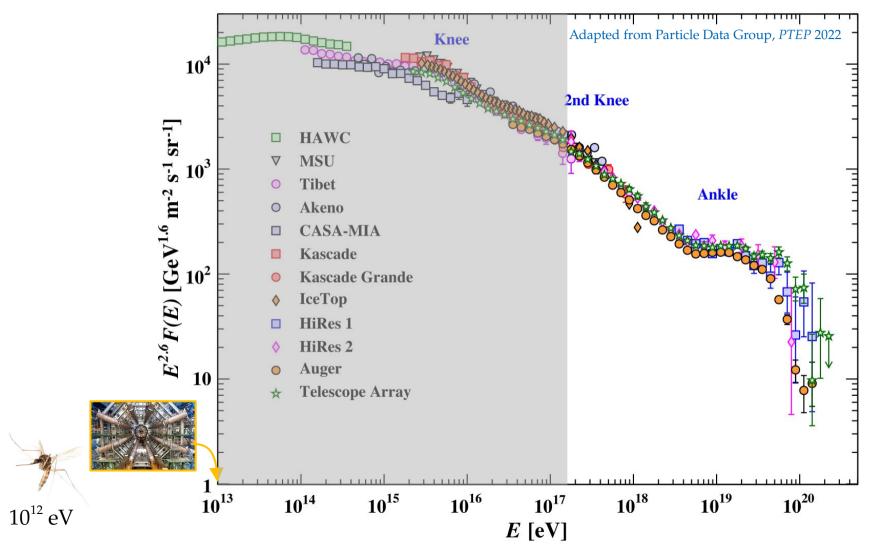




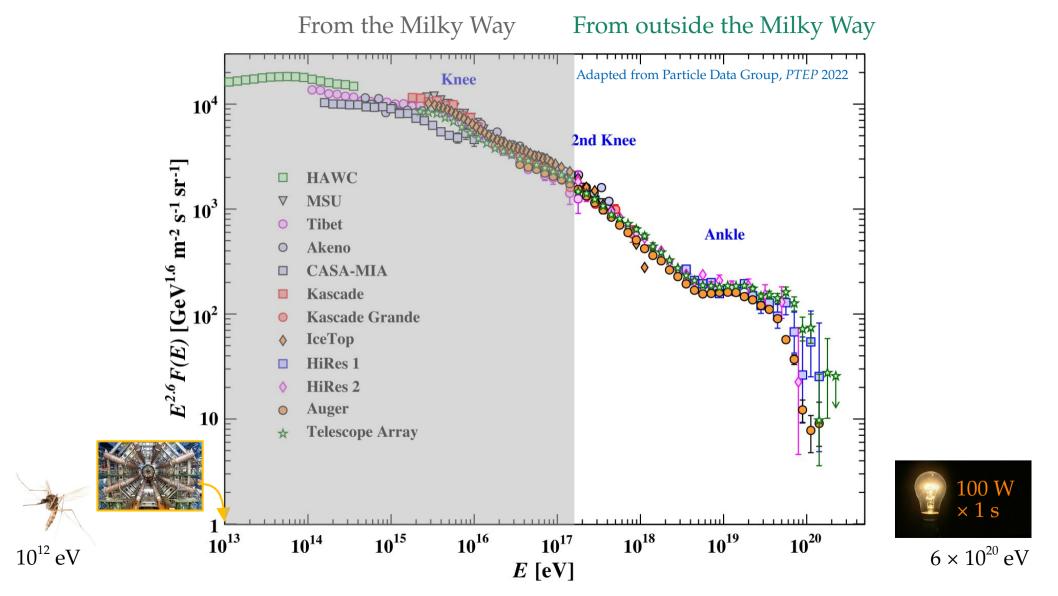


 $6 \times 10^{20} \,\mathrm{eV}$

From the Milky Way





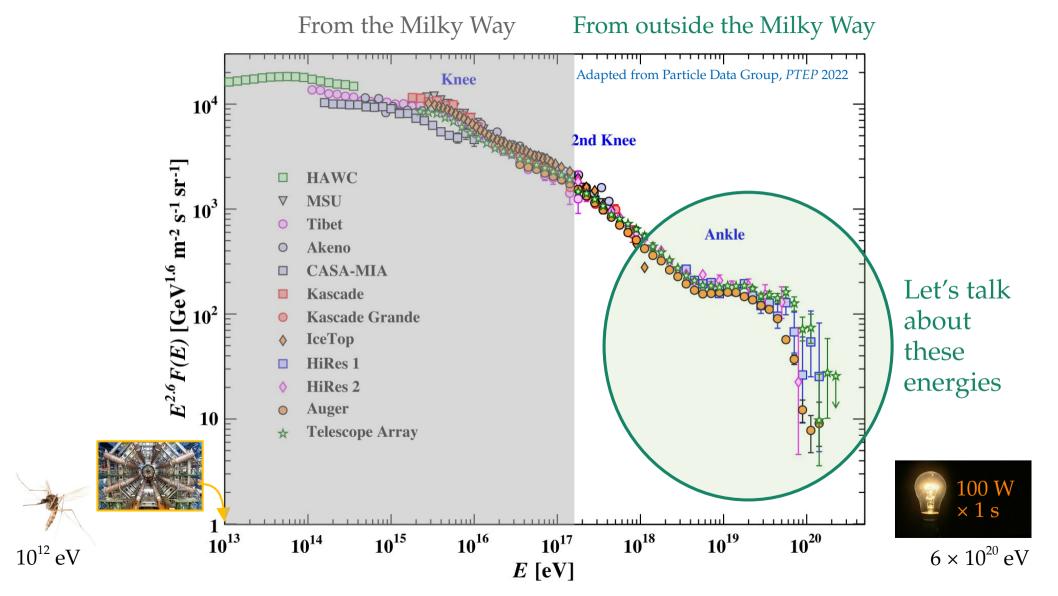


From the Milky Way From outside the Milky Way Adapted from Particle Data Group, PTEP 2022 Knee 10^4 2nd Knee $E^{2.6}F(E)$ [GeV^{1.6} m⁻² s⁻¹ sr⁻¹ **HAWC MSU Tibet Ankle** Akeno **CASA-MIA** Kascade **Kascade Grande IceTop** HiRes 1 HiRes 2 Auger **Telescope Array** ► Extensive-air-shower detectors (*e.g.*, Auger) (Old-school) balloon and satellite detectors (e.g., AMS-02) 10¹³ 10^{20} 10^{15} 10^{16} 10^{18} 10^{19} 10^{14} 10^{17} $10^{12} \, eV$

E [eV]



From the Milky Way From outside the Milky Way Adapted from Particle Data Group, PTEP 2022 Knee 10^4 2nd Knee $E^{2.6}F(E)$ [GeV^{1.6} m⁻² s⁻¹ sr⁻¹ **HAWC MSU Tibet Ankle** Akeno **CASA-MIA** Kascade **Kascade Grande IceTop** HiRes 1 HiRes 2 1 km⁻² century⁻¹ Auger 1 km⁻² yr⁻¹ **Telescope Array** 100 W × 1 s 10^{20} 10¹³ 10^{18} 10^{19} 10^{15} 10^{16} 10^{14} 10^{17} $10^{12} \, eV$ $6 \times 10^{20} \, \text{eV}$ E [eV]



What are they?

Protons and nuclei with energies above 10¹⁷ eV

Is that a lot?

Yes.

10⁵–10⁸ times higher than LHC protons

A 10²⁰-eV <u>proton</u> has the kinetic energy of a kicked football

We know no particles more energetic than UHECRs

So what's making them?

Good question. We don't know.

Whatever it is, it is one of the most violent processes in the Universe

(Ok, fine: extragalactic non-thermal astrophysical sources that act as cosmic particle accelerators)

Why is it so hard?

UHECRs don't travel in straight lines (the Universe is magnetized)

+

UHECRs are rare (the Universe is opaque to them)

Are we getting closer?

Yes.

We detect a growing number of UHECRs and

we can use neutrinos, too (more on this later)

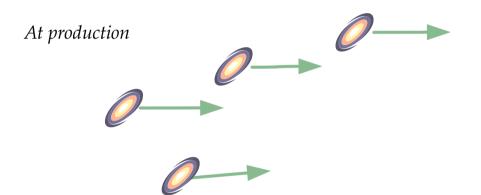
Redshift z = 0

At production:
Each source injects
UHECRs





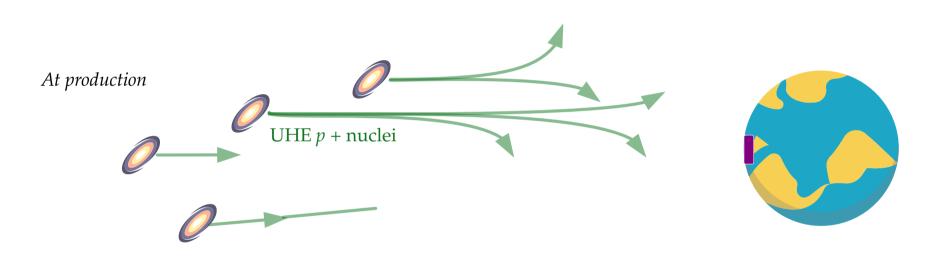
UHECR sources distributed in redshift



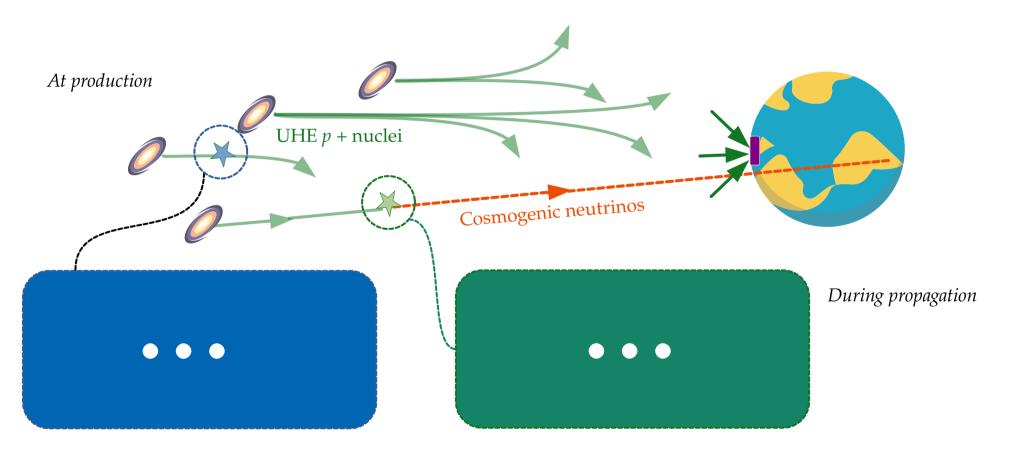


UHECR sources distributed in redshift

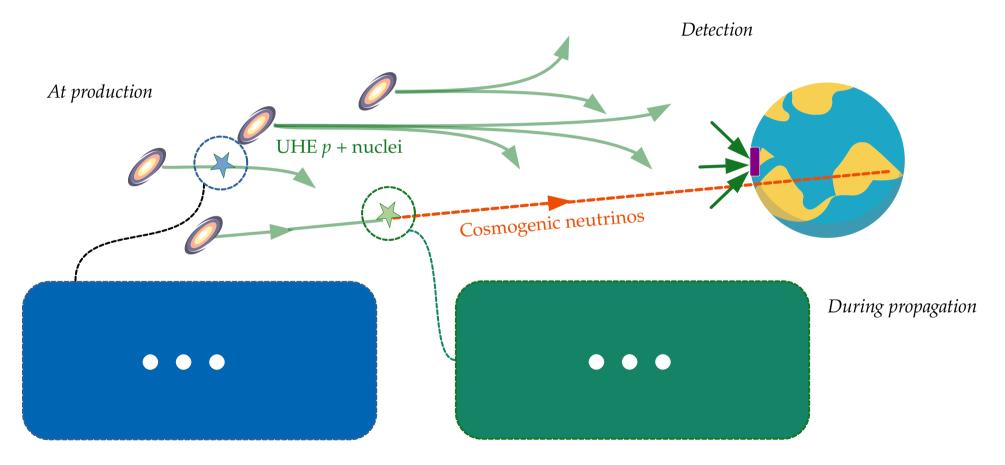
During propagation



During propagation

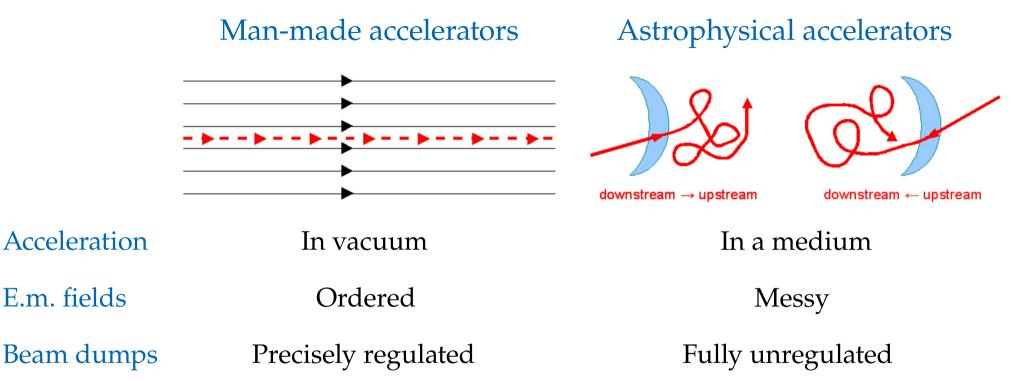


During propagation



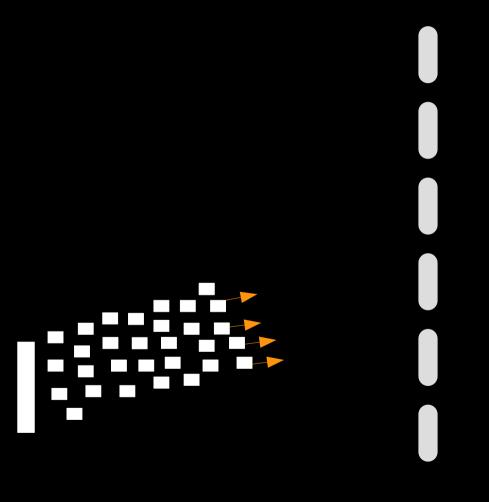
UHECR production

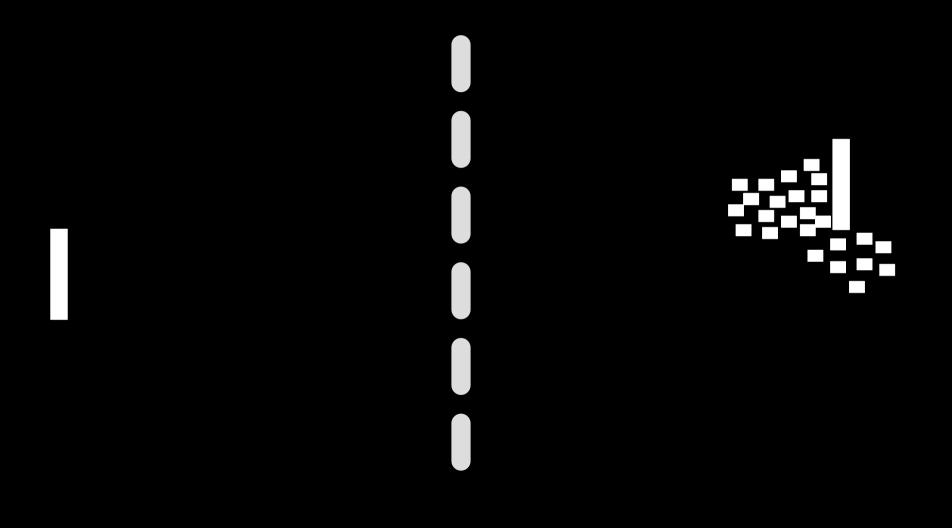
UHECR sources are messy

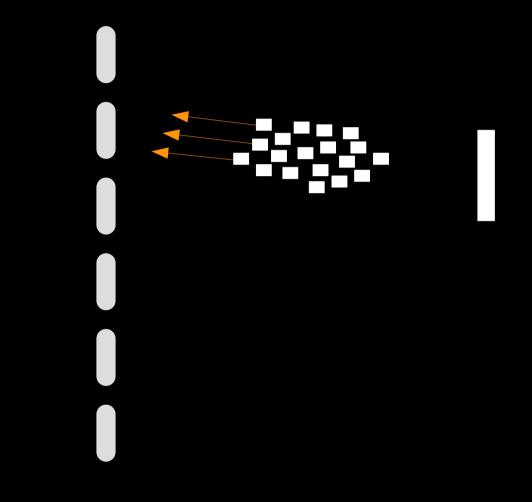


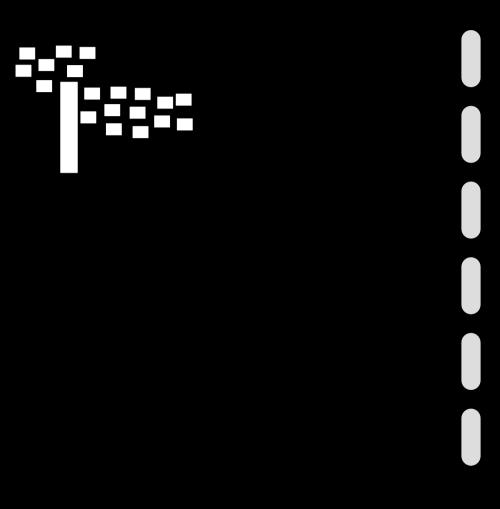
Astrophysical accelerators inevitably make high-energy secondaries

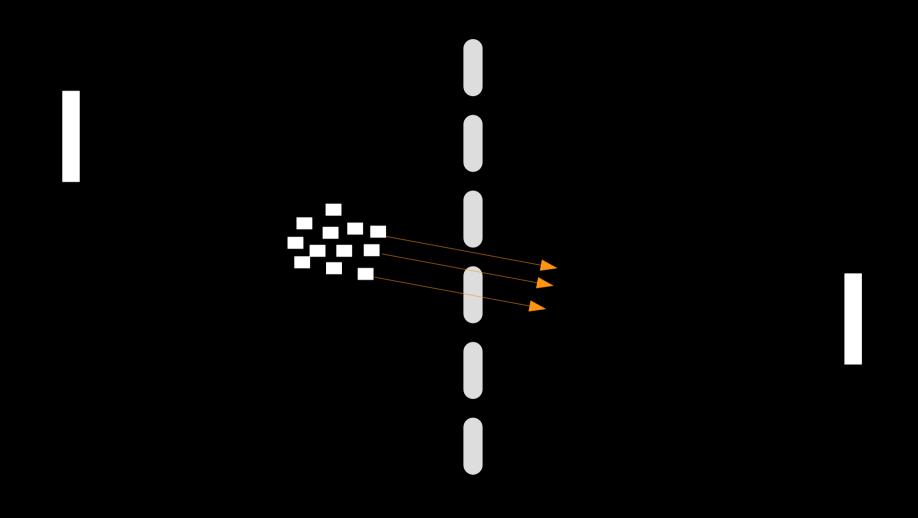














Fermi acceleration

Central emitter

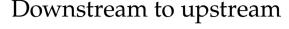
Upstream to downstream

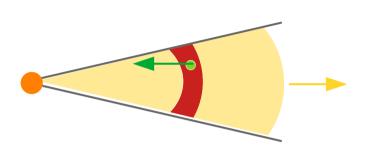
Charged particle

Shock front

In each crossing, the particle gains energy

$$\Delta E \propto v_{\rm shock}$$





Average energy of a particle after one crossing: $E = k E_0$

Probability that the particle remains in the acceleration region after one crossing: P

Relativistic outflow

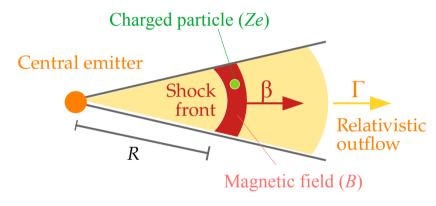
After *n* collisions, $N = N_0 P^n$ particle remain, with energy $E = E_0 k^n$

Energy spectrum: $N(E)dE \propto E^{-1 + \frac{\ln P}{\ln k}} dE$

$$\left\langle \frac{\Delta E}{E} \right\rangle = \frac{4}{3} \left(\frac{v}{c} \right)$$
 and $P = 1 - P_{\rm esc} = 1 - \frac{4}{3} \left(\frac{v}{c} \right) \Rightarrow N(E) dE \propto E^{-2} dE$

Hillas criterion

A necessary condition to accelerate charged particles is confinement within the acceleration region.

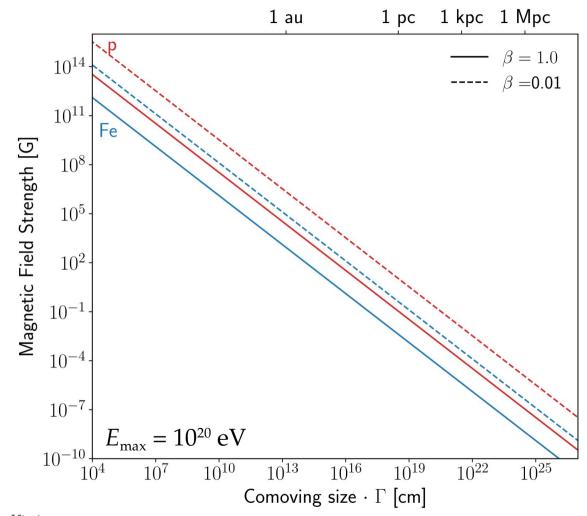


Confinement holds until

Larmor radius (R_L) = Size of region (R)

$$\frac{E_{\max}}{ZeB} = \beta \Gamma R$$

$$\Rightarrow E_{\max} = \eta^{-1} \beta \Gamma ZeBR$$
Acceleration efficiency

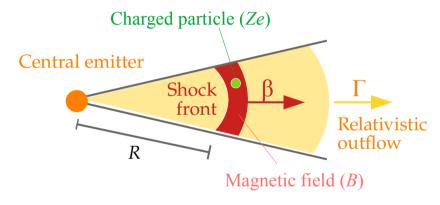


Hillas, Ann. Rev. Astron. Astrophys. 1984

Alves Batista et al. (inc. MB), Front. Astron. Space Sci. 2019

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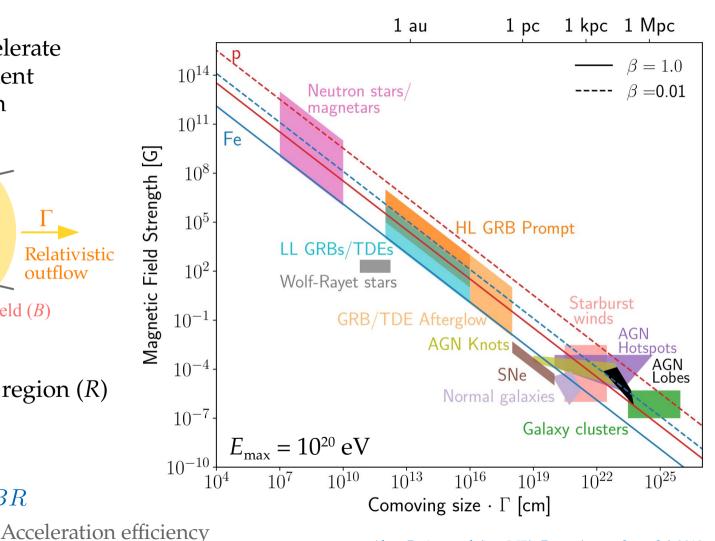


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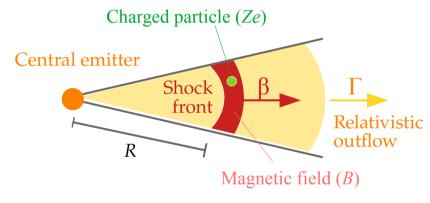
Hillas, Ann. Rev. Astron. Astrophys. 1984

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Hillas criterion

But not sufficient!

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Confinement holds until

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$$rac{E_{
m max}}{ZeB}=eta\Gamma R$$

$$\Rightarrow E_{
m max}=\eta^{-1}eta\Gamma ZeBR$$
Acceleration efficiency

1 au 1 pc 1 kpc 1 Mpc $\beta = 1.0$ 10^{14} $\beta = 0.01$ Neutron stars/ magnetars 10^{11} Magnetic Field Strength [G] 10^{8} 10^{5} HL GRB Prompt LL GRBs/TDEs 10^{2} Wolf-Rayet stars Starburst 10^{-1} GRB/TDE Afterglow AGN AGN Knots Hotspots AGN SNe obes Normal galaxies 10^{-7} Galaxy clusters $E_{\text{max}} = 10^{20} \text{ eV}$ $10^{\overline{10}}$ $10^{\overline{13}}$ 10^{16} 10^{19} 10^{22} 10^{25} Comoving size $\cdot \Gamma$ [cm]

Hillas, Ann. Rev. Astron. Astrophys. 1984

Alves Batista et al. (inc. MB), Front. Astron. Space Sci. 2019

UHECR anisotropy

How do we know that UHECRs have an extragalactic origin?

Their energies are so large that their Larmor radius cannot be contained by the Milky Way

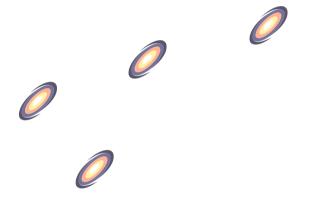
$$R_L = \frac{E_p}{eB} \approx \frac{10^{18} \text{ eV}}{e \times 1 \mu\text{G}} \gg 100 \text{ kpc}$$

We can look at the distribution of arrival directions of UHECRs (more on this later!)

UHECR propagation

Calculating the UHECR flux at Earth

Redshift = 0





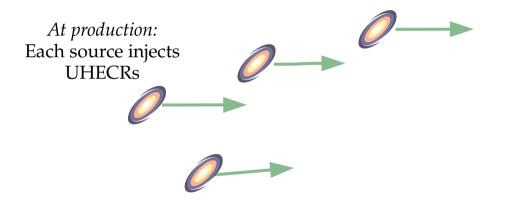
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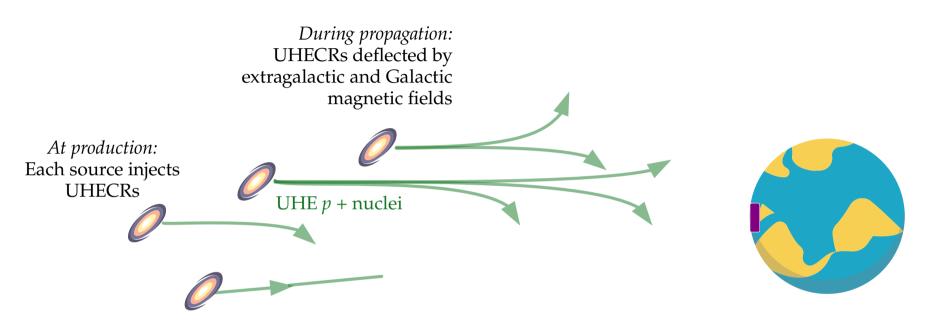


UHECR sources distributed in redshift (e.g., as star-formation rate)





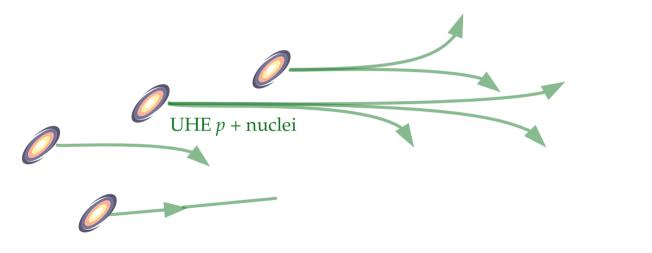
UHECR sources distributed in redshift (e.g., as star-formation rate)

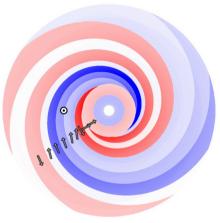


Redshift = 0

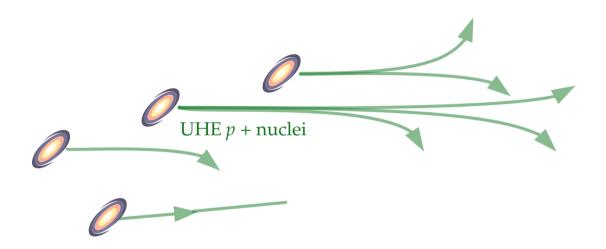
Extragalactic $B \sim nG$ (?)

Galactic $B \sim \mu G$





Extragalactic $B \sim nG$ (?)



Larger charge bends more

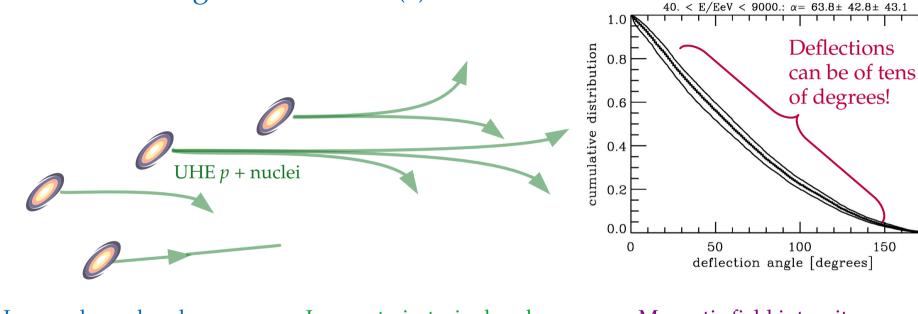
Longer trajectories bend more

Magnetic field intensity

$$\delta_{
m rms} pprox 0.8^{\circ} Z igg(rac{10 \; {
m EeV}}{E} igg) igg(rac{L}{10 \; {
m Mpc}} igg)^{1/2} igg(rac{L_c}{{
m Mpc}} igg)^{1/2} igg(rac{B_{
m rms}}{n {
m G}} igg)$$
 Larger charge bends more L_c : field coherence length

Redshift z = 0





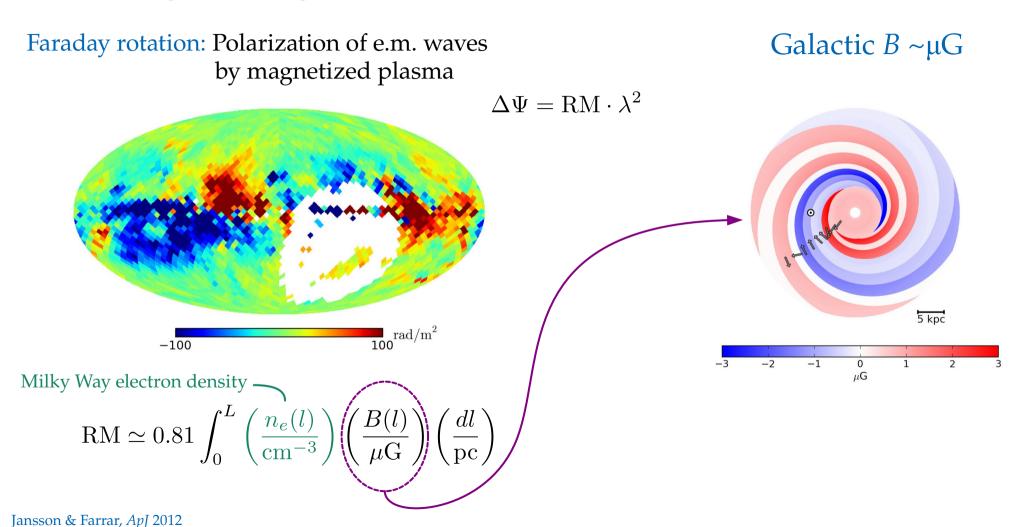
Larger charge bends more Longer trajectories bend more Magnetic field intensity $\delta_{
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Larger charge bends more

 L_c : field coherence length

150

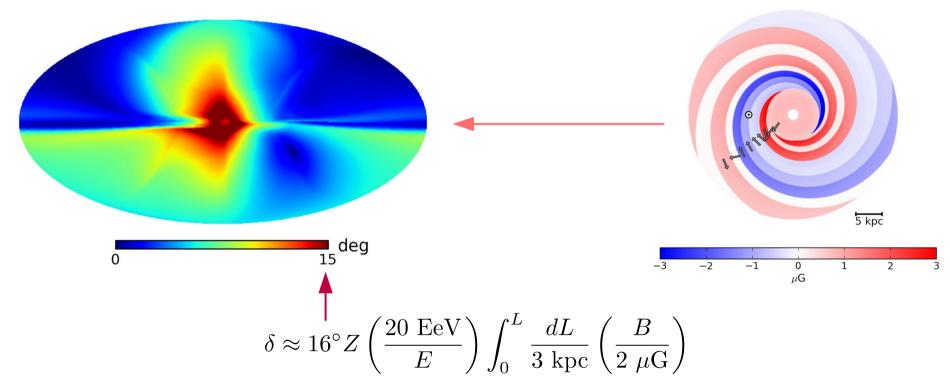
Scattering on magnetic fields



Scattering on magnetic fields

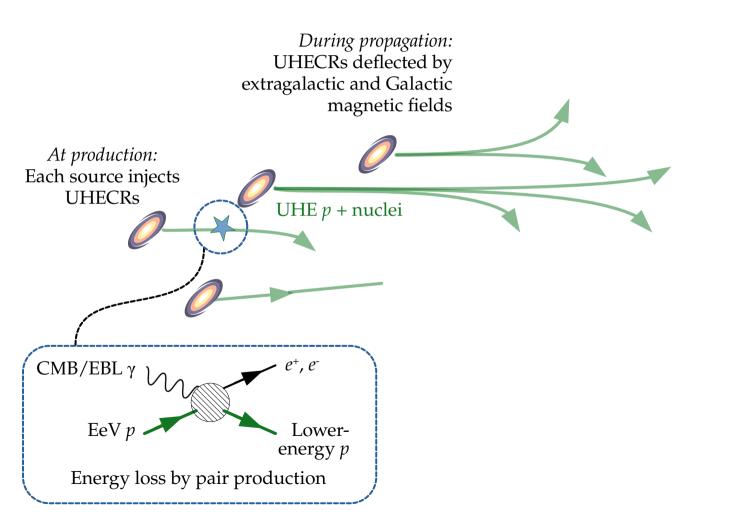
Galactic *B* ~μG

Galactic deflections of 60-EeV protons



Auger Collab., Astropart. Phys. 2007

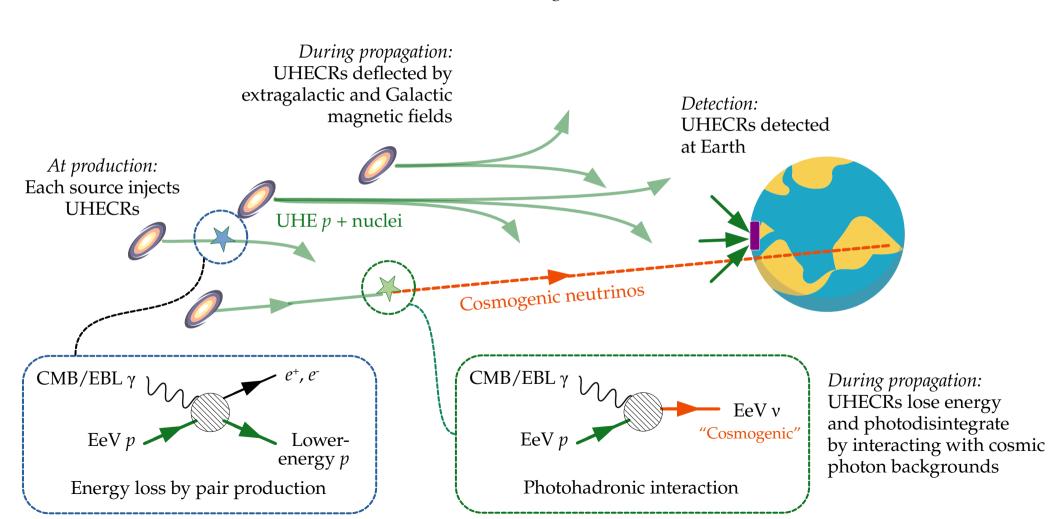
UHECR sources distributed in redshift (e.g., as star-formation rate)





During propagation:
UHECRs lose energy
and photodisintegrate
by interacting with cosmic
photon backgrounds

UHECR sources distributed in redshift (e.g., as star-formation rate)



a: Scale factor n_p : Real number density

Comoving number density of protons (GeV⁻¹ cm⁻³): $Y_p(E,z) = a^3(z) n_p(E,z) = \frac{1}{(1+z)^3} n_p(E,z)$

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Solve a propagation equation:

$$\dot{Y}_p = \partial_E(HEY_p) + \partial_E(b_{e^+e^-}Y_p) + \partial_E(b_{p\gamma}Y_p) + \mathcal{L}_{CR}$$

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Energy loss due to adiabatic cosmological expansion

a: Scale factor n_v : Real number density

Comoving number density of protons (GeV⁻¹ cm⁻³): $Y_p(E,z) = a^3(z) n_p(E,z) = \frac{1}{(1+z)^3} n_p(E,z)$

Solve a propagation equation:

Energy loss rates:
$$b \equiv -\frac{dE}{dt}$$

equation: Energy loss rates:
$$b \equiv -\frac{dE}{dt}$$

$$\dot{Y}_p = \partial_E(HEY_p) + \partial_E(b_{e^+e^-}Y_p) + \partial_E(b_{p\gamma}Y_p) + \mathcal{L}_{\mathrm{CR}}$$

Energy loss due to adiabatic cosmological expansion

a: Scale factor n_p : Real number density

Comoving number density of protons (GeV⁻¹ cm⁻³): $Y_p(E,z) = a^3(z)n_p(E,z) = \frac{1}{(1+z)^3}n_p(E,z)$

Solve a propagation equation:

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Energy loss due to photohadronic int.:

$$p + \gamma \rightarrow p + \pi^{0}$$

$$p + \gamma \rightarrow n + \pi^{+}$$
+ other process
+ *n* beta-decay into *p*

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Cosmic-ray injection by UHECR sources

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Recast in terms of redshift using

$$\frac{dz}{dt} = -(1+z)H(z)$$

with Hubble parameter

$$H(z) = H_0 \sqrt{\Omega_m (1+z)^3 + \Omega_\Lambda}$$

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$$\partial_z Y_p(E, z) = \frac{-1}{(1+z)H(z)} \left\{ \partial_E (H(z)EY_p(E, z)) + \partial_E (b_{e^+e^-}(E, z)Y_p(E, z)) + \partial_E (b_{p\gamma}(E, z)Y_p(E, z)) + \mathcal{L}_{CR}(E, z) \right\}$$

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$$\begin{split} \sqrt{\partial_z Y_p(E,z)} &= \frac{-1}{(1+z)H(z)} \left\{ \partial_E(H(z)EY_p(E,z)) + \partial_E(b_{e^+e^-}(E,z)Y_p(E,z)) \right. \\ &\quad + \partial_E(b_{p\gamma}(E,z)Y_p(E,z)) + \mathcal{L}_{\mathrm{CR}}(E,z) \right\} \end{split}$$
 Evolve this equation from $z_{\mathrm{max}} \sim 4$ to Earth $(z=0)$

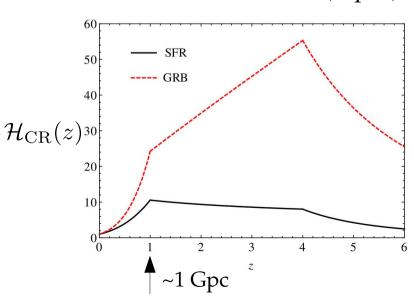
$$\partial_z Y_p(E, z) = \frac{-1}{(1+z)H(z)} \left\{ \partial_E (H(z)EY_p(E, z)) + \partial_E (b_{e^+e^-}(E, z)Y_p(E, z)) + \partial_E (b_{p\gamma}(E, z)Y_p(E, z)) + \mathcal{L}_{CR}(E, z) \right\}$$

Cosmic-ray injection by UHECR sources

Each source injects UHECRs with a spectrum (GeV⁻¹ s⁻¹)

 $Q_{\mathrm{CR}}(E) \propto E^{-\gamma} e^{-E/E_{\mathrm{max}}}$ $\mathcal{L}_{\mathrm{CR}} = Q_{\mathrm{CR}}(E(1+z))\mathcal{H}_{\mathrm{CR}}(z)$

The number density of sources evolves with redshift (Mpc⁻³)



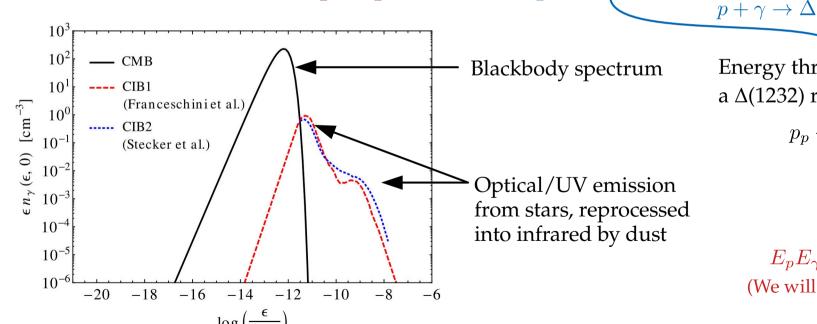
$$\partial_z Y_p(E, z) = \frac{-1}{(1+z)H(z)} \left\{ \partial_E (H(z)EY_p(E, z)) + \partial_E (b_{e^+e^-}(E, z)Y_p(E, z)) + \partial_E (b_{p\gamma}(E, z)Y_p(E, z)) + \mathcal{L}_{CR}(E, z) \right\}$$

Adiabatic cosmological expansion

Energy at Earth =
$$\frac{\text{Energy at production}}{1+z}$$

$$\partial_z Y_p(E, z) = \frac{-1}{(1+z)H(z)} \left\{ \partial_E (H(z)EY_p(E, z)) + \partial_E (b_{e^+e^-}(E, z)Y_p(E, z)) + \partial_E (b_{p\gamma}(E, z)Y_p(E, z)) + \mathcal{L}_{CR}(E, z) \right\}$$

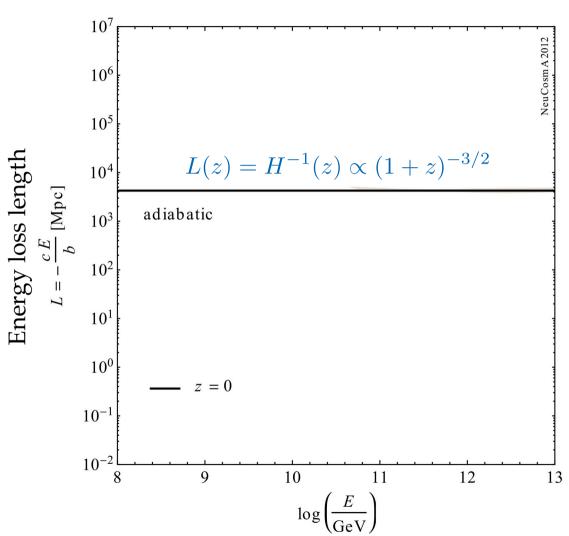
Interaction with cosmological backgrounds (pair production + photohadronic)

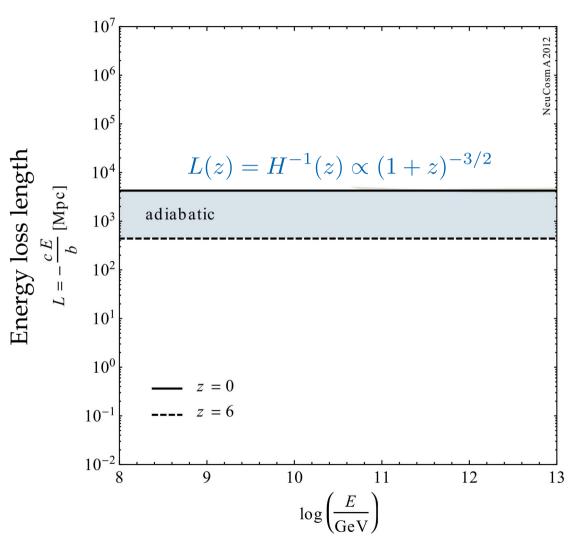


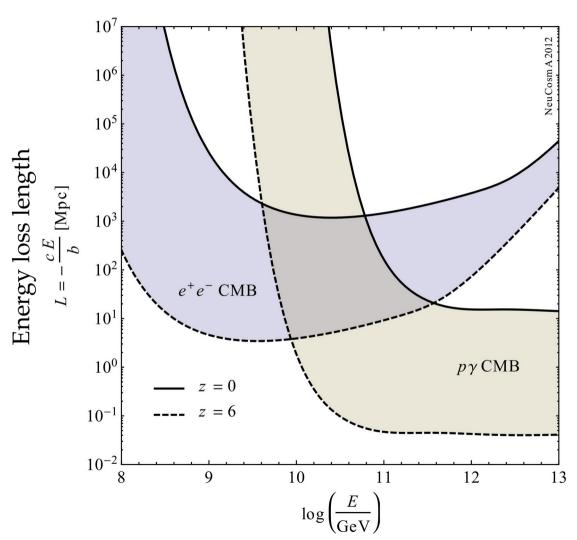
Energy threshold to produce a $\Delta(1232)$ resonance:

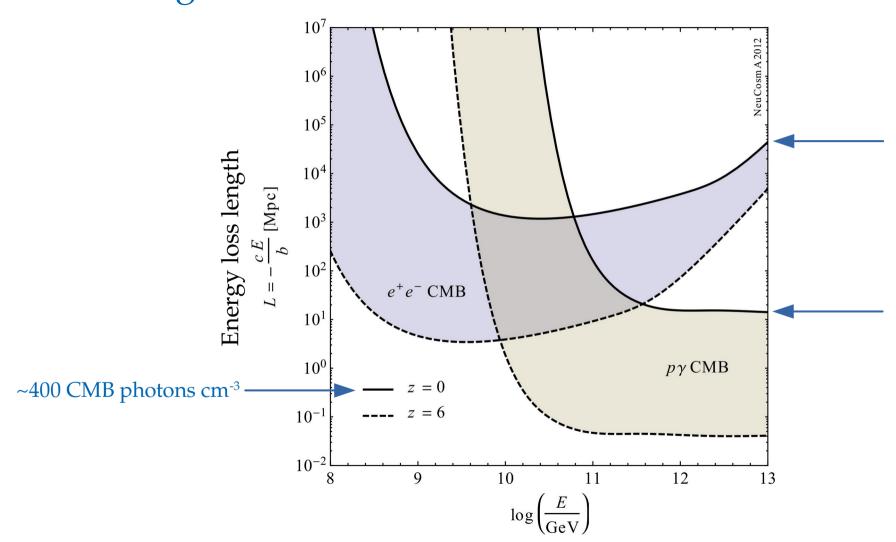
$$p_p + p_{\gamma} = p_{\Delta}$$

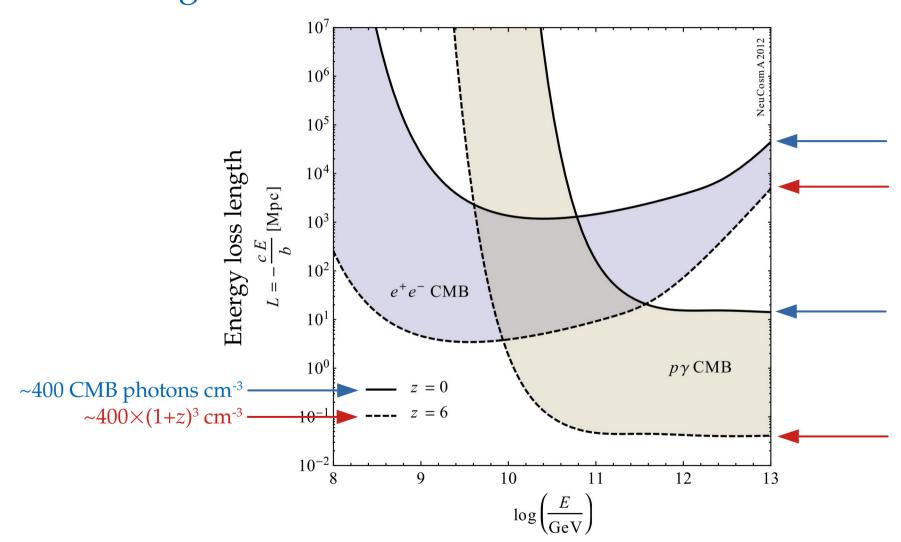
 $E_p E_\gamma \approx 0.16 \; \mathrm{GeV}^2$ (We will use this later, too)

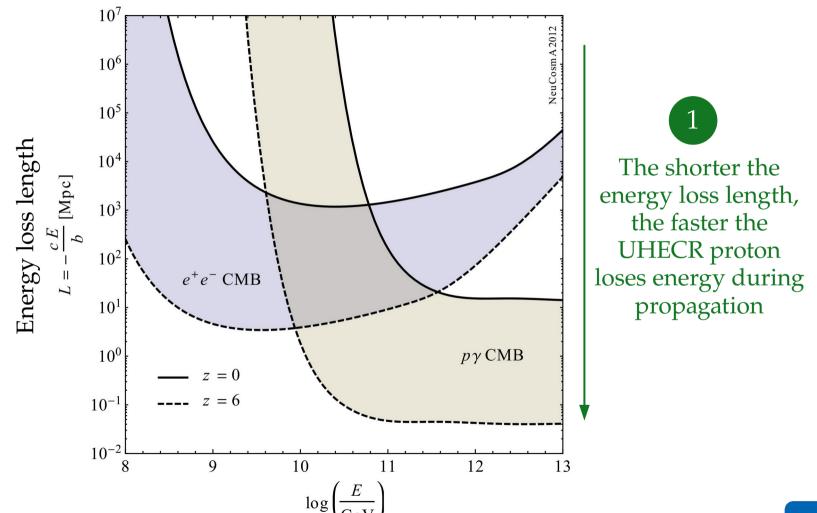


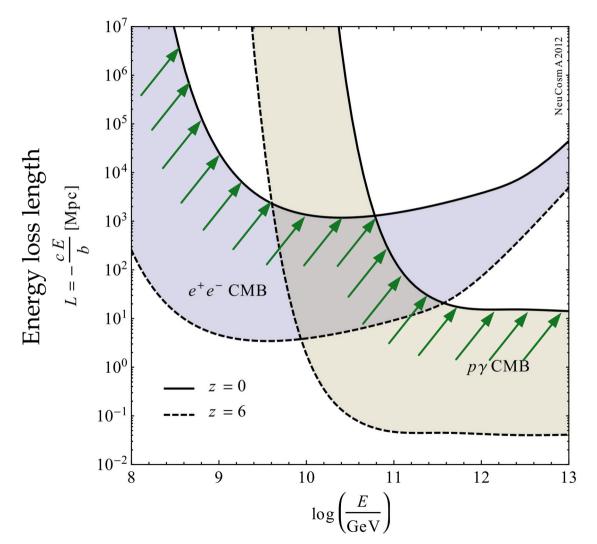






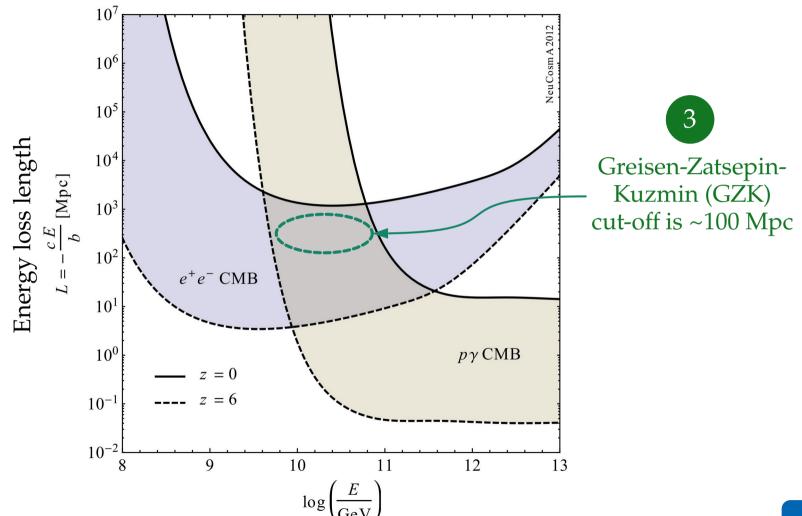


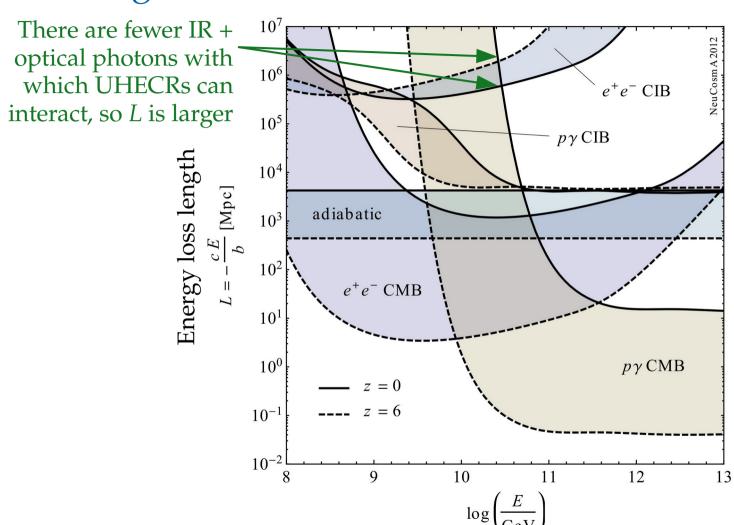


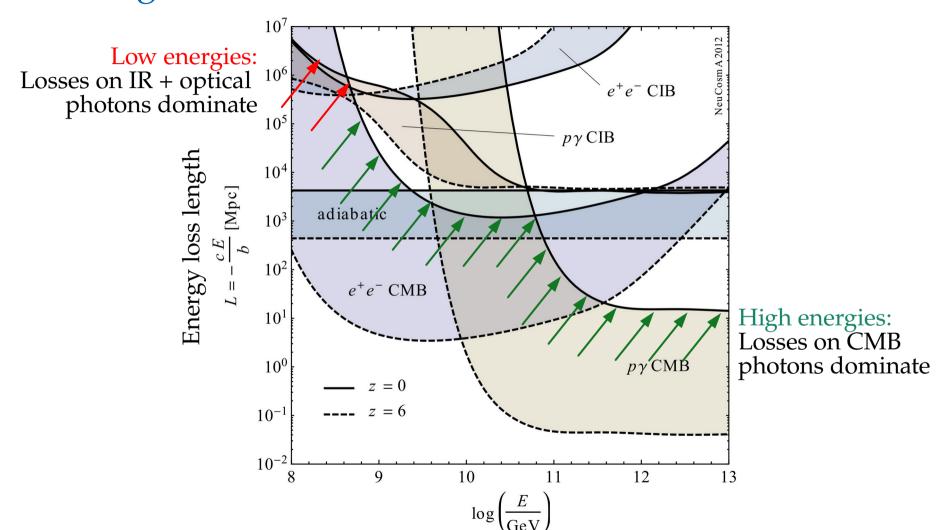


2

At each energy, the energy loss length is dominated by the fastest energy-loss process







Photohadronic processes:

$$p + \gamma \to \Delta \to \begin{cases} p + \pi^0 \\ n + \pi^+ \\ \downarrow \nu_{\mu} + \nu_{\mu} + \nu_{e} + e^+ \end{cases}$$

Pair production:

$$p + \gamma \rightarrow p + e^- + e^+$$

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Greisen-Zatsepin-Kuzmin (GZK) cut-off:

$$E_p \approx \frac{0.16 \text{ GeV}^2}{0.66 \text{ meV}} \approx 2 \cdot 10^{11} \text{ GeV}$$
Mean CMB photon energy

(Assuming only photohadronic interaction)

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$$E_p \approx 5 \cdot 10^{10} \text{ GeV}$$

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Mean free path:

$$(n_{\gamma} \langle \sigma \rangle_{p\gamma})^{-1} = (413 \text{ cm}^{-3} \times 200 \text{ µbarn})^{-1}$$

 $\approx 10^{25} \text{ cm}$
 $\approx 4 \text{ Mpc}$

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$$L = (E/\Delta E)(n_{\gamma} \langle \sigma \rangle_{p\gamma})^{-1}$$

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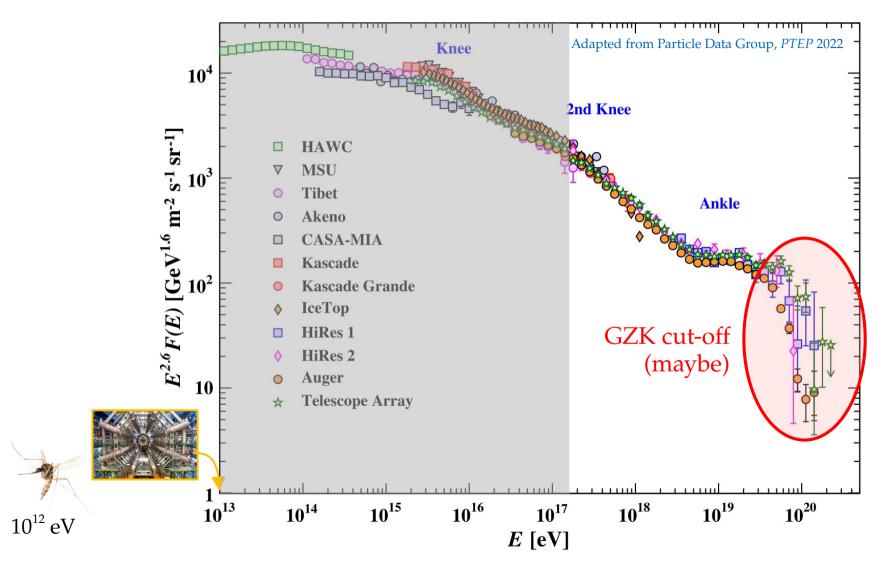
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A more detailed calculation yields

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m Mpc}$$





 $6 \times 10^{20} \,\mathrm{eV}$

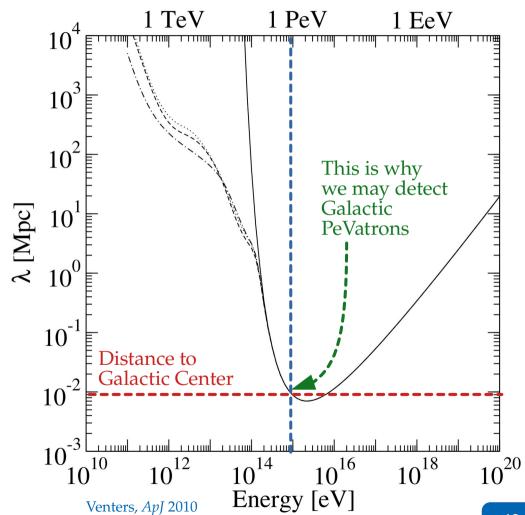
The Universe is *also* opaque to PeV gamma rays

Pair production:

$$\gamma_{\rm astro} + \gamma_{\rm cosmo} \rightarrow e^{-} + e^{+}$$

Inverse Compton scattering:

$$e^{\pm} + \gamma_{\text{cosmo}} \rightarrow e^{\pm} + \gamma$$



Fermi-LAT, ApJ 2015

The Universe is *also* opaque to PeV gamma rays

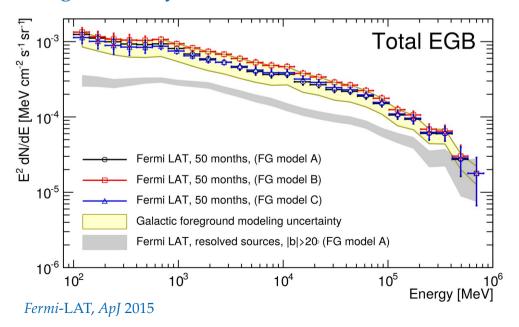
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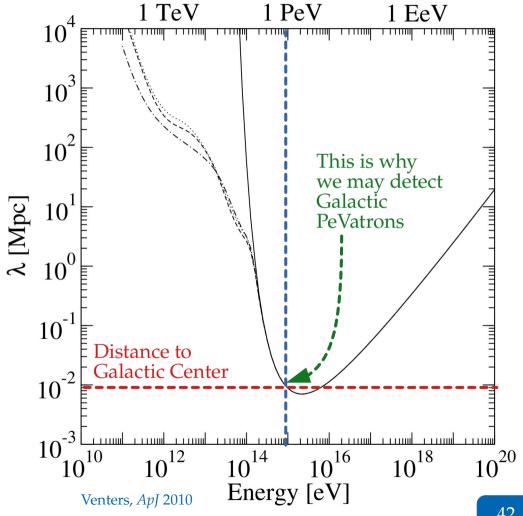
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PeV gamma rays cascade down to MeV-GeV:





Putting it all together...

