

Measuring the neutrino-nucleon cross section at ultra-high energies: *detailed forecasts for IceCube-Gen2*

Mauricio Bustamante

Niels Bohr Institute, University of Copenhagen

In collaboration with Victor Valera & Christian Glaser
arXiv:2204.04237 (accepted in JHEP)

NPAC Seminar
June 09, 2022

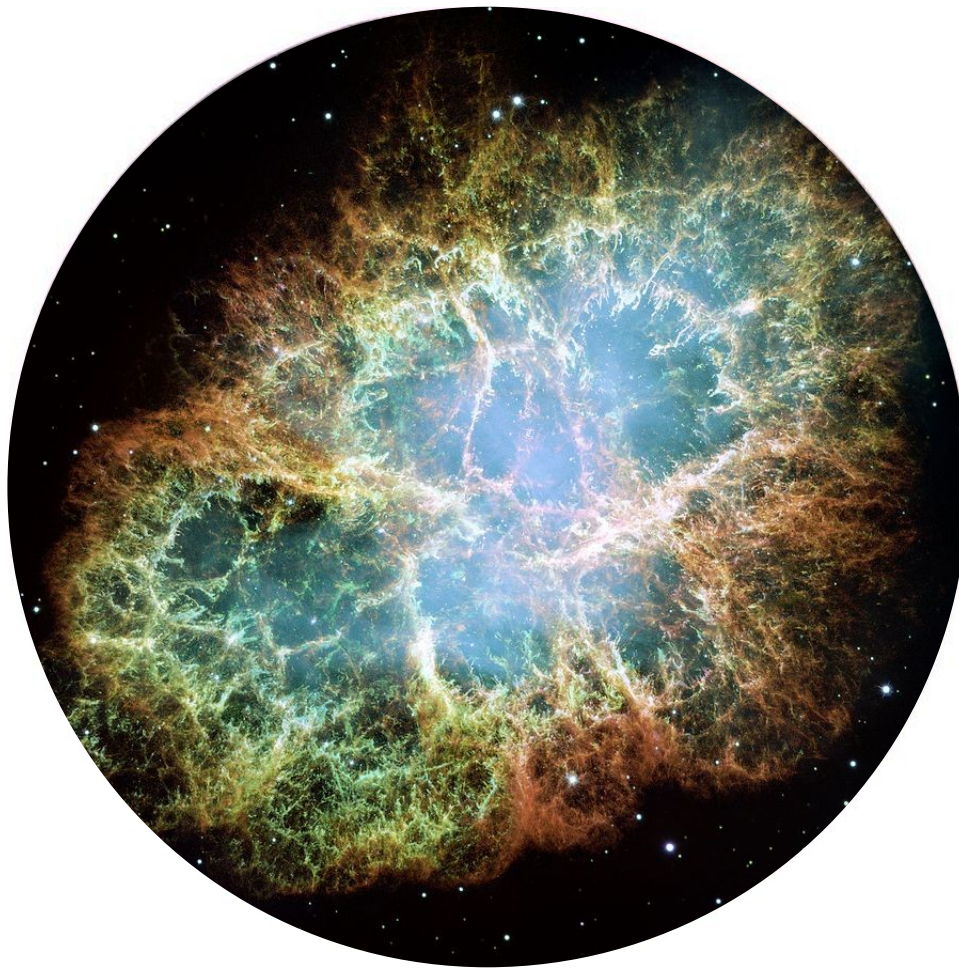
UNIVERSITY OF
COPENHAGEN

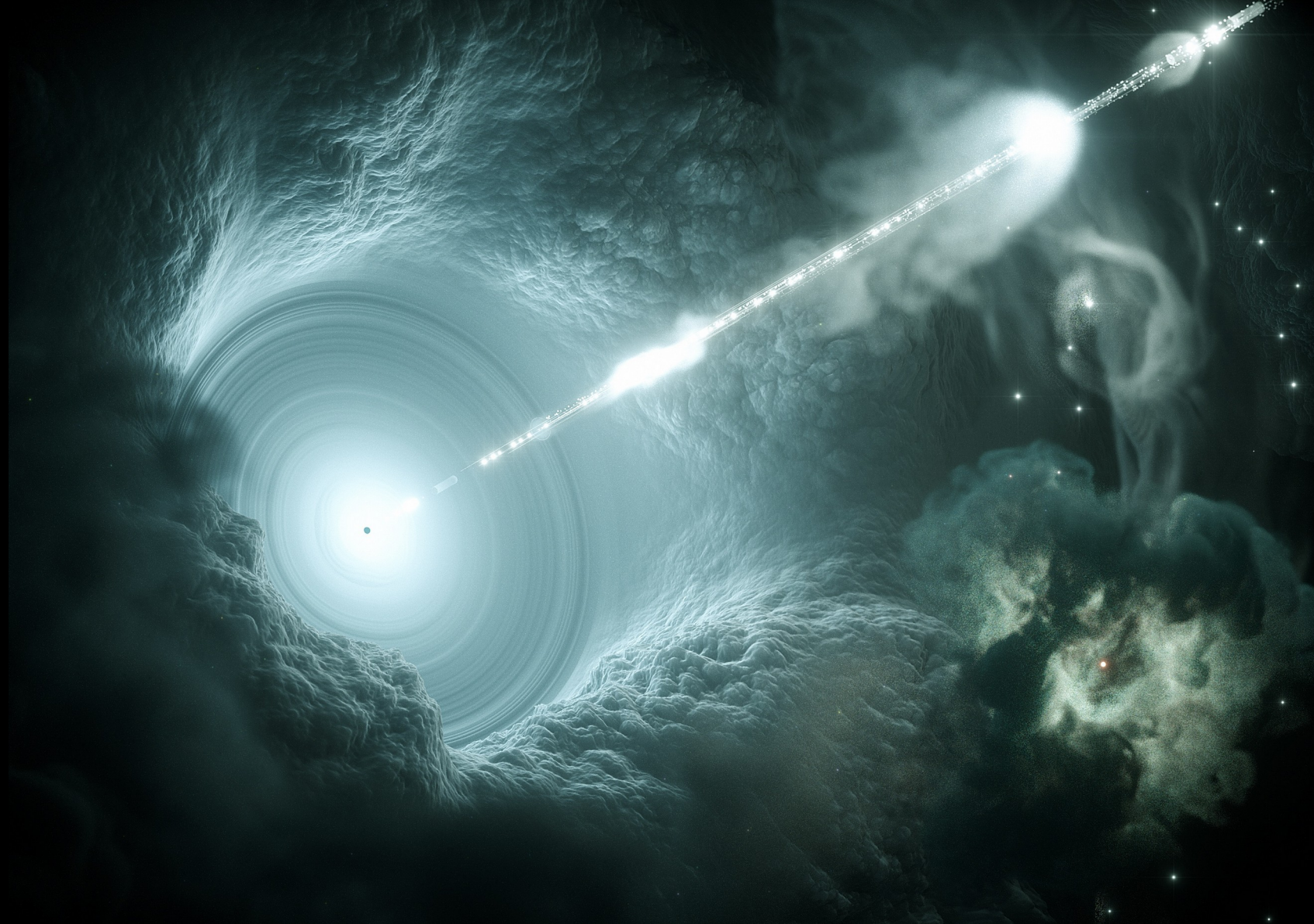


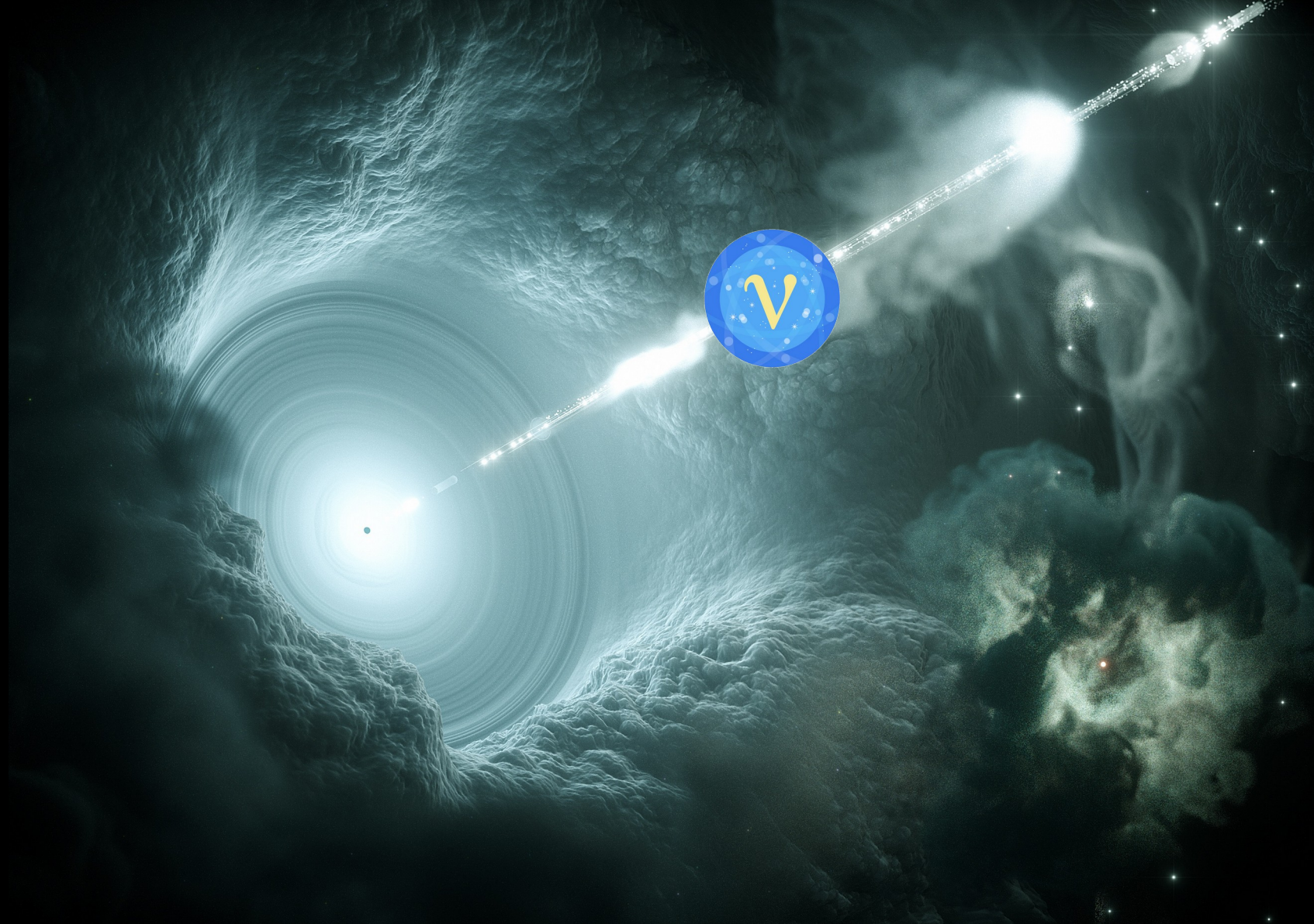
VILLUM FONDEN



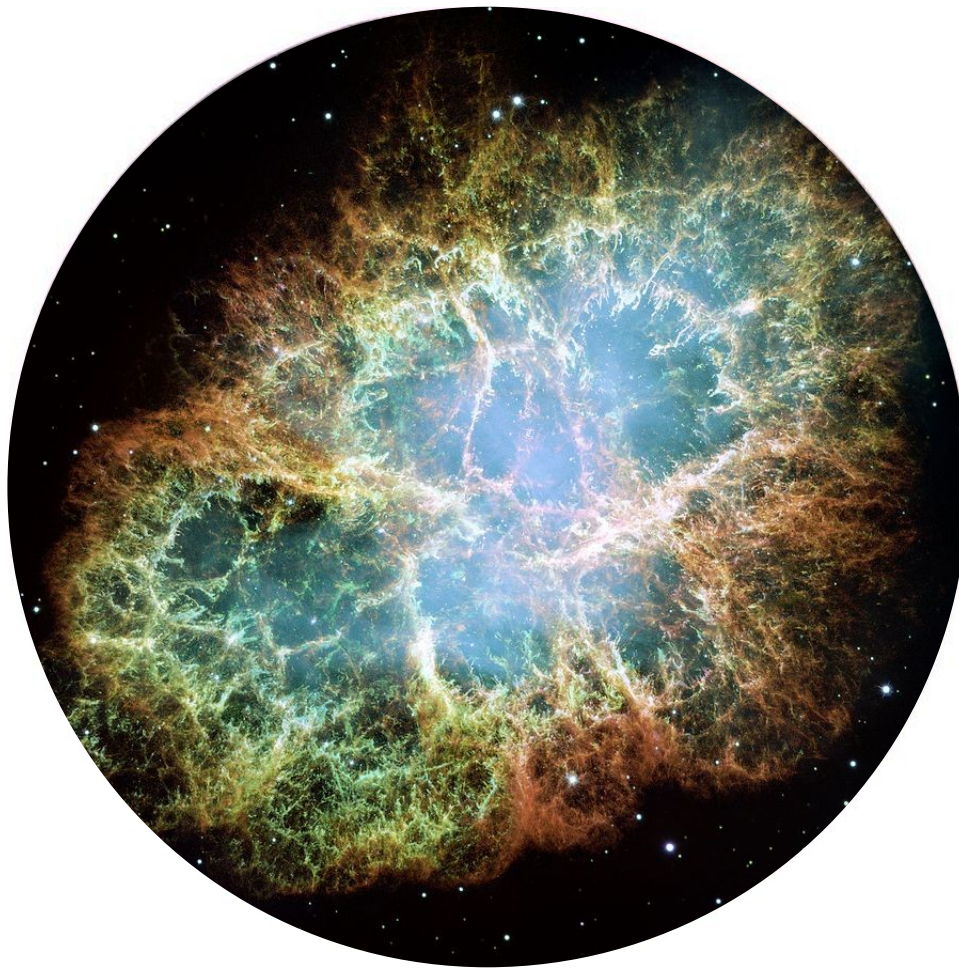


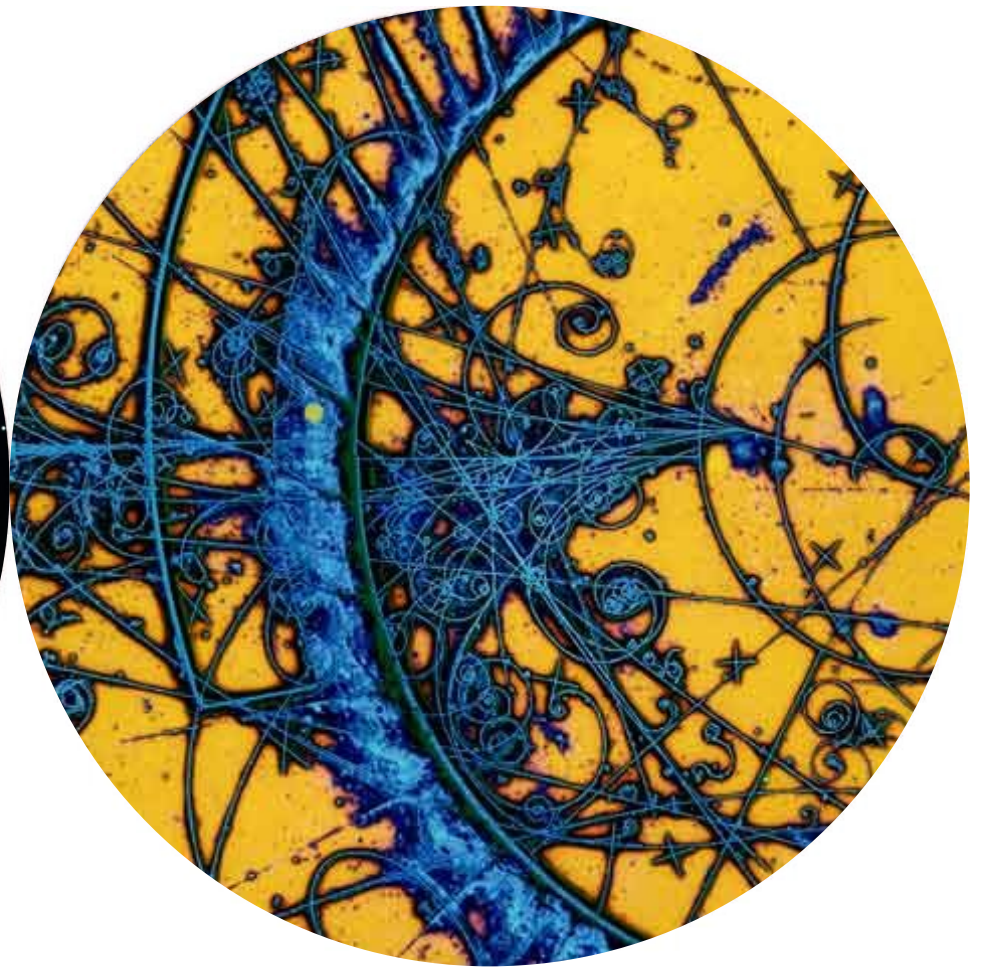
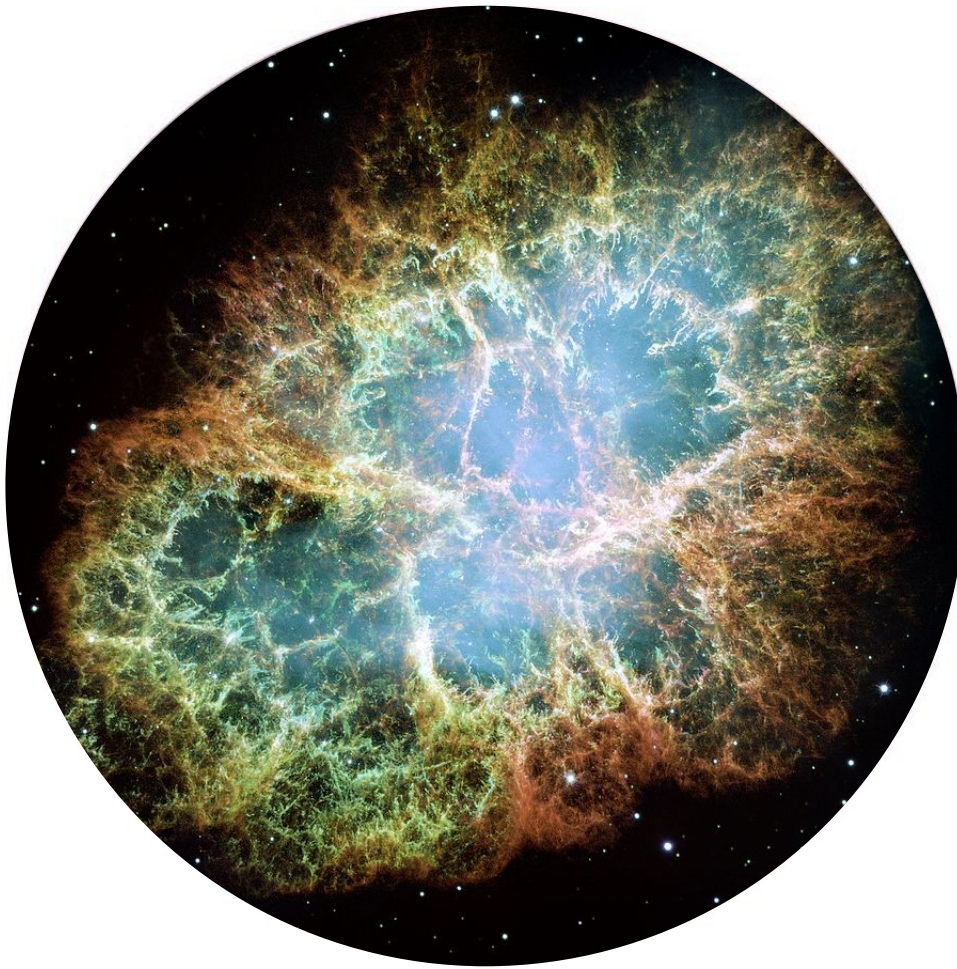




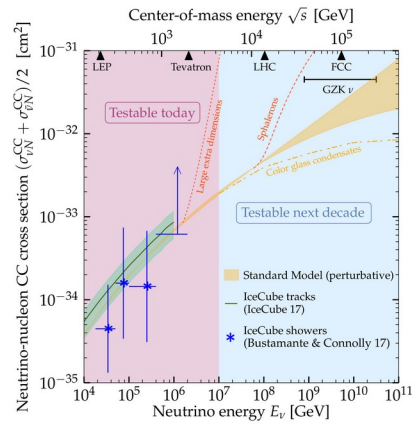






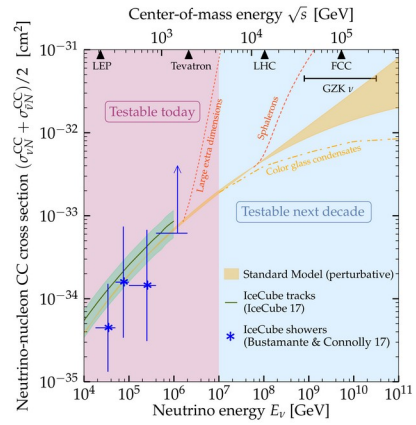


TeV–EeV ν cross sections



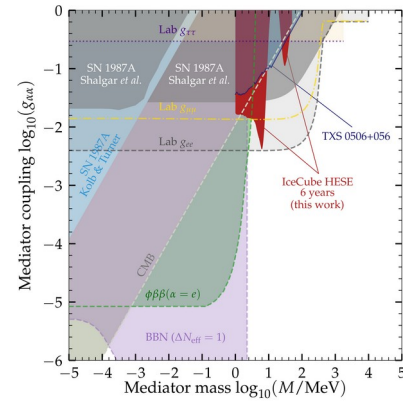
MB & Connolly, *PRL* 2019

TeV–EeV ν cross sections



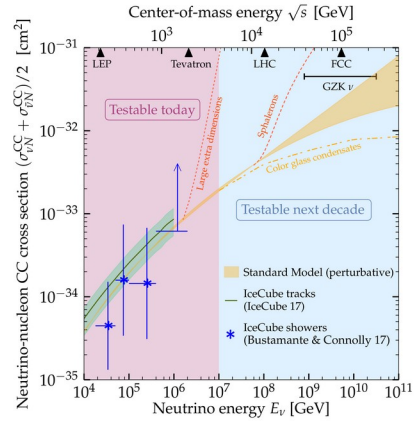
MB & Connolly, *PRL* 2019

ν self-interactions



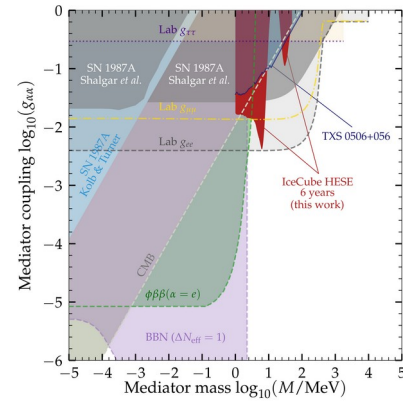
MB, Rosenström, Shalgar, Tamborra, *PRD* 2020

TeV–EeV ν cross sections



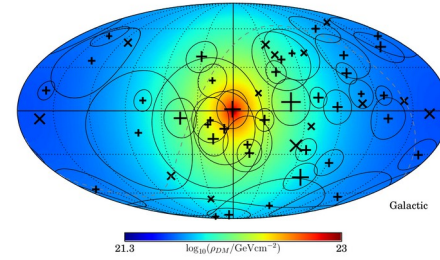
MB & Connolly, *PRL* 2019

ν self-interactions



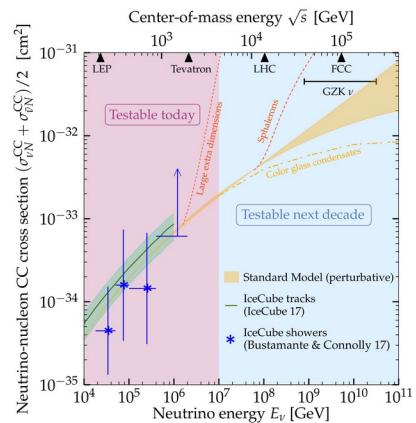
MB, Rosenström, Shalgar, Tamborra, *PRD* 2020

ν scattering on Galactic DM



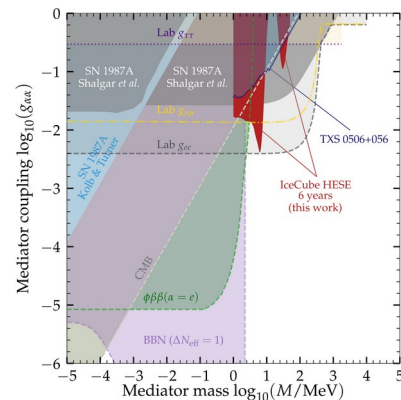
Argüelles, Kheirandish, Vincent, *PRL* 2017

TeV–EeV ν cross sections



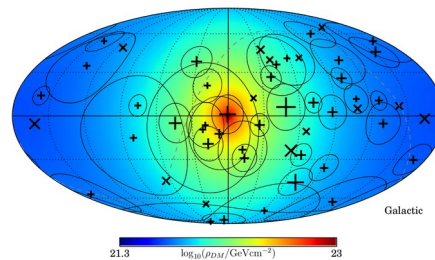
MB & Connolly, PRL 2019

ν self-interactions



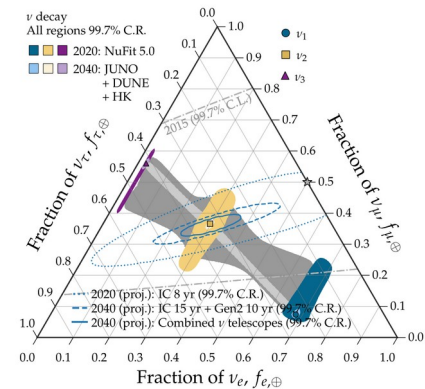
MB, Rosenström, Shalgar, Tamborra, PRD 2020

ν scattering on Galactic DM



Argüelles, Kheirandish, Vincent, PRL 2017

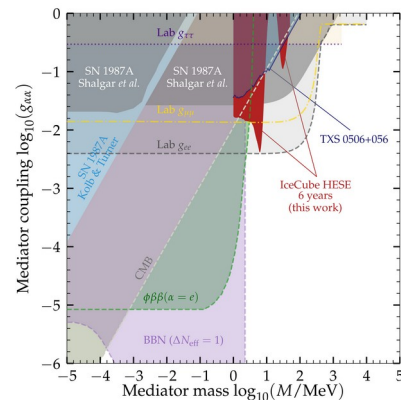
ν decay



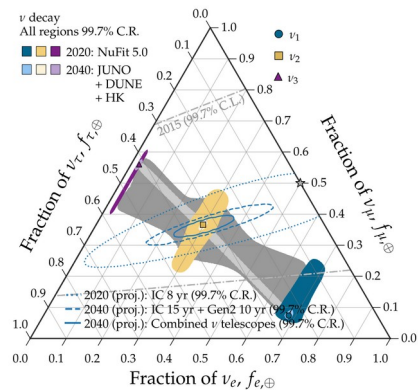
Song, Li, Argüelles, MB, Vincent, JCAP 2021

Figure 1 is a log-log plot showing the neutrino-nucleon CC cross section $(\sigma_{\nu N}^{CC} + \sigma_{\nu N}^{CC})/2$ [cm²] versus Neutrino energy E_ν [GeV]. The y-axis ranges from 10^{-35} to 10^{-31} , and the x-axis ranges from 10^4 to 10^{11} GeV. The plot is divided into regions for different physical processes: 'Testable today' (pink), 'Testable next decade' (blue), and 'Standard Model (perturbative)' (yellow). Key features include 'Large extra dimensions' (dashed red line), 'Spontaneous' (dashed orange line), and 'Color glass condensates' (dashed orange line). Experimental constraints are shown for LEP, Tevatron, LHC, FCC, and GZK. IceCube tracks (green line) and IceCube showers (blue stars) are also plotted.

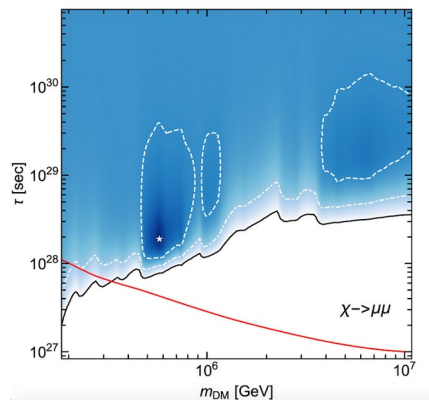
ν self-interactions



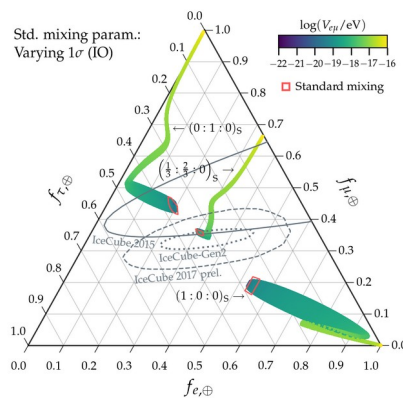
ν decay



Dark matter decay

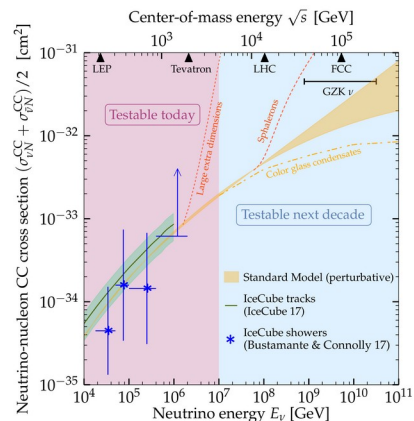


ν -electron interaction



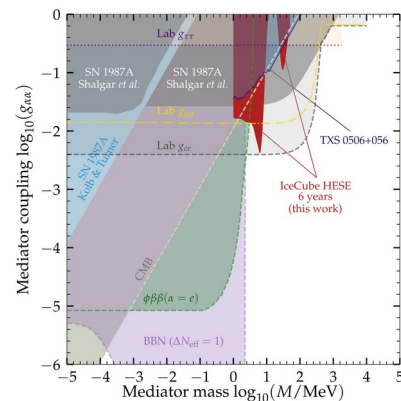
MB & Agarwalla, PRL 2019

TeV–EeV ν cross sections



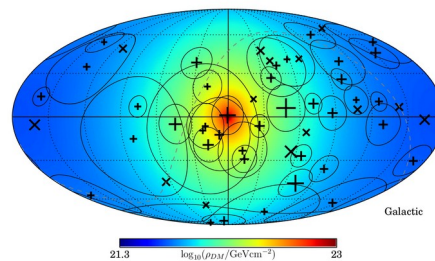
MB & Connolly, PRL 2019

ν self-interactions



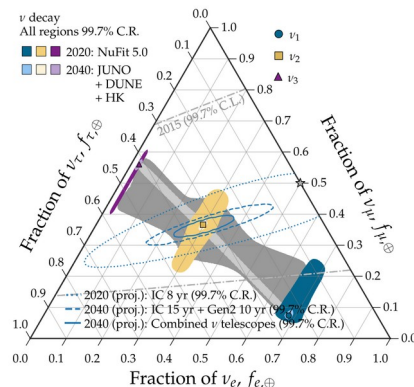
MB, Rosenström, Shalgar, Tamborra, PRD 2020

ν scattering on Galactic DM



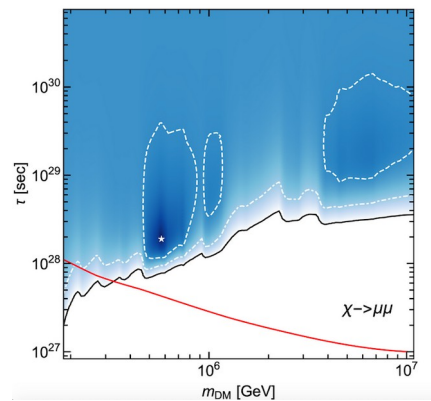
Argüelles, Kheirandish, Vincent, PRL 2017

ν decay



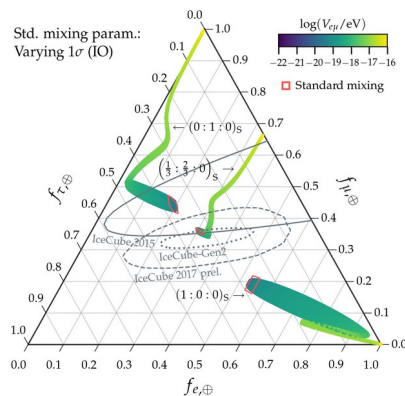
Song, Li, Argüelles, MB, Vincent, JCAP 2021

Dark matter decay



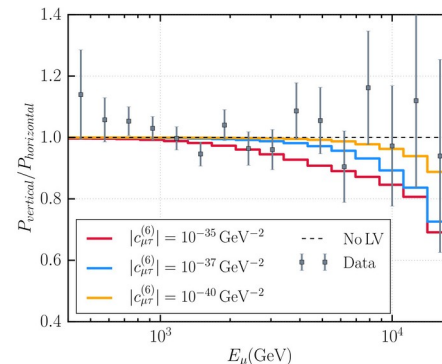
Chianese, Fiorillo, Miele, Morisi, Pisanti, JCAP 2019

ν -electron interaction



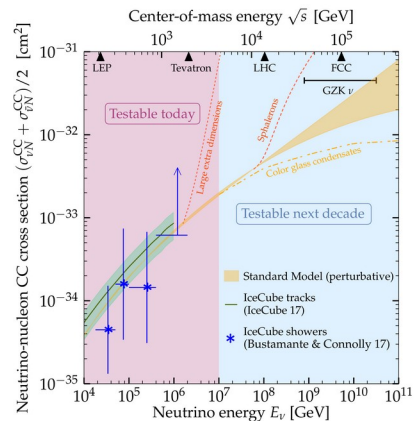
MB & Agarwalla, PRL 2019

Lorentz-invariance violation



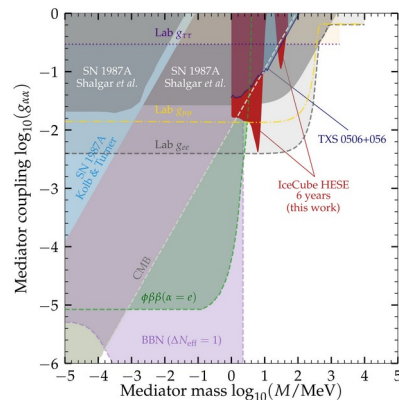
IceCube, Nature Phys. 2018

TeV–EeV ν cross sections



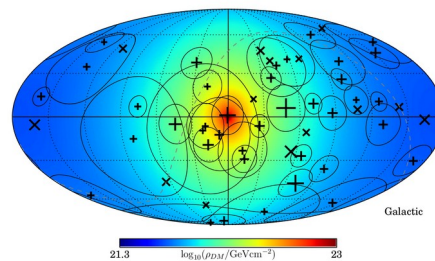
MB & Connolly, PRL 2019

ν self-interactions



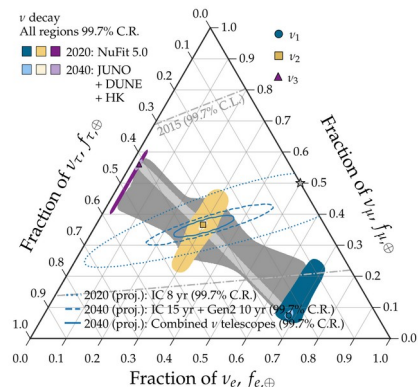
MB, Rosenström, Shalgar, Tamborra, PRD 2020

ν scattering on Galactic DM



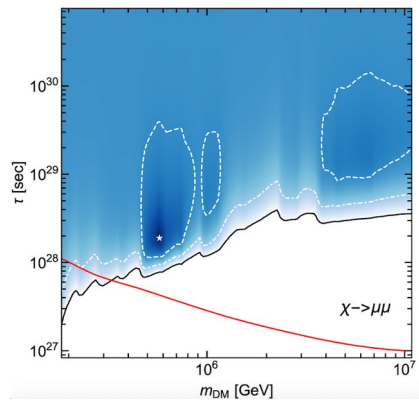
Argüelles, Kheirandish, Vincent, PRL 2017

ν decay



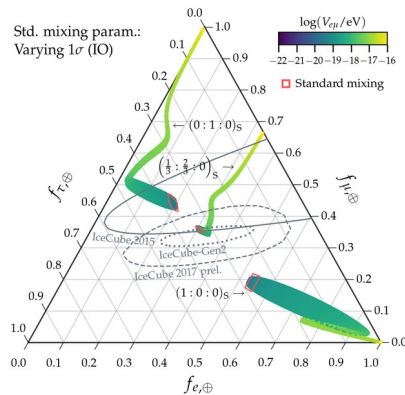
Song, Li, Argüelles, MB, Vincent, JCAP 2021

Dark matter decay



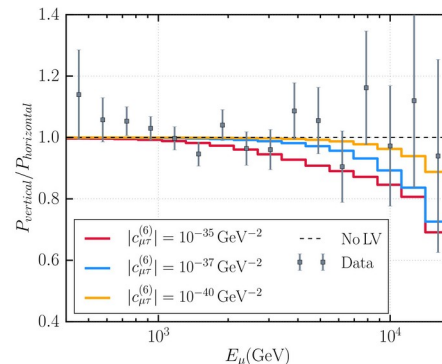
Chianese, Fiorillo, Miele, Morisi, Pisanti, JCAP 2019

ν -electron interaction



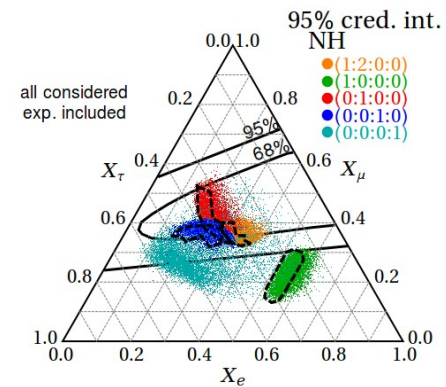
MB & Agarwalla, PRL 2019

Lorentz-invariance violation



IceCube, Nature Phys. 2018

Sterile neutrinos



Brdar, Kopp, Wang, JCAP 2017

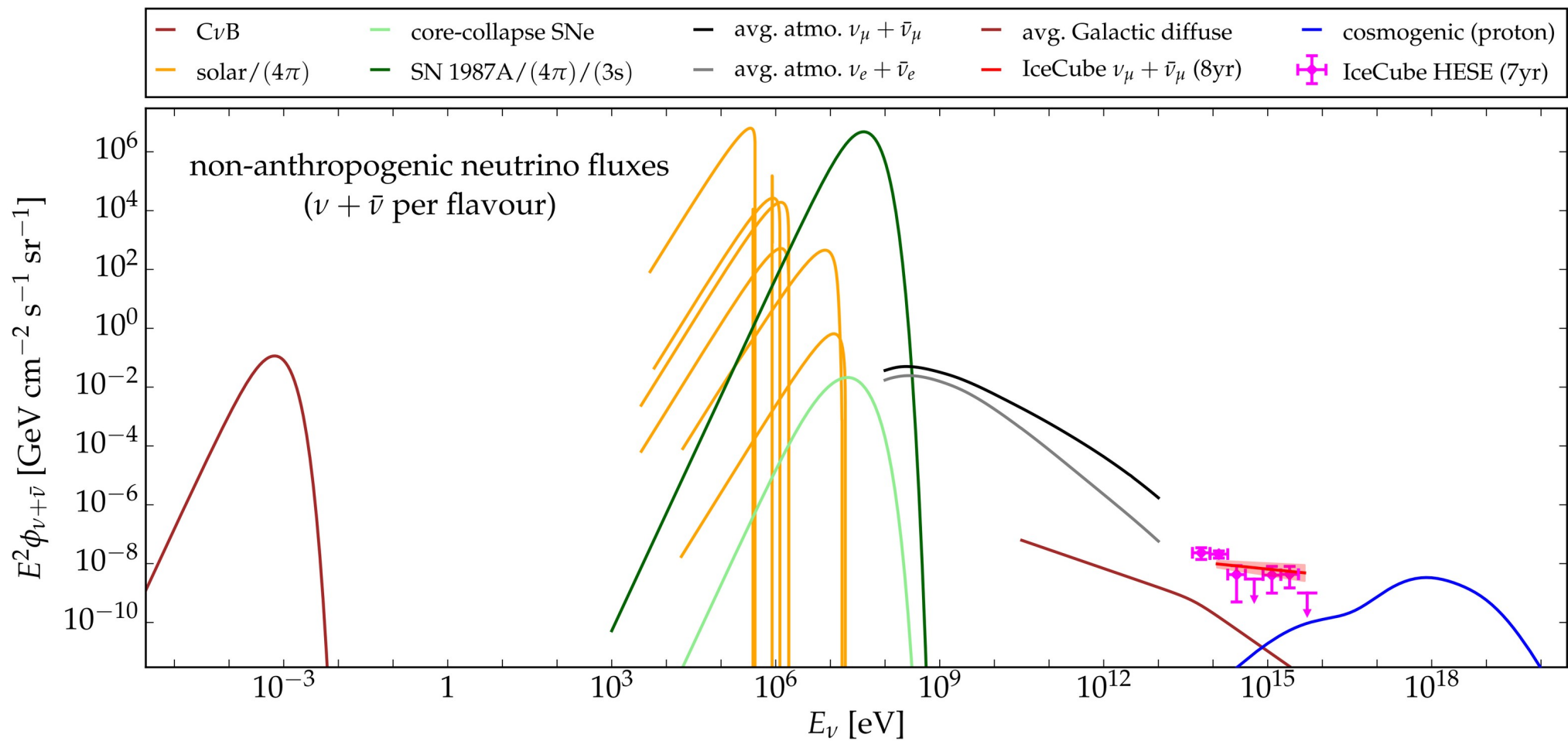


Figure courtesy of Markus Ahlers
Maoloud, De Wasseige, Ahlers, MB, Van Elewyck, PoS(ICRC2019), 1023

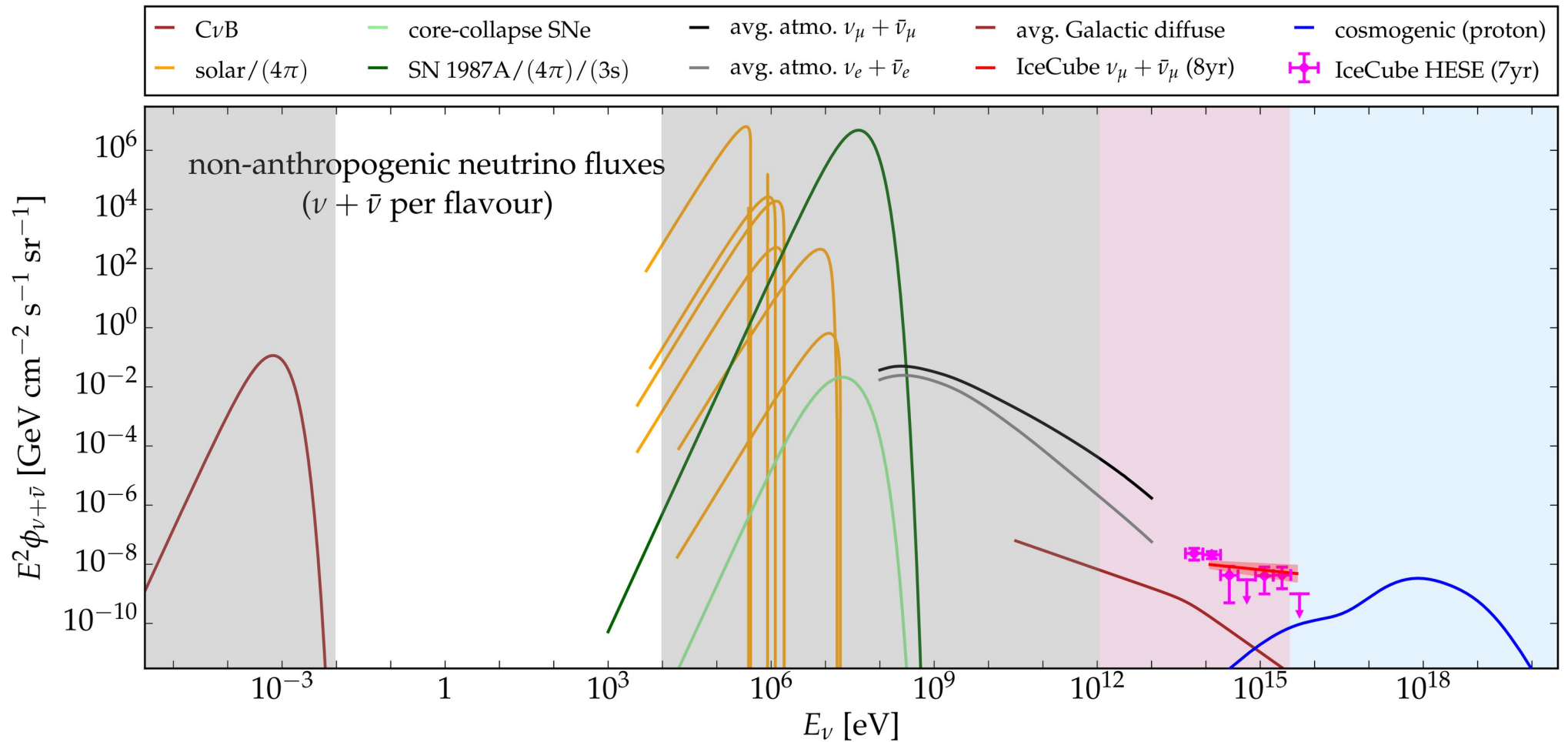


Figure courtesy of Markus Ahlers
 Maoloud, De Wasseige, Ahlers, MB, Van Elewyck, PoS(ICRC2019), 1023

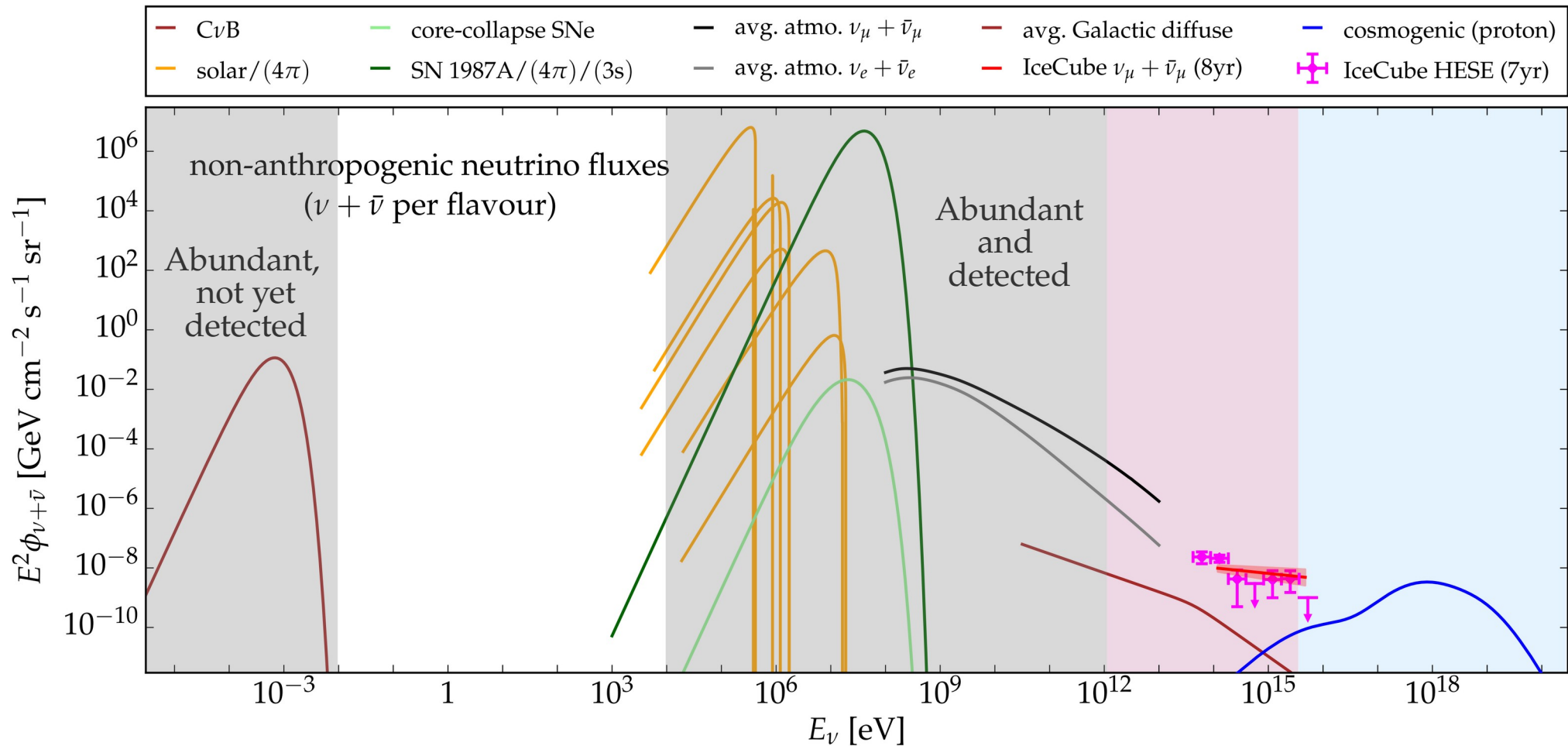


Figure courtesy of Markus Ahlers
 Maoloud, De Wasseige, Ahlers, MB, Van Elewyck, PoS(ICRC2019), 1023

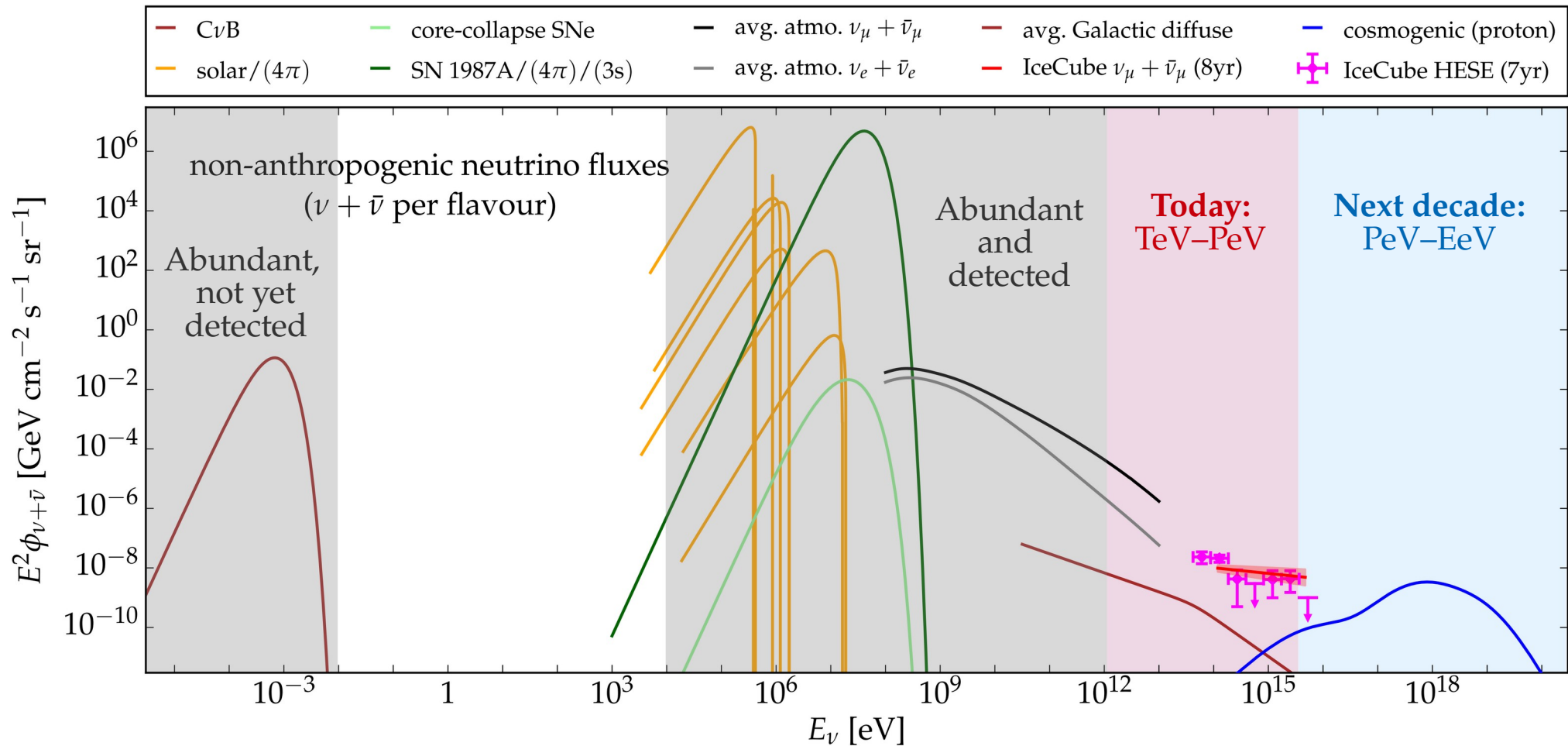


Figure courtesy of Markus Ahlers
 Maoloud, De Wasseige, Ahlers, MB, Van Elewyck, PoS(ICRC2019), 1023

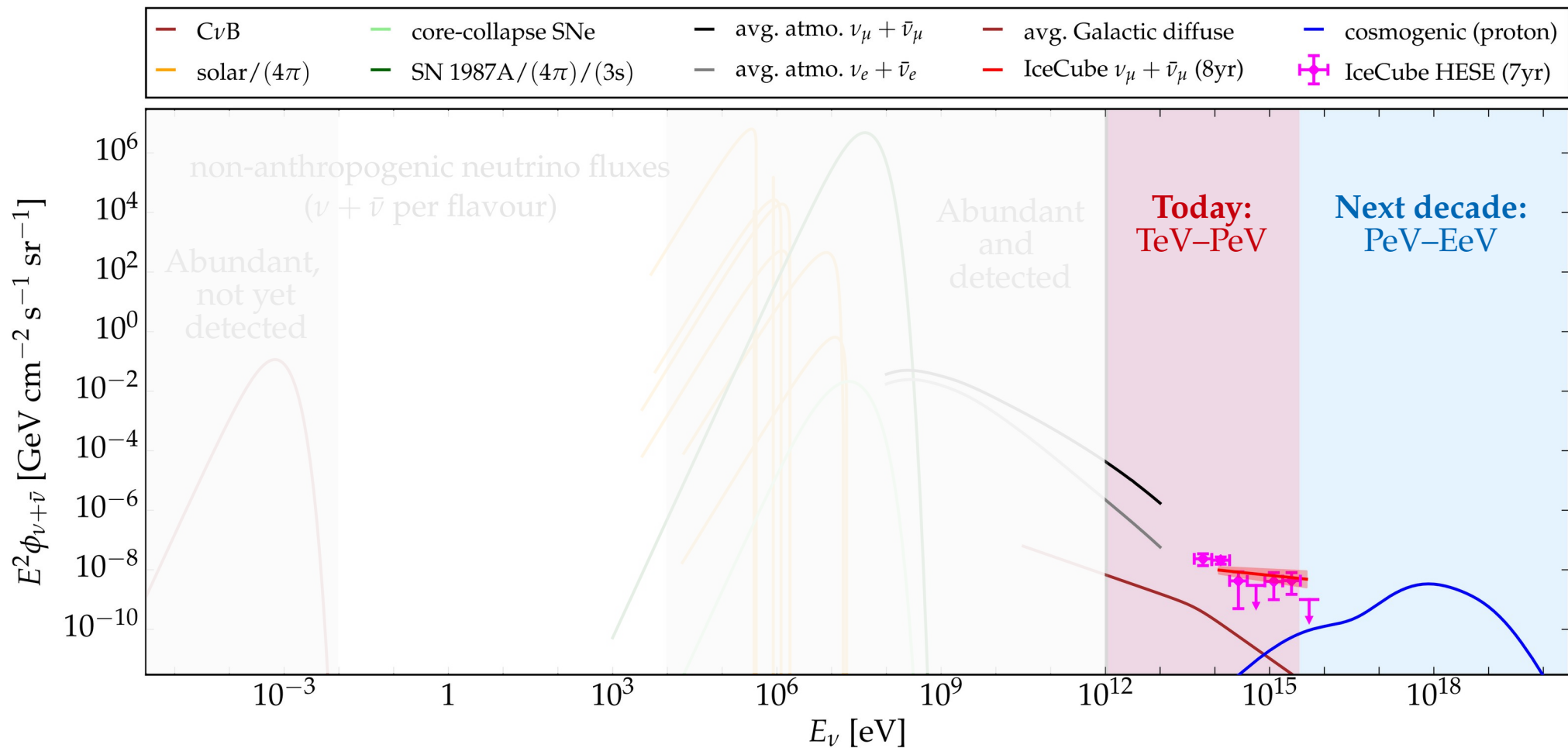
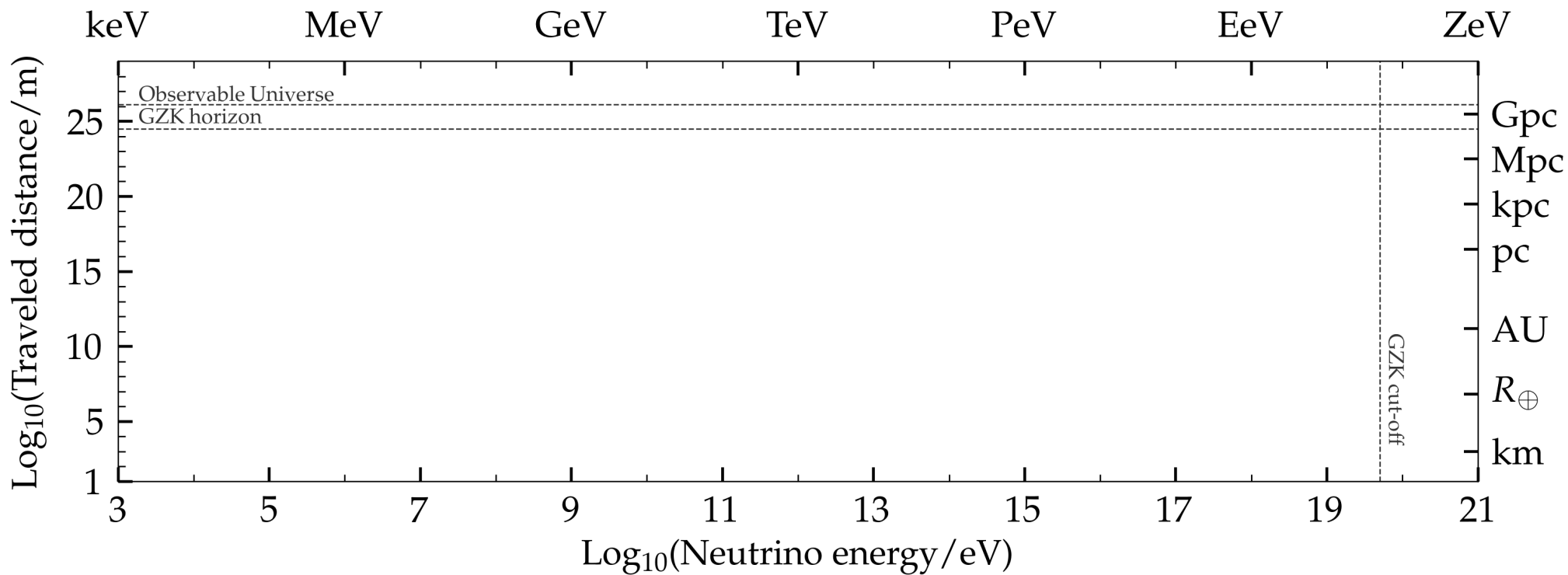
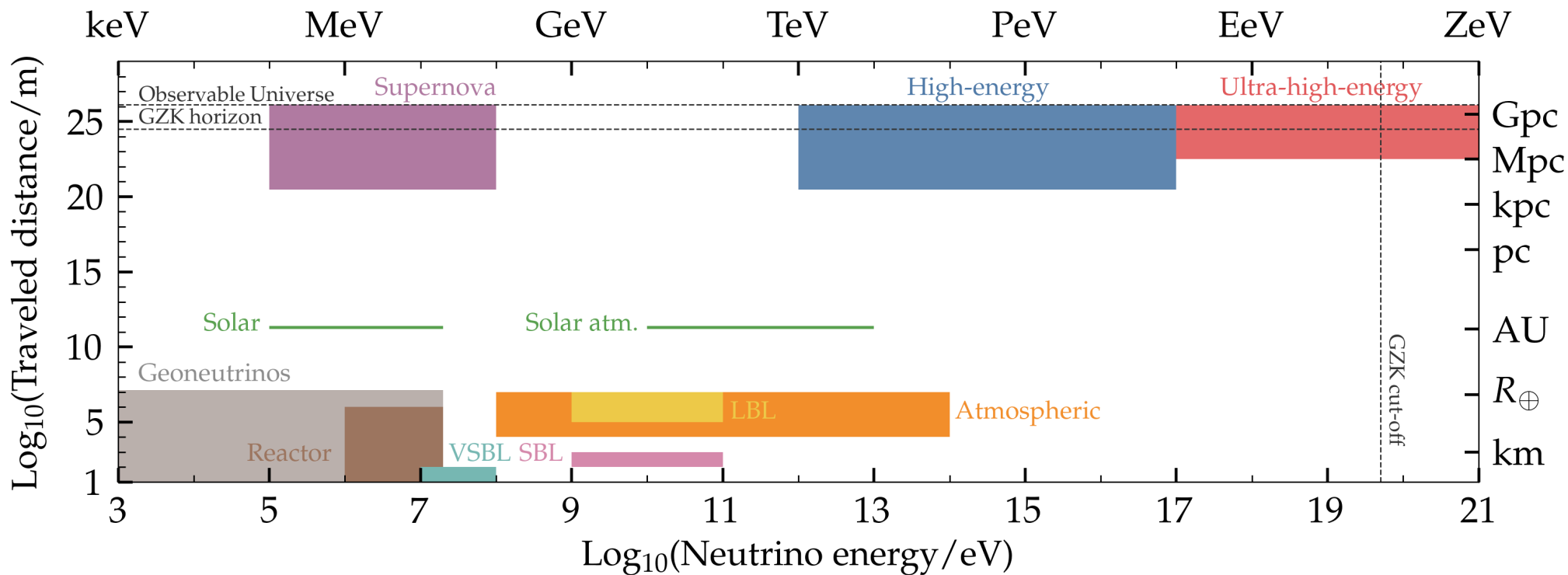


Figure courtesy of Markus Ahlers
 Maoloud, De Wasseige, Ahlers, MB, Van Elewyck, PoS(ICRC2019), 1023

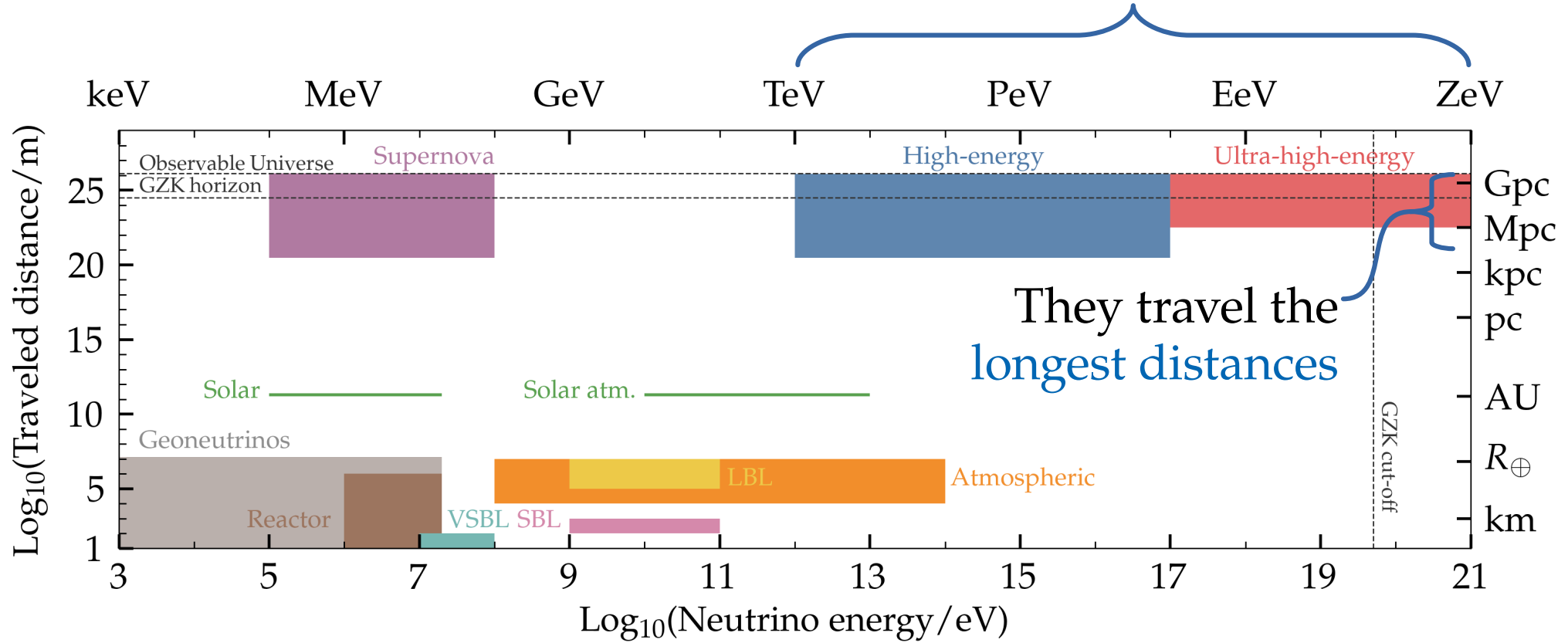
High-energy neutrinos: TeV–PeV
(*Discovered*)

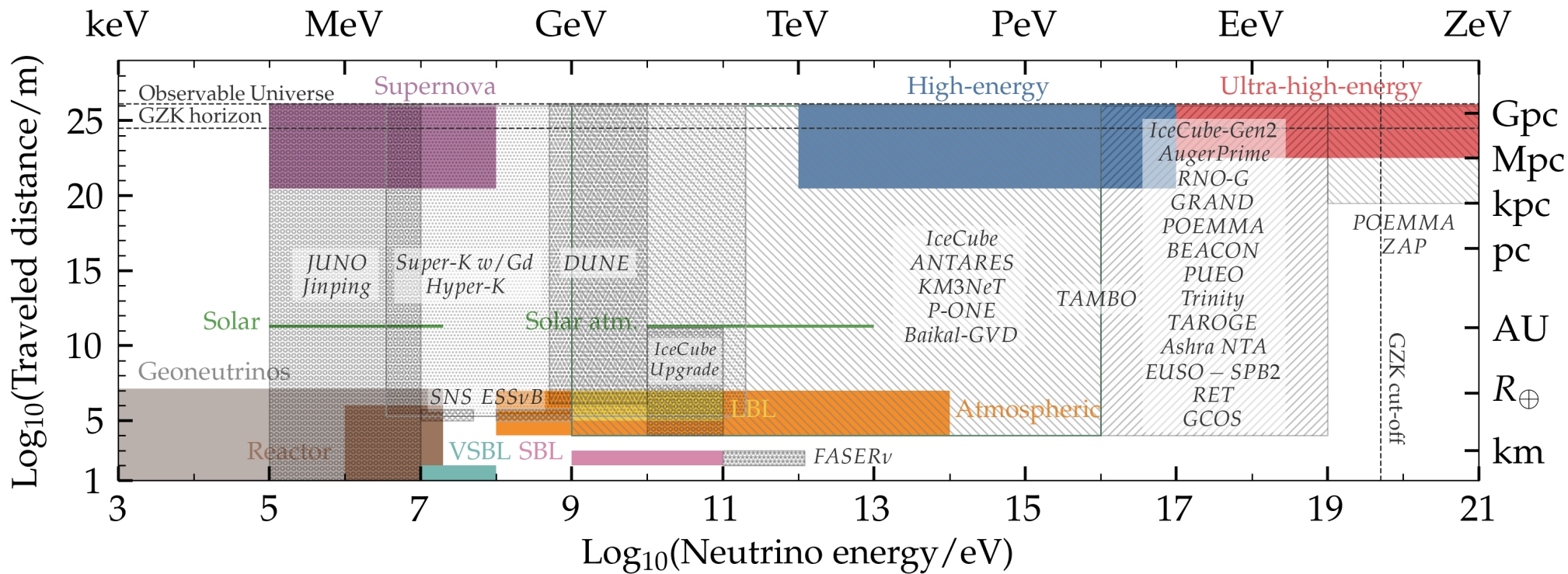
Ultra-high-energy neutrinos: > 100 PeV
(*Predicted but undiscovered*)

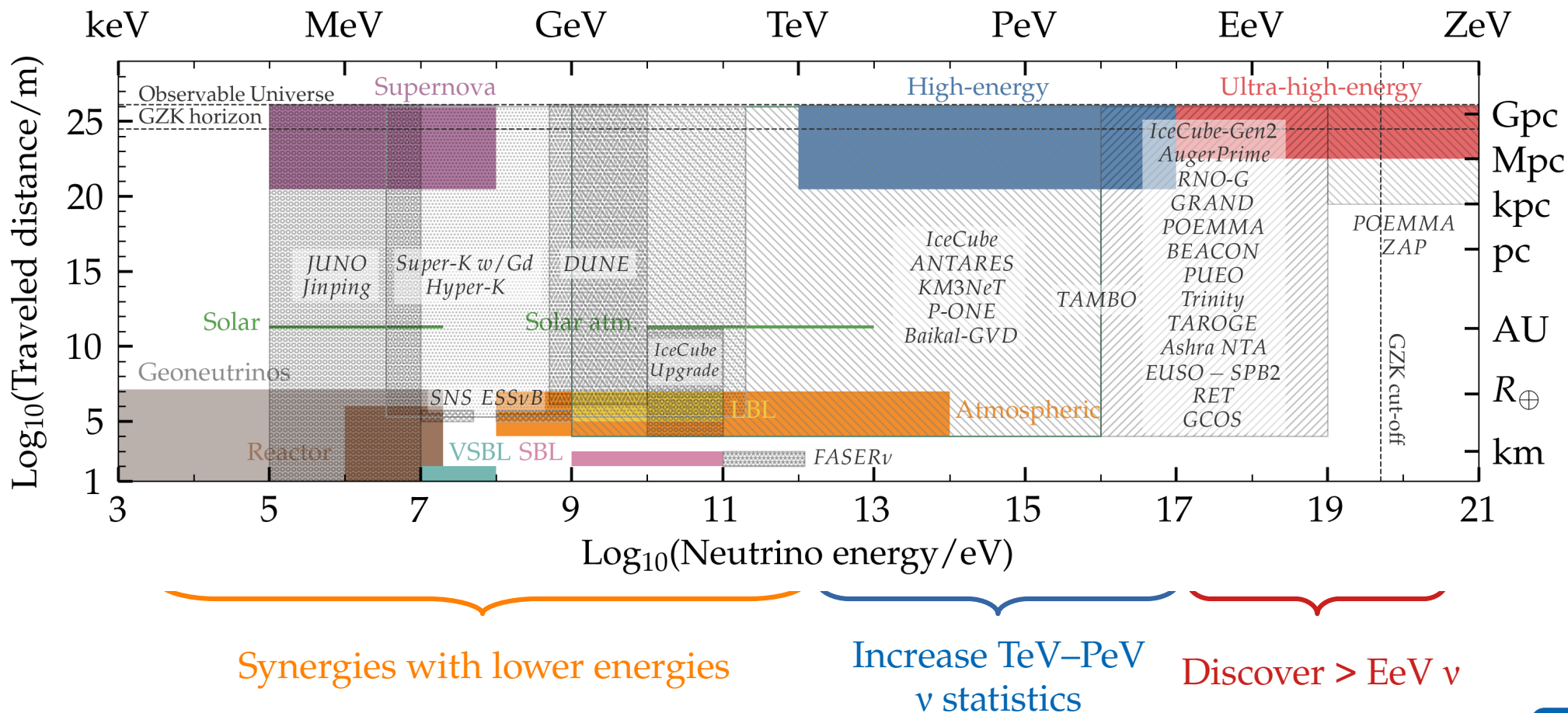


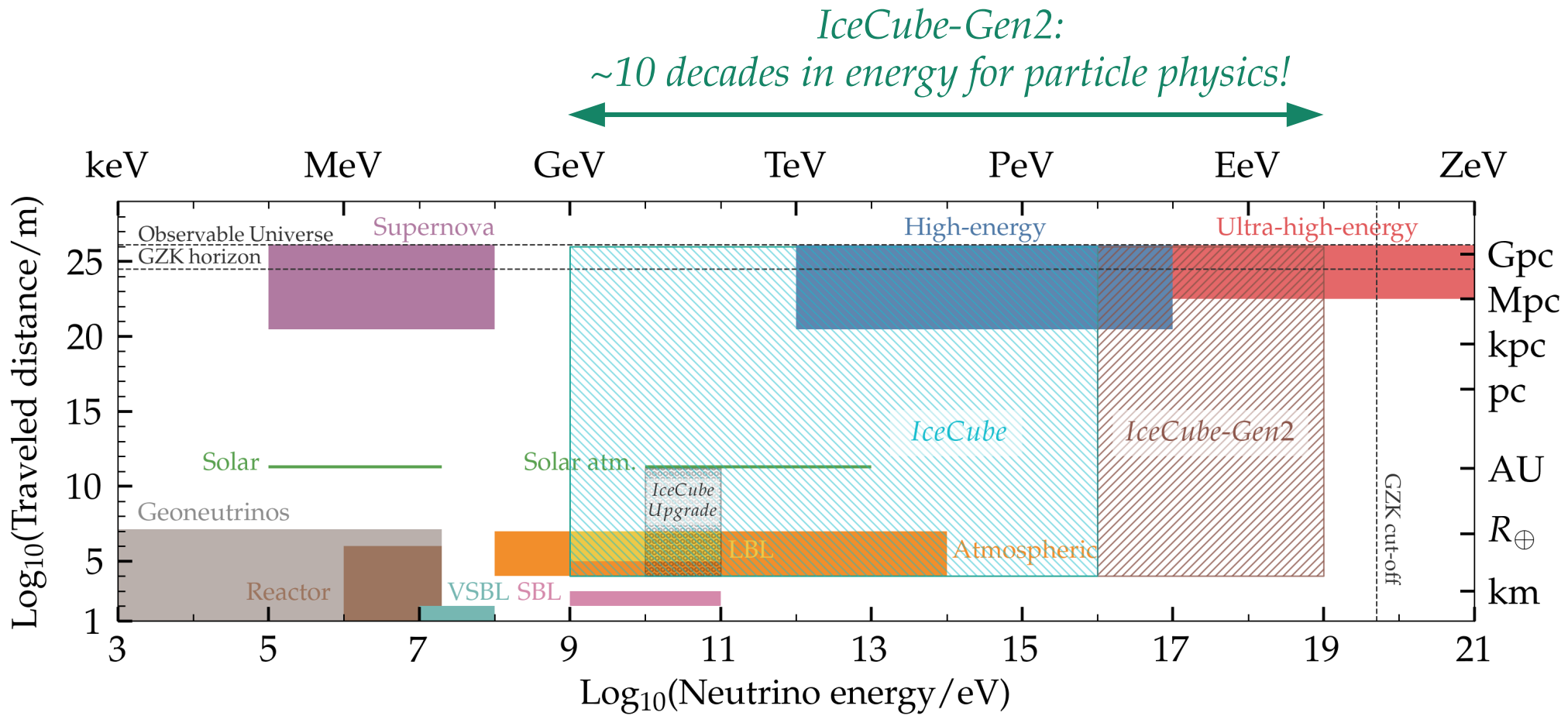


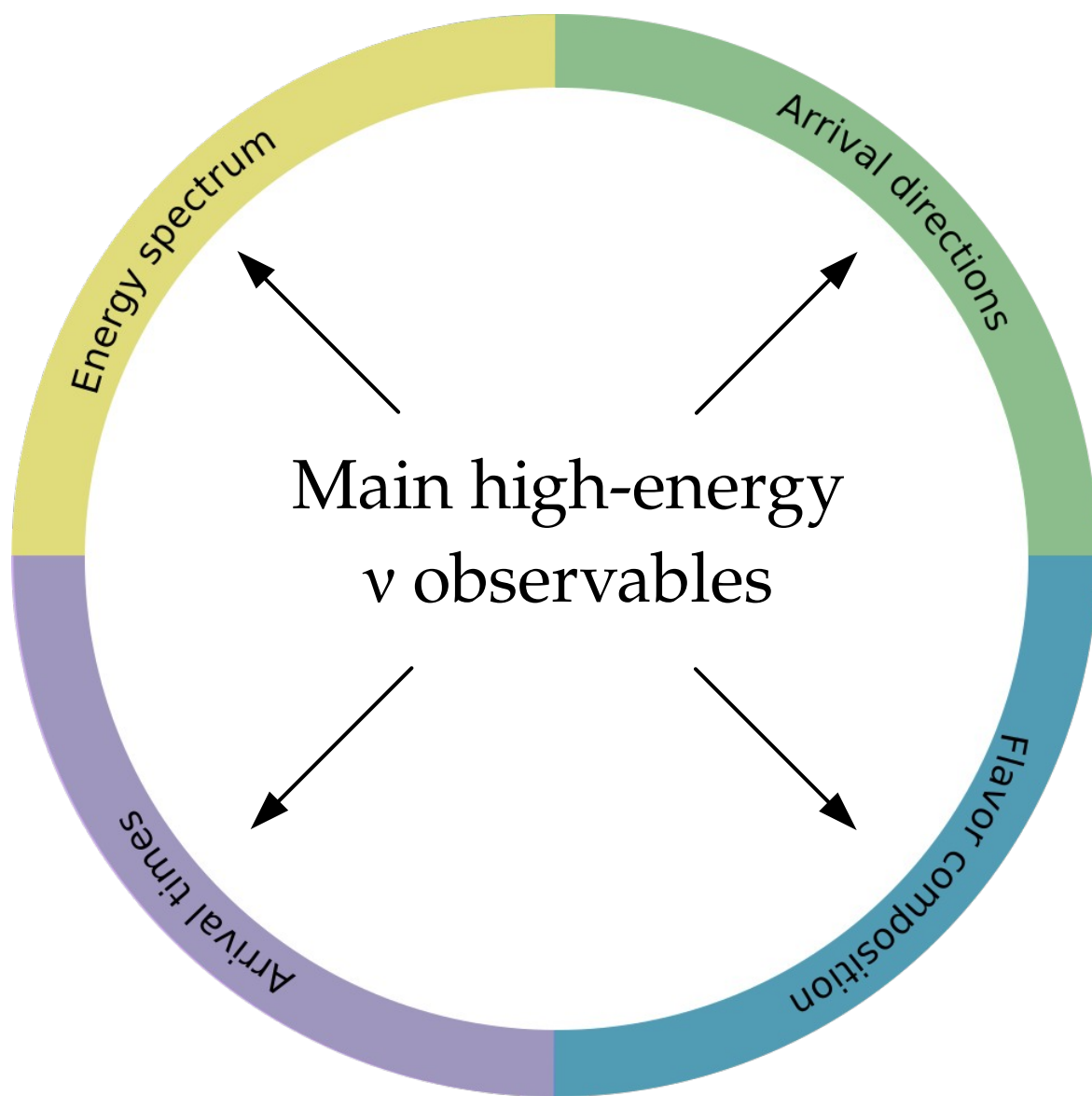
They have the **highest energies**









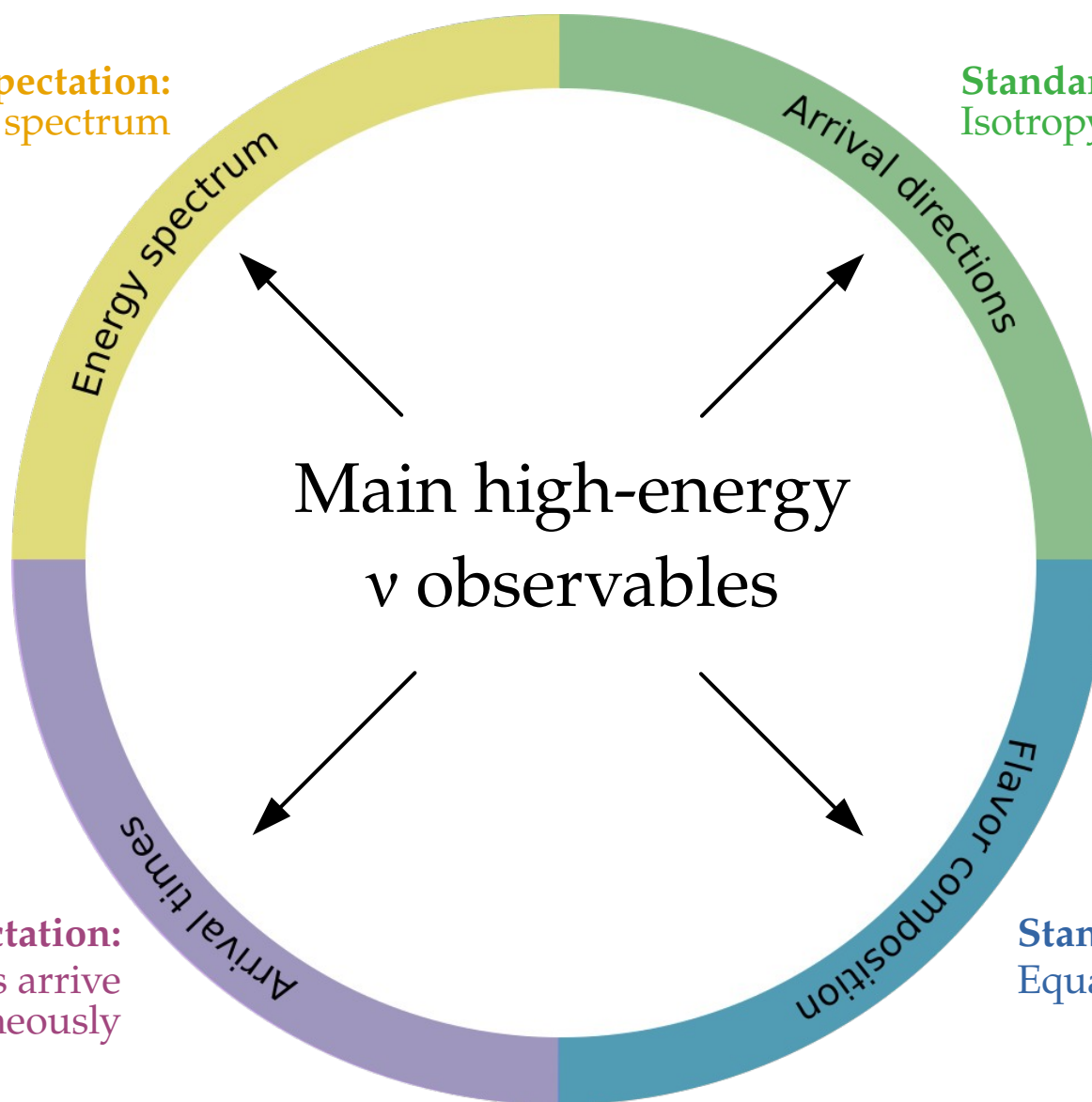


Standard expectation:
Power-law energy spectrum

Standard expectation:
Isotropy (for diffuse flux)

Standard expectation:
 ν and γ from transients arrive
simultaneously

Standard expectation:
Equal number of ν_e , ν_μ , ν_τ

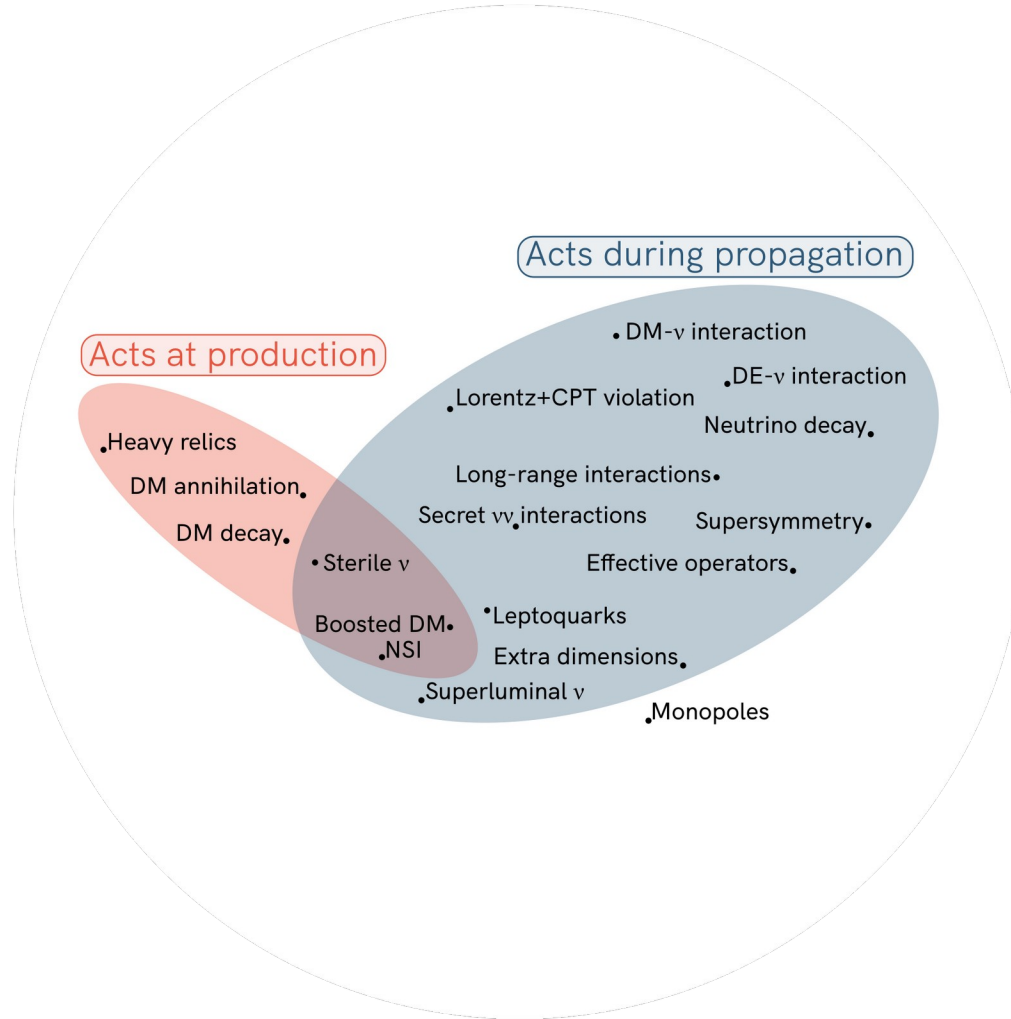




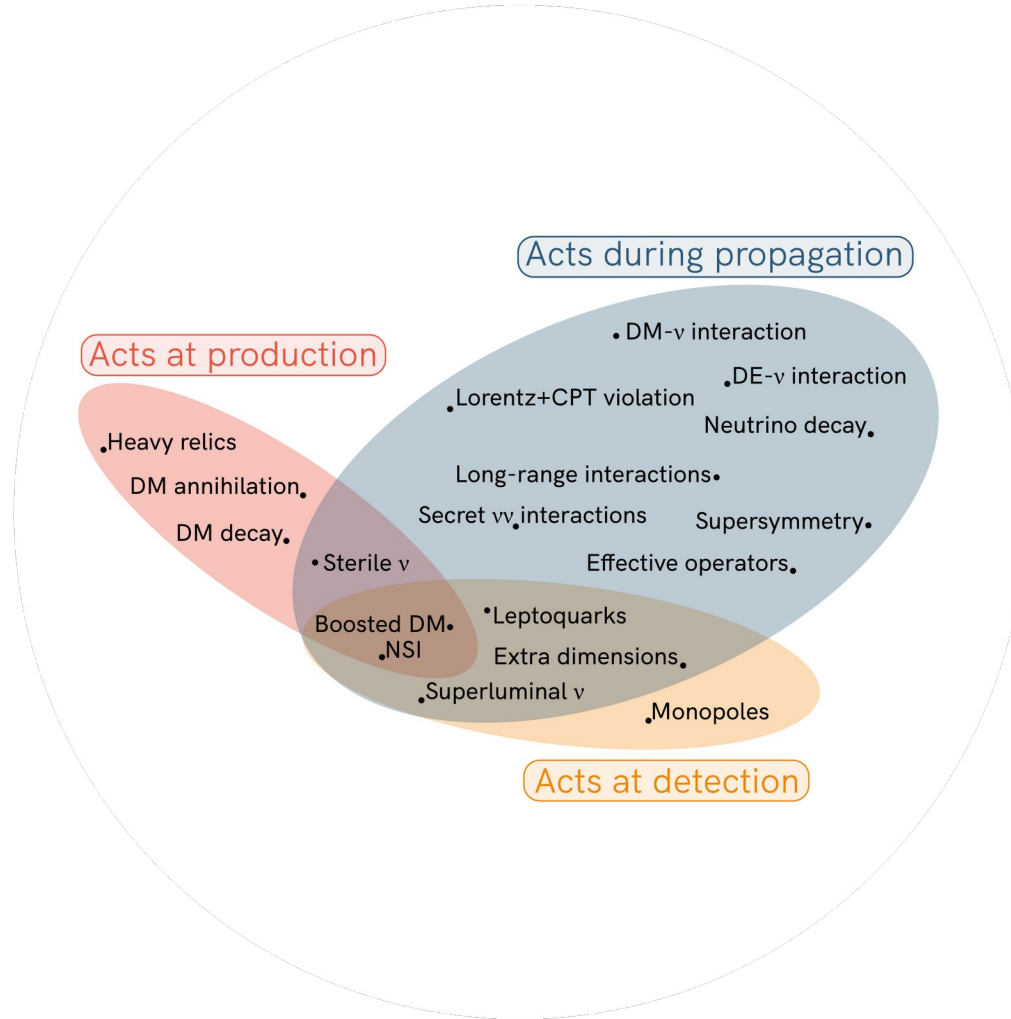
Note: Not an exhaustive list



Note: Not an exhaustive list



Note: Not an exhaustive list



Note: Not an exhaustive list

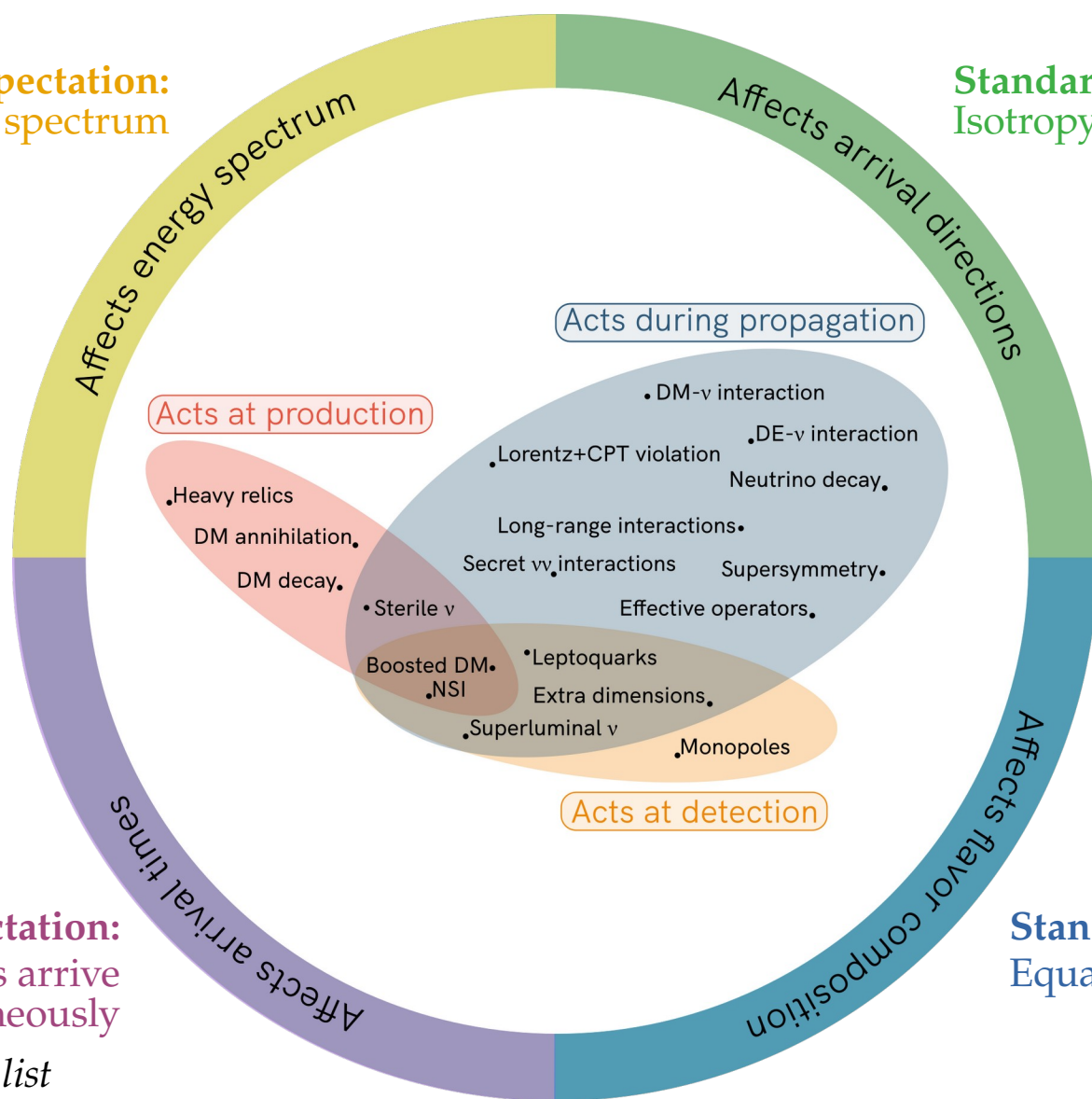
Standard expectation:
Power-law energy spectrum

Standard expectation:
Isotropy (for diffuse flux)

Standard expectation:
 ν and γ from transients arrive
simultaneously

Standard expectation:
Equal number of ν_e , ν_μ , ν_τ

Note: Not an exhaustive list



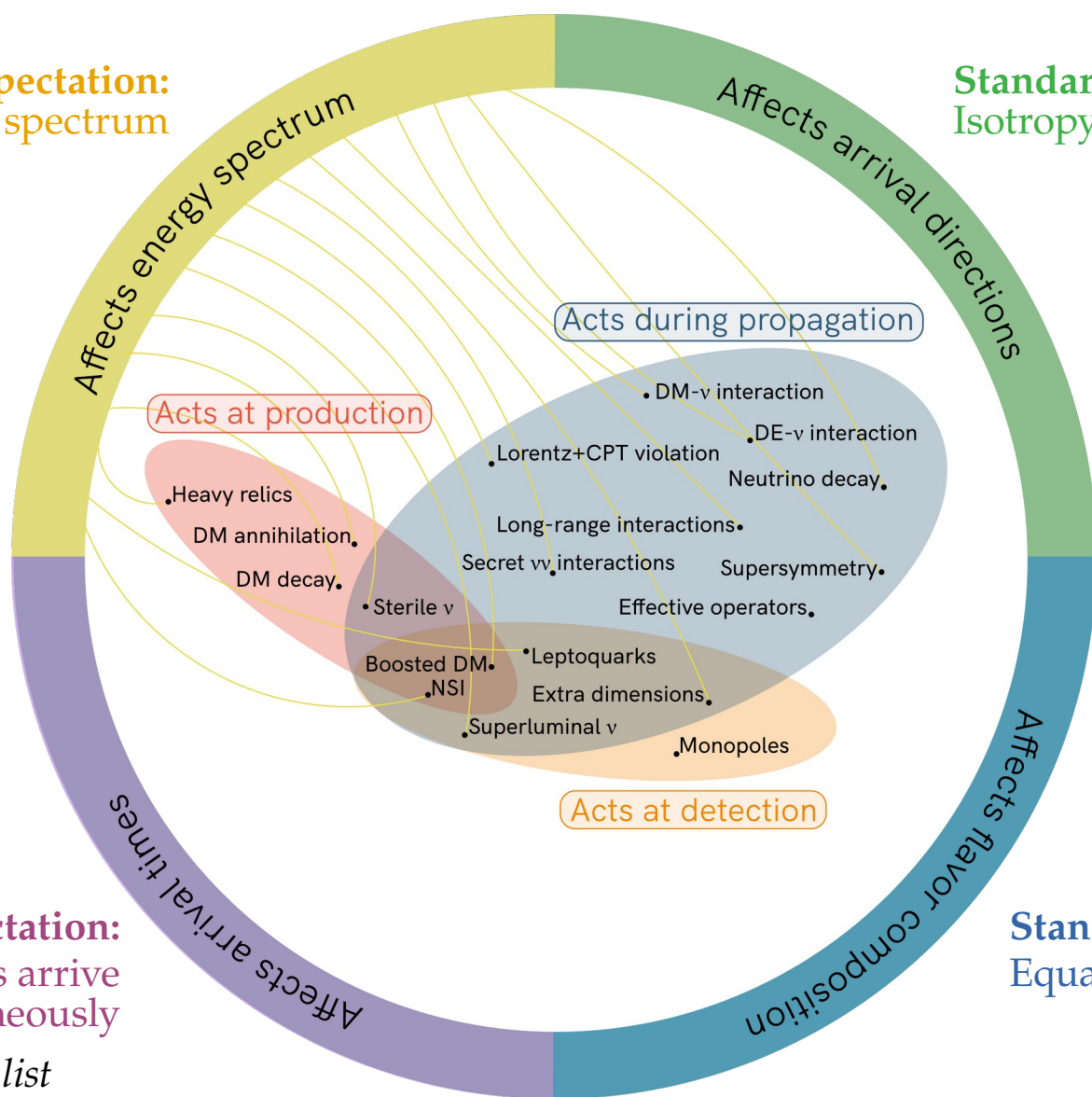
Standard expectation:
Power-law energy spectrum

Standard expectation:
Isotropy (for diffuse flux)

Standard expectation:
 ν and γ from transients arrive
simultaneously

Standard expectation:
Equal number of ν_e , ν_μ , ν_τ

Note: Not an exhaustive list



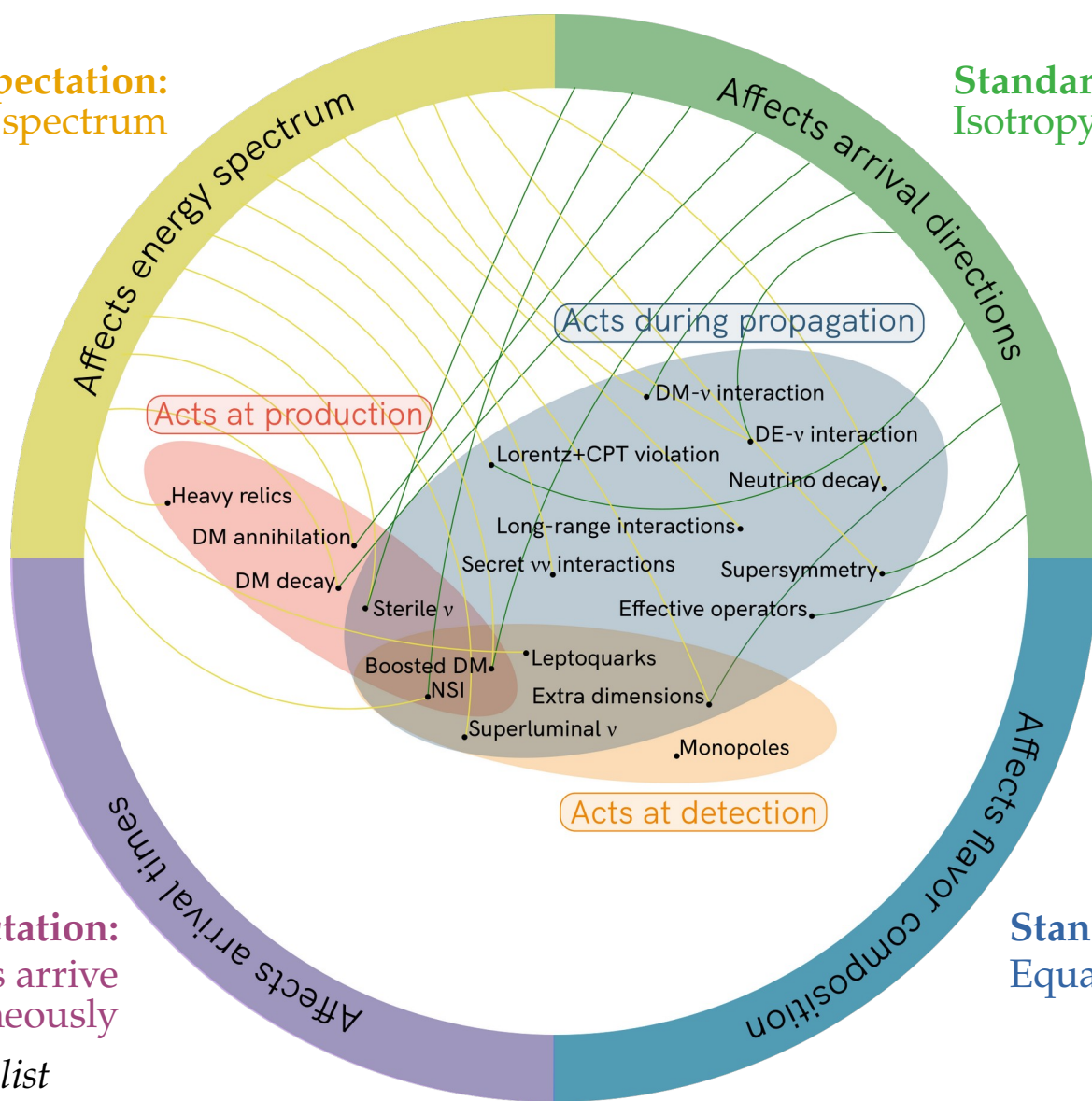
Standard expectation:
Power-law energy spectrum

Standard expectation:
Isotropy (for diffuse flux)