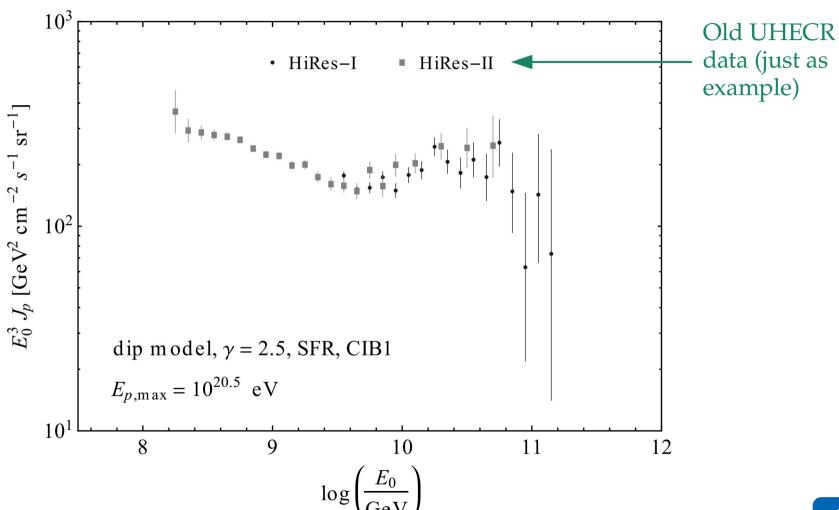
$$\partial_z Y_p(E, z) = \frac{-1}{(1+z)H(z)} \left\{ \partial_E (H(z)EY_p(E, z)) + \partial_E (b_{e^+e^-}(E, z)Y_p(E, z)) + \partial_E (b_{p\gamma}(E, z)Y_p(E, z)) + \mathcal{L}_{CR}(E, z) \right\}$$

Evolve numerically from
$$z_{\text{max}} \sim 4$$
 to Earth $(z = 0)$

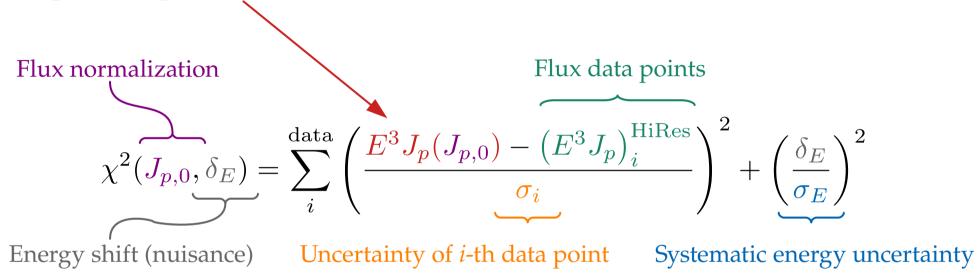
Diffuse UHECR proton flux at Earth (GeV⁻¹ cm⁻² s⁻¹ sr⁻¹):

$$J_p(E) = \underbrace{\frac{c}{4\pi}}_{n_p}(E, z = 0)$$

This factor converts density to flux —



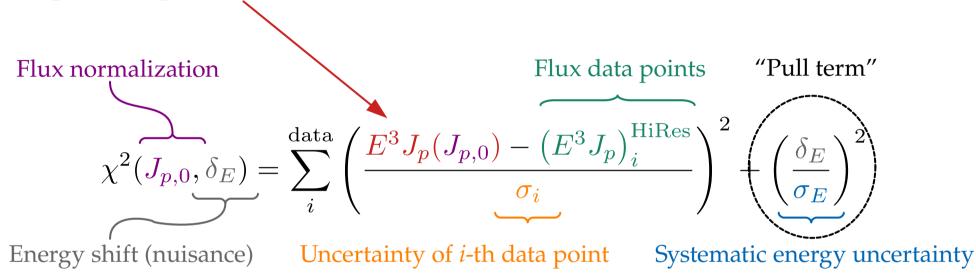
Compare our predicted flux to the measured flux:



Minimize the function with respect to $J_{p,0}$ and δ_E

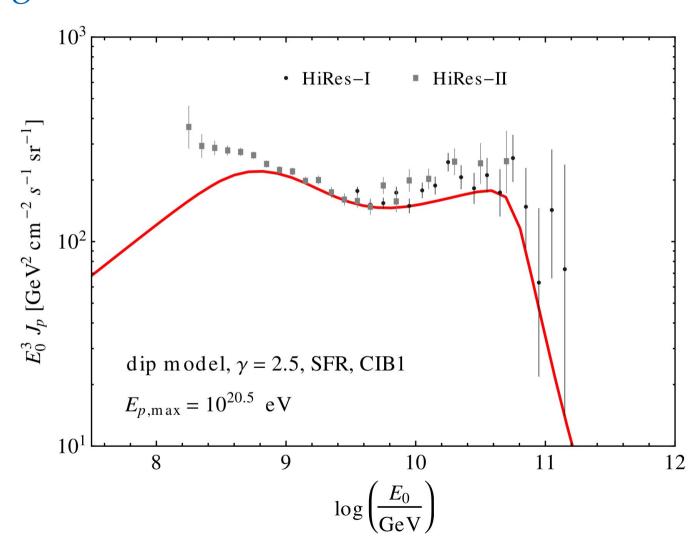
Note: This is a simplified setup; in reality, many flux parameters are jointly varied

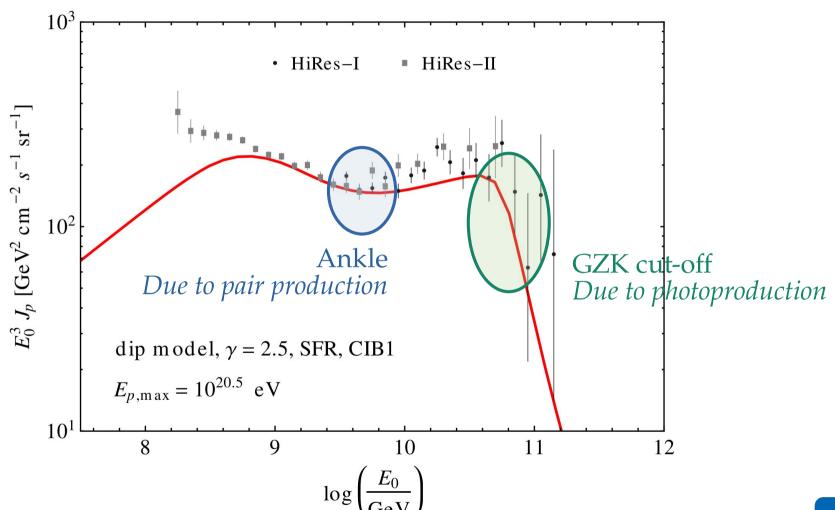
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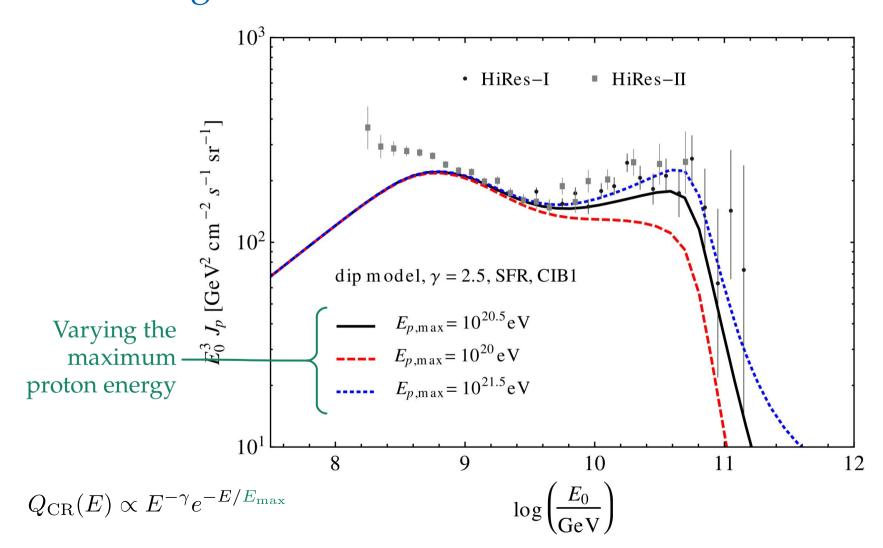


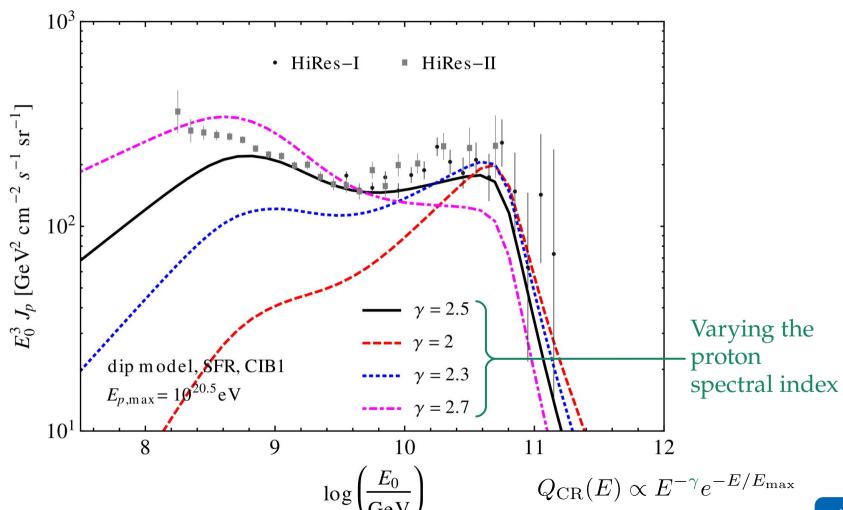
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UHECR detection

Space

Atmosphere

Space

pt Incoming cosmic ray

p⁺

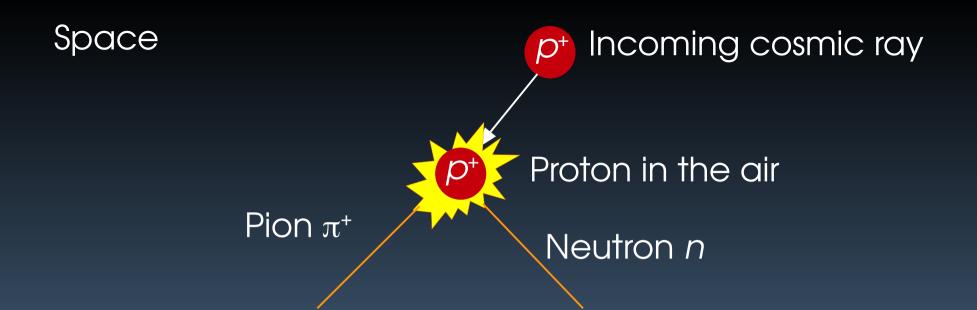
Proton in the air

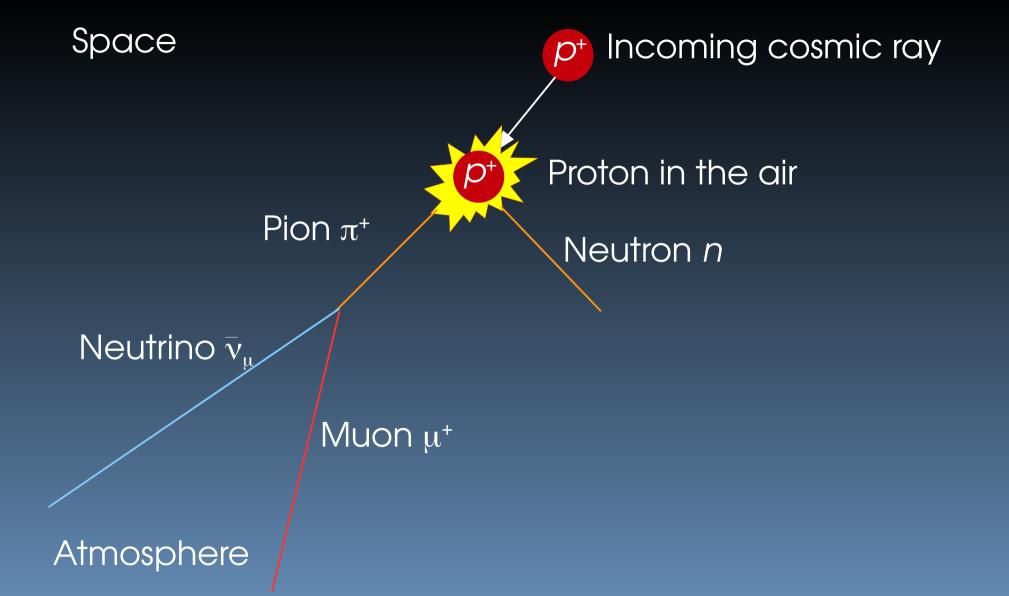
Atmosphere

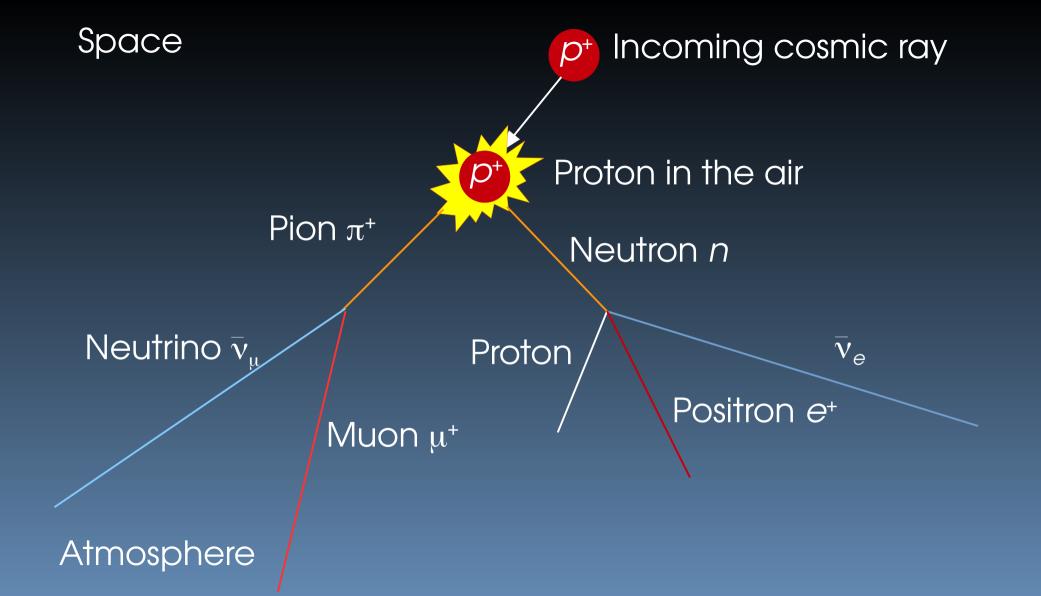
Space

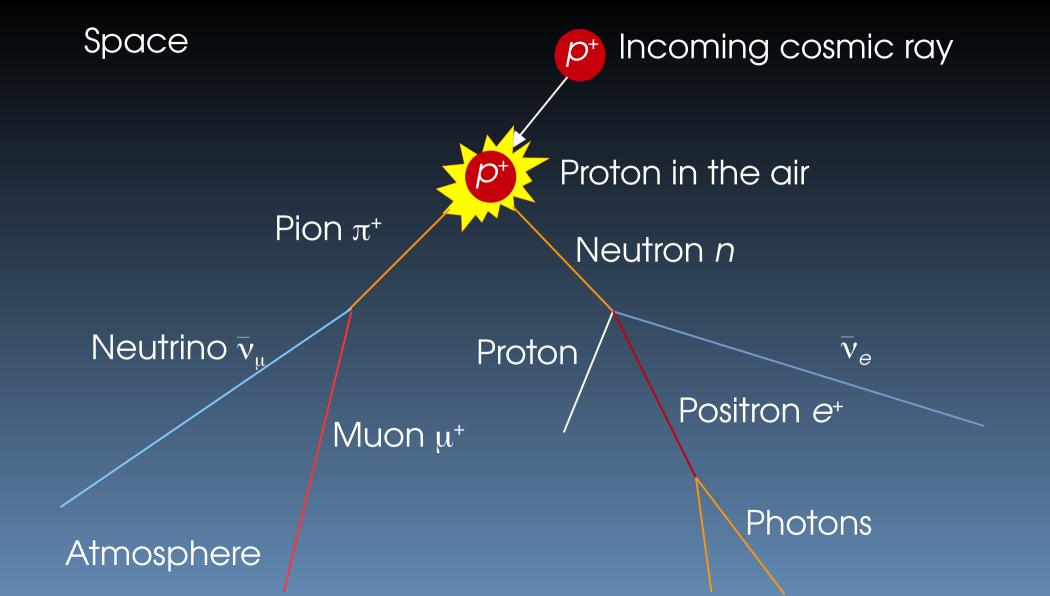
Incoming cosmic ray

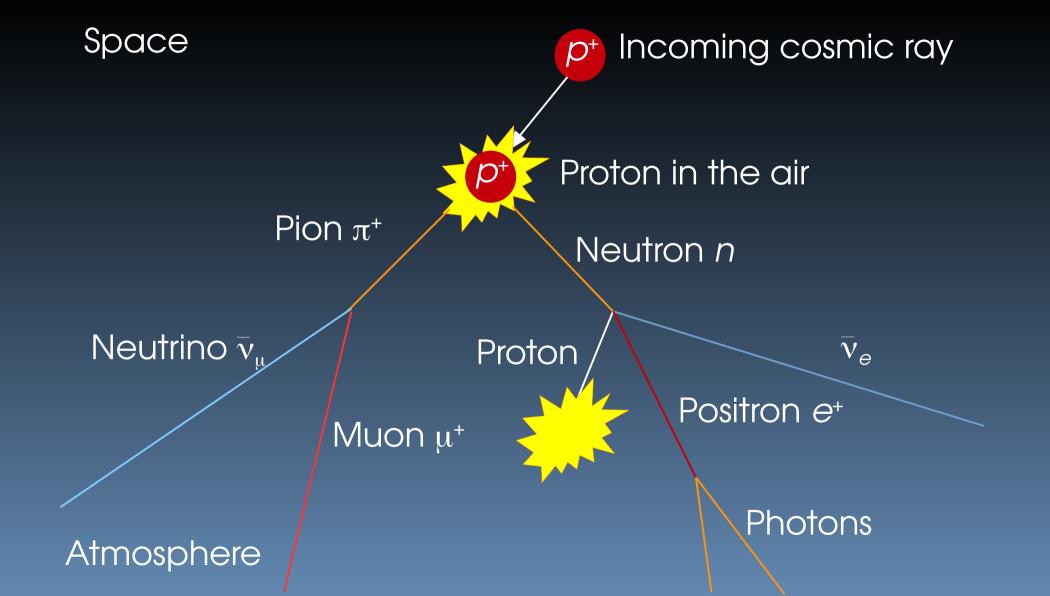
Proton in the air

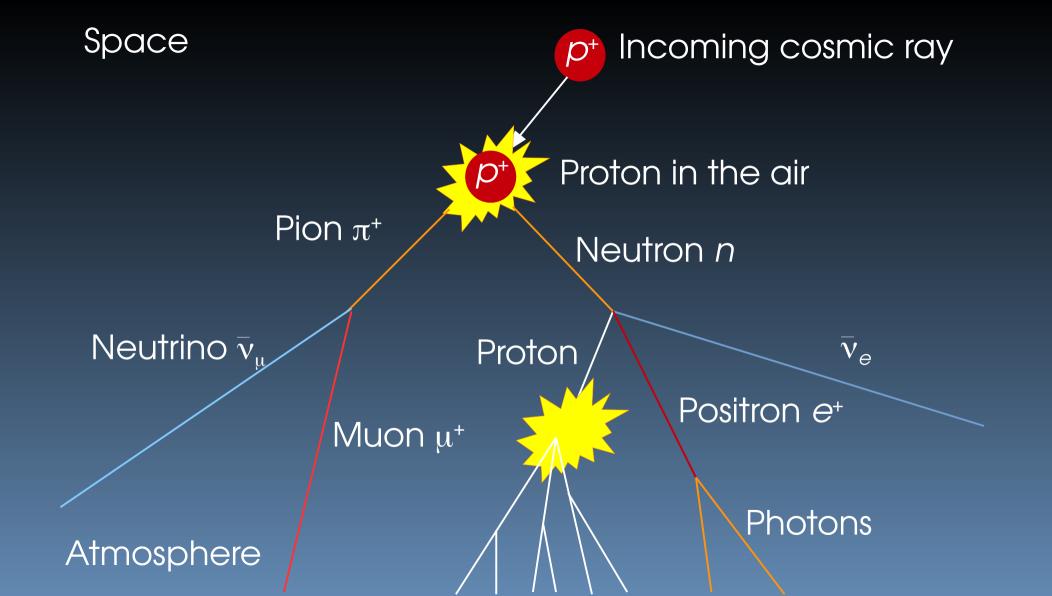


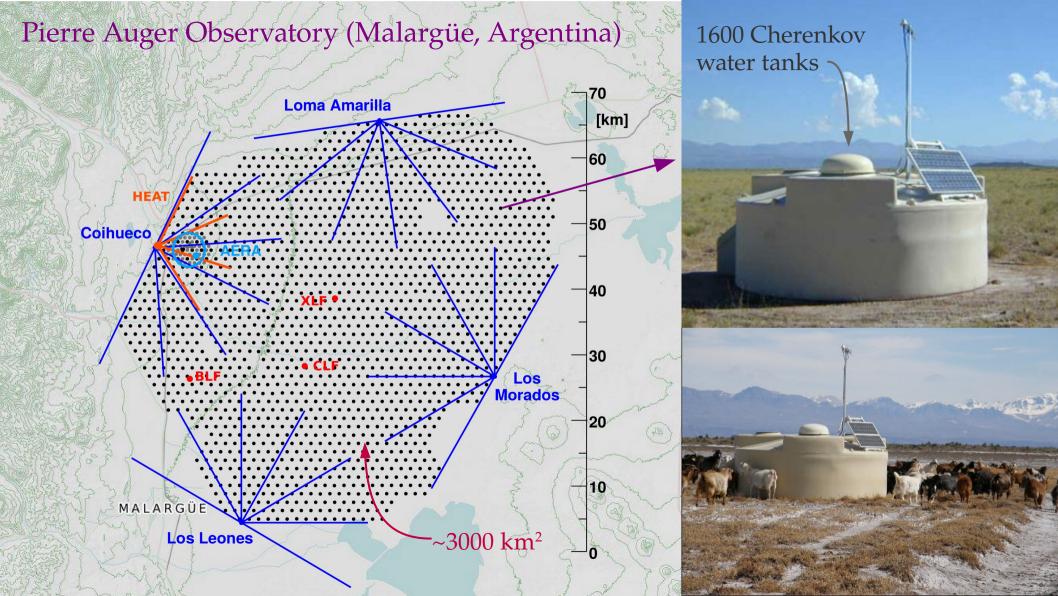


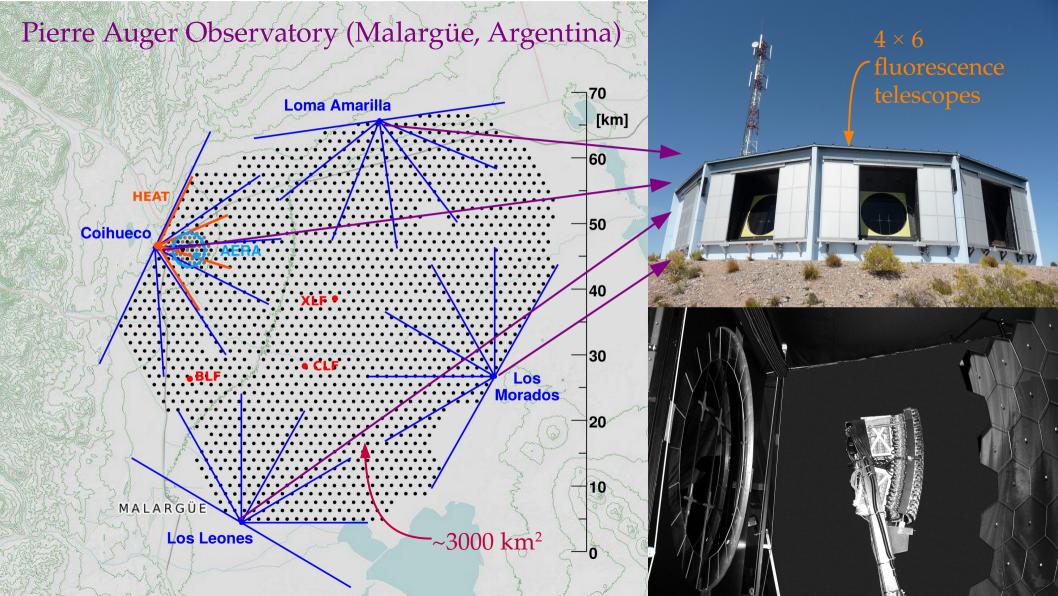




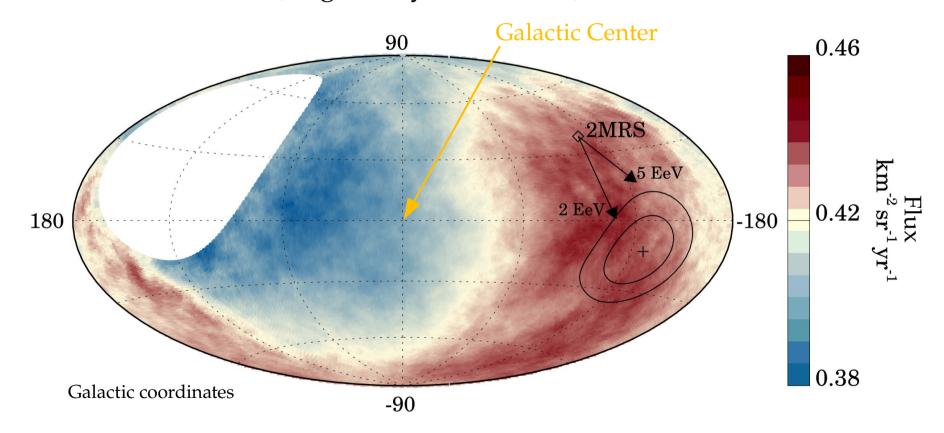




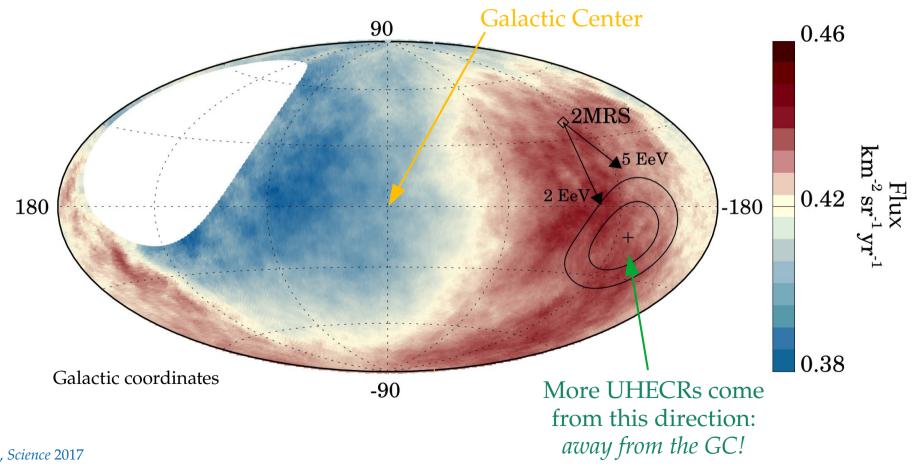




Flux of UHECRs > 8 EeV (Auger, 12 years of data):

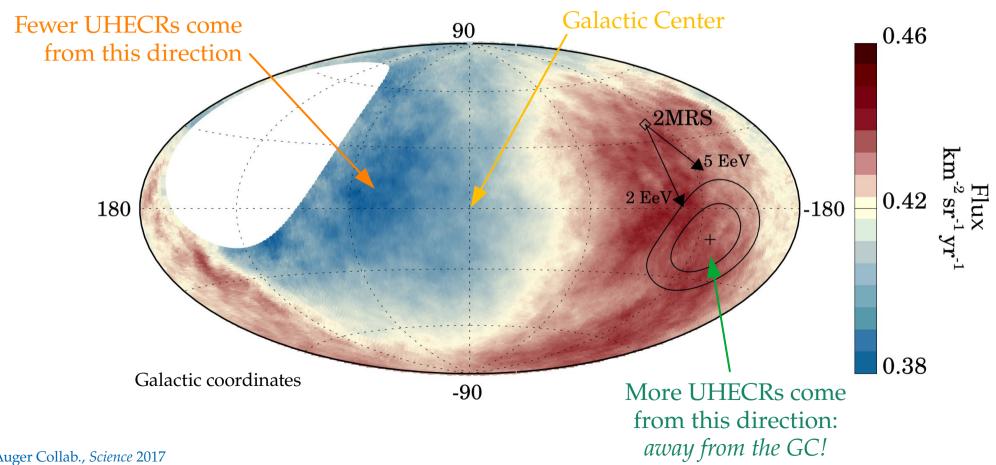


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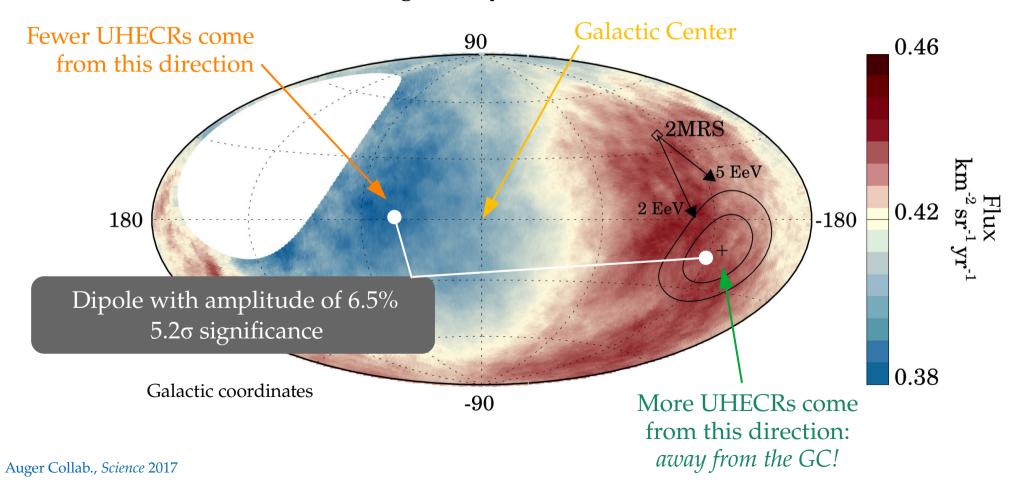


Auger Collab., Science 2017

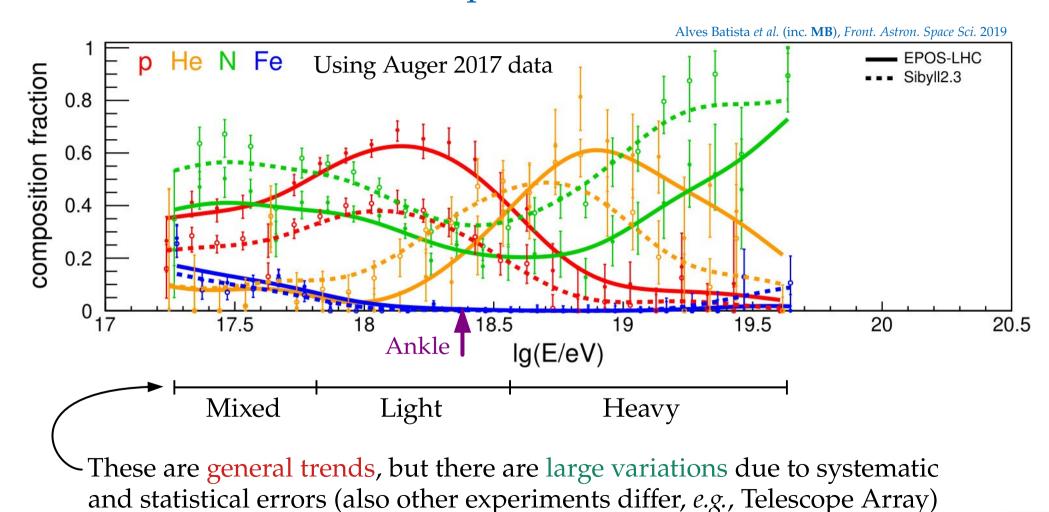
Flux of UHECRs > 8 EeV (Auger, 12 years of data):



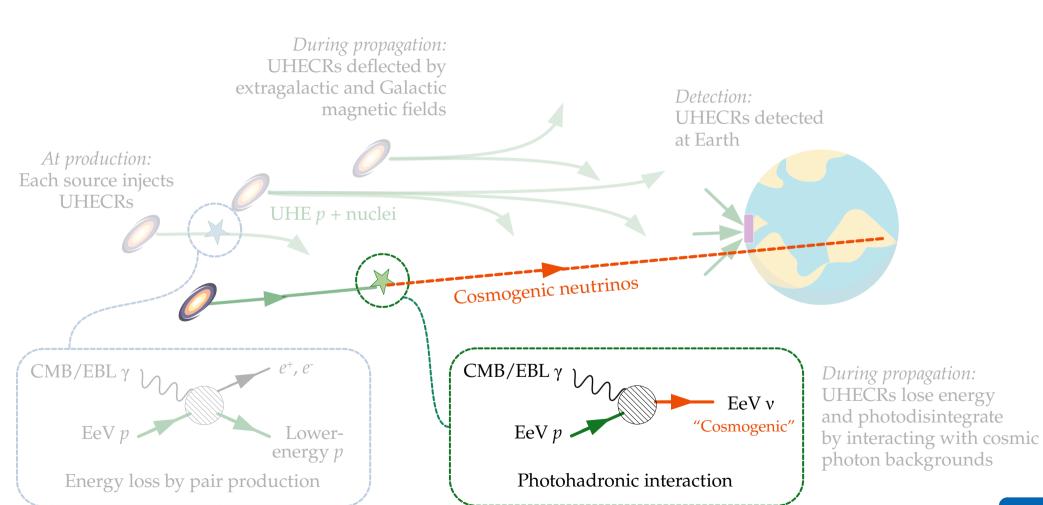
Flux of UHECRs > 8 EeV (Auger, 12 years of data):



X_{max} and UHECR mass composition



High-energy cosmic neutrinos



What about the cosmogenic neutrinos?

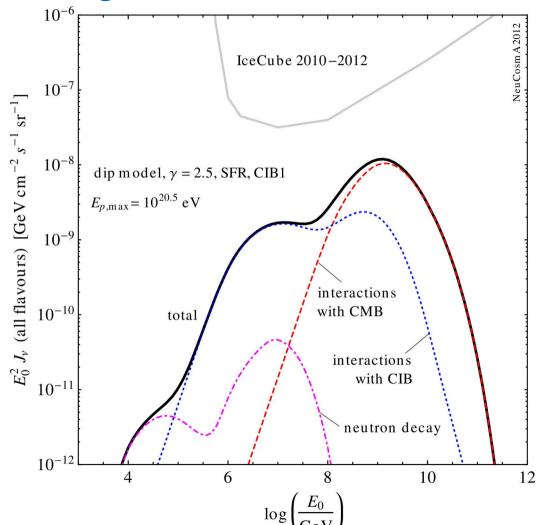
Co-evolve UHECRs and cosmogenic neutrinos:

UHECRs:
$$\partial_z Y_p(E,z) = \frac{-1}{(1+z)H(z)} \left\{ \partial_E (H(z)EY_p(E,z)) + \partial_E (b_{e^+e^-}(E,z)Y_p(E,z)) + \partial_E (b_{p\gamma}(E,z)Y_p(E,z)) + \mathcal{L}_{CR}(E,z) \right\}$$

Neutrinos: $\partial_z Y_\nu(E,z) = \frac{-1}{(1+z)H(z)} \left\{ \partial_E (H(z)EY_\nu(E,z)) + \mathcal{L}_\nu(E,z) \right\}$

Note: We can propagate gamma rays by adding an additional equation for them

Cosmogenic neutrinos



The position of the v bump is determined by the Δ -resonance production threshold,

$$E_p E_\gamma \approx 0.2 \text{ GeV}^2$$

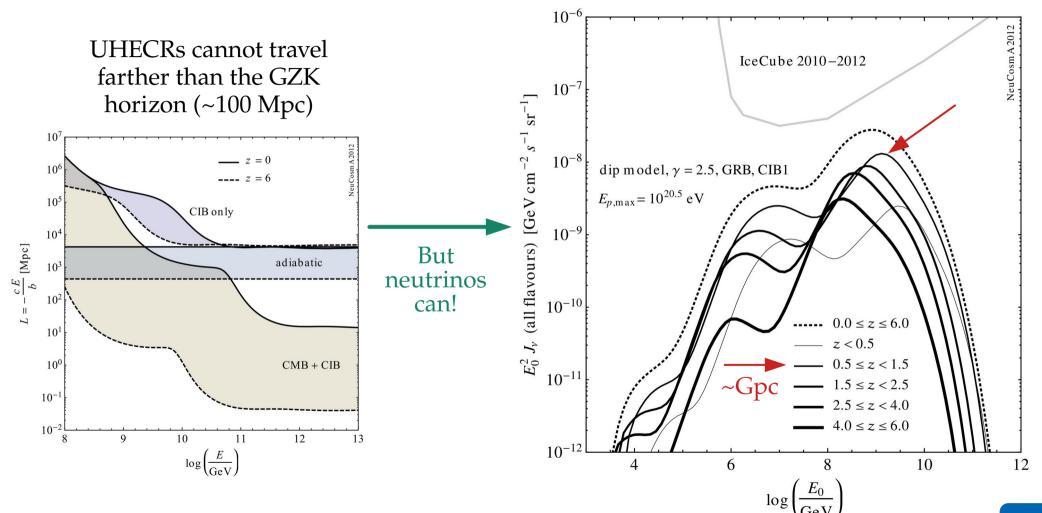
and the relation between neutrino energy and proton energy,

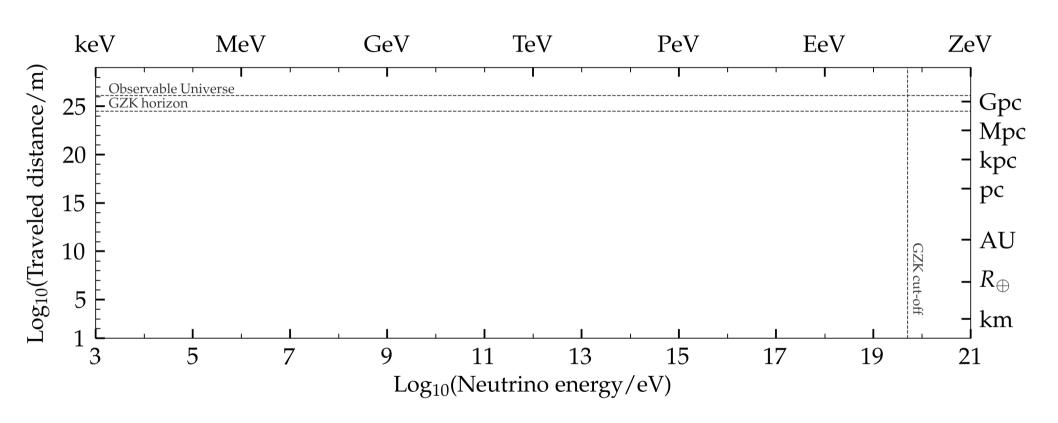
$$E_{\nu} \approx E_p/20$$
.

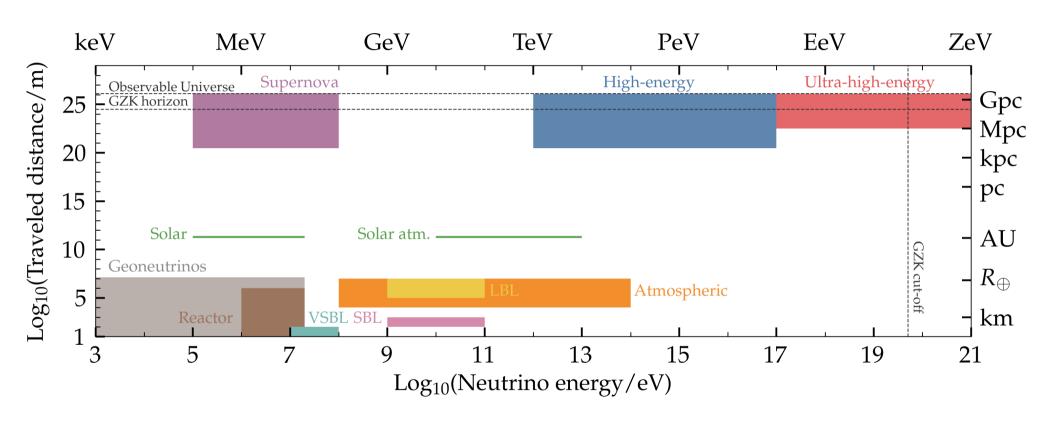
So the neutrino spectrum peaks at

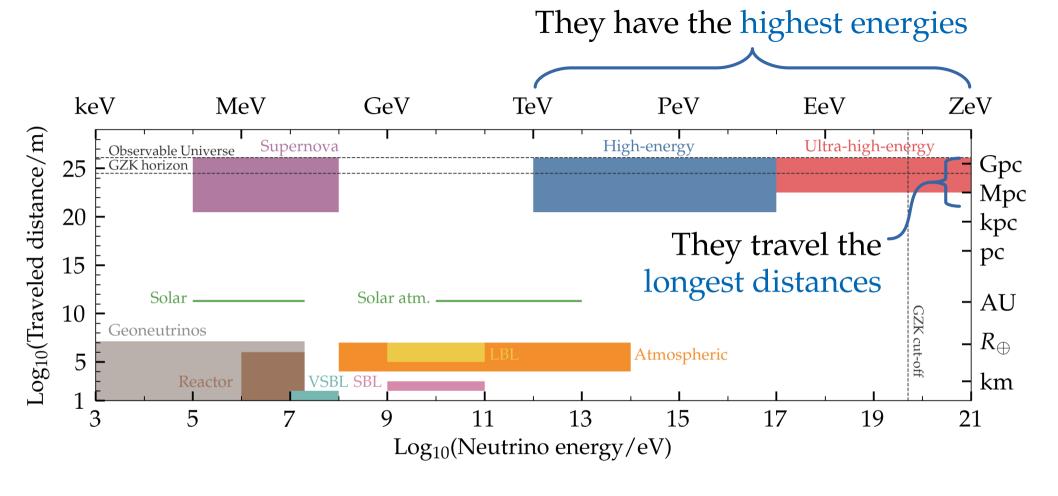
$$E_{\nu} \approx \frac{0.01 \text{ GeV}}{E_{\gamma}/\text{GeV}}$$

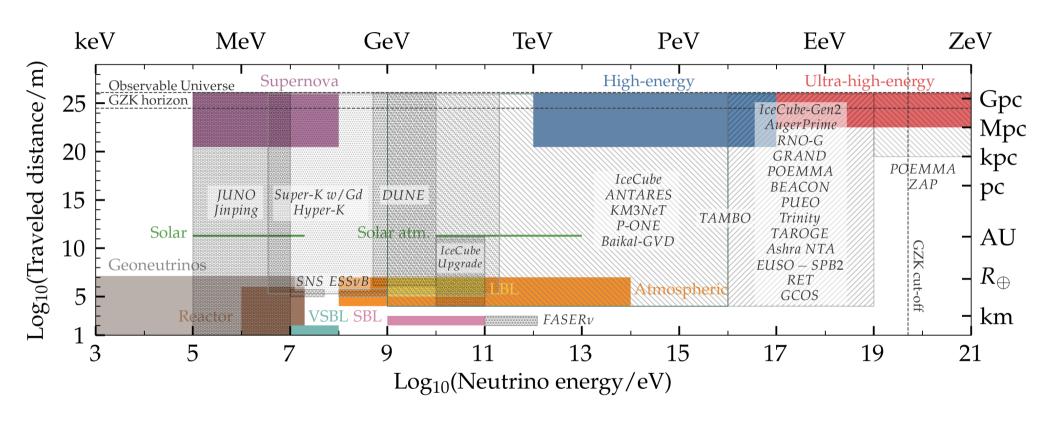
Cosmogenic neutrinos—they come from afar

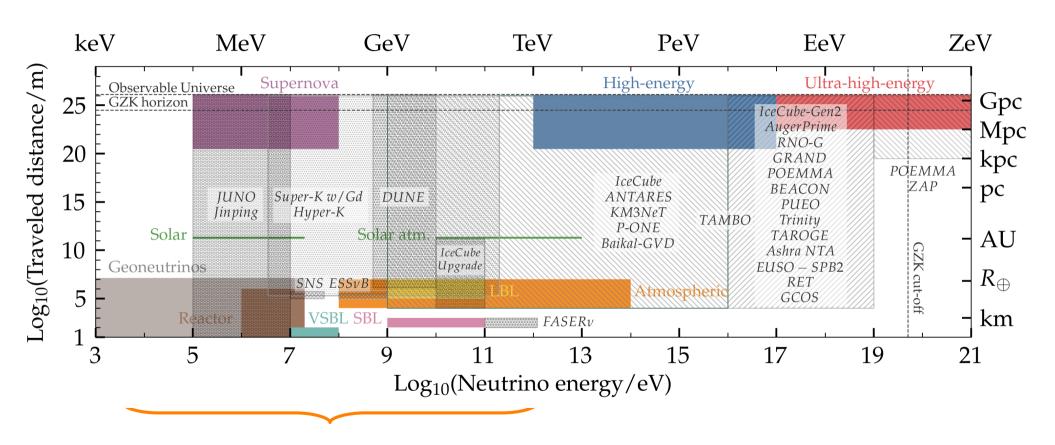




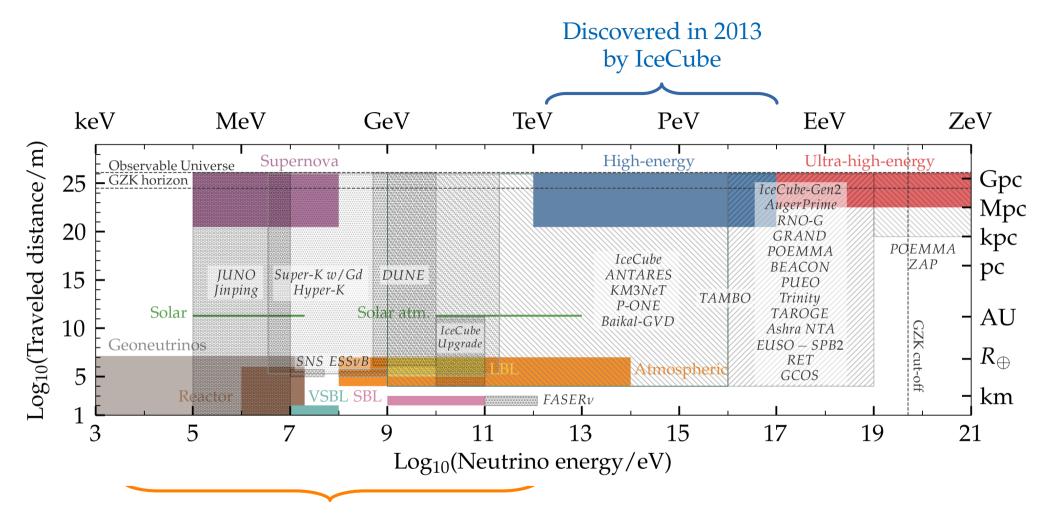




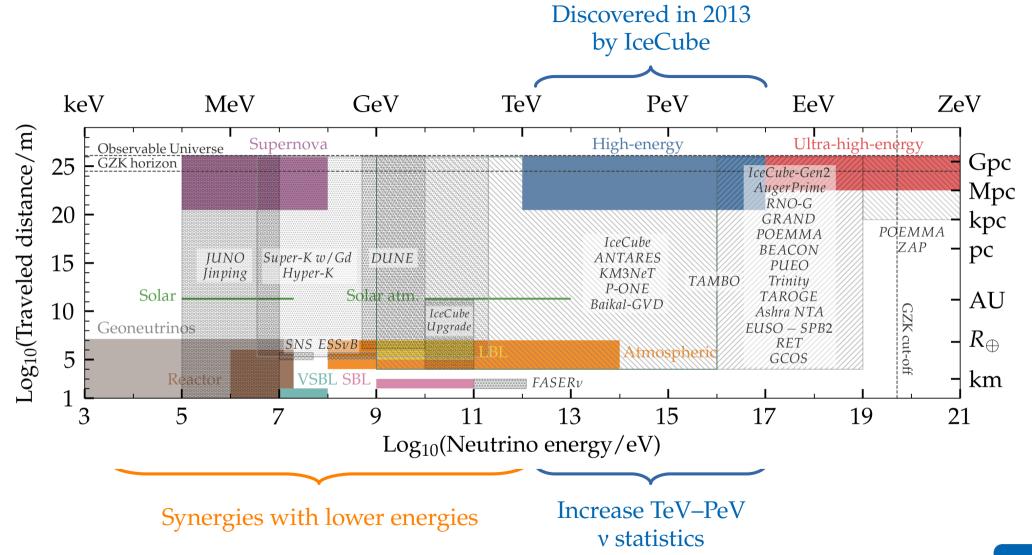


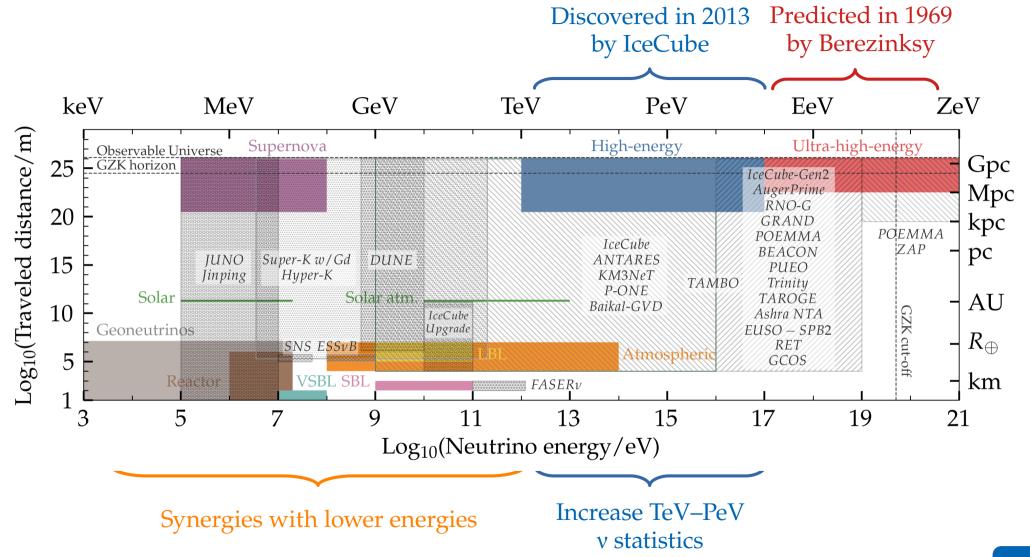


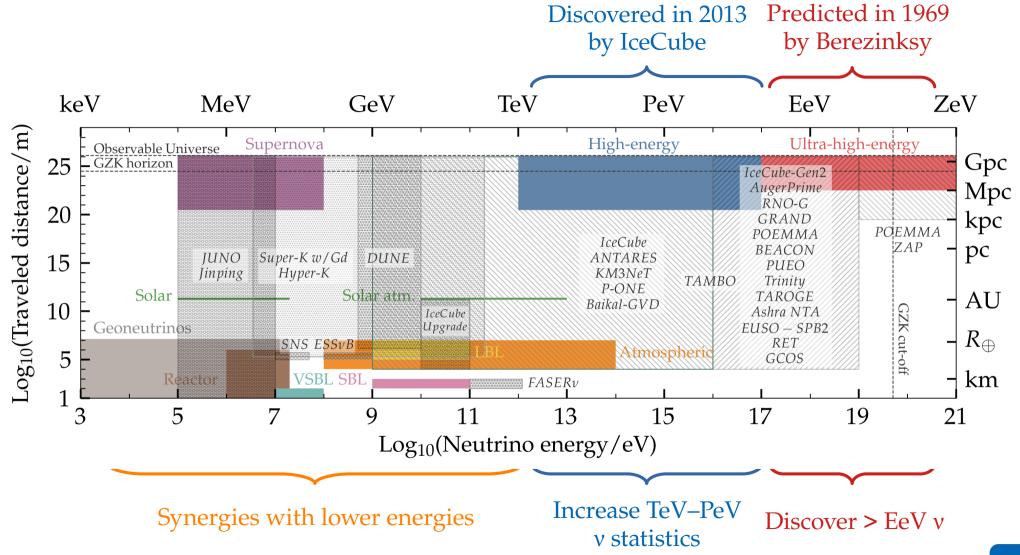
Synergies with lower energies



Synergies with lower energies







Today TeV–PeV v

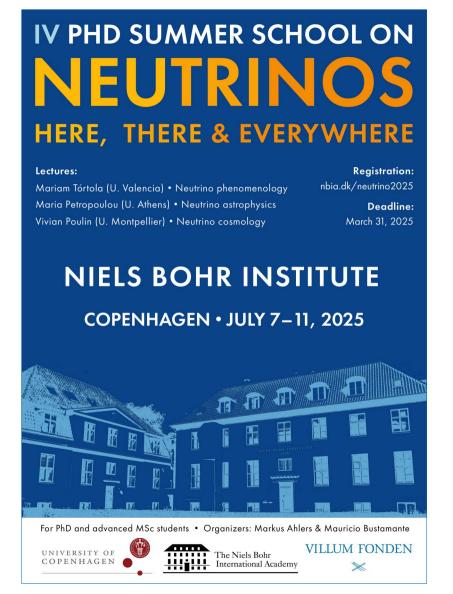
Astro: Find & understand sources

Particle: Turn predictions into tests

Next decade

> 100 - PeV v

Make predictions for a new energy regime

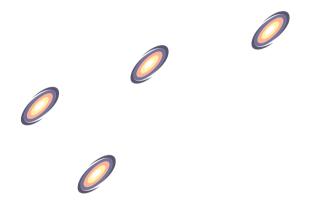


- ► Three tracks:
 - Neutrino phenomenology: Mariam Tórtola (Valencia)
 - Neutrino astrophysics:Maria Petropoulou (Athens)
 - ► Neutrino cosmology: Vivian Poulin (Montpellier)
- ▶ Plus topical seminars & student talks
- ► Registration open (deadline: March 31)

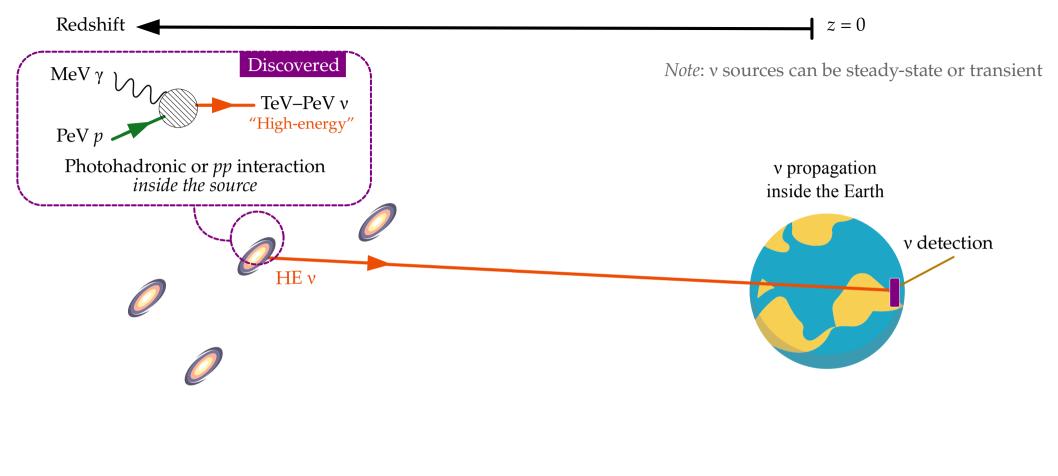
nbia.dk/neutrino2025

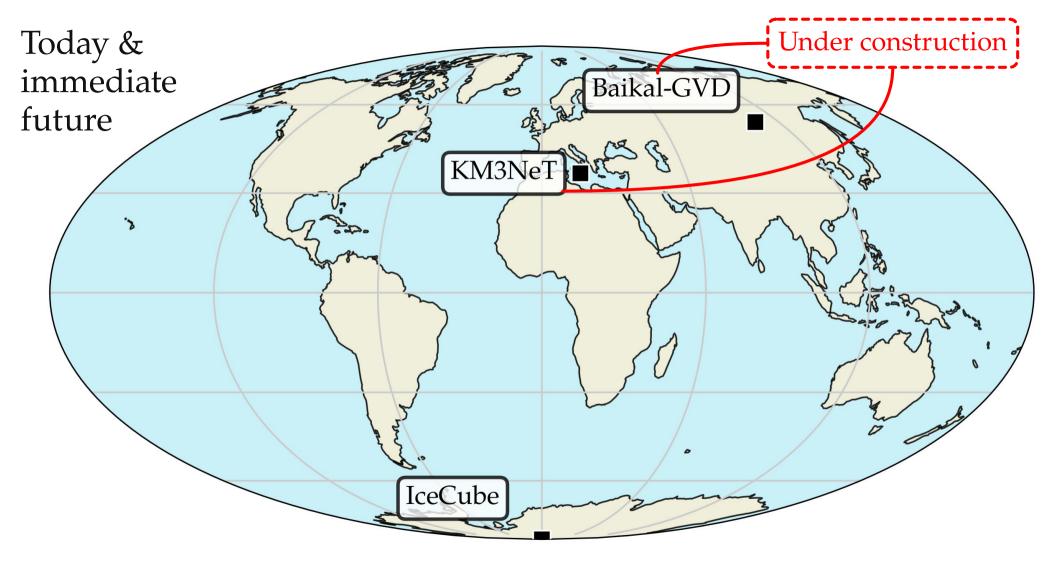
The story so far

Note: v sources can be steady-state or transient

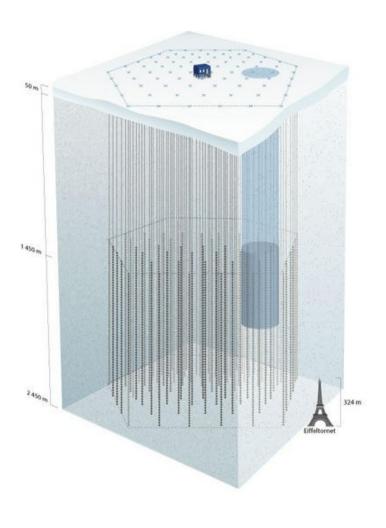








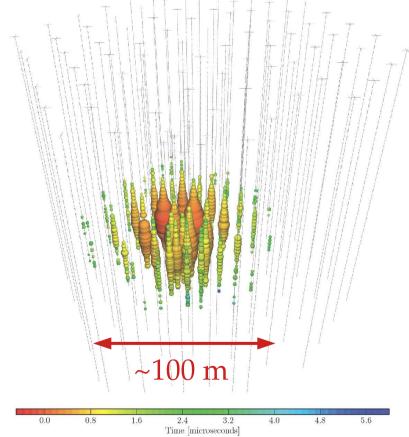
IceCube – What is it?