Standard expectation:
 ν and γ from transients arrive
simultaneously

Standard expectation:
Equal number of ν_e , ν_μ , ν_τ

Note: Not an exhaustive list



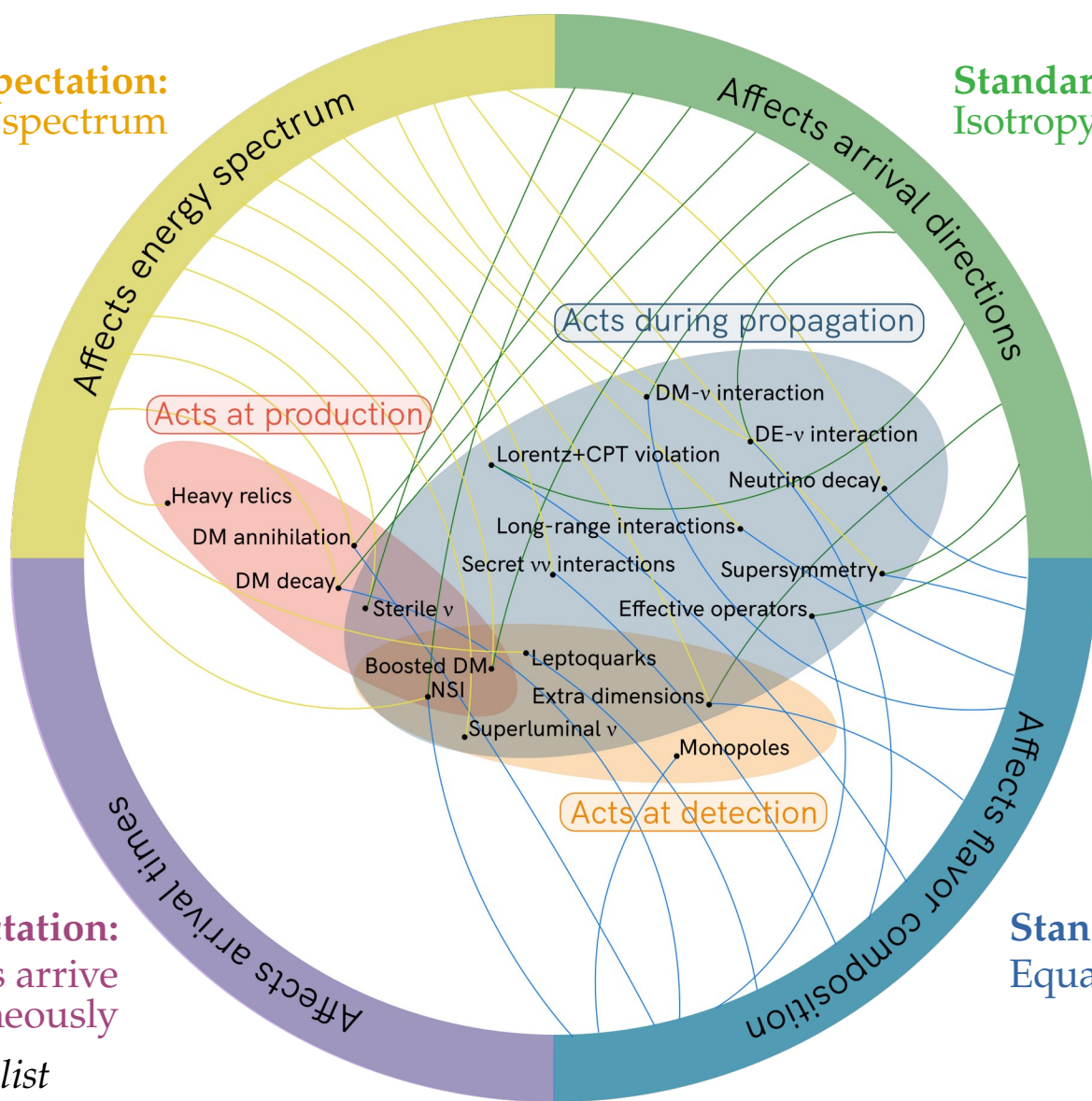
Standard expectation:
Power-law energy spectrum

Standard expectation:
Isotropy (for diffuse flux)

Standard expectation:
 ν and γ from transients arrive
simultaneously

Standard expectation:
Equal number of ν_e , ν_μ , ν_τ

Note: Not an exhaustive list



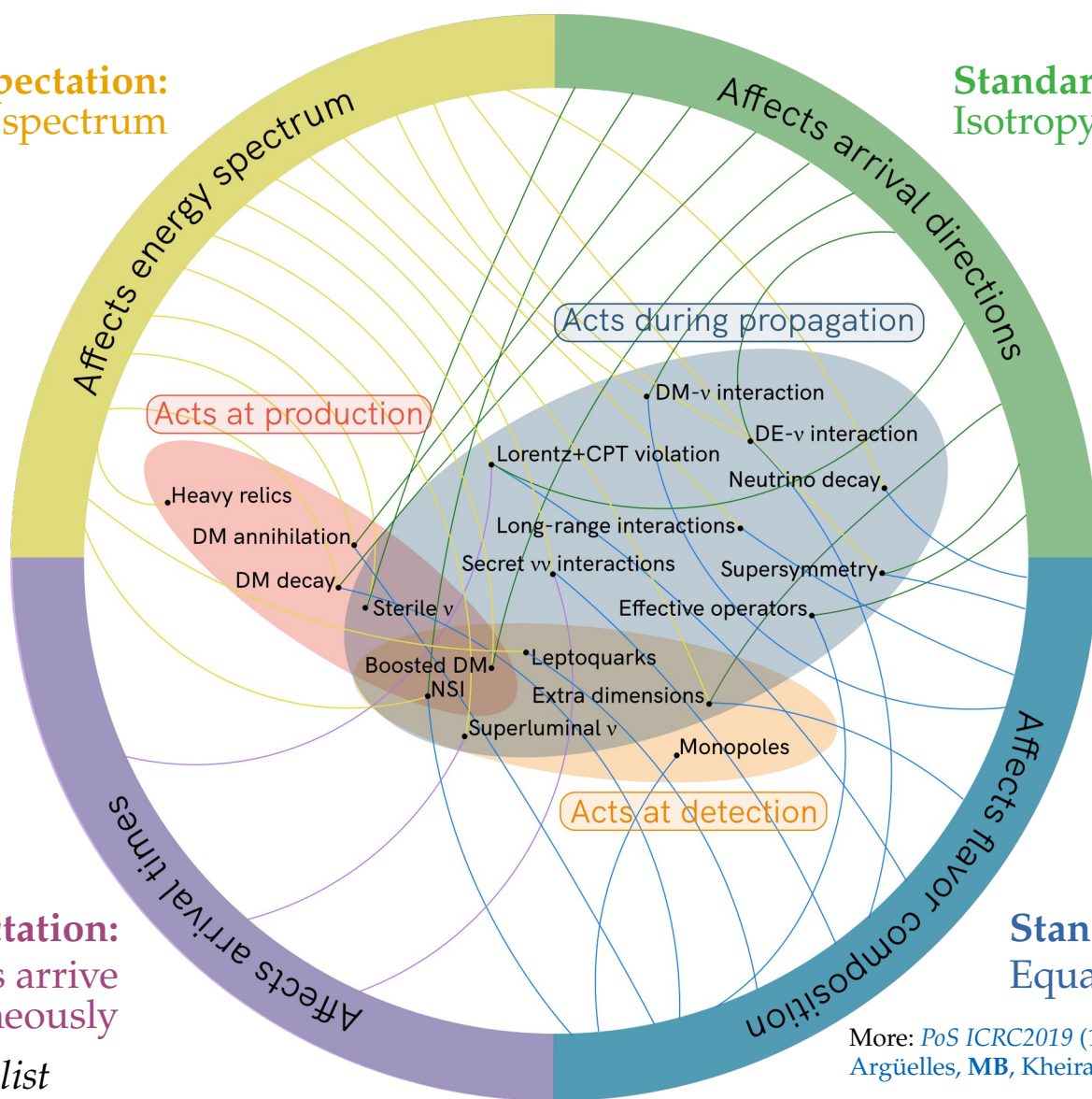
Standard expectation:
Power-law energy spectrum

Standard expectation:
Isotropy (for diffuse flux)

Standard expectation:
 ν and γ from transients arrive
simultaneously

Standard expectation:
Equal number of ν_e , ν_μ , ν_τ

Note: Not an exhaustive list



More: *PoS ICRC2019 (1907.08690)*

Argüelles, MB, Kheirandish, Palomares-Ruiz, Salvadó, Vincent

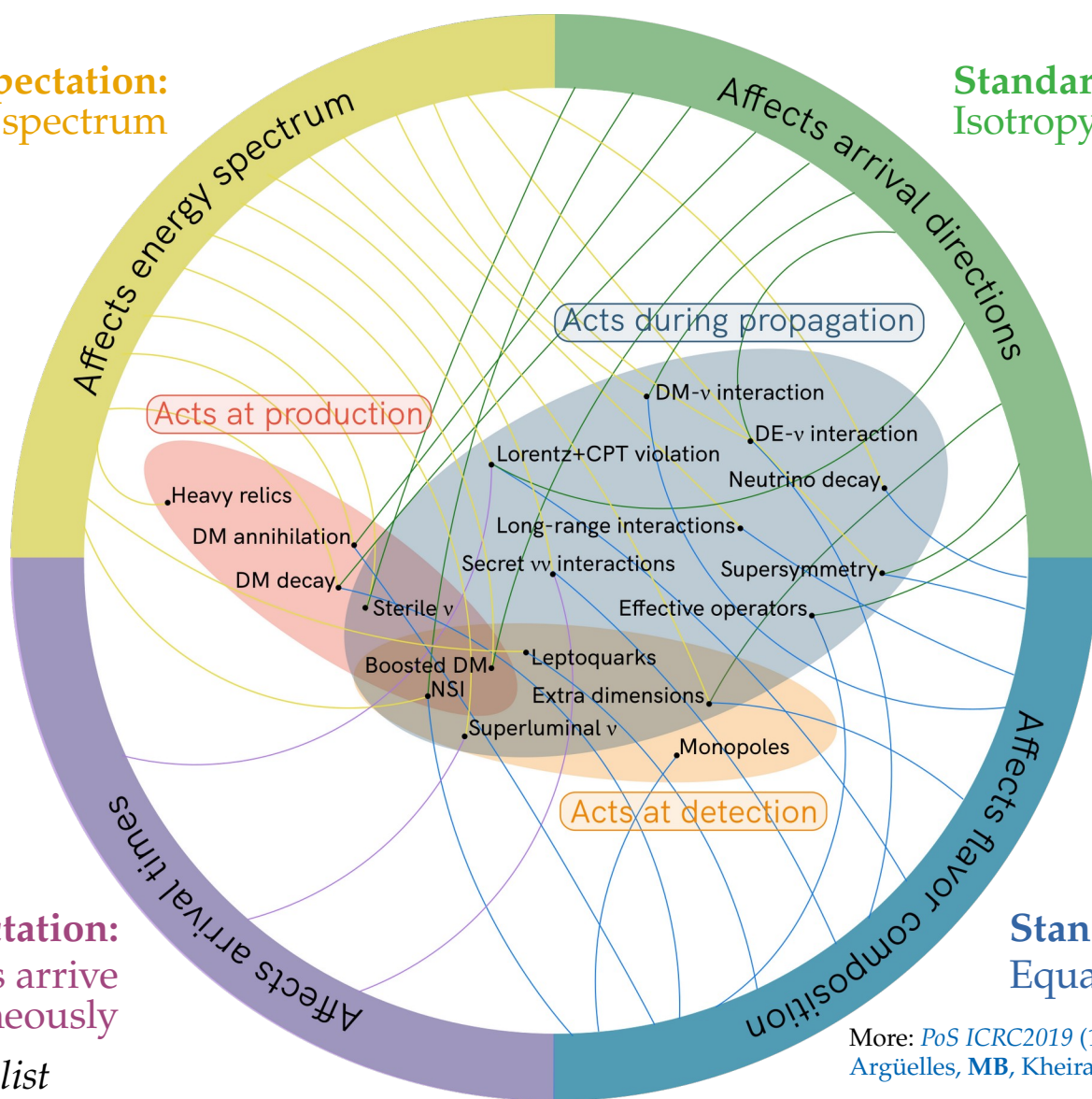
Standard expectation:
Power-law energy spectrum

Standard expectation:
Isotropy (for diffuse flux)

Standard expectation:
 ν and γ from transients arrive
simultaneously

Standard expectation:
Equal number of ν_e , ν_μ , ν_τ

Note: Not an exhaustive list



More: *PoS ICRC2019 (1907.08690)*

Argüelles, MB, Kheirandish, Palomares-Ruiz, Salvadó, Vincent

Standard expectation:
Power-law energy spectrum

Standard expectation:
Isotropy (for diffuse flux)

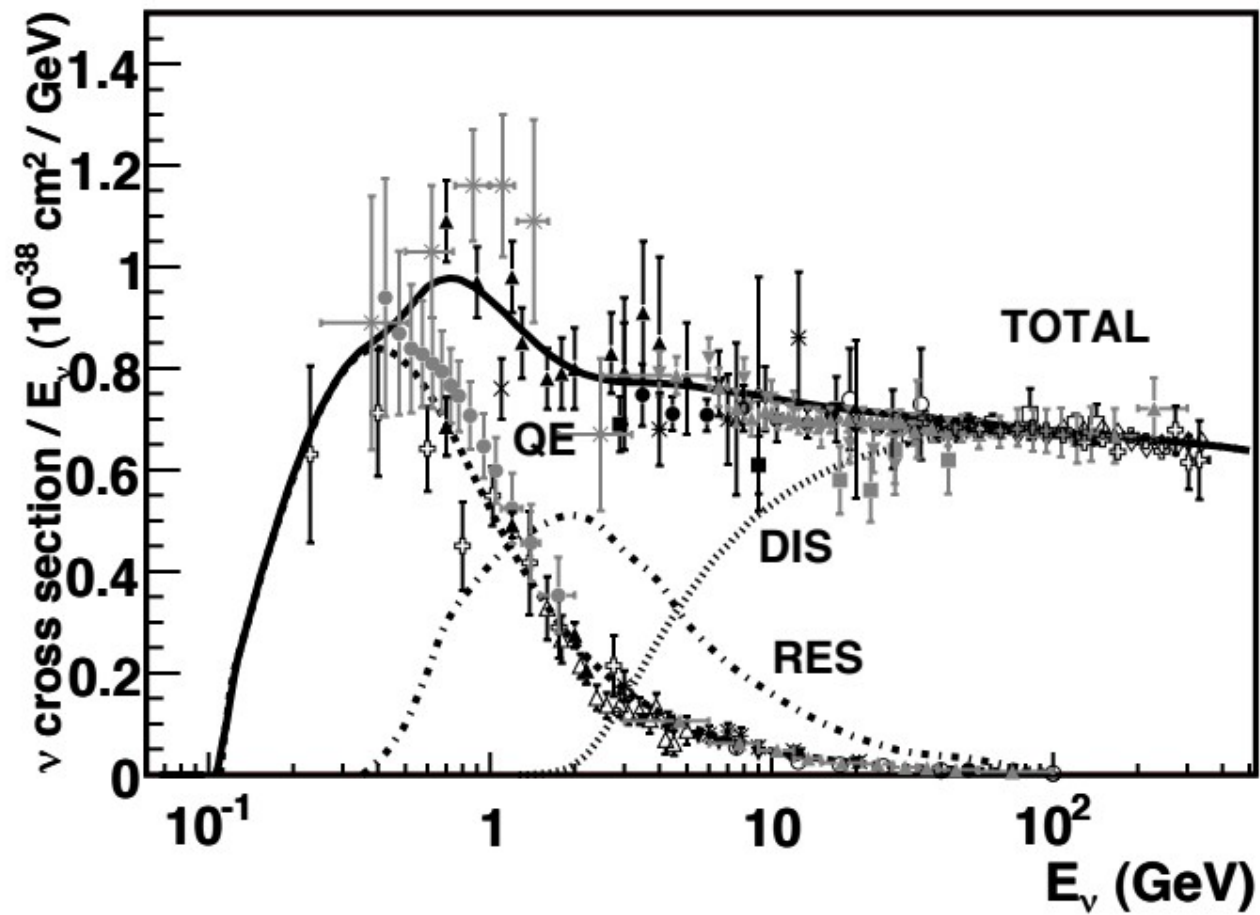
Reviews:
Ahlers, Helbing, De los Heros, *EPJC* 2018
Argüelles, MB, Kheirandish, Palomares-Ruiz, Salvadó, Vincent, *ICRC* 2019 [1907.08690]
Ackermann, Ahlers, Anchordoqui, MB, et al., *Astro2020 Decadal Survey* [1903.04333]

Standard expectation:
 ν and γ from transients arrive
simultaneously

Standard expectation:
Equal number of ν_e , ν_μ , ν_τ

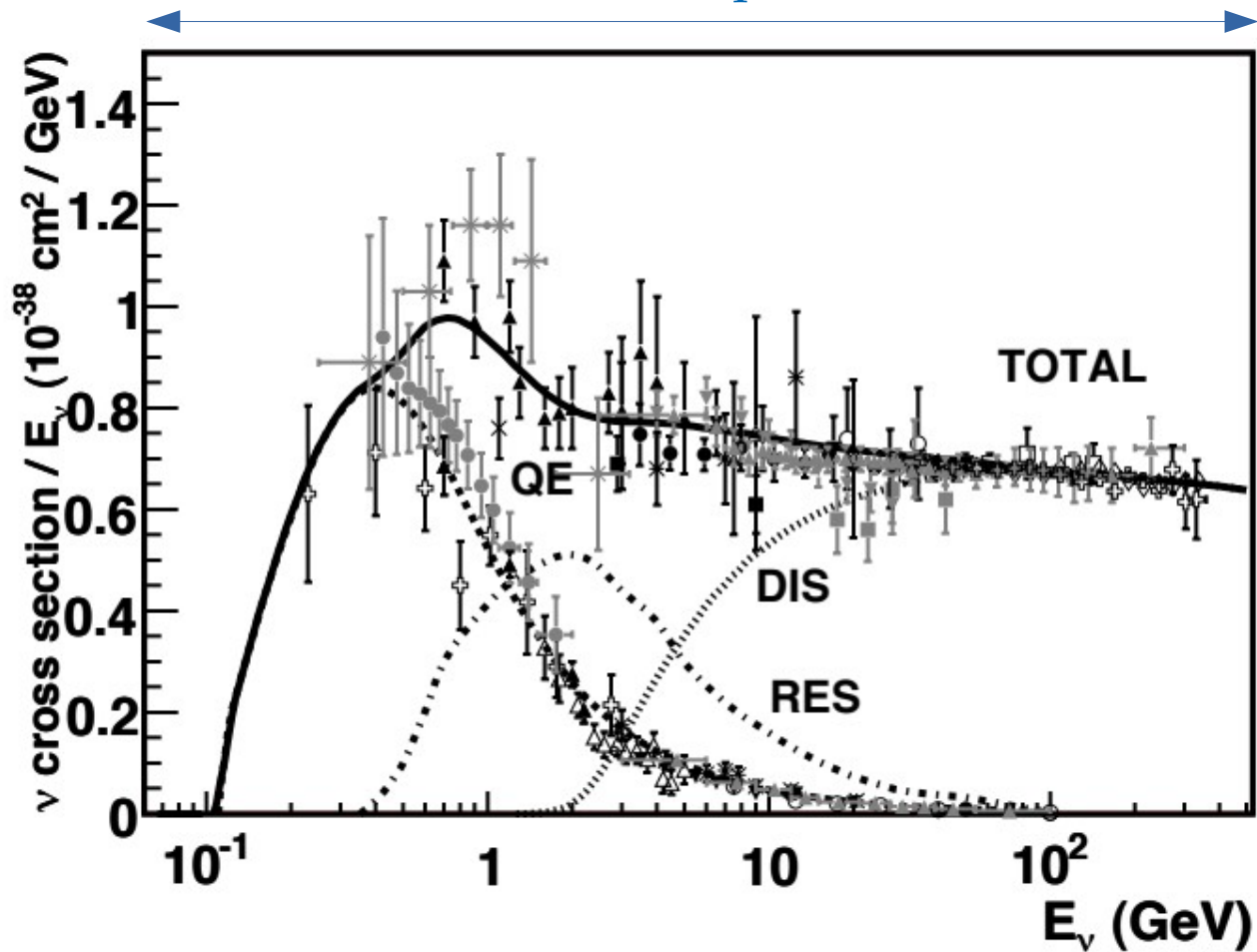
Note: Not an exhaustive list

More: *PoS ICRC2019* (1907.08690)
Argüelles, MB, Kheirandish, Palomares-Ruiz, Salvadó, Vincent



Particle Data Group

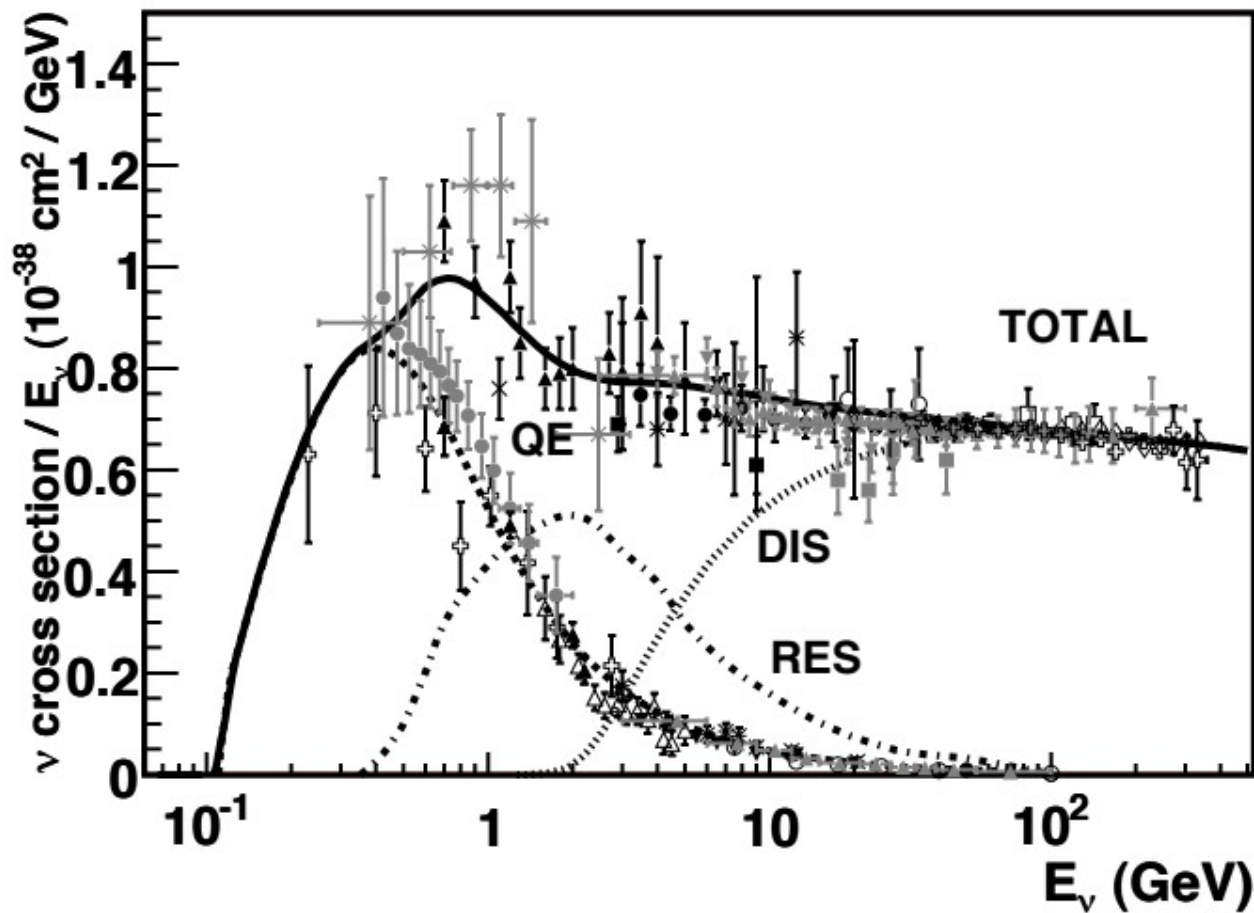
Accelerator experiments



Particle Data Group

Accelerator experiments

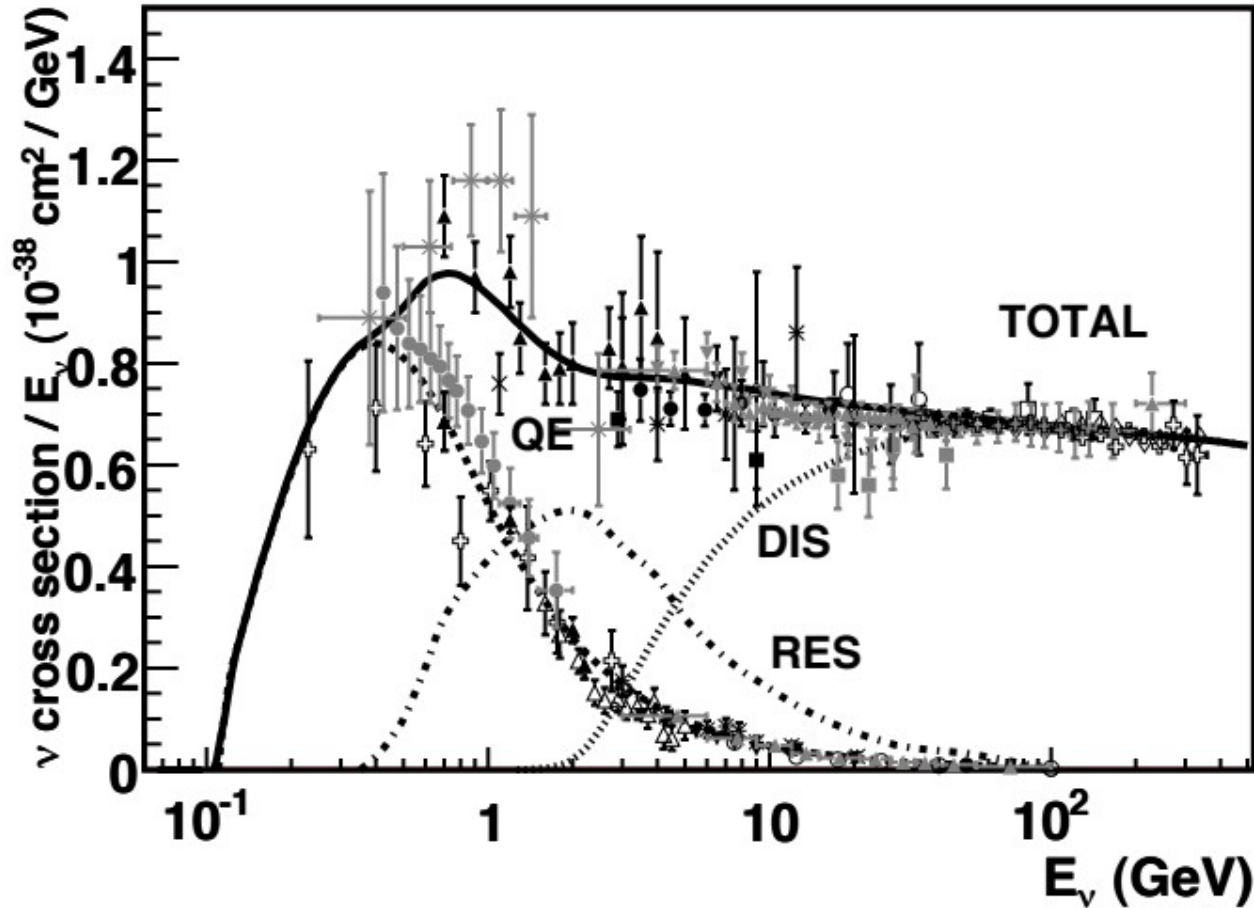
One recent
measurement
(COHERENT)



Particle Data Group

Accelerator experiments

One recent
measurement
(COHERENT)

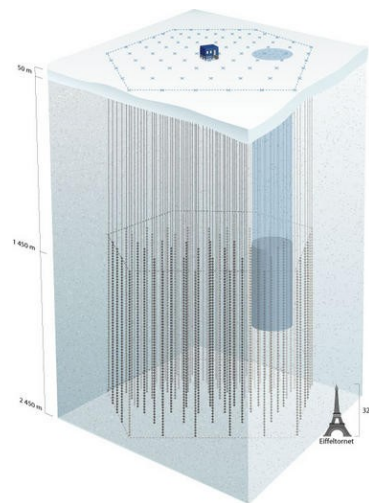
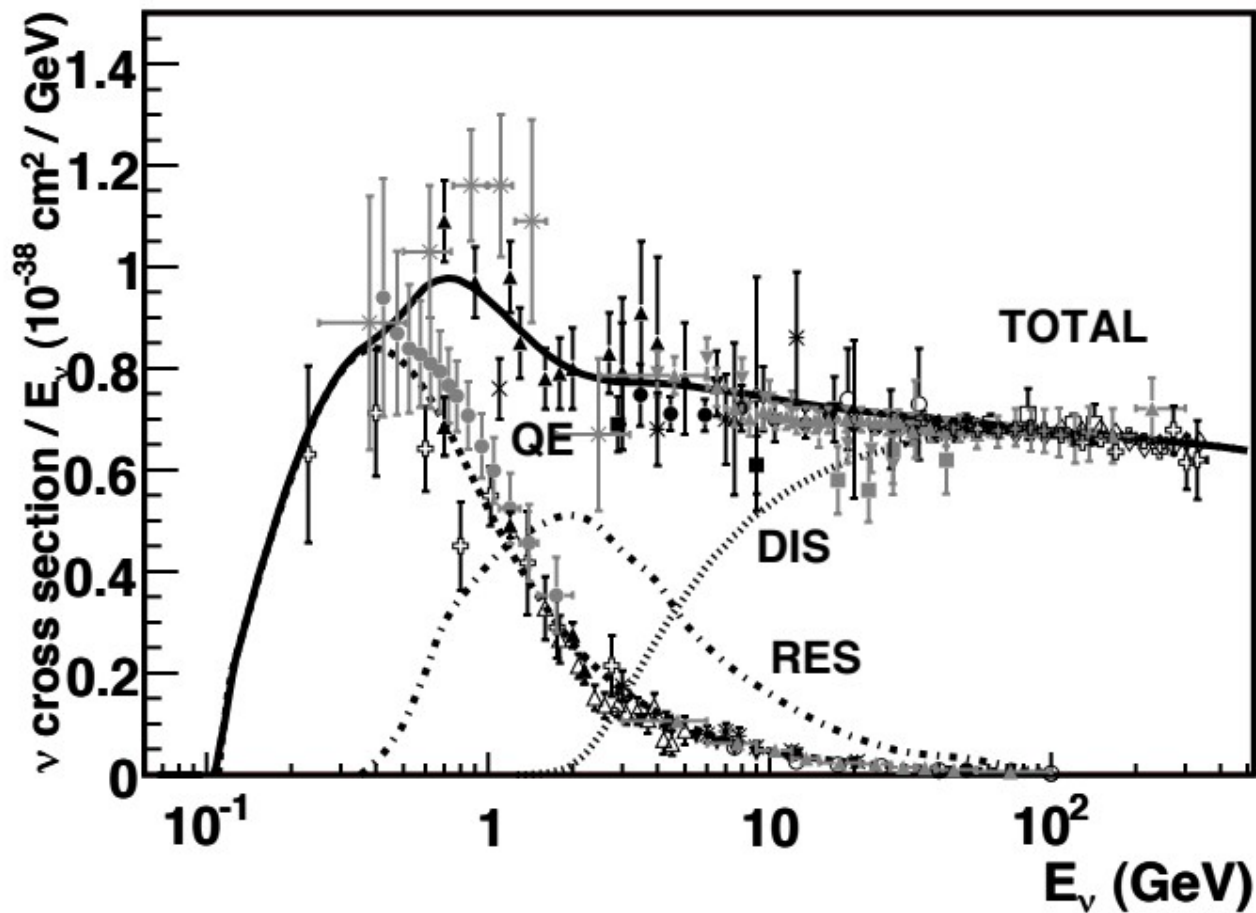


No
measurements
... until recently!

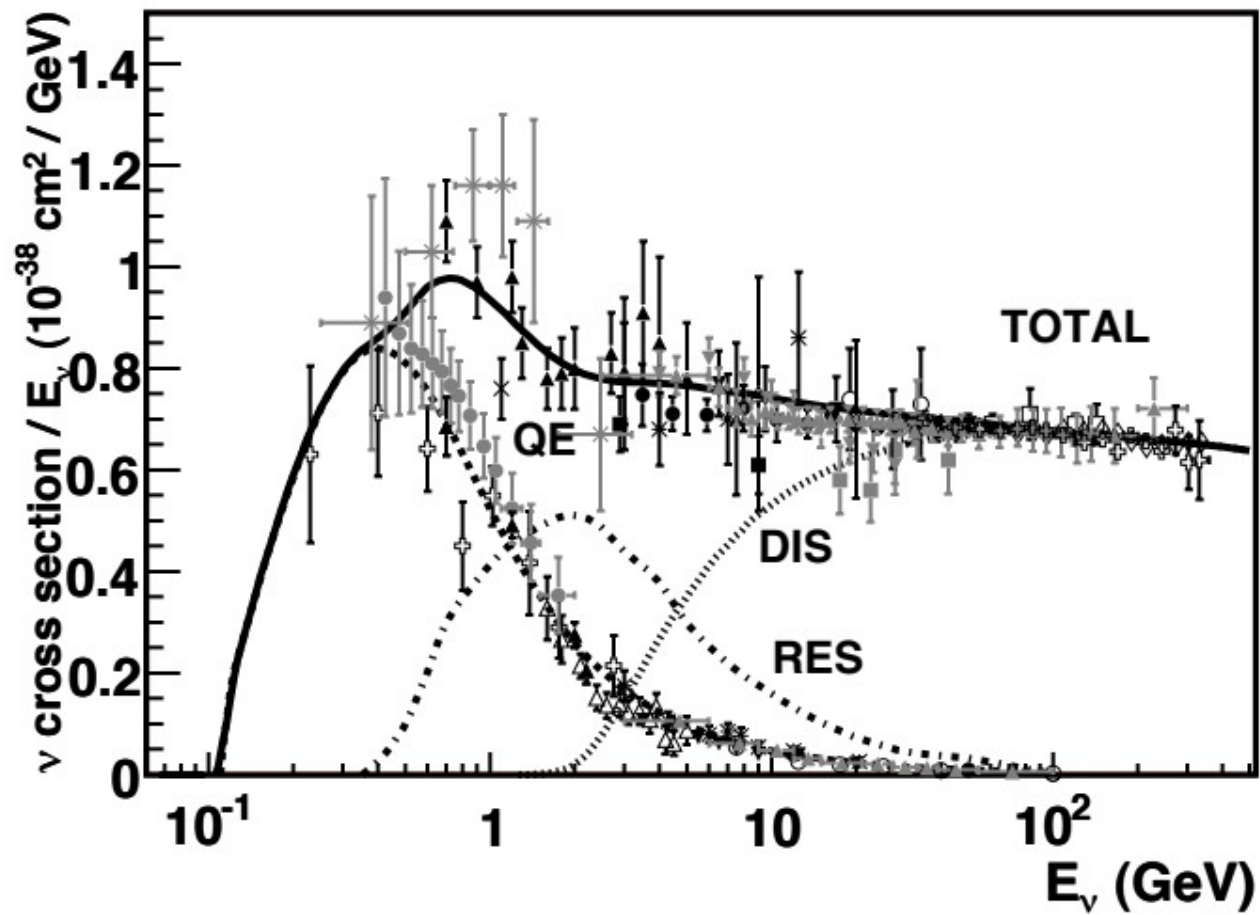
Particle Data Group

Accelerator experiments

One recent
measurement
(COHERENT)



Particle Data Group

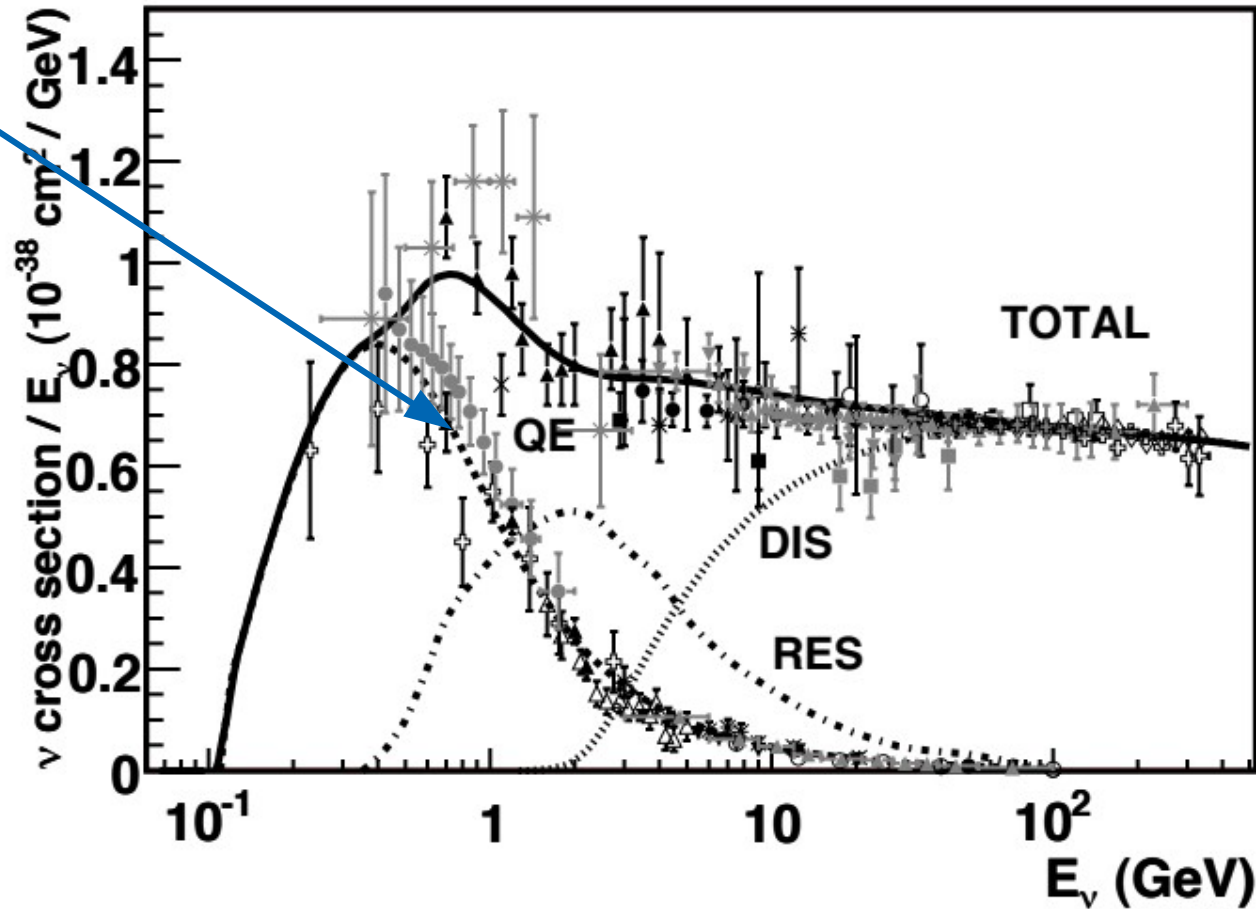


Particle Data Group

Quasi-elastic
scattering:

$$\nu_l + n \rightarrow l^- + p$$

$$\bar{\nu}_l + p \rightarrow l^+ + n$$

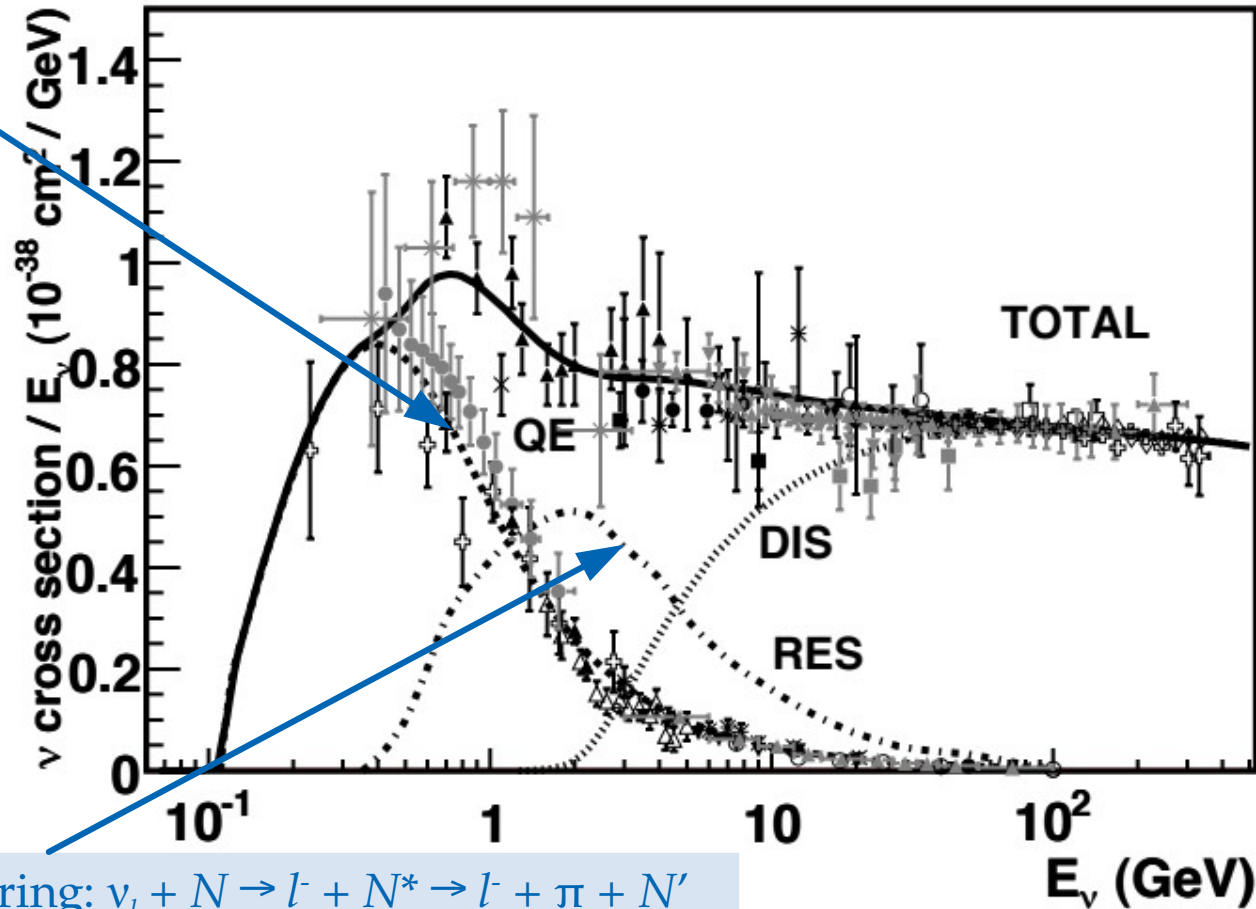


Particle Data Group

Quasi-elastic
scattering:

$$\nu_l + n \rightarrow l^- + p$$

$$\bar{\nu}_l + p \rightarrow l^+ + n$$



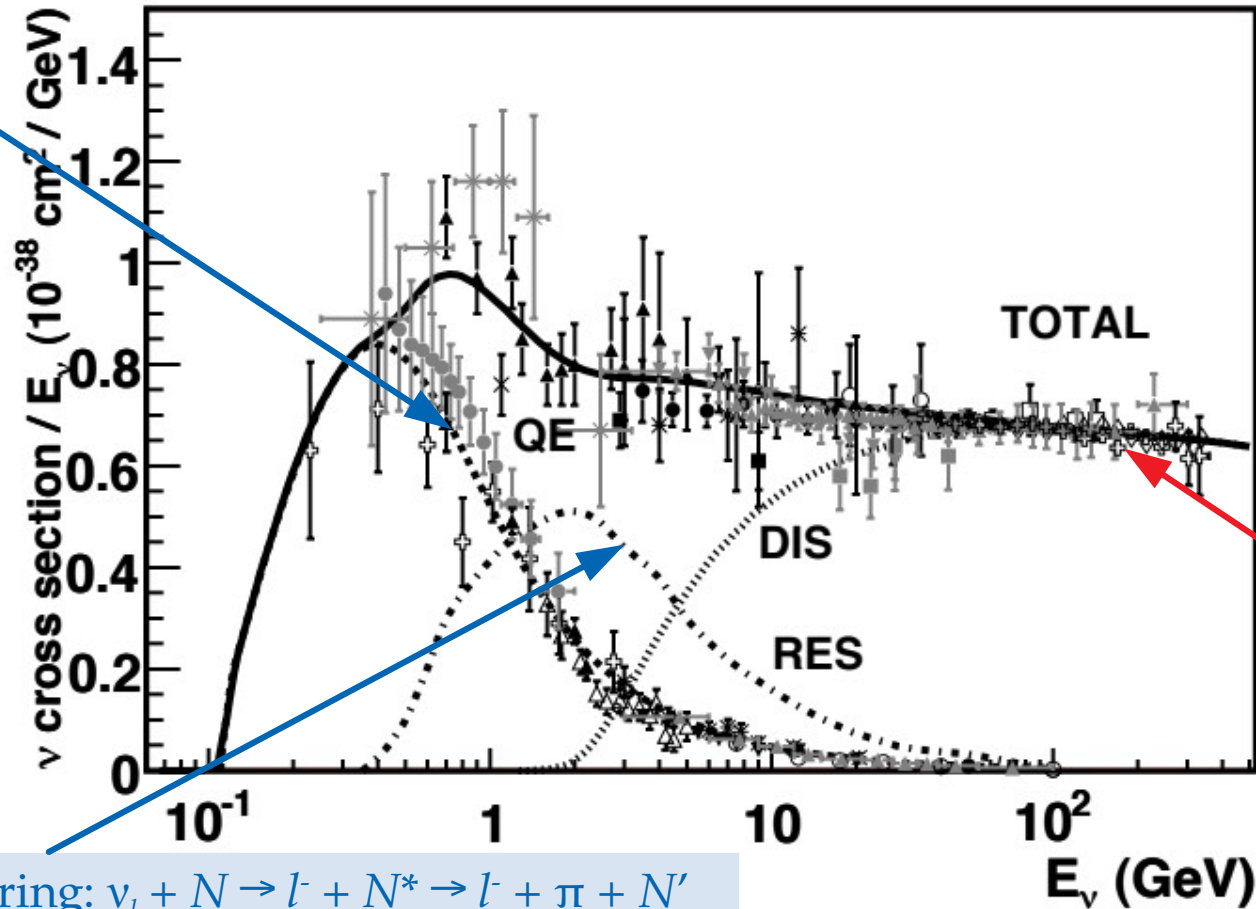
Resonant scattering: $\nu_l + N \rightarrow l^- + N^* \rightarrow l^- + \pi + N'$

Particle Data Group

Quasi-elastic
scattering:

$$\nu_l + n \rightarrow l^- + p$$

$$\bar{\nu}_l + p \rightarrow l^+ + n$$



Deep inelastic
scattering:

$$\nu_l + N \rightarrow l^- + X$$

$$\bar{\nu}_l + N \rightarrow l^+ + X$$

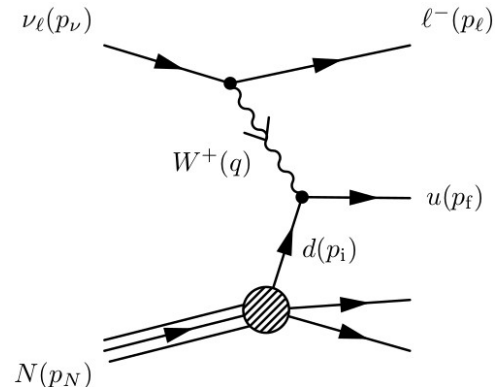
Resonant scattering: $\nu_l + N \rightarrow l^- + N^* \rightarrow l^- + \pi + N'$

Particle Data Group

Extrapolating the cross section to high energies

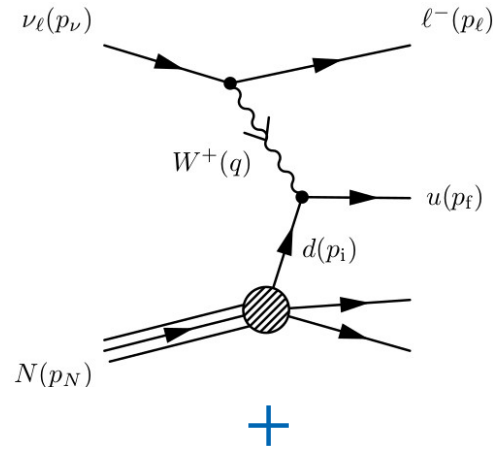
Extrapolating the cross section to high energies

From theory:
Standard Model
neutrino-quark
cross section

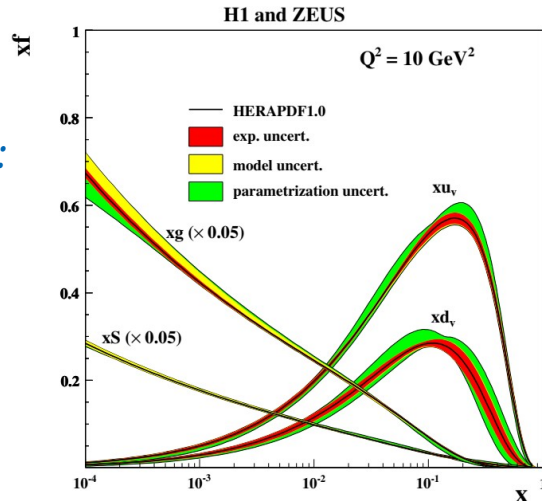


Extrapolating the cross section to high energies

From theory:
Standard Model
neutrino-quark
cross section

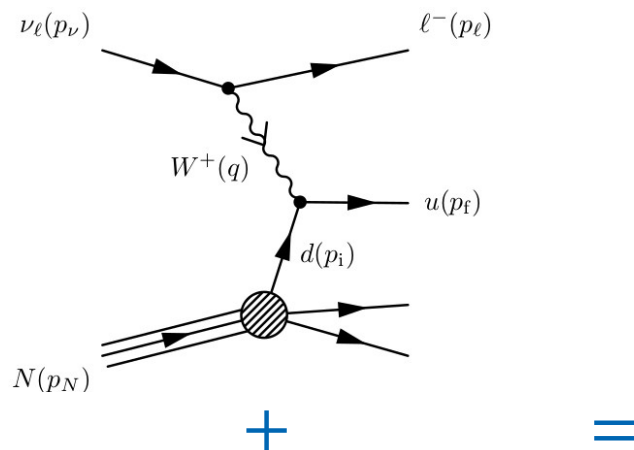


From colliders:
parton
distribution
functions

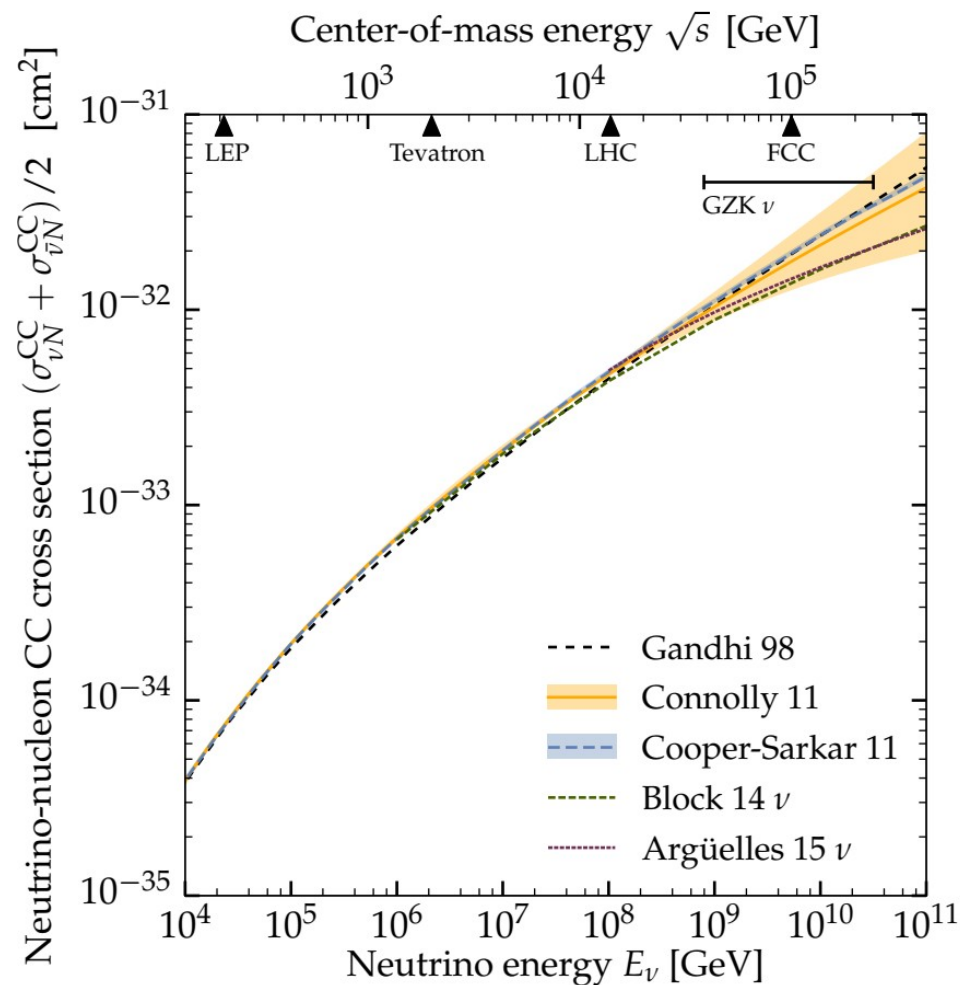
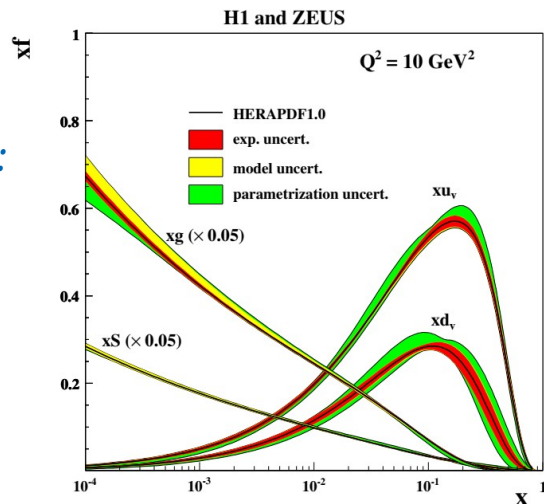


Extrapolating the cross section to high energies

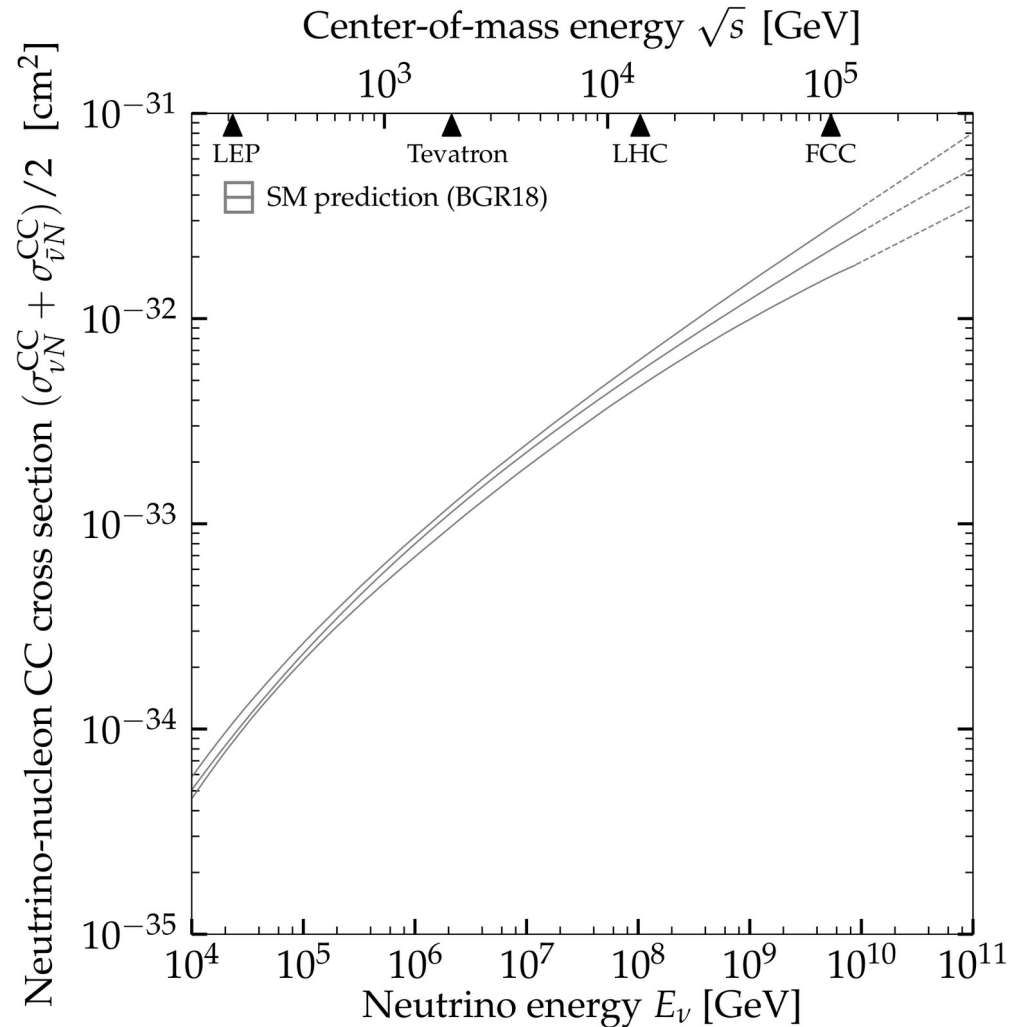
From theory:
Standard Model
neutrino-quark
cross section



From colliders:
parton
distribution
functions



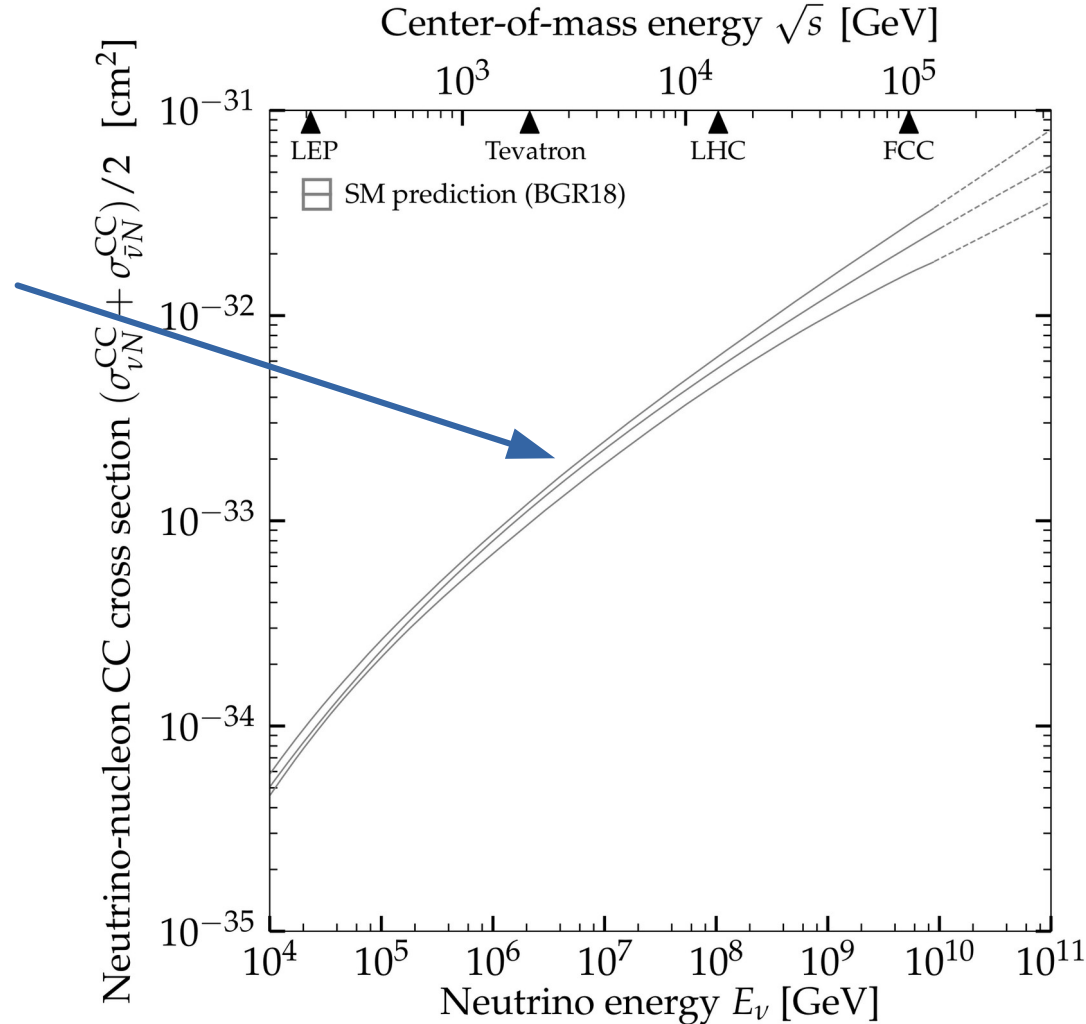
High-energy νN cross section: *prediction*



High-energy νN cross section: *prediction*

Softer-than-linear
dependence on E_ν
due to the W pole

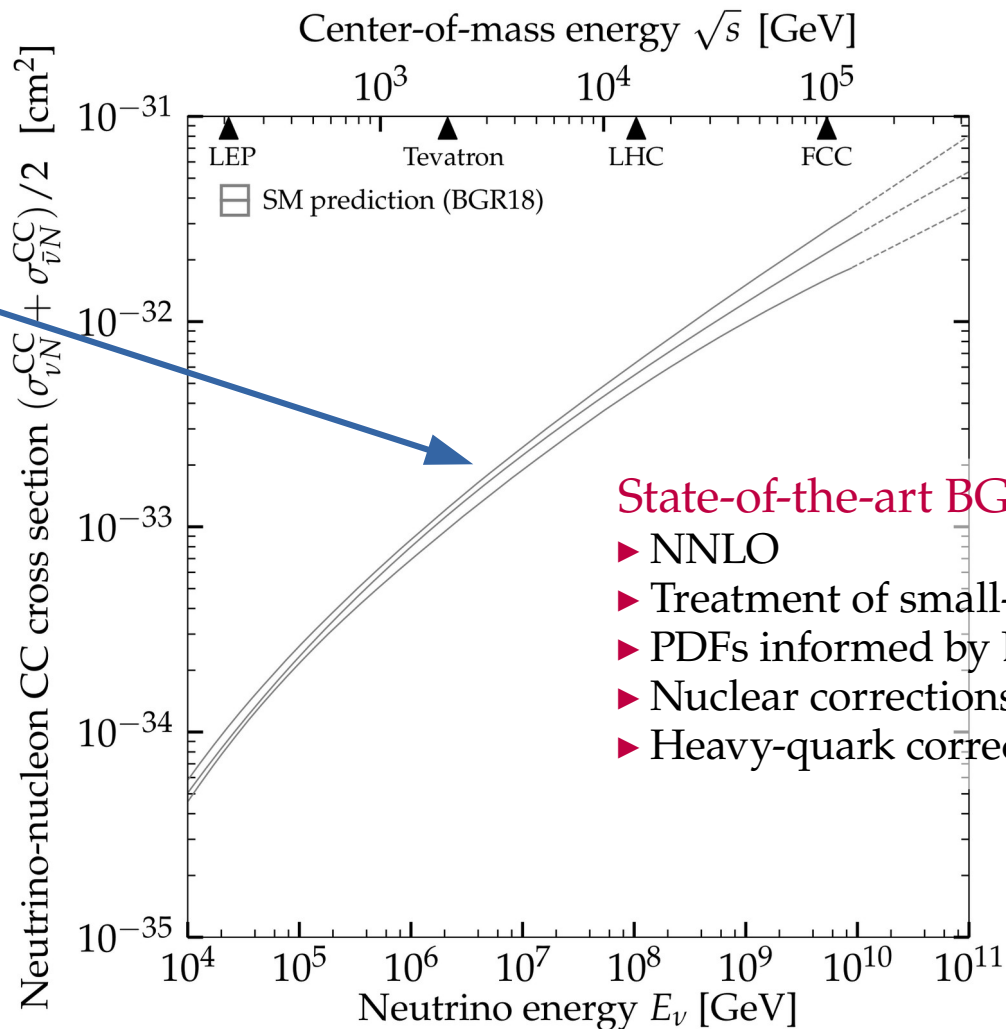
Uncertainty from
extrapolating parton
distribution functions
(PDFs) to Bjorken
 $x \sim m_W/E_\nu \sim 10^{-6}$



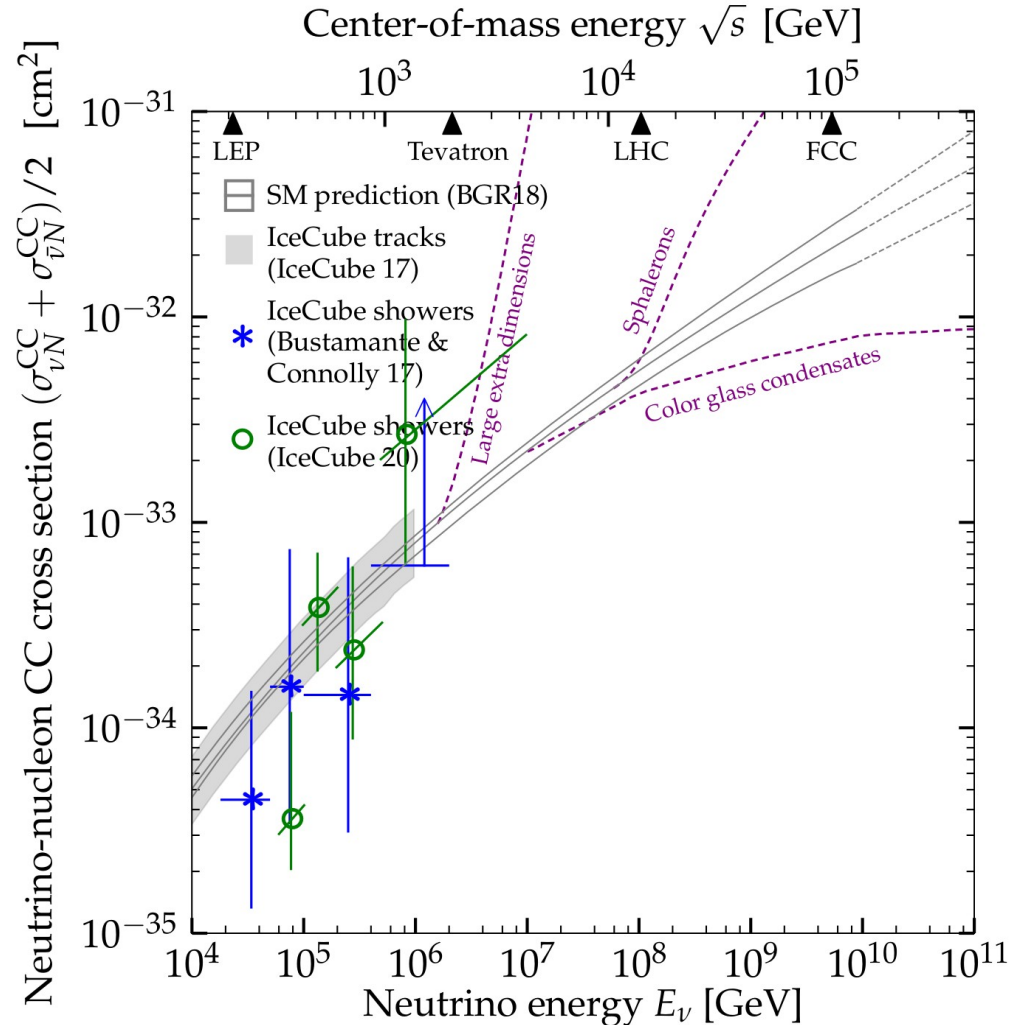
High-energy νN cross section: *prediction*

Softer-than-linear
dependence on E_ν
due to the W pole

Uncertainty from
extrapolating parton
distribution functions
(PDFs) to Bjorken
 $x \sim m_W/E_\nu \sim 10^{-6}$



High-energy νN cross section: *today*

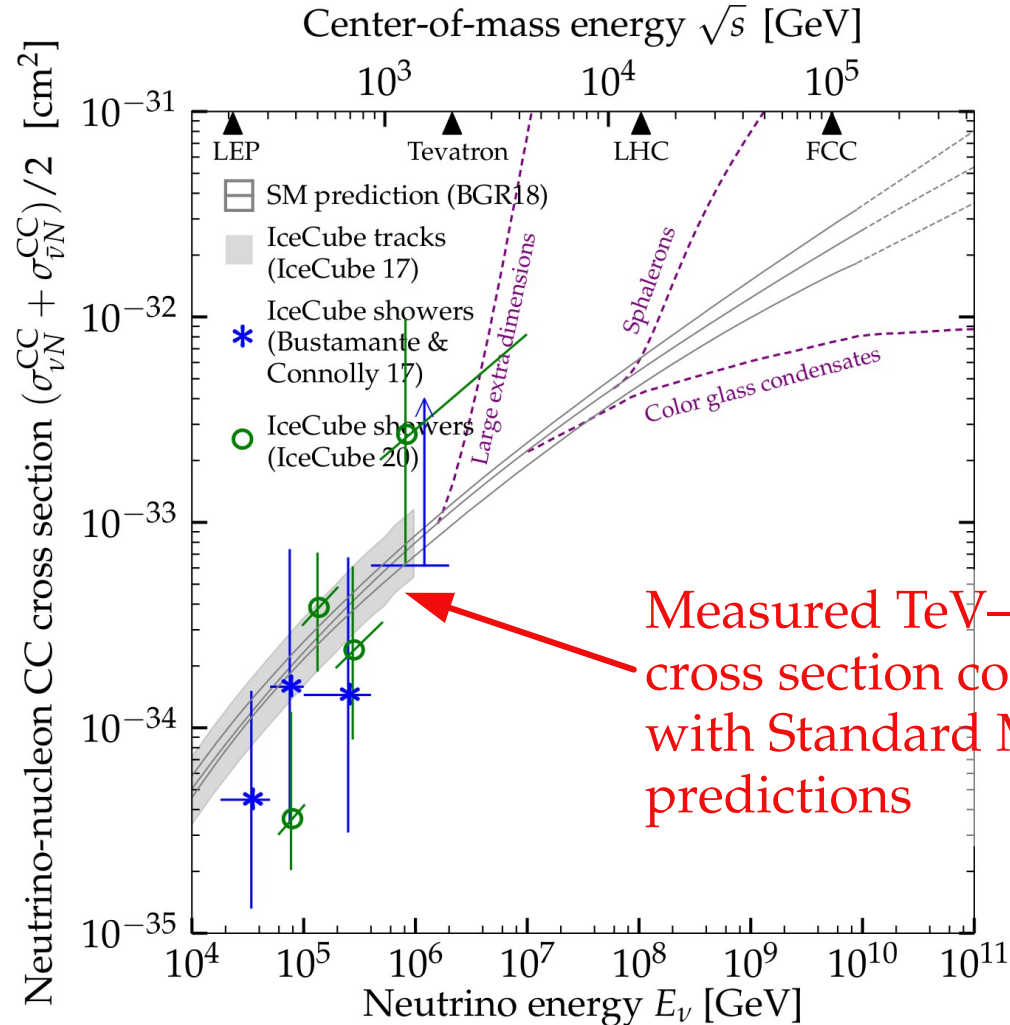


BGR18 prediction from:
Bertone, Gaud, Rojo, *JHEP* 2019

See also:
García, Gaud, Heijboer, Rojo, *JCAP* 2020

Measurements from:
IceCube, 2011.03560
MB & Connolly, *PRL* 2019
IceCube, *Nature* 2017

High-energy νN cross section: *today*

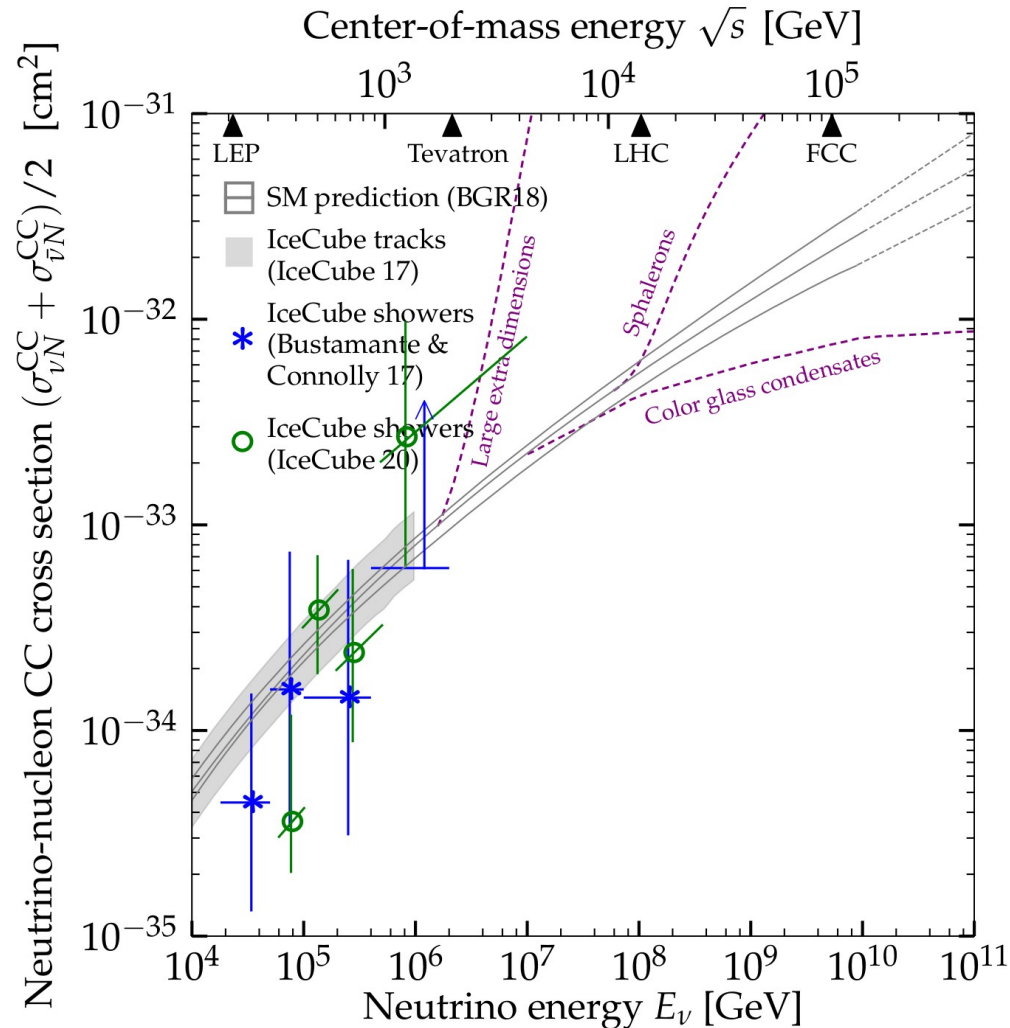


BGR18 prediction from:
Bertone, Gauld, Rojo, *JHEP* 2019

See also:
García, Gauld, Heijboer, Rojo, *JCAP* 2020

Measurements from:
IceCube, 2011.03560
MB & Connolly, *PRL* 2019
IceCube, *Nature* 2017

High-energy νN cross section: *today*



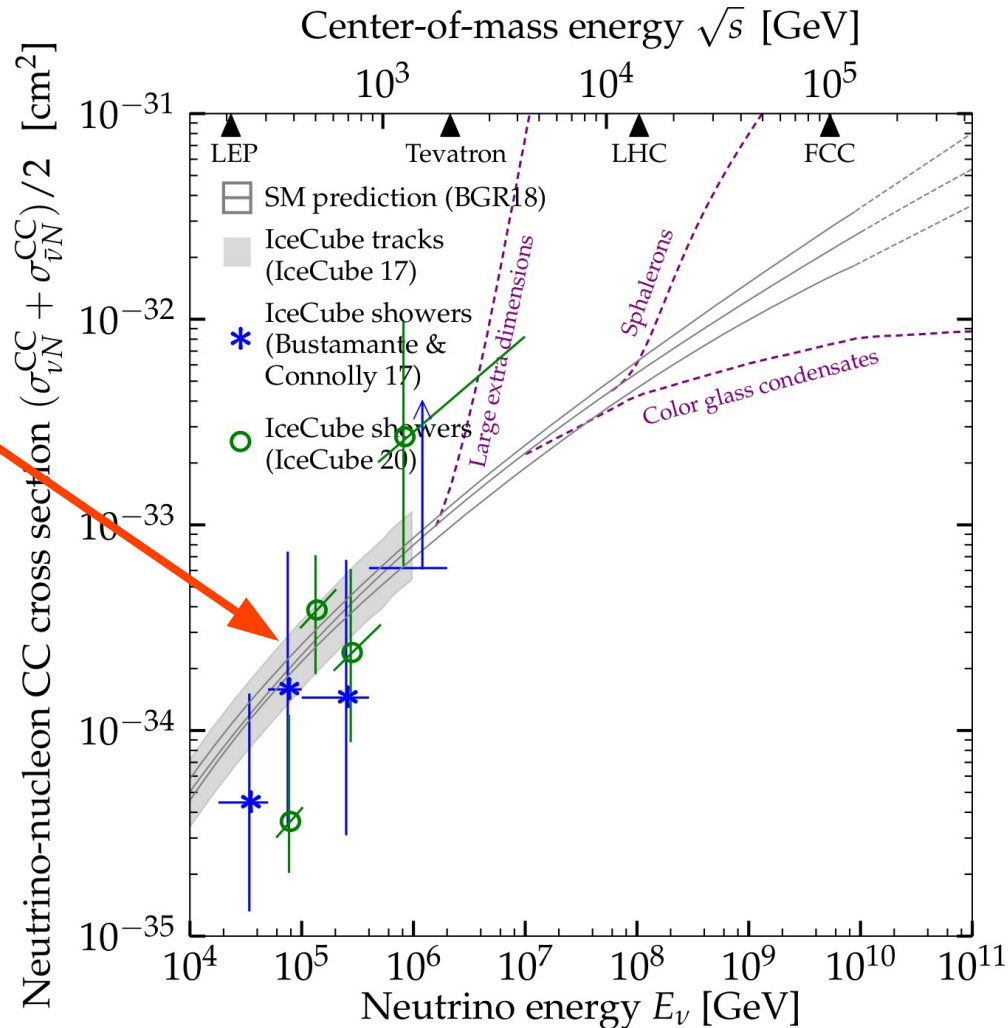
BGR18 prediction from:
[Bertone, Gauld, Rojo, JHEP 2019](#)

See also:
[García, Gauld, Heijboer, Rojo, JCAP 2020](#)

Measurements from:
[IceCube, 2011.03560](#)
[MB & Connolly, PRL 2019](#)
[IceCube, Nature 2017](#)

High-energy νN cross section: *today*

Measured:
TeV – PeV
cross section



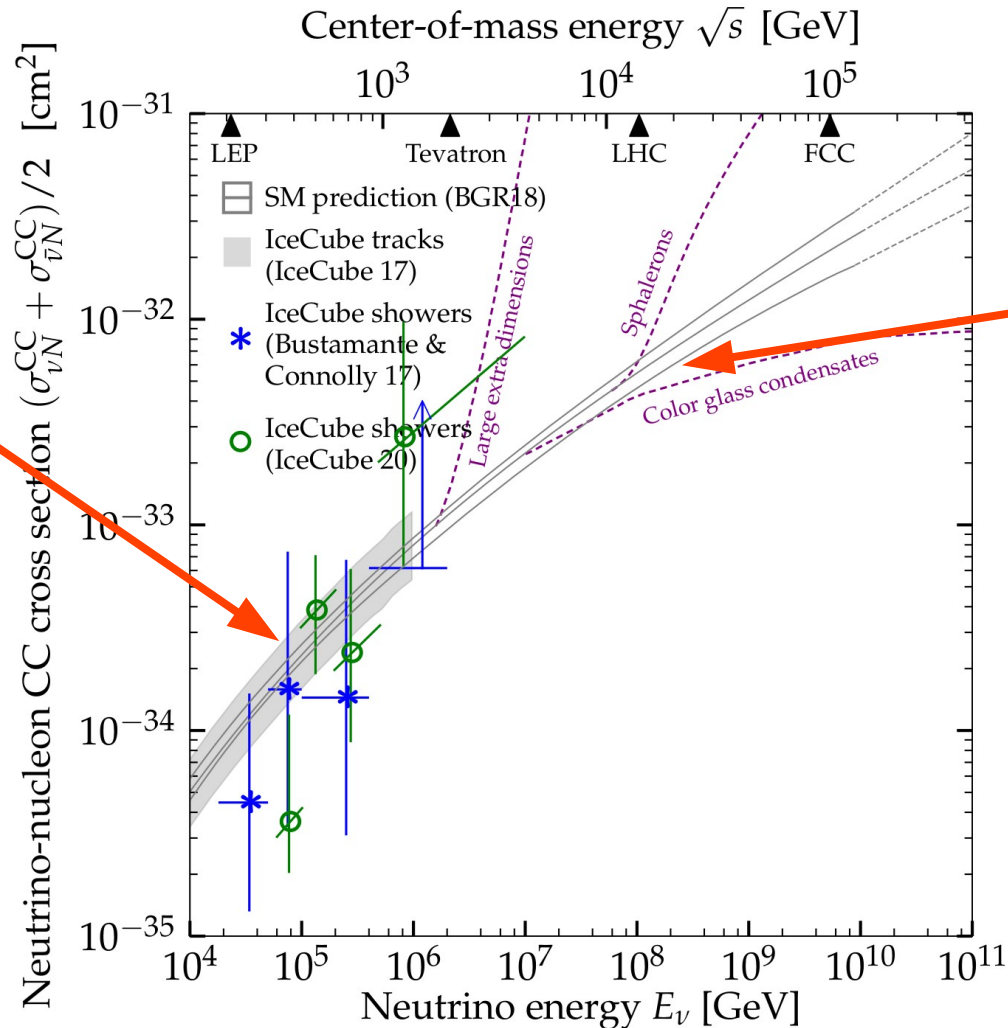
BGR18 prediction from:
[Bertone, Gauld, Rojo, JHEP 2019](#)

See also:
[García, Gauld, Heijboer, Rojo, JCAP 2020](#)

Measurements from:
[IceCube, 2011.03560](#)
[MB & Connolly, PRL 2019](#)
[IceCube, Nature 2017](#)

High-energy νN cross section: *today*

Measured:
TeV – PeV
cross section



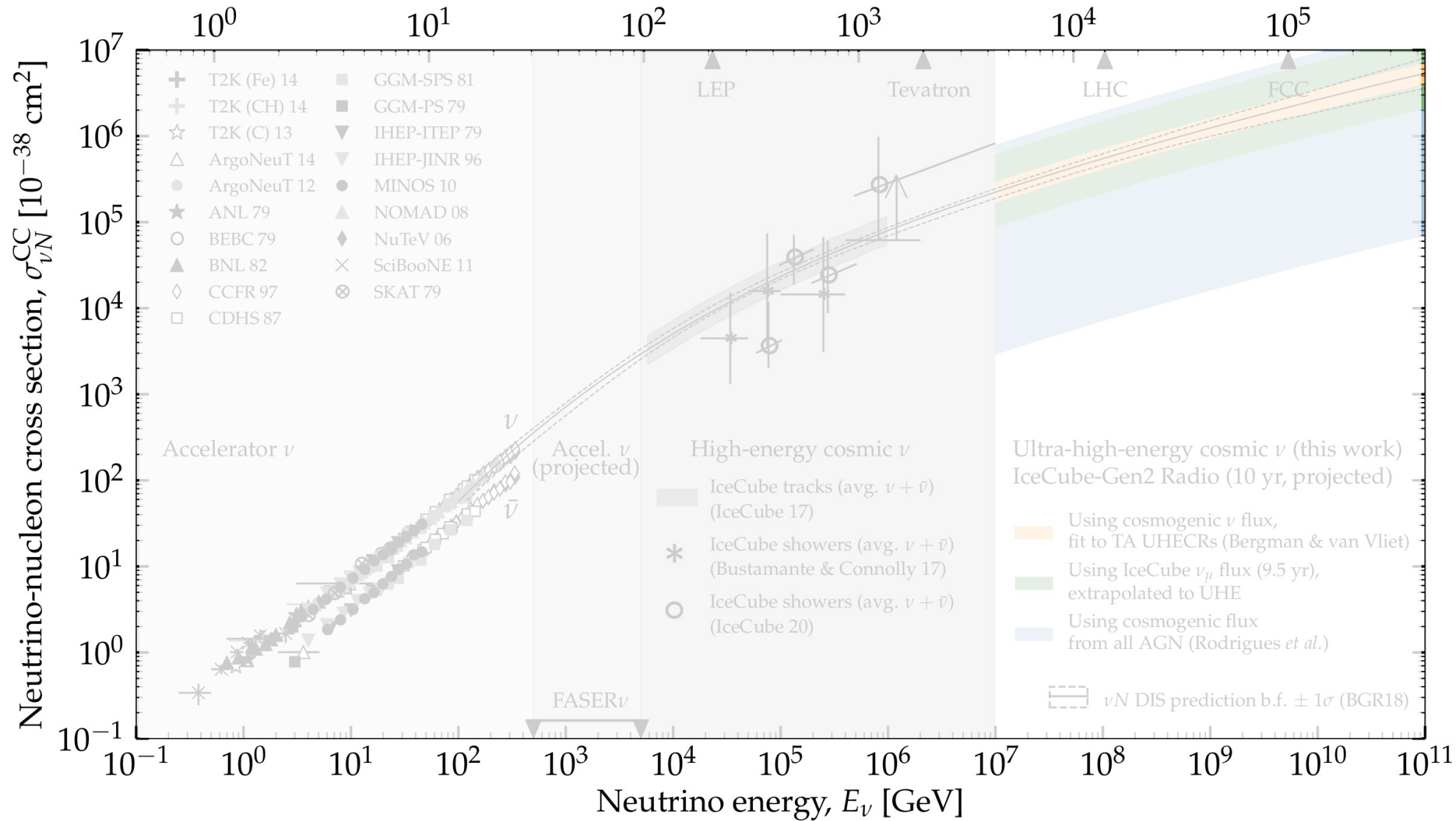
Not measured:
> 10-PeV
cross section

BGR18 prediction from:
[Bertone, Gauld, Rojo, JHEP 2019](#)

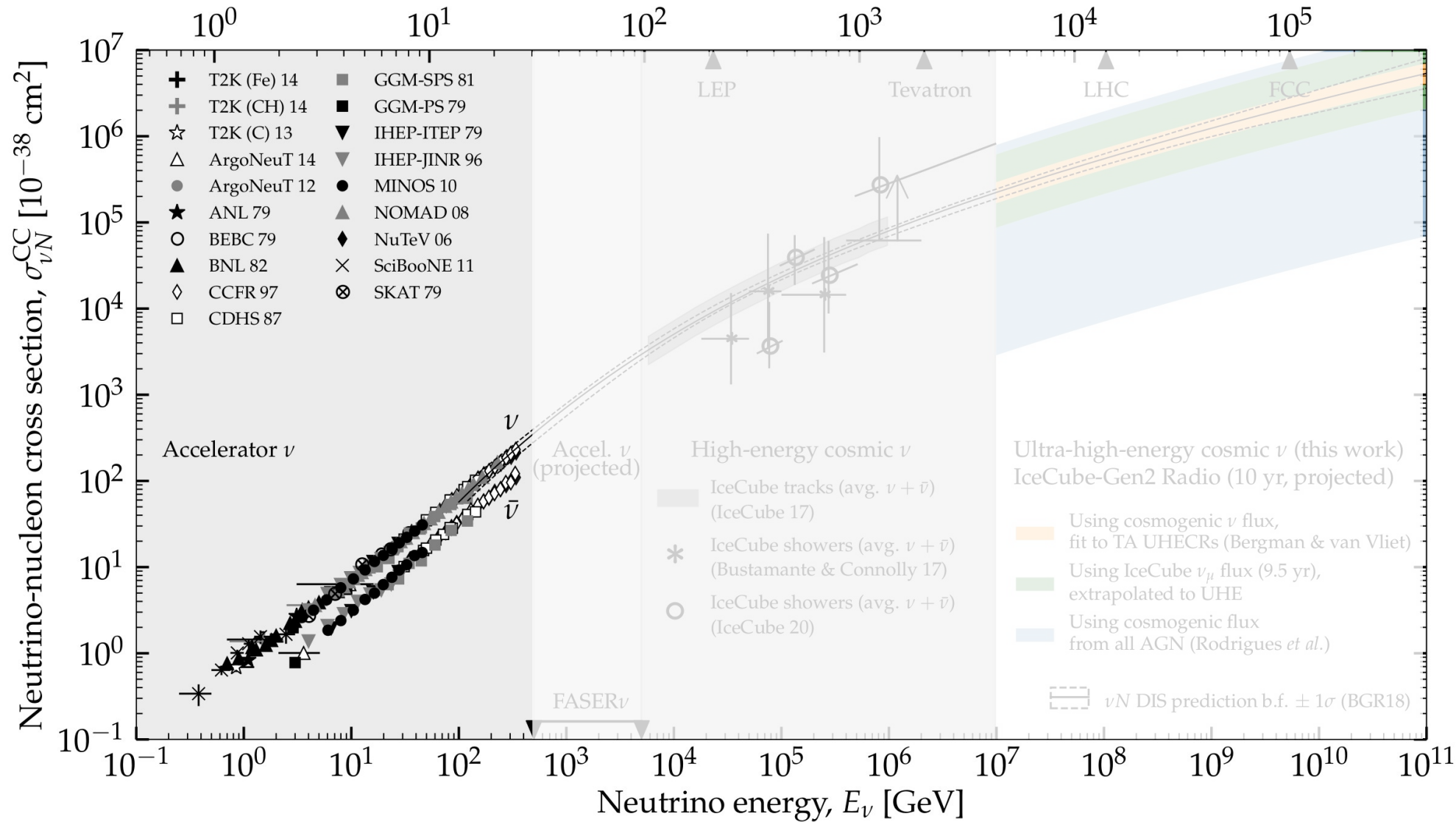
See also:
[García, Gauld, Heijboer, Rojo, JCAP 2020](#)

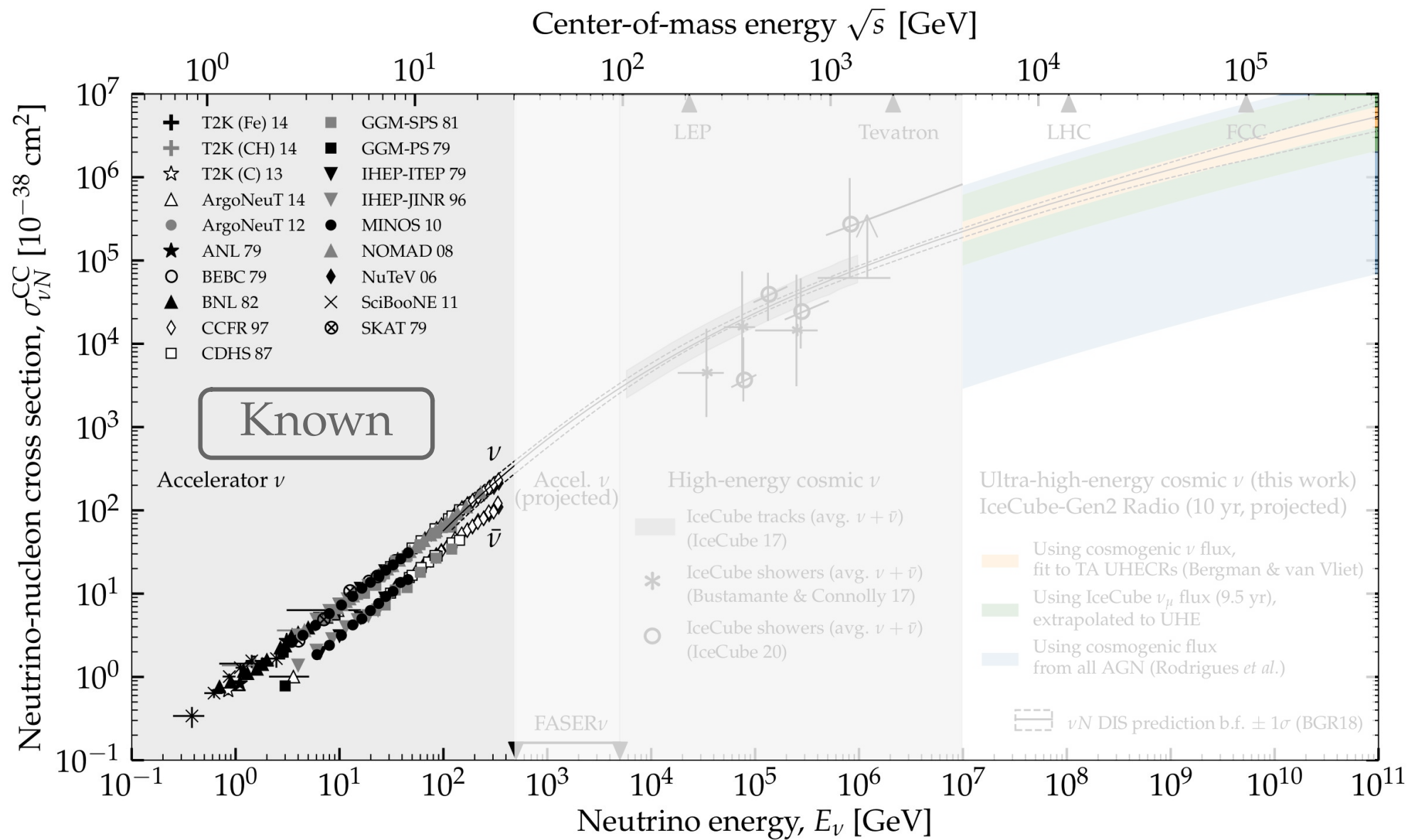
Measurements from:
[IceCube, 2011.03560](#)
[MB & Connolly, PRL 2019](#)
[IceCube, Nature 2017](#)

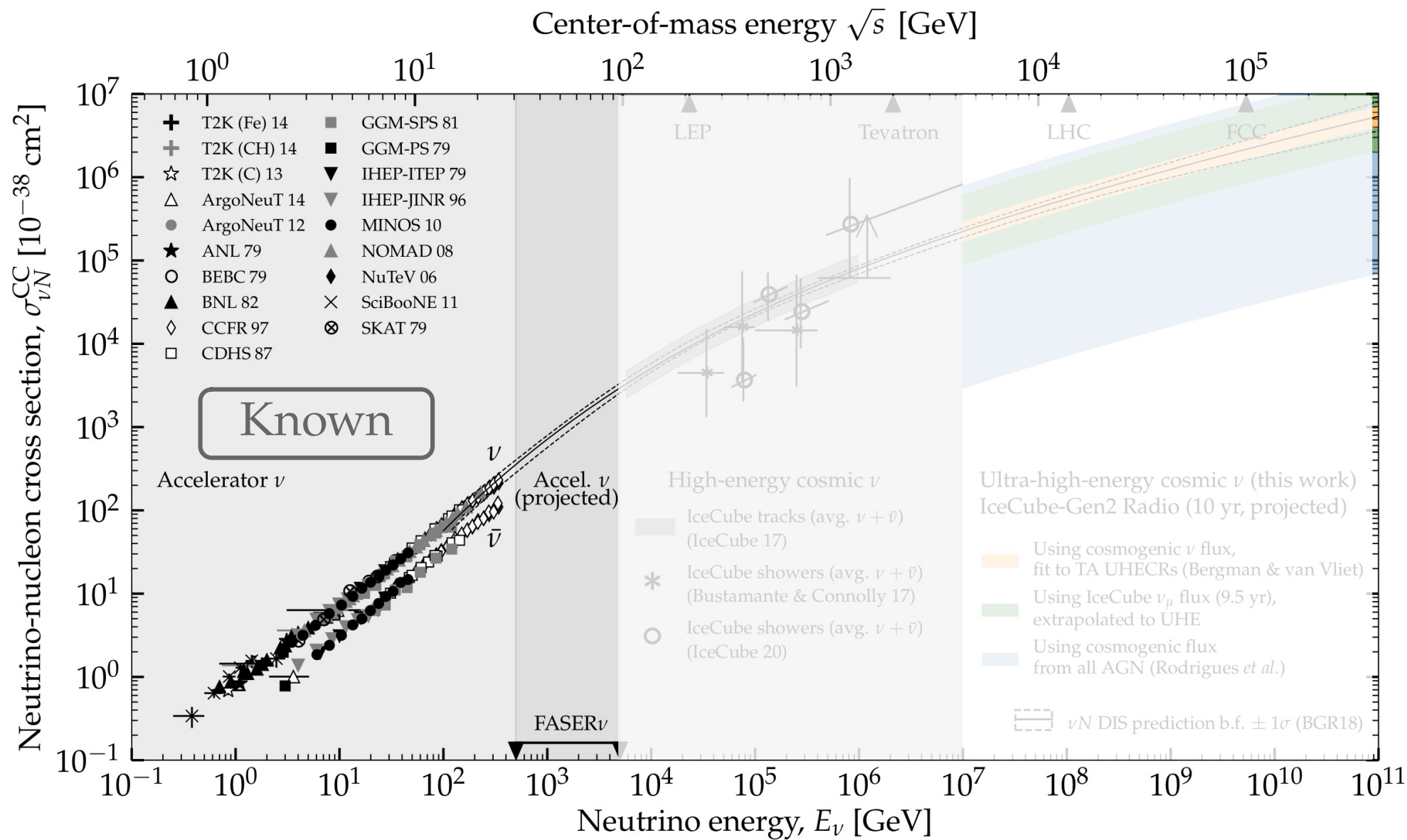
Center-of-mass energy \sqrt{s} [GeV]

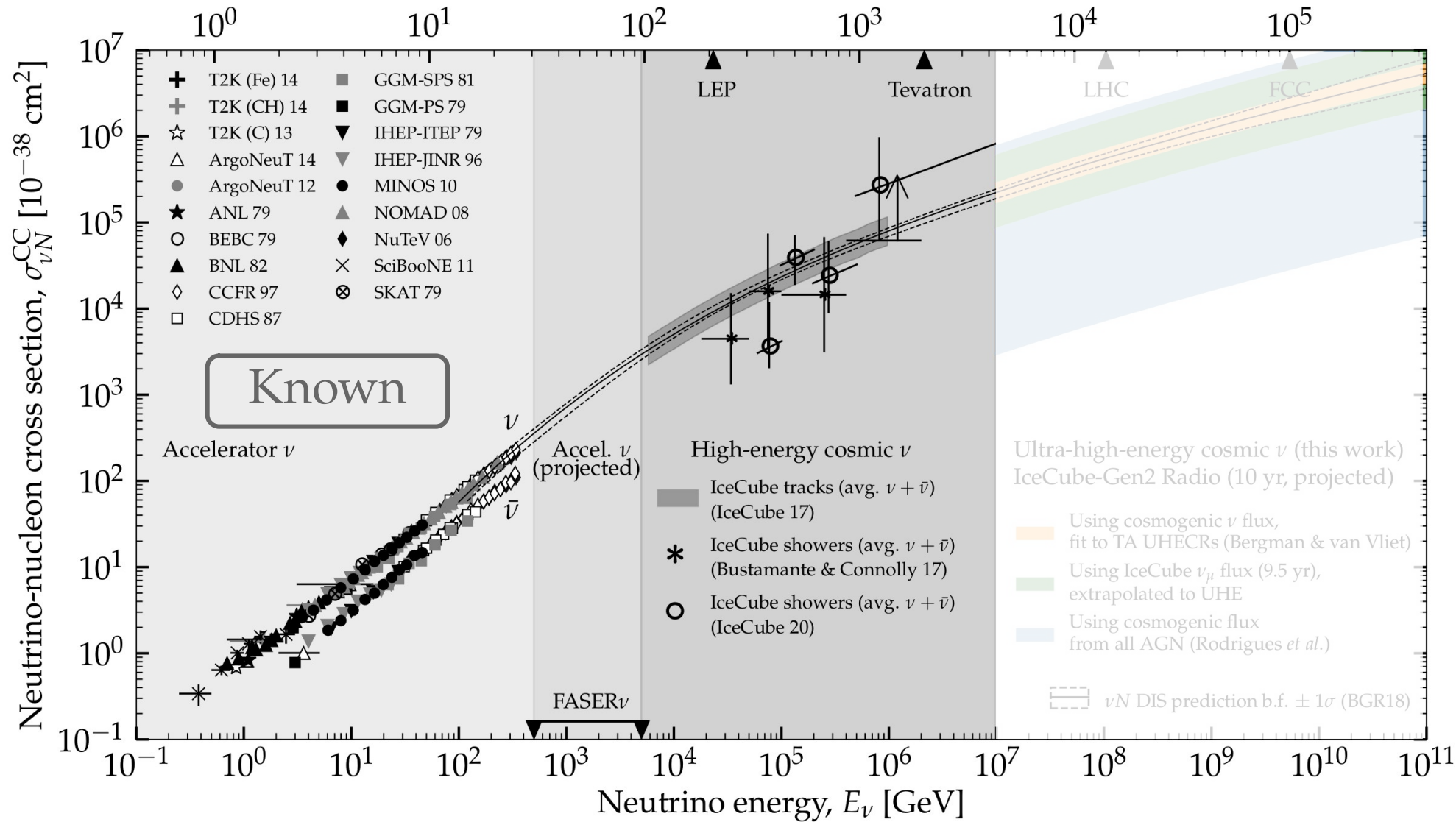


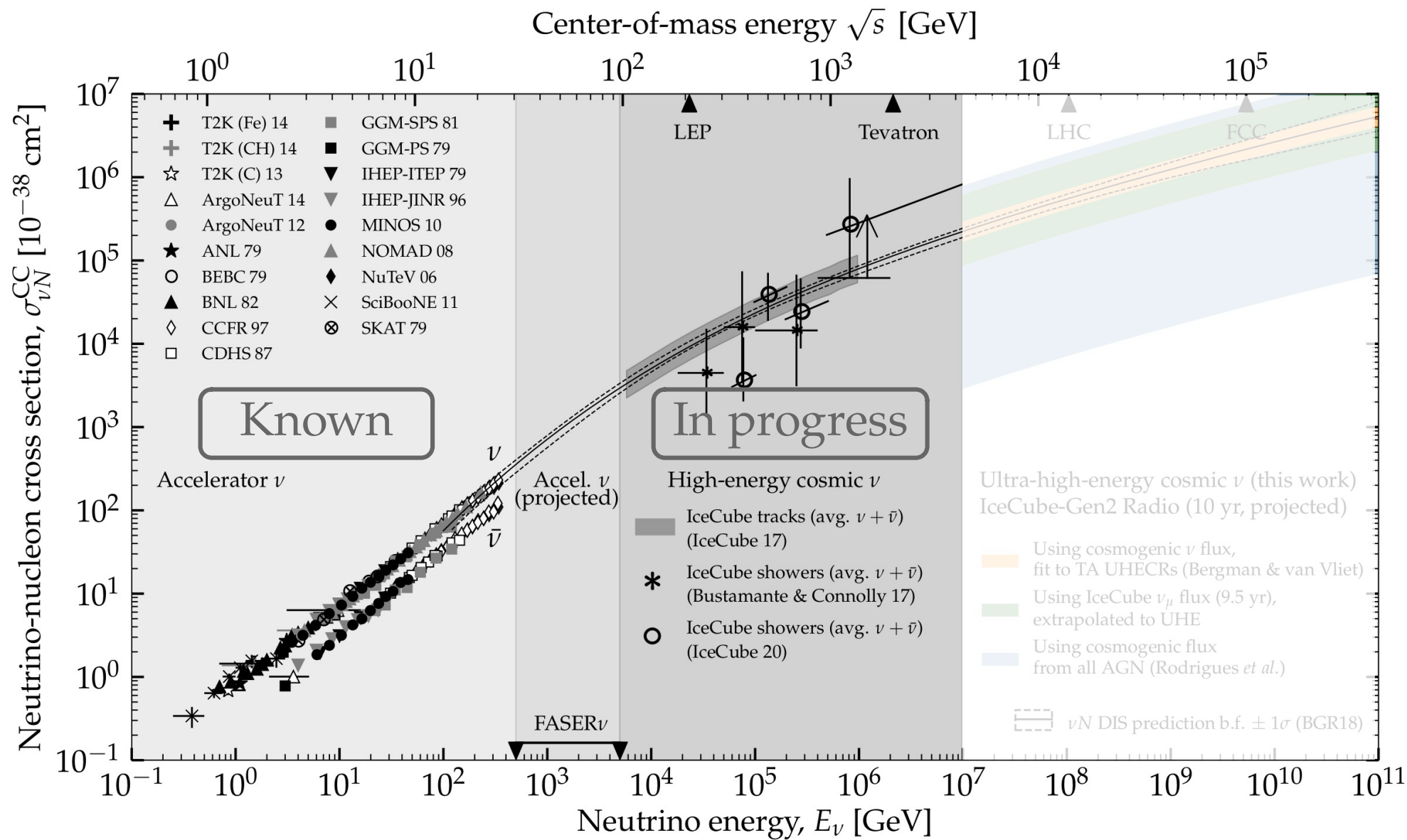
Center-of-mass energy \sqrt{s} [GeV]