- ► Km³ in-ice Cherenkov detector in Antarctica
- > 5000 PMTs at 1.5–2.5 km of depth
- ► Sensitive to neutrino energies > 10 GeV

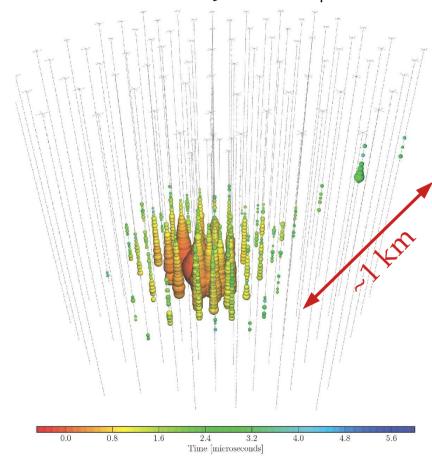


Shower (mainly from v_e and v_{τ})

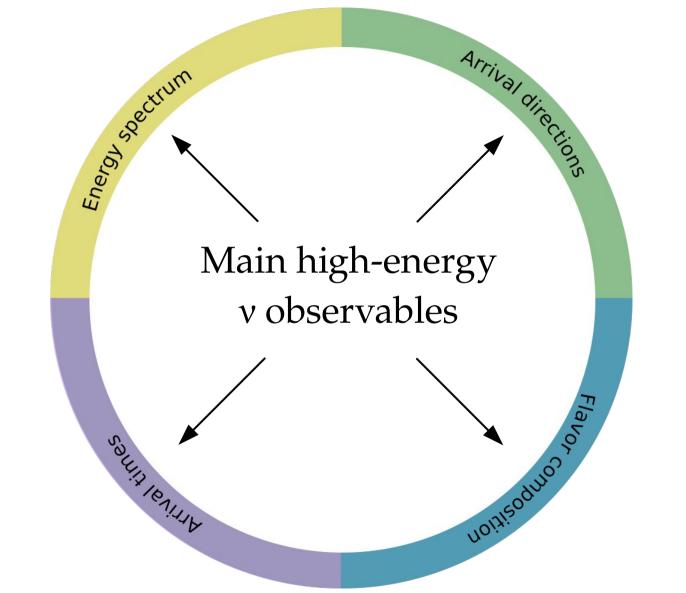


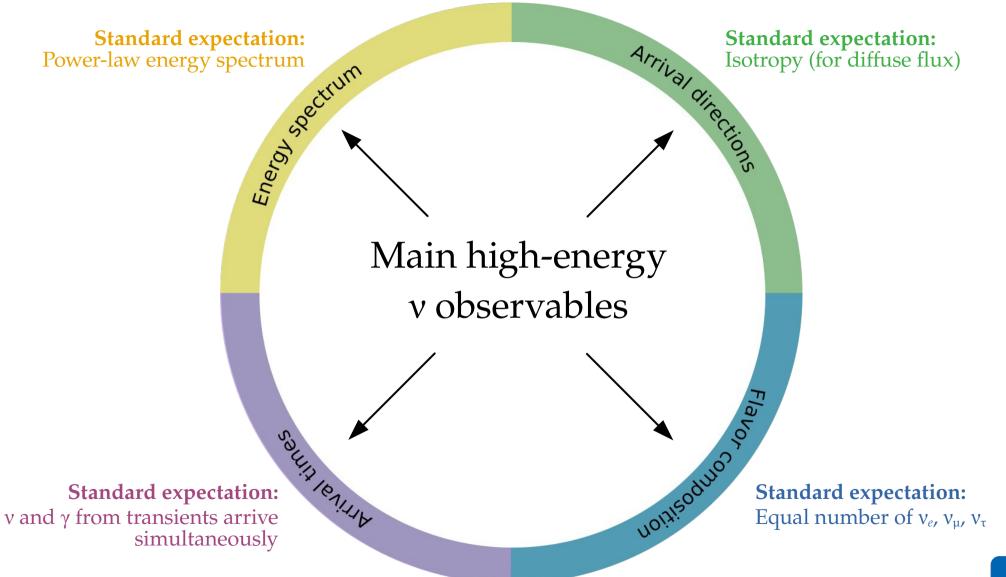
Poor angular resolution: $\geq 5^{\circ}$





Angular resolution: $< 1^{\circ}$





Standard expectation:
Power-law energy spectrum

Standard expectation: Isotropy (for diffuse flux

Standard expectation

v and γ from transients arrive simultaneously

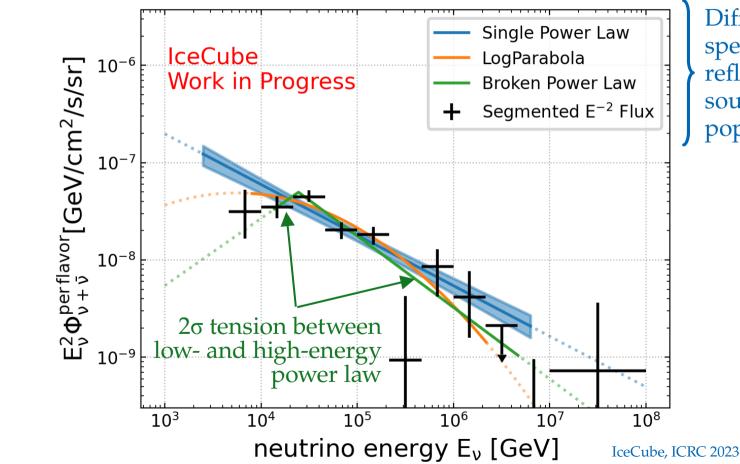
IEVITAL S

Standard expectation:

Equal number of v_e , v_{μ} , v_{τ}

Neutrino energy spectrum

With > 10 years of data, deviations from a power law start to be testable:



Different spectra might reflect different source populations **Standard expectation:** Power-law energy spectrum

Spectrum

Standard expectation:
Isotropy (for diffuse flux)

Arrival directions

Standard expectation

v and γ from transients arrive simultaneously

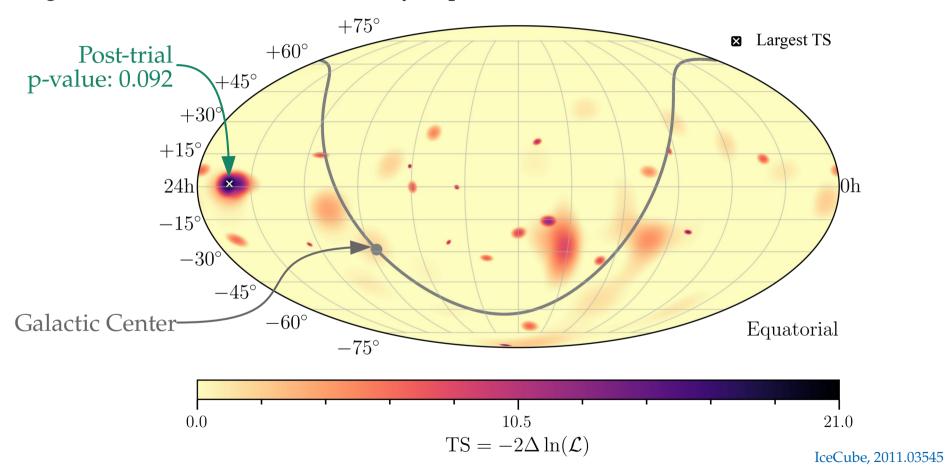
144 A

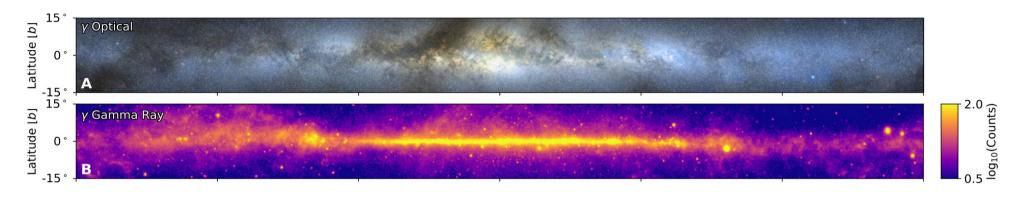
Standard expectation:

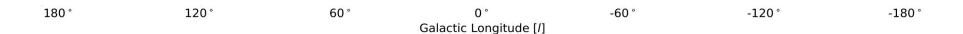
Equal number of v_e , v_μ , v_τ

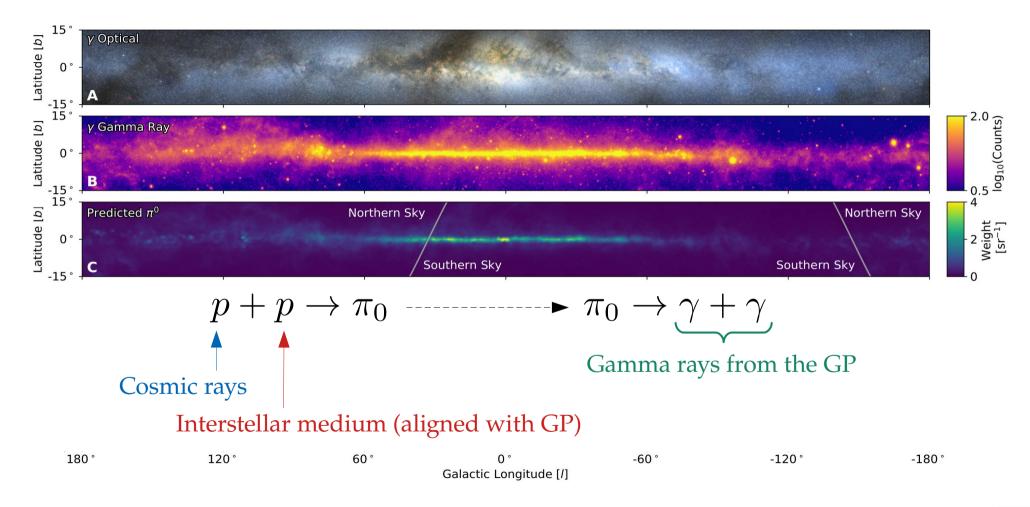
Distribution of arrival directions (7.5 yr)

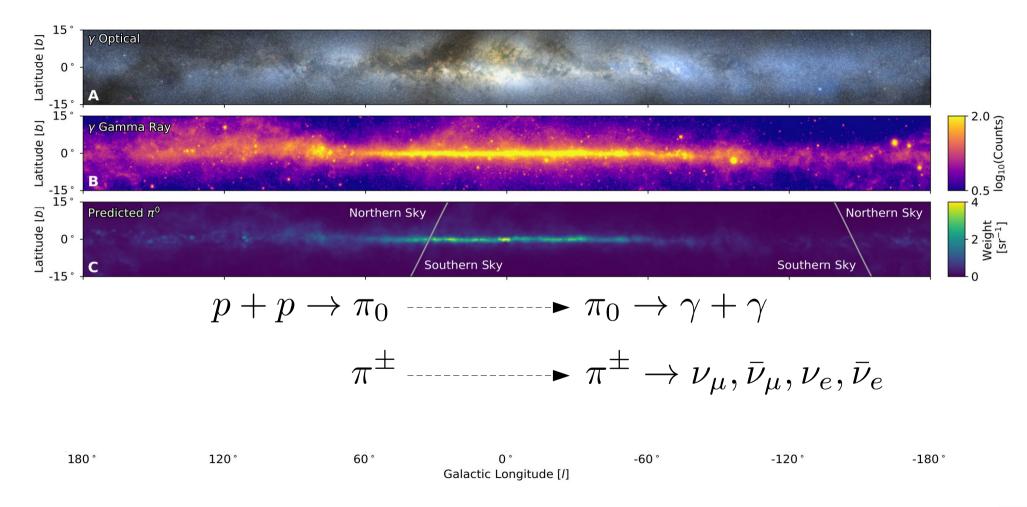
No significant excess in the neutrino skymap:

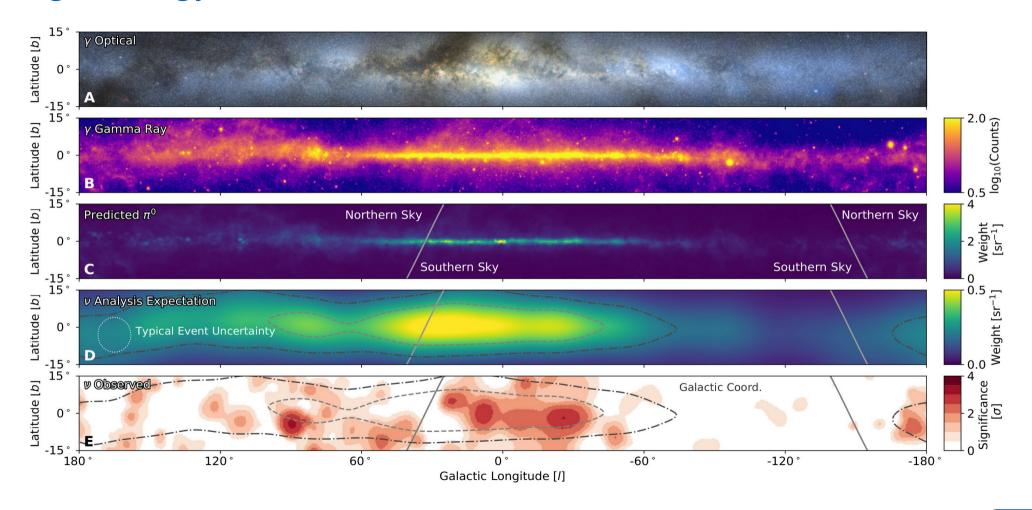


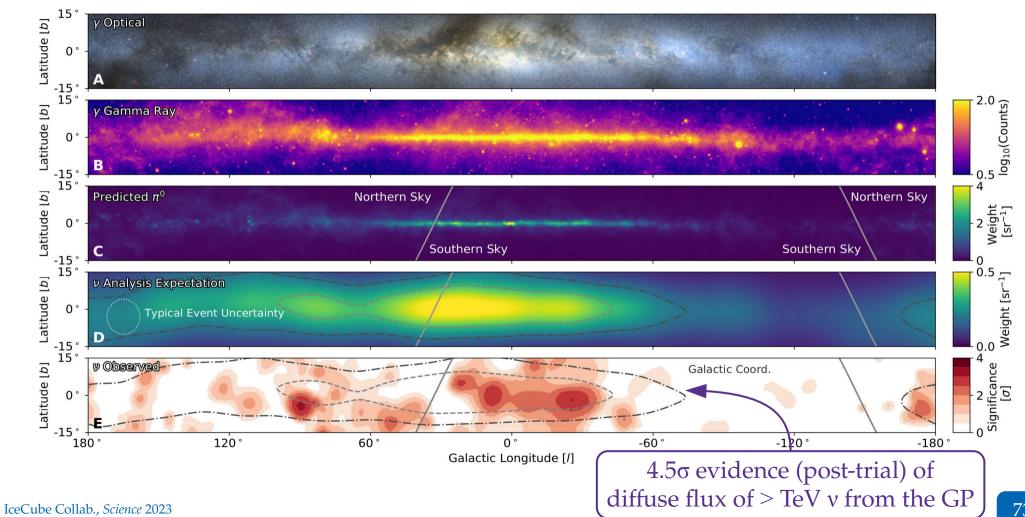












Standard expectation:

ower-law energy spectrum

Social

Standard expectation

Isotropy (for diffuse flux)

Te CH.

Standard expectation

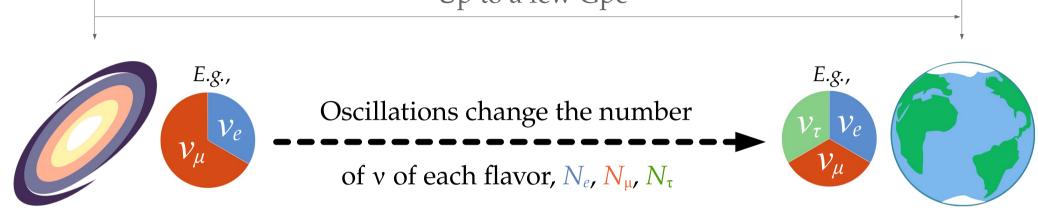
v and γ from transients arrive simultaneously

S IEVITAP

Standard expectation:

Equal number of ν_e, ν_μ, ν_τ

Up to a few Gpc



Different production mechanisms yield different flavor ratios:

$$(f_{e,S}, f_{\mu,S}, f_{\tau,S}) \equiv (N_{e,S}, N_{\mu,S}, N_{\tau,S})/N_{\text{tot}}$$

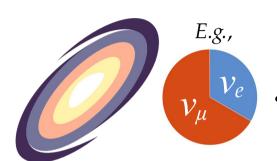
Flavor ratios at Earth ($\alpha = e, \mu, \tau$):

$$f_{\alpha,\oplus} = \sum_{\beta=e,\mu,\tau} P_{\nu_{\beta}\to\nu_{\alpha}} f_{\beta,S}$$



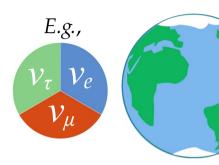
Earth

Up to a few Gpc



Oscillations change the number

of v of each flavor, N_e , N_{μ} , N_{τ}



Different production mechanisms yield different flavor ratios:

$$(f_{e,S}, f_{\mu,S}, f_{\tau,S}) \equiv (N_{e,S}, N_{\mu,S}, N_{\tau,S})/N_{\text{tot}}$$

Flavor ratios at Earth
$$(\alpha = e, \mu, \tau)$$

Flavor ratios at Earth (
$$\alpha = e, \mu, \tau$$
):
$$f_{\alpha, \oplus} = \sum_{\beta = e, \mu, \tau} P_{\nu_{\beta} \to \nu_{\alpha}} f_{\beta, S}$$

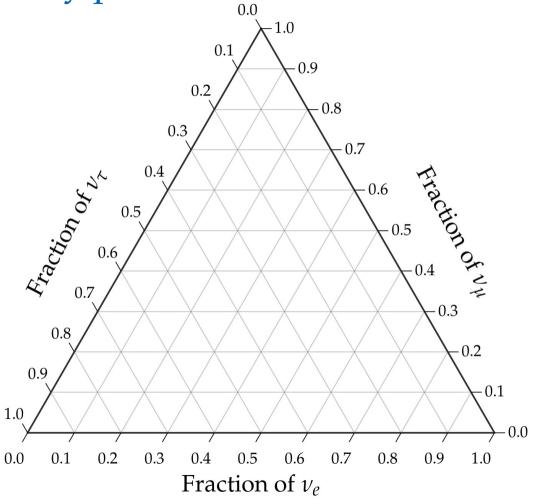
Standard oscillations or new physics

Assumes underlying unitarity – sum of projections on each axis is 1

How to read it:

Follow the tilt of the tick marks

Always in this order: (f_e, f_{μ}, f_{τ})

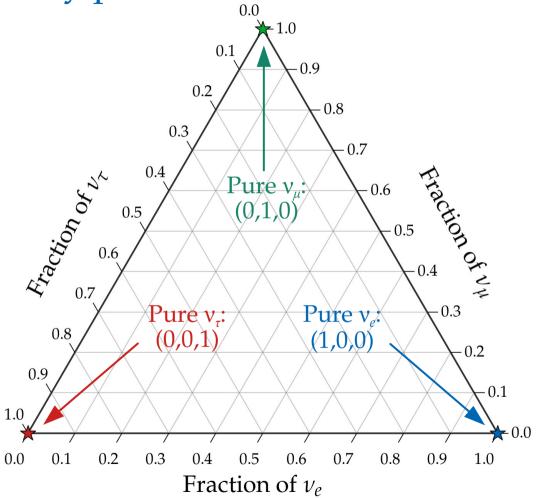


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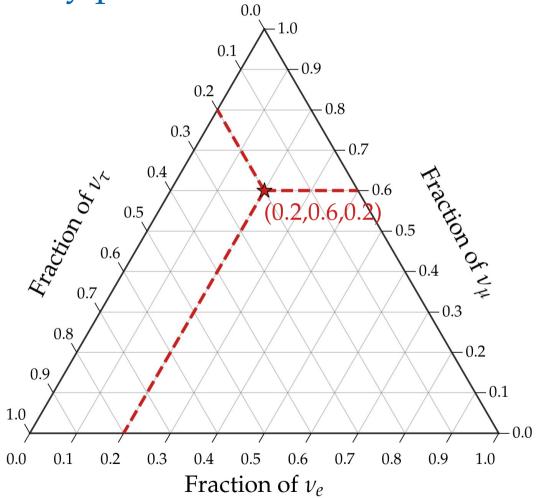


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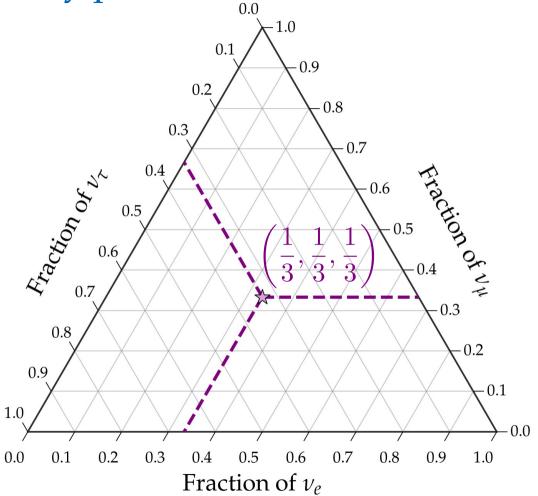


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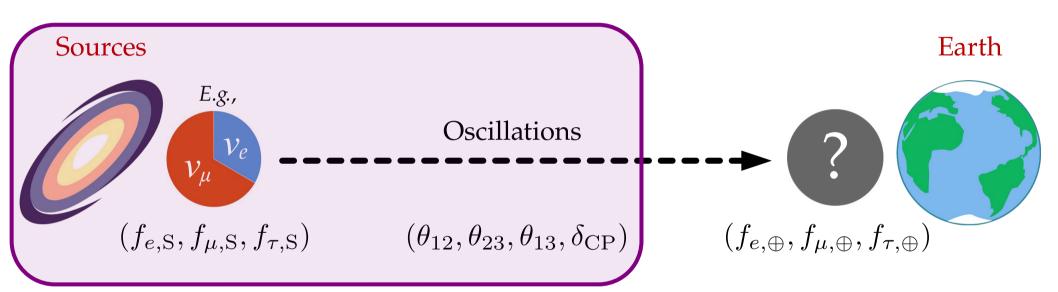
How to read it:

Follow the tilt of the tick marks

Always in this order: (f_e, f_{μ}, f_{τ})



From sources to Earth: we learn what to expect when measuring $f_{\alpha,\oplus}$



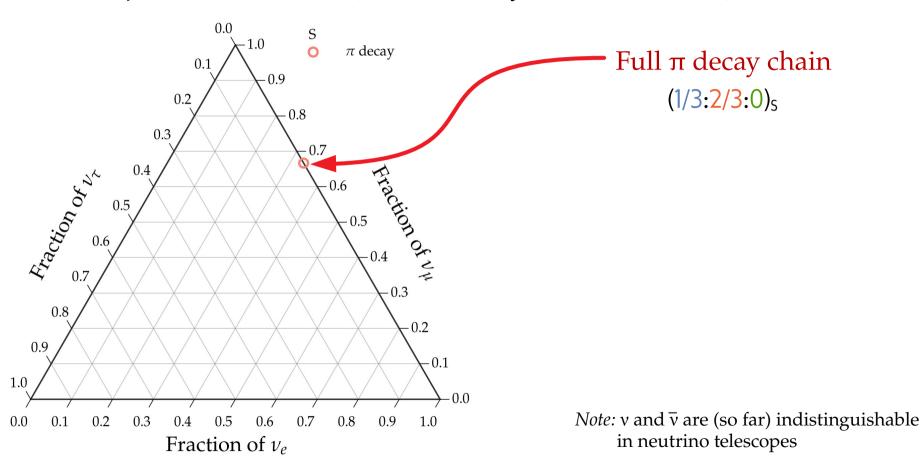
One likely TeV–PeV v production scenario: $p + \gamma \rightarrow \pi^+ \rightarrow \mu^+ + \frac{1}{\nu_{\mu}}$ followed by $\mu^+ \rightarrow e^+ + \frac{1}{\nu_{\mu}}$

Full π decay chain (1/3:2/3:0)₅

Note: v and \overline{v} are (so far) indistinguishable in neutrino telescopes

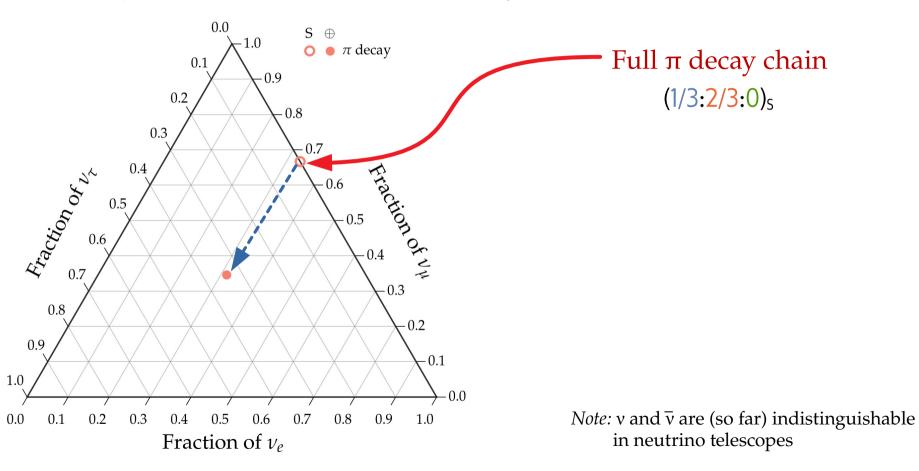
One likely TeV–PeV v production scenario:

$$p + \gamma \rightarrow \pi^+ \rightarrow \mu^+ + \nu_{\mu}$$
 followed by $\mu^+ \rightarrow e^+ + \nu_e + \overline{\nu_{\mu}}$



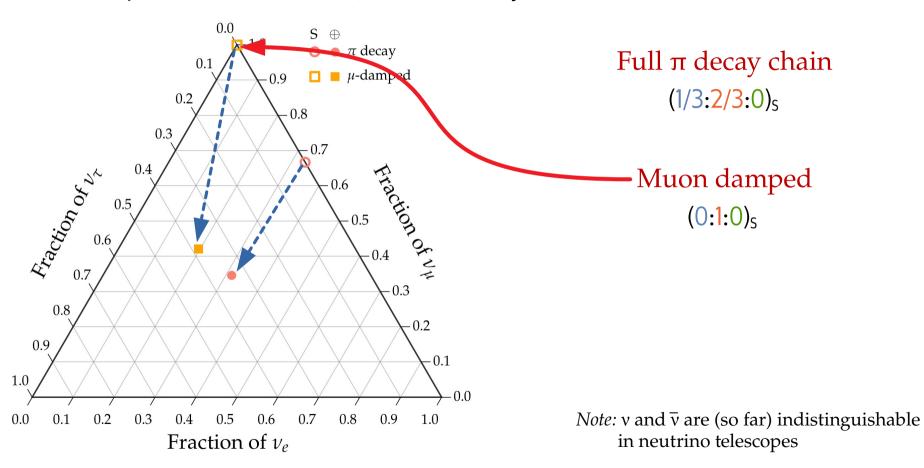
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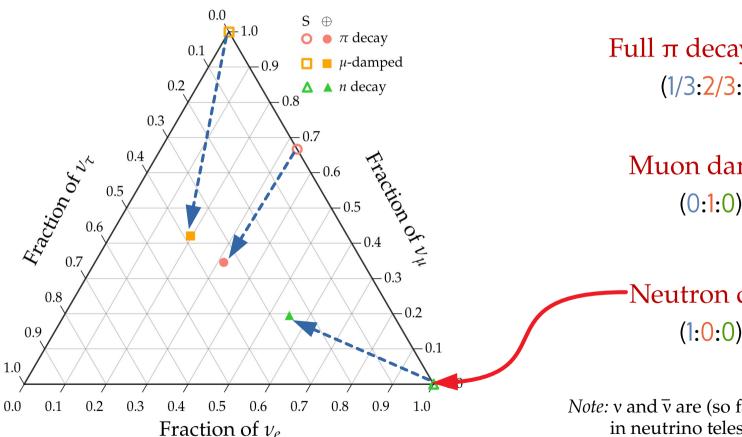
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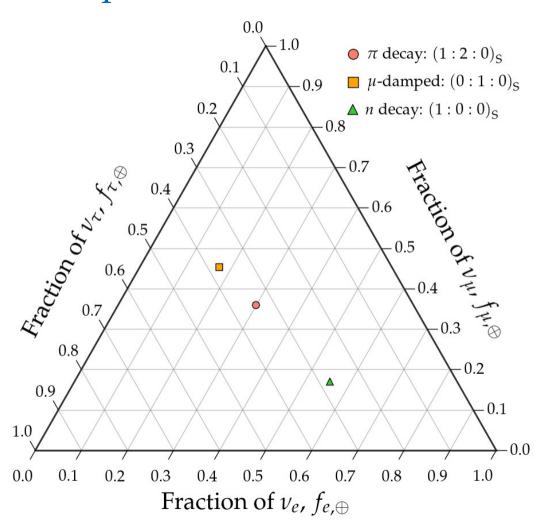


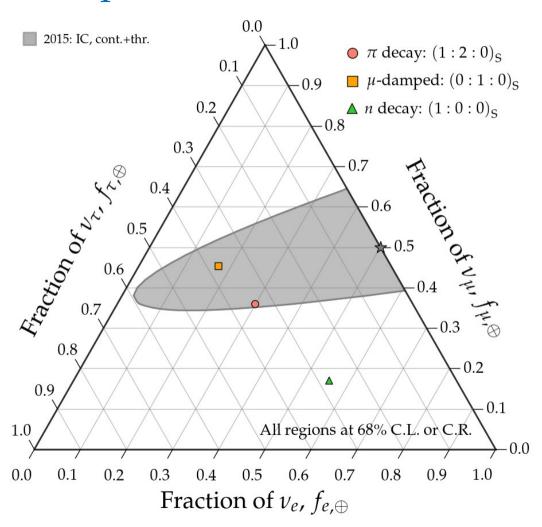
Full π decay chain $(1/3:2/3:0)_{5}$

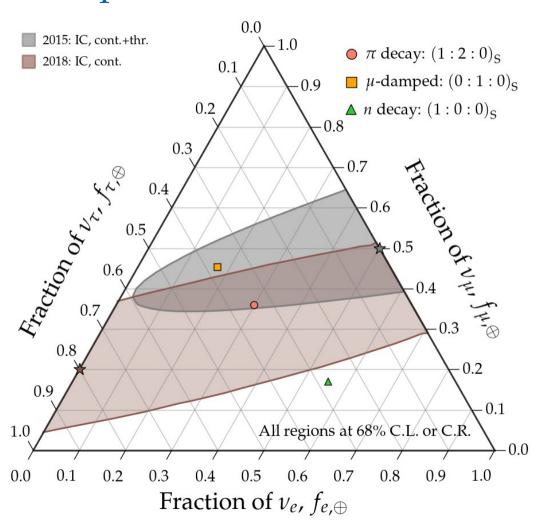
Muon damped $(0:1:0)_{S}$

Neutron decay $(1:0:0)_{S}$

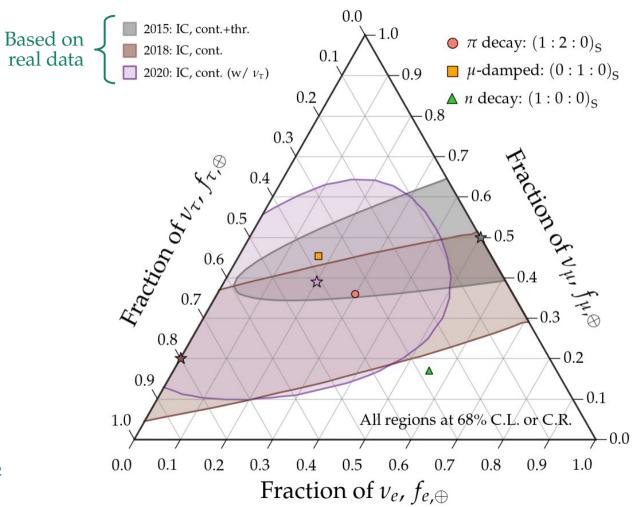
Note: v and \overline{v} are (so far) indistinguishable in neutrino telescopes







IceCube Collab., *EPJC* 2022 IceCube Collab., *PRD* 2019 IceCube Collab., *ApJ* 2015



Standard expectation: Power-law energy spectrum

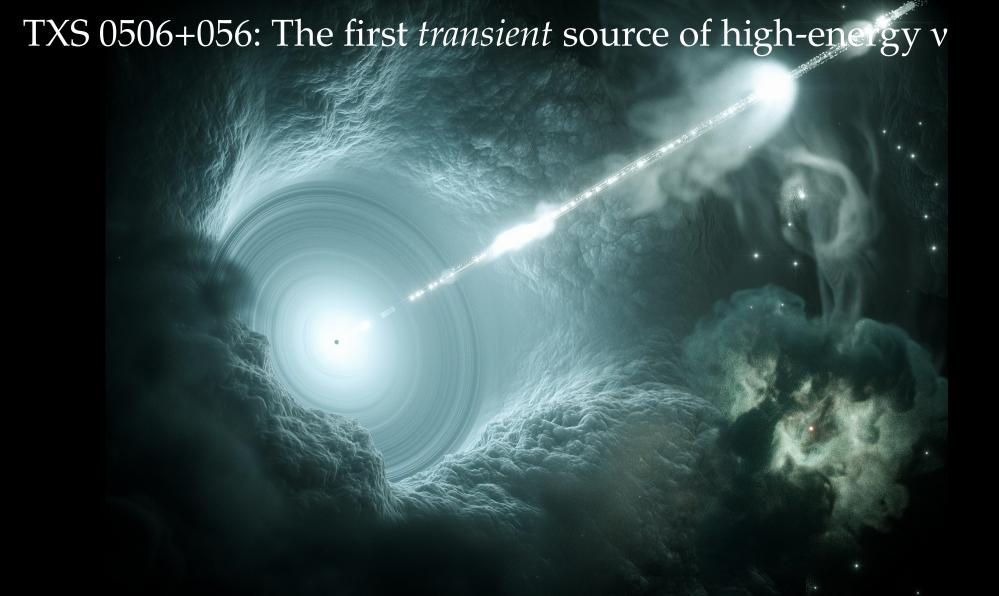
Standard expectation: Isotropy (for diffuse flux

Standard expectation: v and γ from transients arrive

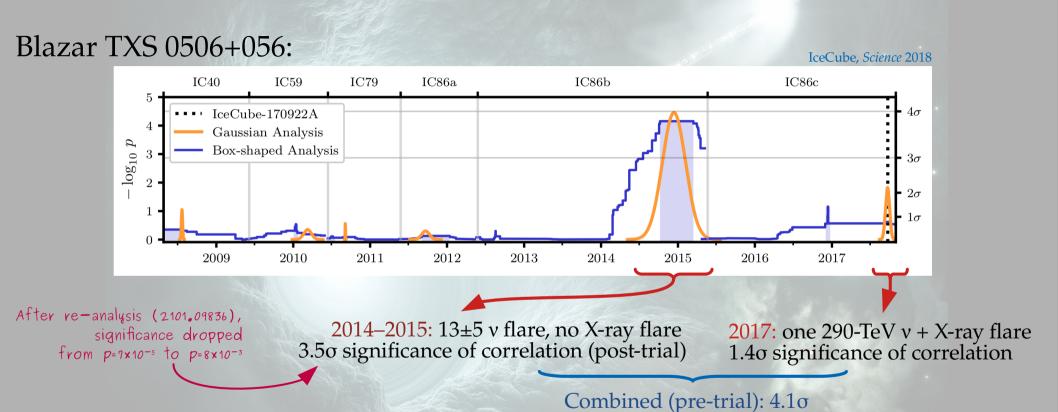
i γ from transients arrive simultaneously

noi il sodin

Standard expectation: Equal number of v_e , v_μ , v_τ



TXS 0506+056: The first transient source of high-energy v



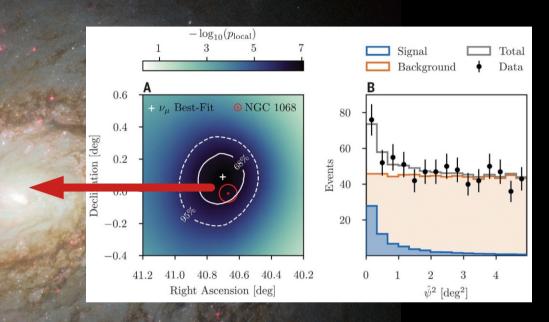
NGC1068: The first steady-state source of high-energy v

Active galactic nucleus

Brightest type-2 Seyfert

 79^{+22}_{-20} v of TeV energy

Significance: 4.2\significance)



Today TeV–PeV v

Astro: Find & understand sources

Particle: Turn predictions into tests

Key developments:

Larger statistics

Better reconstruction

Smaller astrophysical uncertainties

High-energy neutrino physics today

Fundamental physics with high-energy cosmic neutrinos

► Numerous new v physics effects grow as $\sim \kappa_n \cdot E^n \cdot L$

► So we can probe $\kappa_n \sim 4 \cdot 10^{-47} \, (E/\text{PeV})^{-n} \, (L/\text{Gpc})^{-1} \, \text{PeV}^{1-n}$

▶ Improvement over limits using atmospheric v: κ_0 < 10⁻²⁹ PeV, κ_1 < 10⁻³³

Fundamental physics with high-energy cosmic neutrinos

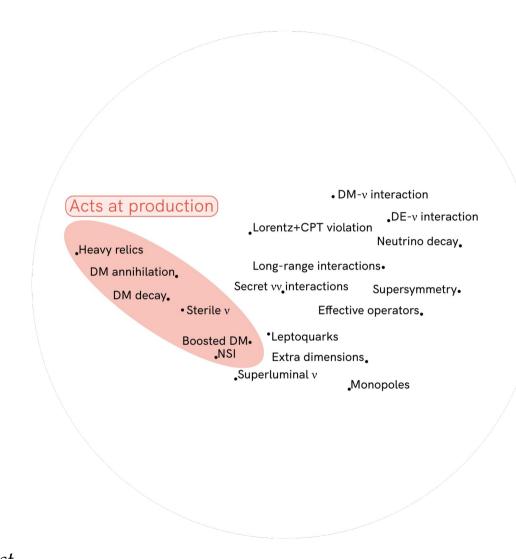
► Numerous new v physics effects grow as ~ $\kappa_n \cdot E^n \cdot L$ $\begin{cases} E.g., \\ n = -1: \text{ neutrino decay} \\ n = 0: \text{ CPT-odd Lorentz violation} \\ n = +1: \text{ CPT-even Lorentz violation} \end{cases}$

► So we can probe $\kappa_n \sim 4 \cdot 10^{-47} \, (E/\text{PeV})^{-n} \, (L/\text{Gpc})^{-1} \, \text{PeV}^{1-n}$

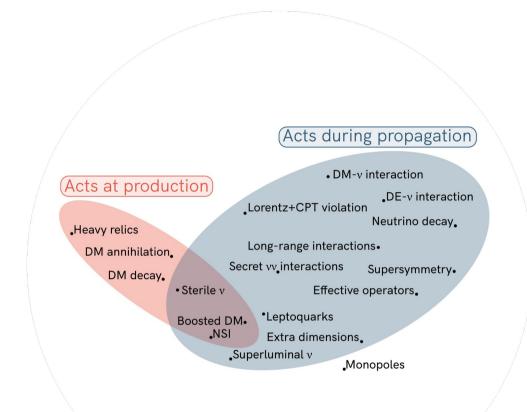
▶ Improvement over limits using atmospheric v: κ_0 < 10⁻²⁹ PeV, κ_1 < 10⁻³³

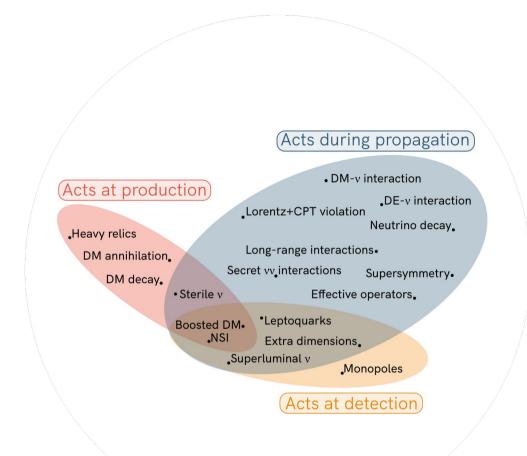


Note: Not an exhaustive list

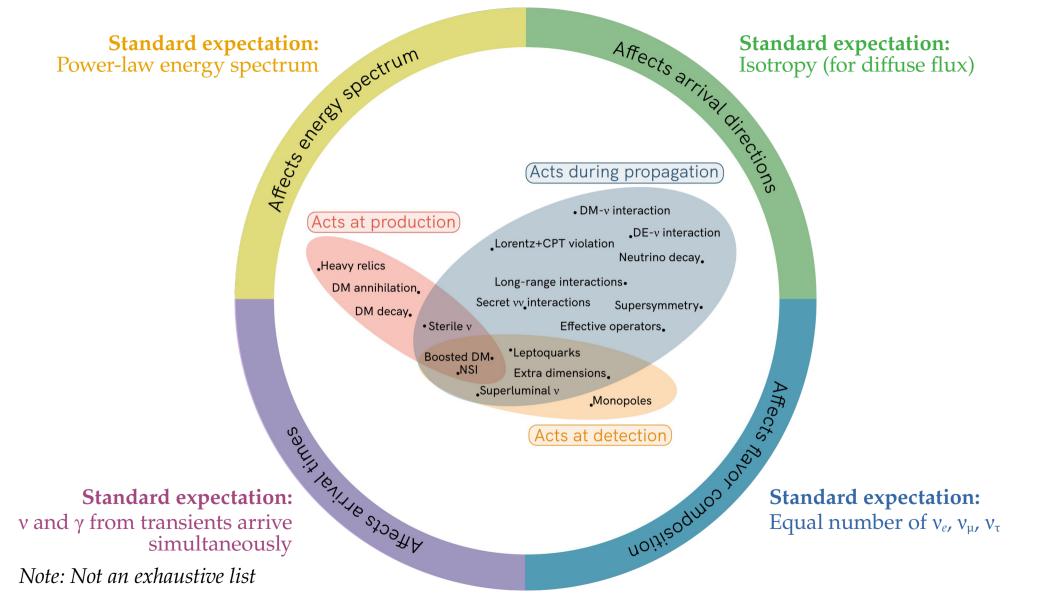


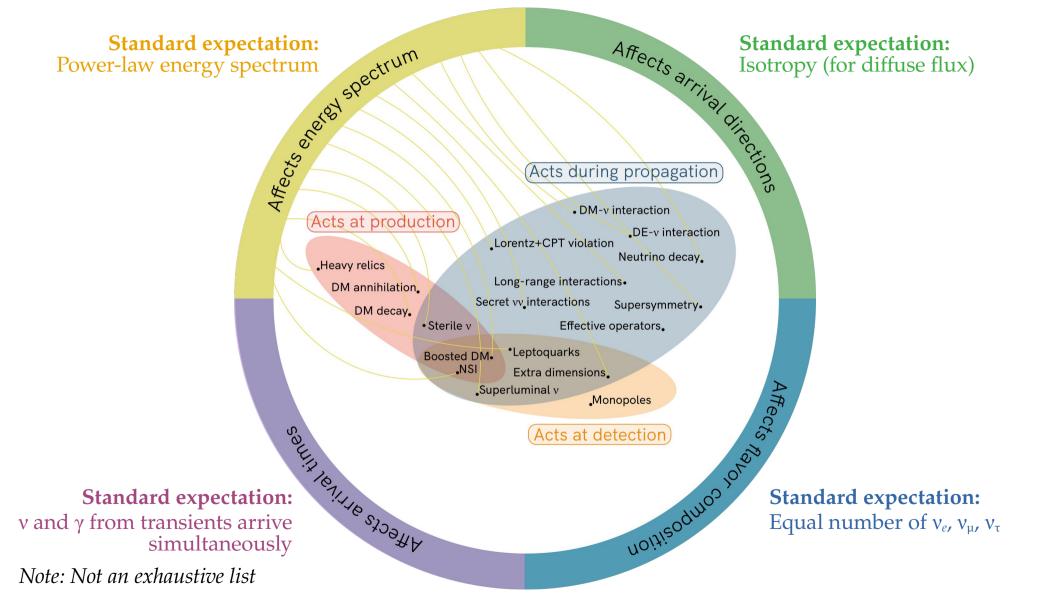
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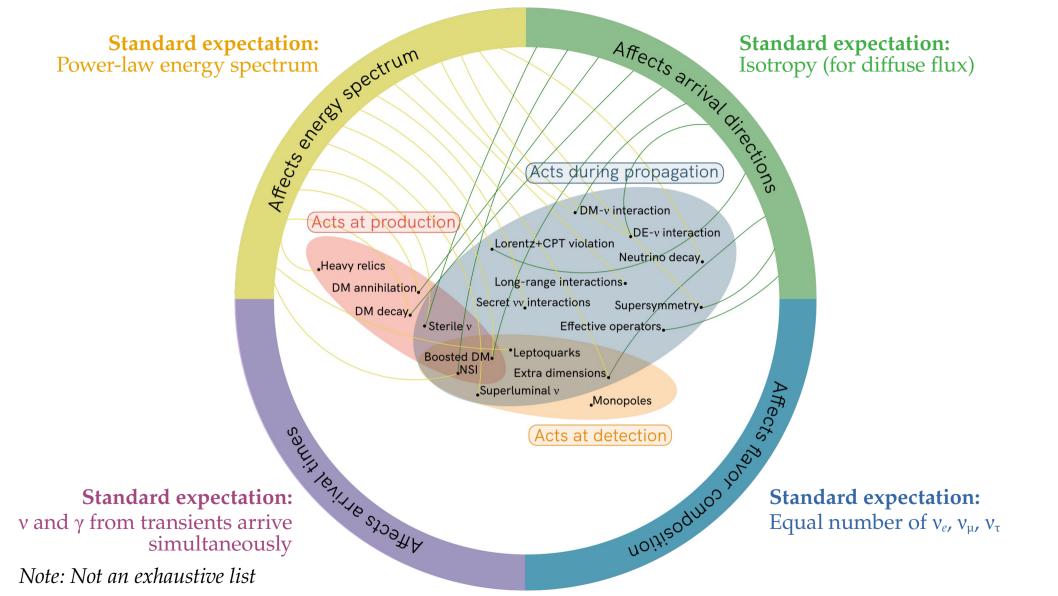


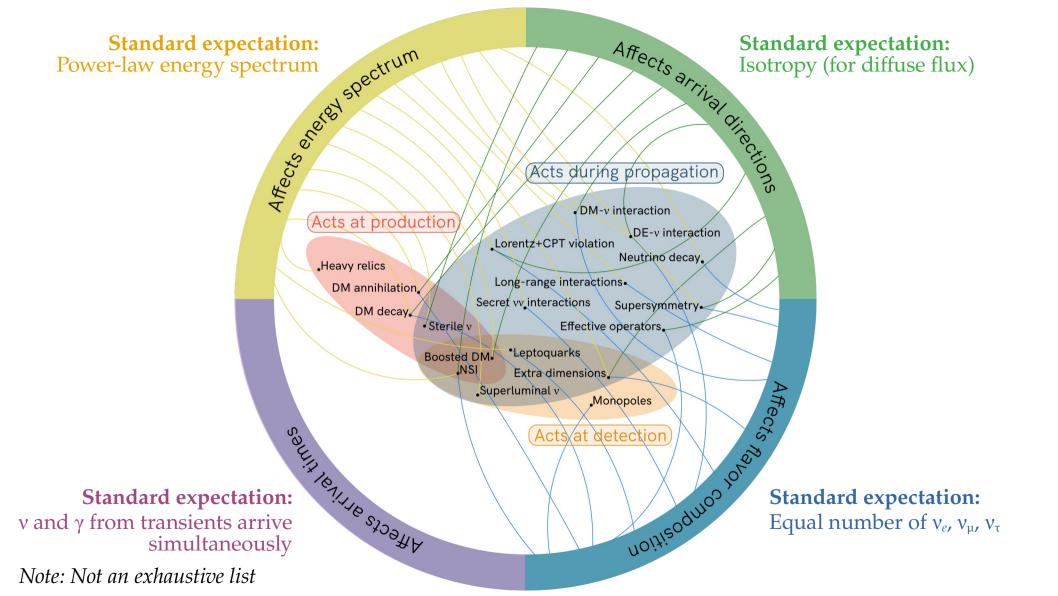


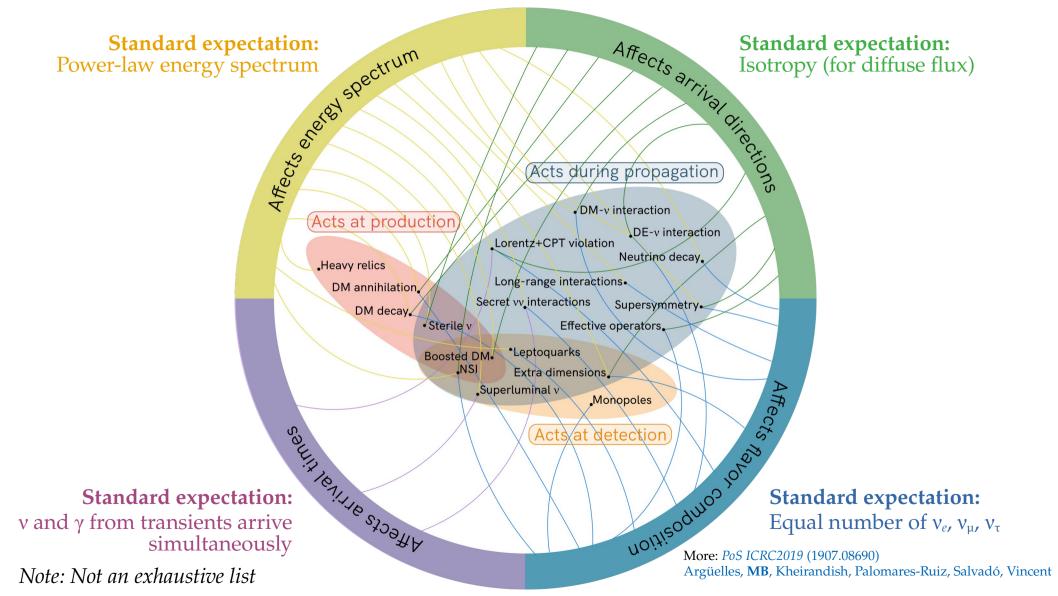
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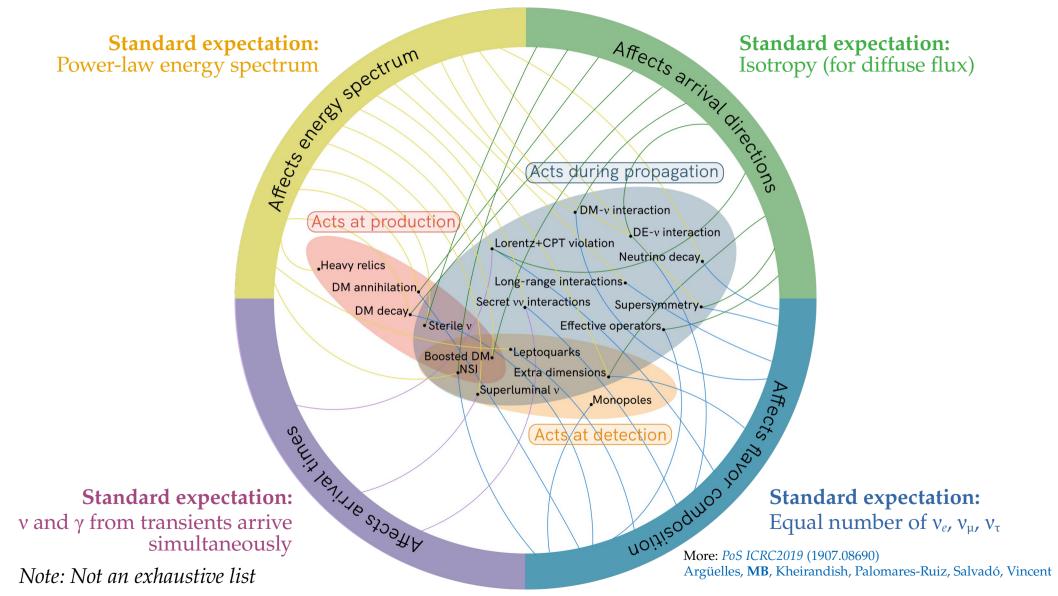