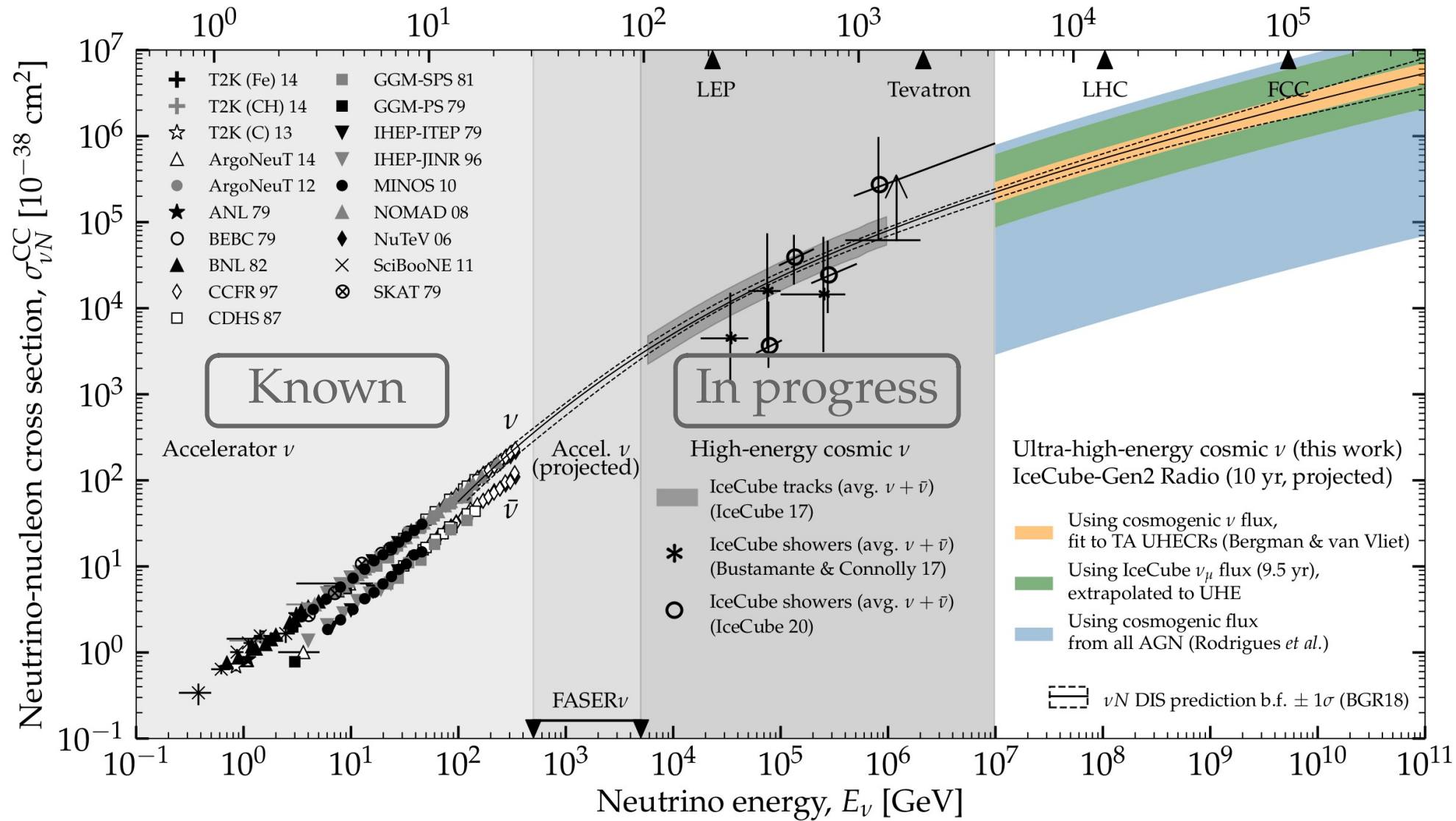




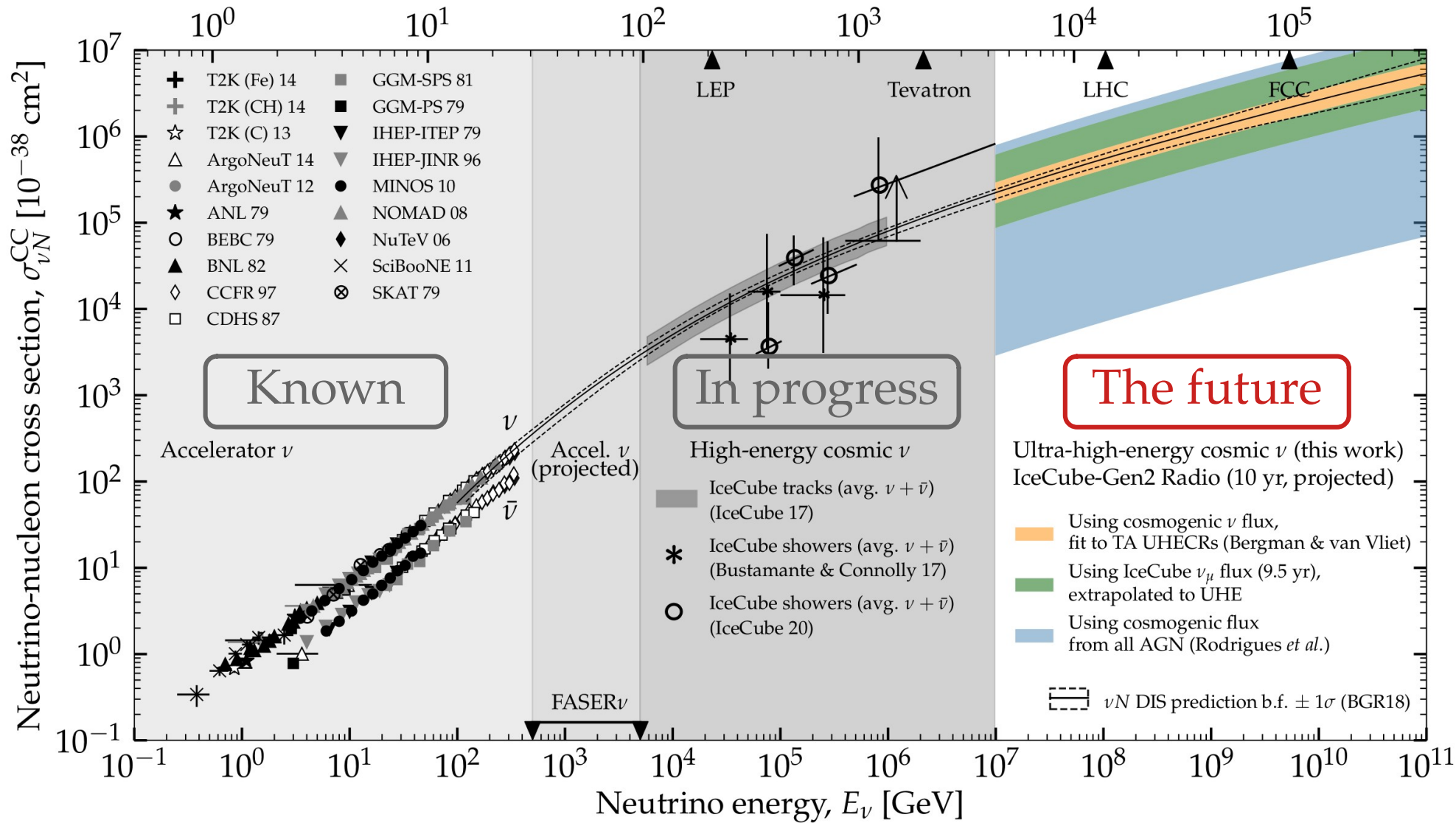


Center-of-mass energy \sqrt{s} [GeV]



Center-of-mass energy \sqrt{s} [GeV]

Center-of-mass energy \sqrt{s} [GeV]



Measuring high-energy neutrino-matter interactions

Why? Probe nucleons deeper than ever
 Search for new high-energy physics

Measuring high-energy neutrino-matter interactions

Why? Probe nucleons deeper than ever
 Search for new high-energy physics

How? Use high-energy & ultra-high-energy cosmic neutrinos
 Use the Earth as target

Measuring high-energy neutrino-matter interactions

Why? Probe nucleons deeper than ever
Search for new high-energy physics

How? Use high-energy & ultra-high-energy cosmic neutrinos
Use the Earth as target

When? With TeV–PeV ν : already now (IceCube)
With EeV ν : in 10–20 yr (IceCube-Gen2)[†]

Measuring high-energy neutrino-matter interactions

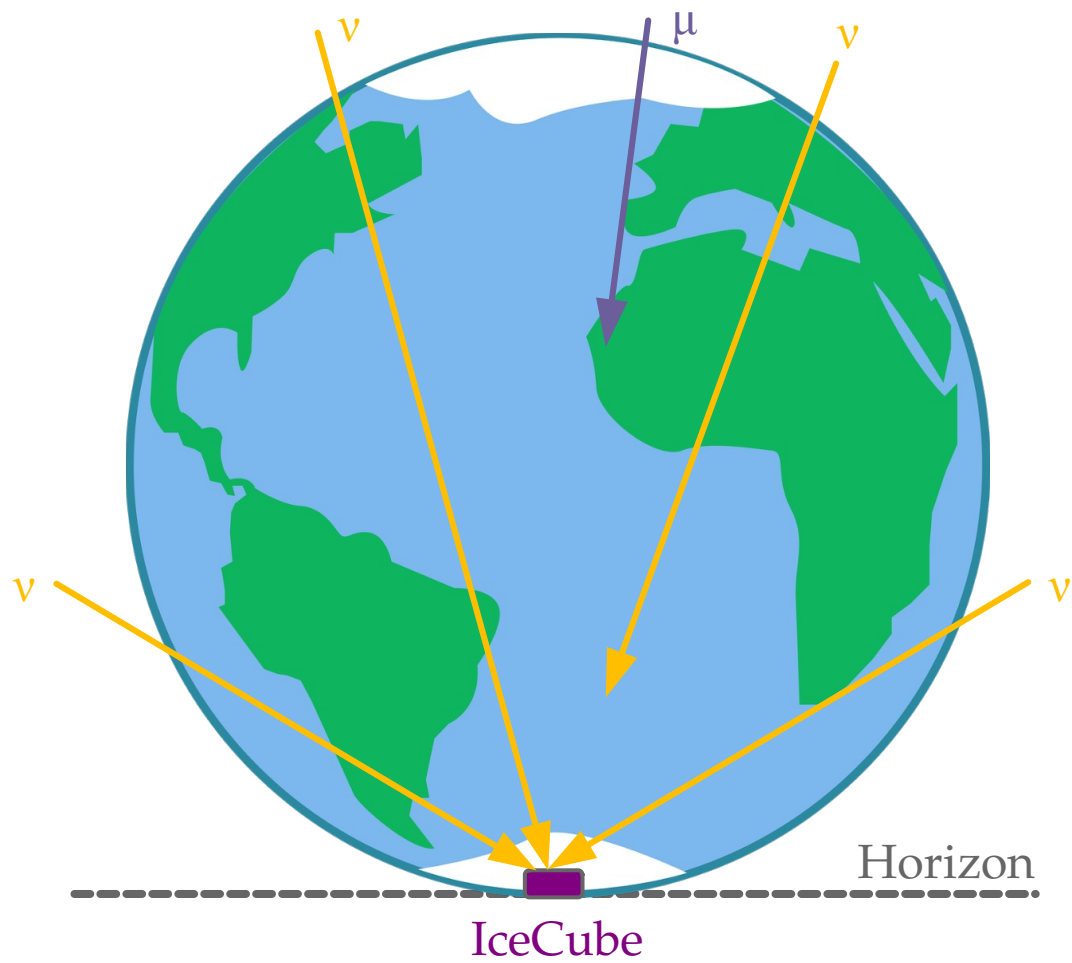
Why? Probe nucleons deeper than ever
Search for new high-energy physics

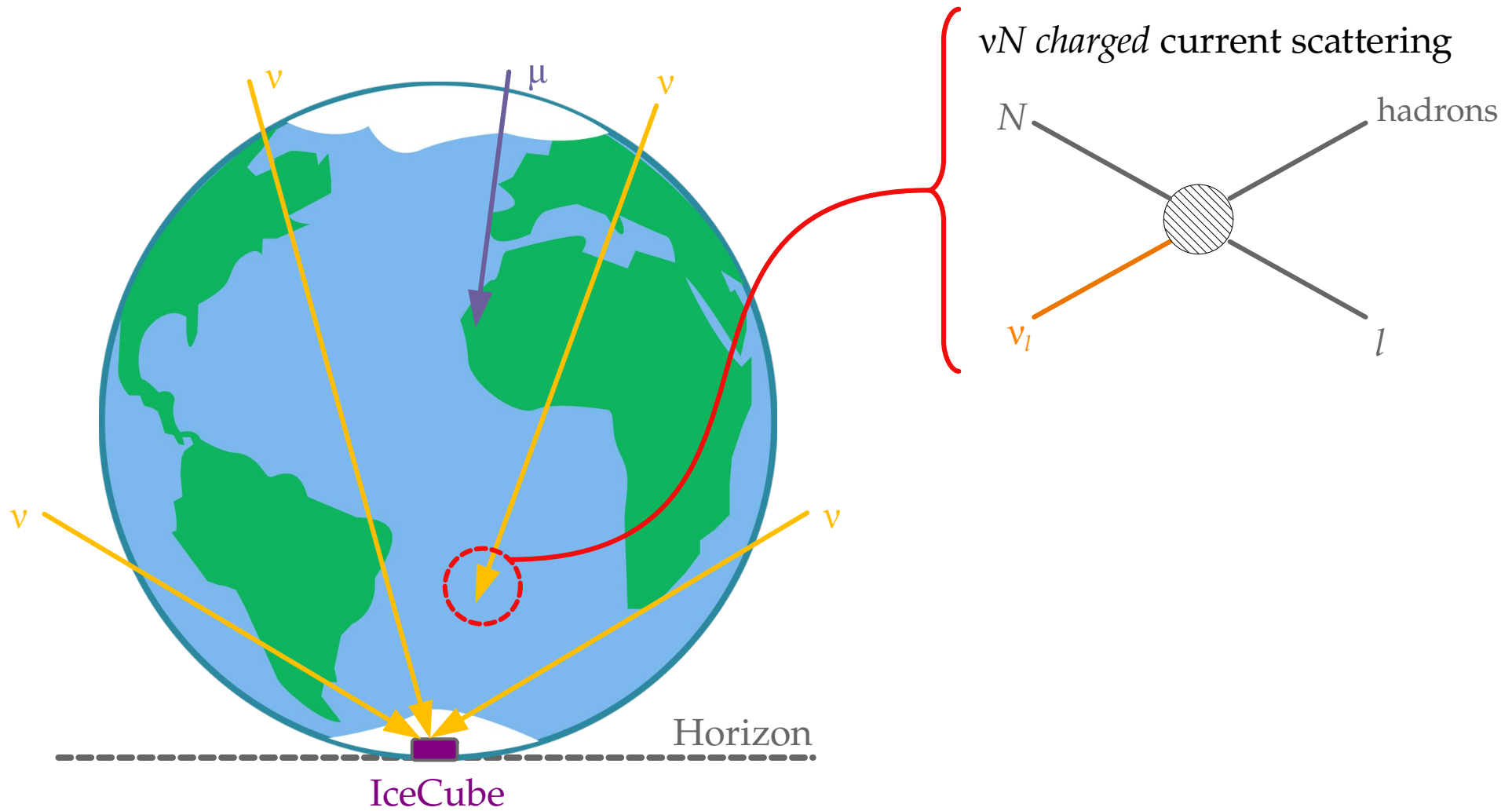
How? Use high-energy & ultra-high-energy cosmic neutrinos
Use the Earth as target

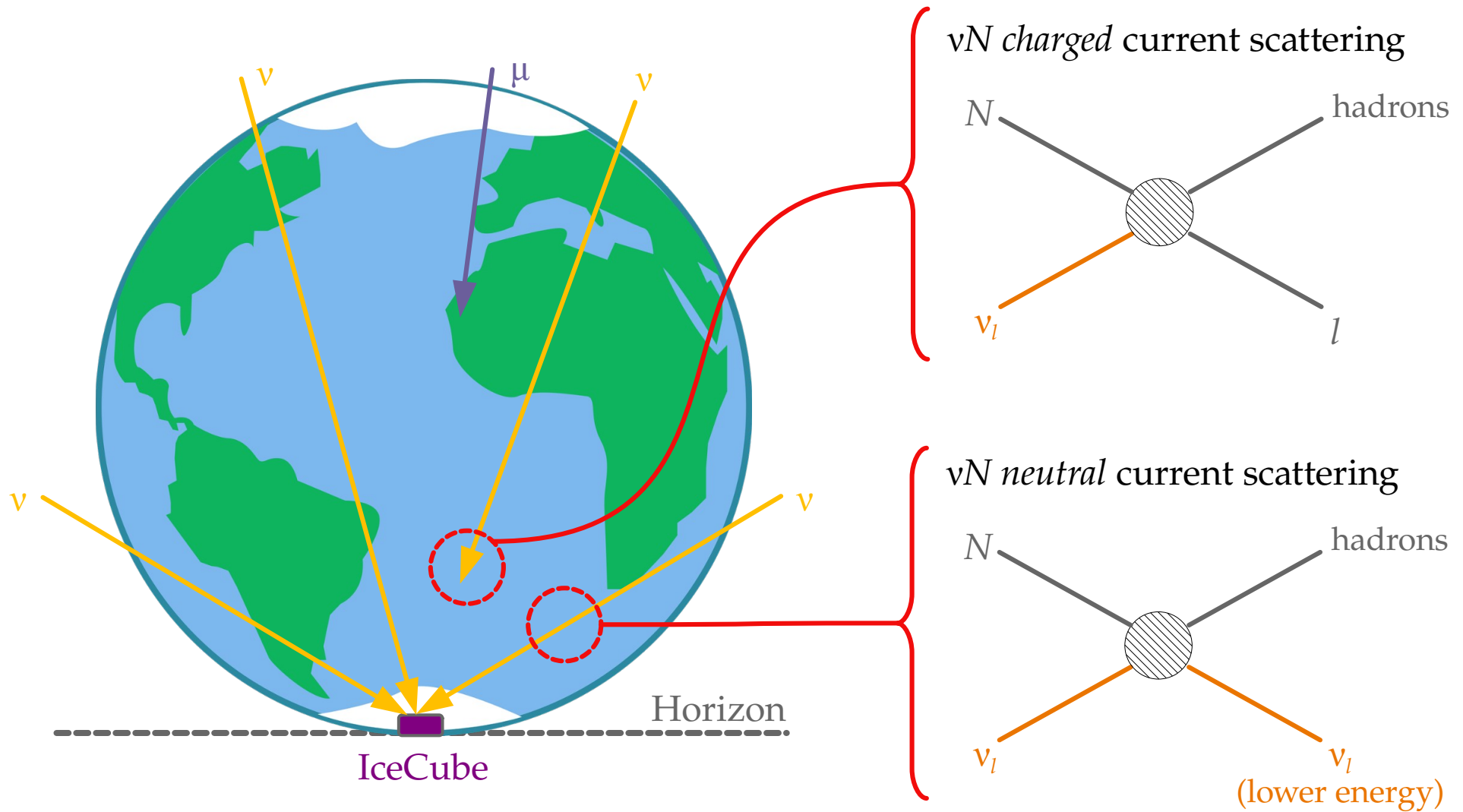
When? With TeV–PeV ν : already now (IceCube)
With EeV ν : in 10–20 yr (IceCube-Gen2)[†]

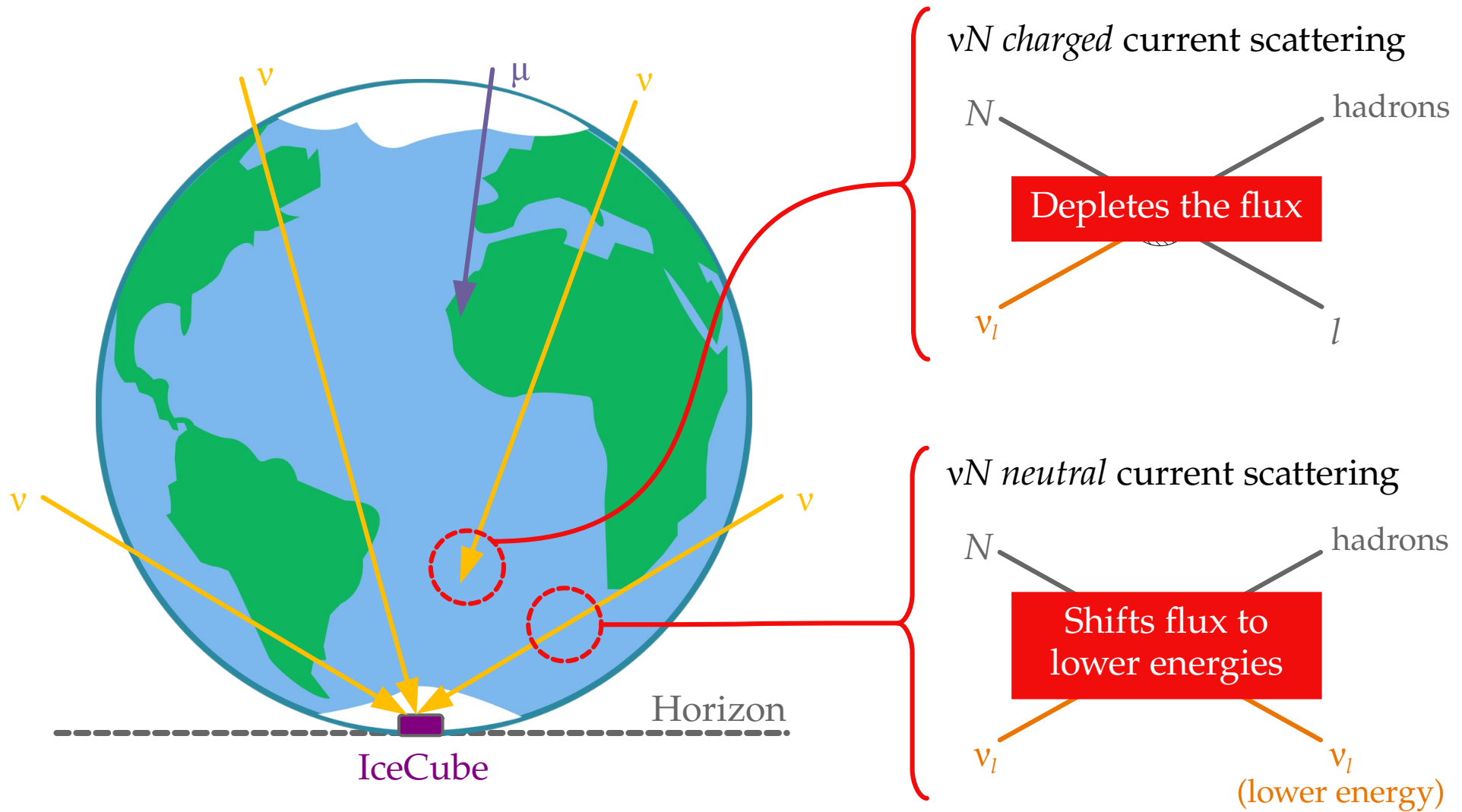
Why hard? Limited event statistics
At UHE, need to have decent angular resolution ($\sim 2^\circ$)

[†]Fingers crossed









Measuring the high-energy νN cross section

Number of detected neutrinos (simplified):

$$N \propto \underbrace{\Phi_\nu}_{\text{Neutrino flux}} \underbrace{\sigma_{\nu N}}_{\text{Cross section}} e^{-\tau_{\nu N}} = \Phi_\nu \sigma_{\nu N} e^{-L \sigma_{\nu N} n_N}$$

Measuring the high-energy νN cross section

Number of detected neutrinos (simplified):

$$N \propto \underbrace{\Phi_\nu}_{\text{Neutrino flux}} \underbrace{\sigma_{\nu N}}_{\text{Cross section}} e^{-\tau_{\nu N}} = \Phi_\nu \sigma_{\nu N} e^{-L \sigma_{\nu N} n_N}$$

Downgoing neutrinos
(L short \rightarrow no matter)

$$N \propto \Phi_\nu \sigma_{\nu N}$$

Measuring the high-energy νN cross section

Number of detected neutrinos (simplified):

$$N \propto \underbrace{\Phi_\nu}_{\text{Neutrino flux}} \underbrace{\sigma_{\nu N}}_{\text{Cross section}} e^{-\tau_{\nu N}} = \Phi_\nu \sigma_{\nu N} e^{-L \sigma_{\nu N} n_N}$$

Downgoing neutrinos
(L short \rightarrow no matter)

$$N \propto \underbrace{\Phi_\nu \sigma_{\nu N}}_{\text{Degeneracy}}$$

Measuring the high-energy νN cross section

Number of detected neutrinos (simplified):

$$N \propto \underbrace{\Phi_\nu}_{\text{Neutrino flux}} \underbrace{\sigma_{\nu N}}_{\text{Cross section}} e^{-\tau_{\nu N}} = \Phi_\nu \sigma_{\nu N} e^{-L \sigma_{\nu N} n_N}$$

Downgoing neutrinos
(L short \rightarrow no matter)

$$N \propto \underbrace{\Phi_\nu \sigma_{\nu N}}_{\text{Degeneracy}}$$

Upgoing neutrinos
(L long \rightarrow lots of matter)

$$N \propto \Phi_\nu \sigma_{\nu N} e^{-L \sigma_{\nu N} n_N}$$

Measuring the high-energy νN cross section

Number of detected neutrinos (simplified):

$$N \propto \underbrace{\Phi_\nu}_{\text{Neutrino flux}} \underbrace{\sigma_{\nu N}}_{\text{Cross section}} e^{-\tau_{\nu N}} = \Phi_\nu \sigma_{\nu N} e^{-L \sigma_{\nu N} n_N}$$

Downgoing neutrinos
(L short \rightarrow no matter)

$$N \propto \underbrace{\Phi_\nu \sigma_{\nu N}}_{\text{Degeneracy}}$$

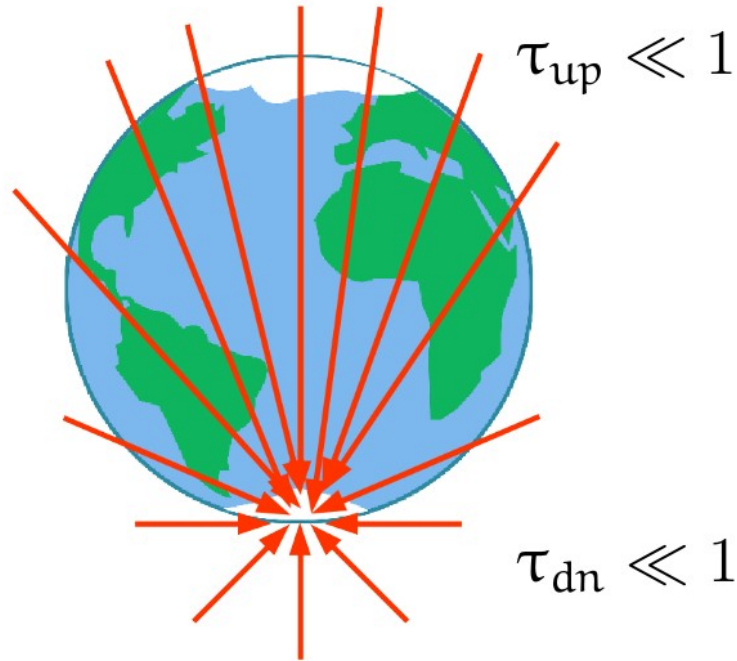
Upgoing neutrinos
(L long \rightarrow lots of matter)

$$N \propto \Phi_\nu \sigma_{\nu N} \underbrace{e^{-L \sigma_{\nu N} n_N}}_{\text{Breaks the degeneracy}}$$

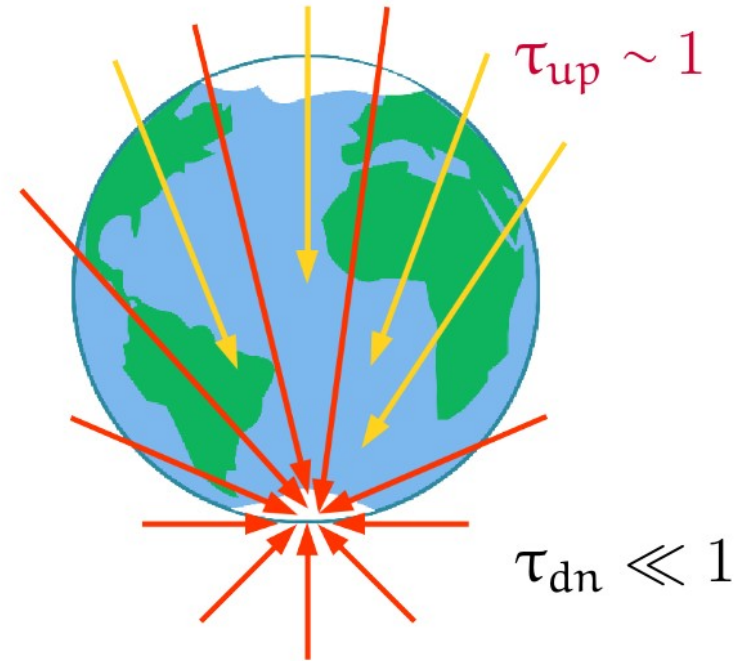
Measuring the high-energy νN cross section

$$\text{Optical depth to } \nu N \text{ int's} = \frac{\text{Distance from Earth's surface to IceCube}}{\text{Mean free path inside Earth}} \equiv \tau(E_\nu, \theta_z) \propto \sigma_{\nu N}$$

Below ~ 10 TeV: Earth is transparent



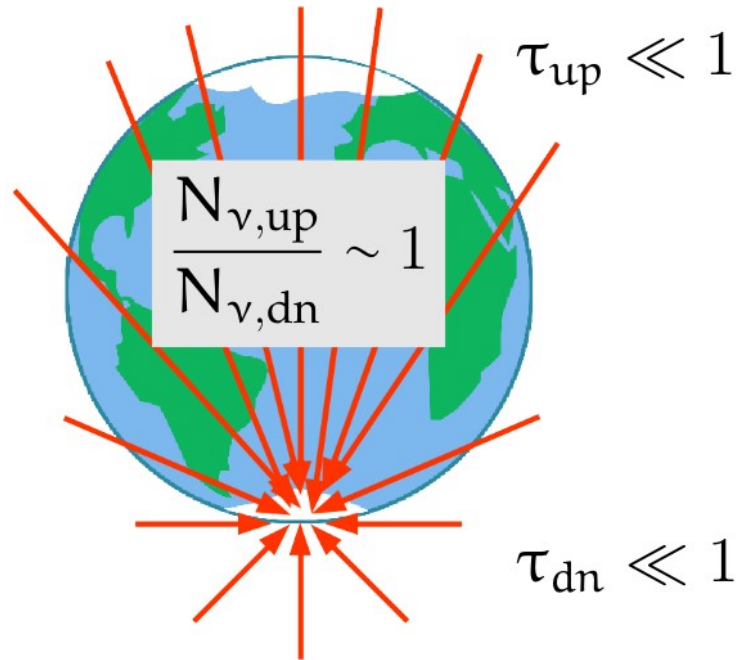
Above ~ 10 TeV: Earth is opaque



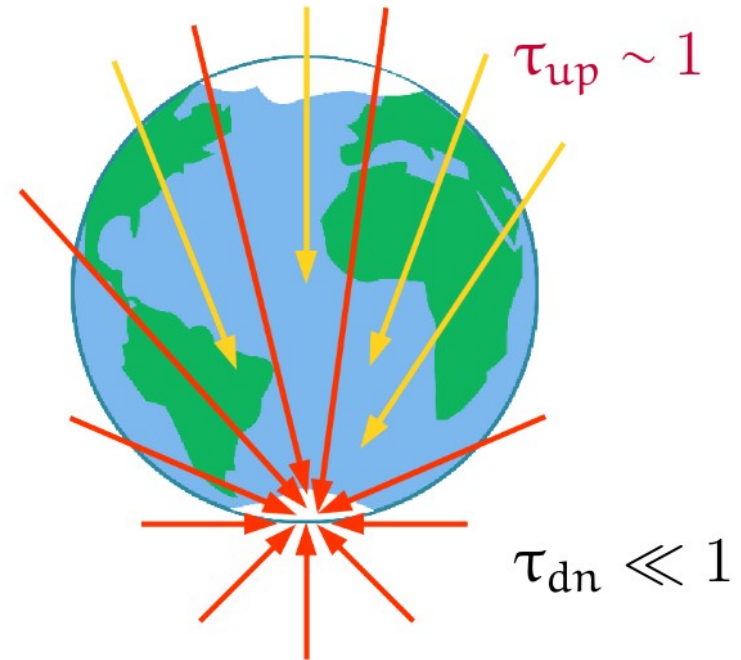
Measuring the high-energy νN cross section

$$\text{Optical depth to } \nu N \text{ int's} = \frac{\text{Distance from Earth's surface to IceCube}}{\text{Mean free path inside Earth}} \equiv \tau(E_\nu, \theta_z) \propto \sigma_{\nu N}$$

Below ~ 10 TeV: Earth is transparent



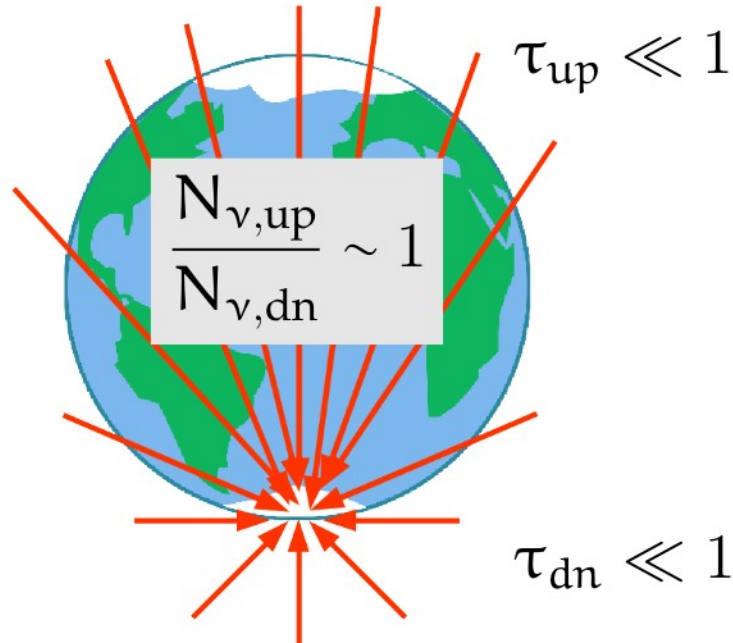
Above ~ 10 TeV: Earth is opaque



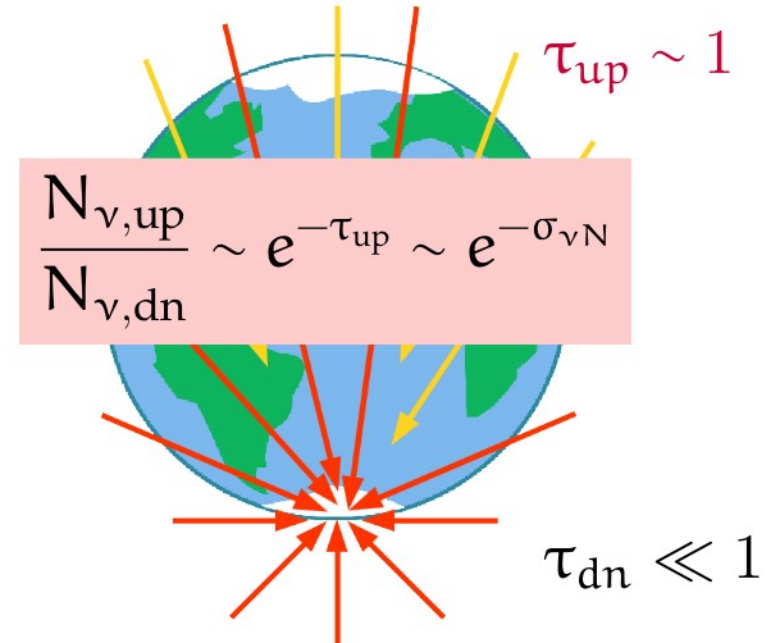
Measuring the high-energy νN cross section

$$\text{Optical depth to } \nu N \text{ int's} = \frac{\text{Distance from Earth's surface to IceCube}}{\text{Mean free path inside Earth}} \equiv \tau(E_\nu, \theta_z) \propto \sigma_{\nu N}$$

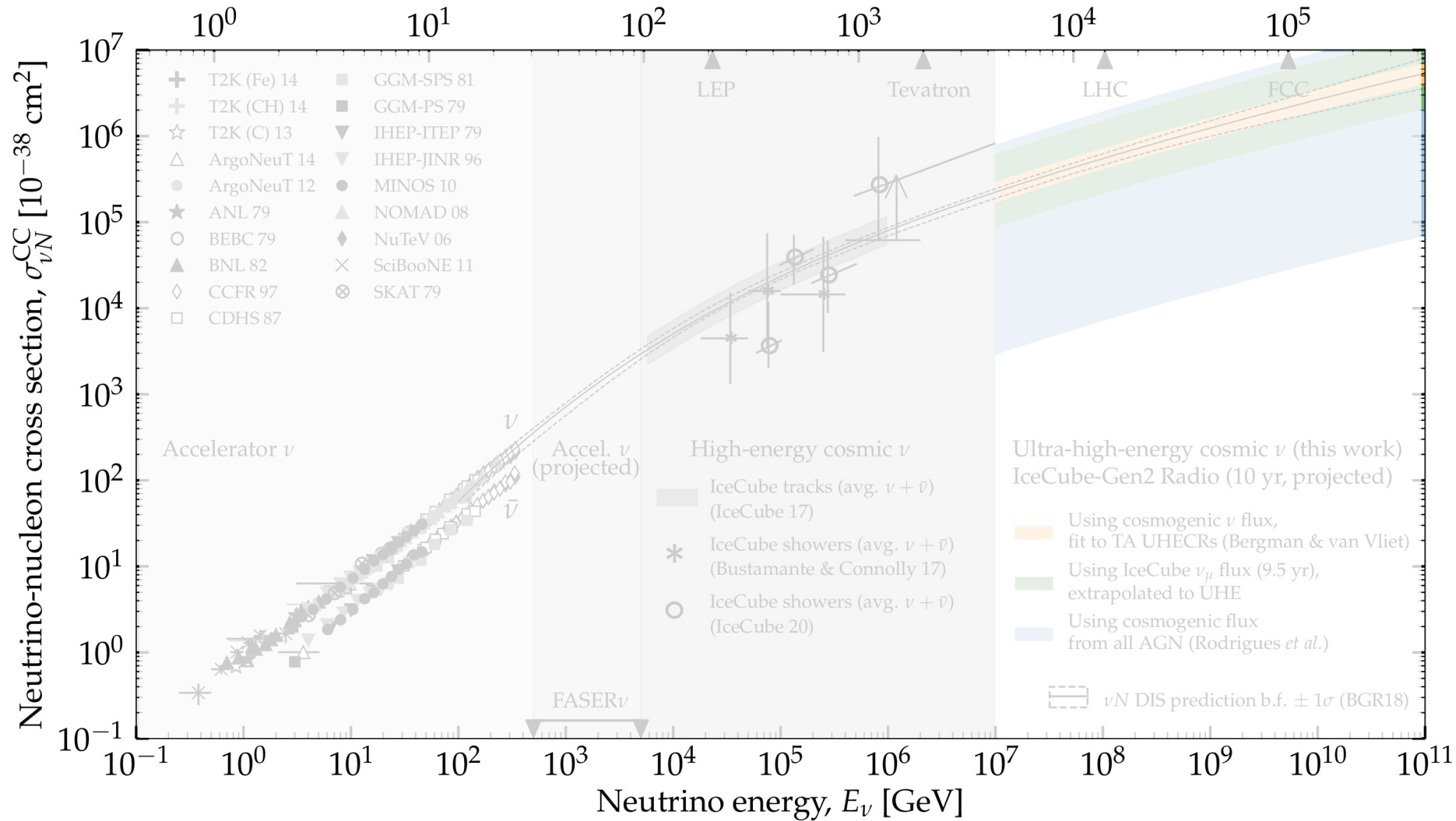
Below ~ 10 TeV: Earth is transparent

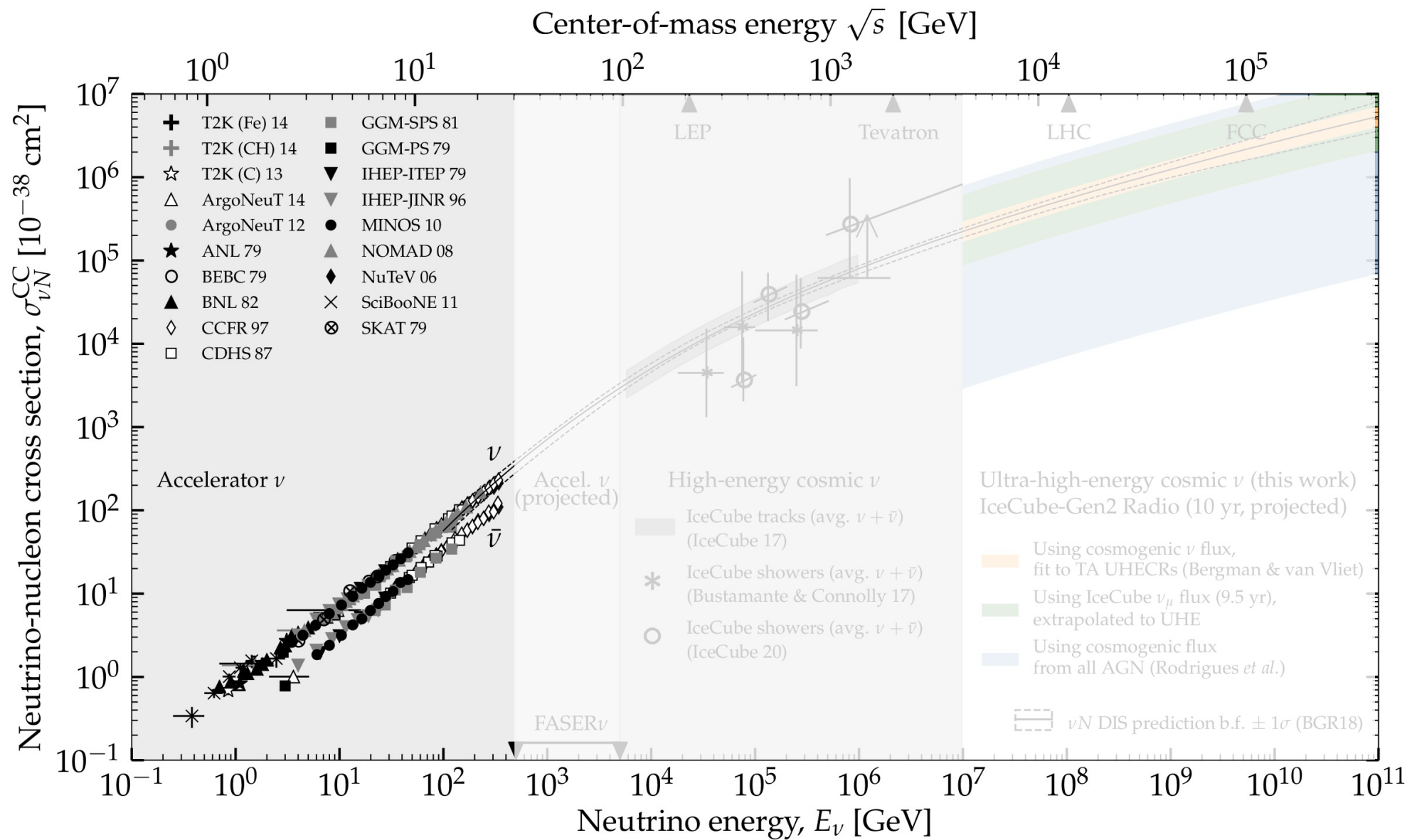


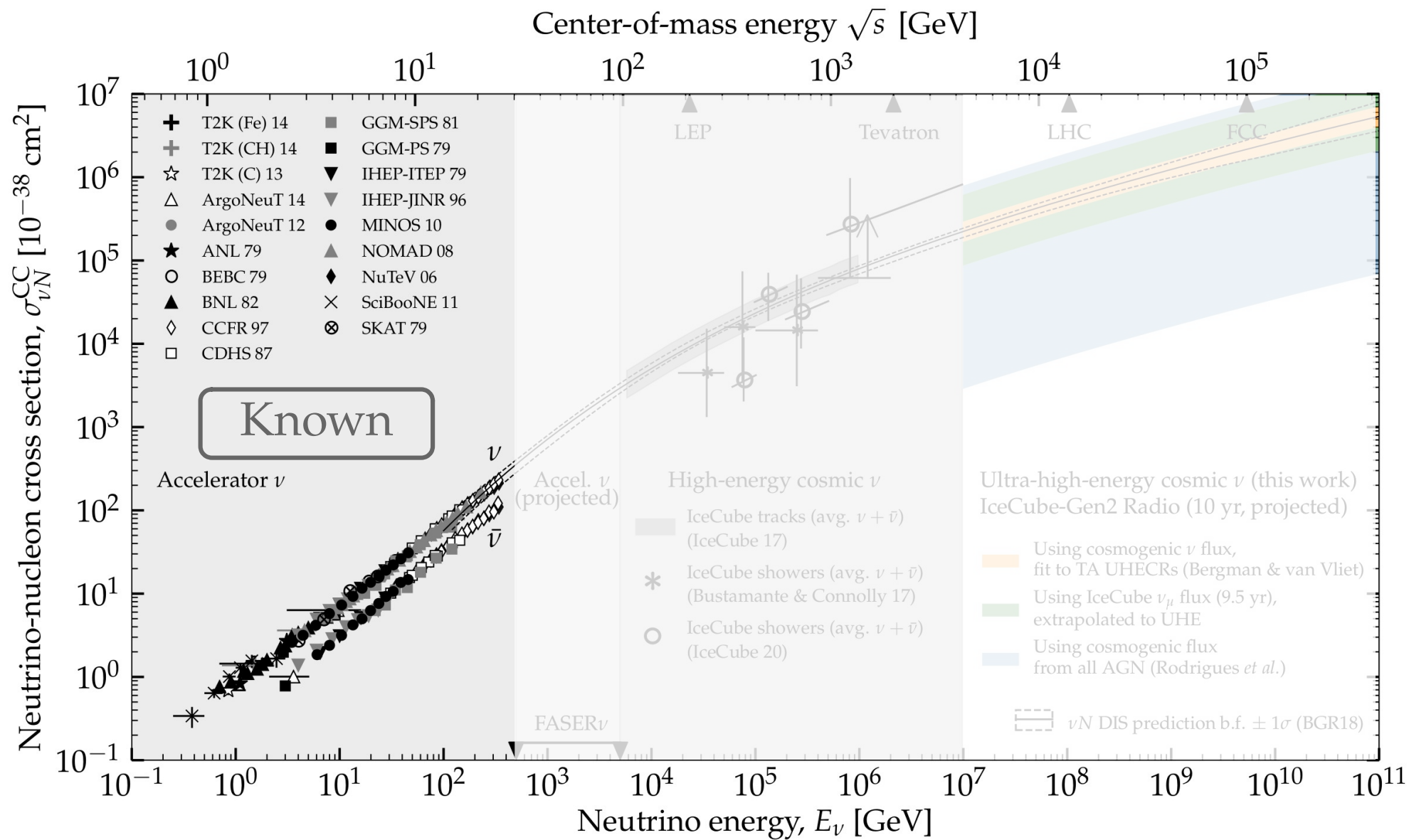
Above ~ 10 TeV: Earth is opaque

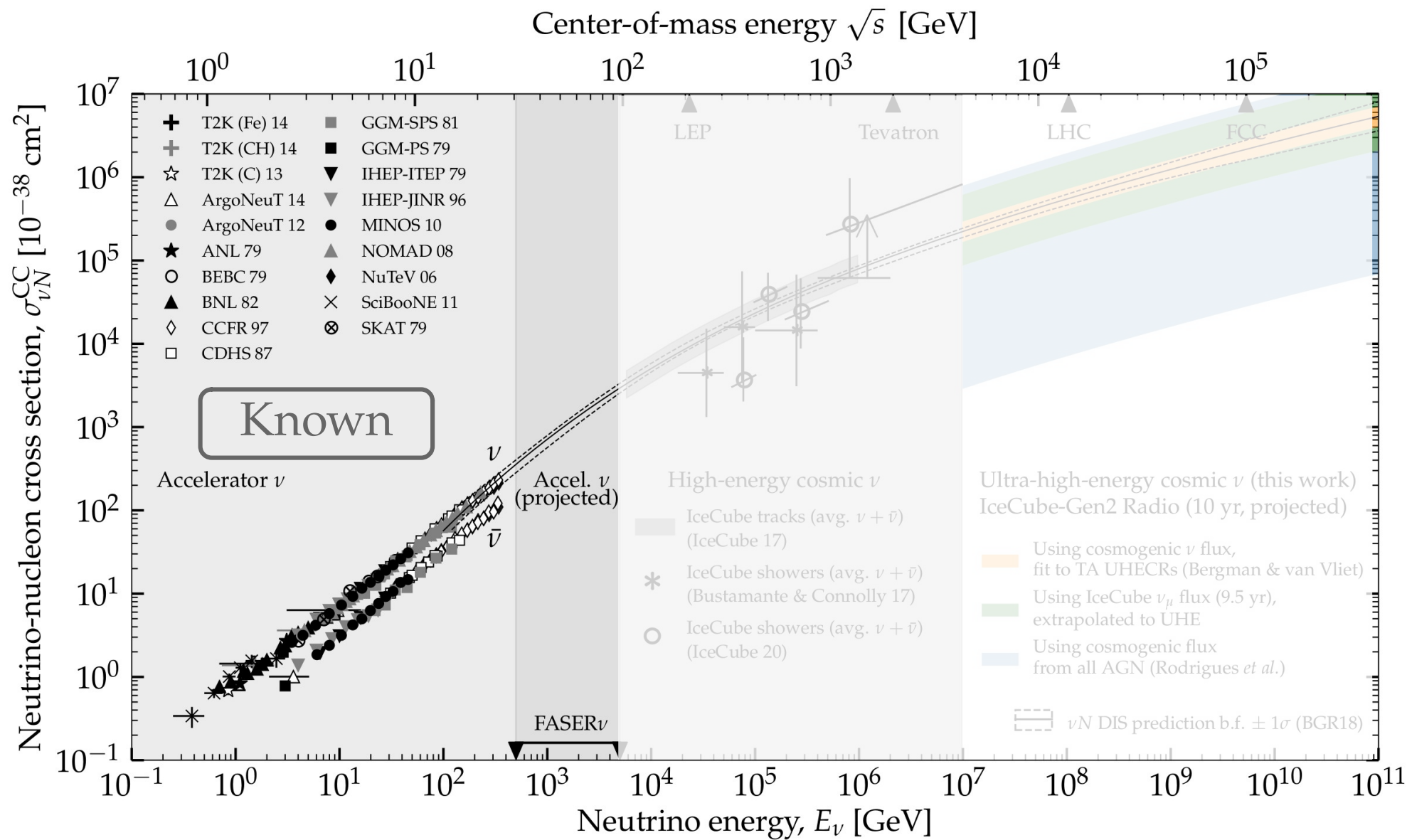


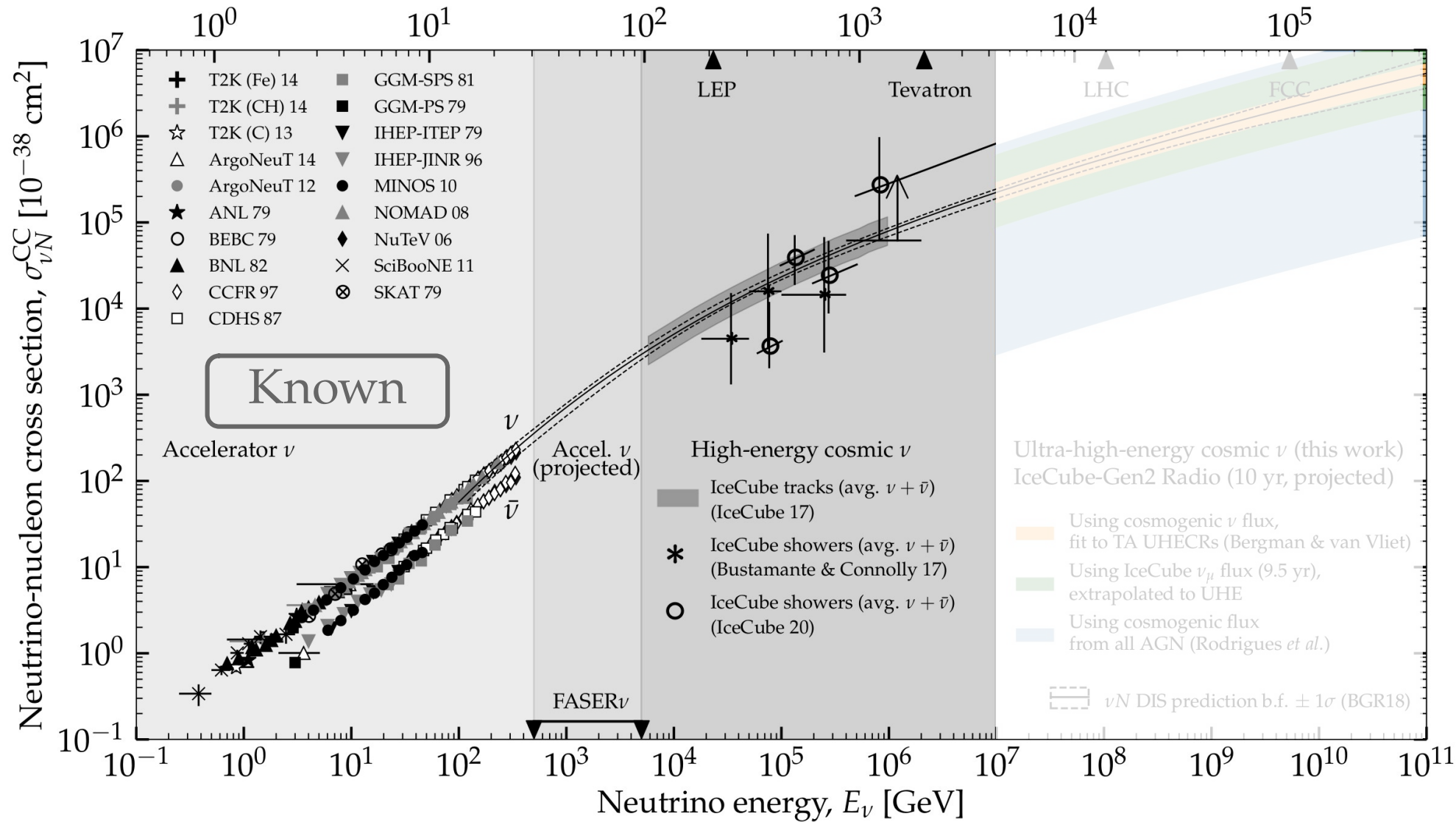
Center-of-mass energy \sqrt{s} [GeV]