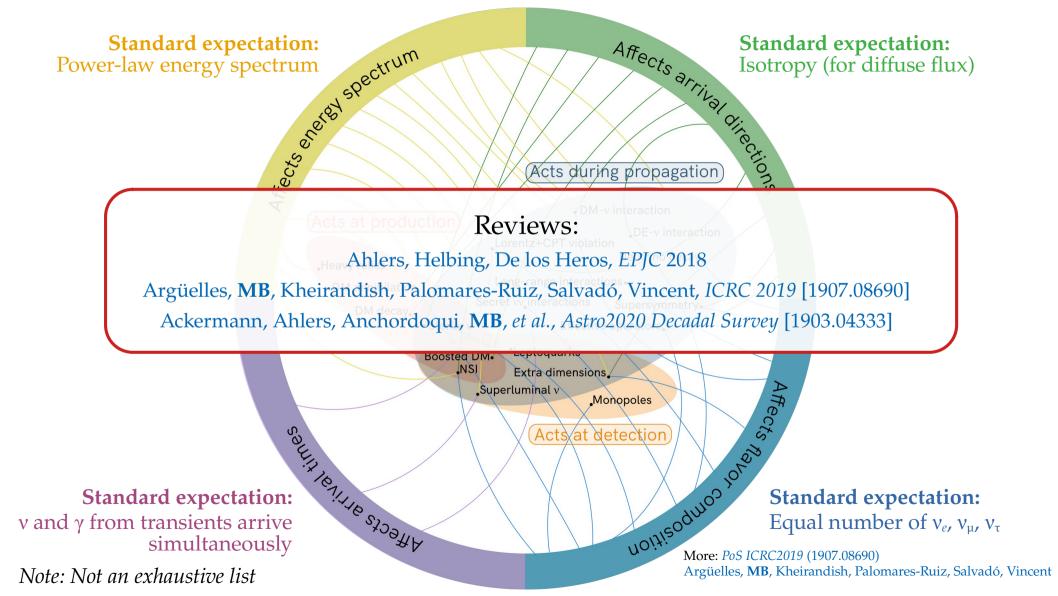










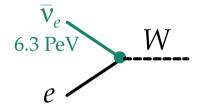


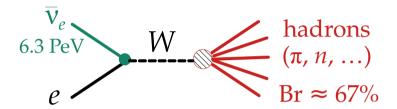
A selection of neutrino physics

- 1 Discovering the Glashow resonance
- 2 Neutrino-matter cross section
- 3 Flavor physics
- 4 Dark matter
- 5 Secret neutrino interactions
- 6 Neutrino decay

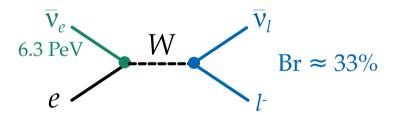
Find this in the backup slides

1. Glashow resonance: Long-sought, finally seen

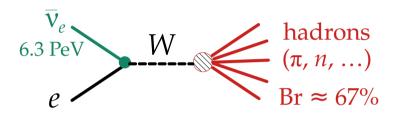


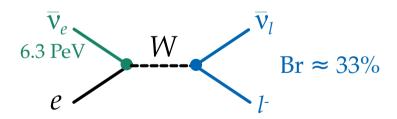




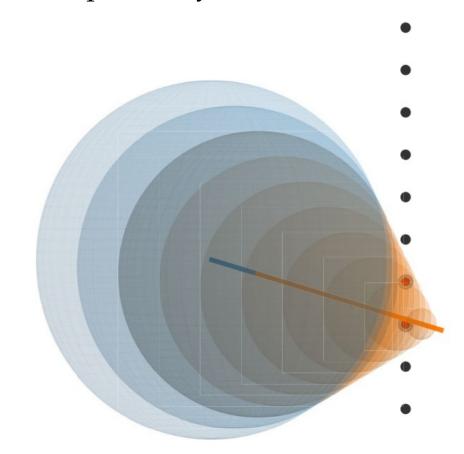


Predicted in 1960:



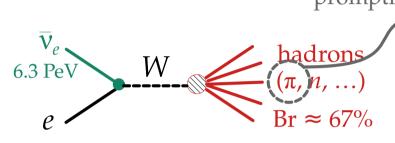


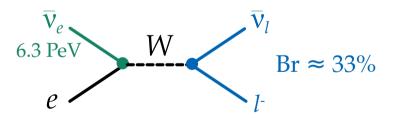
First reported by IceCube in 2021:

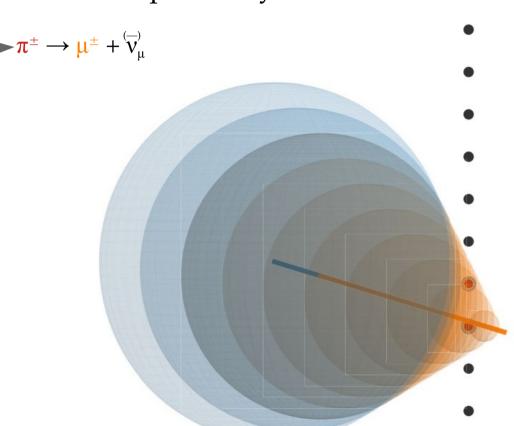


Predicted in 1960: First reported by IceCube in 2021:

Pions decay promptly

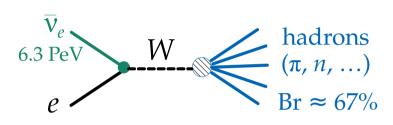


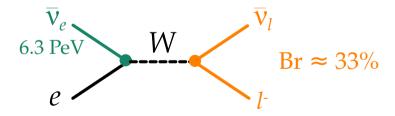




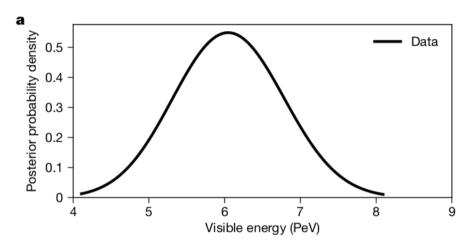
Predicted in 1960: First reported by IceCube in 2021: Pions decay promptly hadrons W6.3 PeV Early muons detected $Br \approx 67\%$ before the shower W6.3 PeV $Br \approx 33\%$

Predicted in 1960:



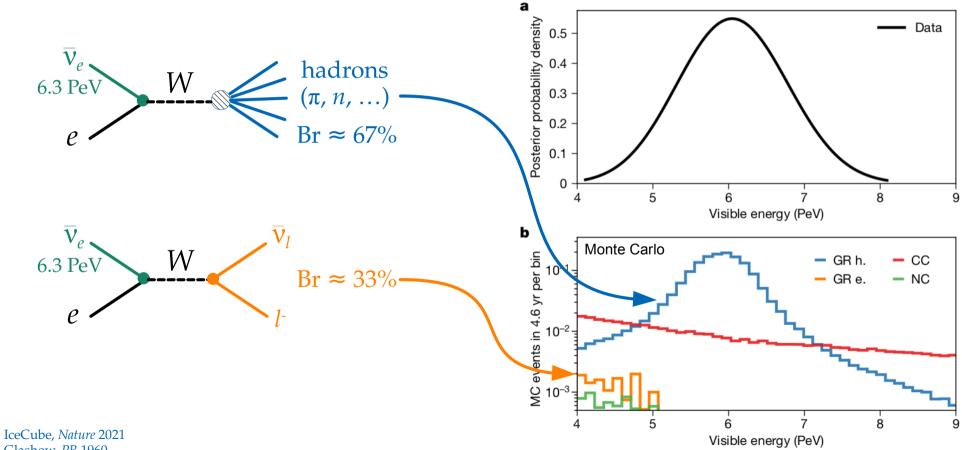


First reported by IceCube in 2021:

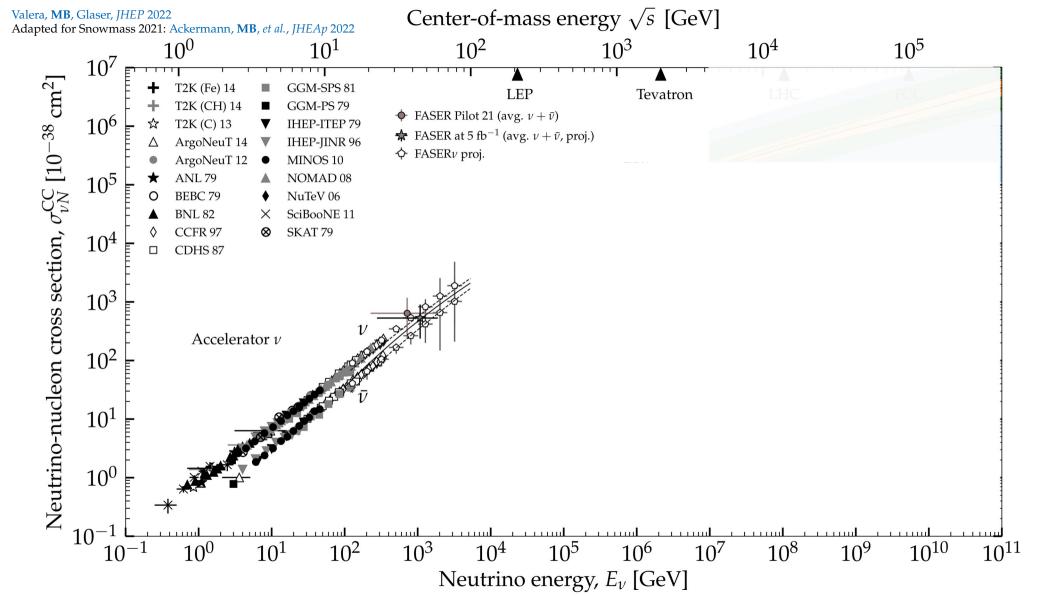


Predicted in 1960:

First reported by IceCube in 2021:



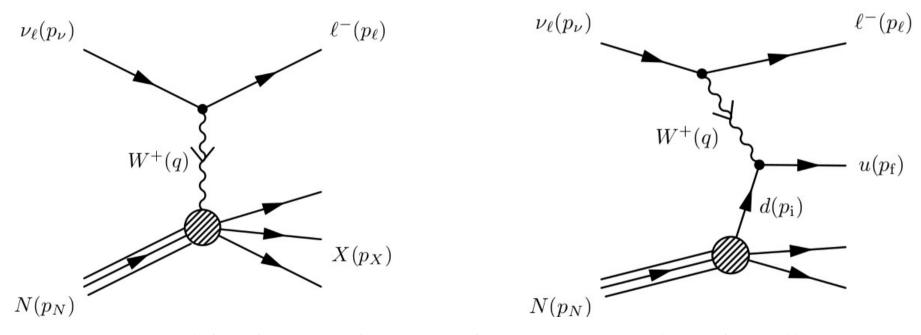
2. Neutrino-matter cross section: From TeV to PeV



How does DIS probe nucleon structure?

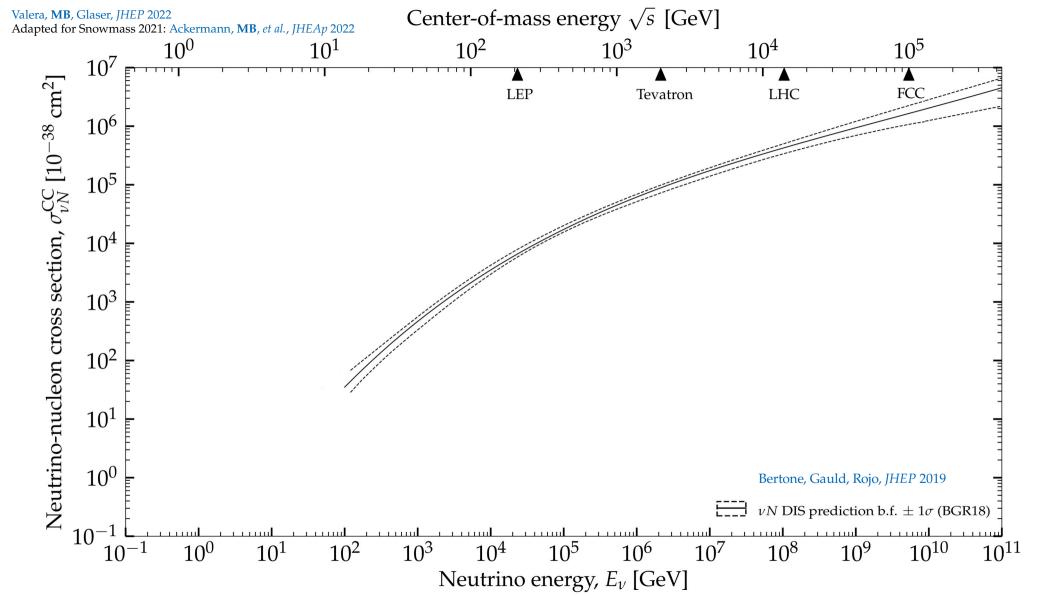
What you see

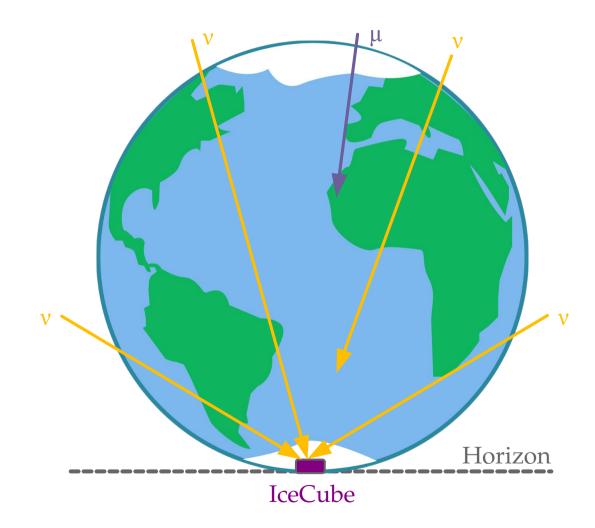
Beneath the hood

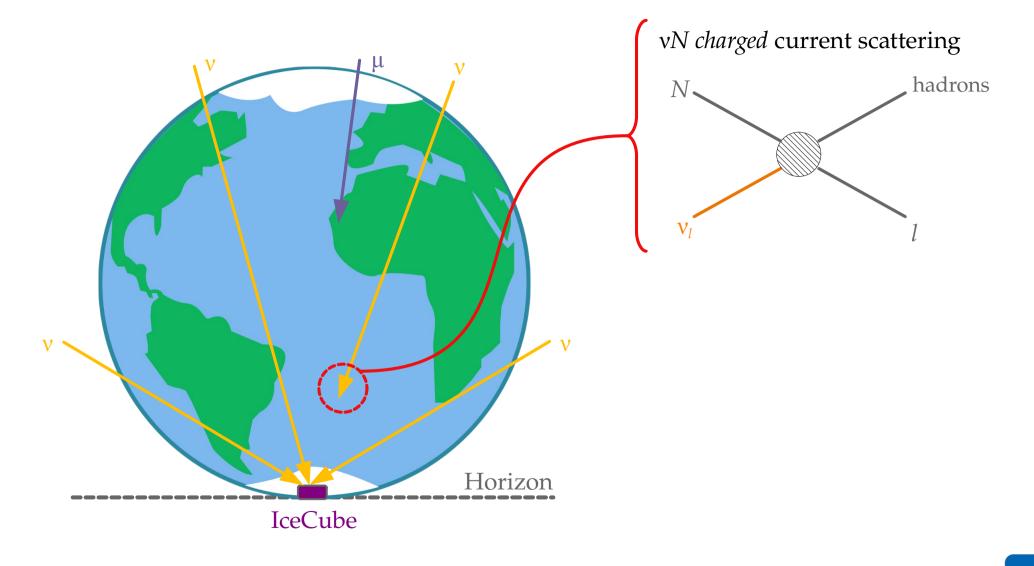


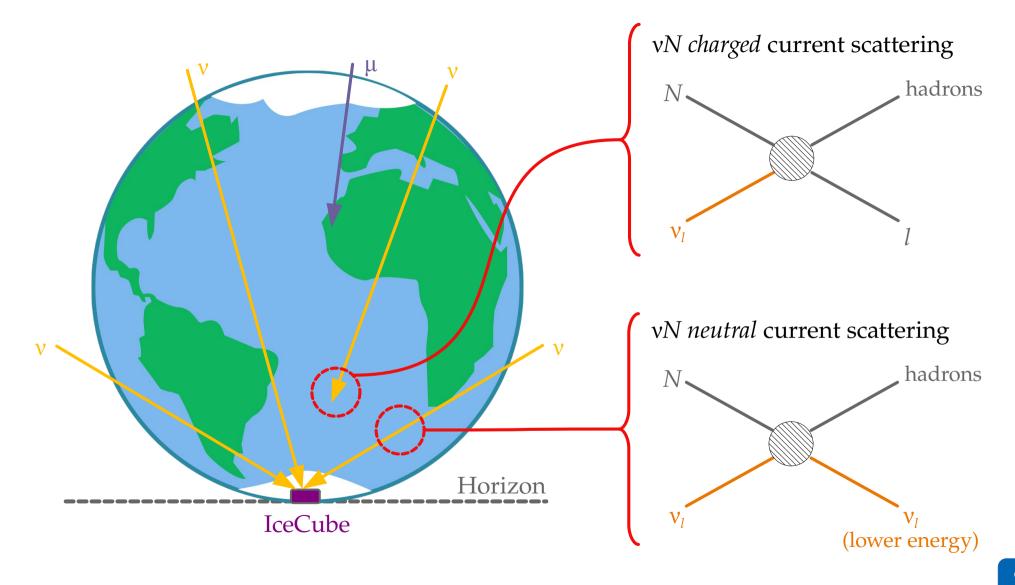
(Plus the equivalent neutral-current process (*Z*-exchange))

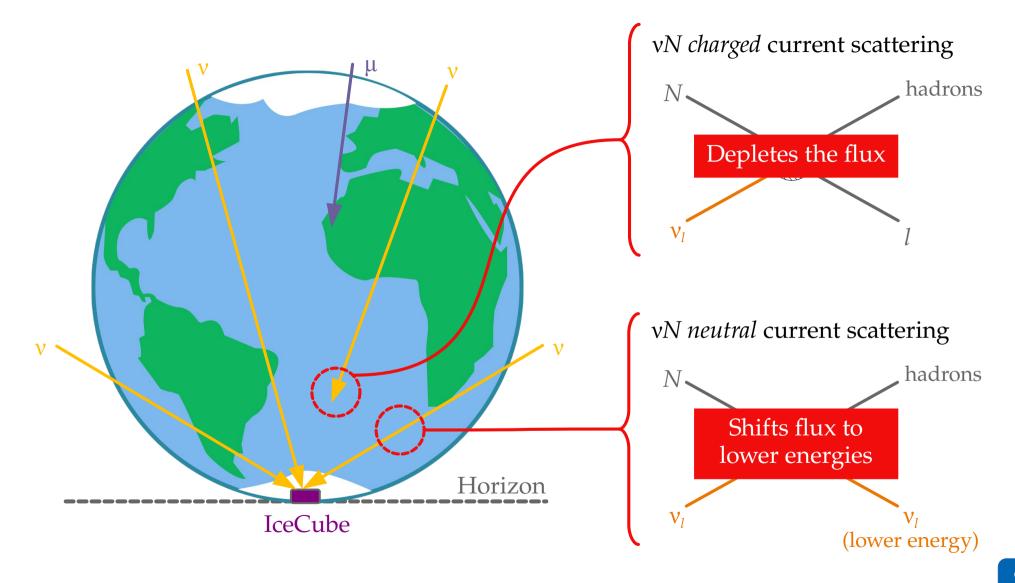
Giunti & Kim, Fundamentals of Neutrino Physics & Astrophysics





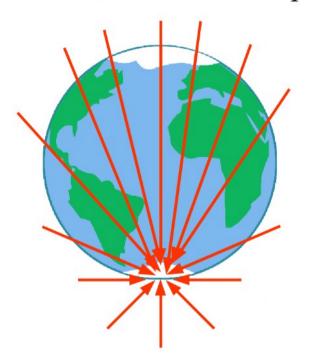




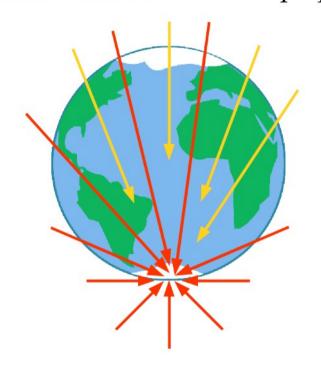


Measuring the high-energy *vN* cross section

Below ~ 10 TeV: Earth is transparent

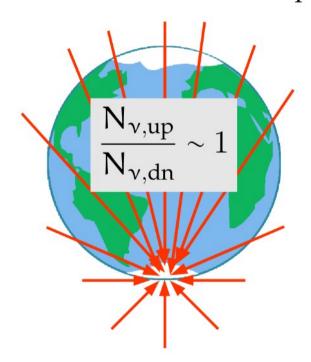


Above ~ 10 TeV: Earth is opaque

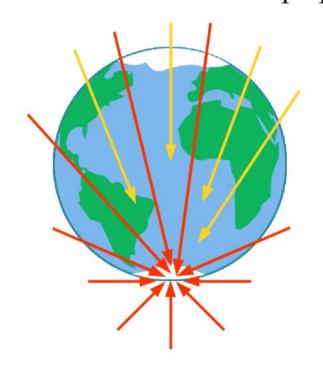


Measuring the high-energy *vN* cross section

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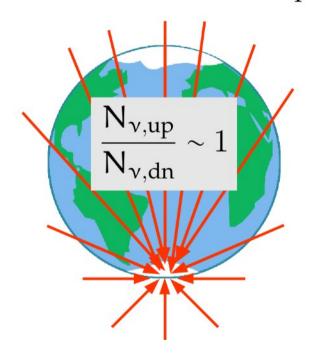


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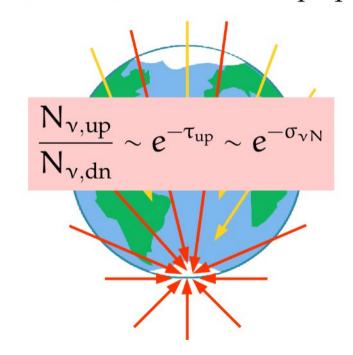


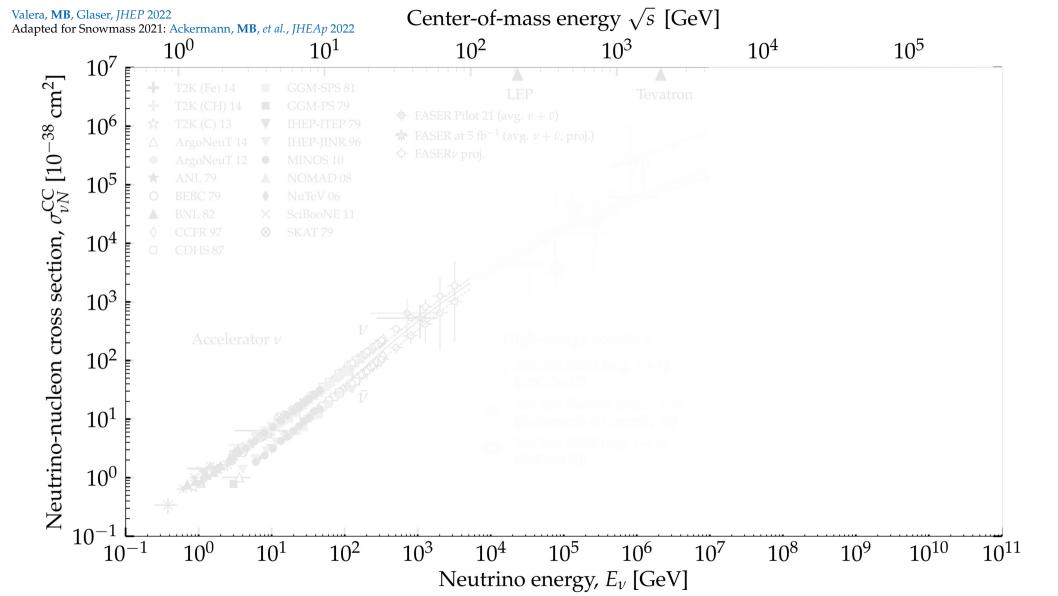
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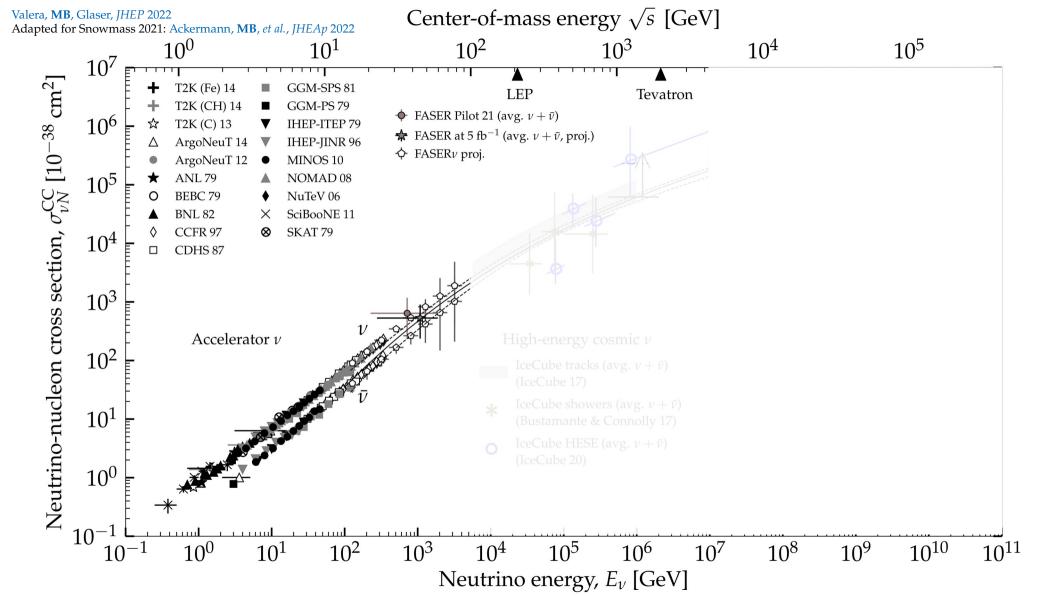
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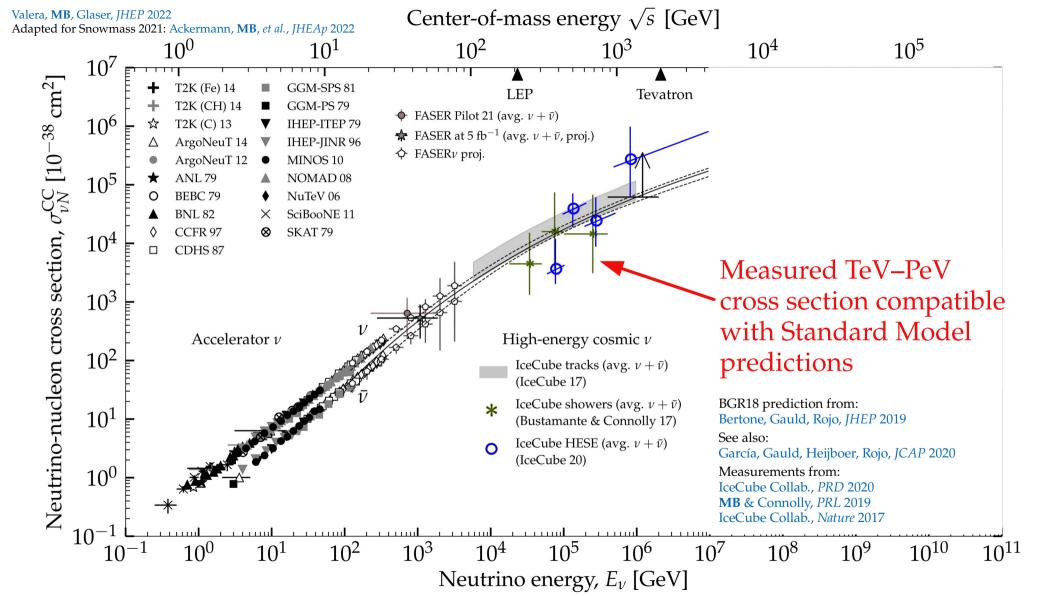


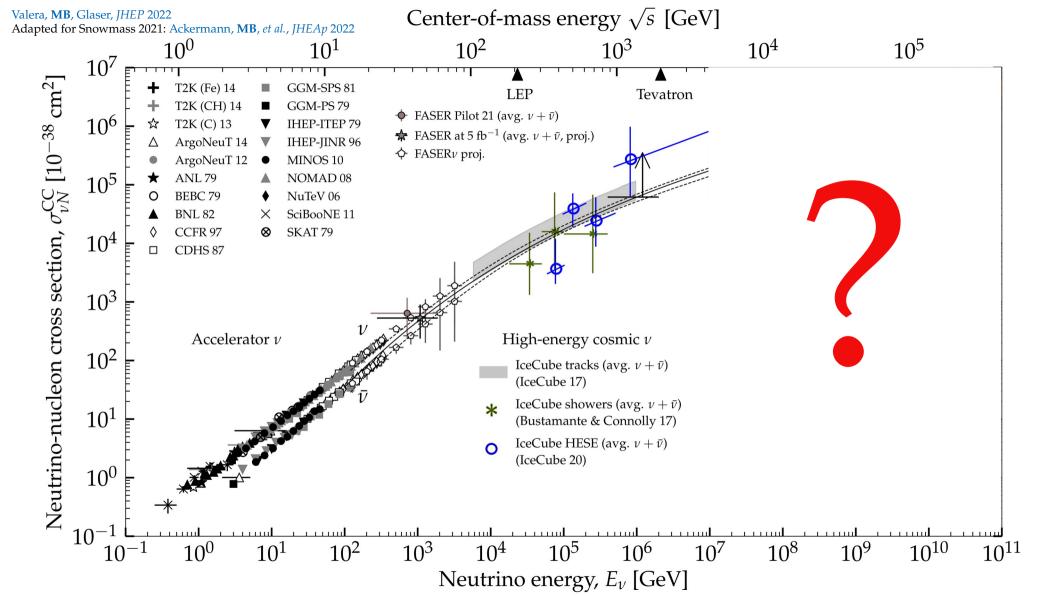
Above ~ 10 TeV: Earth is opaque





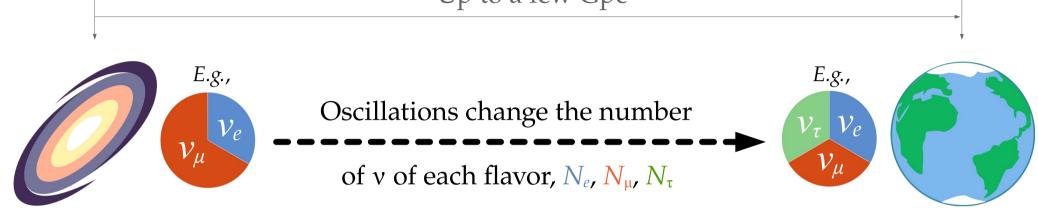






3. New physics via flavor *Hard to do, but worth it*

Up to a few Gpc



Different production mechanisms yield different flavor ratios:

$$(f_{e,S}, f_{\mu,S}, f_{\tau,S}) \equiv (N_{e,S}, N_{\mu,S}, N_{\tau,S})/N_{\text{tot}}$$

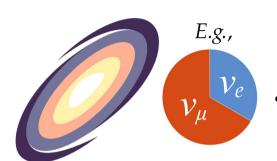
Flavor ratios at Earth ($\alpha = e, \mu, \tau$):

$$f_{\alpha,\oplus} = \sum_{\beta=e,\mu,\tau} P_{\nu_{\beta}\to\nu_{\alpha}} f_{\beta,S}$$



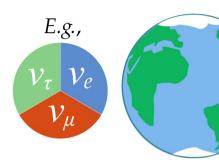
Earth

Up to a few Gpc



Oscillations change the number

of v of each flavor, N_e , N_{μ} , N_{τ}



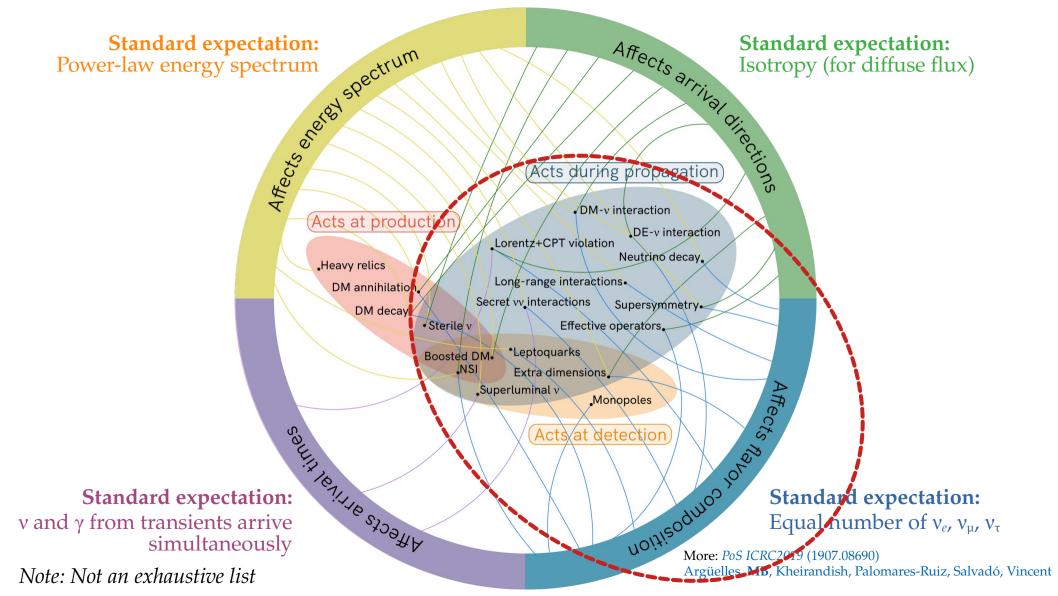
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$$(\alpha = e, \mu, \tau)$$

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Standard oscillations or new physics

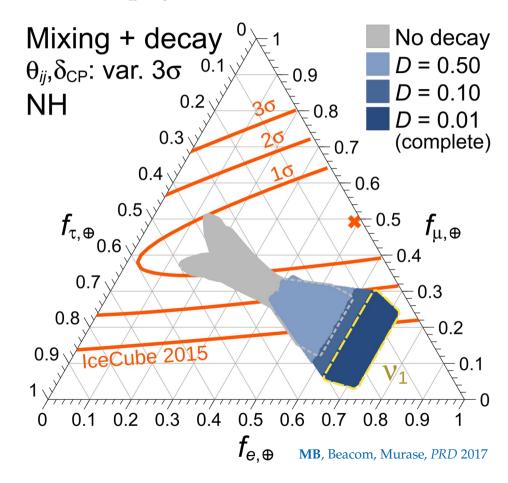


Repurpose the flavor sensitivity to test new physics:

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► Neutrino decay [Beacom *et al.*, *PRL* 2003; Baerwald, **MB**, Winter, JCAP 2010; **MB**, Beacom, Winter, *PRL* 2015; **MB**, Beacom, Murase, *PRD* 2017]

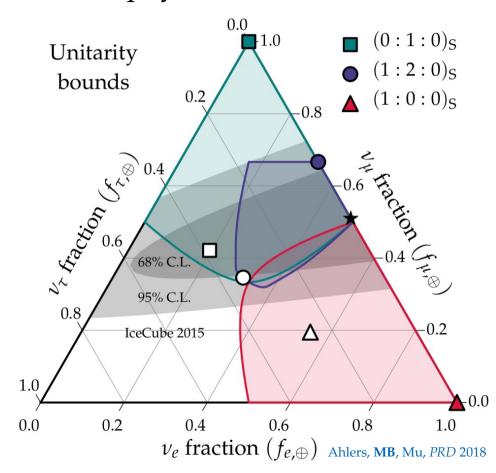


Reviews:

Mehta & Winter, JCAP 2011; Rasmussen et al., PRD 2017

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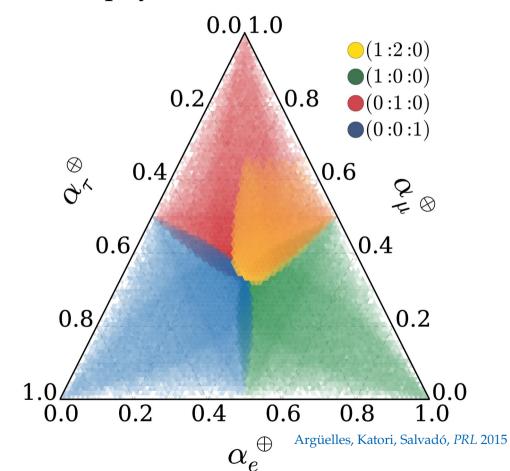


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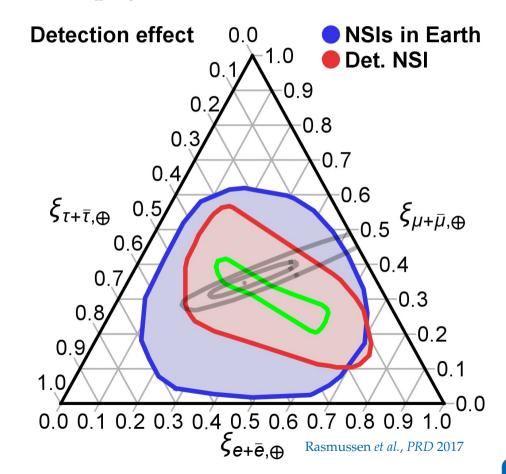
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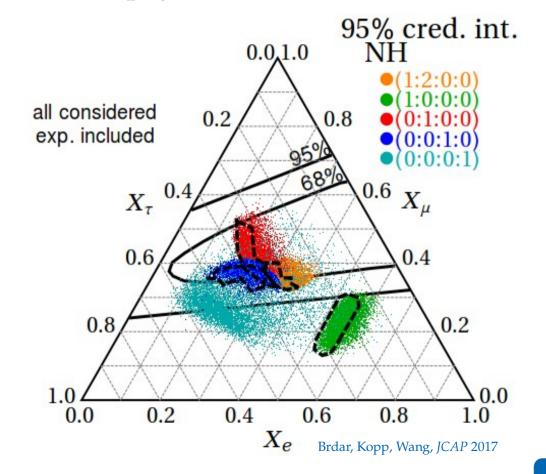
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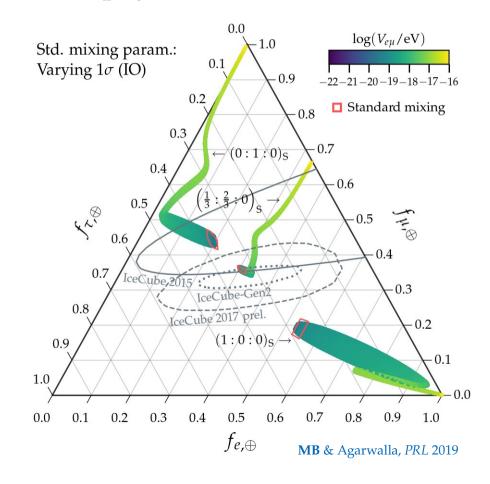
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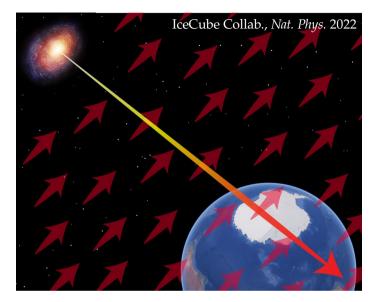
► Active-sterile v mixing
[Aeikens et al., JCAP 2015; Brdar, Kopp, Wang, JCAP 2017;
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► Long-range ev interactions [MB & Agarwalla, PRL 2019]

Reviews:



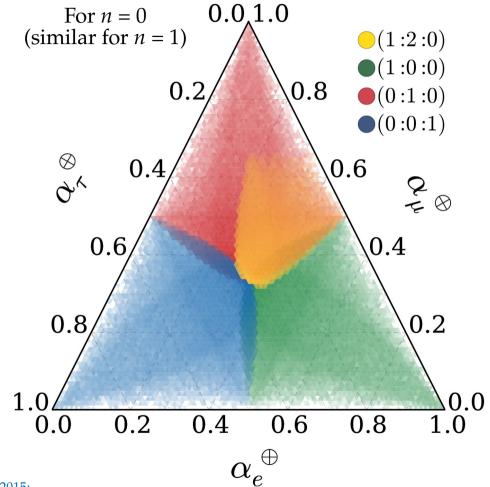
Lorentz-invariance violation can fill up the flavor triangle



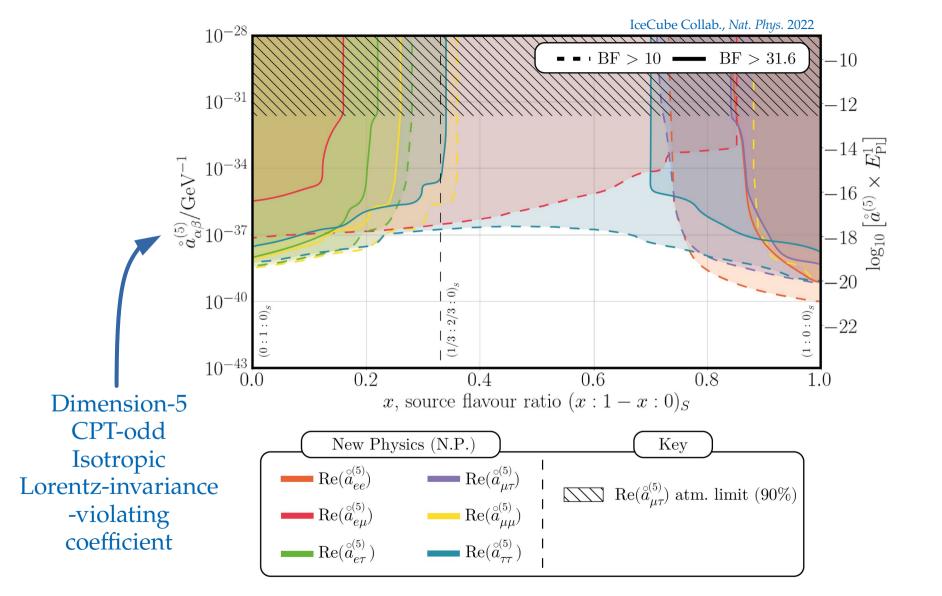
$$H_{\text{tot}} = H_{\text{std}} + H_{\text{NP}}$$

$$H_{\mathrm{std}} = \frac{1}{2E} U_{\mathrm{PMNS}}^{\dagger} \operatorname{diag}\left(0, \Delta m_{21}^{2}, \Delta m_{31}^{2}\right) U_{\mathrm{PMNS}}$$

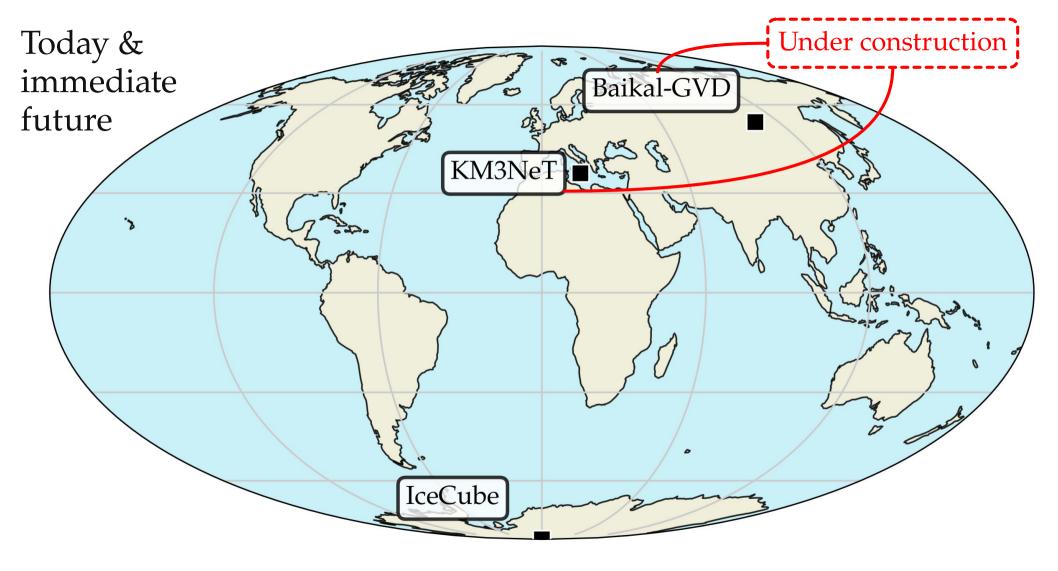
$$H_{\mathsf{NP}} = \sum \left(\frac{E}{\Lambda_n}\right)^n U_n^{\dagger} \operatorname{diag}\left(O_{n,1}, O_{n,2}, O_{n,3}\right) U_n$$

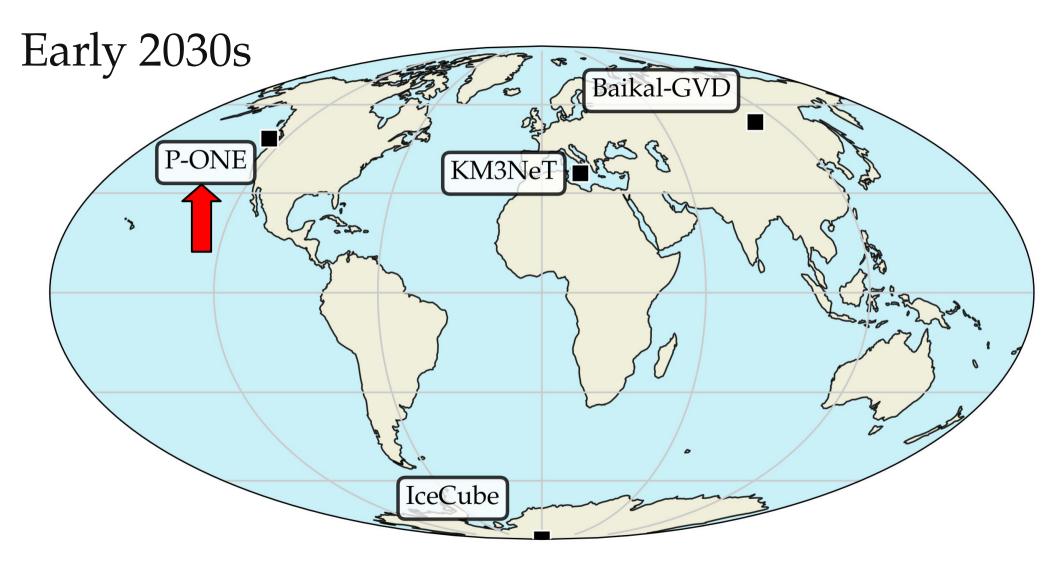


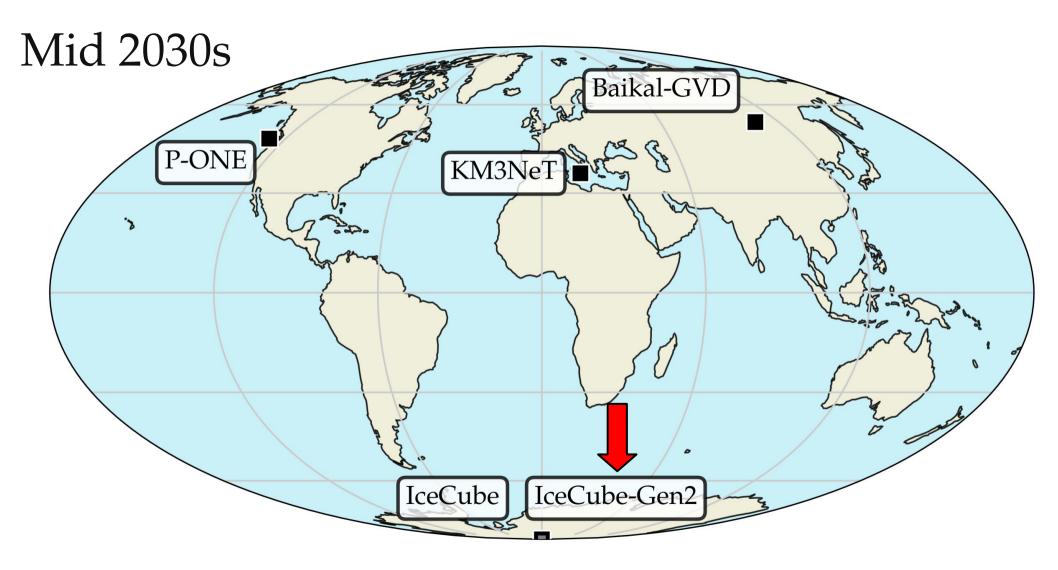
See also: Ahlers, **MB**, Mu, *PRD* 2018; Rasmusen *et al.*, *PRD* 2017; **MB**, Beacom, Winter *PRL* 2015; **MB**, Gago, Peña-Garay *JCAP* 2010; Bazo, **MB**, Gago, Miranda *IJMPA* 2009; + many others

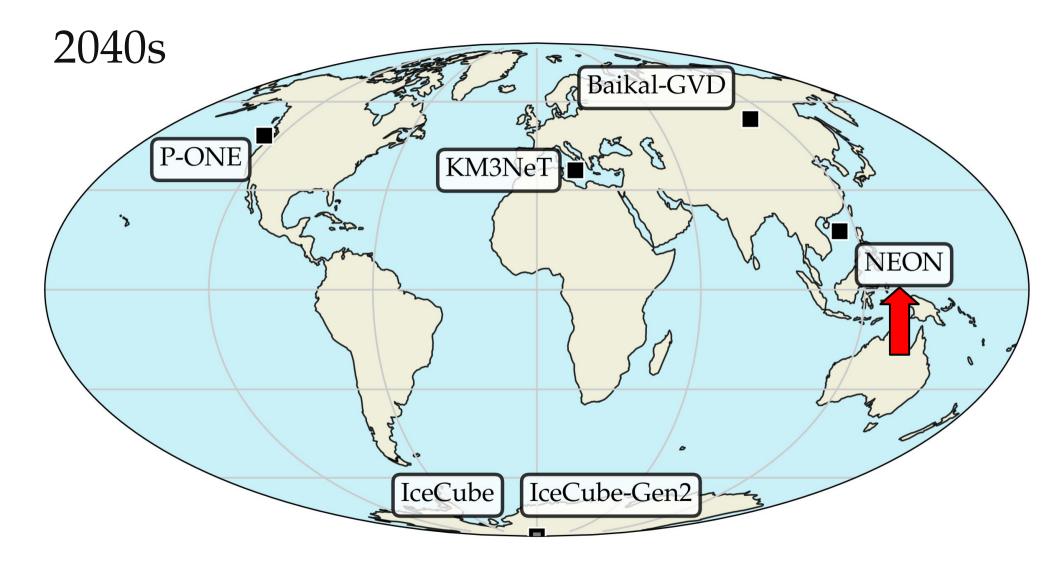


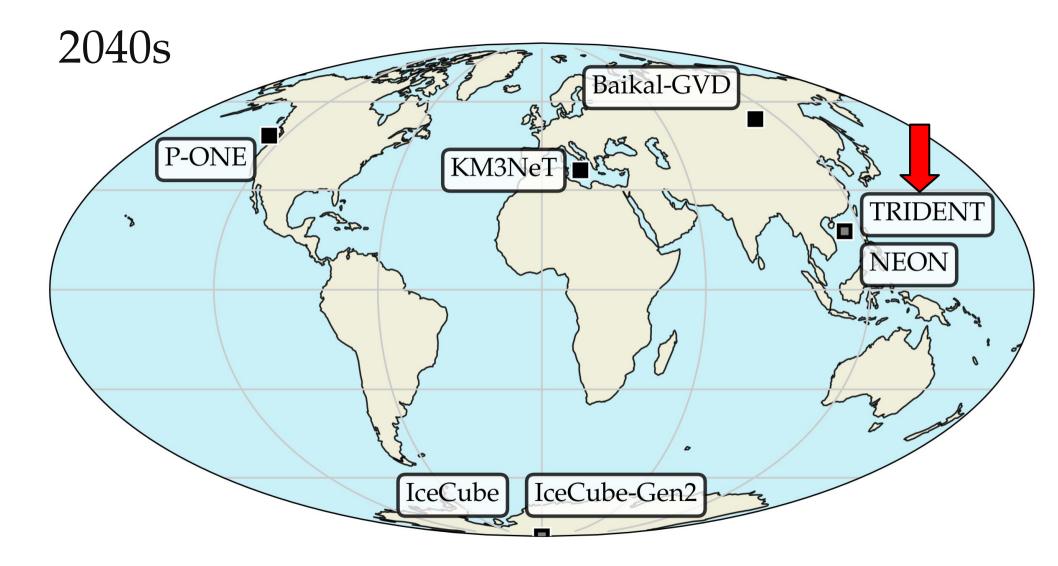
The future

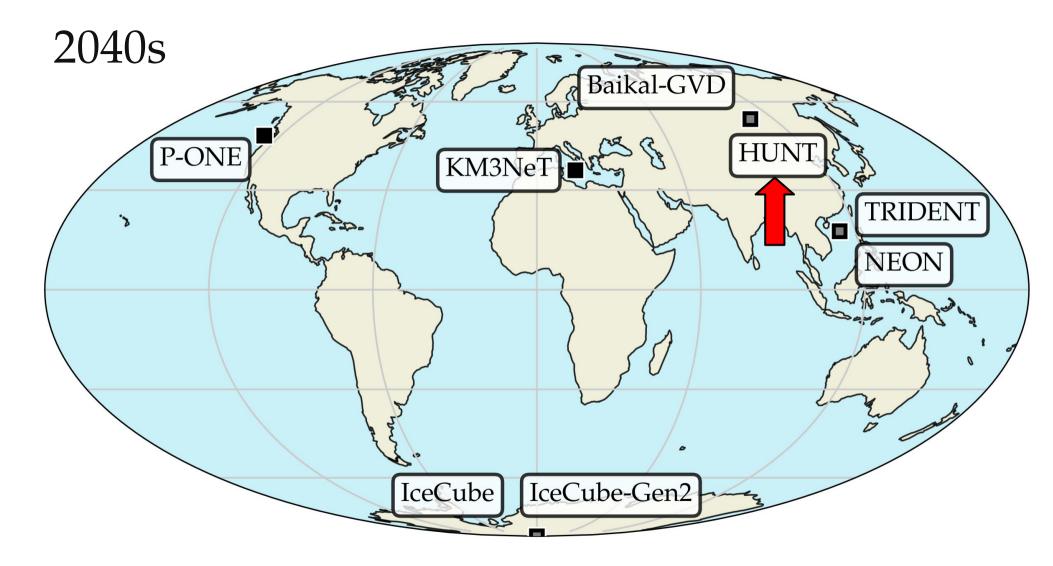


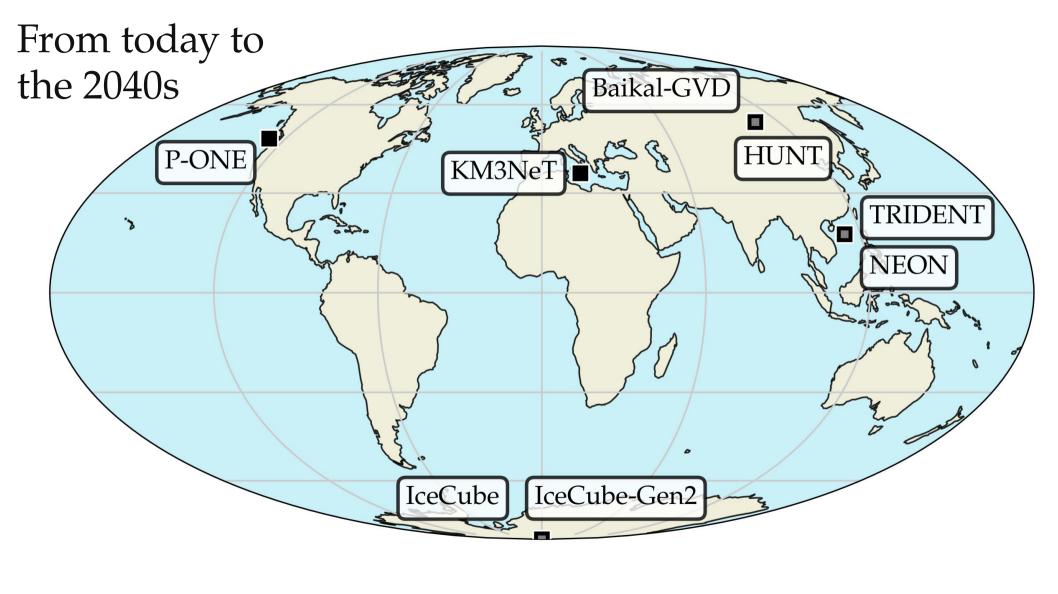


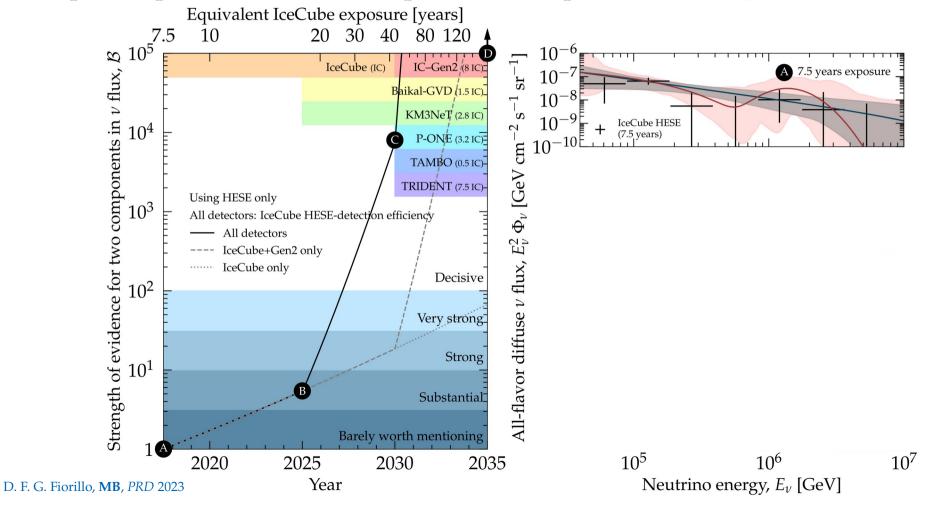


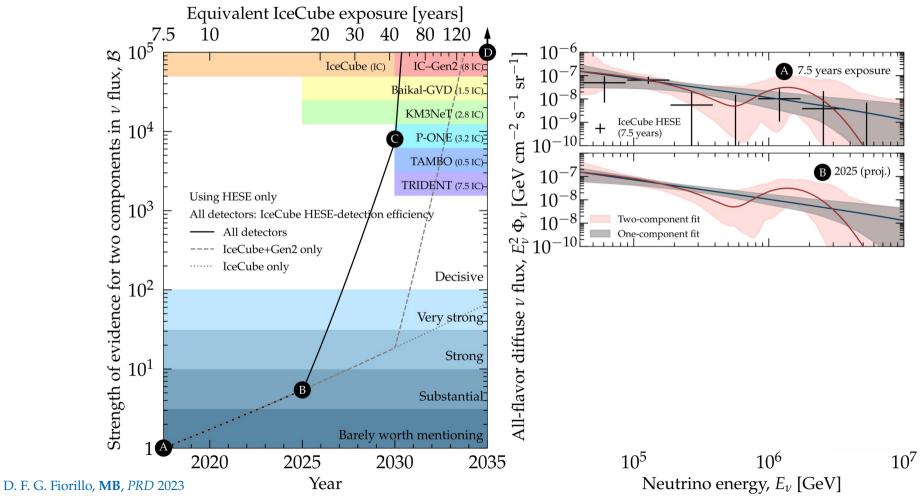


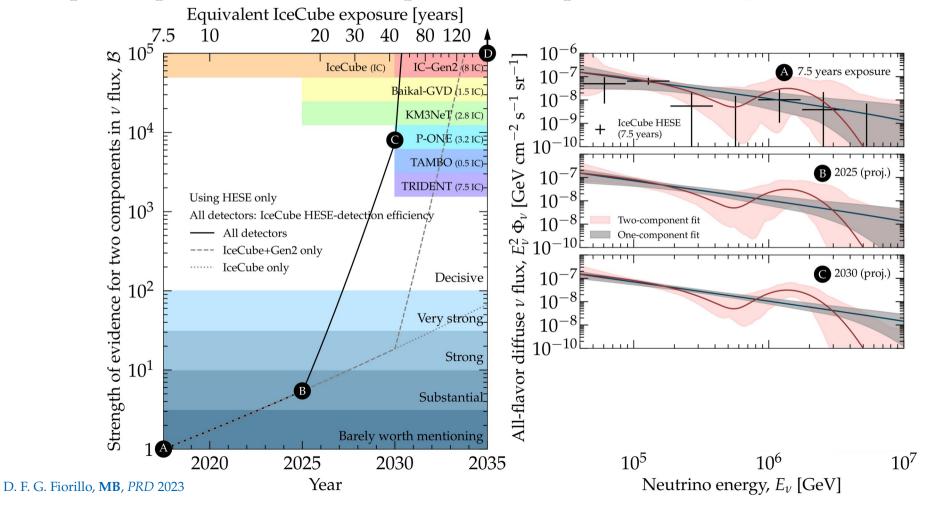


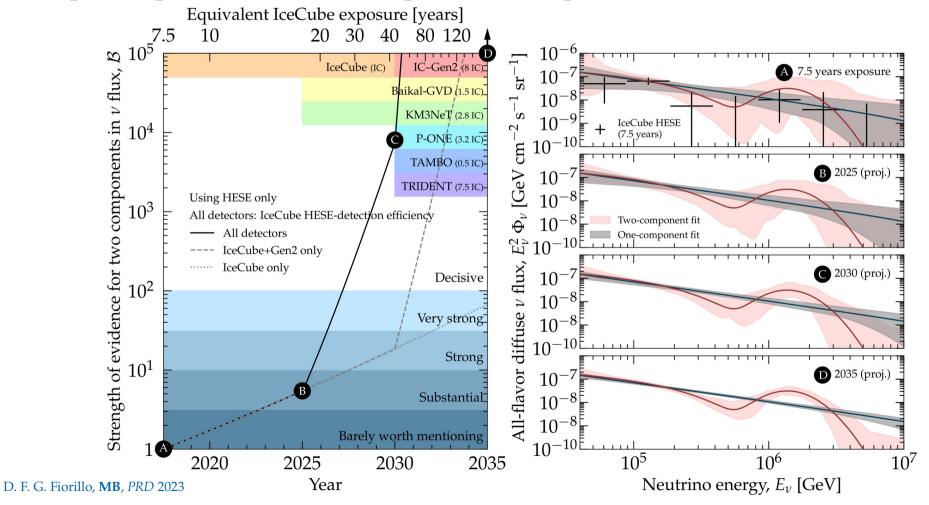


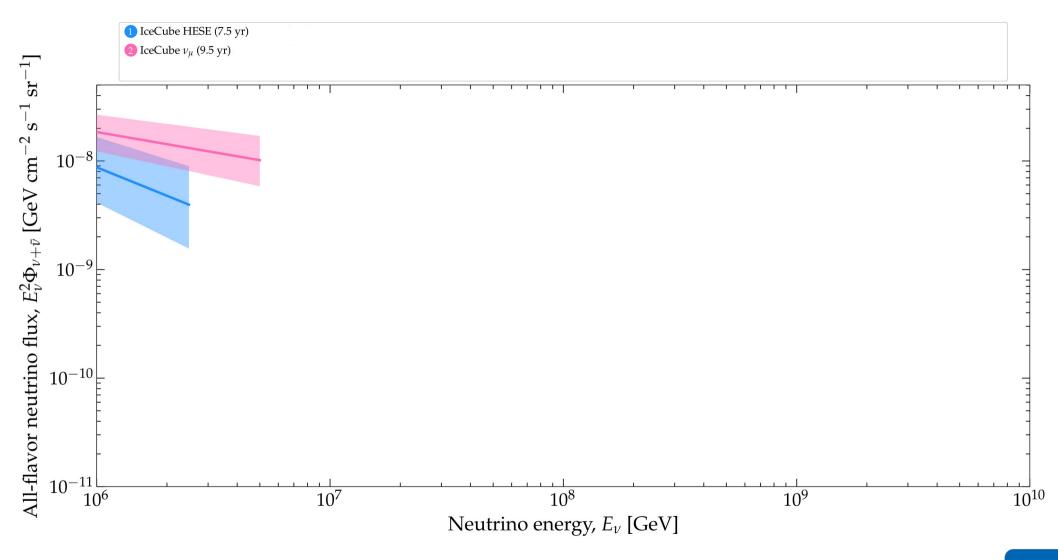


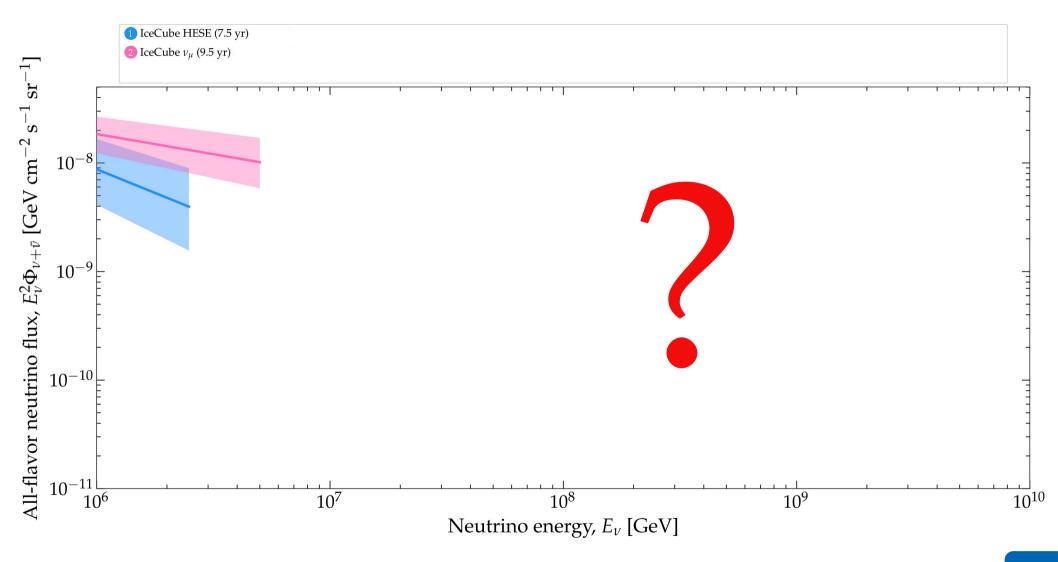


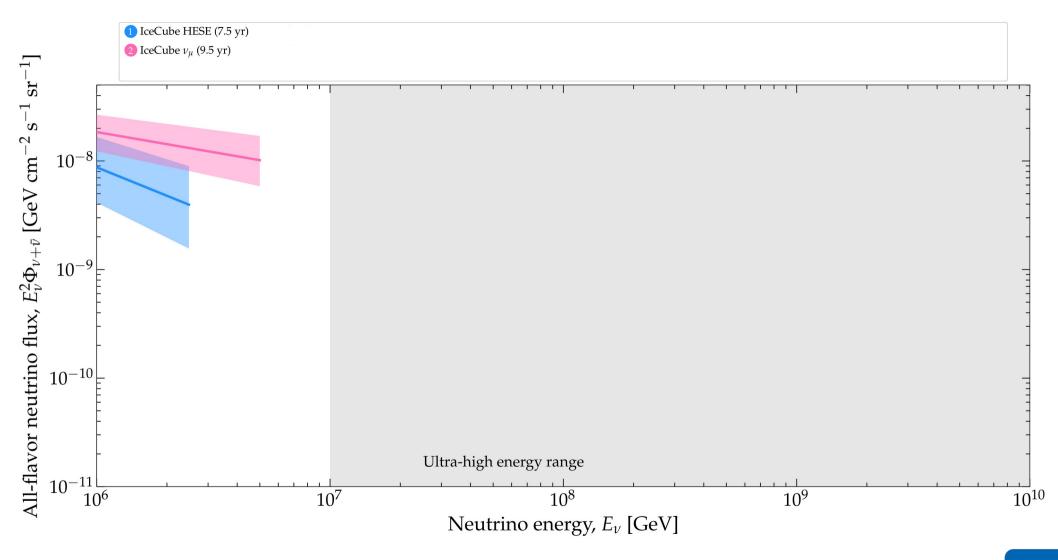


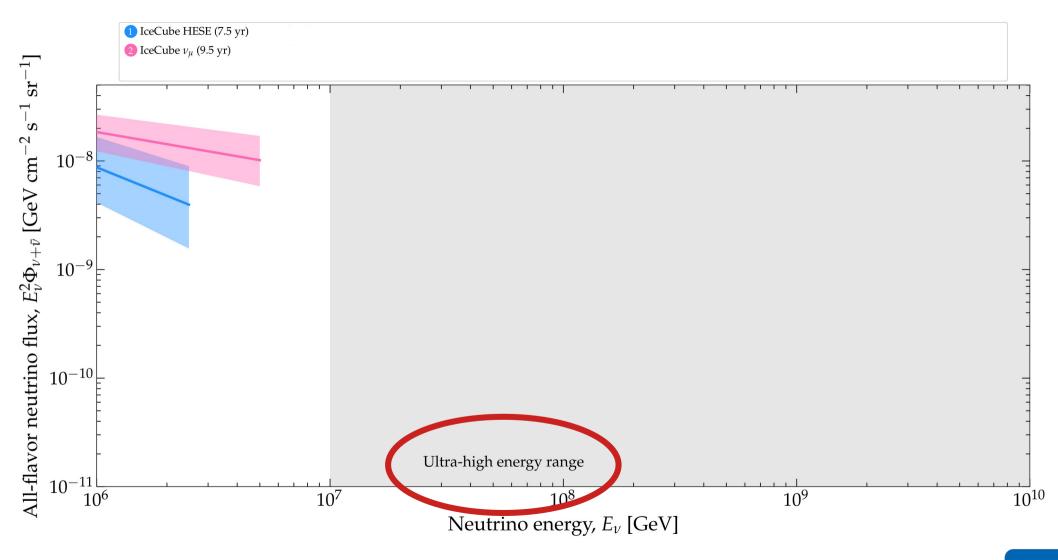


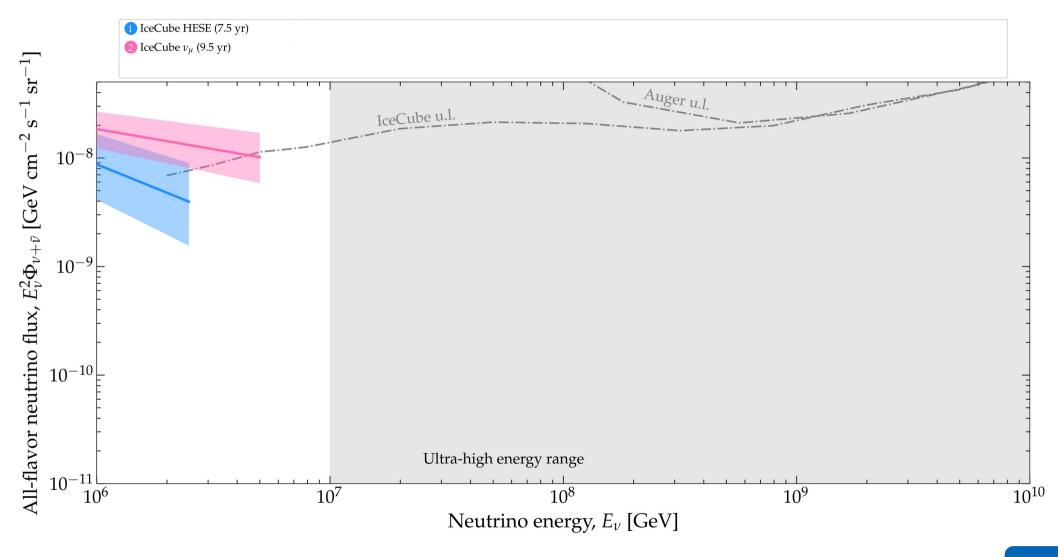


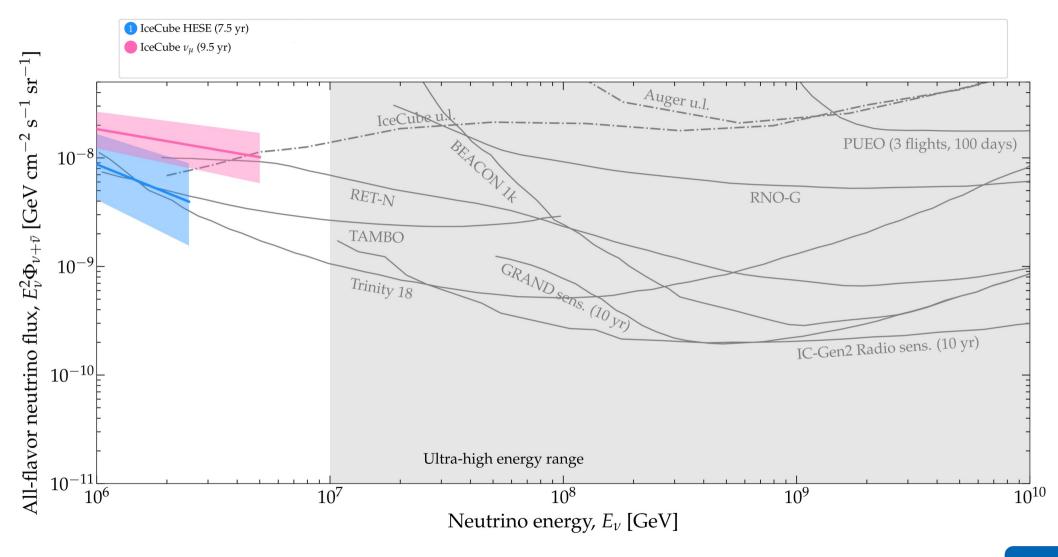


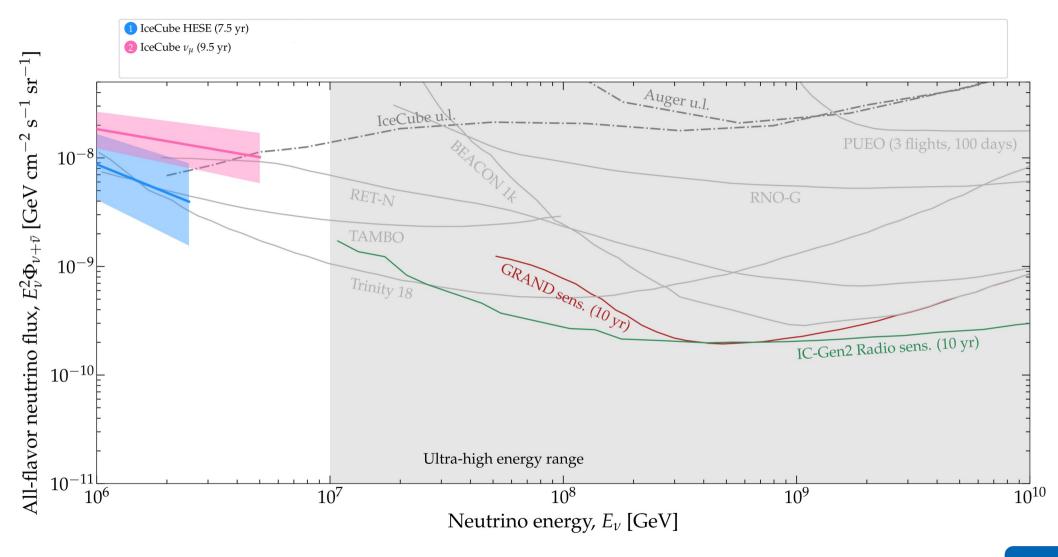


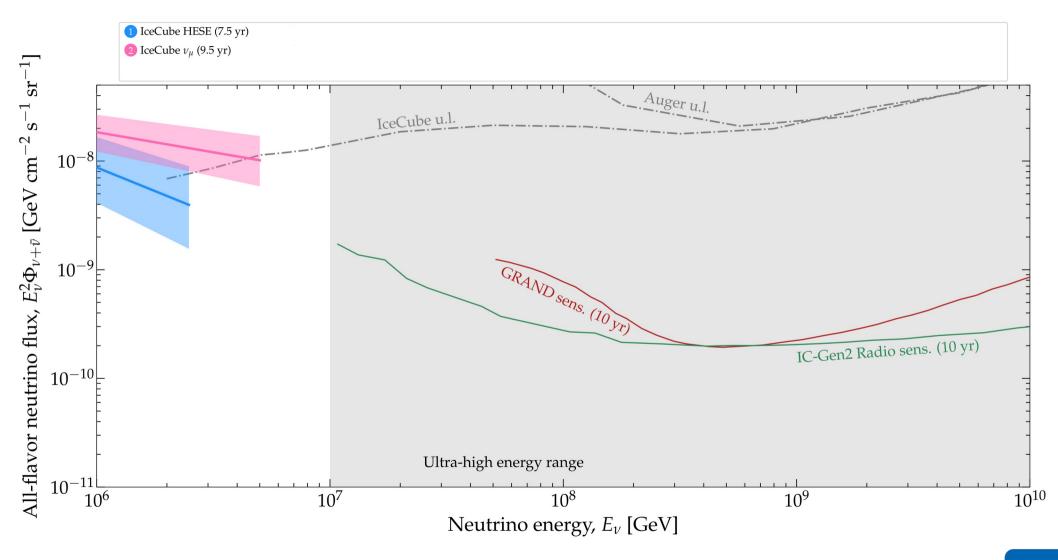




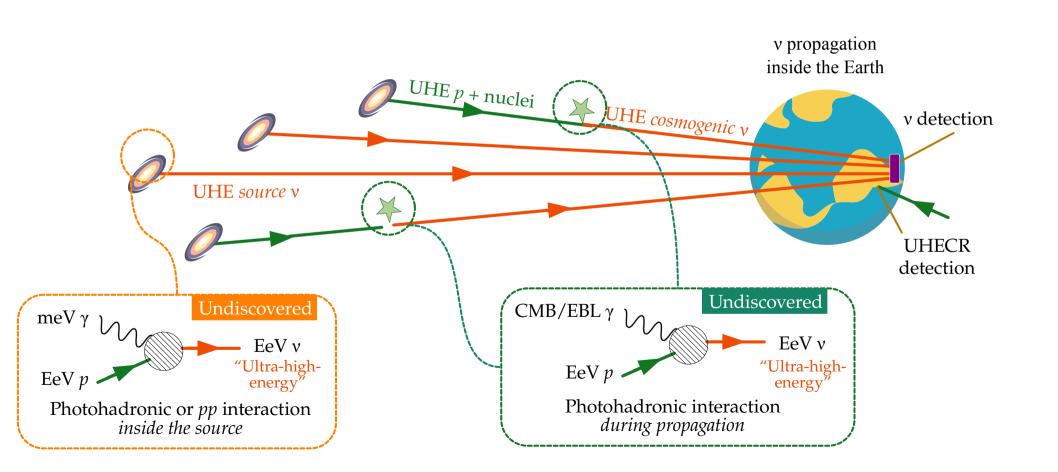


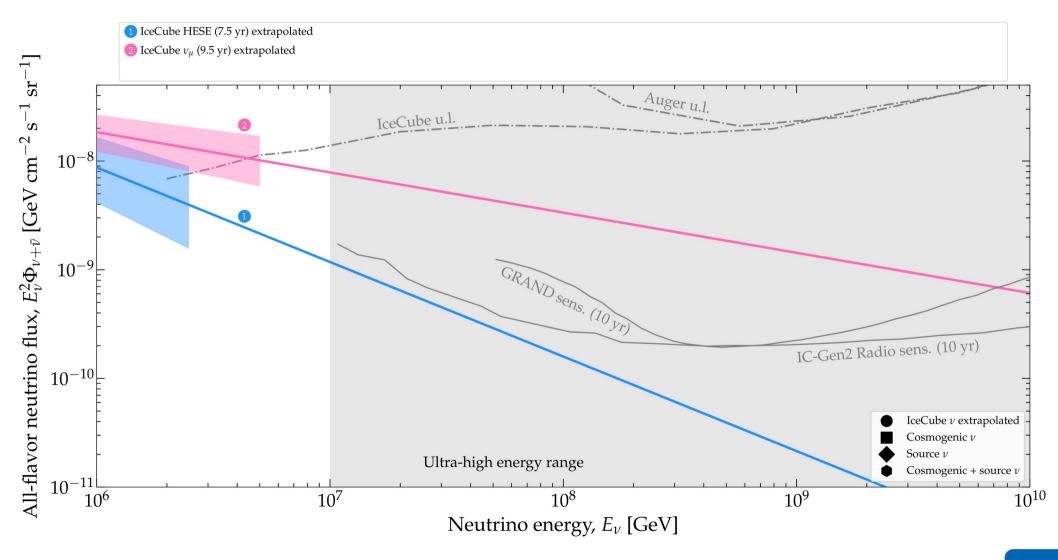


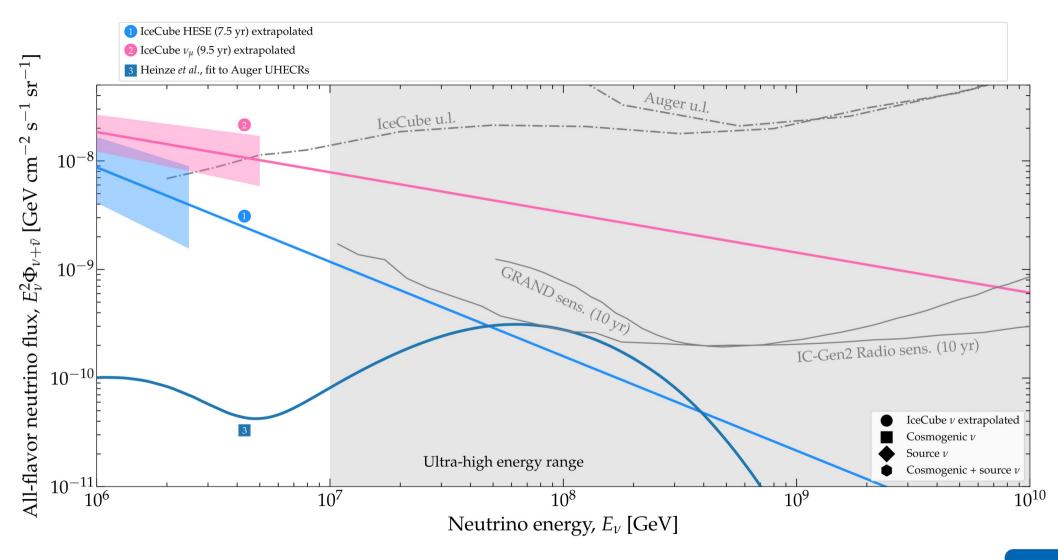


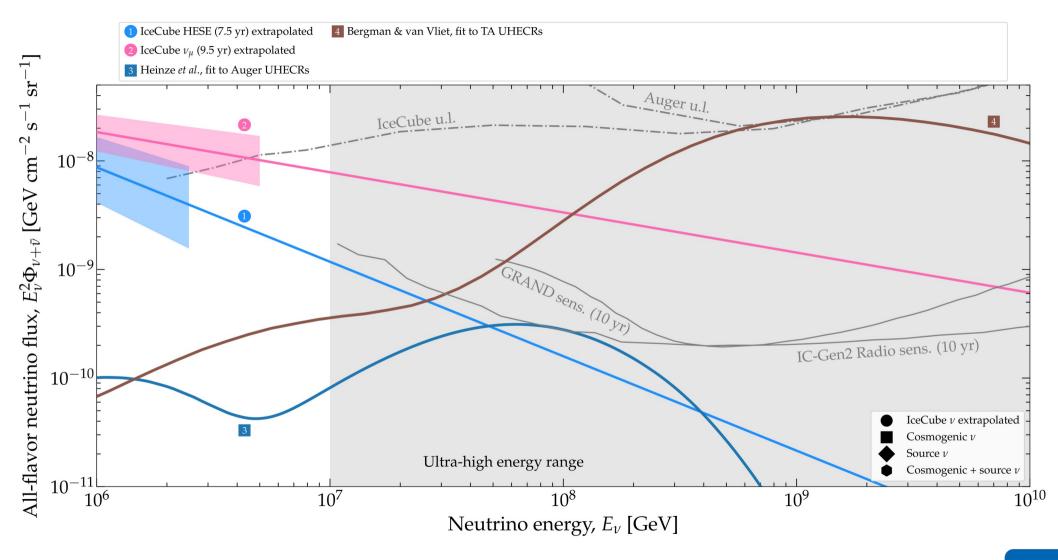


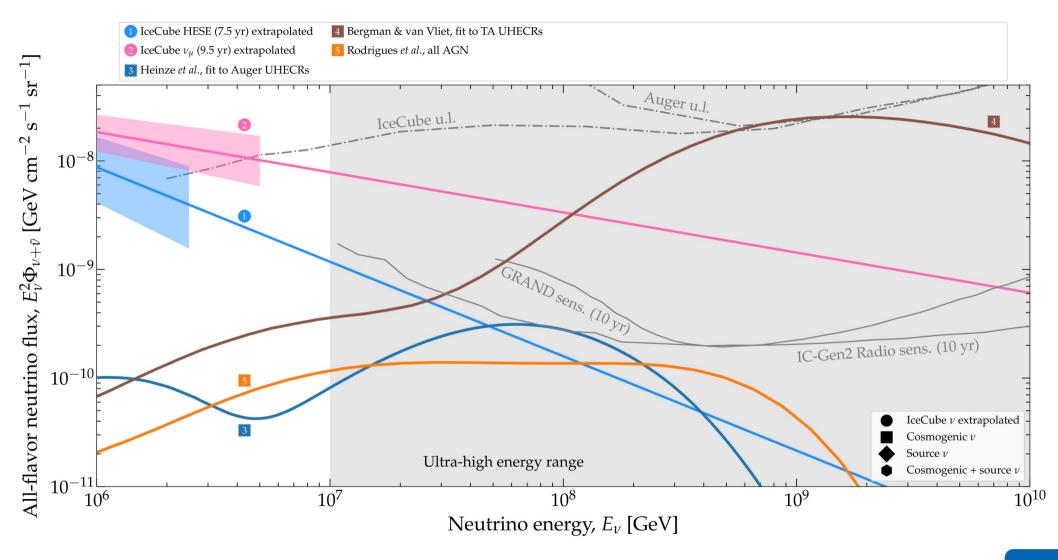
Note: v sources can be steady-state or transient

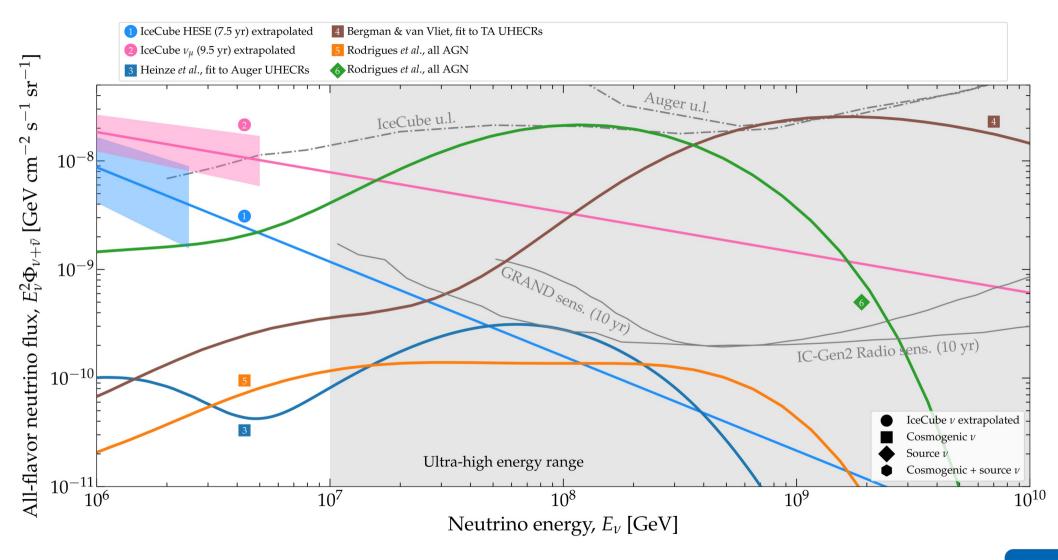


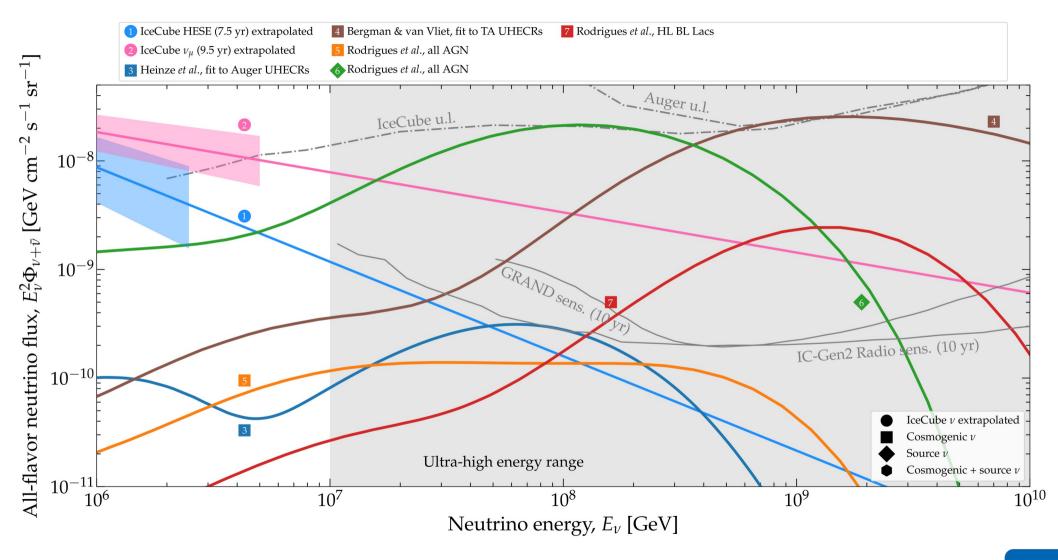


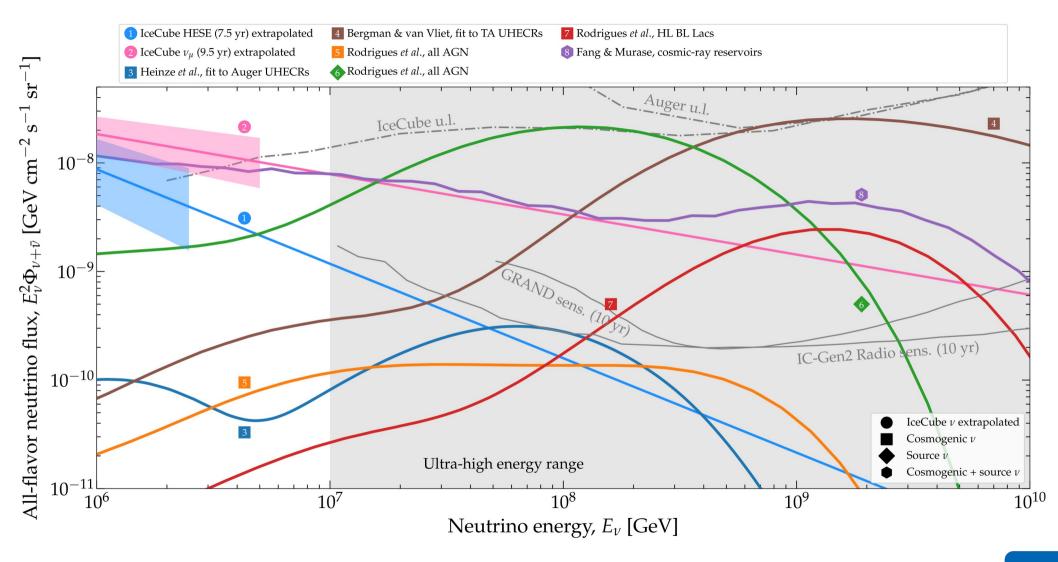


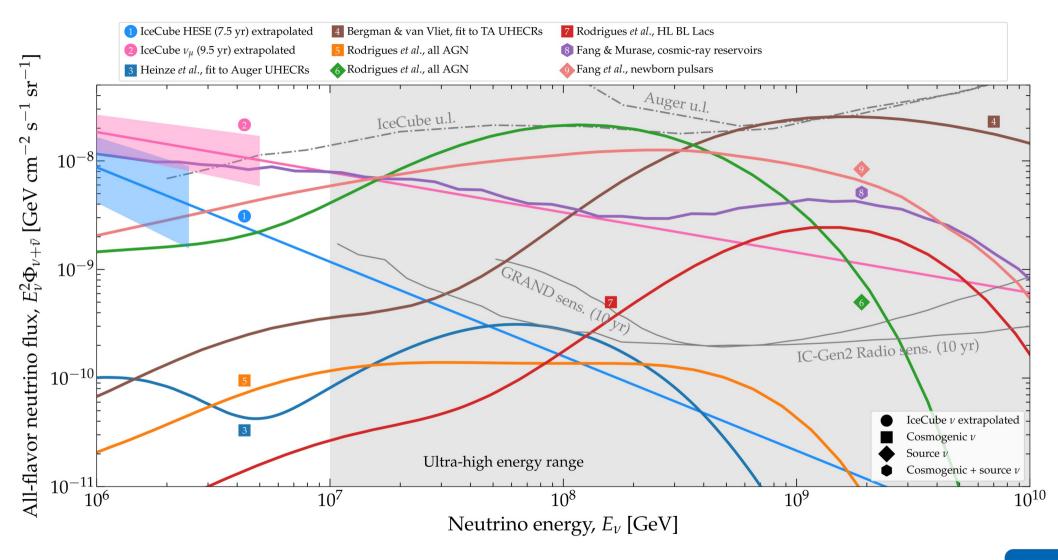


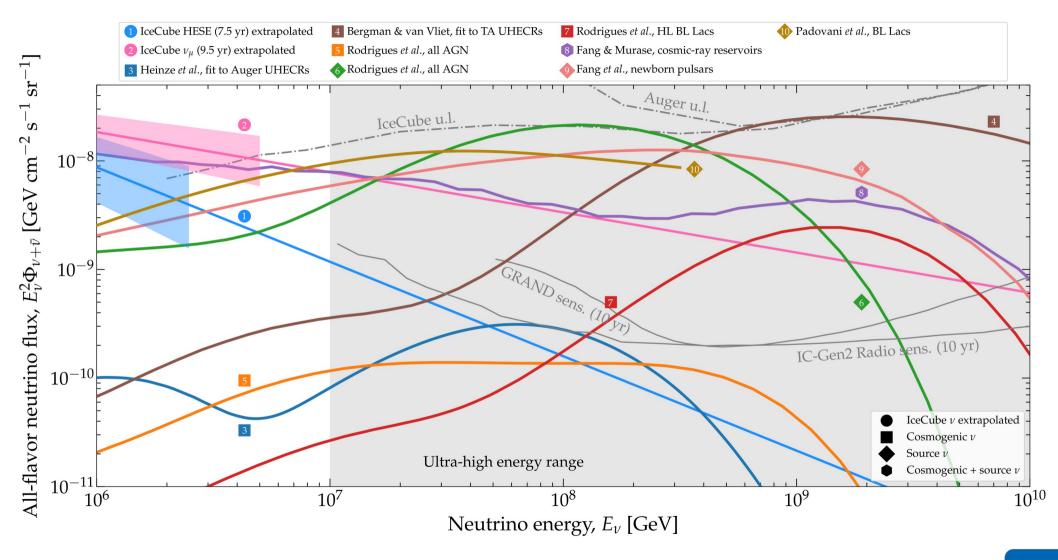


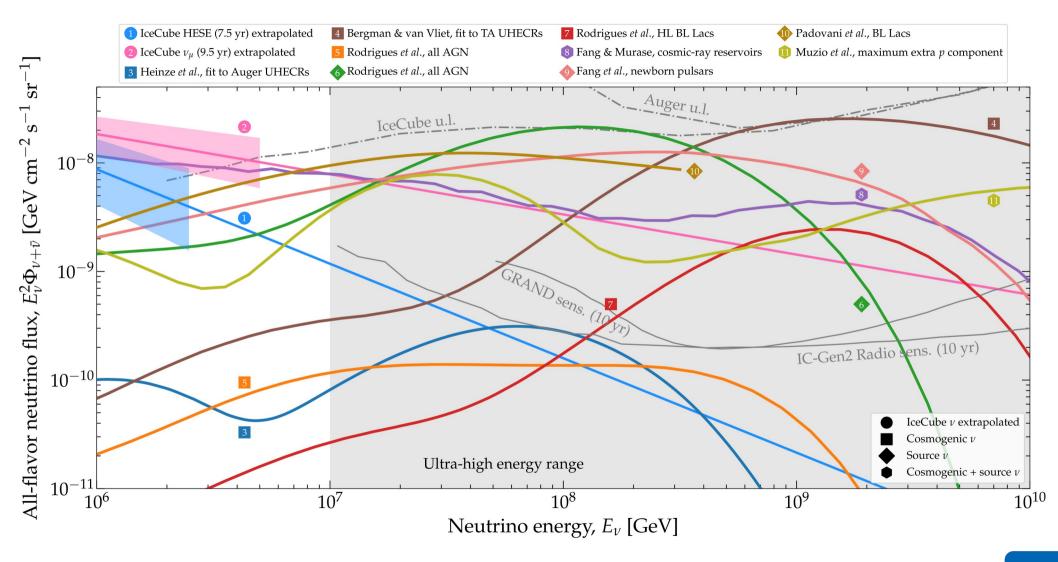


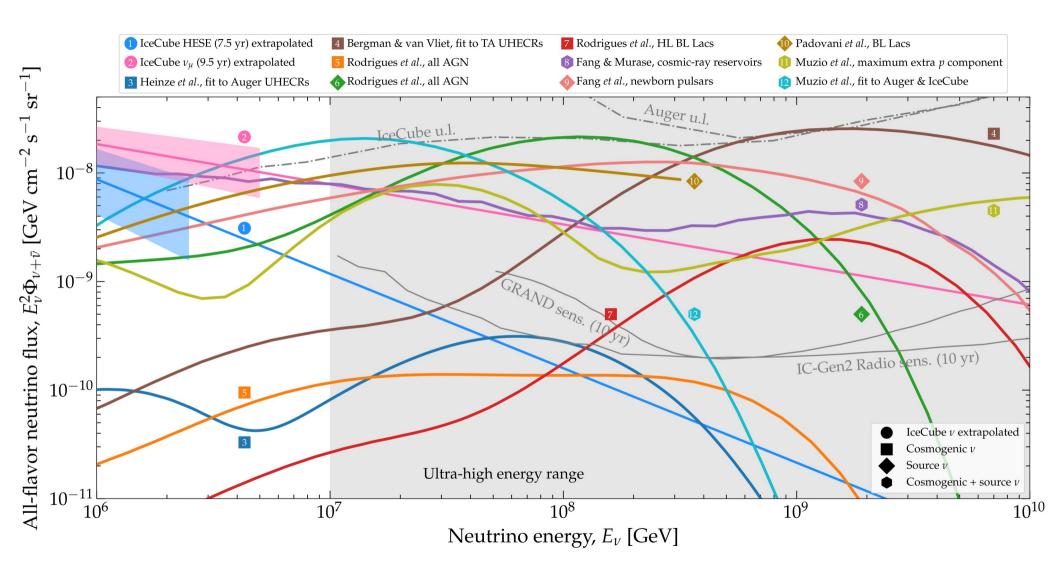


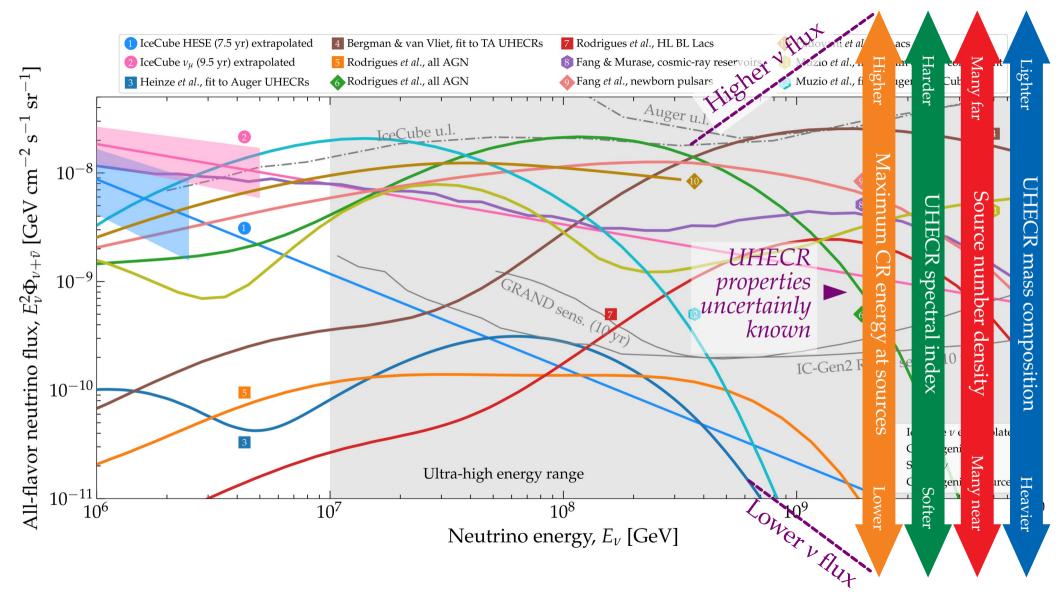


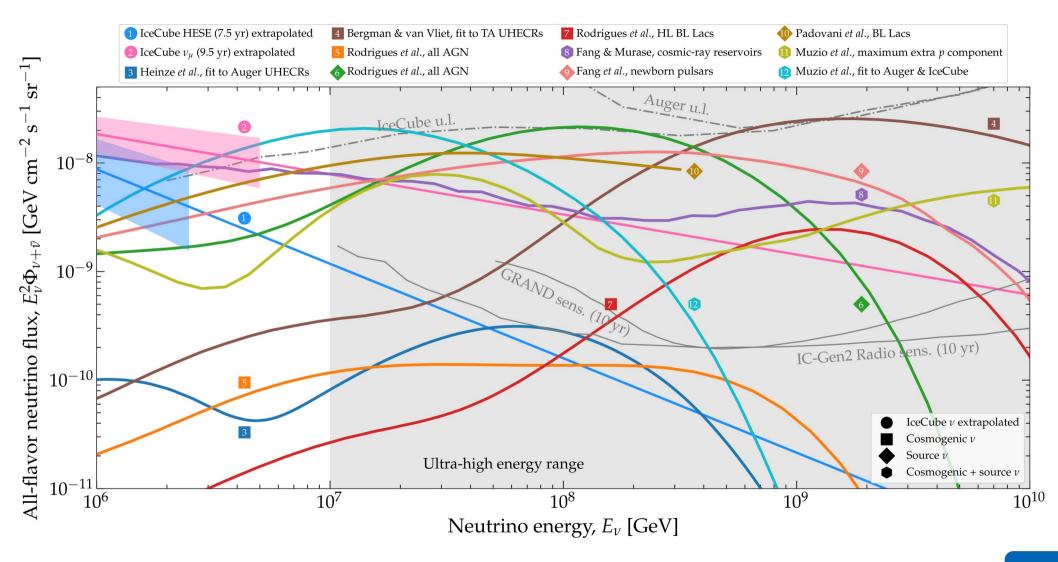


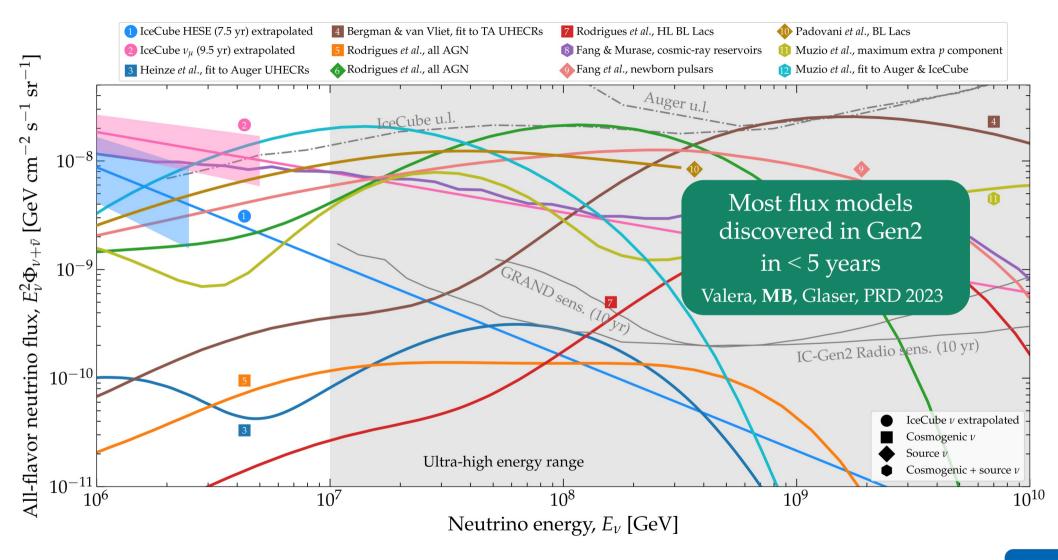


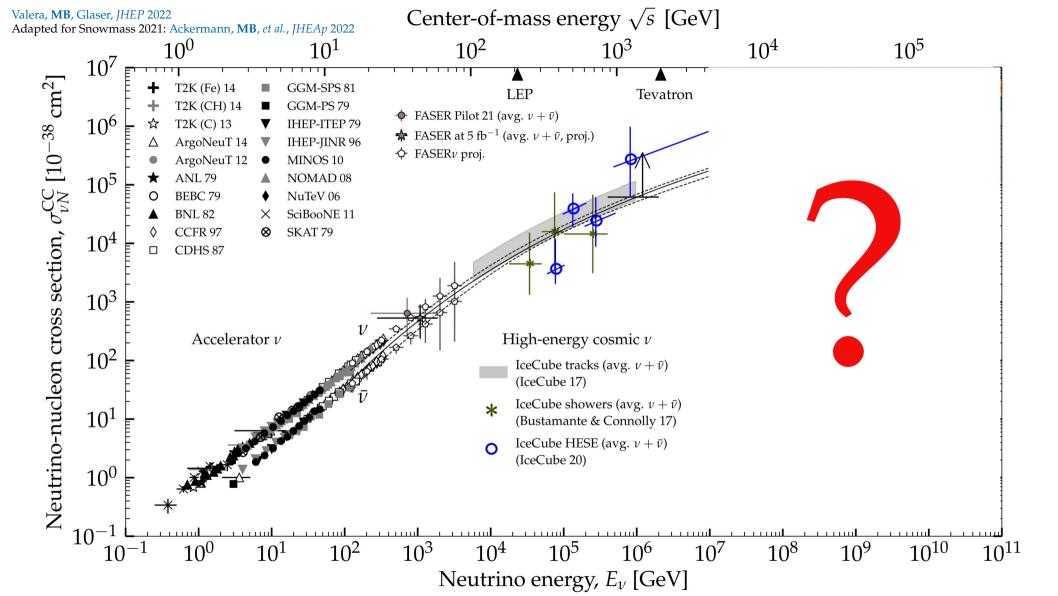


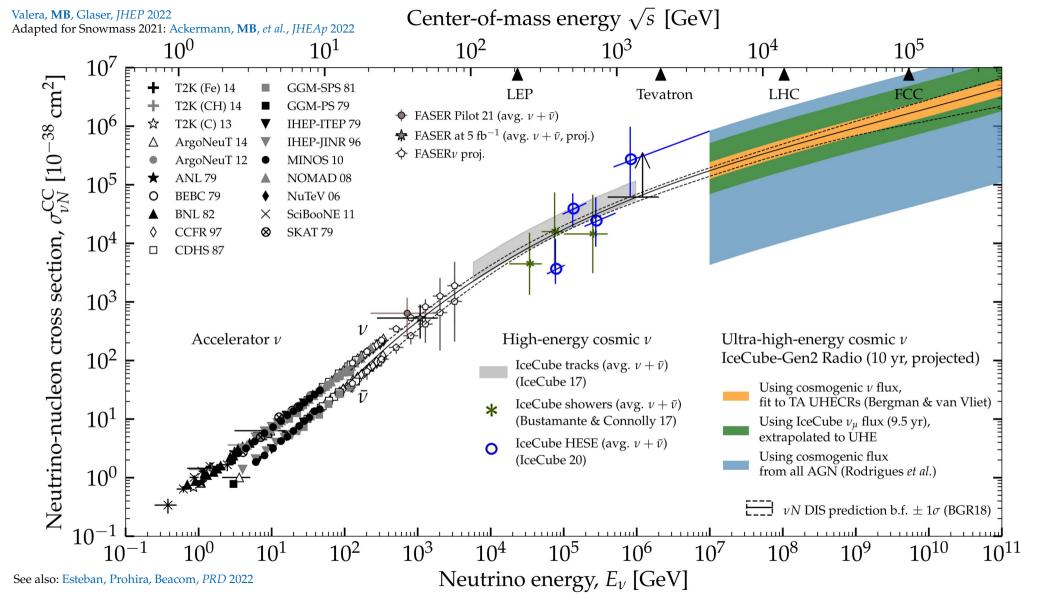


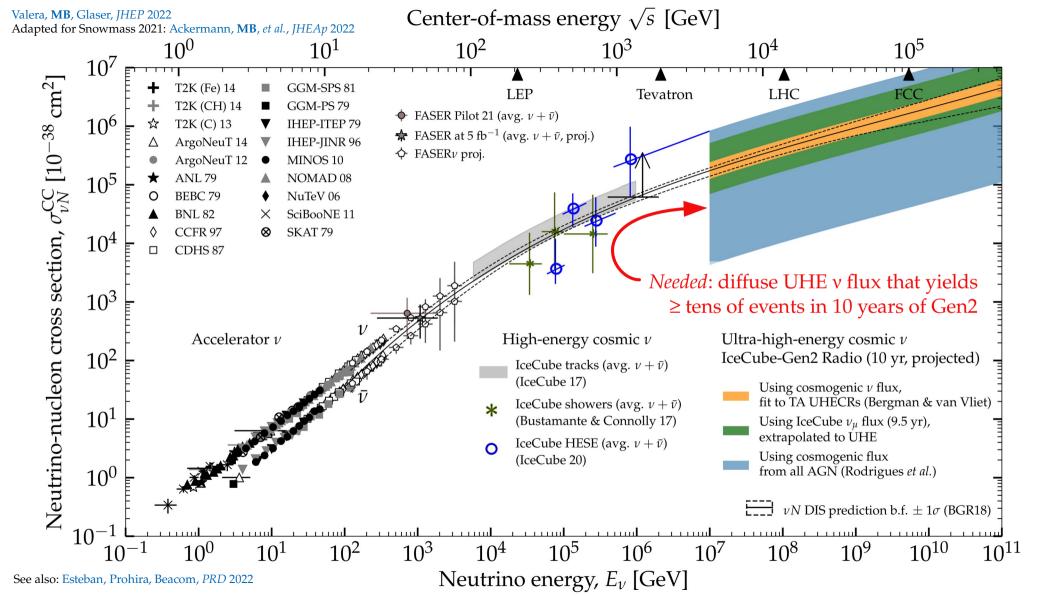












Turn predictions into data-driven tests

Key developments:

Bigger detectors → larger statistics

Better reconstruction

Smaller astrophysical uncertainties

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Smaller astrophysical uncertainties

Next decade > 100-PeV v

Turn predictions into data-driven tests

Key developments:

Bigger detectors → larger statistics

Better reconstruction

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Make predictions for a new energy regime

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Made robust and meaningful by accounting for all relevant particle and astrophysics uncertainties

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Key developments:

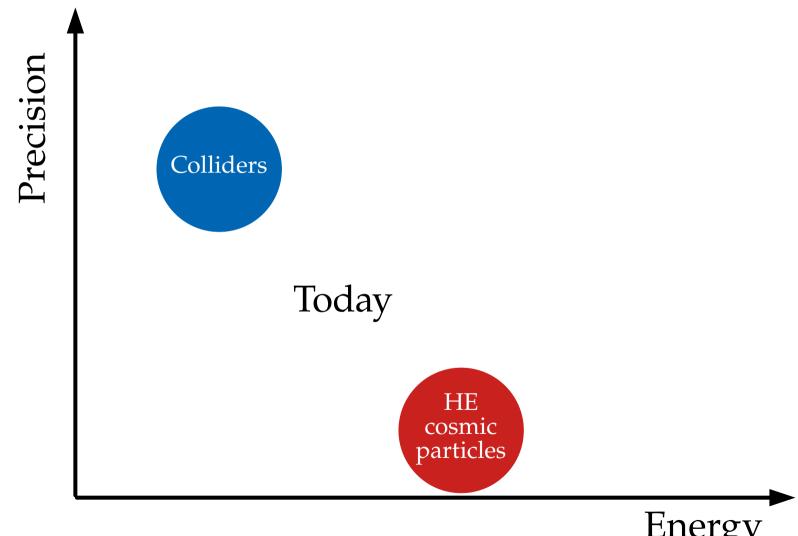
Discovery

New detection techniques

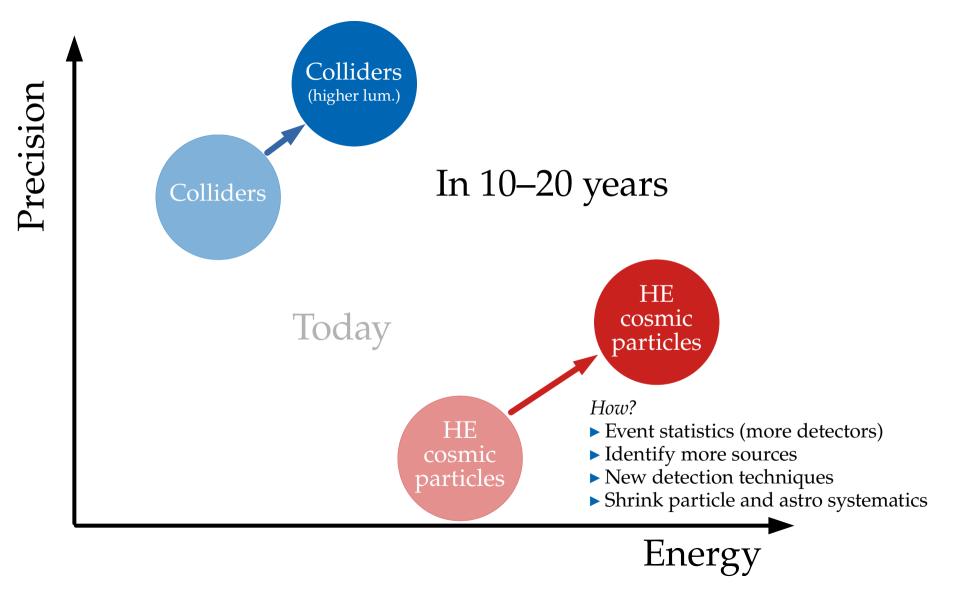
Better UHE v flux predictions

Similar to the evolution of cosmology to a high-precision field in the 1990s

Made robust and meaningful by accounting for all relevant particle and astrophysics uncertainties



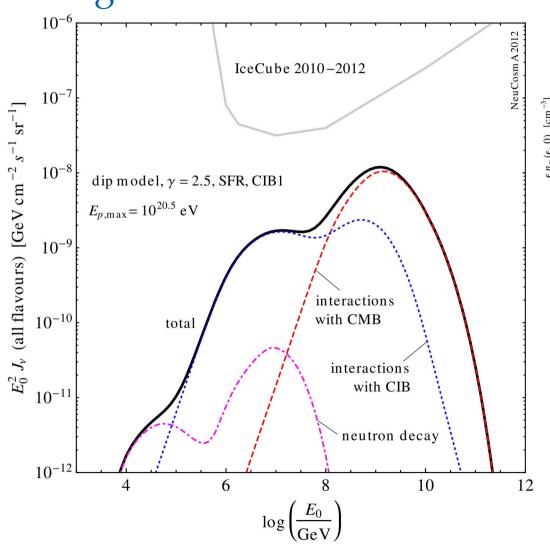
Energy

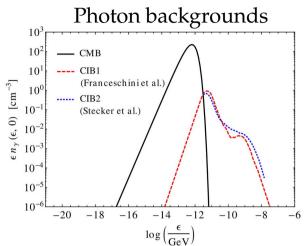


Thanks!