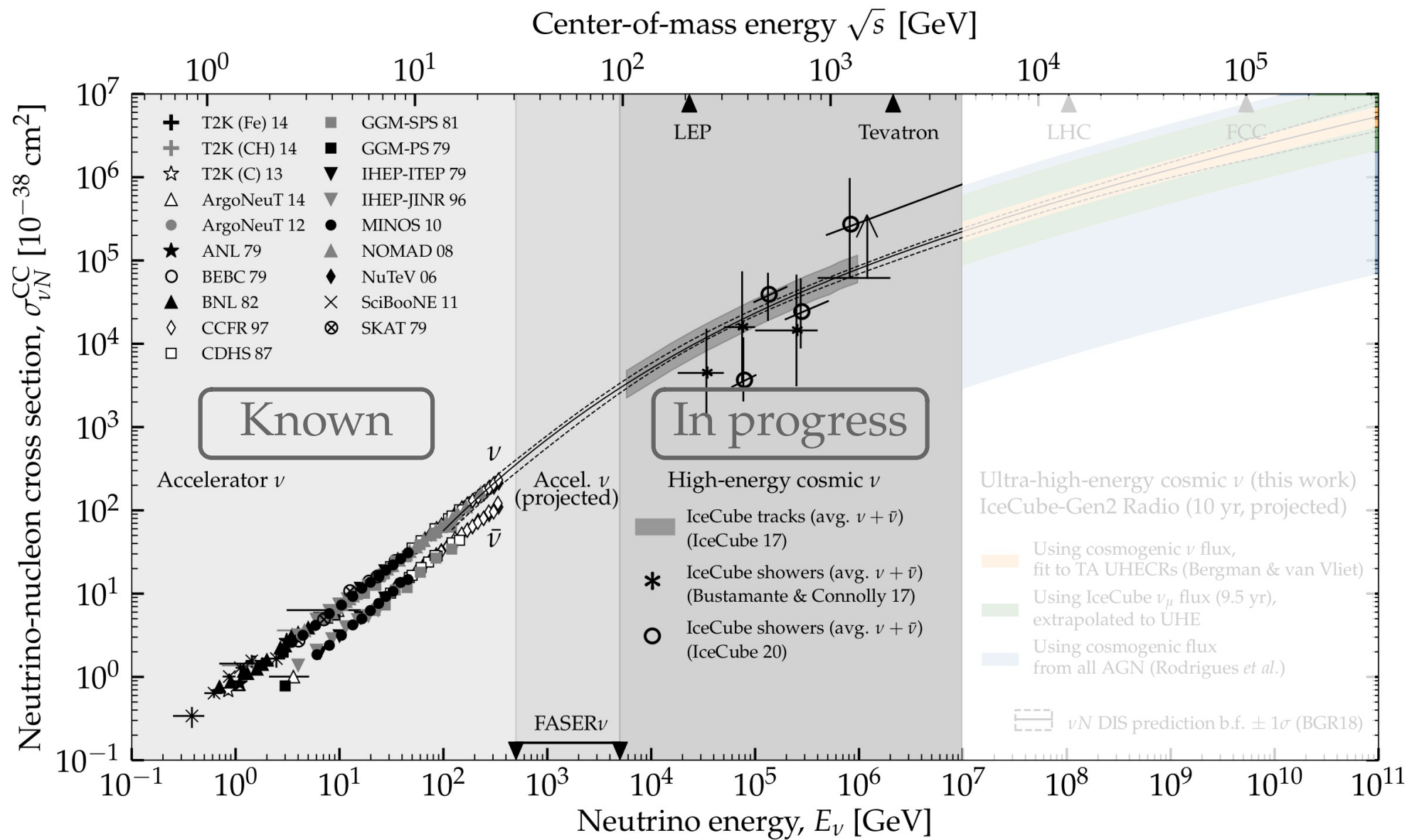


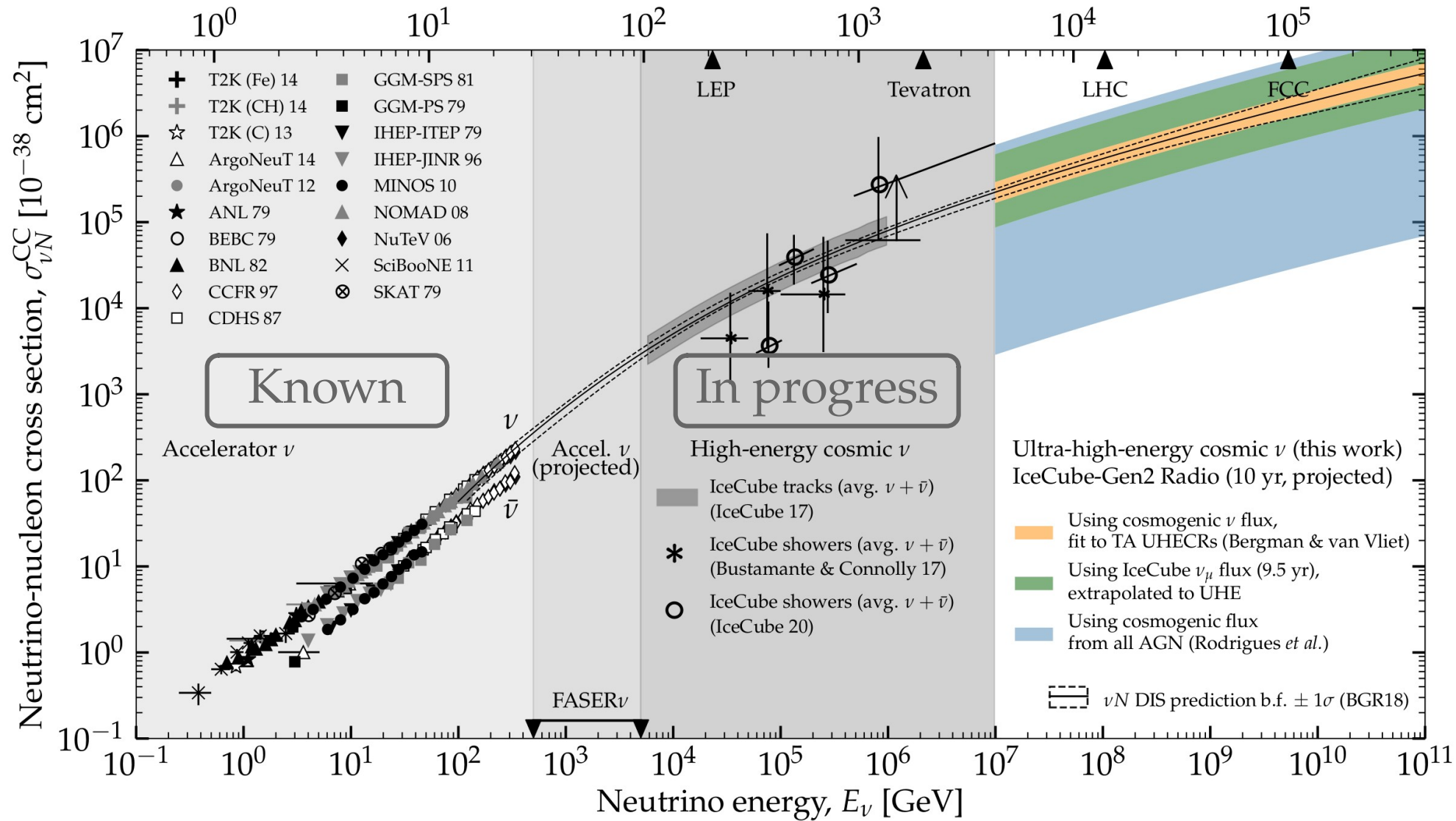




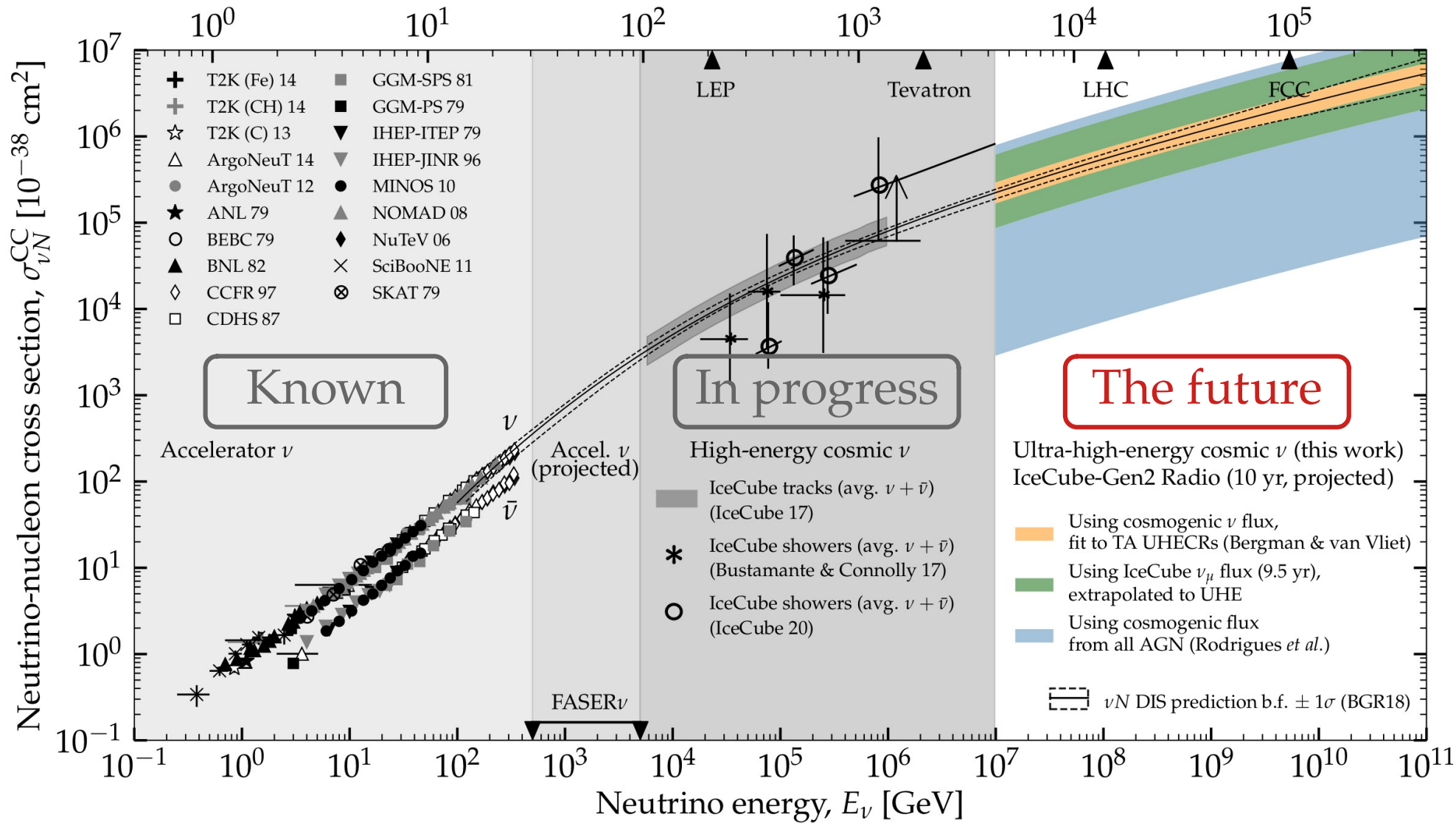


Center-of-mass energy \sqrt{s} [GeV]

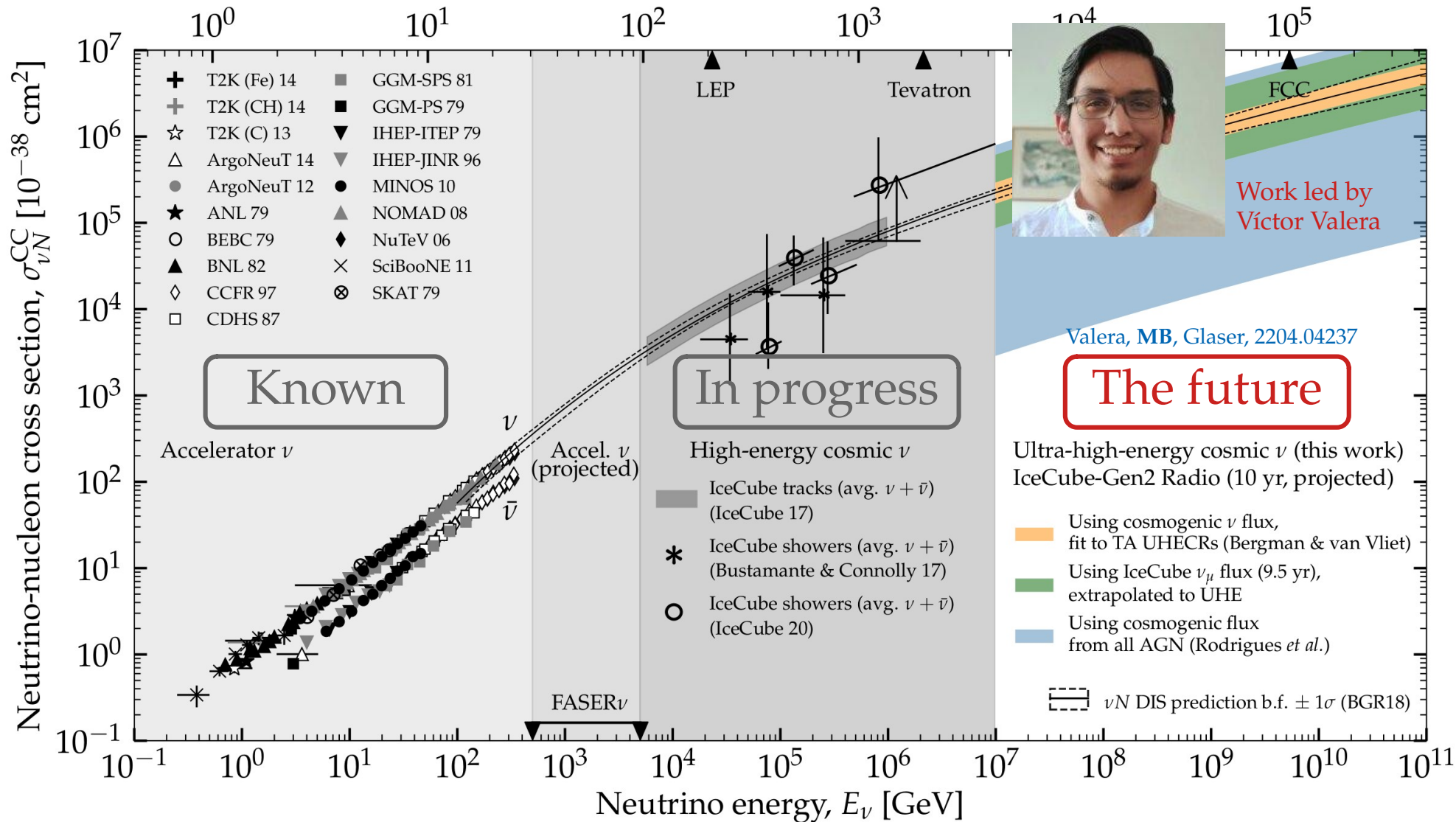


Center-of-mass energy \sqrt{s} [GeV]

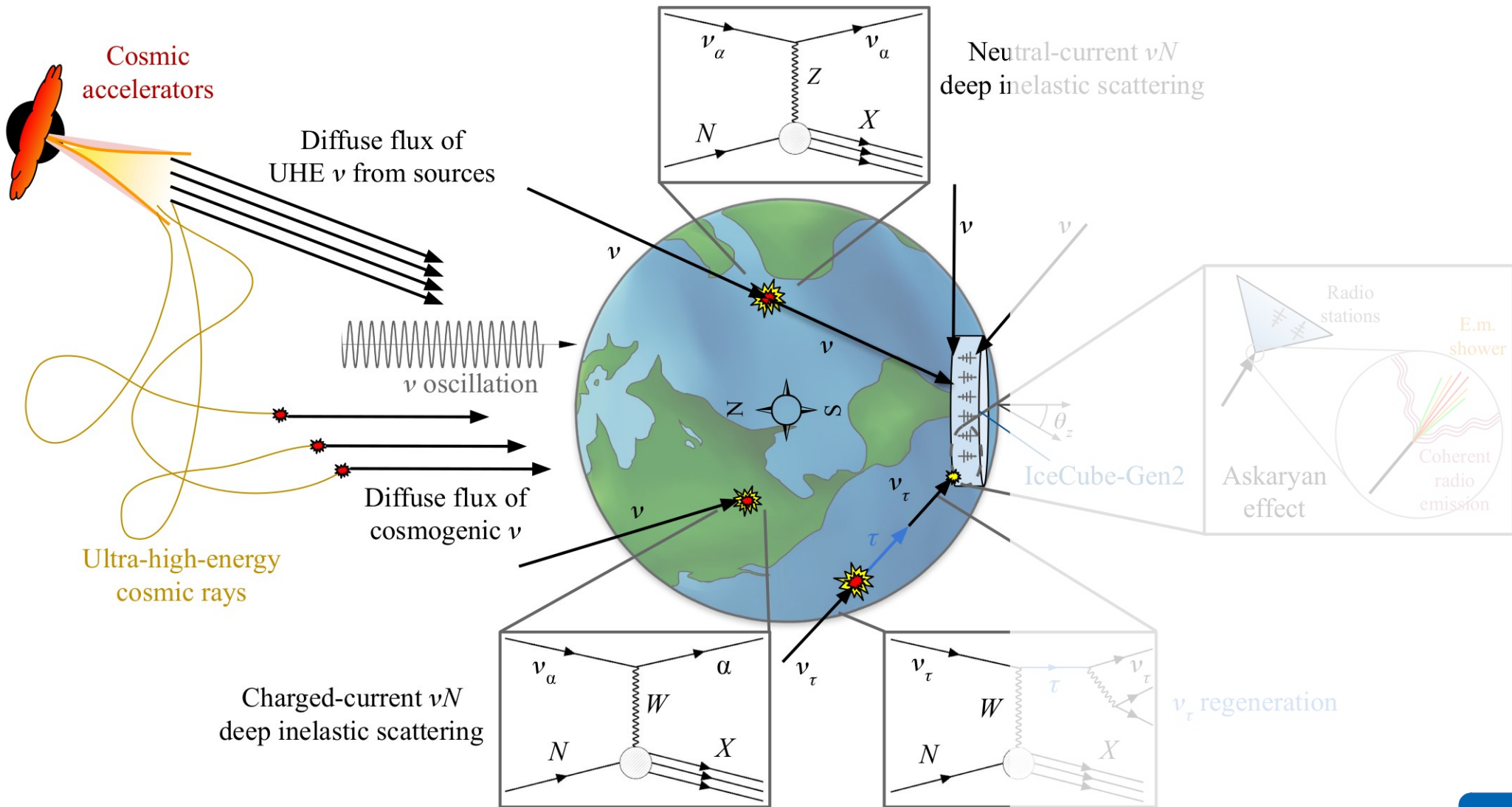
Center-of-mass energy \sqrt{s} [GeV]

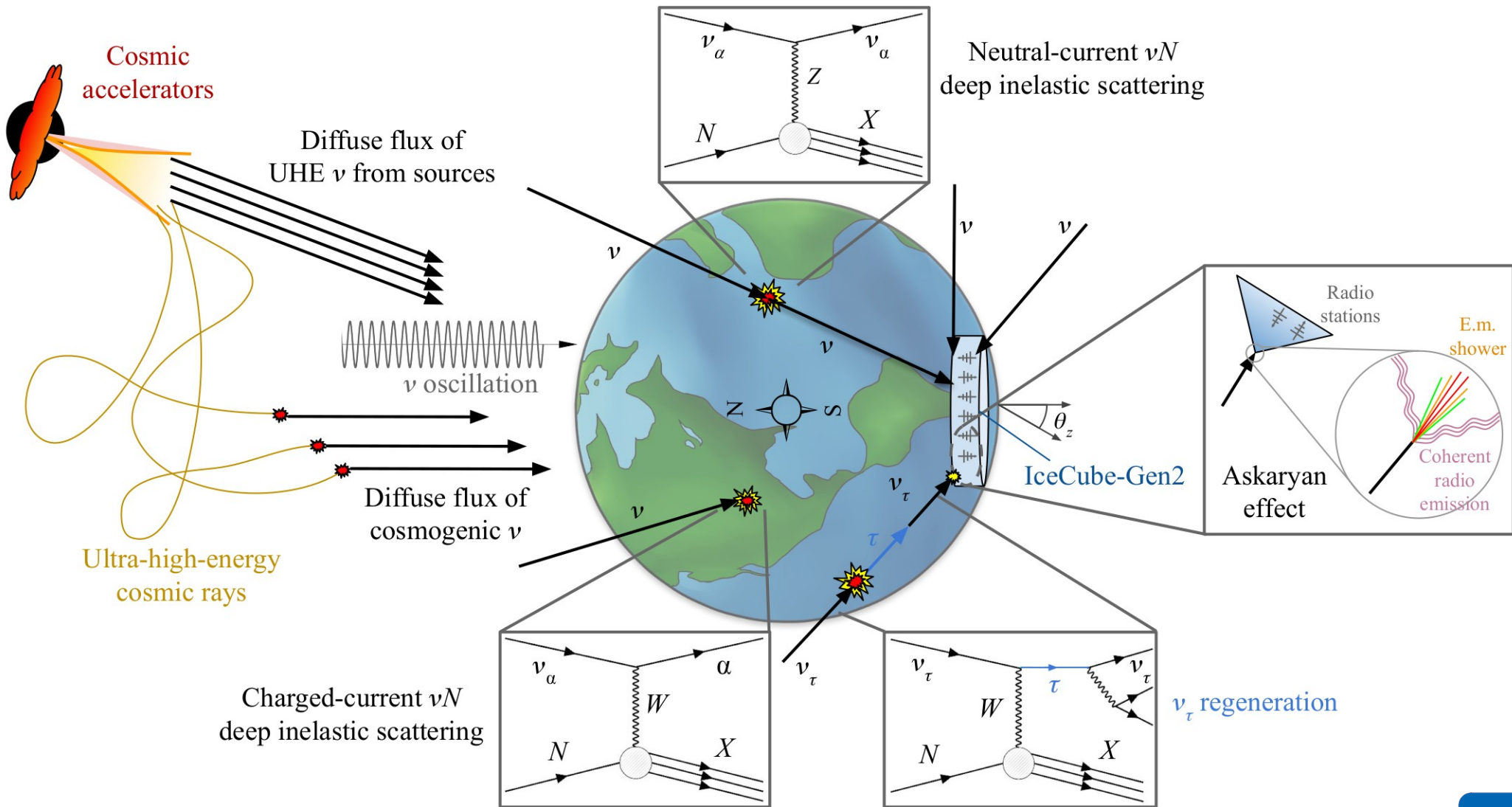


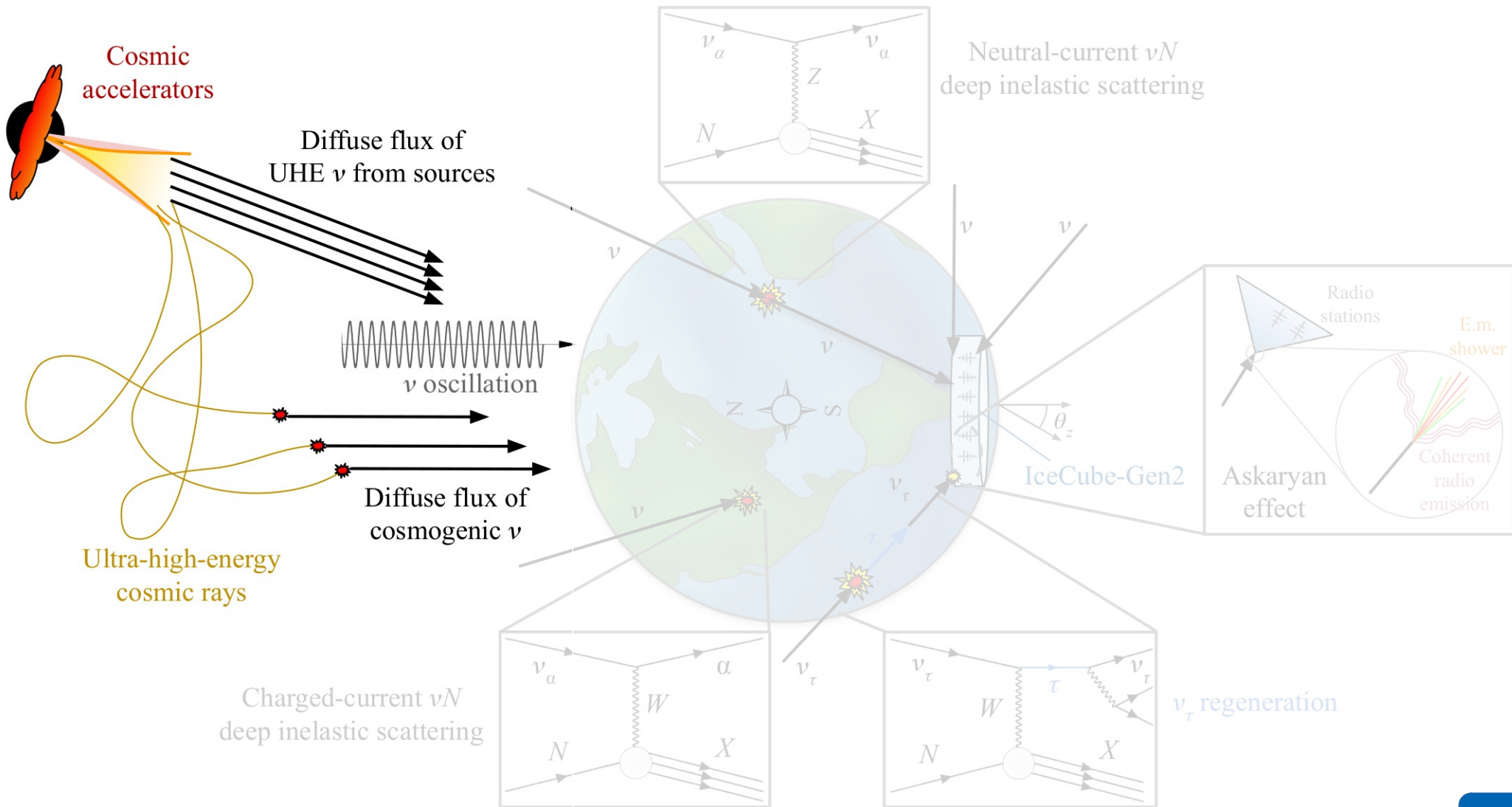
Center-of-mass energy \sqrt{s} [GeV]









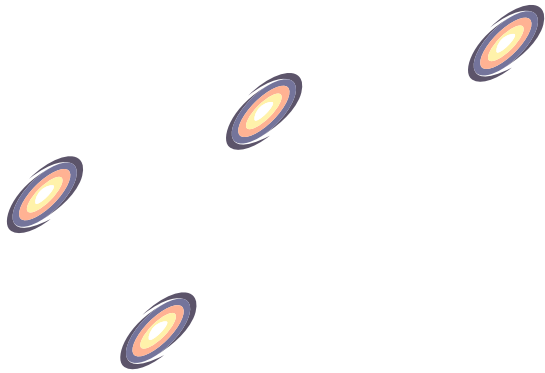


Redshift



$z = 0$

Note: v sources can be steady-state or transient



Redshift

$z = 0$

Discovered

MeV γ

PeV p

TeV–PeV ν

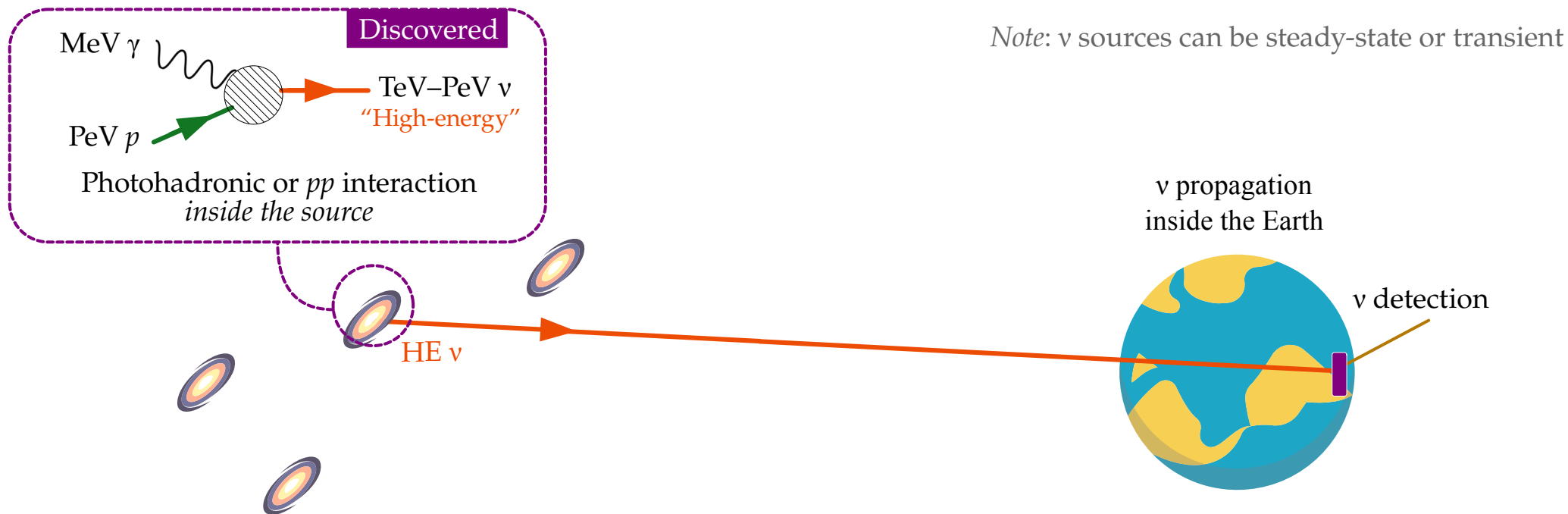
“High-energy”

Photohadronic or pp interaction
inside the source

Note: ν sources can be steady-state or transient

ν propagation
inside the Earth

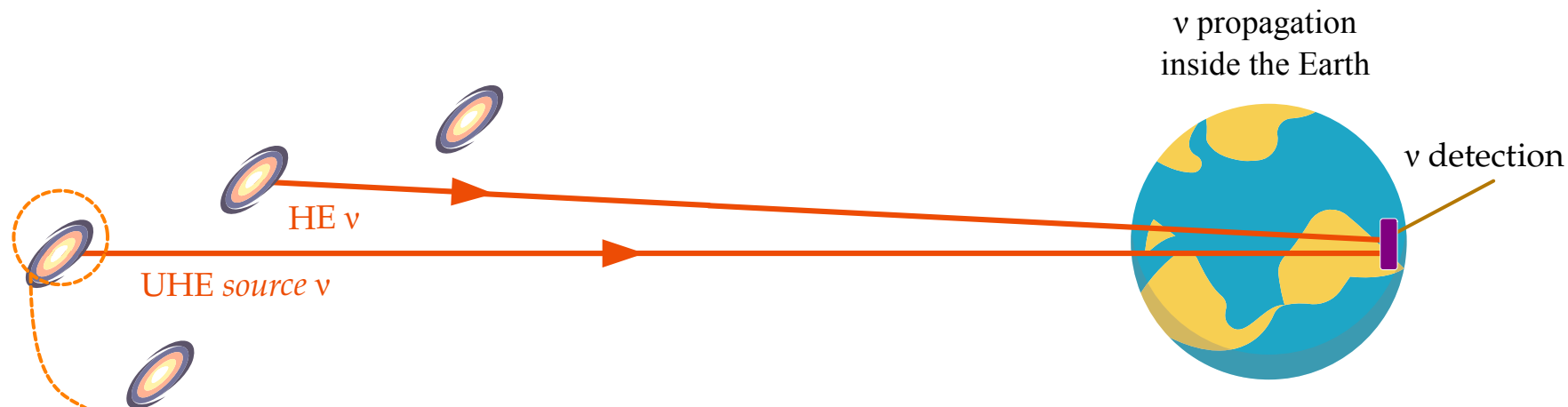
ν detection



Redshift

$z = 0$

Note: ν sources can be steady-state or transient



Undiscovered

meV γ

EeV p

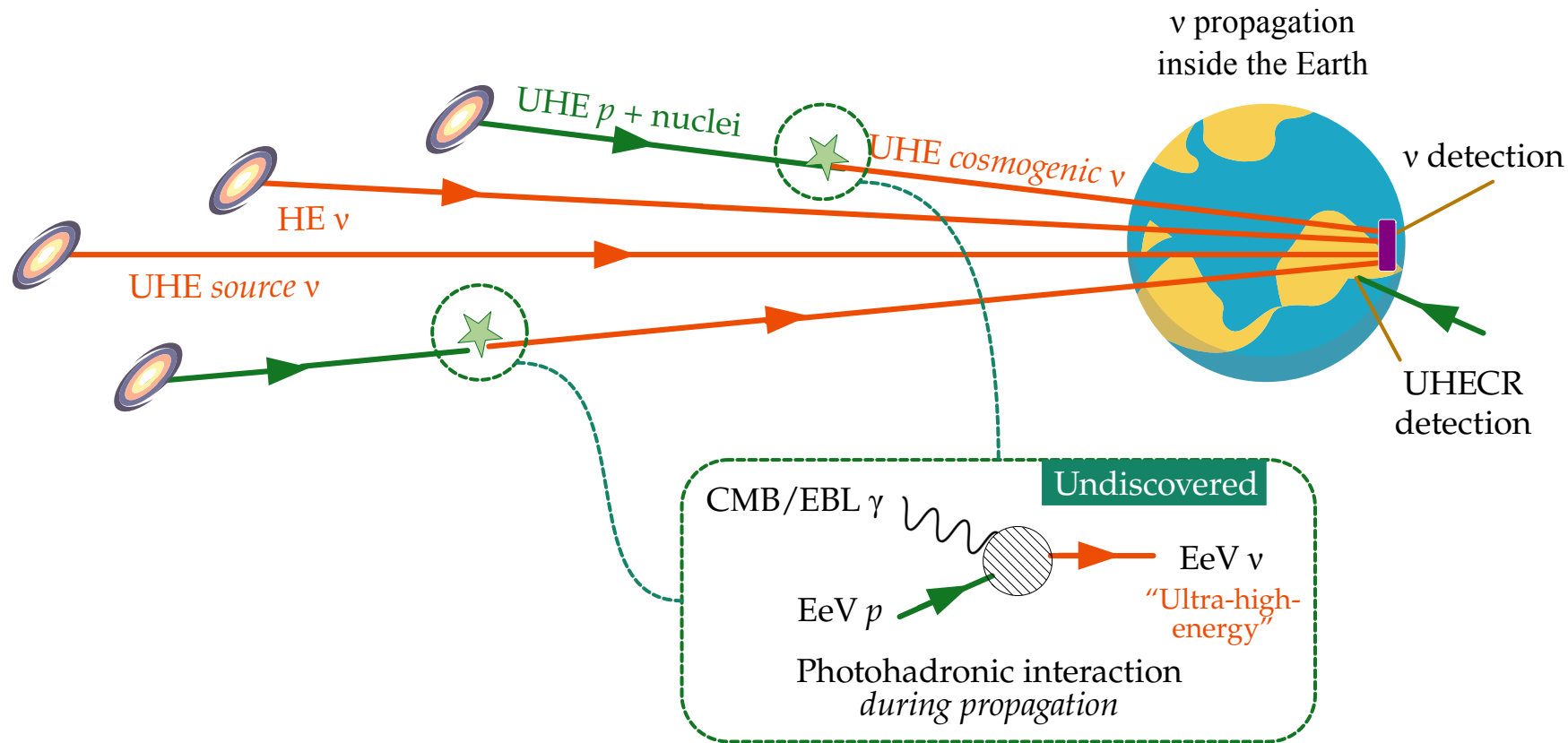
EeV ν

"Ultra-high-energy"

Photohadronic or pp interaction
inside the source

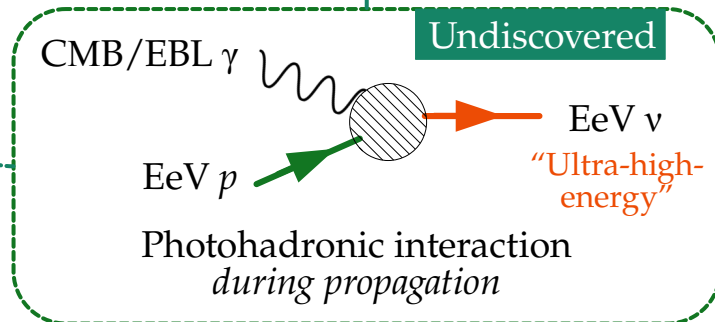
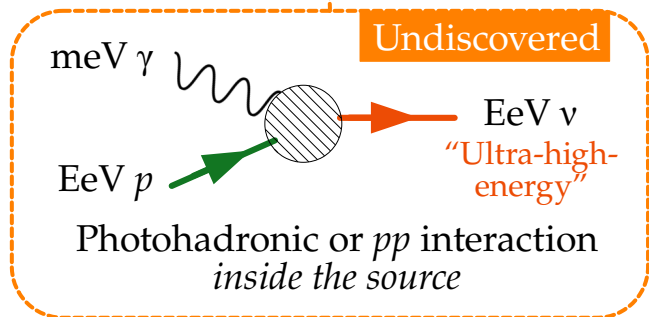
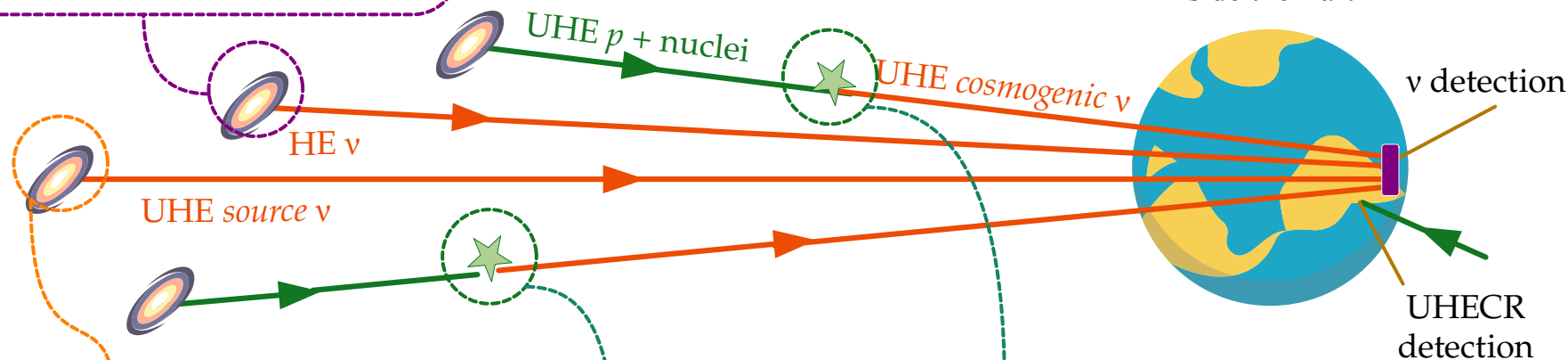
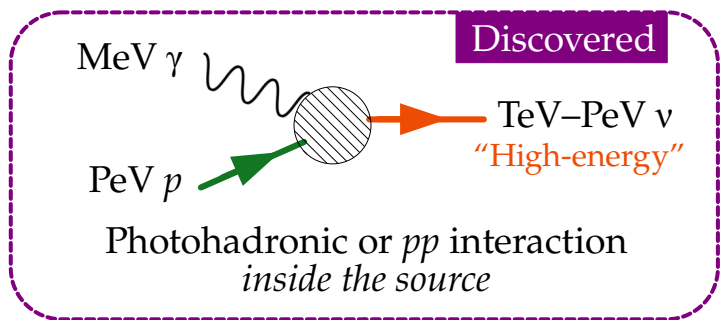
Redshift ← $z = 0$

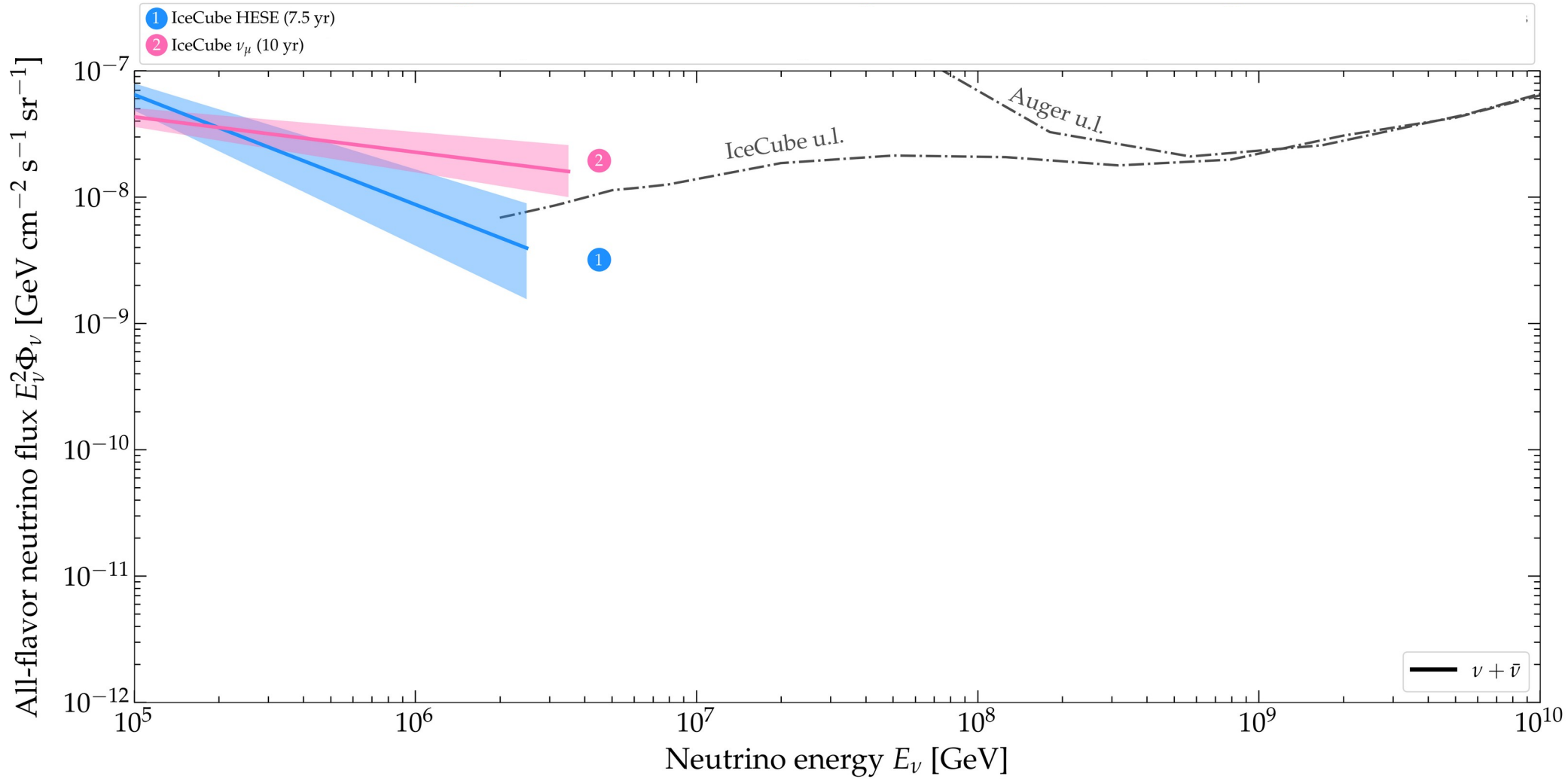
Note: ν sources can be steady-state or transient