Backup slides

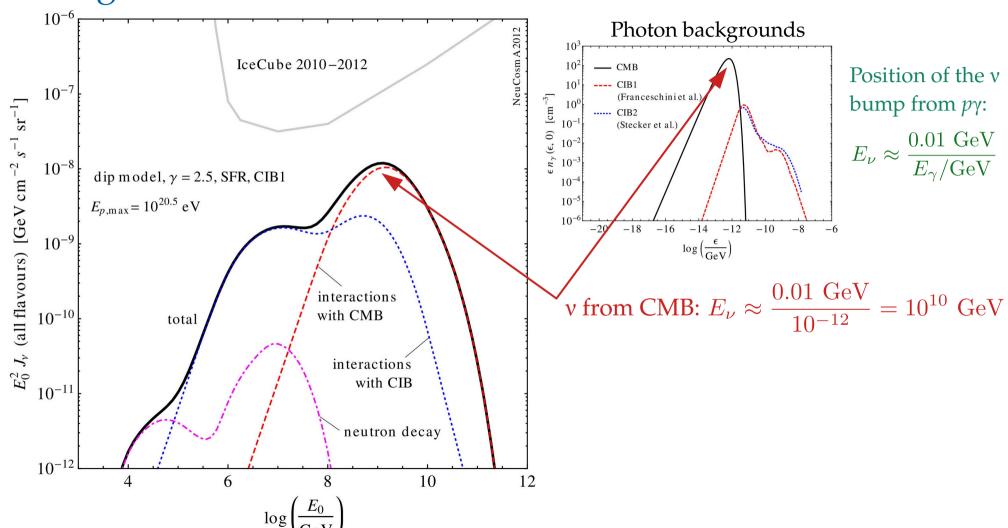
UHECRs

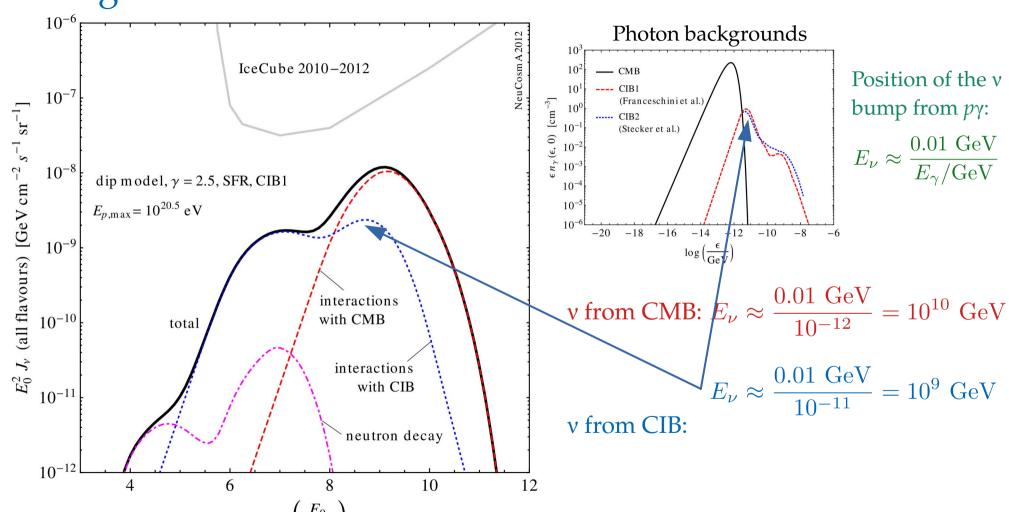


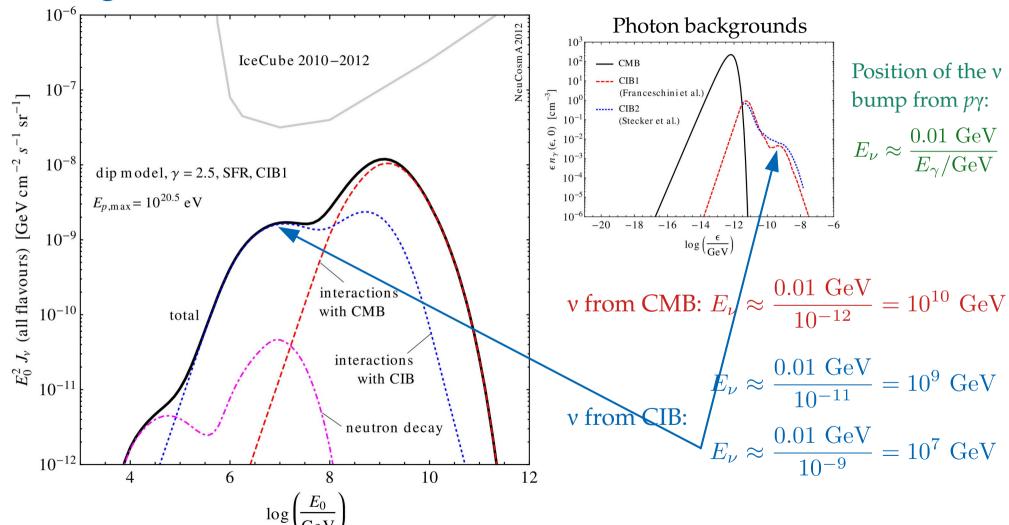


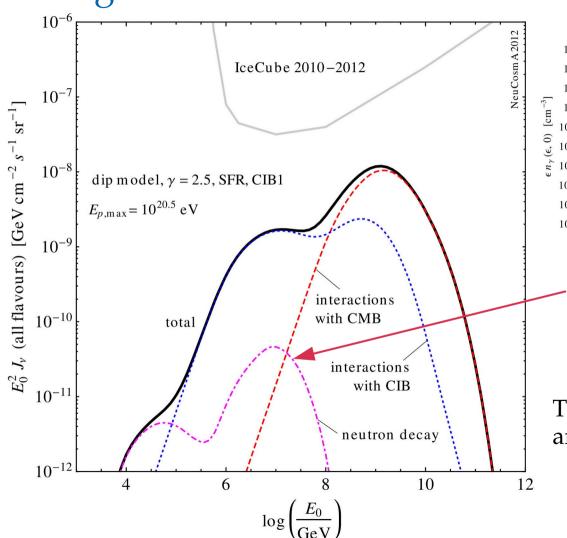
Position of the v bump from $p\gamma$:

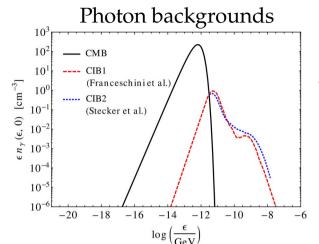
$$E_{\nu} \approx \frac{0.01 \text{ GeV}}{E_{\gamma}/\text{GeV}}$$







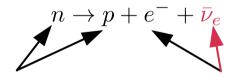




Position of the v bump from $p\gamma$:

$$E_{\nu} pprox rac{0.01 \text{ GeV}}{E_{\gamma}/\text{GeV}}$$

Why are v from n decay lower-energy?



The n and p mass are very similar ...

... so there is little energy left for *e*, **v**

UHECRs: more sophisticated models

Use more data:

Spectrum + mass composition (X_{max})

Five mass groups:

H, He, N, Si, Fe

Common maximum rigidity:

Max. rigidity is $R_{\text{max}} = E_{\text{max}}/Z$

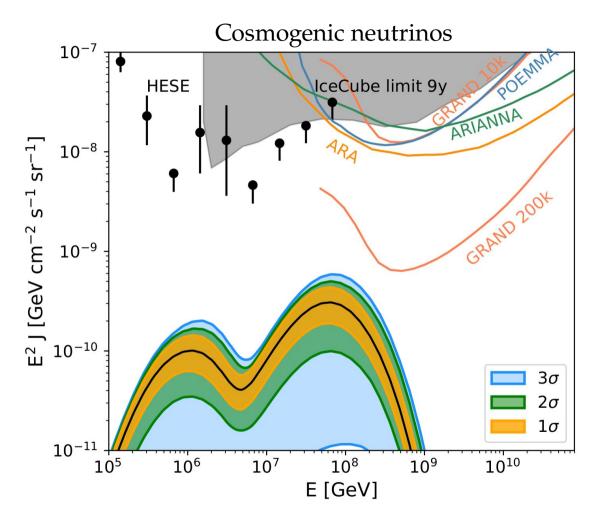
$$Q_Z(E) \propto E^{-\gamma} e^{-E/(ZR_{\text{max}})}$$



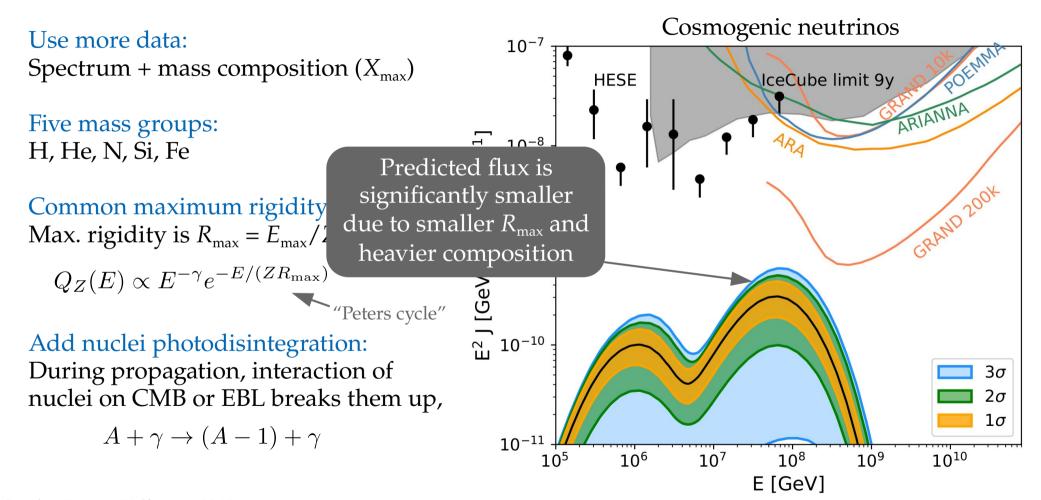
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During propagation, interaction of nuclei on CMB or EBL breaks them up,

$$A + \gamma \rightarrow (A - 1) + \gamma$$



UHECRs: more sophisticated models



See also: Romero-Wolf & Ave, *JCAP* 2018 Alves Batista, Almeida, Lago, Kotera, *JCAP* 2019

The UHECR all-particle spectrum – more features!

 $\ln(10)\frac{4\pi}{c}E^2J(E)$

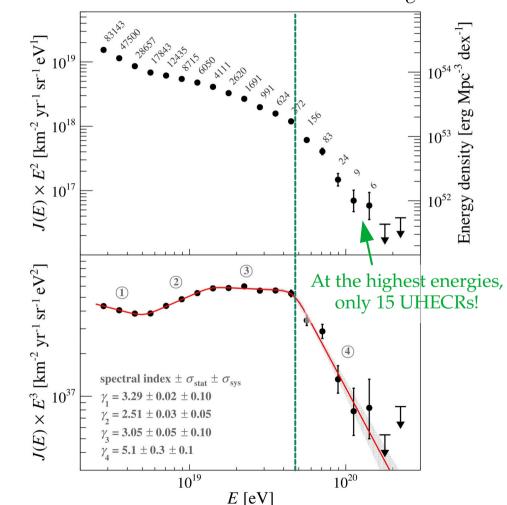
15 years of Auger data (2004–2019)!

~215k events above $2.5 \times 10^{18} \text{ eV}$

Use *hybrid* events detected by surface

- + fluorescence detectors to calibrate
- Allows us to measure energies of other events robustly

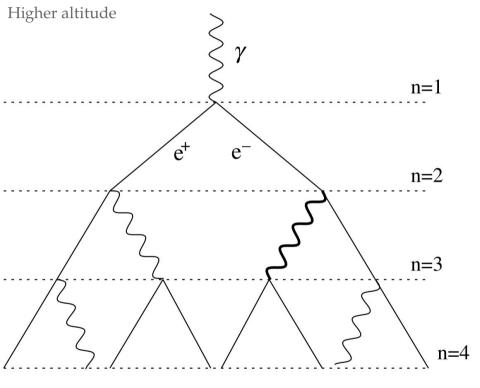
CR luminosity density above 5×10^{18} eV: 6×10^{44} erg Mpc⁻³ yr⁻¹ (could be AGN or starburst galaxies)



Auger Collab., PRL 2020 See also: Auger Collab., PRD 2020

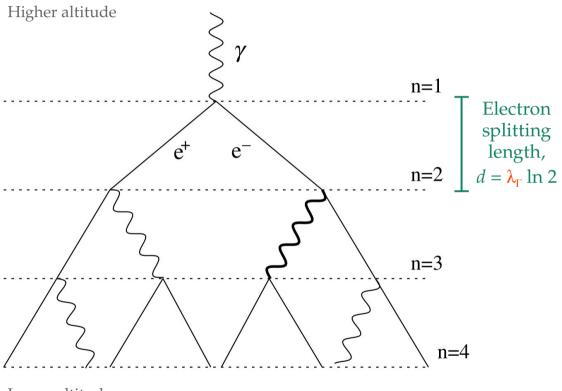
UHECR shower development

Heitler model—simple, but illustrative:



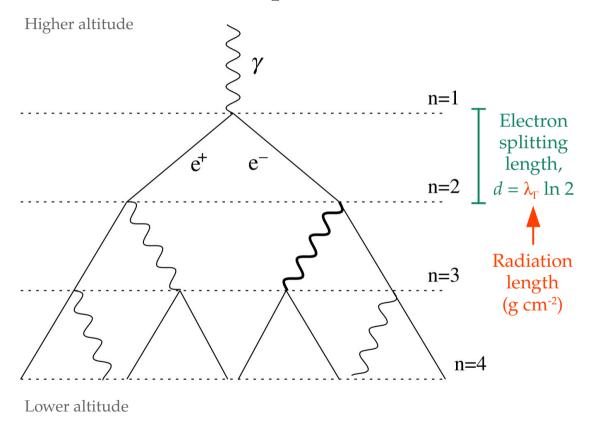
Lower altitude

Heitler model—simple, but illustrative:

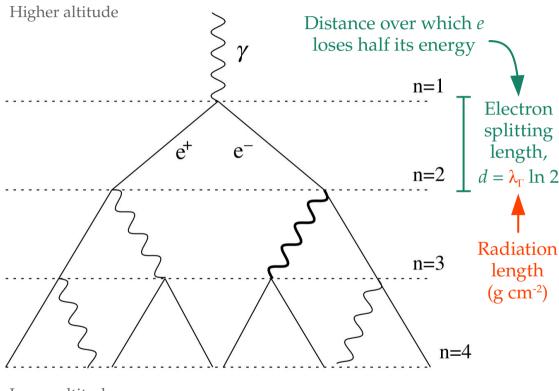


Lower altitude

Heitler model—simple, but illustrative:

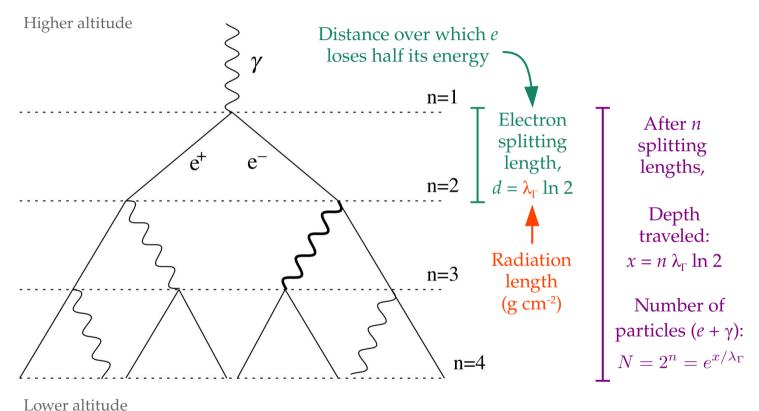


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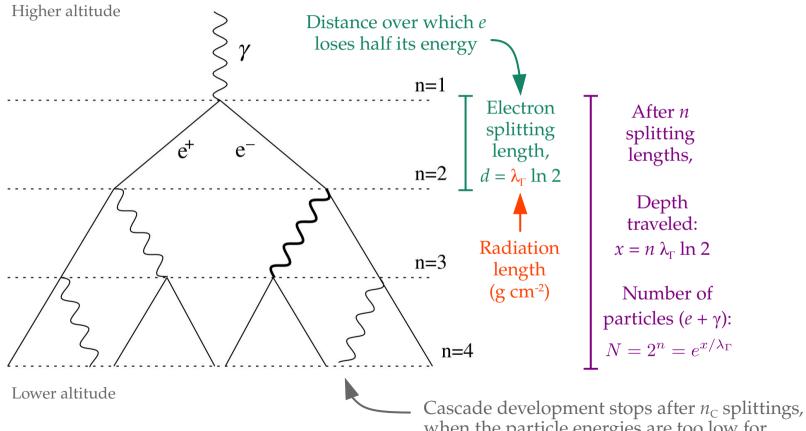


Lower altitude

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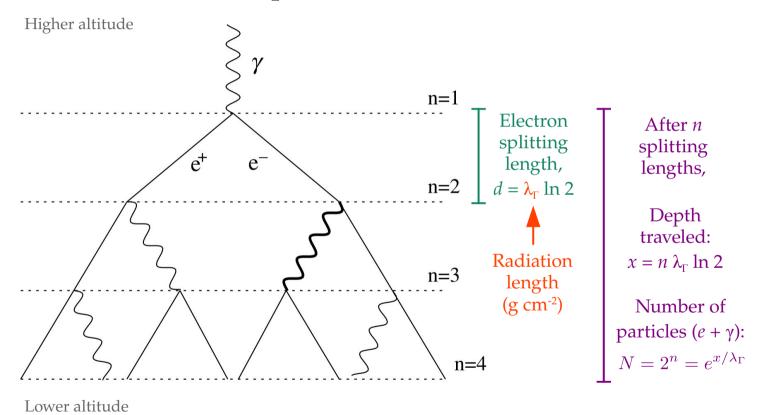
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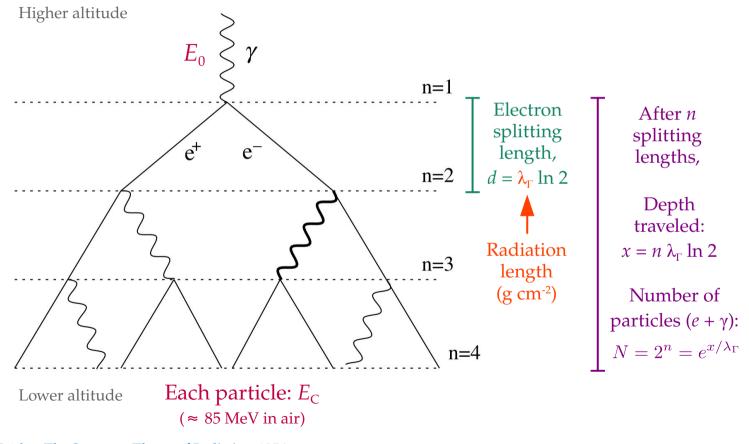
Heitler, The Quantum Theory of Radiation, 1954 Matthews, Astropart. Phys. 2005

when the particle energies are too low for pair production or bremsstrahlung

Heitler model—simple, but illustrative:

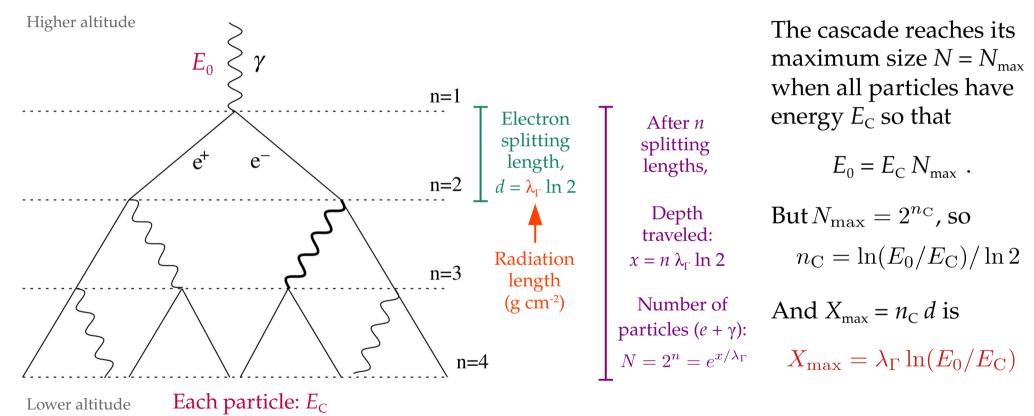


Heitler model—simple, but illustrative:

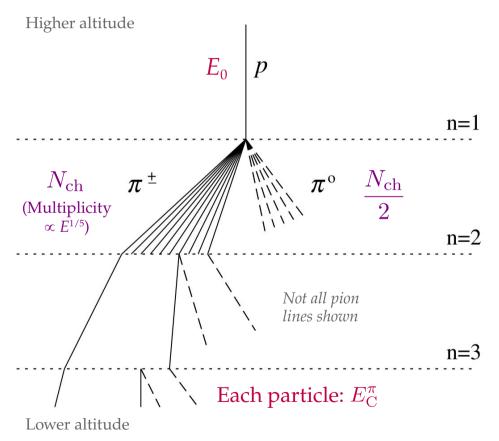


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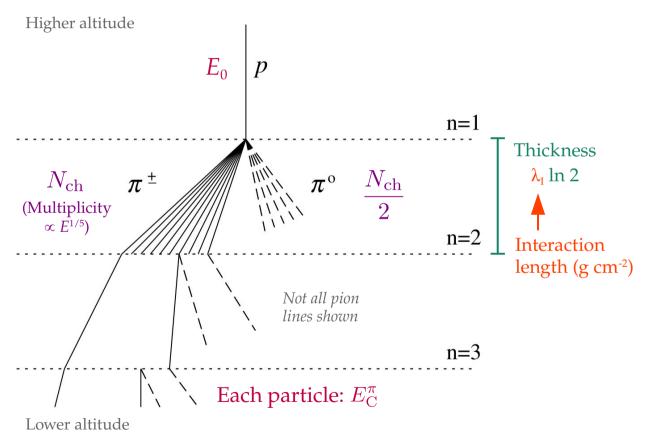
 $(\approx 85 \text{ MeV in air})$



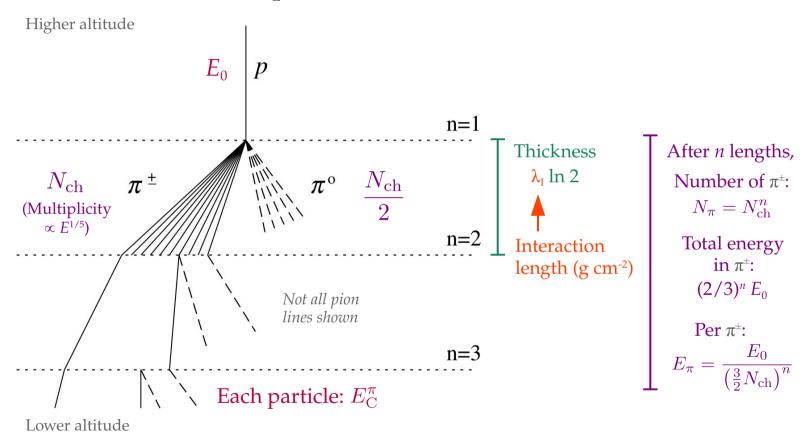
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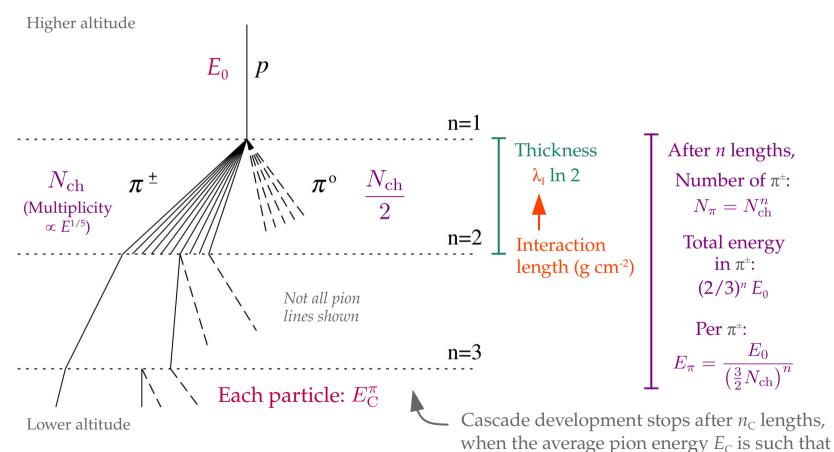
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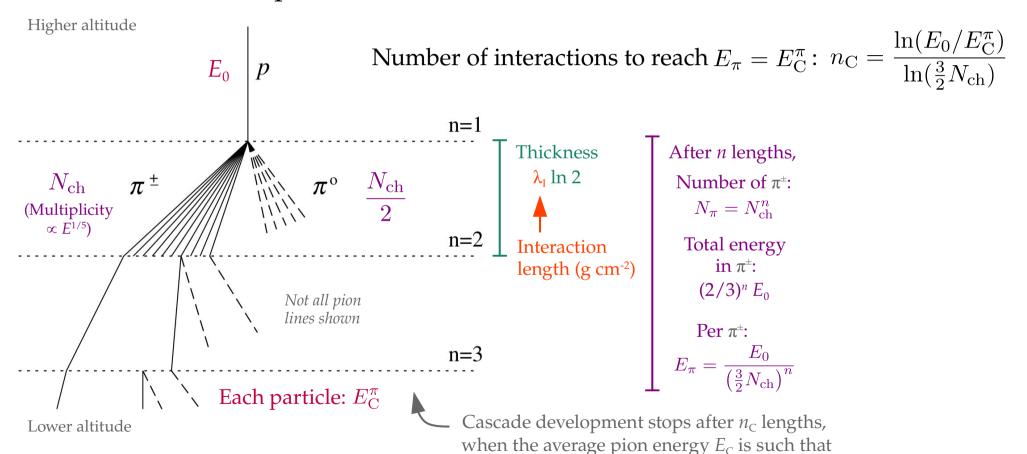


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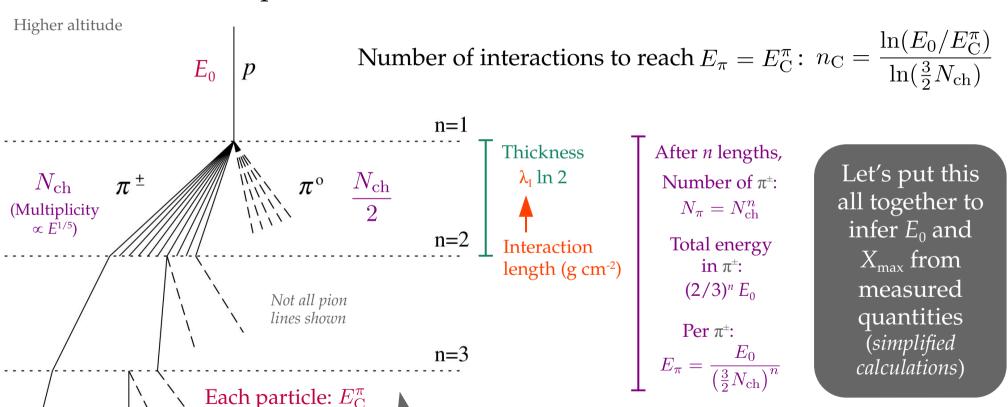
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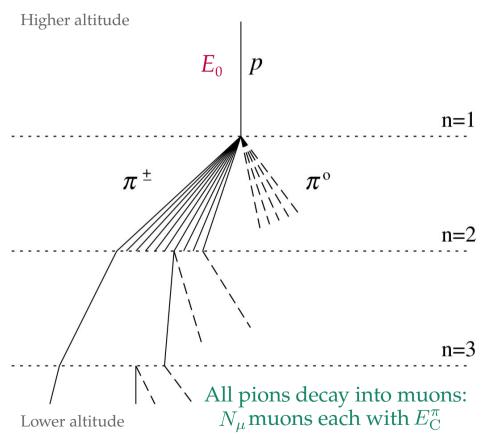


Heitler, *The Quantum Theory of Radiation*, 1954 Matthews, *Astropart. Phys.* 2005

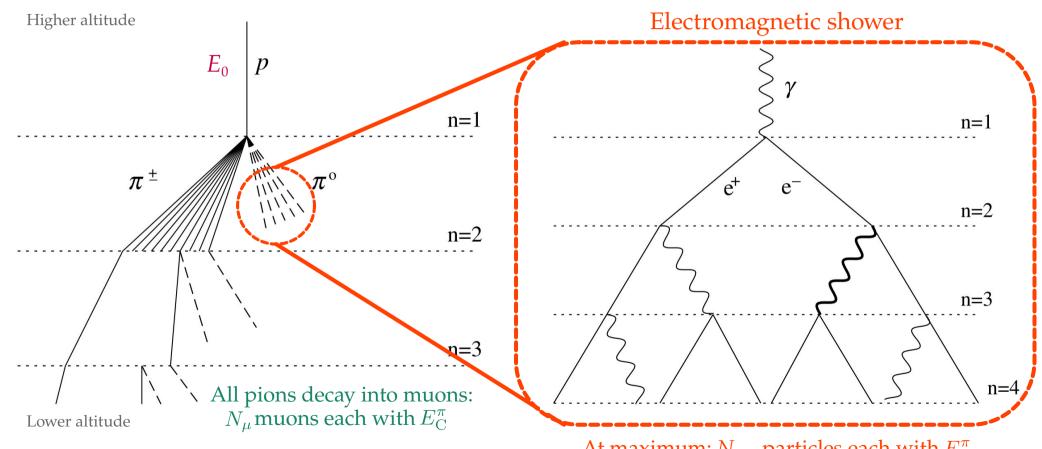
Lower altitude

Cascade development stops after $n_{\rm C}$ lengths, when the average pion energy $E_{\rm C}$ is such that the decay length of π^{\pm} is $< \lambda_{\rm I}$

Inferring the primary UHECR energy:



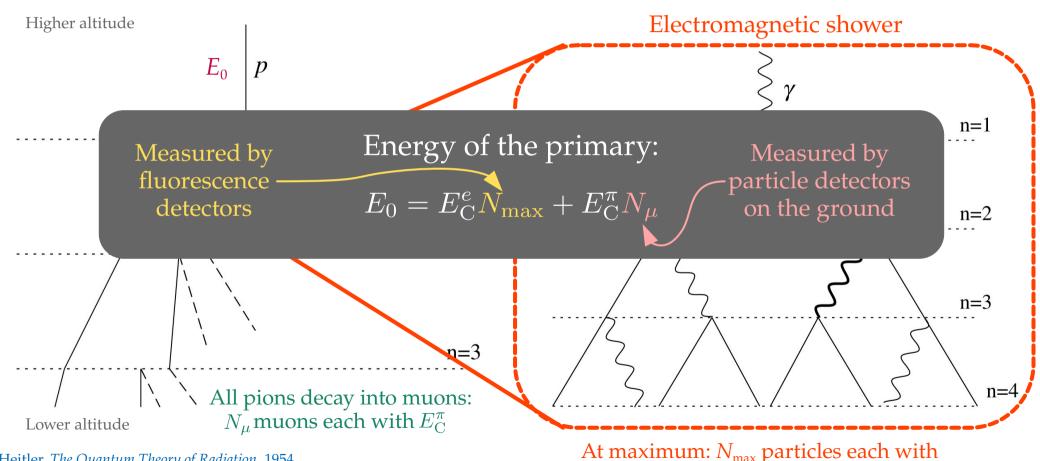
Inferring the primary UHECR energy:



Heitler, The Quantum Theory of Radiation, 1954 Matthews, Astropart. Phys. 2005

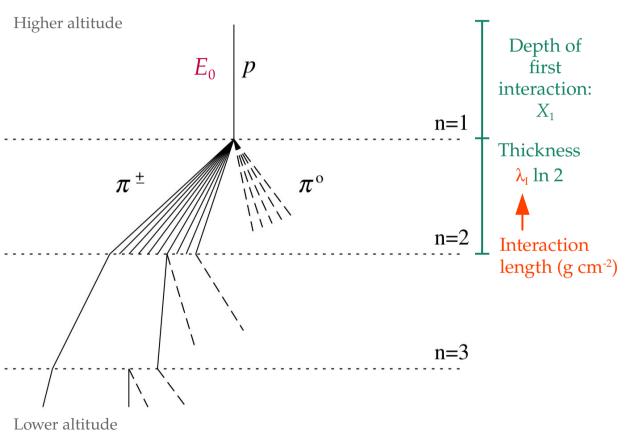
At maximum: N_{max} particles each with E_{C}^{π}

Inferring the primary UHECR energy:

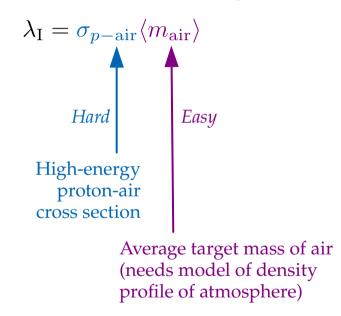


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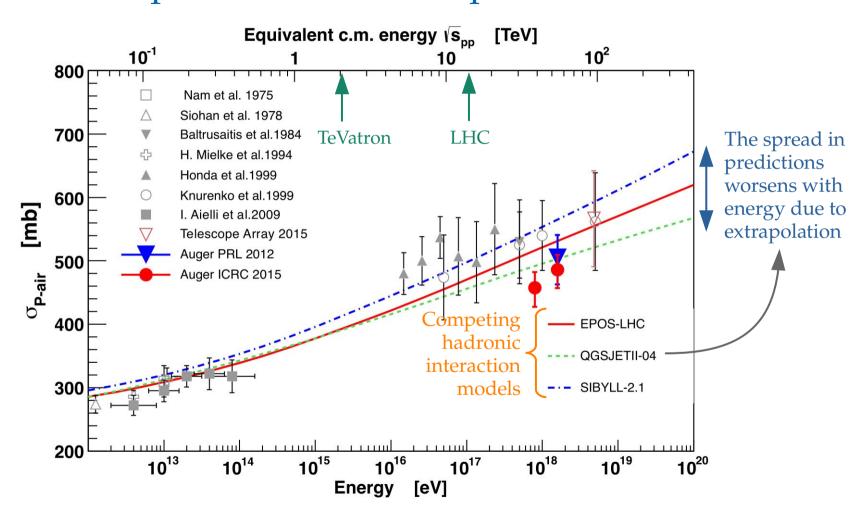
Inferring X_{max} :



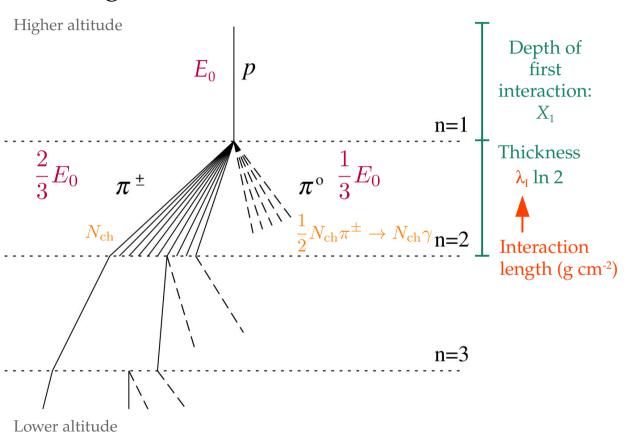
Proton-air interaction length:



Heitler, *The Quantum Theory of Radiation*, 1954 Matthews, *Astropart. Phys.* 2005



Inferring X_{max} :

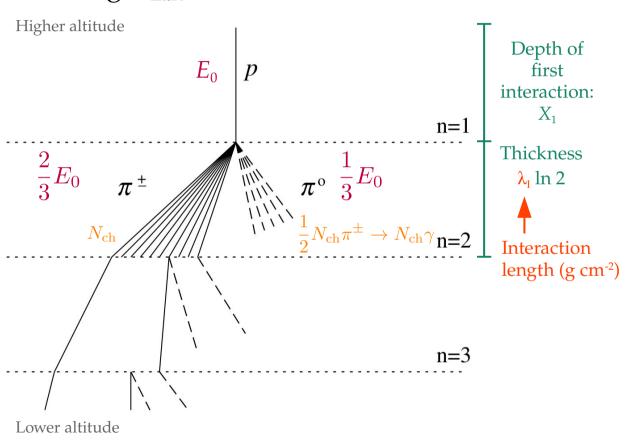


Proton-air interaction length:

$$\lambda_{\rm I} = \sigma_{p-{\rm air}} \langle m_{\rm air} \rangle$$

Heitler, *The Quantum Theory of Radiation*, 1954 Matthews, *Astropart. Phys.* 2005

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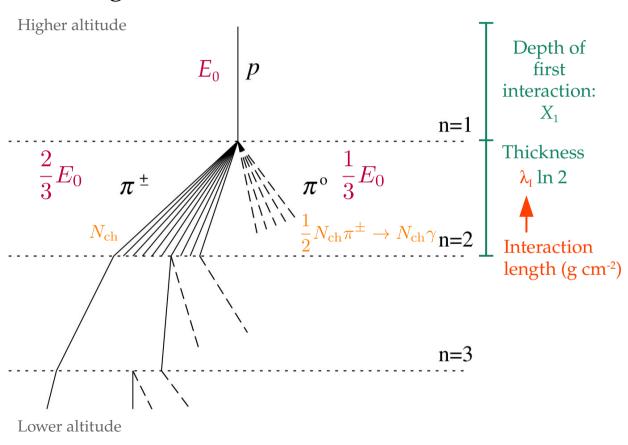
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Depth of first interaction:

$$X_1 = \lambda_{\rm I} \ln 2$$

Inferring X_{max} :



Proton-air interaction length:

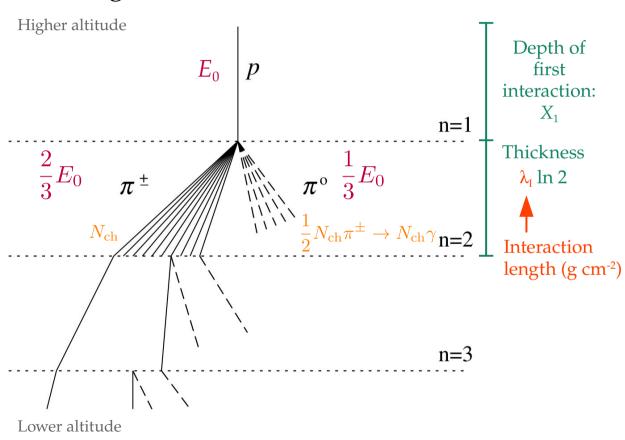
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Each photon from π^0 decay starts a shower of energy $(E_0/3)/N_{\rm ch}$

Inferring X_{max} :



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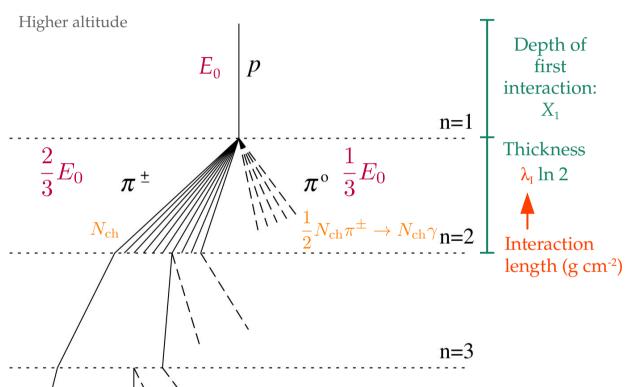
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Each e.m. shower reaches maximum at $\lambda_{\Gamma} \ln[E_0/(3N_{\rm ch})/E_{\rm C}^e]$

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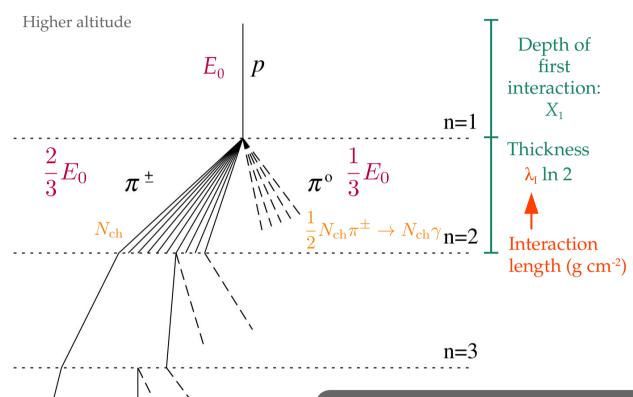
Depth of maximum of the *p*-initiated shower:

$$X_{\text{max}}^p = X_1 + \lambda_{\Gamma} \ln[E_0/(3N_{\text{ch}}E_{\text{C}}^e)]$$

Heitler, *The Quantum Theory of Radiation*, 1954 Matthews, *Astropart. Phys.* 2005

Lower altitude

Inferring X_{max} :



errors from hadronic

interaction models

Proton-air interaction length:

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Each photon from π^0 decay starts a shower of energy $(E_0/3)/N_{\rm ch}$

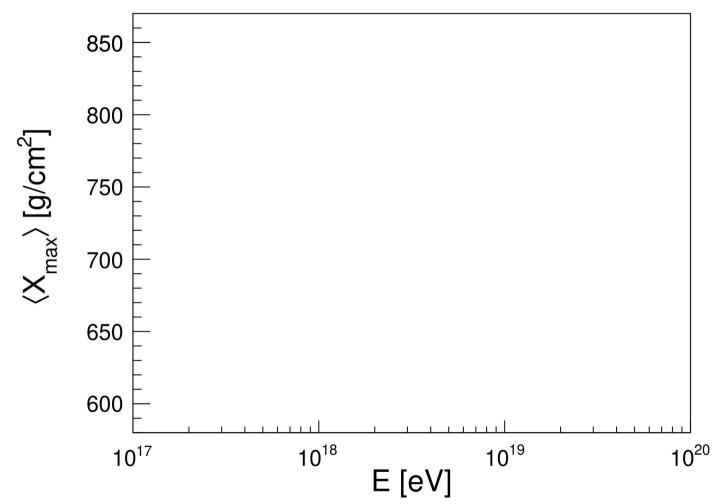
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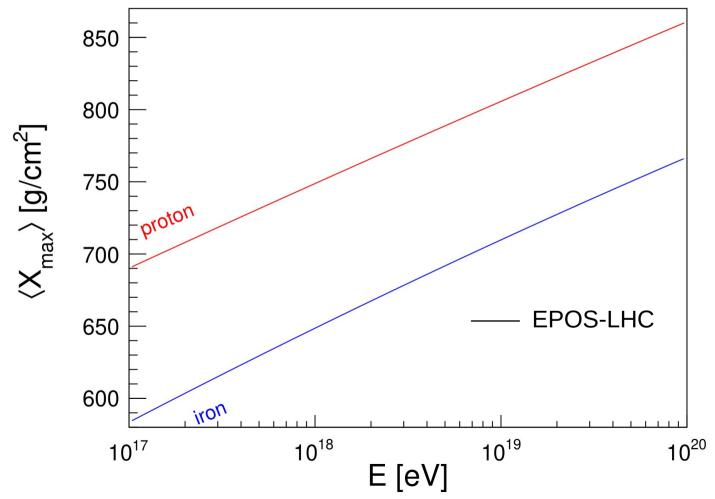
Large Depth of maximum of the *p*-initiated shower:

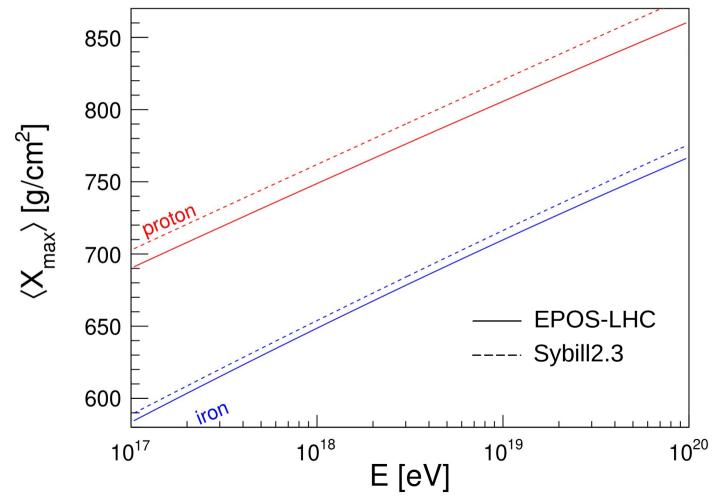
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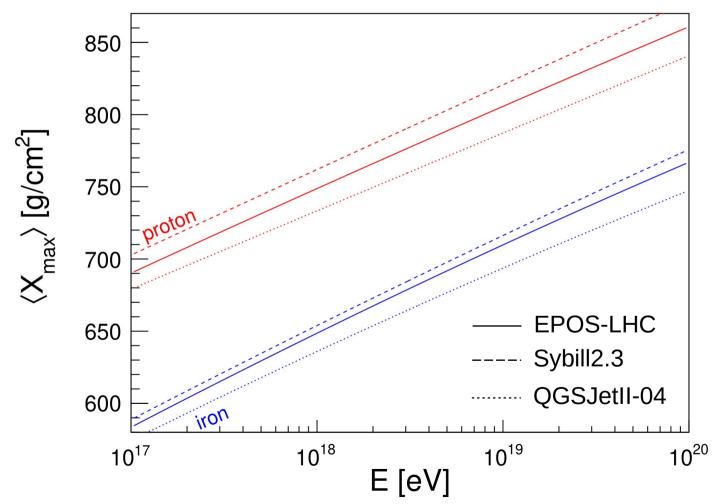
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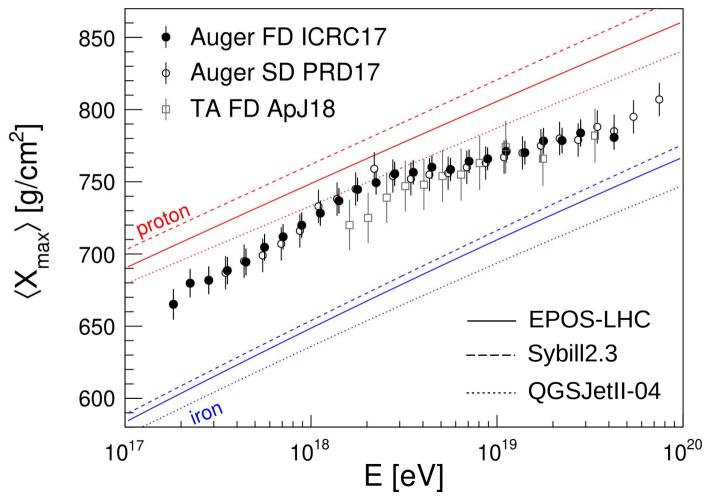
Lower altitude

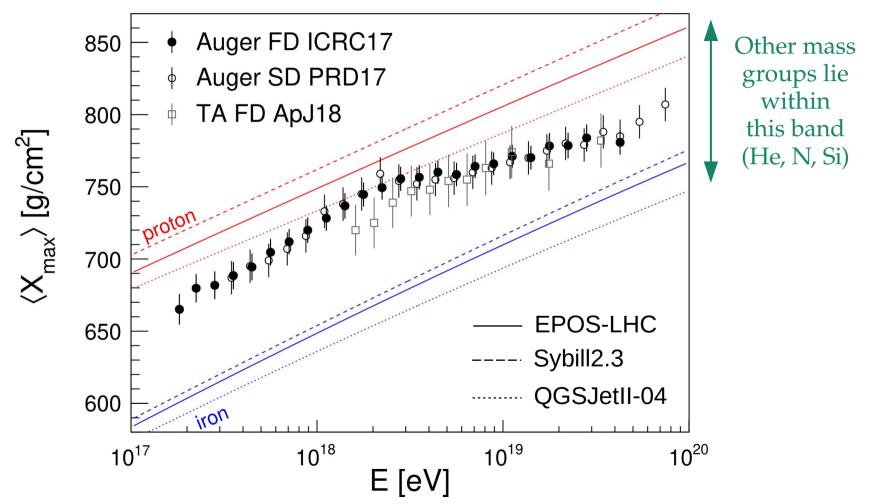


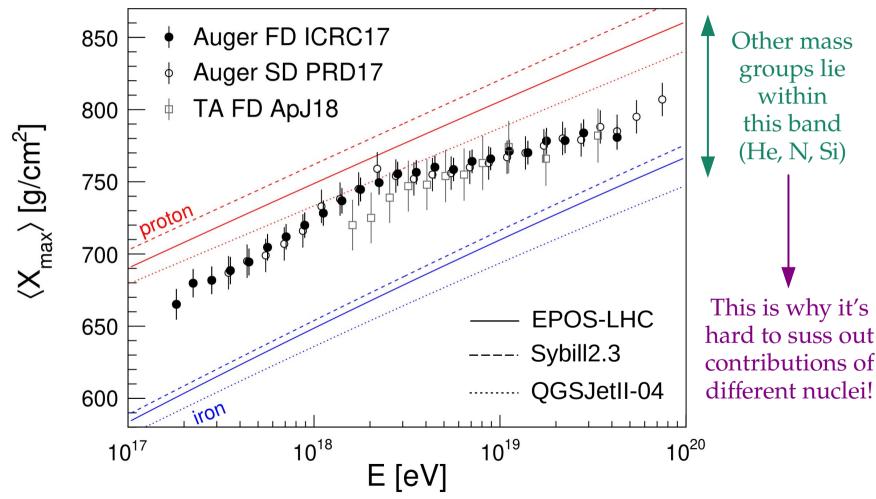












UHECRs: more sophisticated models

Use more data:

Spectrum + mass composition (X_{max})

Five mass groups:

H, He, N, Si, Fe

Common maximum rigidity:

Max. rigidity is $R_{\text{max}} = E_{\text{max}}/Z$

$$Q_Z(E) \propto E^{-\gamma} e^{-E/(ZR_{\rm max})}$$

Add nuclei photodisintegration:

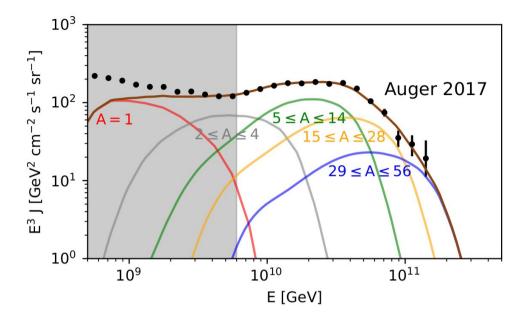
During propagation, interaction of nuclei on CMB or EBL breaks them up,

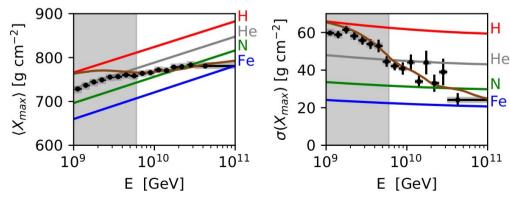
$$A + \gamma \rightarrow (A - 1) + \gamma$$

Heinze, Fedynitch, Boncioli, Winter, ApJ 2019

See also: Romero-Wolf & Ave, JCAP 2018

Alves Batista, Almeida, Lago, Kotera, JCAP 2019





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 "Peters cycle"

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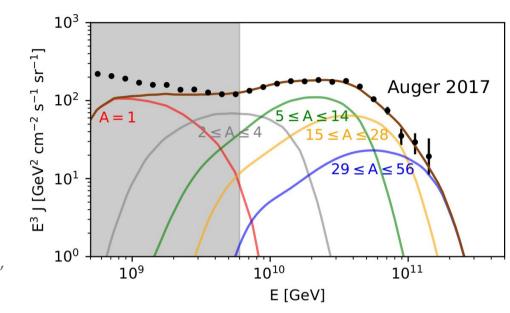
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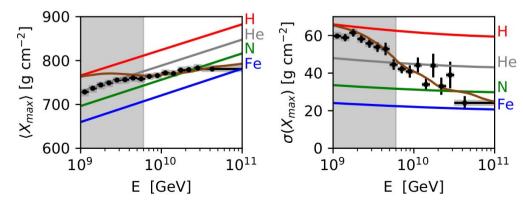
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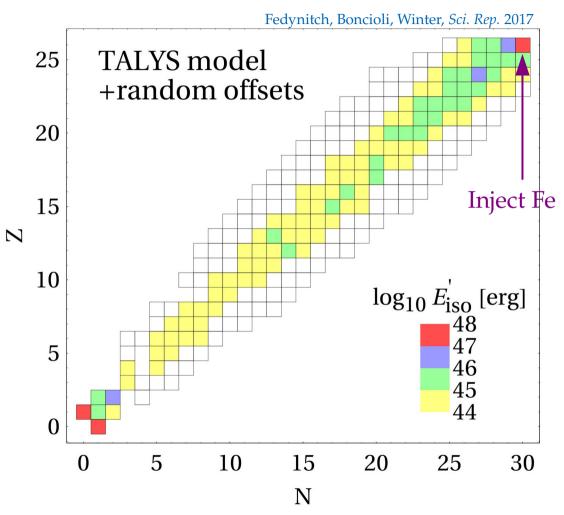
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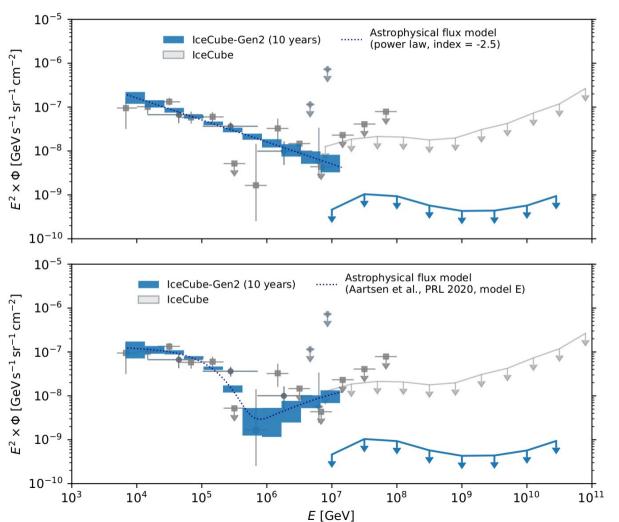
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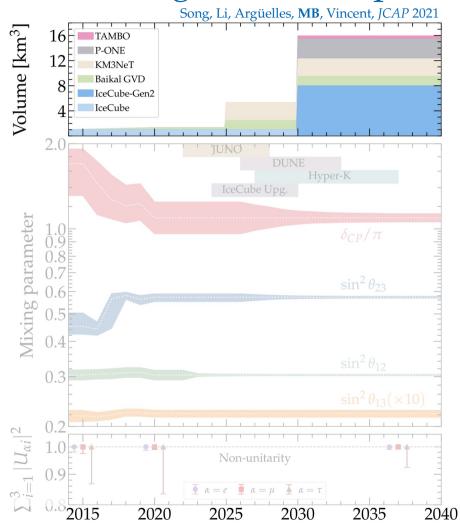
High-energy cosmic neutrinos

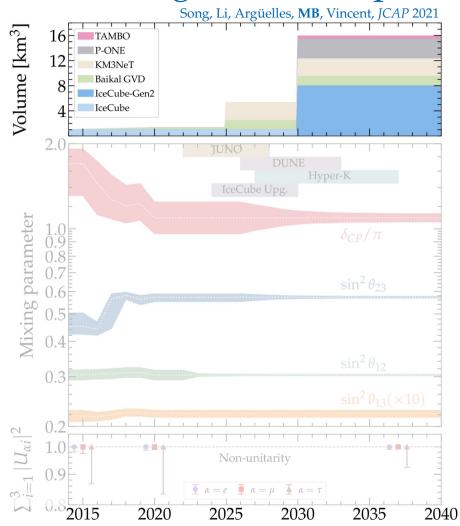
Measuring the diffuse flux precisely

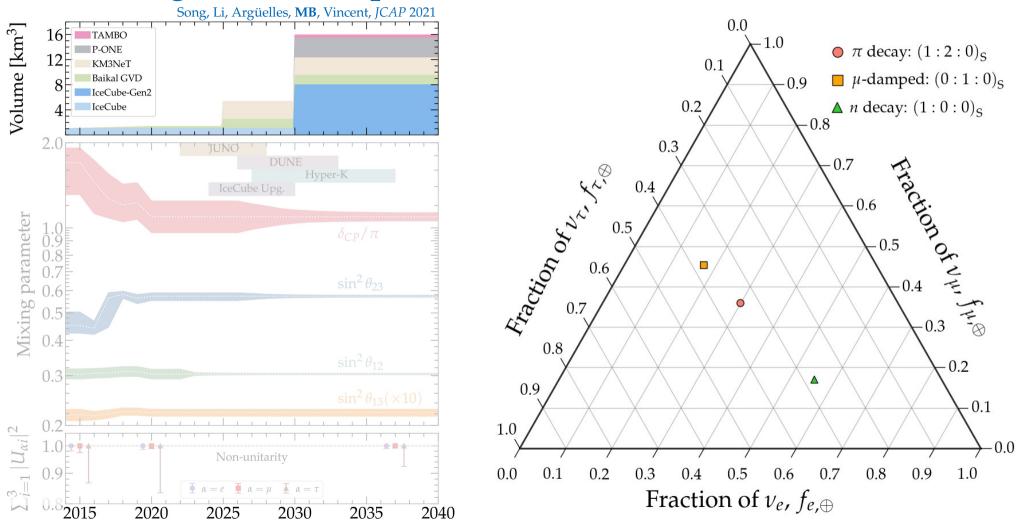


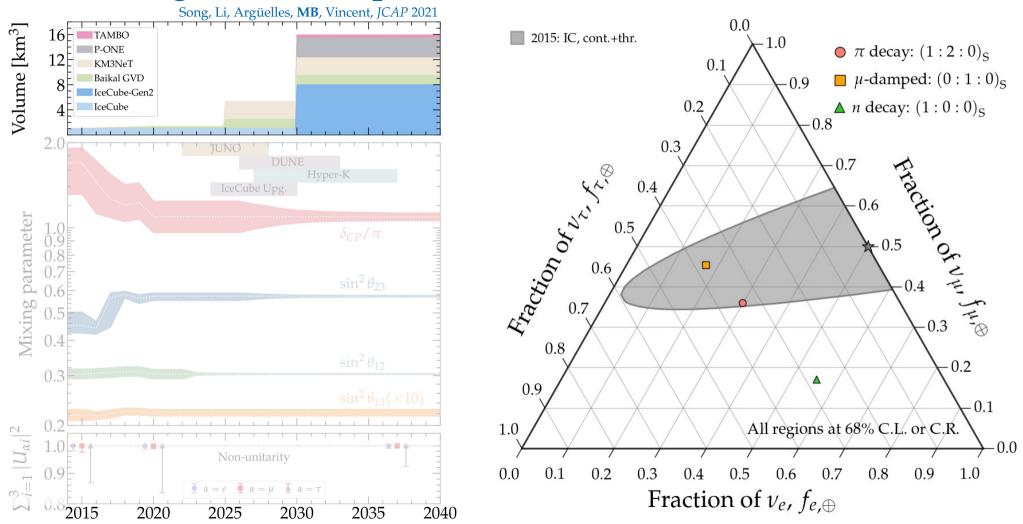
Assuming a powerlaw v flux $\propto E^{-2.5}$

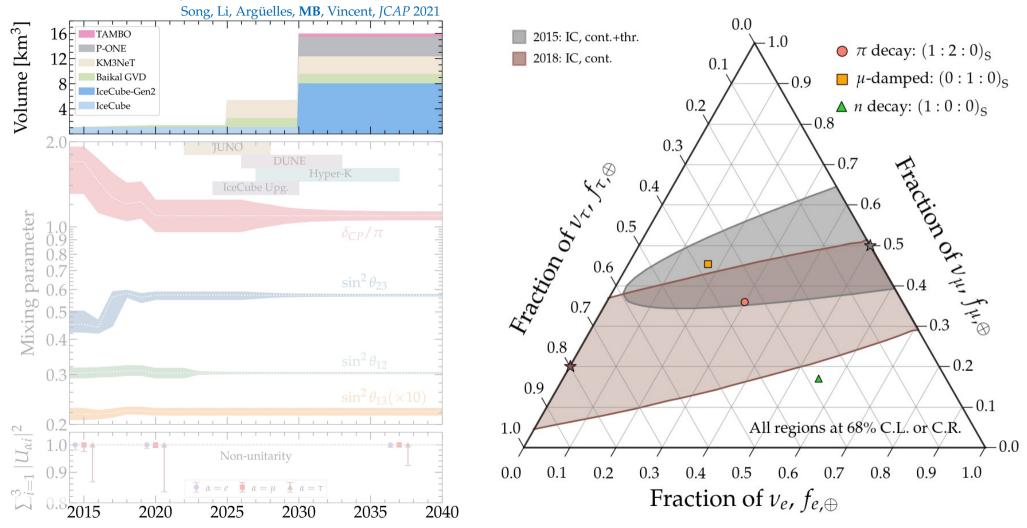
Assuming a power-law v flux with 100-TeV cut-off + $p\gamma$ bump at tens of TeV

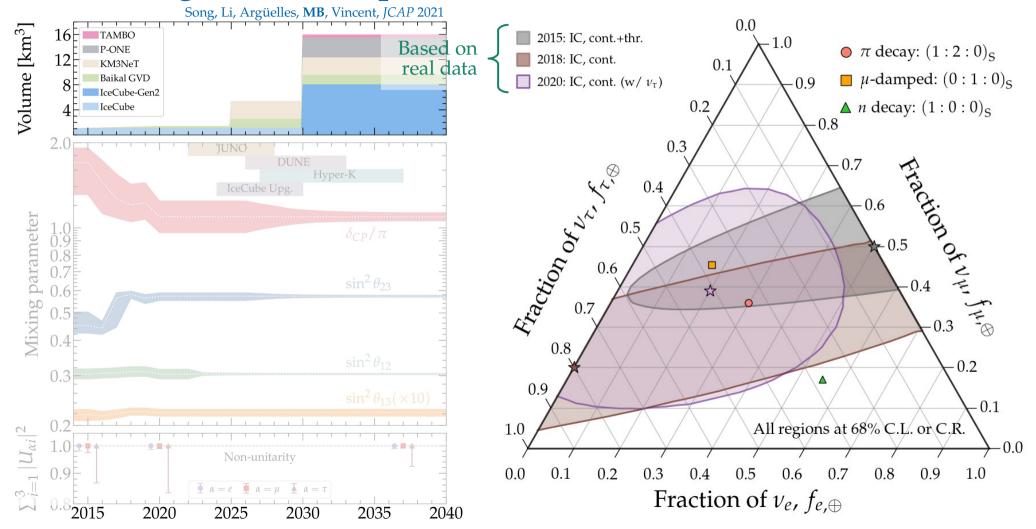


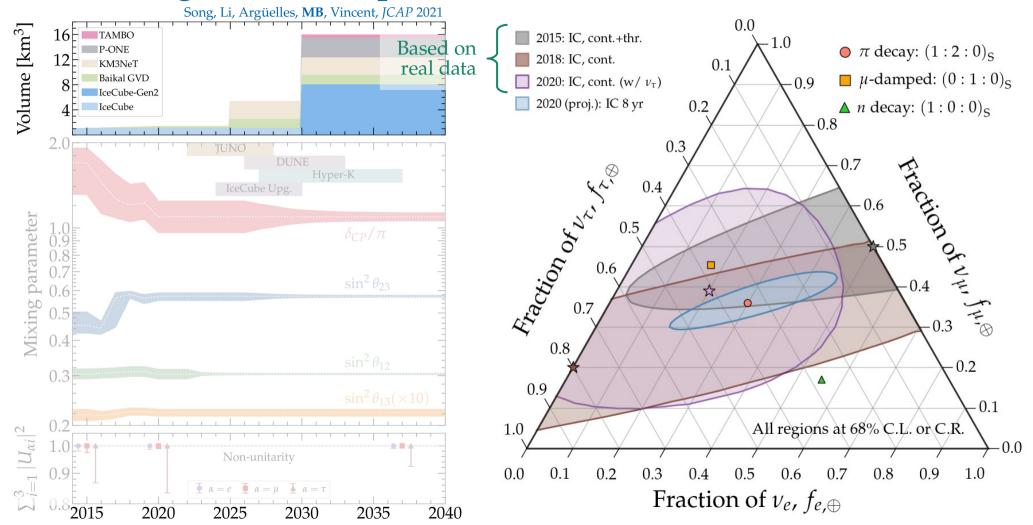


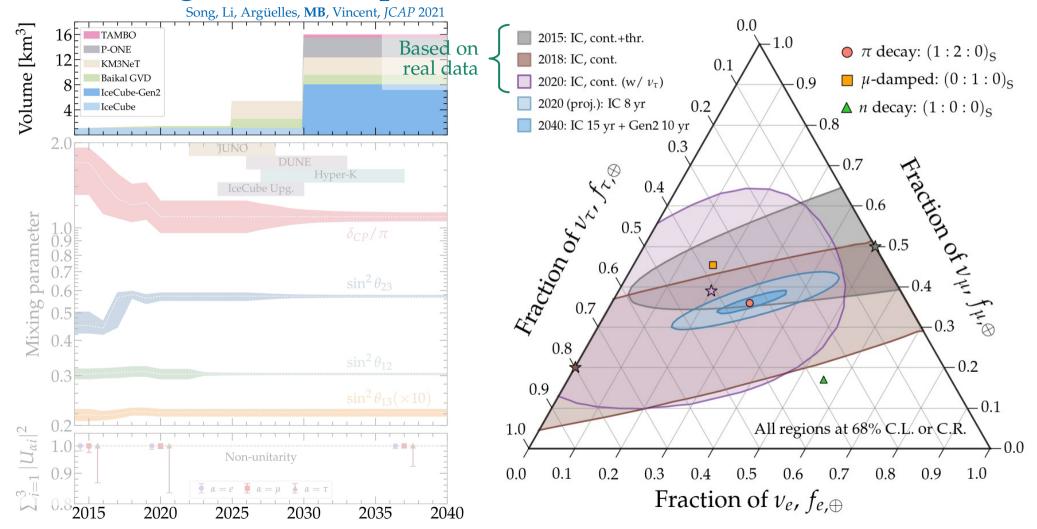


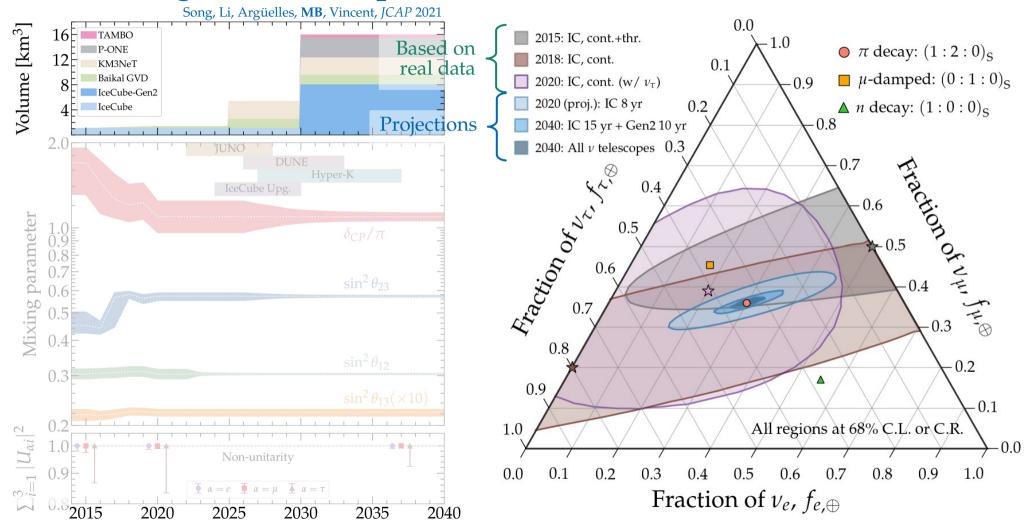




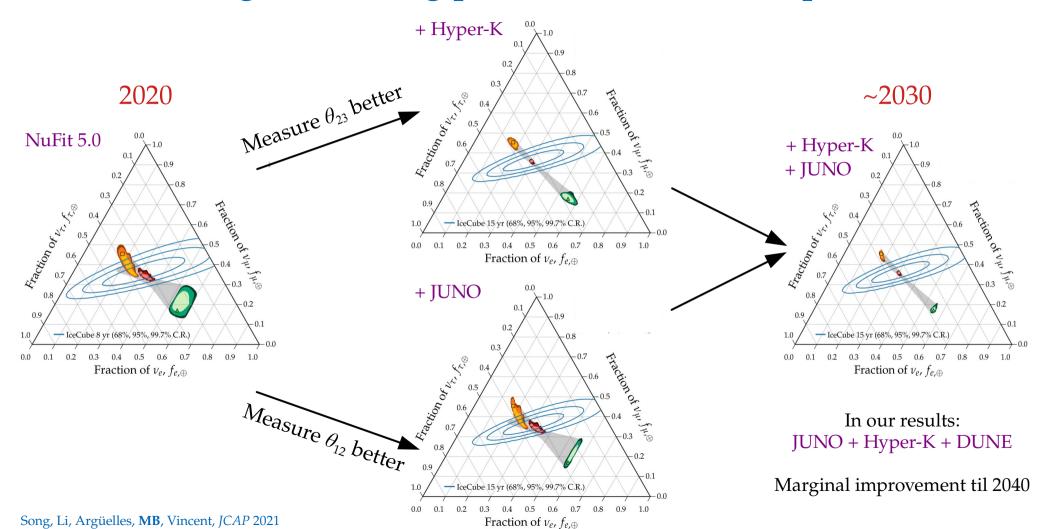




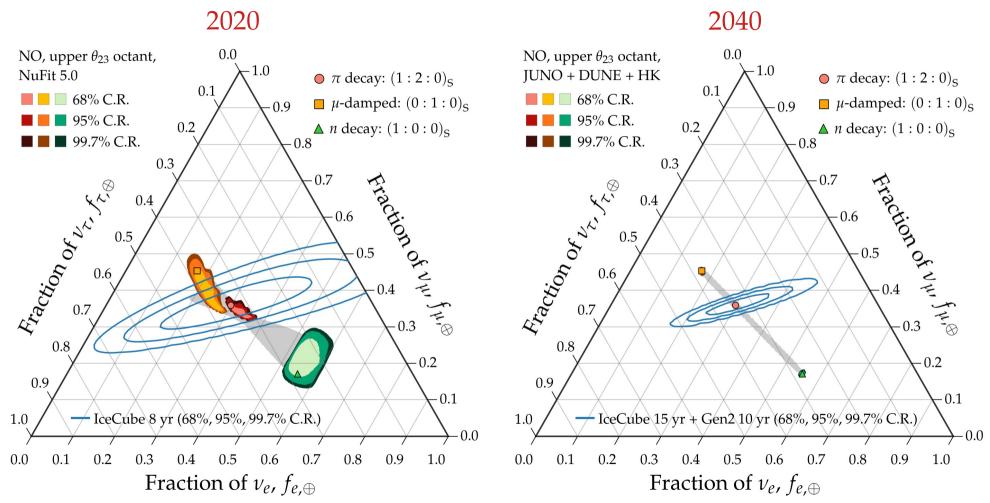




How knowing the mixing parameters better helps



Theoretically palatable regions: $2020 \rightarrow 2040$



Measuring the high-energy *vN* cross section

Number of detected neutrinos (simplified for presentation):

$$N \propto \Phi_{\nu} \sigma_{\nu N} e^{- au_{\nu N}} = \Phi_{\nu} \sigma_{\nu N} e^{-L\sigma_{\nu N} n_N}$$

Neutrino flux Cross section

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Neutrino flux Cross section

Downgoing neutrinos (L short \rightarrow no matter)

$$N \propto \Phi_{\nu} \sigma_{\nu N}$$

Measuring the high-energy *vN* cross section

Number of detected neutrinos (simplified for presentation):

$$N \propto \Phi_{\nu} \sigma_{\nu N} e^{-\tau_{\nu N}} = \Phi_{\nu} \sigma_{\nu N} e^{-L\sigma_{\nu N} n_N}$$

Neutrino flux Cross section

Downgoing neutrinos (L short \rightarrow no matter)

$$N \propto \Phi_{
u} \sigma_{
u N}$$
 Degeneracy

Measuring the high-energy vN cross section

Number of detected neutrinos (simplified for presentation):

$$N \propto \Phi_{\nu} \sigma_{\nu N} e^{-\tau_{\nu N}} = \Phi_{\nu} \sigma_{\nu N} e^{-L\sigma_{\nu N} n_N}$$

Neutrino flux Cross section

Downgoing neutrinos (L short \rightarrow no matter)

$$N \propto \Phi_{
u} \sigma_{
u N}$$
 Degeneracy

Upgoing neutrinos ($L \log \rightarrow \log \log m$)

$$N \propto \Phi_{\nu} \sigma_{\nu N} e^{-L\sigma_{\nu N} n_N}$$

Measuring the high-energy *vN* cross section

Number of detected neutrinos (simplified for presentation):

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Neutrino flux Cross section

Downgoing neutrinos (L short \rightarrow no matter)

$$N \propto \Phi_{
u} \sigma_{
u N}$$
 Degeneracy

Upgoing neutrinos ($L \log \rightarrow \log \log m$)

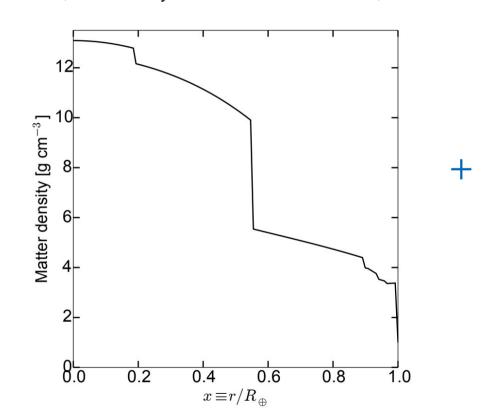
$$N \propto \Phi_{\nu} \sigma_{\nu N} e^{-L\sigma_{\nu N} n_N}$$

Breaks the degeneracy

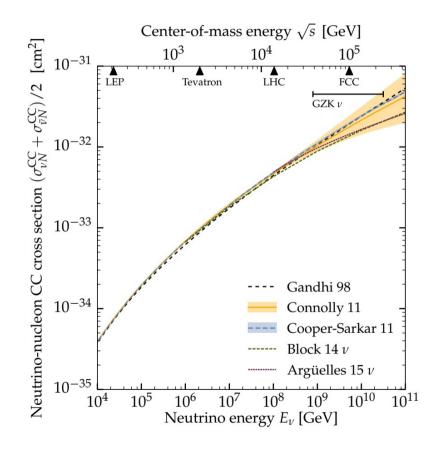
A feel for the in-Earth attenuation

Earth matter density

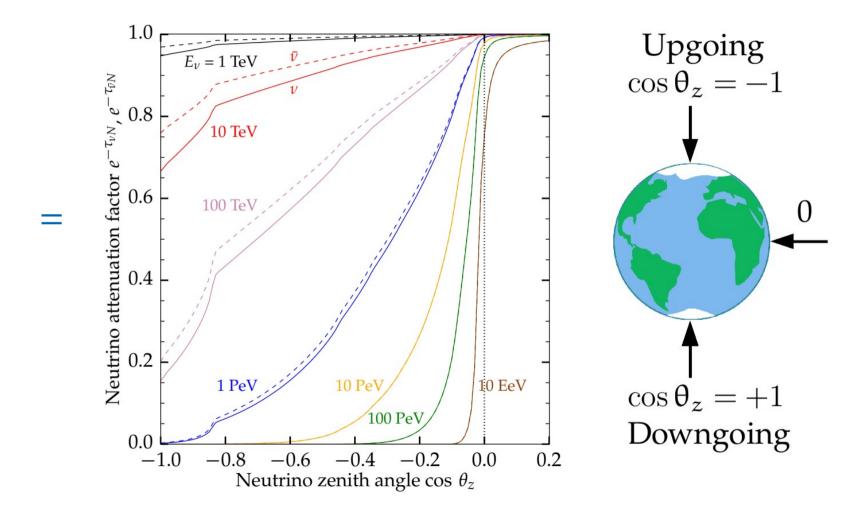
(Preliminary Reference Earth Model)

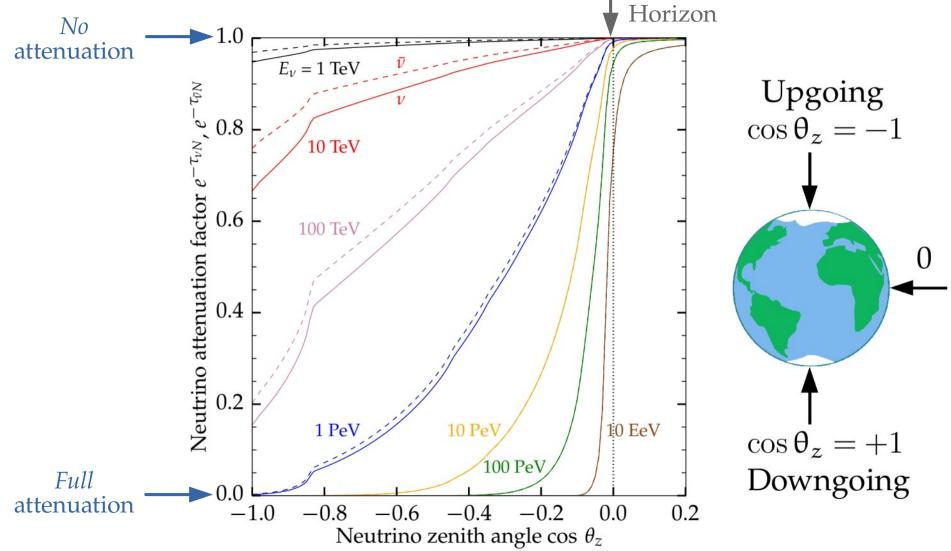


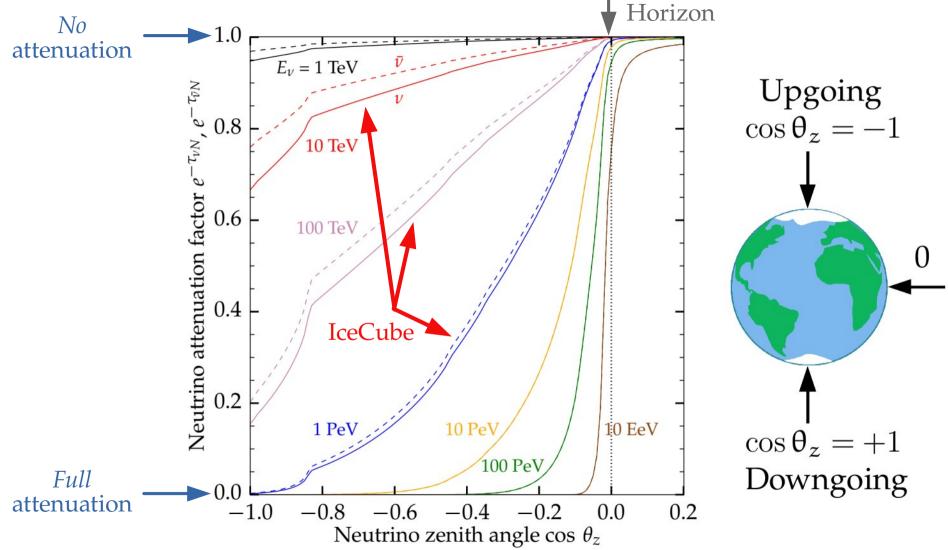
Neutrino-nucleon cross section

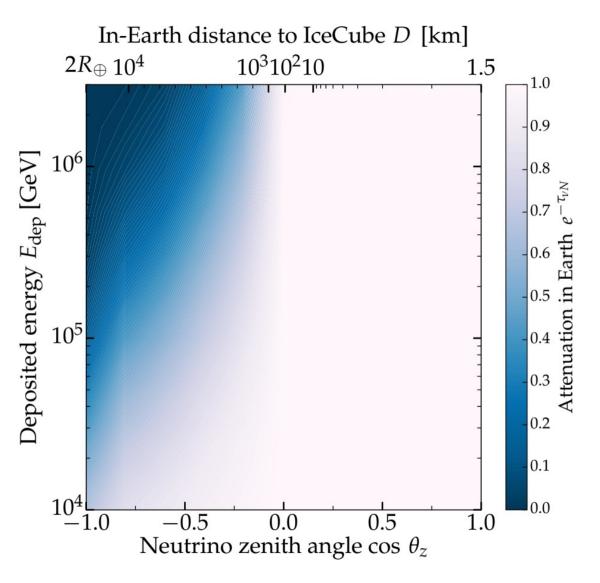


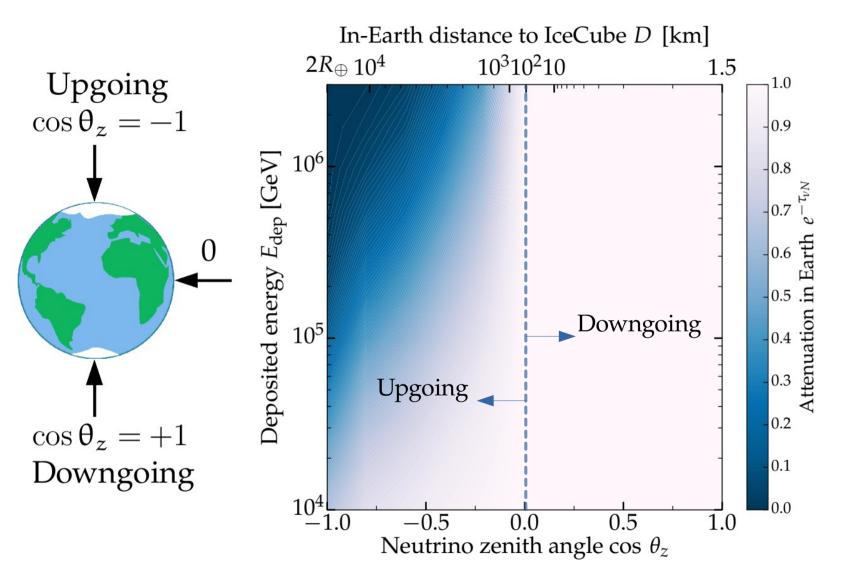
A feel for the in-Earth attenuation

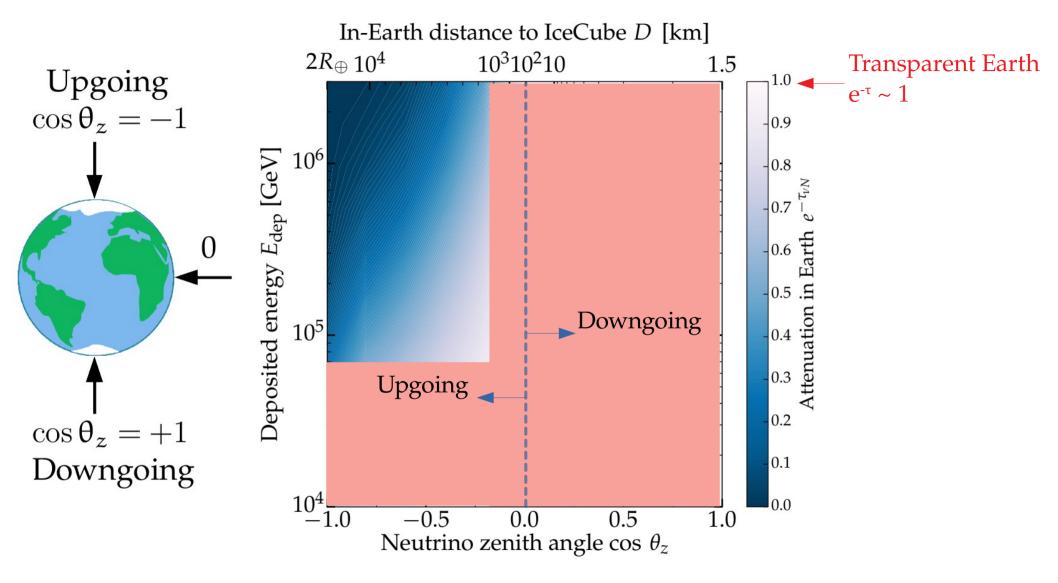


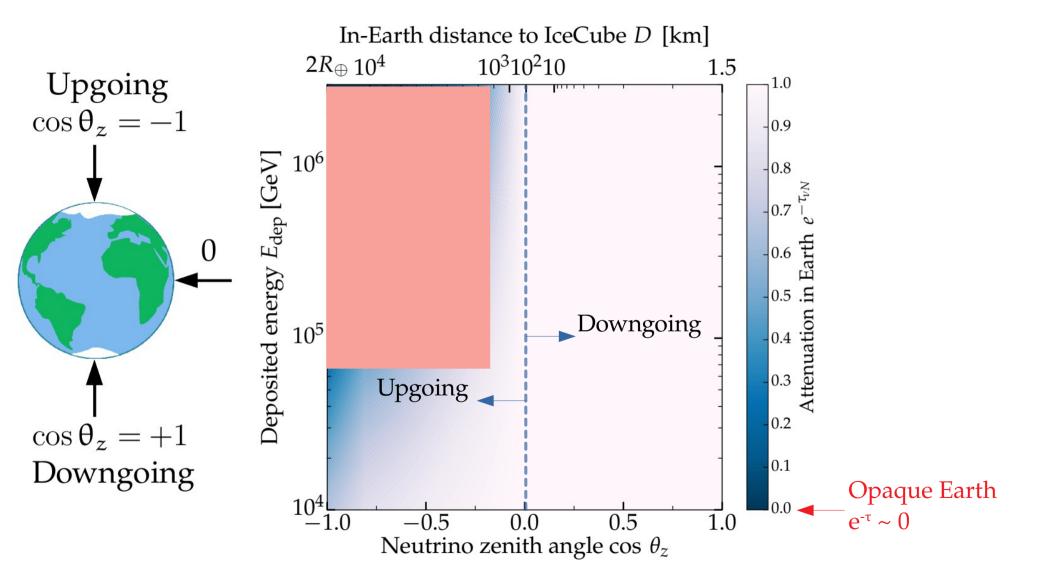




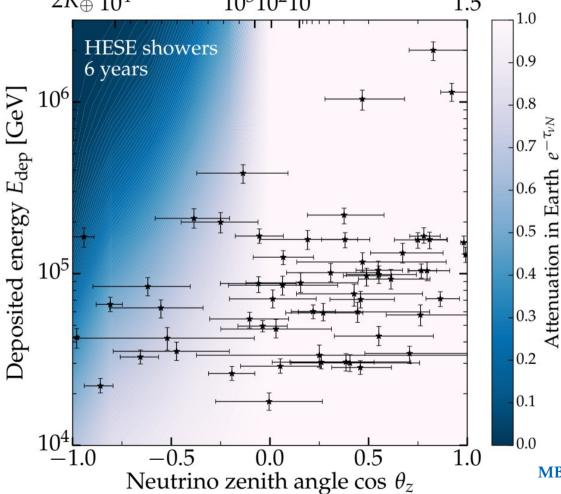




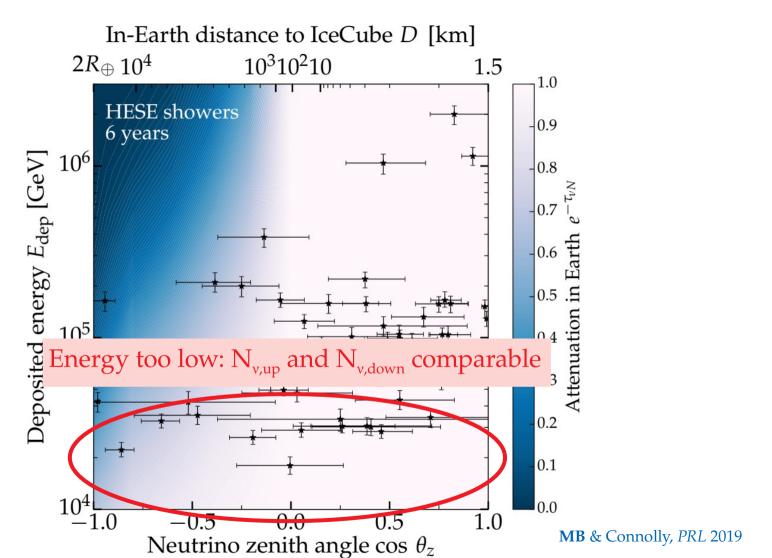


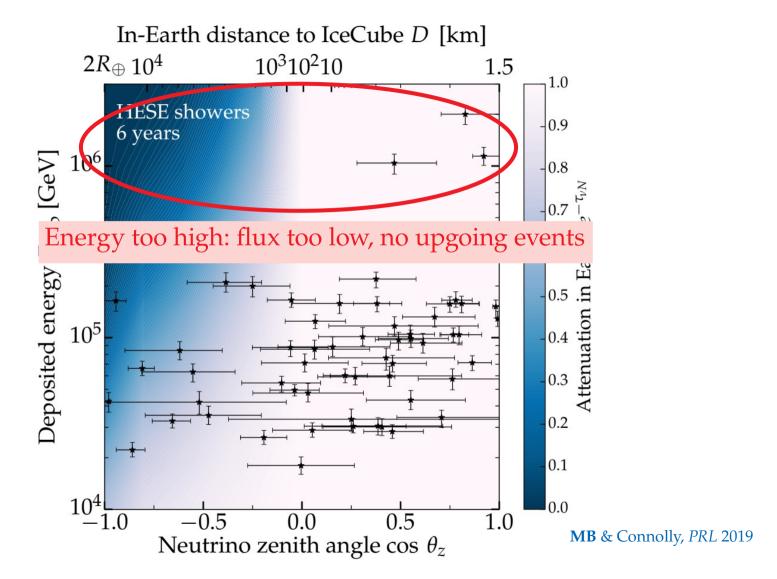


In-Earth distance to IceCube *D* [km] $2R_{\oplus}\,10^4$ $10^3 10^2 10$ 1.5 1.0 **HESE** showers -0.96 years -0.8

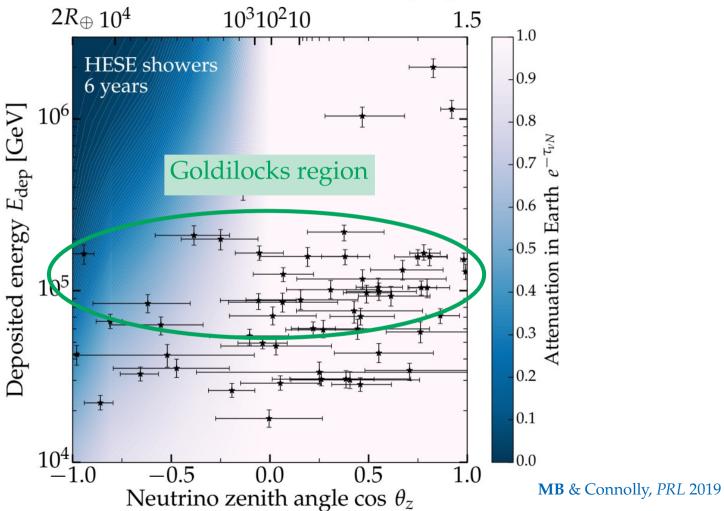


MB & Connolly, PRL 2019

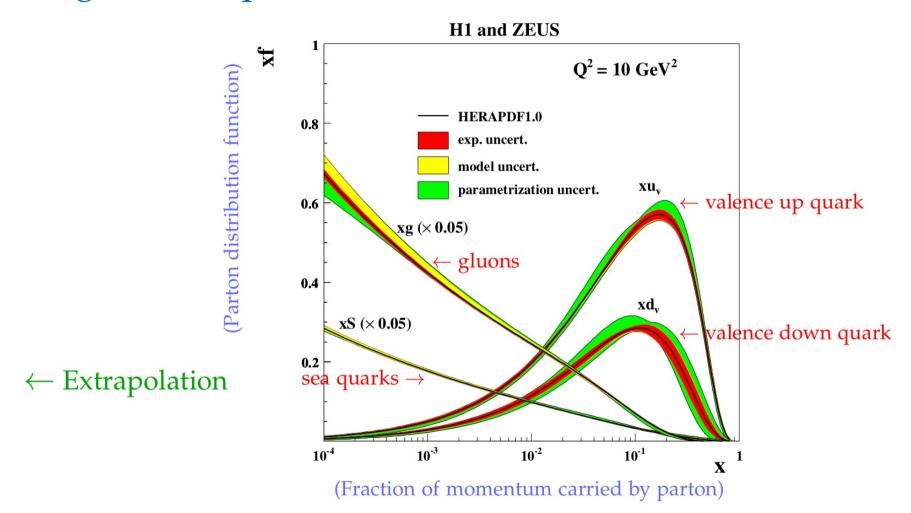




In-Earth distance to IceCube *D* [km]



Peeking inside a proton



4. Dark matter: *Annihilation and decay into v*

High-energy neutrinos from dark matter

Dark matter co-annihilation:

$$\chi + \chi \to \nu + \bar{\nu}$$

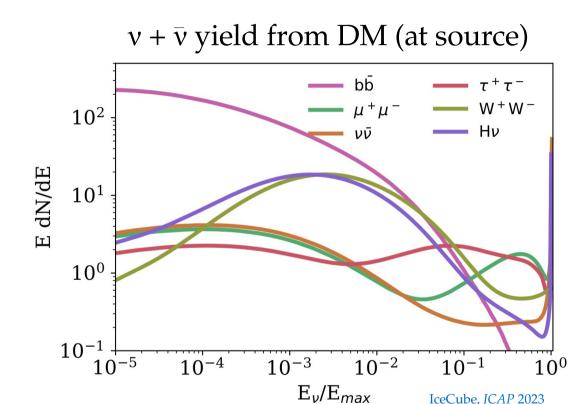
$$\chi + \chi \to \dots \to \nu + \bar{\nu} + \dots$$

$$E_{\text{max}} = m_{\chi}$$

Dark matter decay:

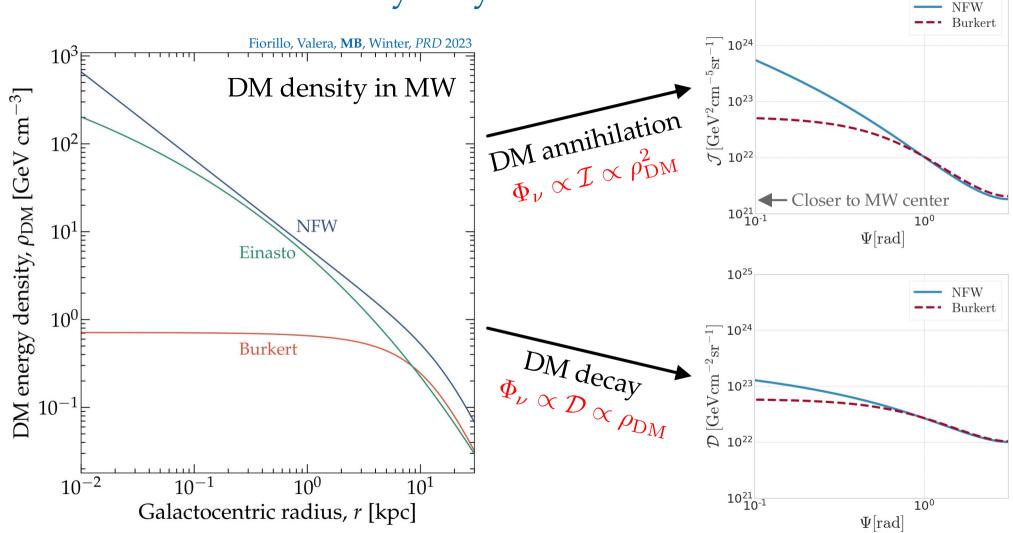
$$\chi \to \nu + \bar{\nu}$$
 $\chi \to \dots \to \nu + \bar{\nu} + \dots$
 $E_{\text{max}} = m_{\chi}/2$

Electroweak corrections (off-shell *W* and *Z* emission) broaden the v spectrum



Approximate independence on m_{χ} valid for $m_{\chi} \approx 100 \text{ TeV} - 10 \text{ PeV}$

Dark matter in the Milky Way



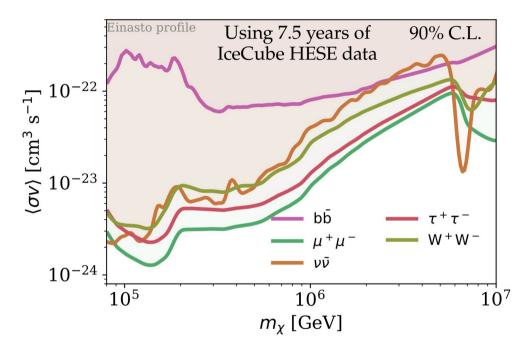
IceCube, PRD 2023

 10^{25}

Limits on dark matter annihilation

Per annihilation channel

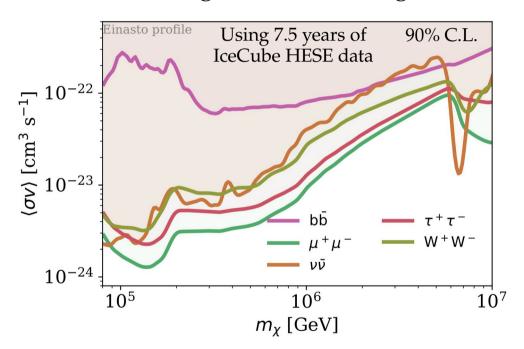
(assuming 100% branching ratio)



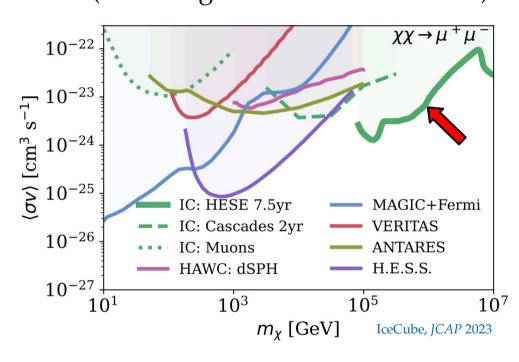
Two DM contributions: Galactic (anisotropic) + extragalactic (isotropic) Plus background of atmospheric neutrinos (anisotropic, but different)

Limits on dark matter annihilation

Per annihilation channel (assuming 100% branching ratio)



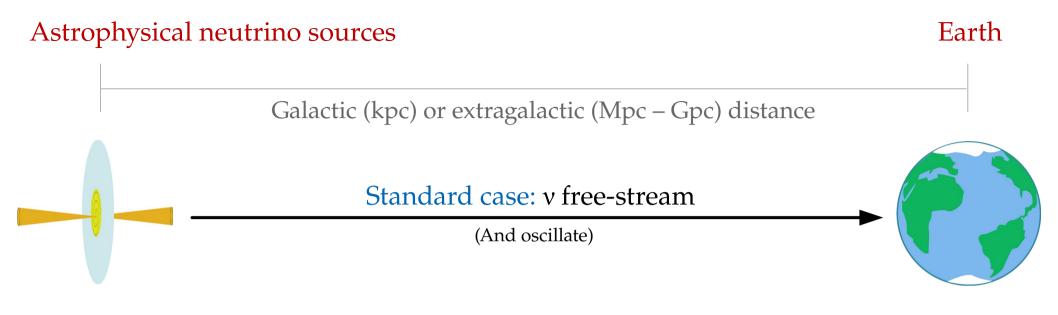
Compared to other limits (assuming annihilation to muons)

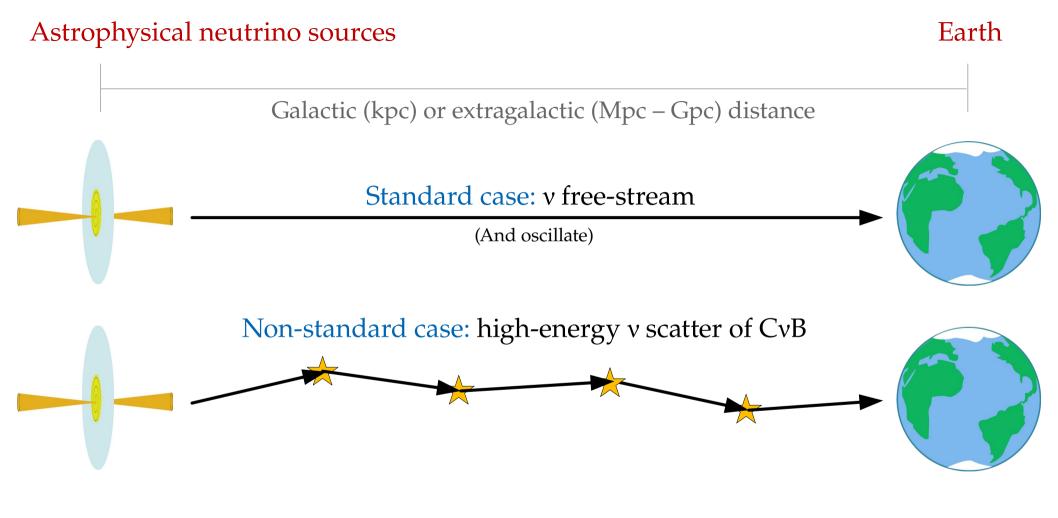


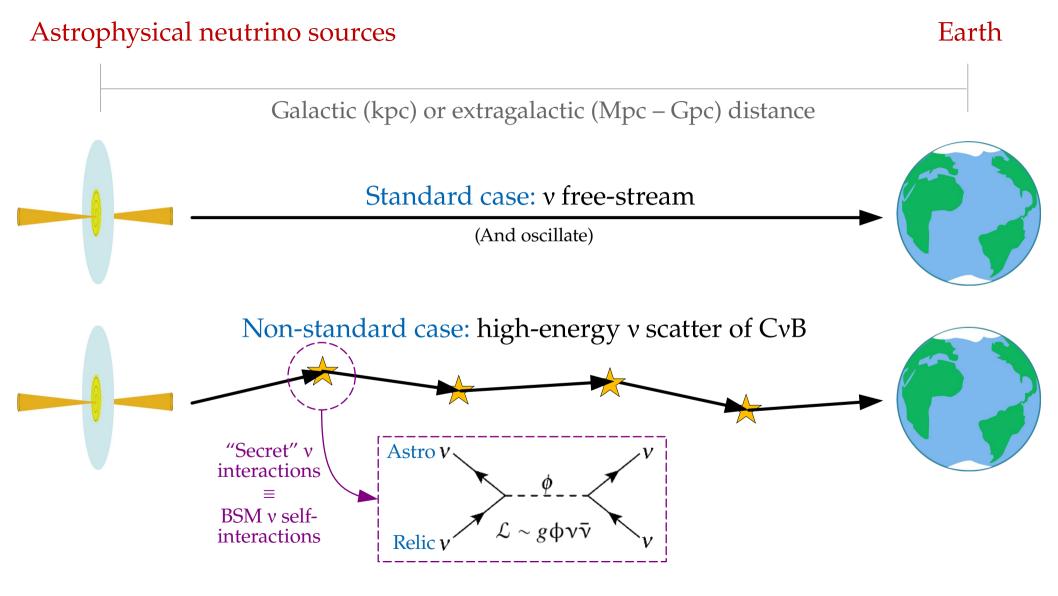
Two DM contributions: Galactic (anisotropic) + extragalactic (isotropic) Plus background of atmospheric neutrinos (anisotropic, but different)

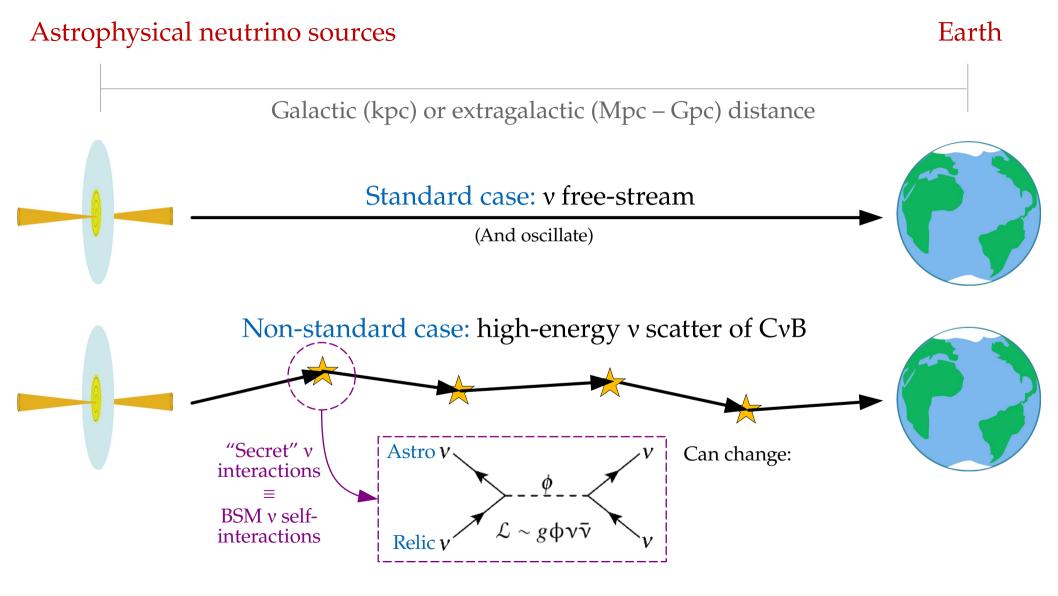
5. New neutrino interactions: *Are there secret vv interactions?*

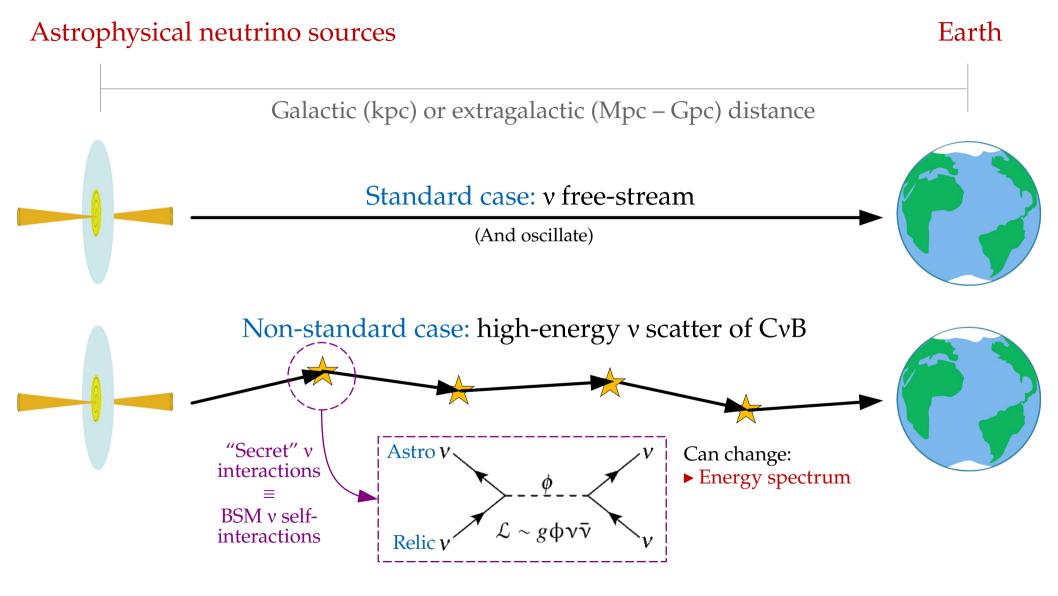
Galactic (kpc) or extragalactic (Mpc – Gpc) distance

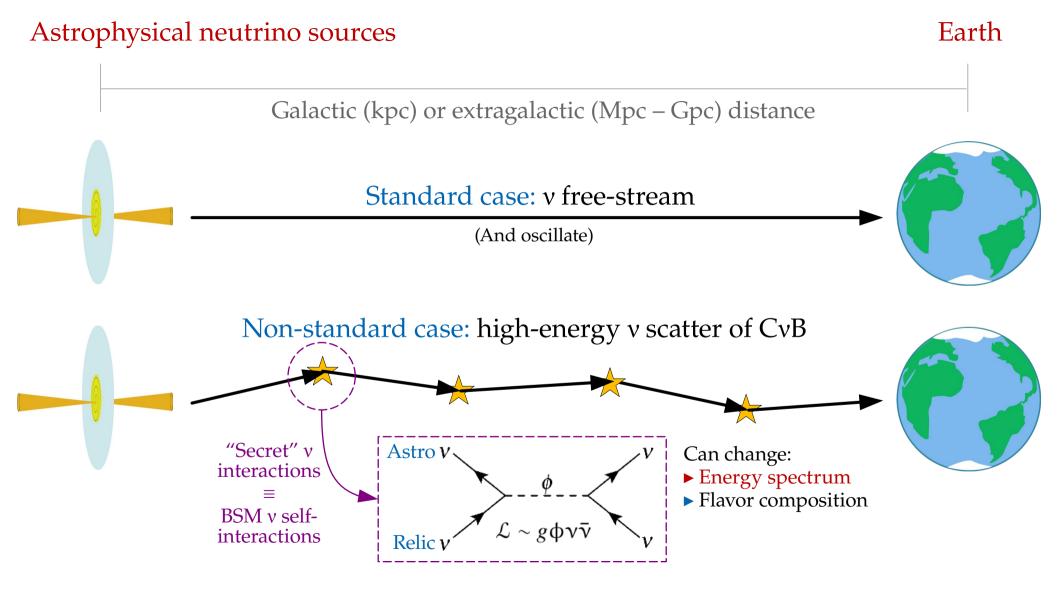


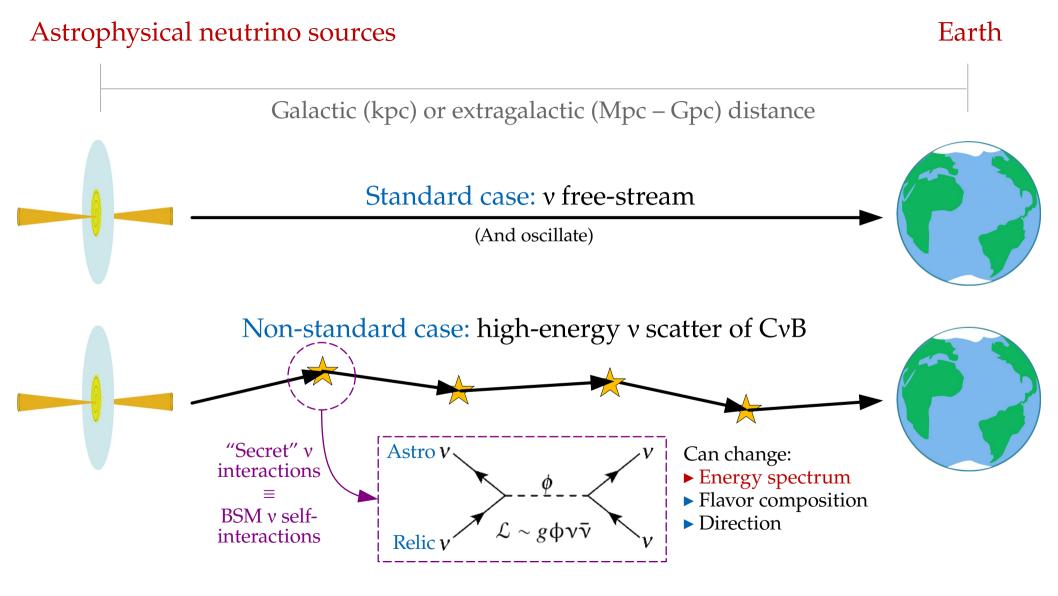


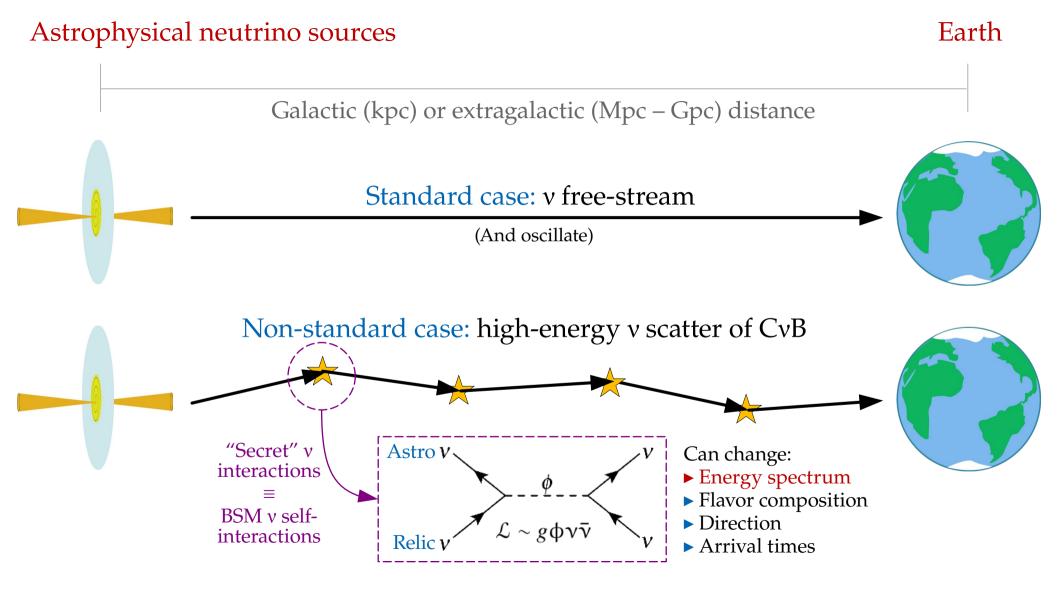




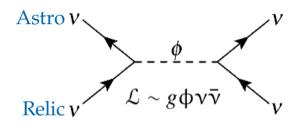






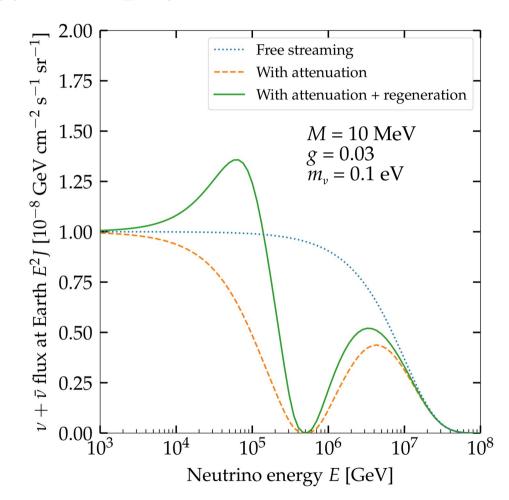


"Secret" neutrino interactions between astrophysical v (PeV) and relic v (0.1 meV):