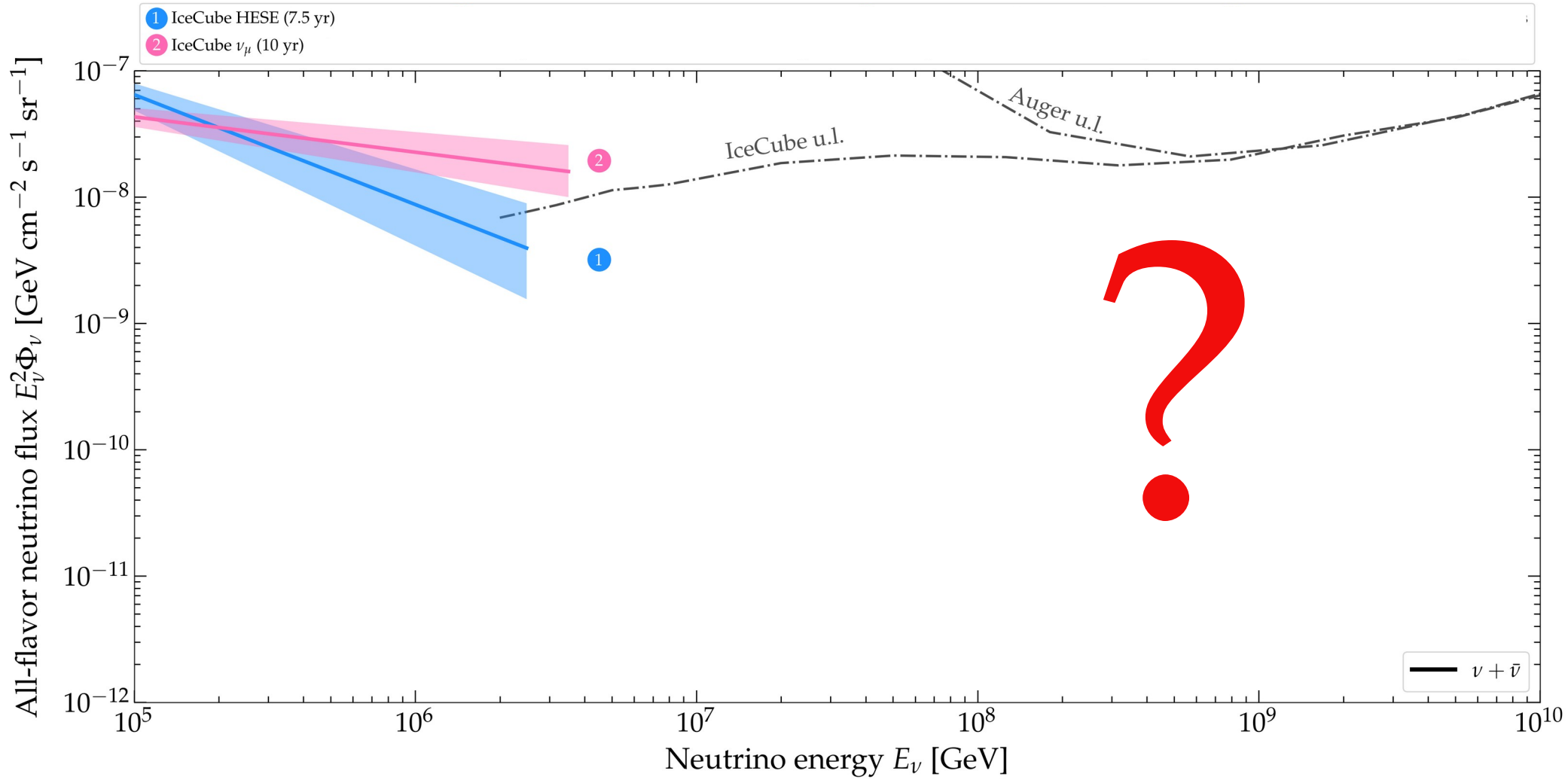


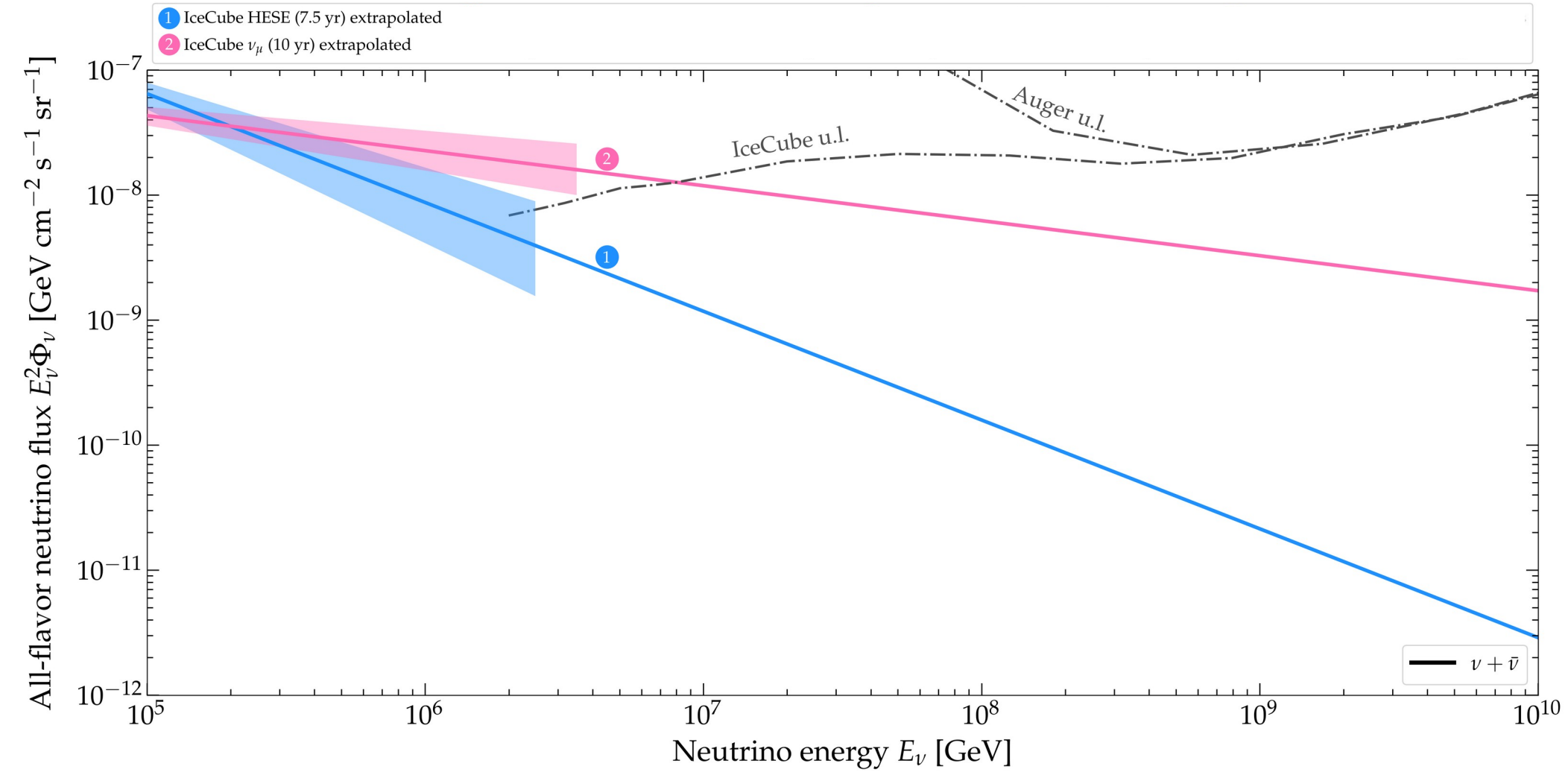
Redshift ← z = 0

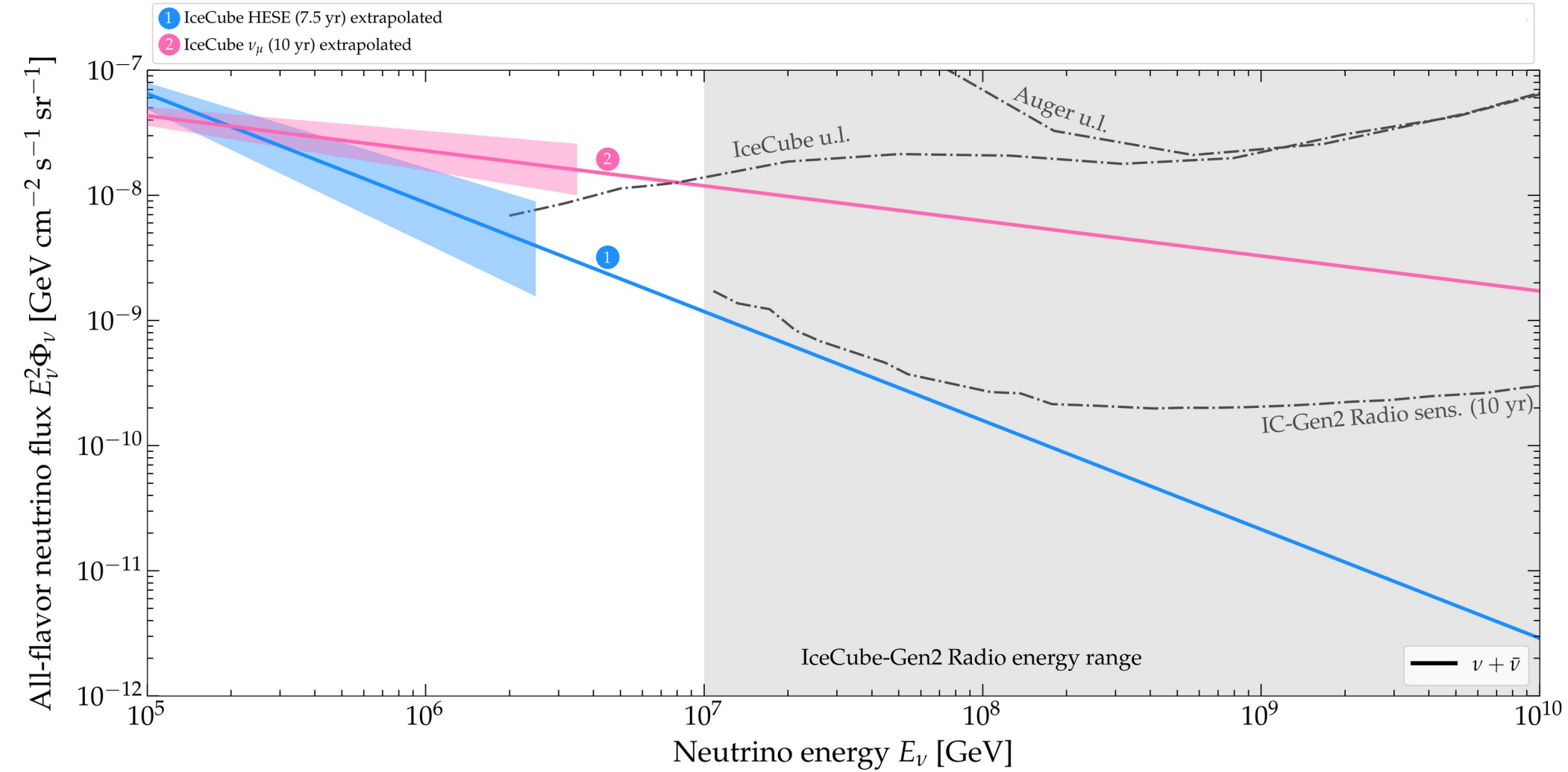
Note: ν sources can be steady-state or transient

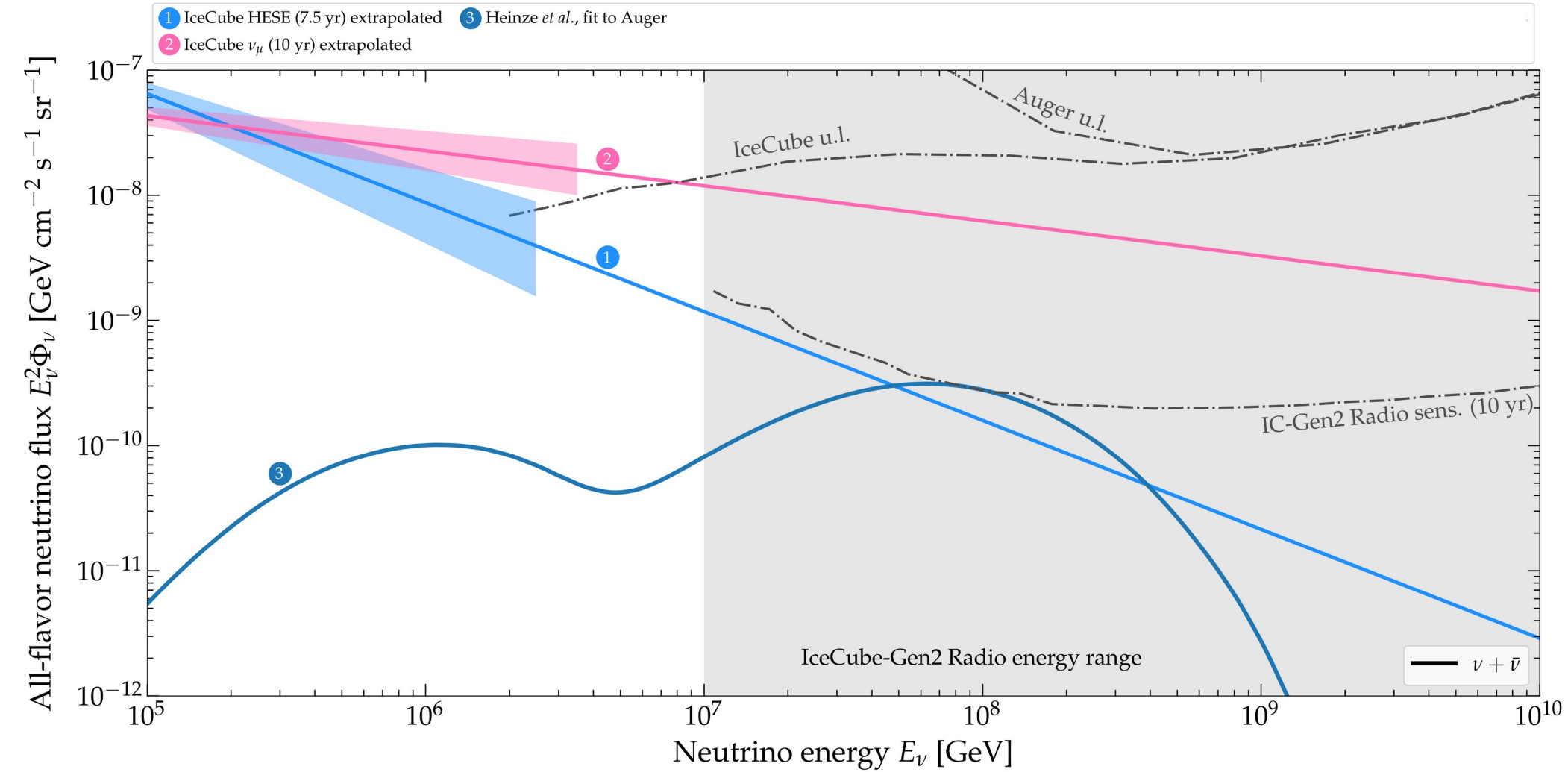


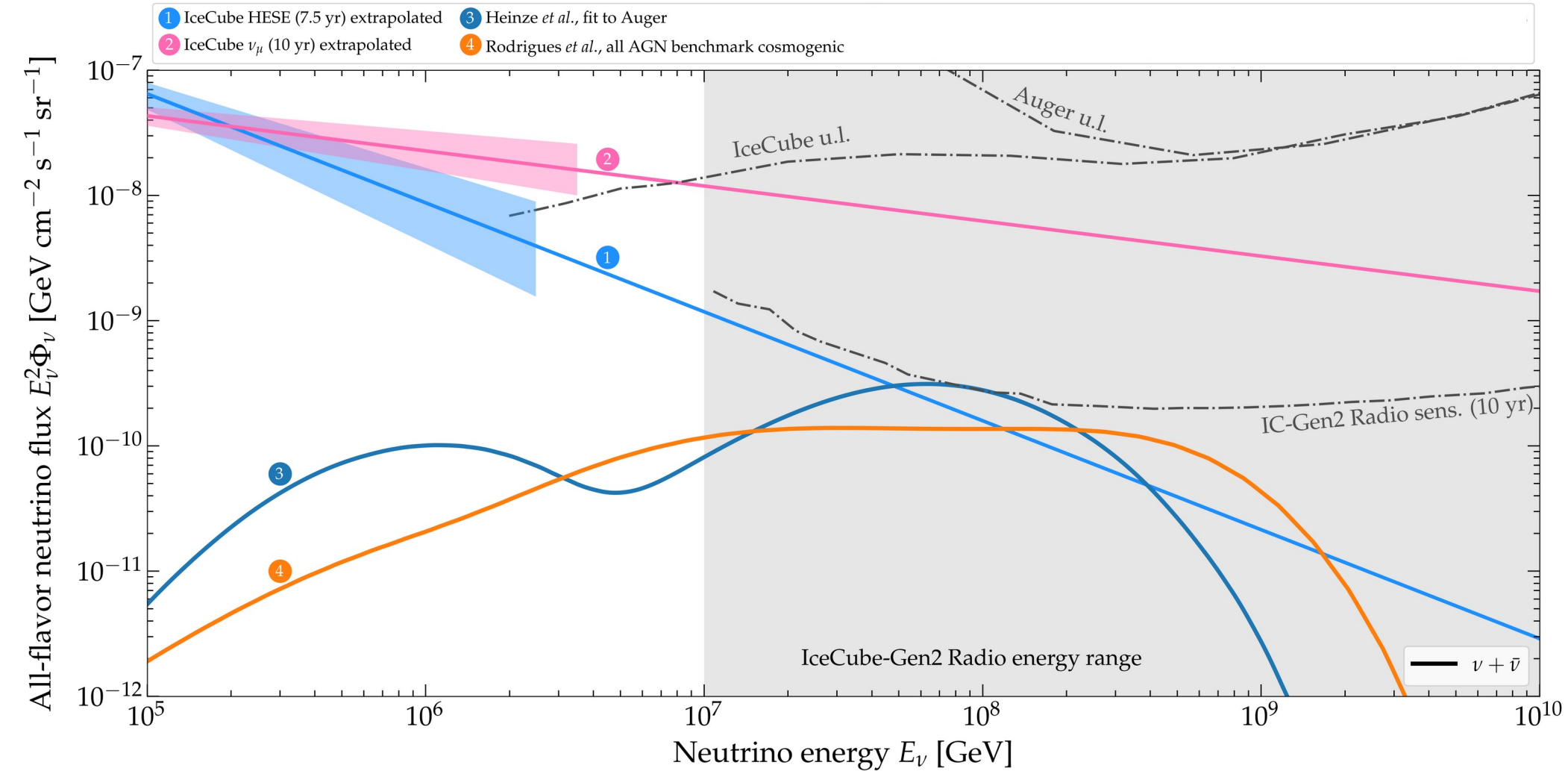


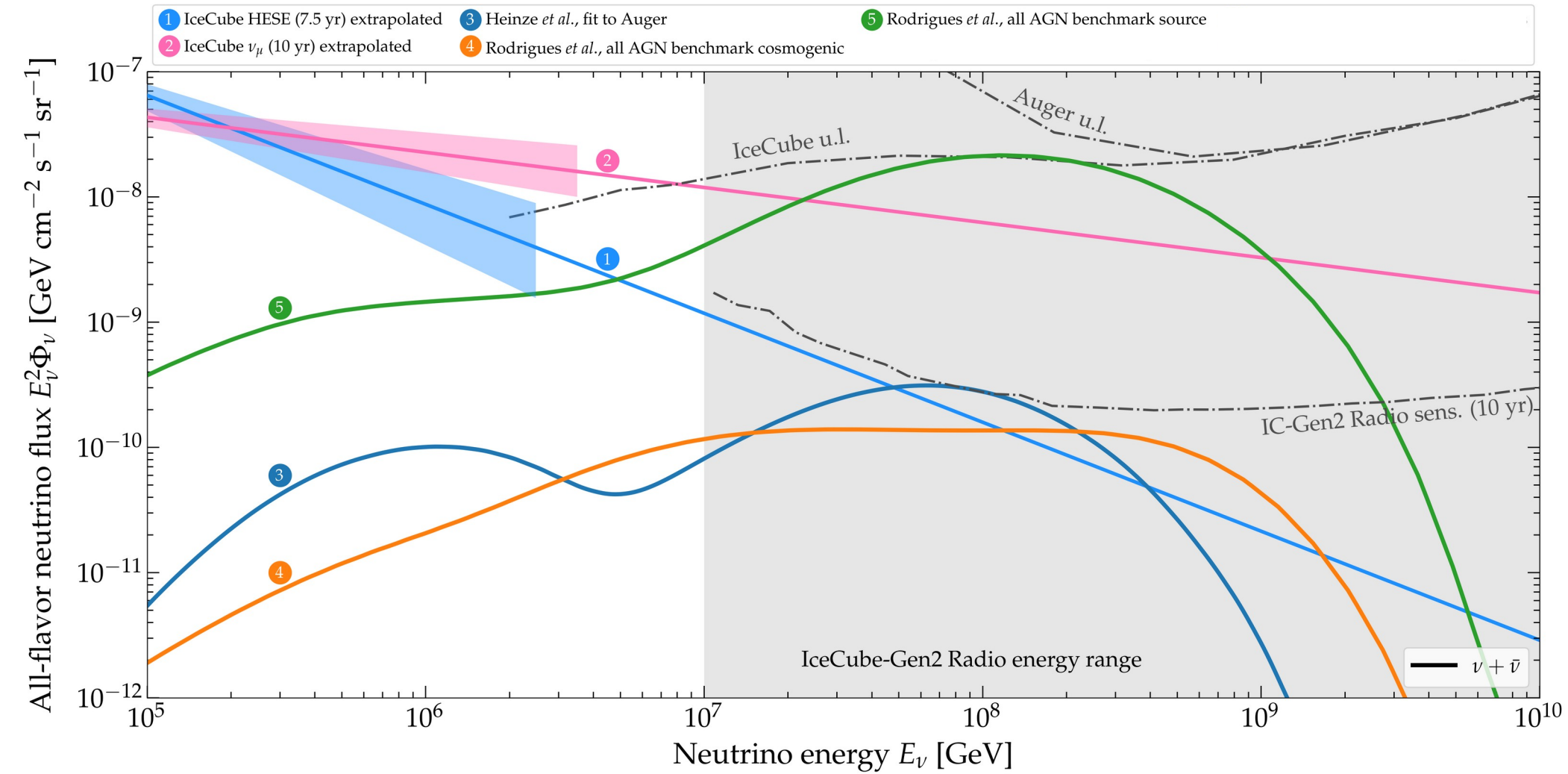


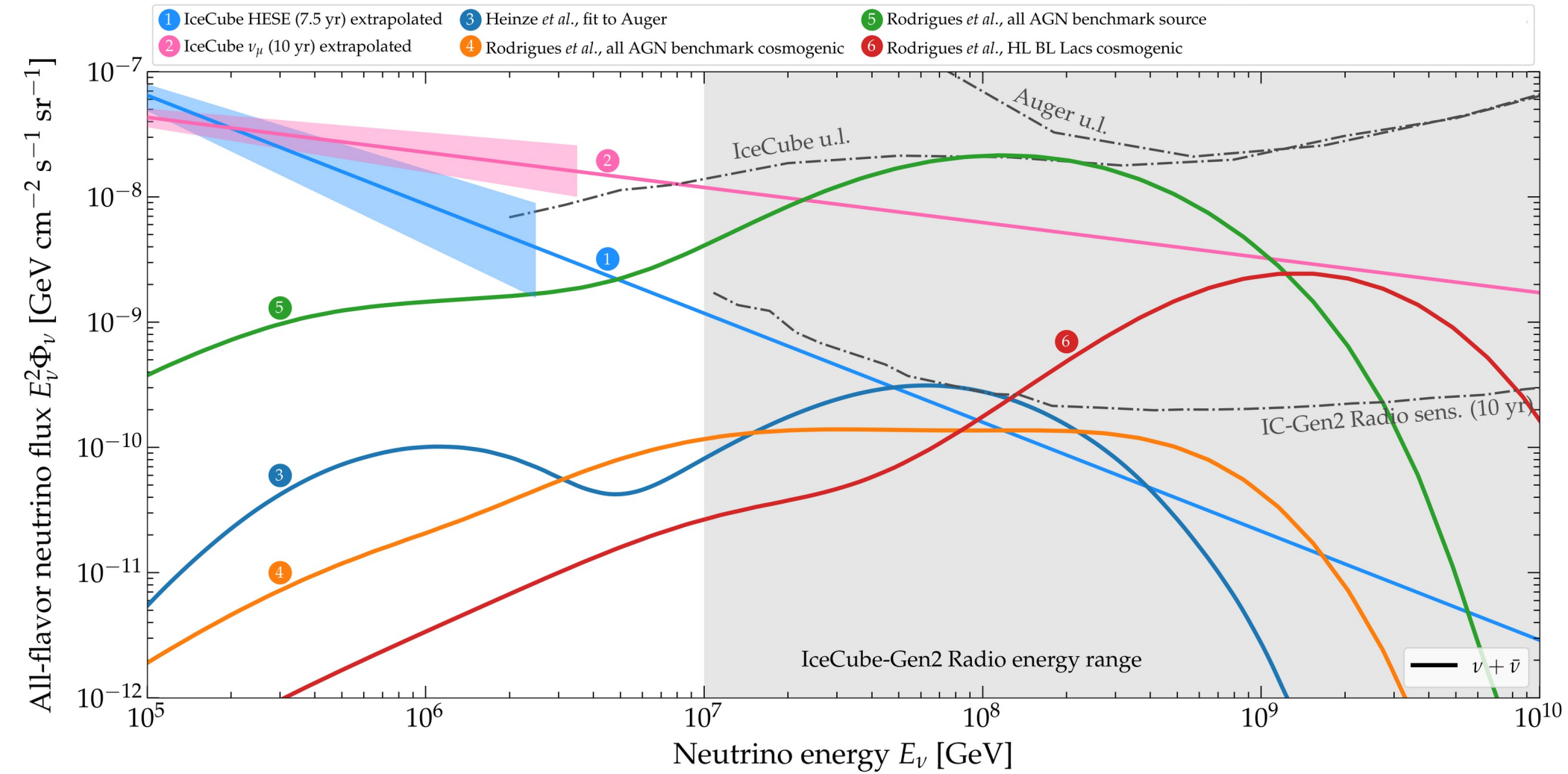


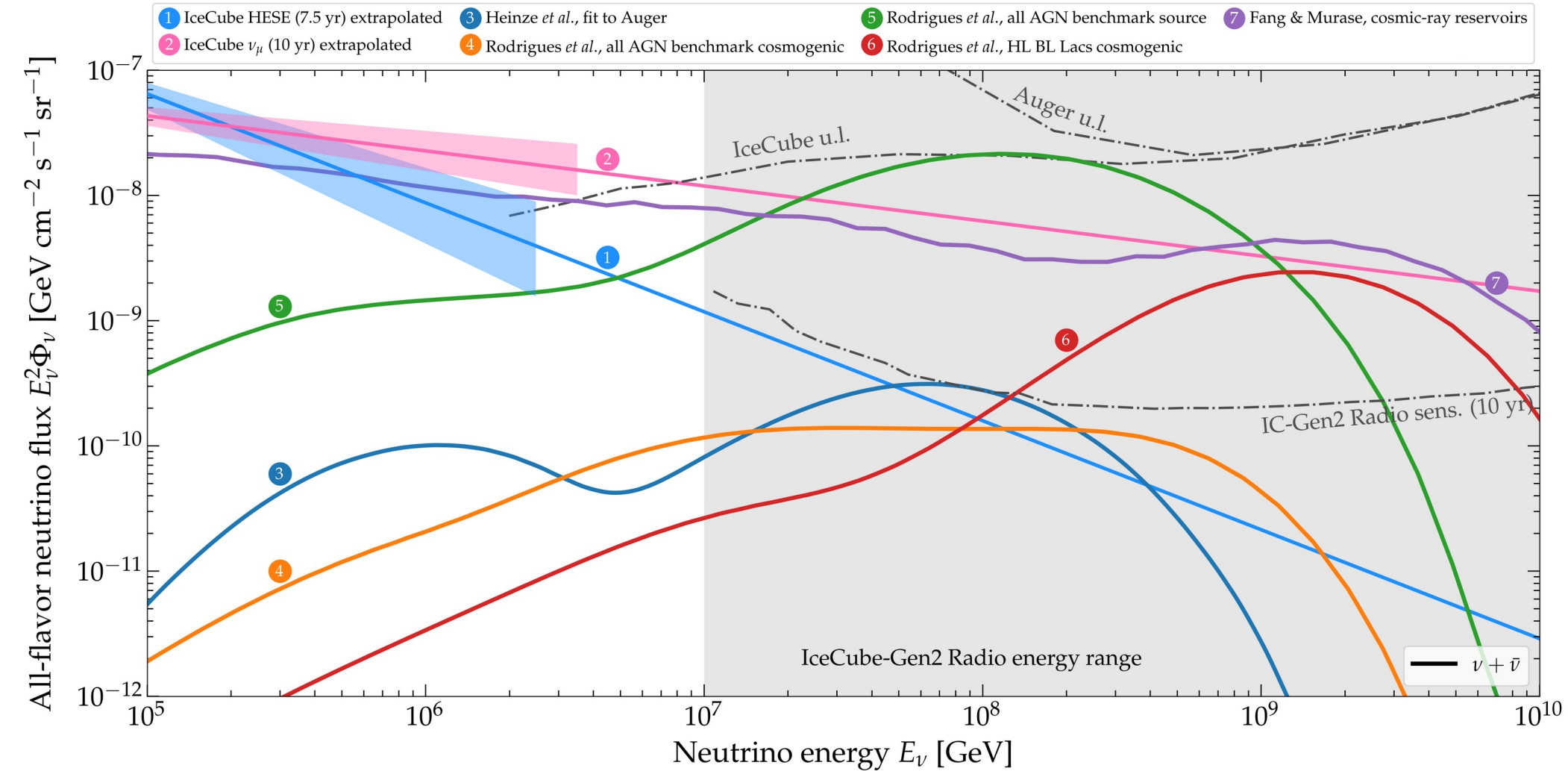


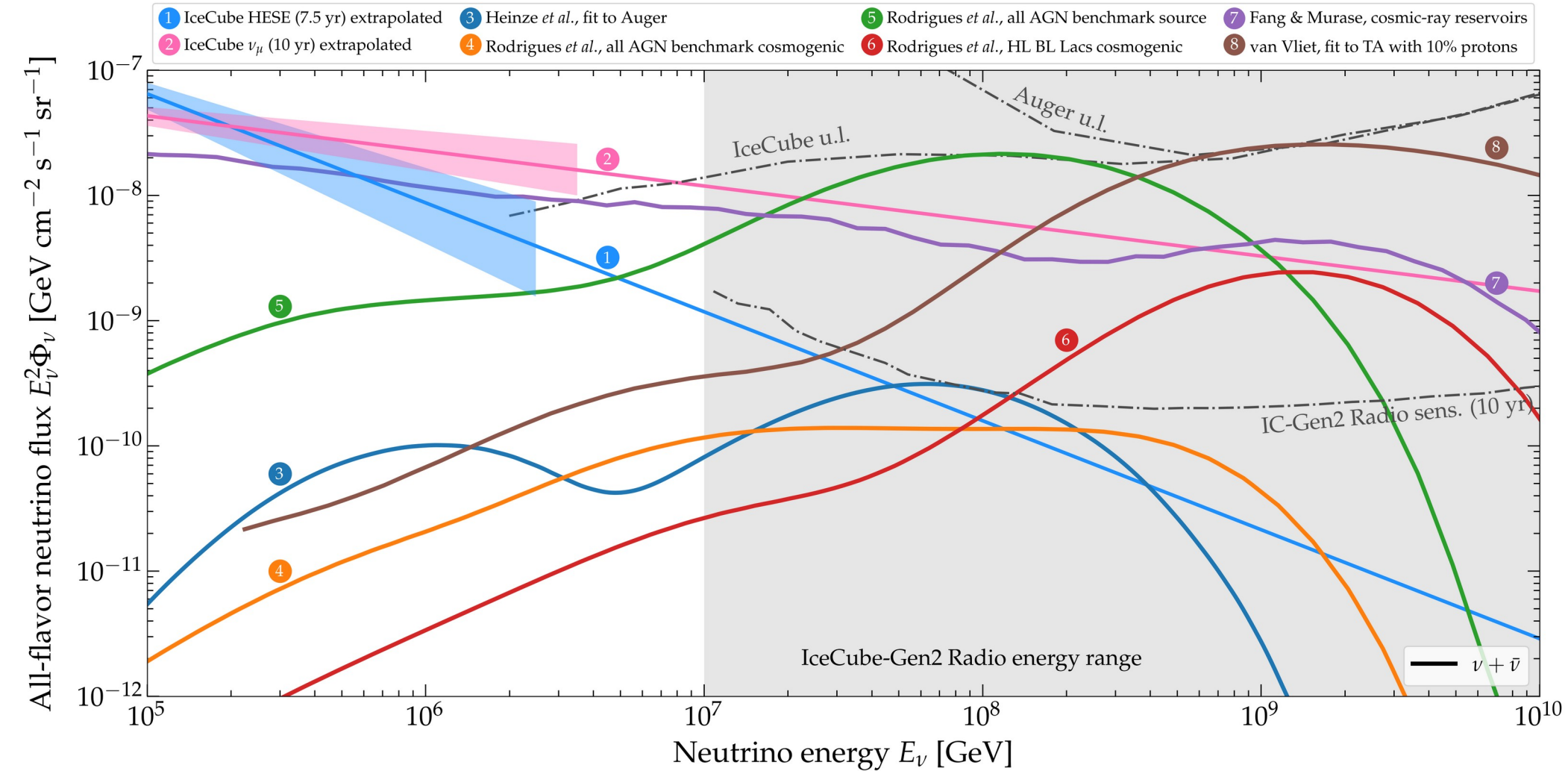


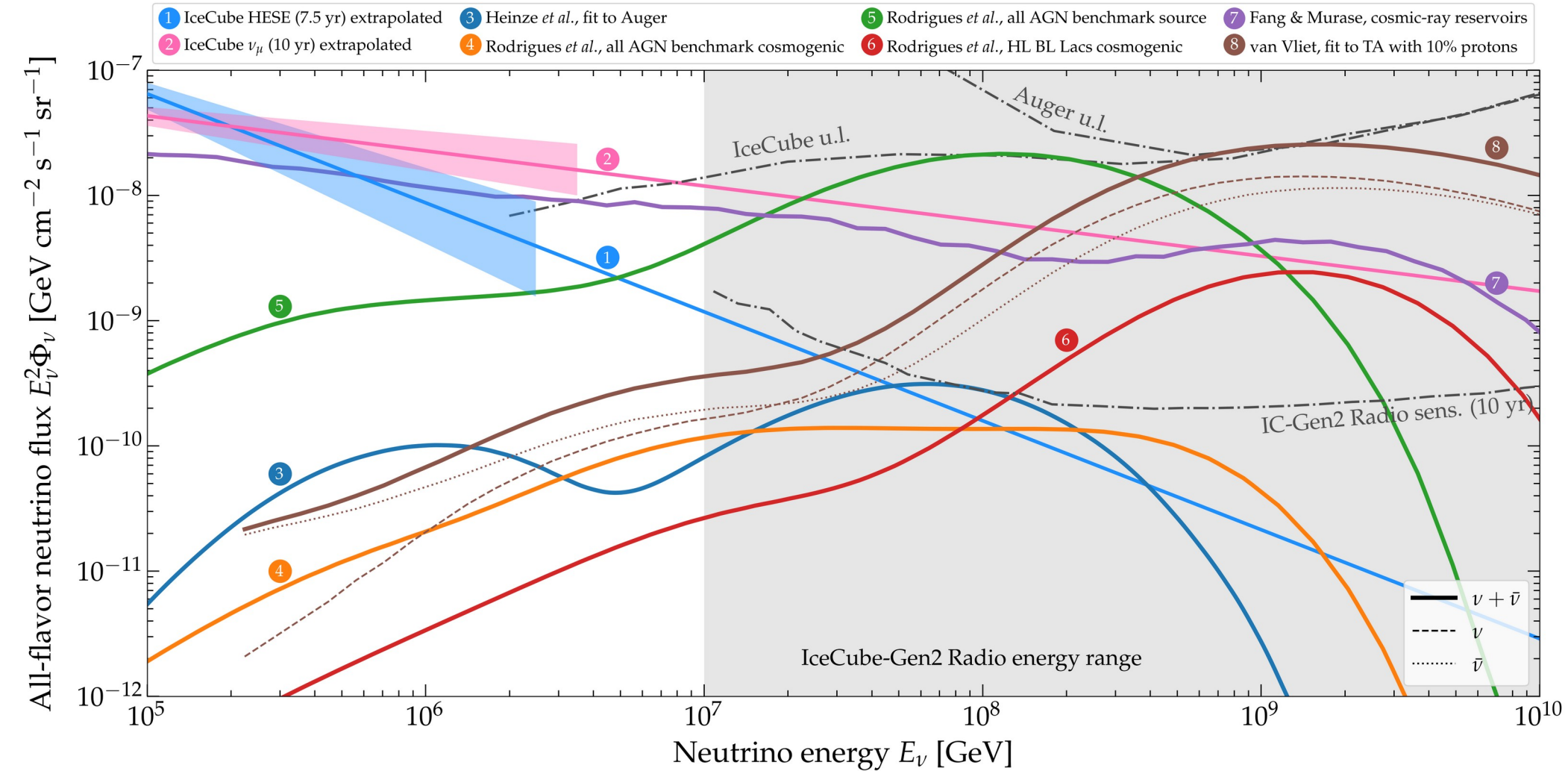


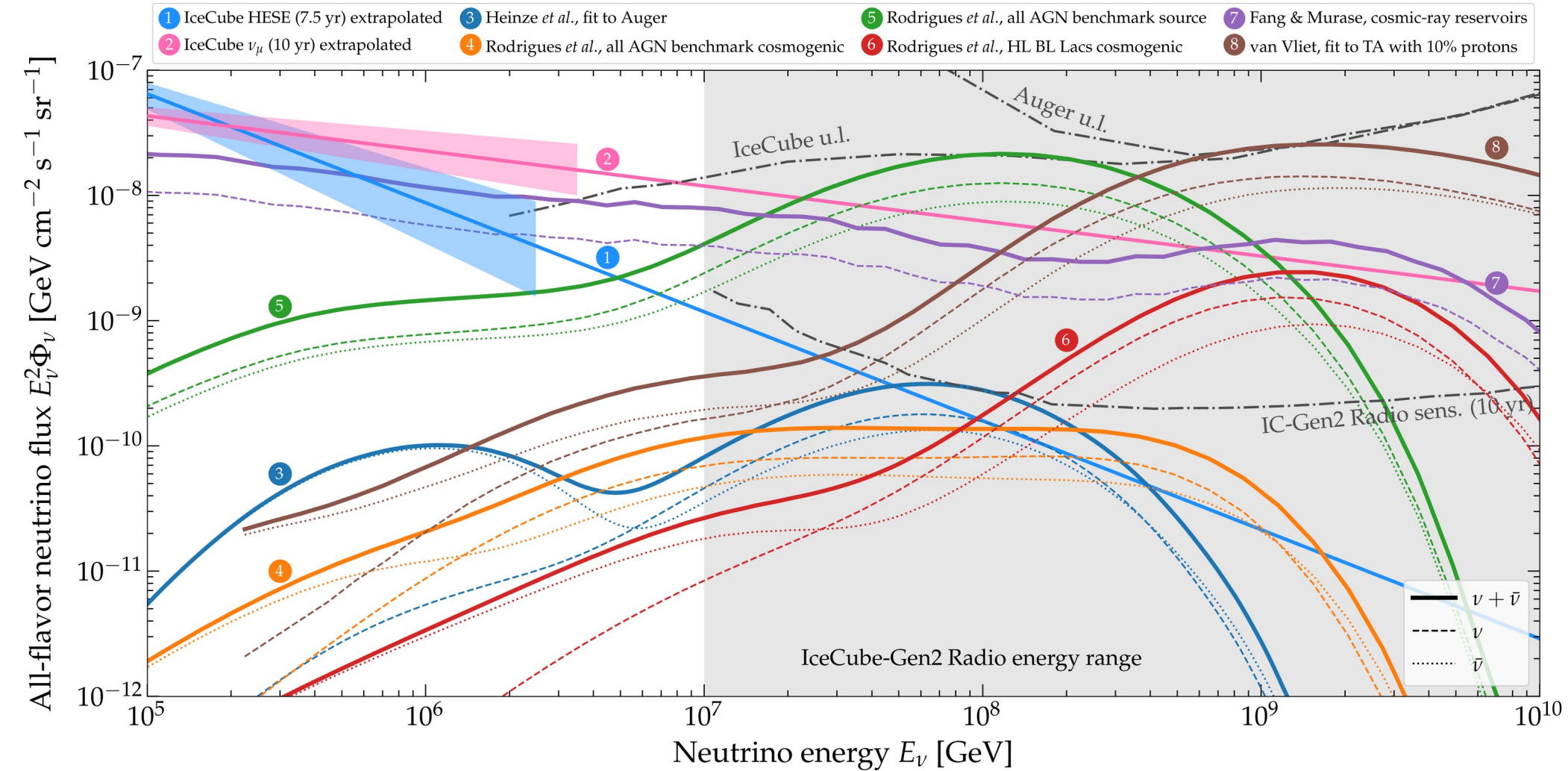


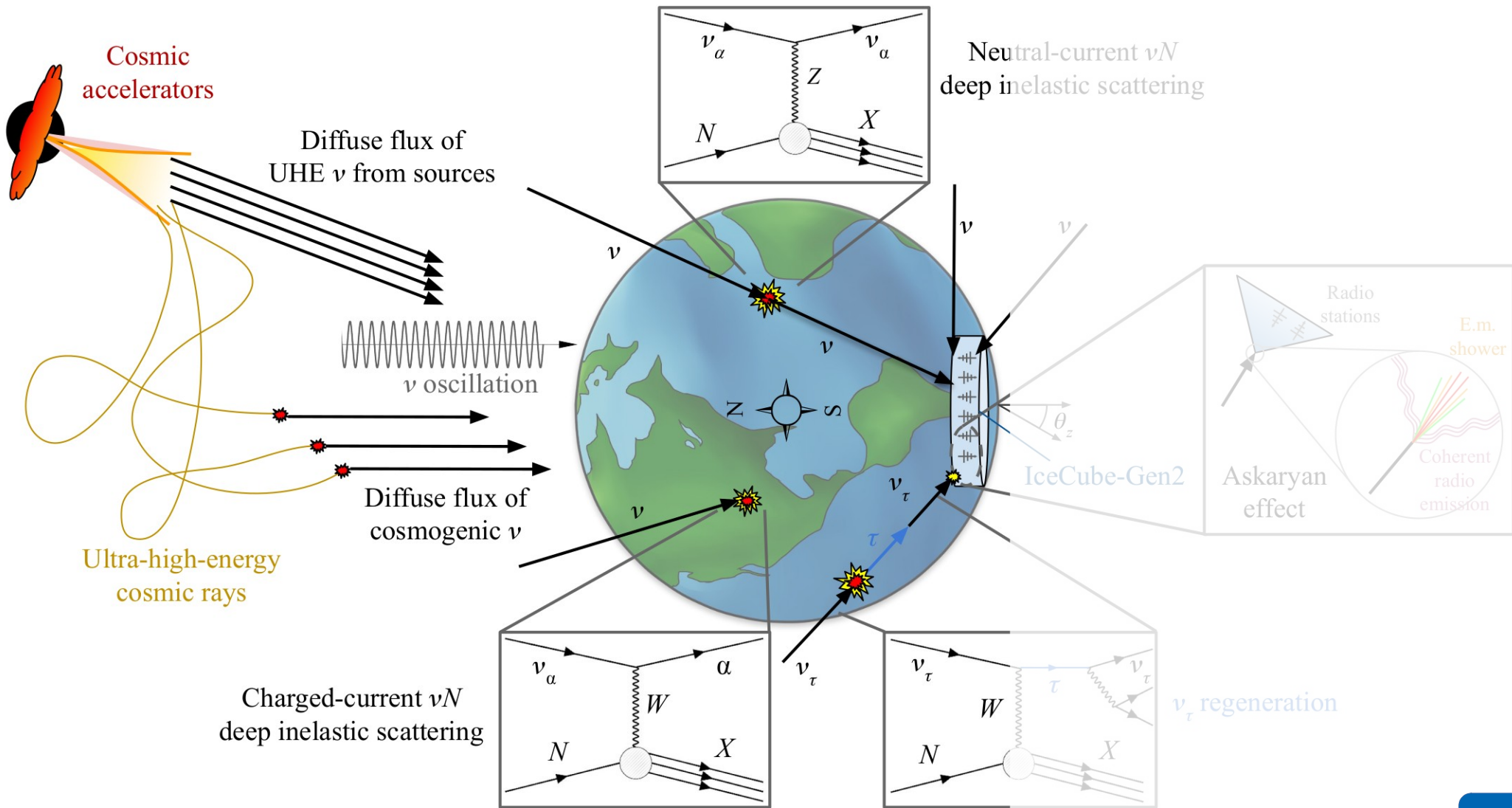








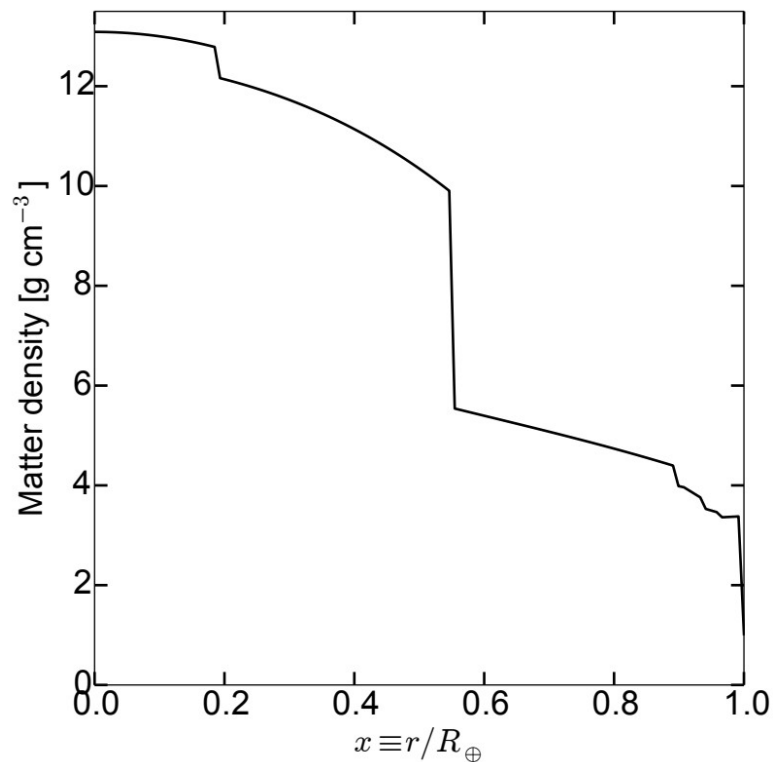




A feel for the in-Earth attenuation

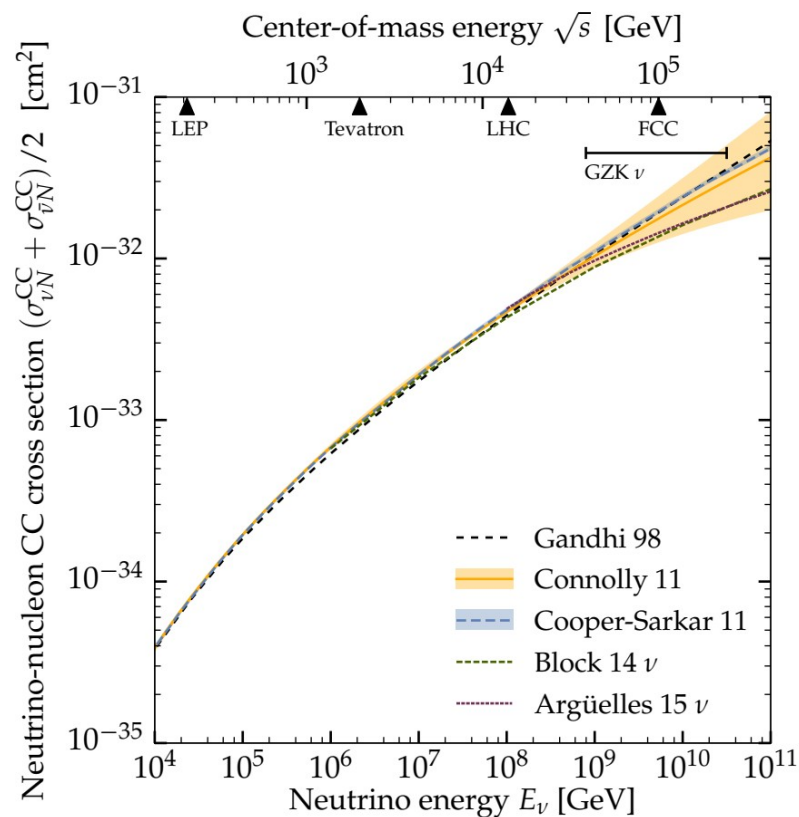
Earth matter density

(Preliminary Reference Earth Model)

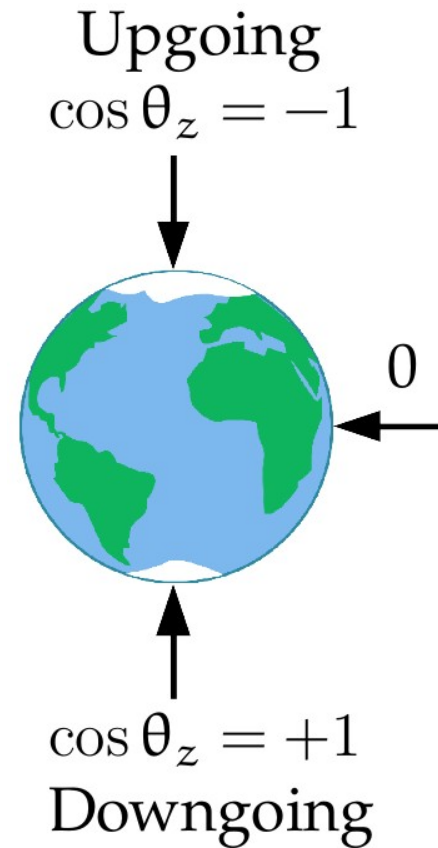
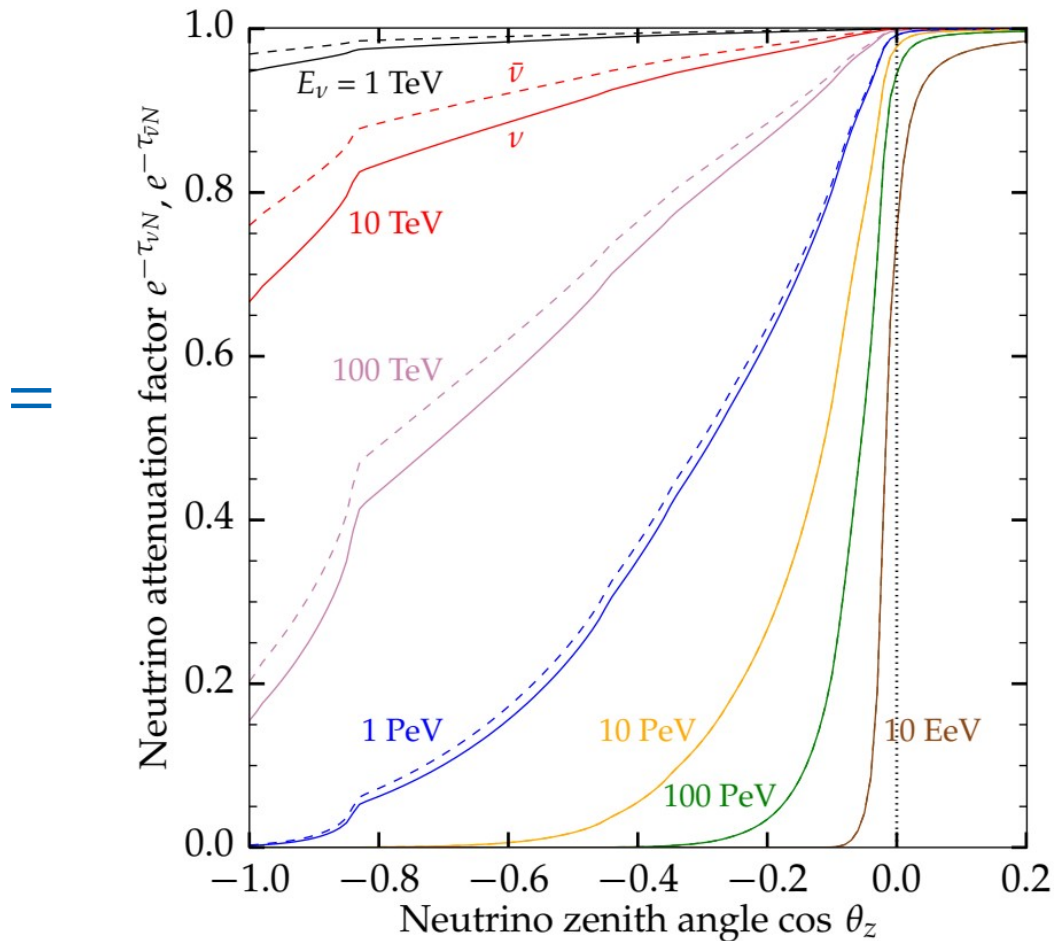