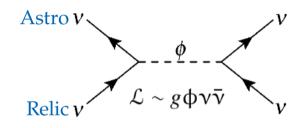


Cross section:
$$\sigma = \frac{g^4}{4\pi} \frac{s}{(s - M^2)^2 + M^2 \Gamma^2}$$

Resonance energy:
$$E_{\text{res}} = \frac{M^2}{2m_{\gamma}}$$

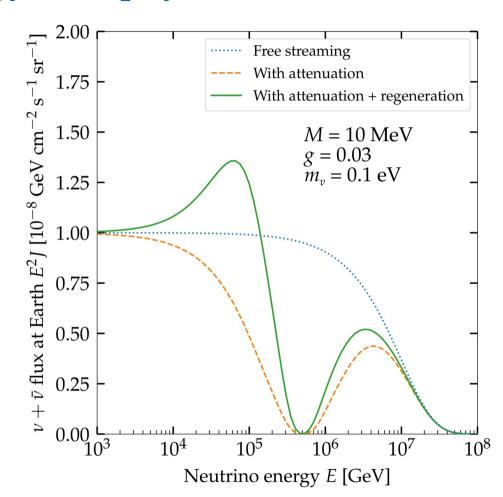


"Secret" neutrino interactions between astrophysical v (PeV) and relic v (0.1 meV):

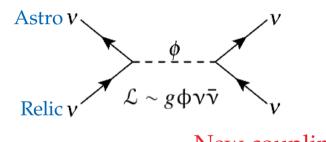


Cross section: $\sigma = \frac{g^4}{4\pi} \frac{s}{(s - M^2)^2 + M^2\Gamma^2}$ Mediator

Resonance energy:
$$E_{\text{res}} = \frac{M^2}{2m_{\gamma}}$$

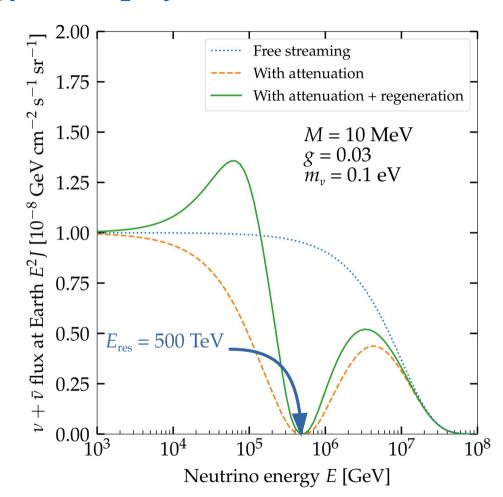


"Secret" neutrino interactions between astrophysical v (PeV) and relic v (0.1 meV):

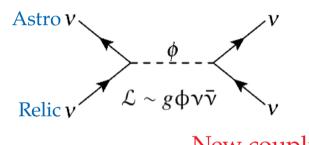


Cross section: $\sigma = \frac{g^4}{4\pi} \frac{s}{(s - M^2)^2 + M^2\Gamma^2}$ Mediator r

Resonance energy:
$$E_{\text{res}} = \frac{M^2}{2m_{\gamma}}$$

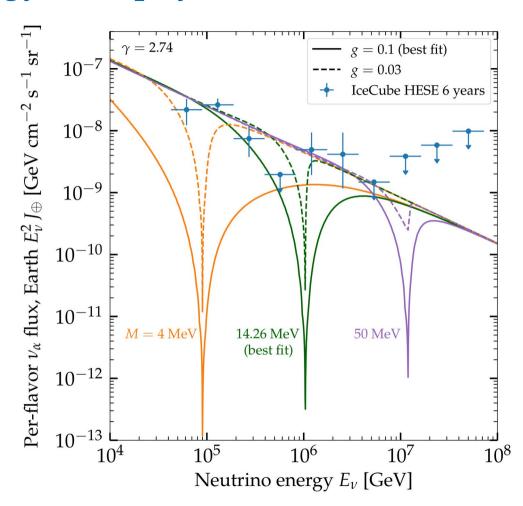


"Secret" neutrino interactions between astrophysical v (PeV) and relic v (0.1 meV):

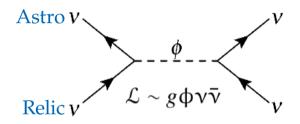


Cross section:
$$\sigma = \frac{g^4}{4\pi} \frac{s}{(s - M^2)^2 + M^2\Gamma^2}$$
Mediator

Resonance energy:
$$E_{\text{res}} = \frac{M^2}{2m_{\gamma}}$$



"Secret" neutrino interactions between astrophysical v (PeV) and relic v (0.1 meV):



Cross section:
$$\sigma = \frac{g^4}{4\pi} \frac{s}{(s - M^2)^2 + M^2 \Gamma^2}$$
Mediator r

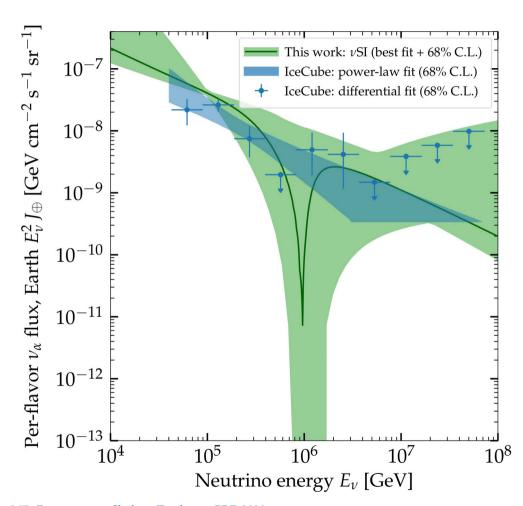
Resonance energy:
$$E_{\text{res}} = \frac{M^2}{2m_2}$$

MB, Rosenstroem, Shalgar, Tamborra, *PRD*See also: Esteban, Pandey, Brdar, Beacom, *PRD*Creque-Sarbinowski, Hyde, Kamionkowski, *PRD*Ng & Beacom, *PRD*Cherry, Friedland, Shoemaker, 1411.1071 Blum, Hook, Murase, 1408.3799

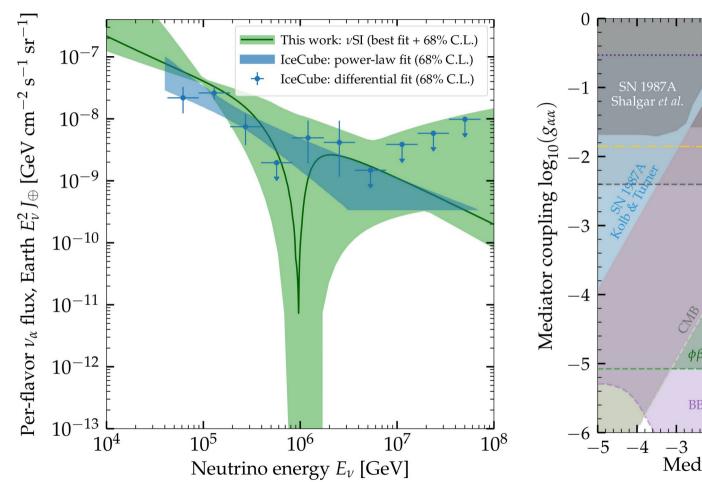
Looking for evidence of vSI

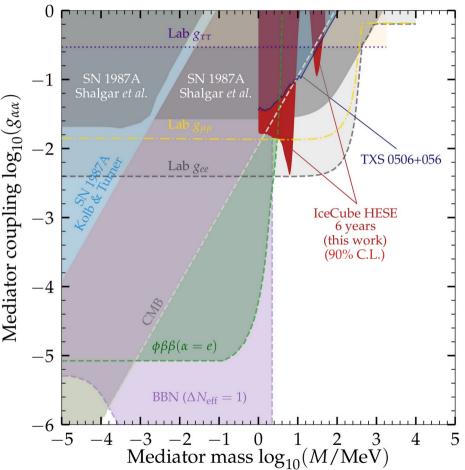
- ► Look for dips in 6 years of public IceCube data (HESE)
- ▶ 80 events, 18 TeV–2 PeV
- Assume flavor-diagonal and universal: $g_{\alpha\alpha} = g \delta_{\alpha\alpha}$
- Bayesian analysis varying M, g, shape of emitted flux (γ)
- ► Account for atmospheric v, in-Earth propagation, detector uncertainties

No significant ($> 3\sigma$) evidence for a spectral dip ...



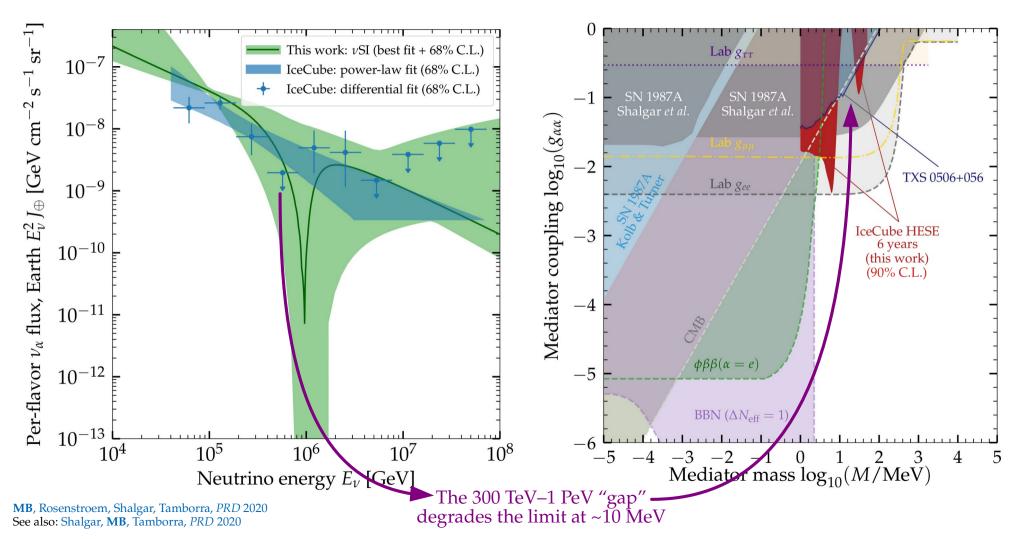
No significant ($> 3\sigma$) evidence for a spectral dip ... so we set upper limits on the coupling g





MB, Rosenstroem, Shalgar, Tamborra, PRD 2020 See also: Shalgar, MB, Tamborra, PRD 2020

No significant ($> 3\sigma$) evidence for a spectral dip ... so we set upper limits on the coupling *g*



6. Unstable neutrinos: *Are neutrinos for ever?*

Are neutrinos forever?

- ▶ In the Standard Model (vSM), neutrinos are essentially stable ($\tau > 10^{36}$ yr):
 - ► One-photon decay $(v_i \rightarrow v_i + \gamma)$: $\tau > 10^{36} (m_i/\text{eV})^{-5} \text{ yr}$
 - ► One-photon decay $(v_i \rightarrow v_j + \gamma)$: $\tau > 10^{36} (m_i/\text{eV})^{-5} \text{ yr}$ ► Two-photon decay $(v_i \rightarrow v_j + \gamma + \gamma)$: $\tau > 10^{57} (m_i/\text{eV})^{-9} \text{ yr}$ $\tau > 10^{57} (m_i/\text{eV})^{-9} \text{ yr}$ $\tau > 10^{57} (m_i/\text{eV})^{-9} \text{ yr}$
 - ► Three-neutrino decay $(v_i \rightarrow v_i + v_k + \overline{v_k})$: $\tau > 10^{55} (m_i/\text{eV})^{-5} \text{ yr}$

► BSM decays may have significantly higher rates: $v_i \rightarrow v_i + \varphi$

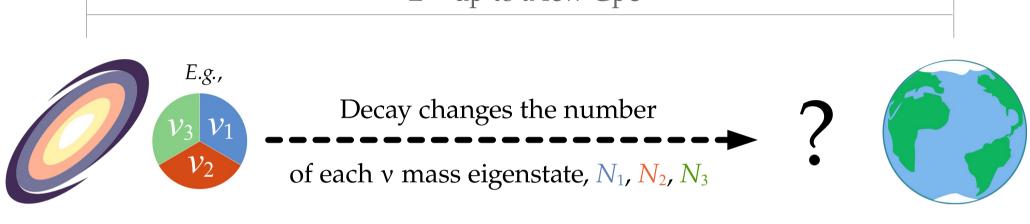
▶ We work in a model-independent way: the nature of φ is unimportant if it is invisible to neutrino detectors

Are neutrinos forever?

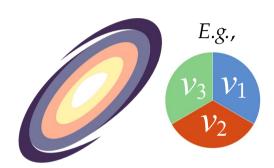
- ▶ In the Standard Model (vSM), neutrinos are essentially stable ($\tau > 10^{36}$ yr):
 - ► One-photon decay $(v_i \rightarrow v_j + \gamma)$: $\tau > 10^{36} (m_i/\text{eV})^{-5} \text{ yr}$
 - Two-photon decay $(v_i \rightarrow v_j + \gamma)$. $\tau > 10^{-7} (m_i / \text{eV})^{-9} \text{ yr}$
 - ► Three-neutrino decay $(v_i \rightarrow v_j + v_k + \overline{v_k})$: $\tau > 10^{55} (m_i/\text{eV})^{-5} \text{ yr}$

» Age of Universe (~ 14.5 Gyr)

- ► BSM decays may have significantly higher rates: $v_i \rightarrow v_j + \phi$ Nambu-Goldstone boson of a broken symmetry
- We work in a model-independent way: the nature of φ is unimportant if it is invisible to neutrino detectors



The flux of v_i is attenuated by $\exp[-(L/E) \cdot (m_i/\tau_i)]$ Mass of v_i Lifetime of v_i



Decay changes the number

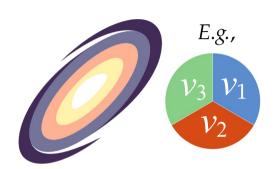
of each v mass eigenstate, N_1 , N_2 , N_3



Only sensitive to their ratio

The flux of v_i is attenuated by $\exp[-(L/E) \cdot (m_i/\tau_i)]$

Mass of v_i Lifetime of v_i



Decay changes the number

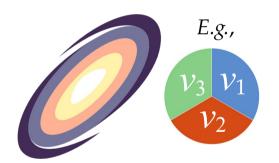
of each v mass eigenstate, N_1 , N_2 , N_3



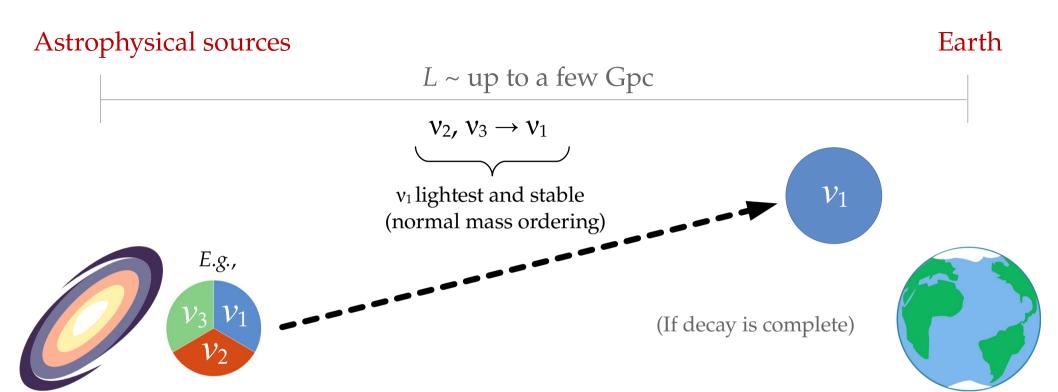
Lower-*E* v are longer-lived...

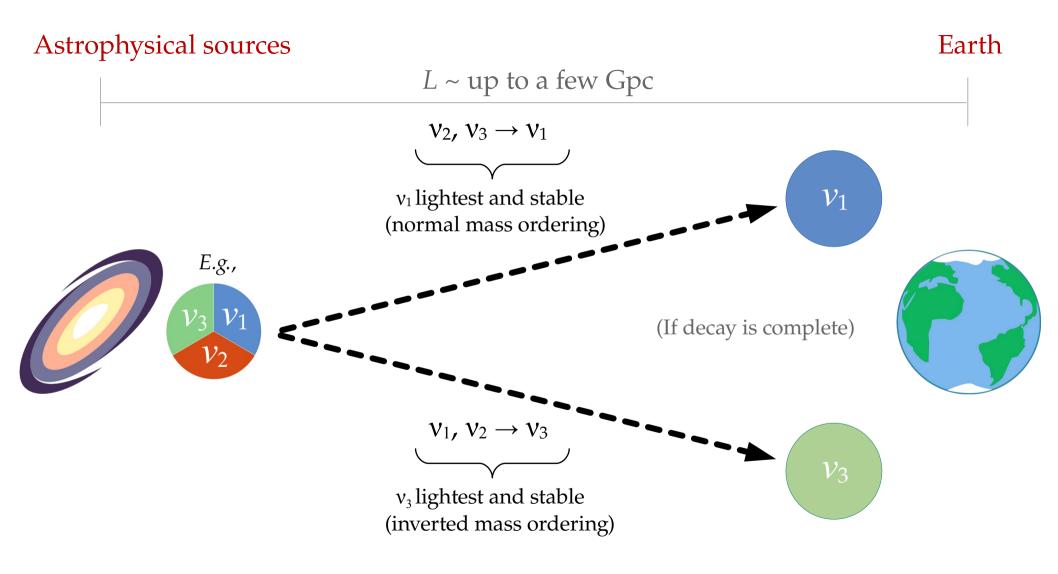
The flux of v_i is attenuated by $\exp[-(L/E) \cdot (m_i/\tau_i)]$

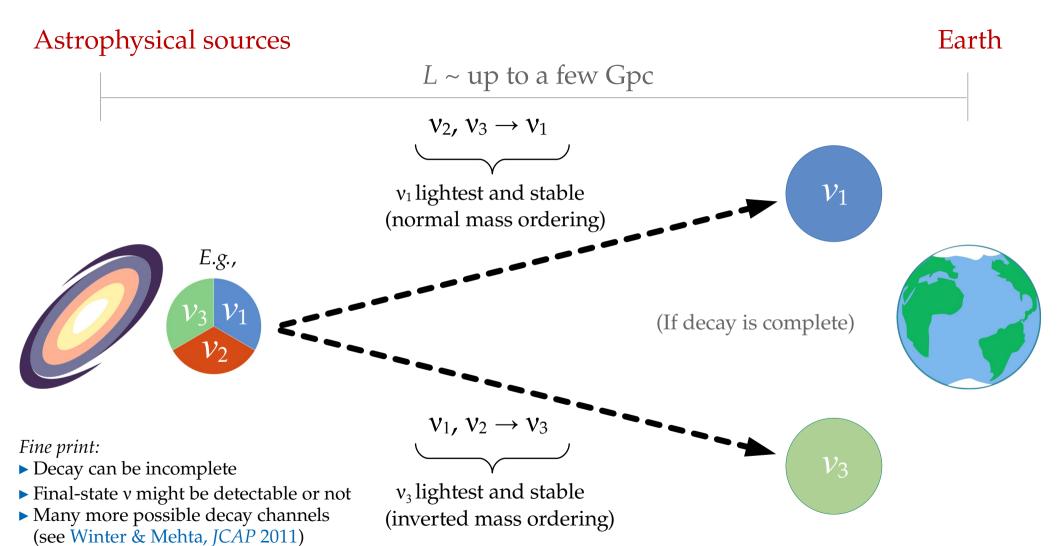
... but v that travel longer *L* are more attenuated!

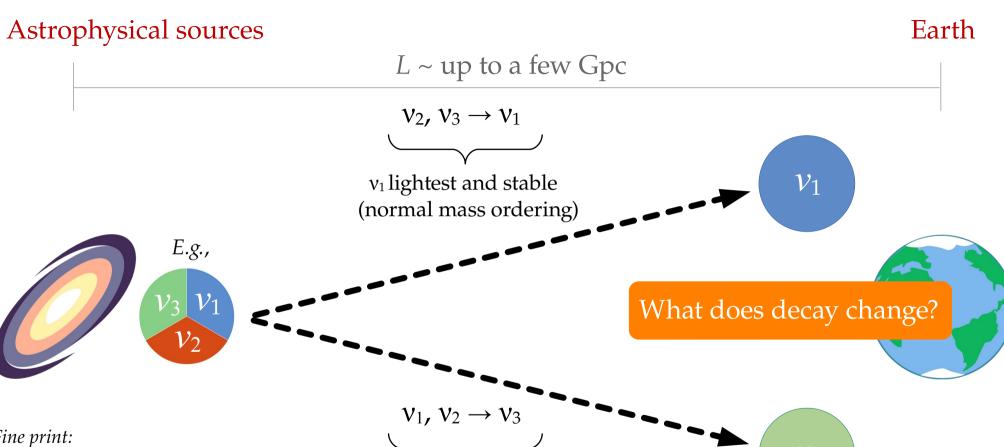












Fine print:

- ▶ Decay can be incomplete
- ▶ Final-state v might be detectable or not
- ▶ Many more possible decay channels (see Winter & Mehta, JCAP 2011)

$$v_3$$
 lightest and stable

(inverted mass ordering)

Flavor composition Spectrum shape Event rate

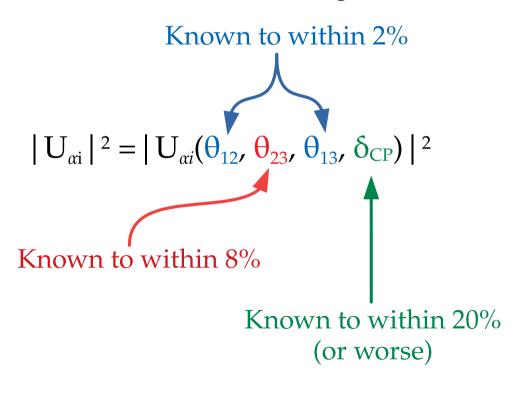
Flavor composition Spectrum shape

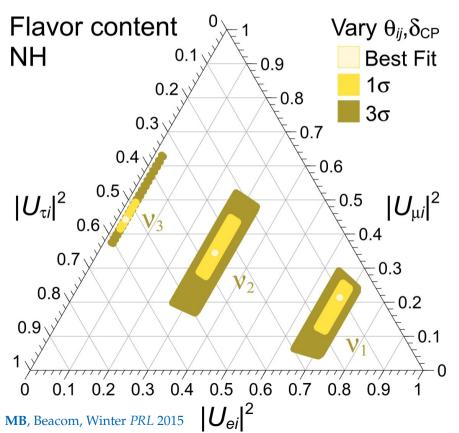


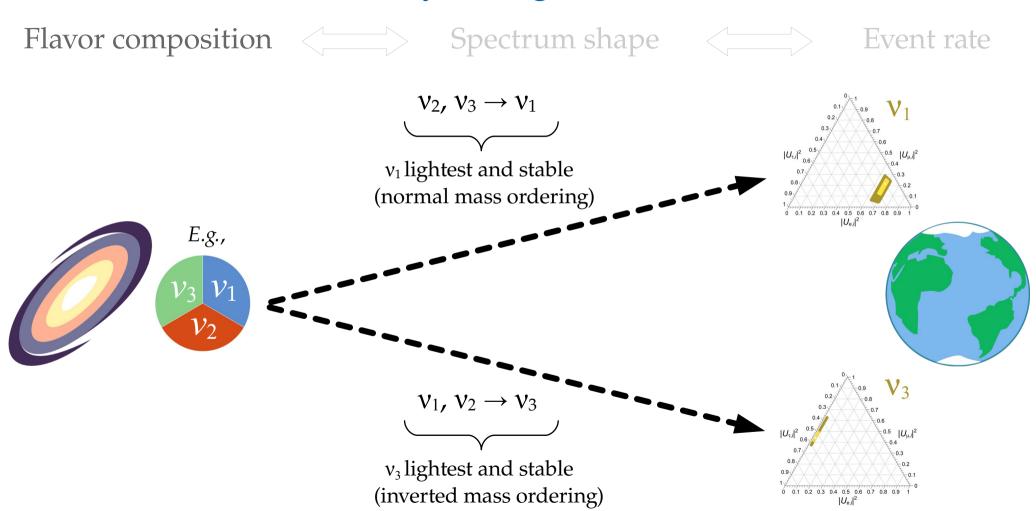


Event rate

Flavor content of mass eigenstates:





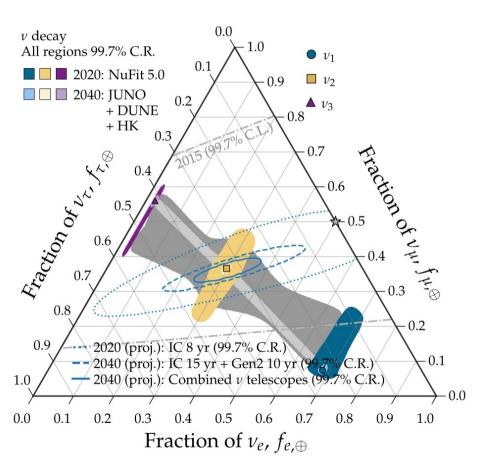


See also: Beacom et al., PRL 2002 / Baerwald, MB, Winter, JCAP 2012 / MB, Beacom, Murase, PRD 2017 / Rasmussen et al., PRD 2017 / Denton & Tamborra, PRL 2018 / Abdullahi & Denton, PRD 2020 / MB, 2004.06844

Flavor composition







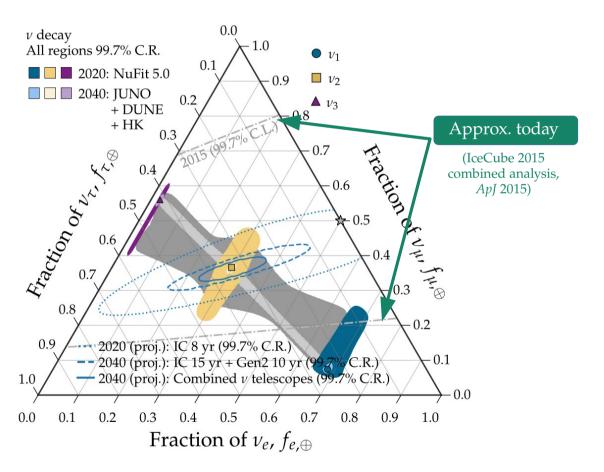
See also: Beacom et al., PRL 2002 / Baerwald, MB, Winter, ICAP 2012 / MB, Beacom, Murase, PRD 2017 / Rasmussen et al., PRD 2017 / Denton & Tamborra, PRL 2018 / Abdullahi & Denton, PRD 2020 / MB, 2004.06844





Spectrum shape





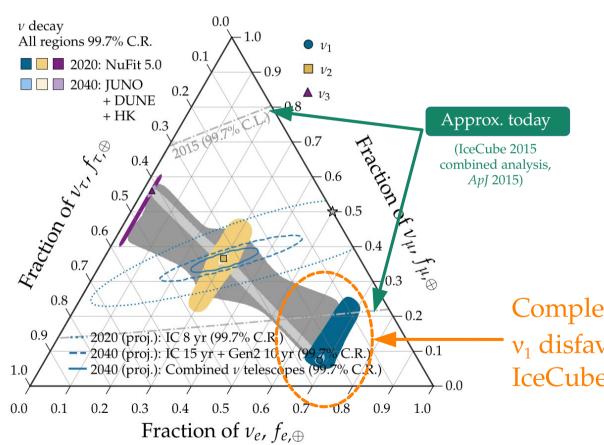
See also: Beacom et al., PRL 2002 / Baerwald, MB, Winter, JCAP 2012 / MB, Beacom, Murase, PRD 2017 / Rasmussen et al., PRD 2017 / Denton & Tamborra, PRL 2018 / Abdullahi & Denton, PRD 2020 / MB, 2004.06844



Spectrum shape



Event rate



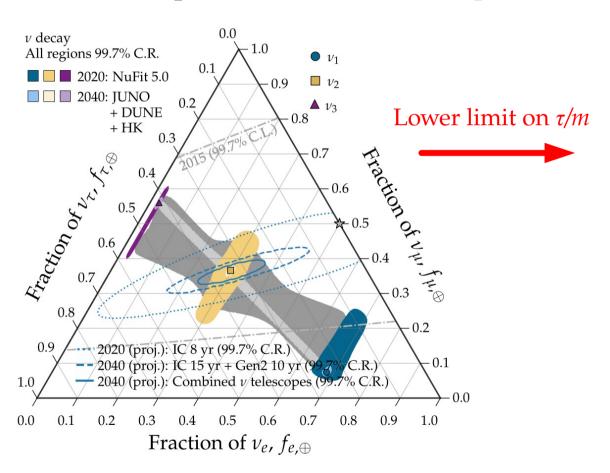
Complete decay into v_1 disfavored by 2015 IceCube flavor measurement

See also: Beacom et al., PRL 2002 / Baerwald, MB, Winter, JCAP 2012 / MB, Beacom, Murase, PRD 2017 / Rasmussen et al., PRD 2017 / Denton & Tamborra, PRL 2018 / Abdullahi & Denton, PRD 2020 / MB, 2004.06844



Spectrum shape





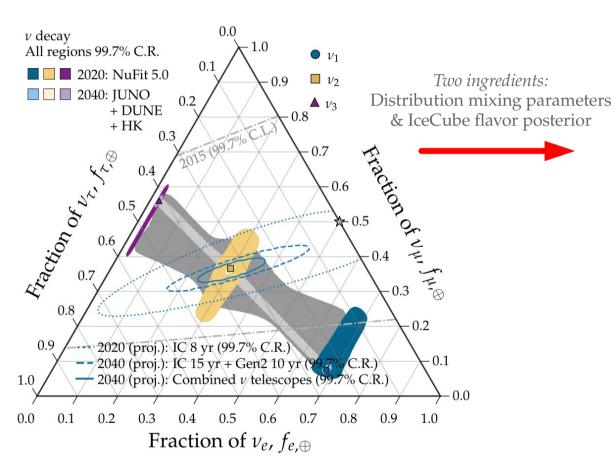
See also: Beacom et al., PRL 2002 / Baerwald, MB, Winter, JCAP 2012 / MB, Beacom, Murase, PRD 2017 / Rasmussen et al., PRD 2017 / Denton & Tamborra, PRL 2018 / Abdullahi & Denton, PRD 2020 / MB, 2004.06844





Spectrum shape





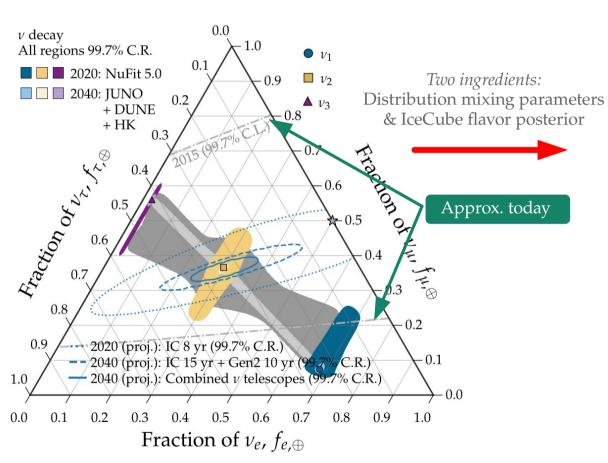
See also: Beacom et al., PRL 2002 / Baerwald, MB, Winter, ICAP 2012 / MB, Beacom, Murase, PRD 2017 / Rasmussen et al., PRD 2017 / Denton & Tamborra, PRL 2018 / Abdullahi & Denton, PRD 2020 / MB, 2004.06844





Spectrum shape





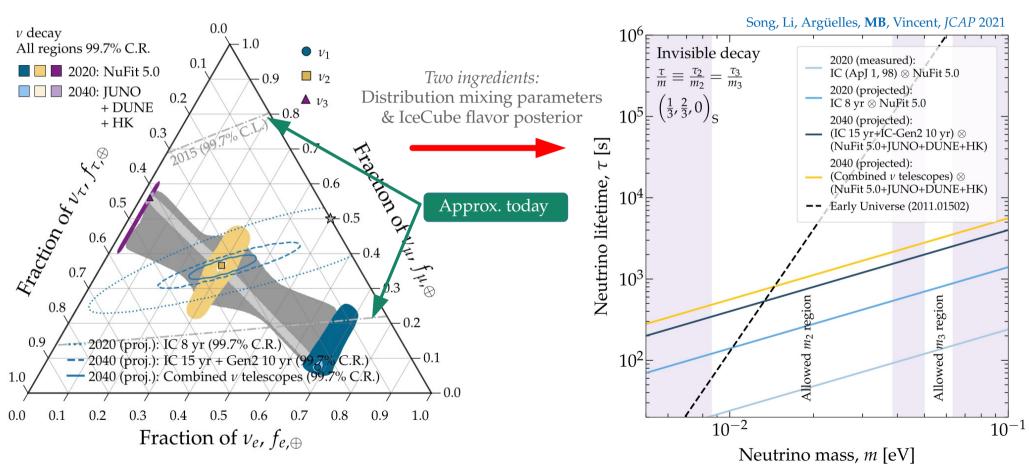
See also: Beacom et al., PRL 2002 / Baerwald, MB, Winter, JCAP 2012 / MB, Beacom, Murase, PRD 2017 / Rasmussen et al., PRD 2017 / Denton & Tamborra, PRL 2018 / Abdullahi & Denton, PRD 2020 / MB, 2004.06844





Spectrum shape





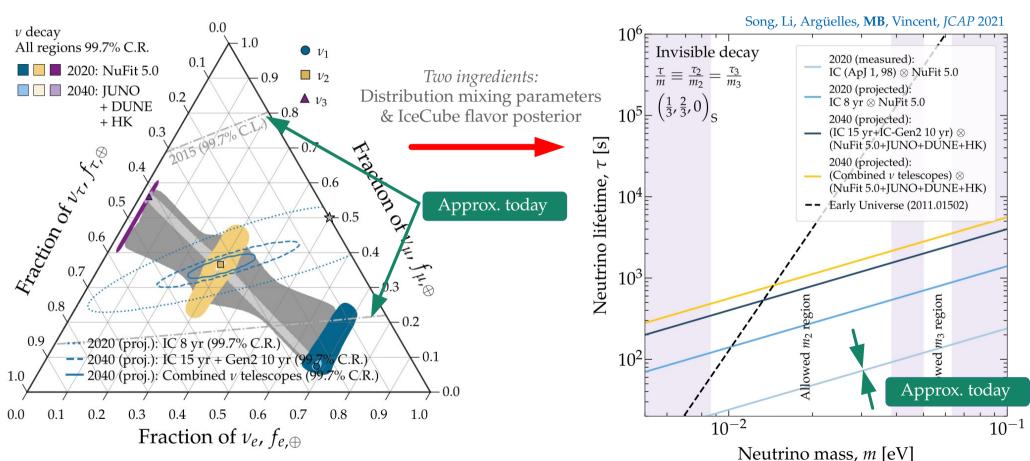
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Spectrum shape





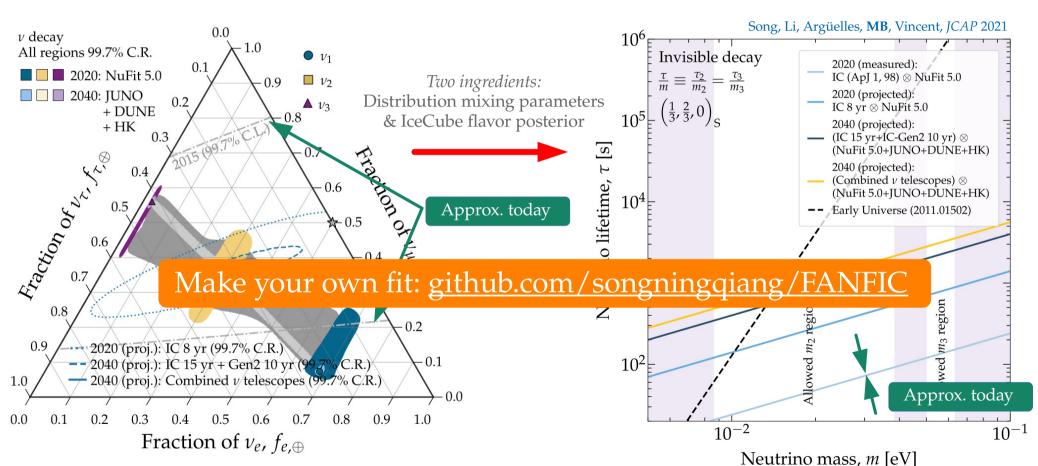
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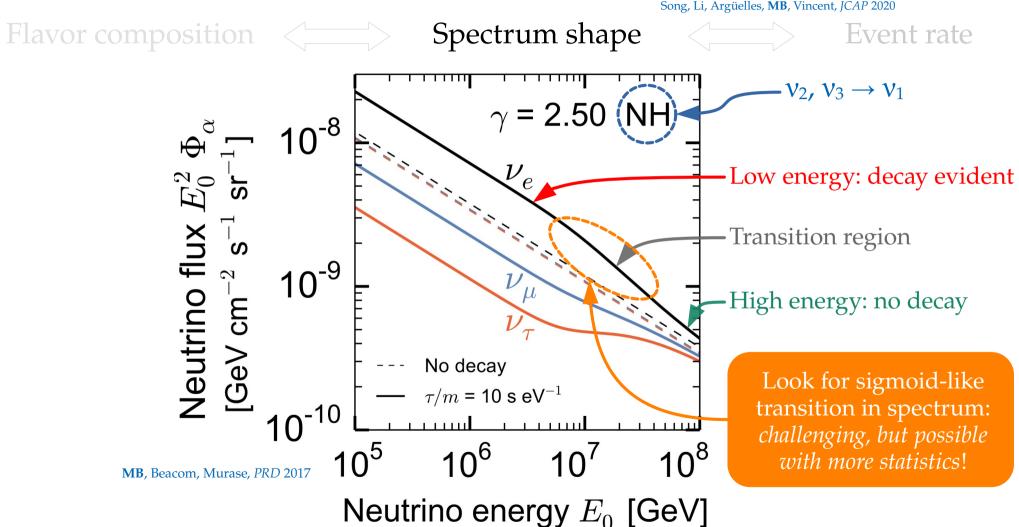


Spectrum shape





See also: Beacom et al., PRL 2002 / Baerwald, MB, Winter, JCAP 2012 / Rasmussen et al., PRD 2017 / Denton & Tamborra, PRL 2018 / Abdullahi & Denton, PRD 2020 / MB, 2004.06844 / Song, Li, Argüelles, MB, Vincent, JCAP 2020

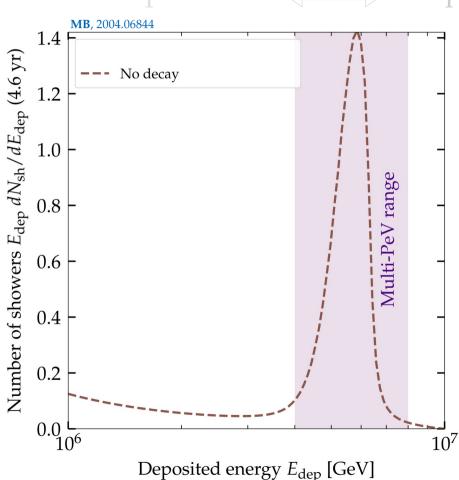


See also: Beacom *et al.*, *PRL* 2002 / Baerwald, **MB**, Winter, *JCAP* 2012 / **MB**, Beacom, Murase, *PRD* 2017 / Rasmussen *et al.*, *PRD* 2017 / Denton & Tamborra, *PRL* 2018 / Abdullahi & Denton, *PRD* 2020 / Song, Li, Argüelles, **MB**, Vincent, *JCAP* 2020









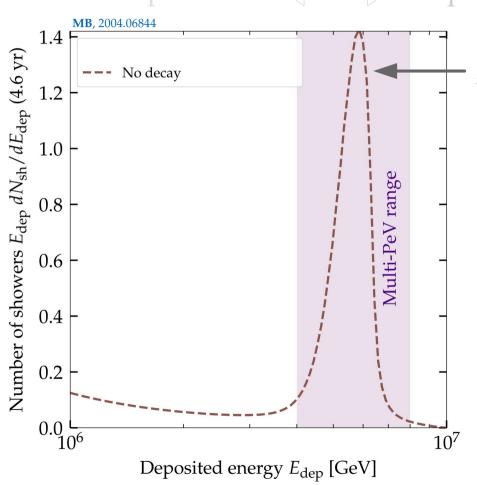
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Event rate

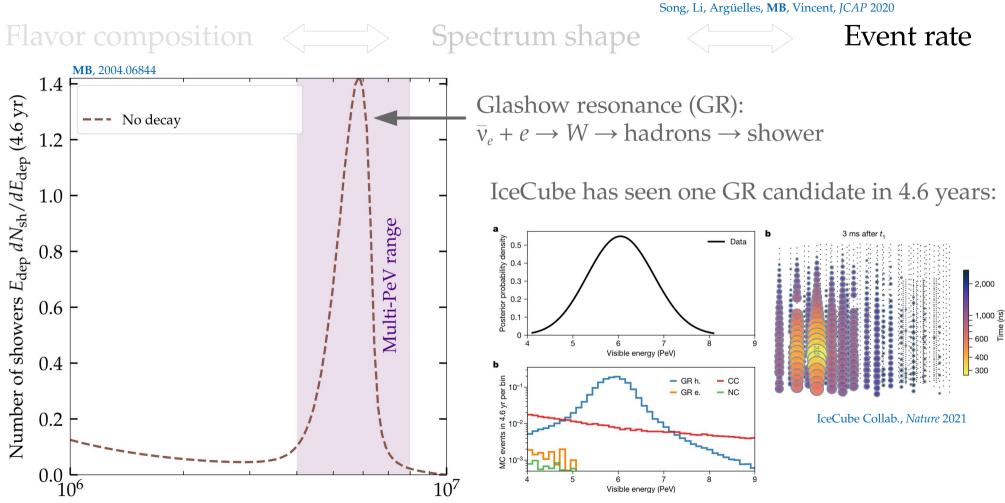


Glashow resonance (GR):

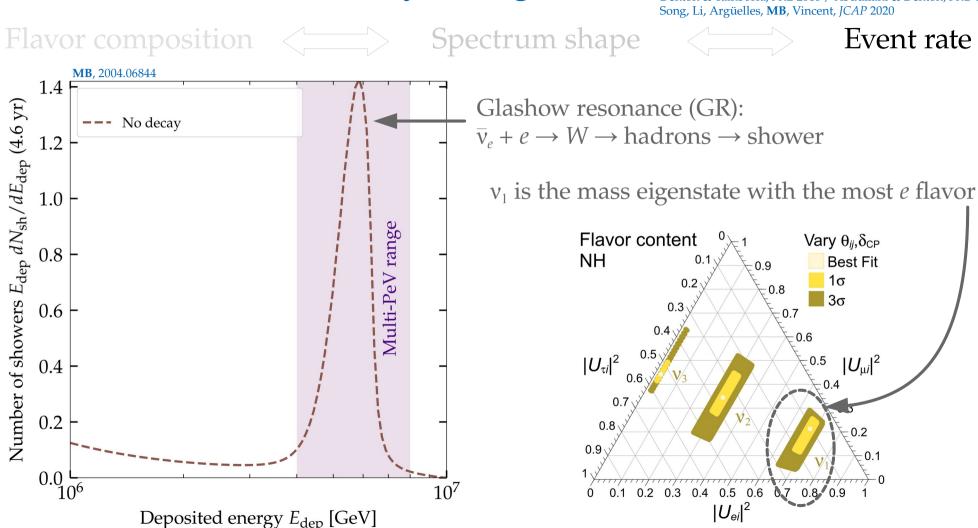
 $\bar{v}_e + e \rightarrow W \rightarrow \text{hadrons} \rightarrow \text{shower}$

Deposited energy E_{dep} [GeV]

See also: Beacom *et al.*, *PRL* 2002 / Baerwald, **MB**, Winter, *JCAP* 2012 / **MB**, Beacom, Murase, *PRD* 2017 / Rasmussen *et al.*, *PRD* 2017 / Denton & Tamborra, *PRL* 2018 / Abdullahi & Denton, *PRD* 2020 / Song, Li, Argüelles, **MB**, Vincent, *JCAP* 2020



See also: Beacom *et al.*, *PRL* 2002 / Baerwald, **MB**, Winter, *JCAP* 2012 / **MB**, Beacom, Murase, *PRD* 2017 / Rasmussen *et al.*, *PRD* 2017 / Denton & Tamborra, *PRL* 2018 / Abdullahi & Denton, *PRD* 2020 / Song, Li, Argüelles, **MB**, Vincent, *JCAP* 2020

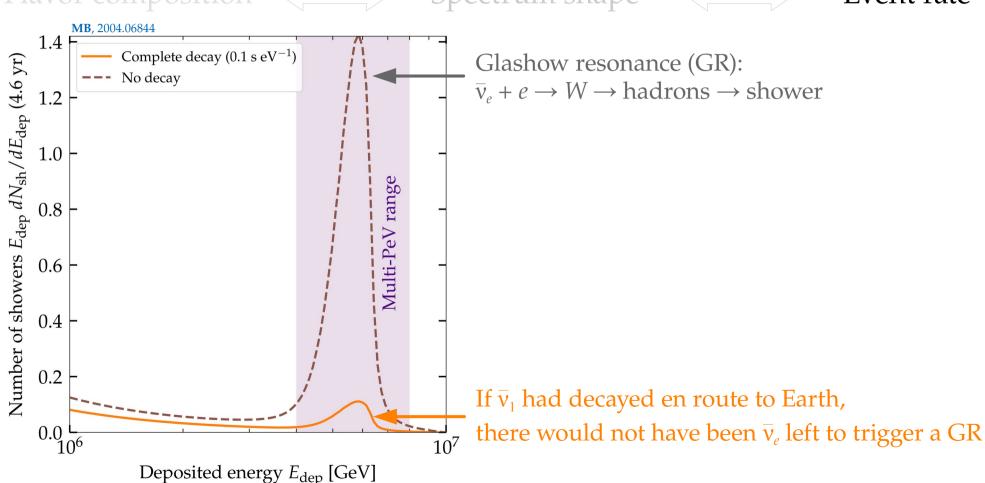


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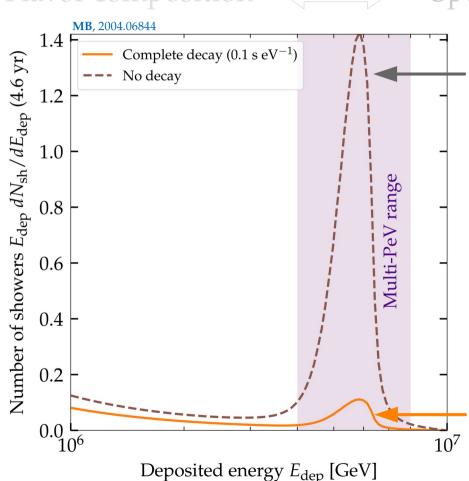
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Event rate



Glashow resonance (GR): $\bar{v}_e + e \rightarrow W \rightarrow \text{hadrons} \rightarrow \text{shower}$

So by having observed 1 GR event we can place a *lower* limit on the lifetime of \bar{v}_1 (= v_1)



If \bar{v}_1 had decayed en route to Earth, there would not have been \bar{v}_e left to trigger a GR

See also: Beacom *et al.*, *PRL* 2002 / Baerwald, **MB**, Winter, *JCAP* 2012 / **MB**, Beacom, Murase, *PRD* 2017 / Rasmussen *et al.*, *PRD* 2017 / Denton & Tamborra, *PRL* 2018 / Abdullahi & Denton, *PRD* 2020 / Song, Li, Argüelles, **MB**, Vincent, *JCAP* 2020

Flavor composition

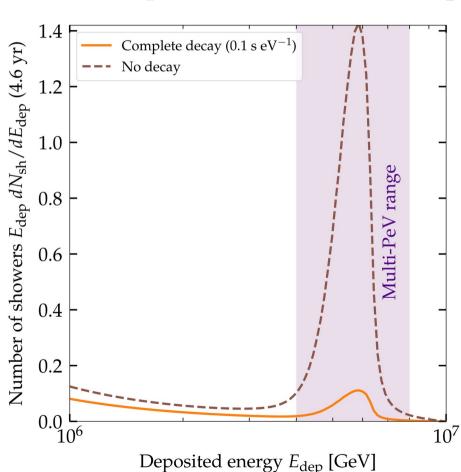


Spectrum shape



Event rate

MB, 2004.06844



See also: Beacom *et al.*, *PRL* 2002 / Baerwald, **MB**, Winter, *JCAP* 2012 / **MB**, Beacom, Murase, *PRD* 2017 / Rasmussen *et al.*, *PRD* 2017 / Denton & Tamborra, *PRL* 2018 / Abdullahi & Denton, *PRD* 2020 / Song, Li, Argüelles, **MB**, Vincent, *JCAP* 2020

Flavor composition

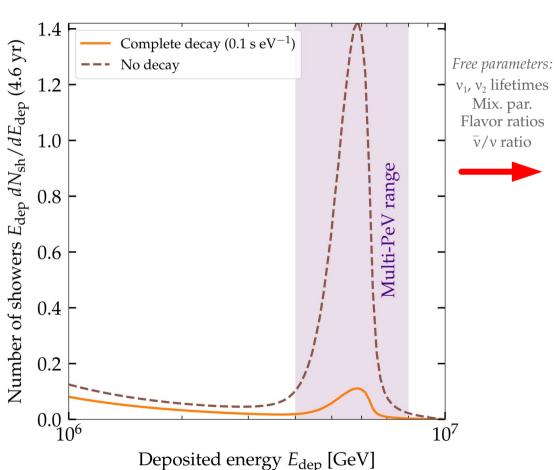


Spectrum shape

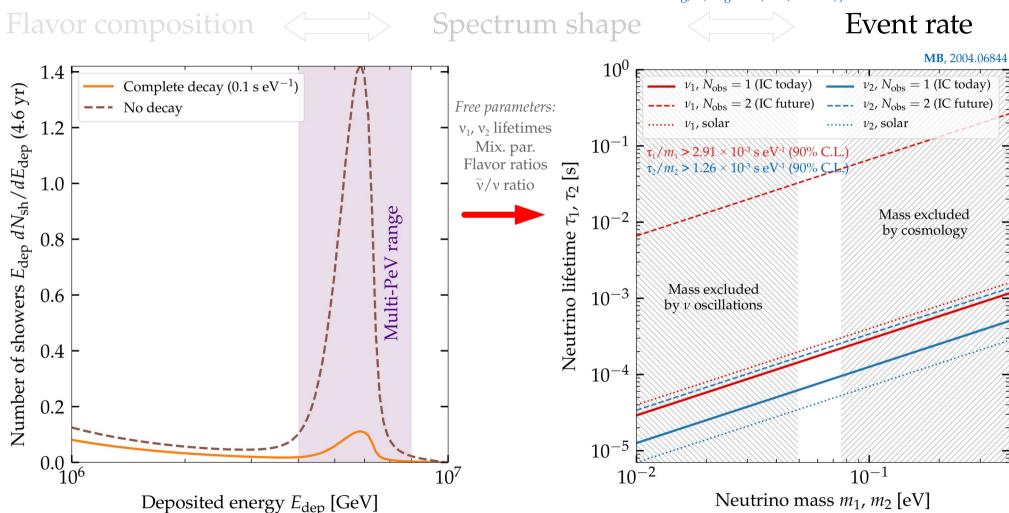


Event rate

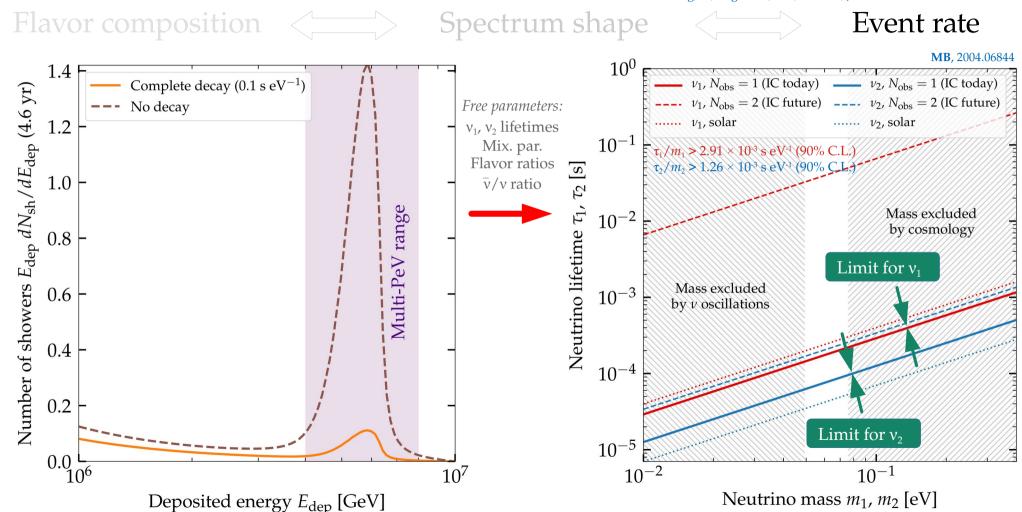
MB, 2004.06844



See also: Beacom *et al.*, *PRL* 2002 / Baerwald, **MB**, Winter, *JCAP* 2012 / **MB**, Beacom, Murase, *PRD* 2017 / Rasmussen *et al.*, *PRD* 2017 / Denton & Tamborra, *PRL* 2018 / Abdullahi & Denton, *PRD* 2020 / Song, Li, Argüelles, **MB**, Vincent, *JCAP* 2020



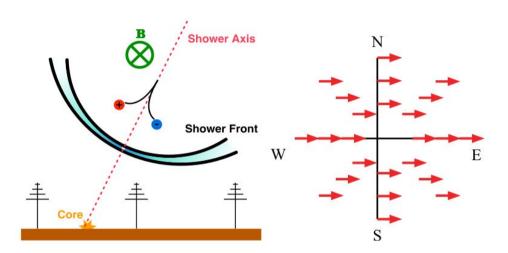
See also: Beacom *et al.*, *PRL* 2002 / Baerwald, **MB**, Winter, *JCAP* 2012 / **MB**, Beacom, Murase, *PRD* 2017 / Rasmussen *et al.*, *PRD* 2017 / Denton & Tamborra, *PRL* 2018 / Abdullahi & Denton, *PRD* 2020 / Song, Li, Argüelles, **MB**, Vincent, *JCAP* 2020



Neutrino radio-detection

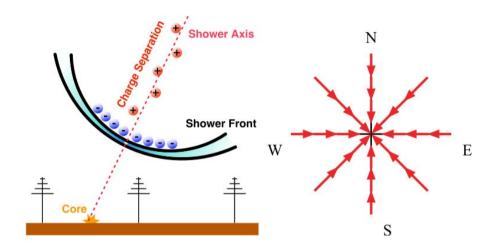
Radio emission: geomagnetic and Askaryan

Geomagnetic



- ► Time-varying transverse current
- ► Linearly polarized parallel to Lorentz force
- ▶ Dominant in air showers

Askaryan



- ► Time-varying negative-charge ~20% excess
- ► Linearly polarized towards axis
- ► Sub-dominant in air showers

Radio emission: geomagnetic and Askaryan