+

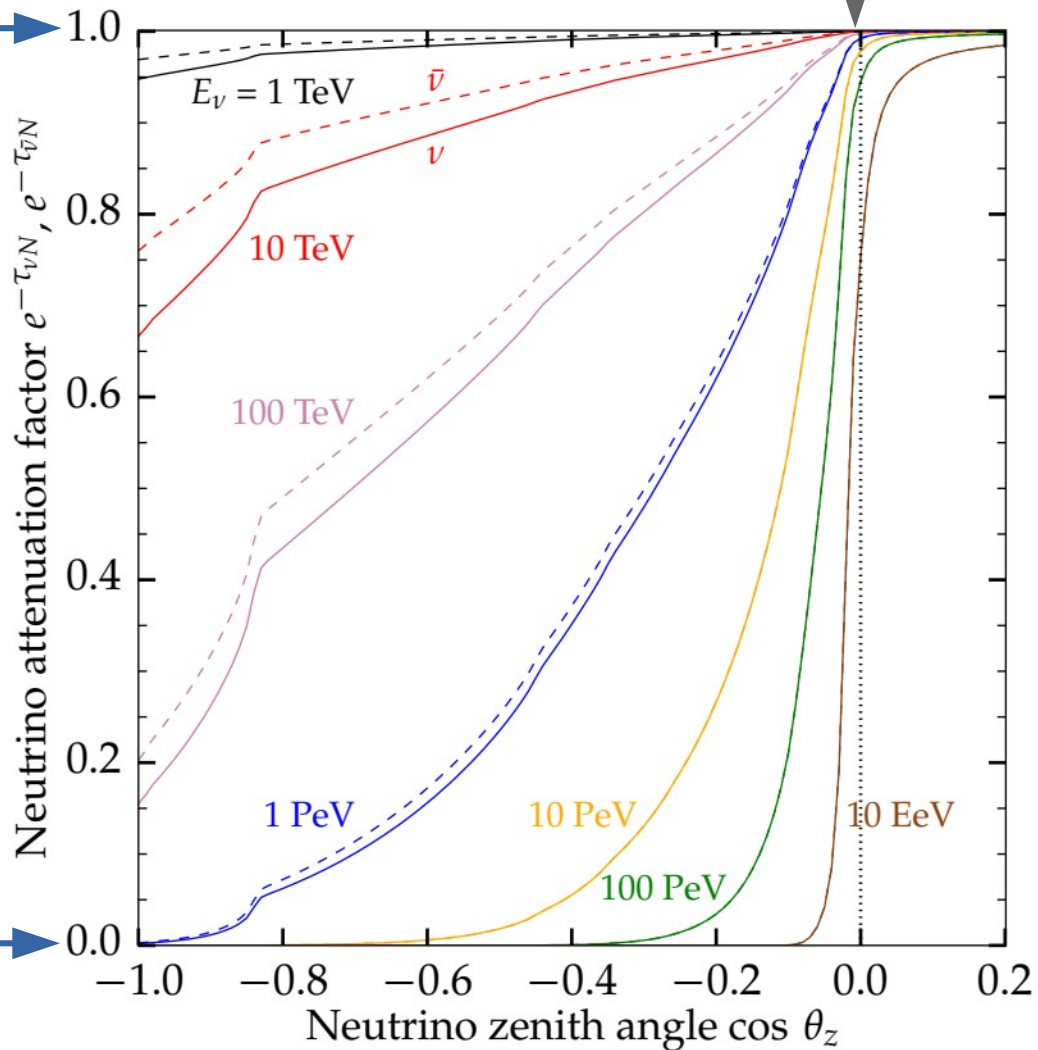
Neutrino-nucleon cross section



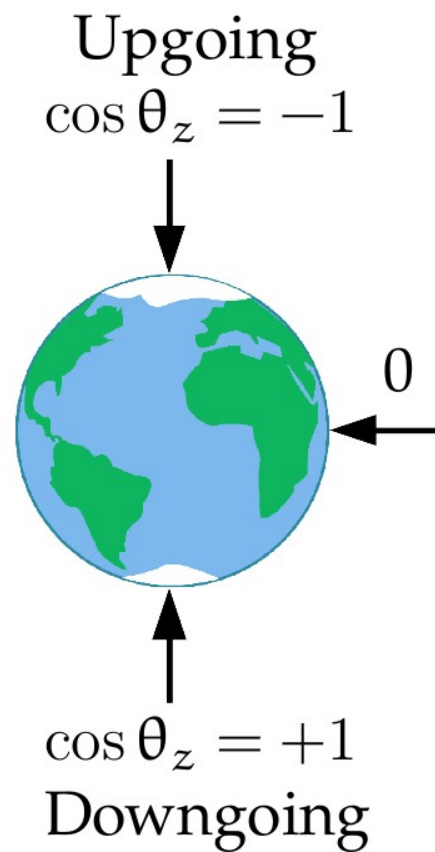
A feel for the in-Earth attenuation



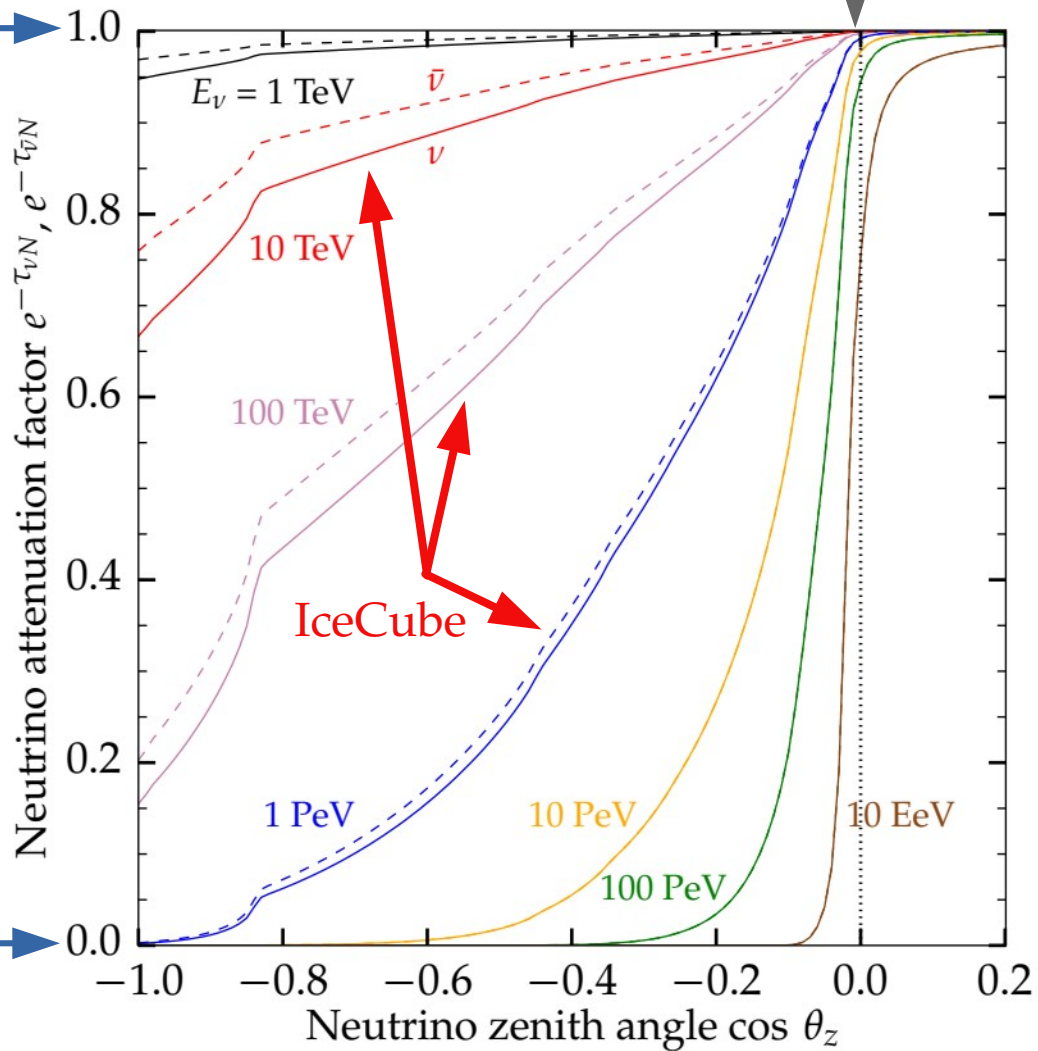
No
attenuation



Full
attenuation

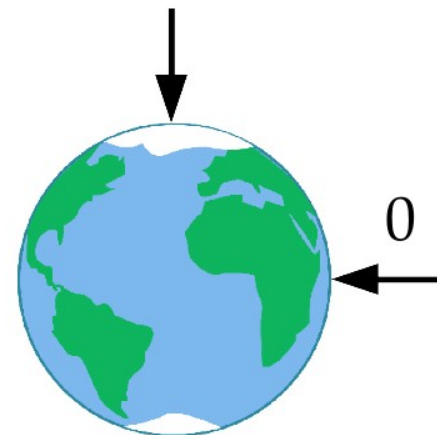


No
attenuation

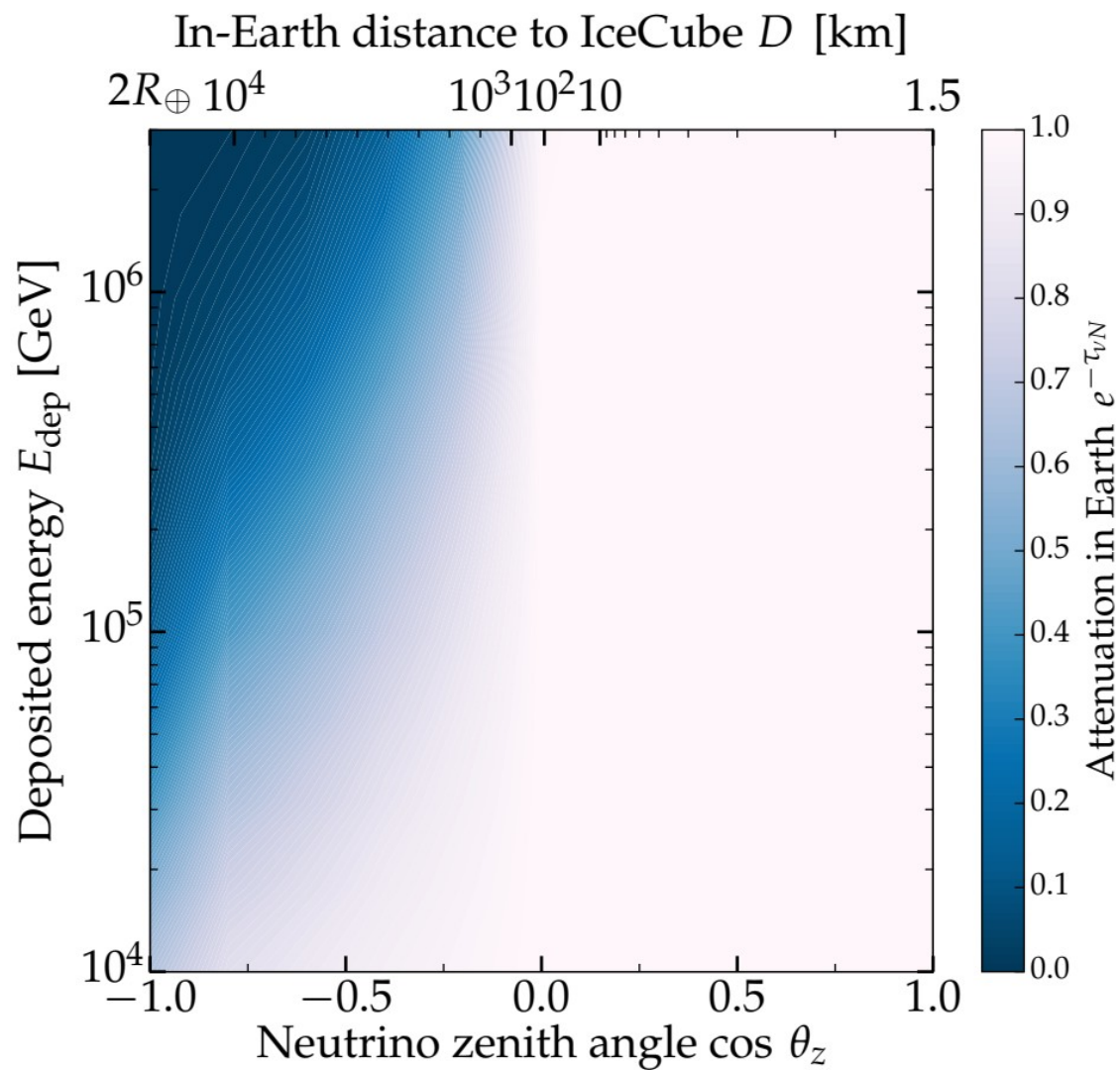


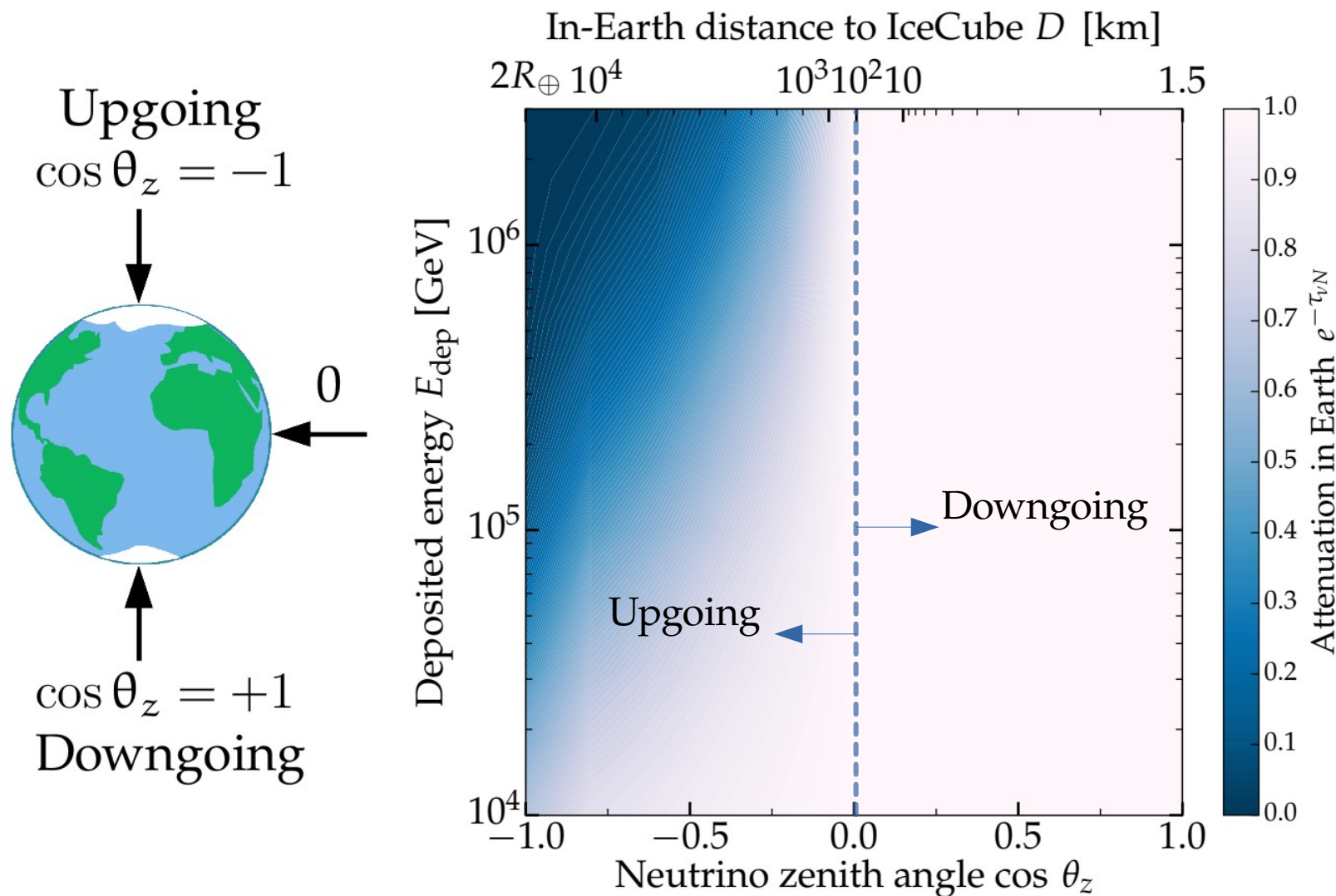
Full
attenuation

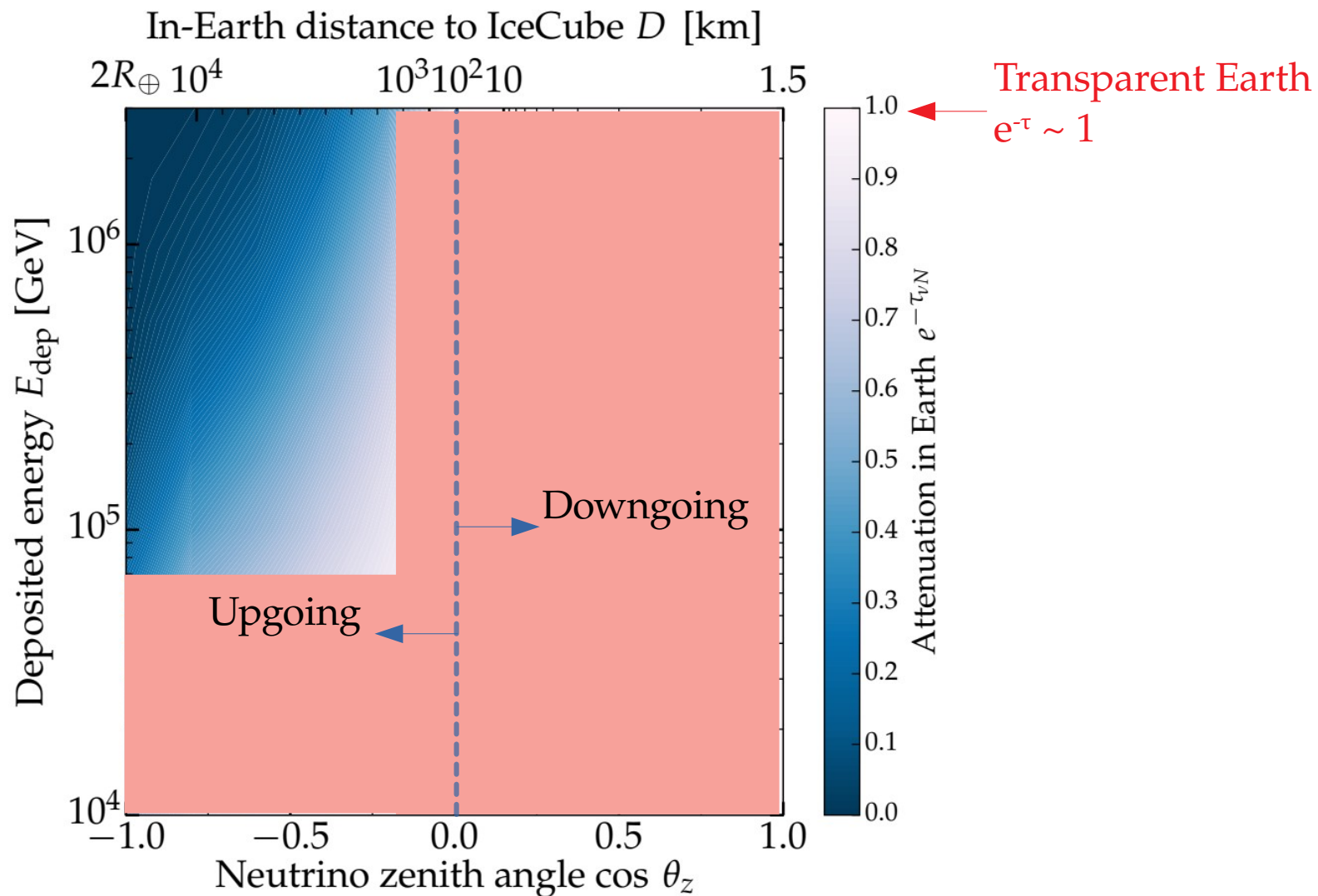
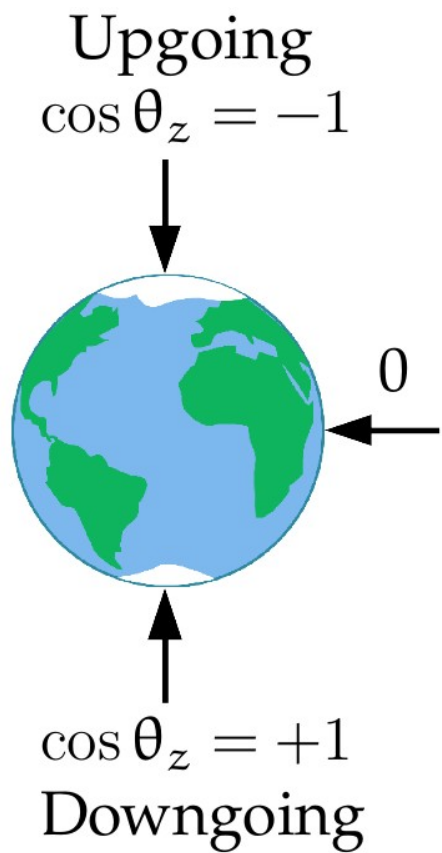
Upgoing
 $\cos \theta_z = -1$

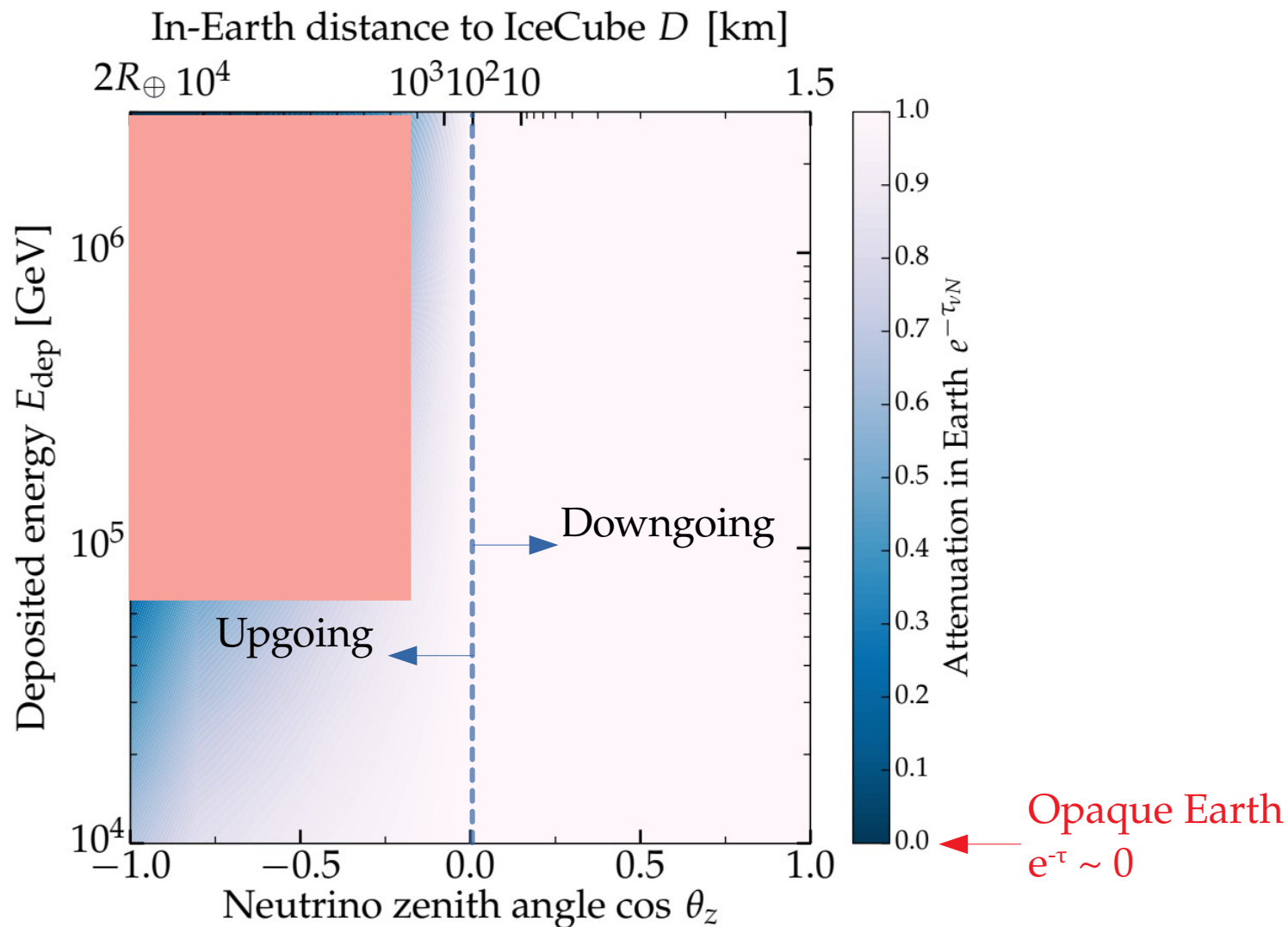
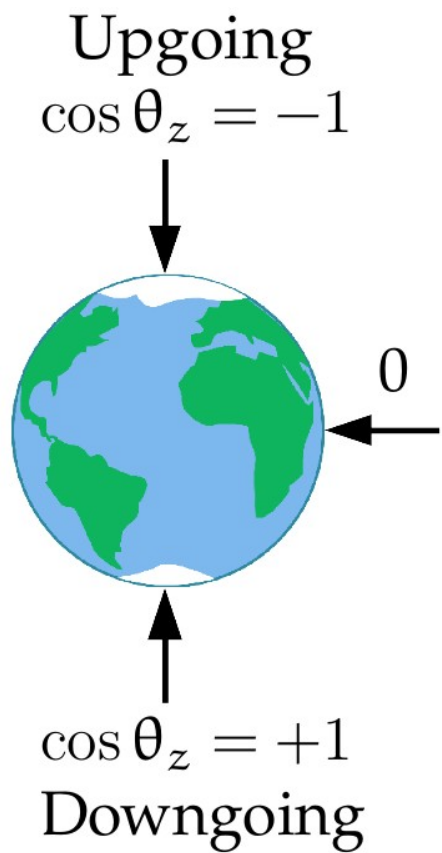


$\cos \theta_z = +1$
Downgoing









Use NuPropEarth for in-Earth propagation

[github.com/pochoarus/NuPropEarth]

Interactions:

- ▶ BGR18 νN deep inelastic scattering (DIS) on partons (**dominant**)
- ▶ DIS on photon field of nucleons
- ▶ Coherent νA scattering
- ▶ Elastic & diffractive νN scattering
- ▶ ν scattering on atomic electrons

Sub-dominant:
increase attenuation
by $\sim 10\%$

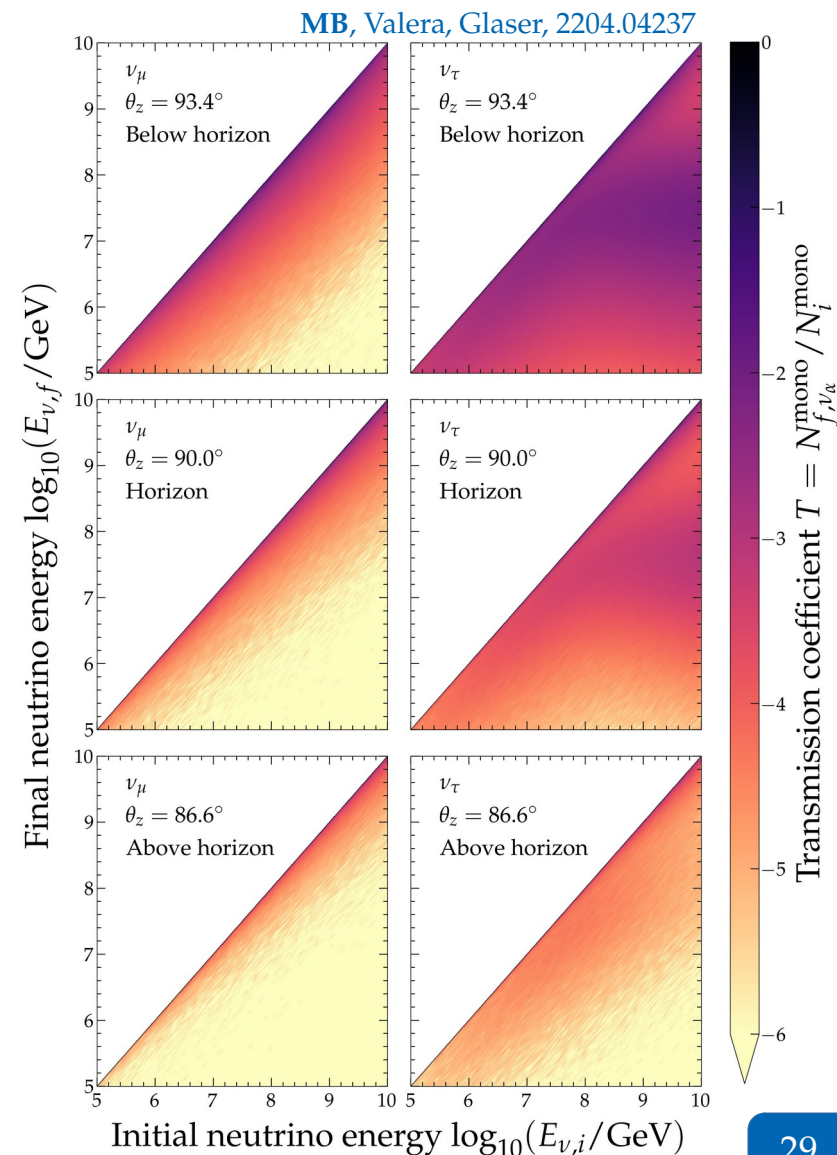
Includes ν_τ regeneration:

- ▶ TAUSIC: Energy losses of intermediate τ
- ▶ TAUOLA: Distribution of τ decay products

Matter inside Earth:

- ▶ Density: Preliminary Reference Earth Model
- ▶ Top layer of ice
- ▶ Varying element composition (non-isoscalar)

We propagate $\nu_e, \bar{\nu}_e, \nu_\mu, \bar{\nu}_\mu, \nu_\tau, \bar{\nu}_\tau$ separately



Use NuPropEarth for in-Earth propagation

[github.com/pochoarus/NuPropEarth]

Interactions:

- ▶ BGR18 νN deep inelastic scattering (DIS) on partons (**dominant**)
- ▶ DIS on photon field of nucleons
- ▶ Coherent νA scattering
- ▶ Elastic & diffractive νN scattering
- ▶ ν scattering on atomic electrons

Sub-dominant:
increase attenuation
by ~10%

Includes ν_τ regeneration:

- ▶ TAUSIC: Energy losses of intermediate τ
- ▶ TAUOLA: Distribution of τ decay products

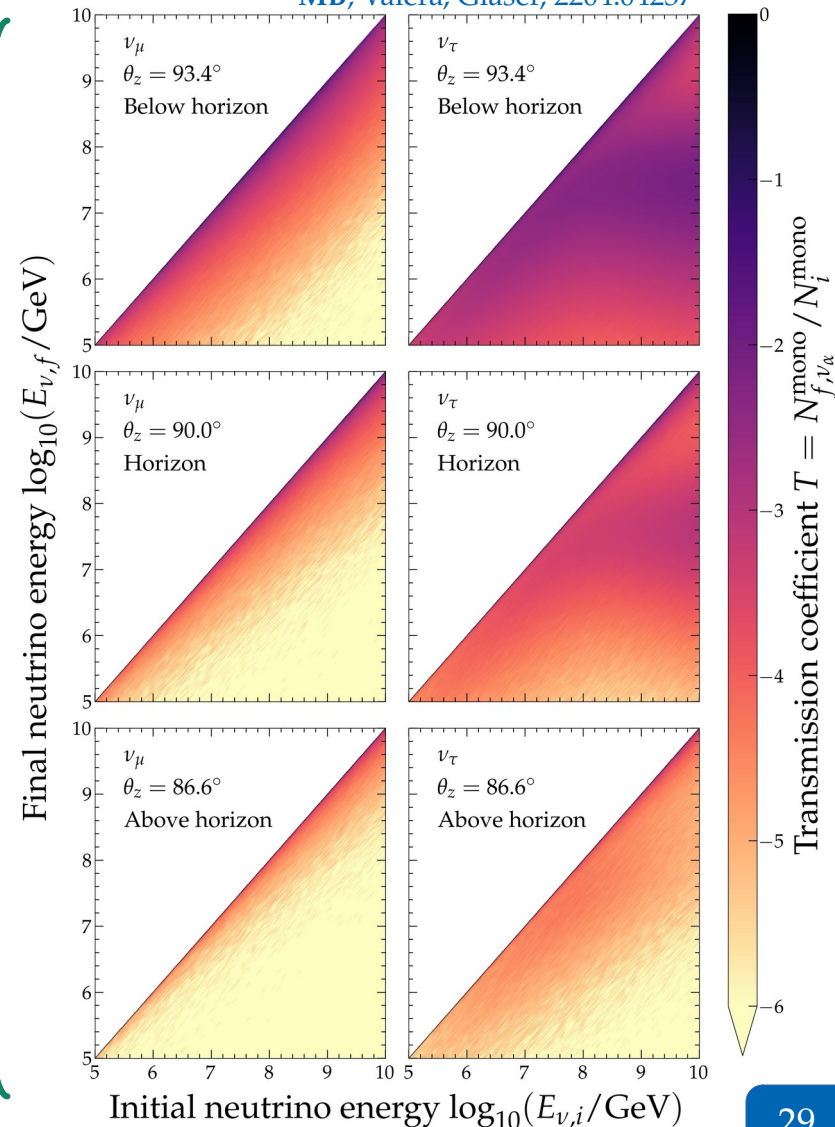
Matter inside Earth:

- ▶ Density: Preliminary Reference Earth Model
- ▶ Top layer of ice
- ▶ Varying element composition (non-isoscalar)

We propagate $\nu_e, \bar{\nu}_e, \nu_\mu, \bar{\nu}_\mu, \nu_\tau, \bar{\nu}_\tau$ separately

Save look-up
tables of
propagated
 ν spectra

MB, Valera, Glaser, 2204.04237



Use NuPropEarth for in-Earth propagation

[github.com/pochoarus/NuPropEarth]

Interactions:

- ▶ BGR18 νN deep inelastic scattering (DIS) on partons
- ▶ DIS on photon field of nucleons
- ▶ Coherent νA scattering
- ▶ Elastic & diffractive νN scattering
- ▶ ν scattering on atomic electrons

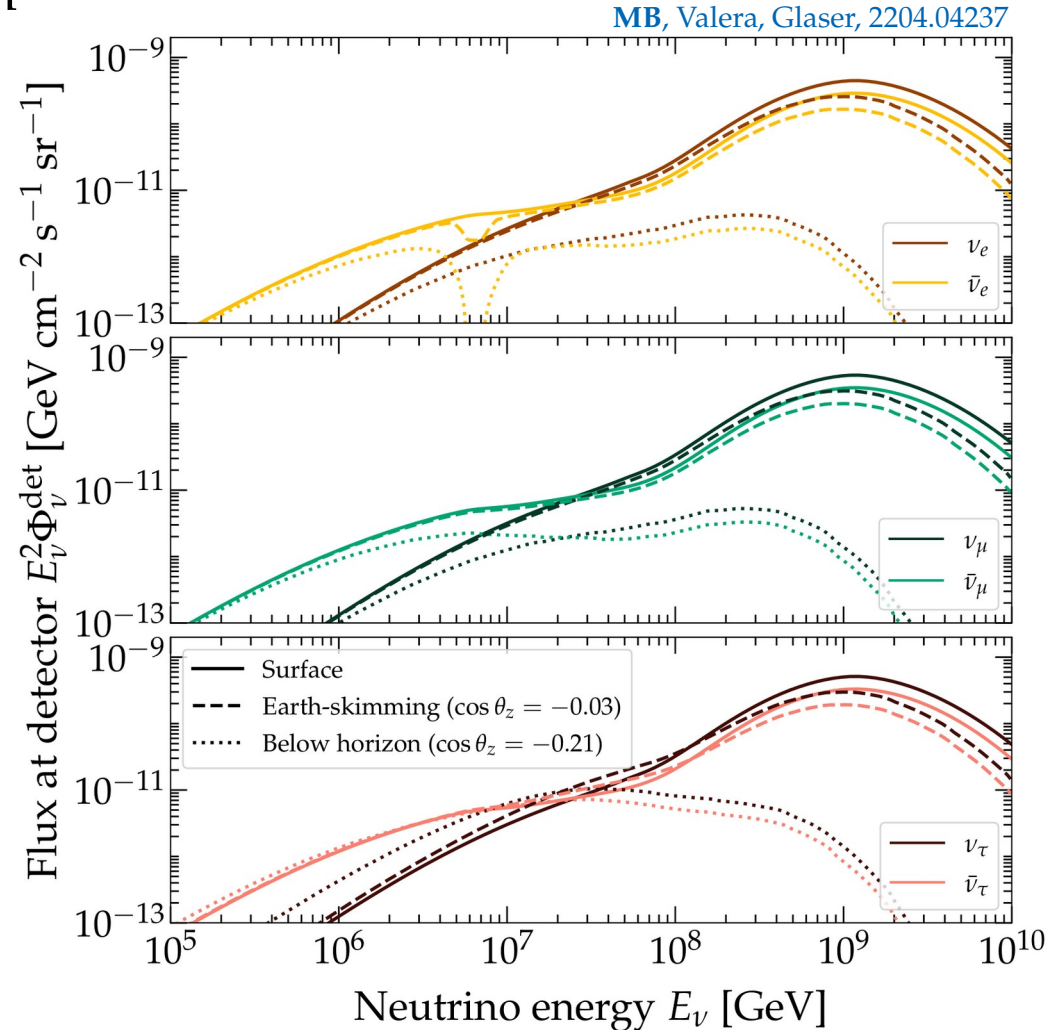
Includes ν_τ regeneration:

- ▶ TAUSIC: Energy losses of intermediate τ
- ▶ TAUOLA: Distribution of τ decay products

Matter inside Earth:

- ▶ Density: Preliminary Reference Earth Model
- ▶ Top layer of ice
- ▶ Varying element composition (non-isoscalar)

We propagate $\nu_e, \bar{\nu}_e, \nu_\mu, \bar{\nu}_\mu, \nu_\tau, \bar{\nu}_\tau$ separately



Detector geometry

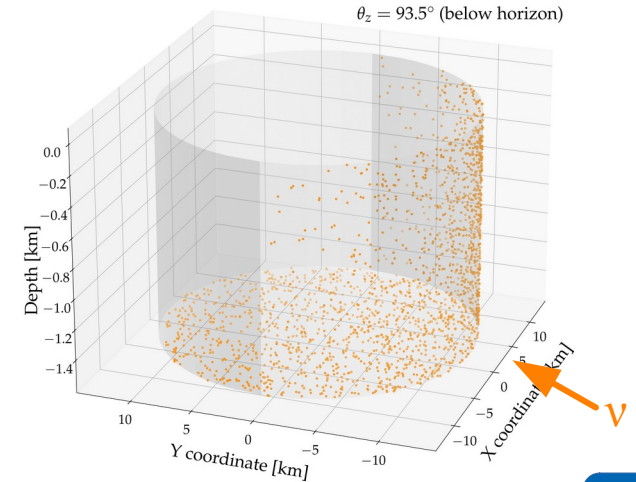
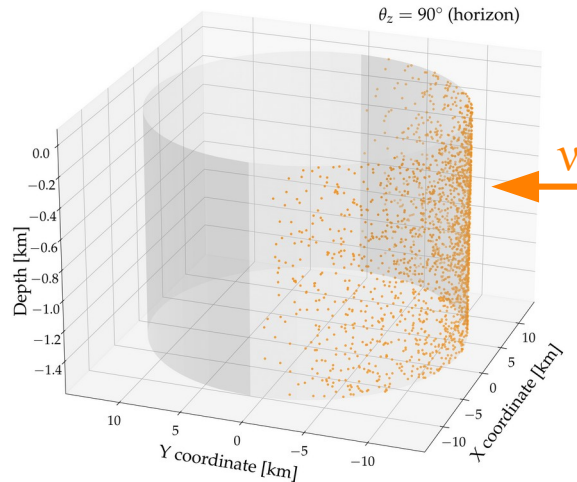
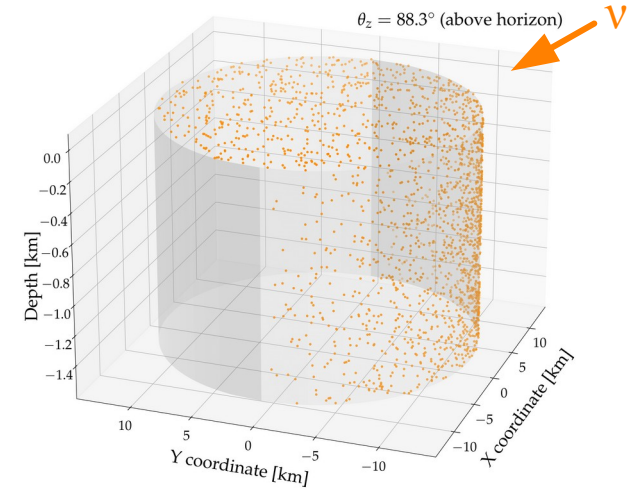
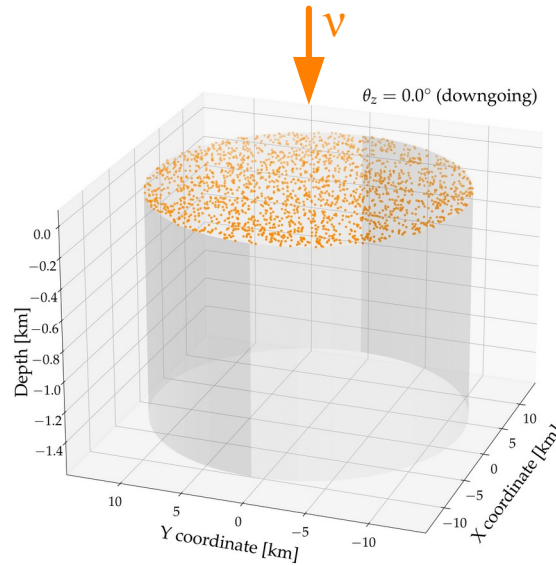
Underground cylinder

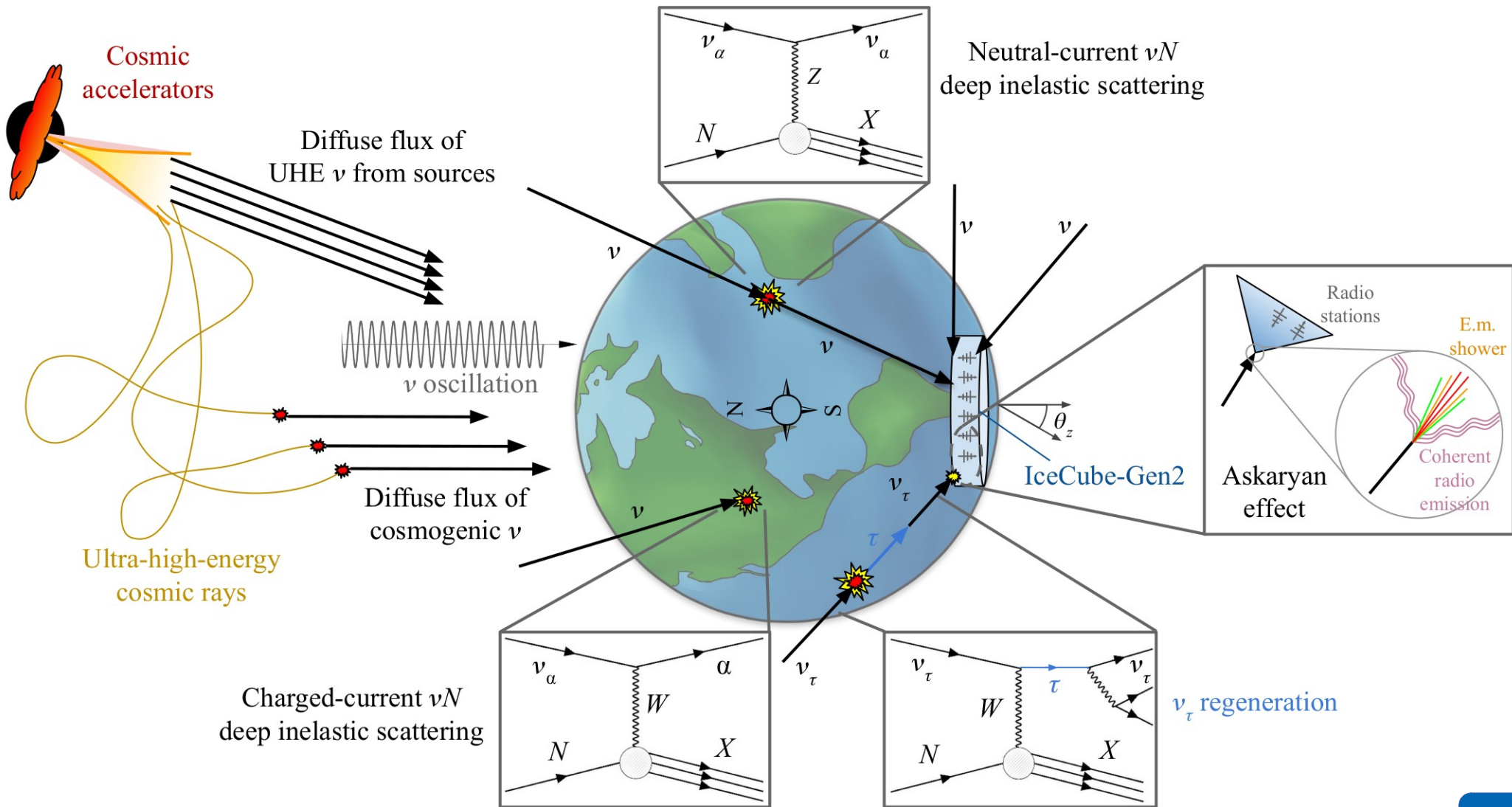
Area of lid: 500 km^2

Height: 1.5 km

Detector geometry now
available in NuPropEarth

[\[github.com/pochoarus/NuPropEarth\]](https://github.com/pochoarus/NuPropEarth)

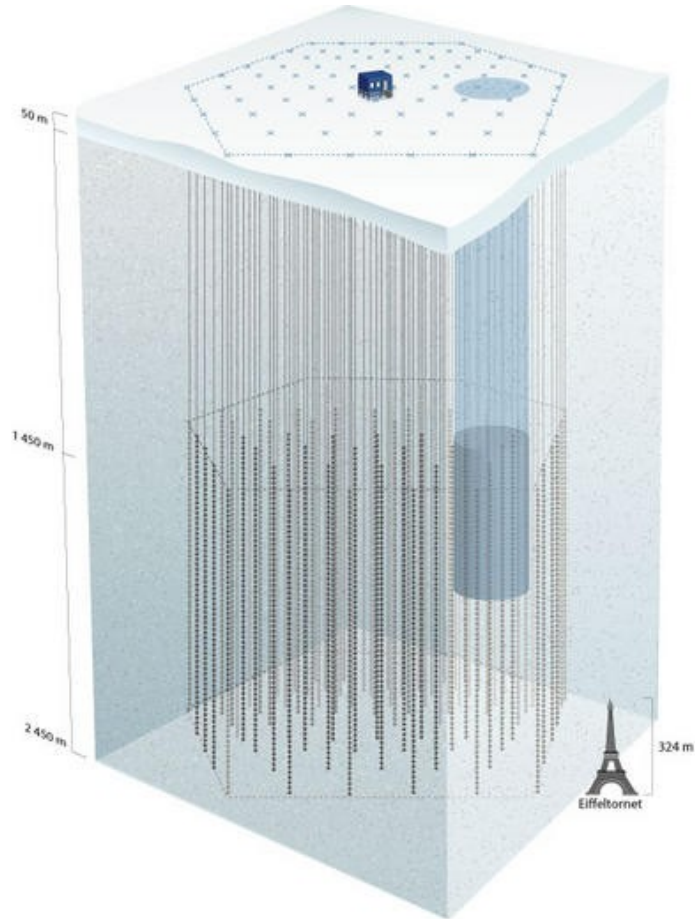




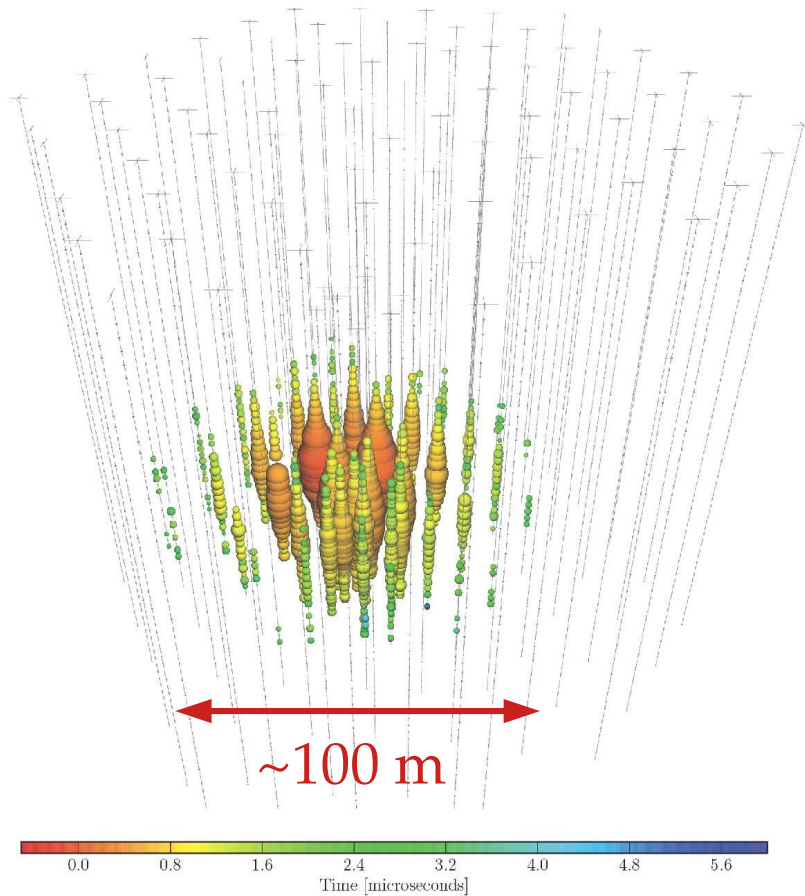


TeV–PeV ν : IceCube

- ▶ Km^3 in-ice Cherenkov detector in Antarctica
- ▶ > 5000 PMTs at 1.5–2.5 km of depth
- ▶ Sensitive to neutrino energies > 10 GeV

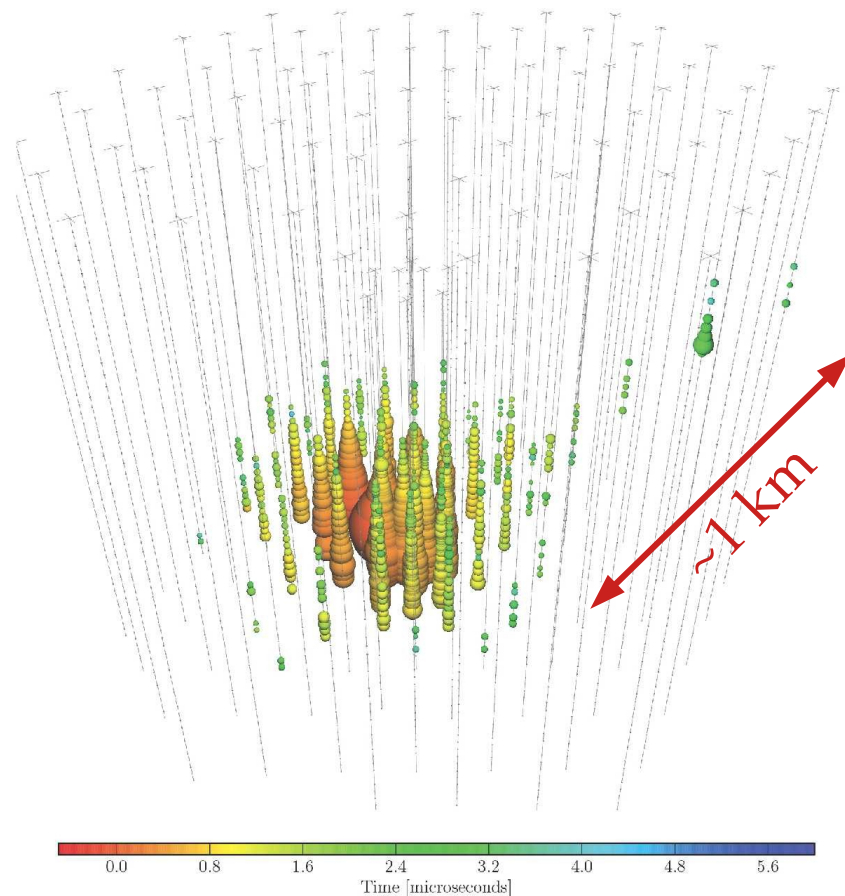


Shower
(mainly from ν_e and ν_τ)



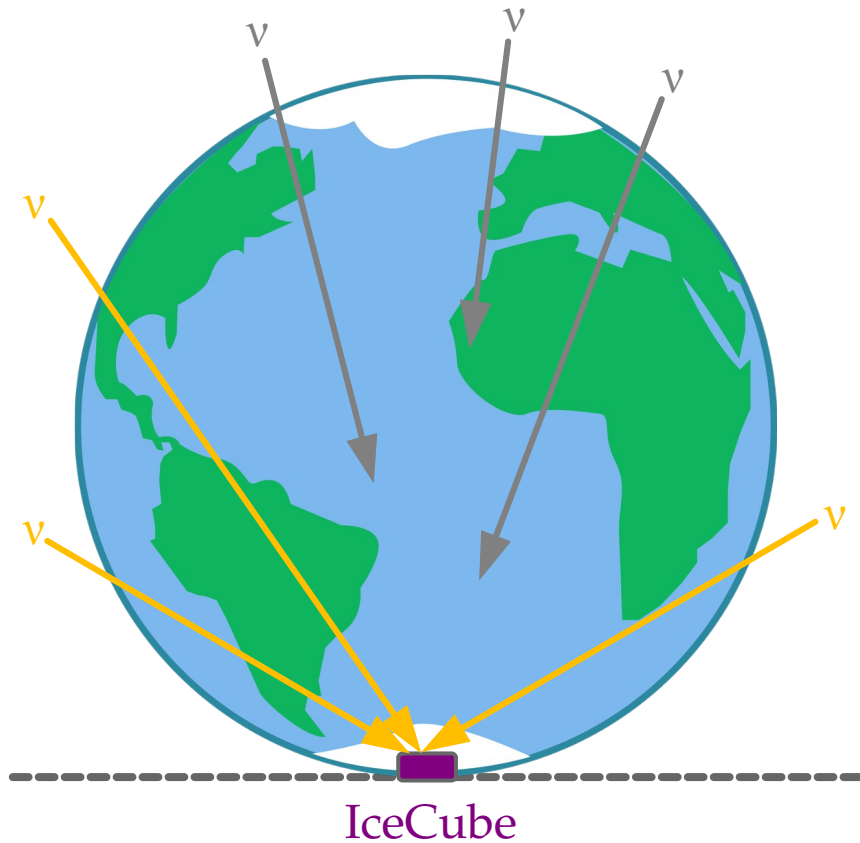
Poor angular resolution: $\sim 10^\circ$

Track
(mainly from ν_μ)

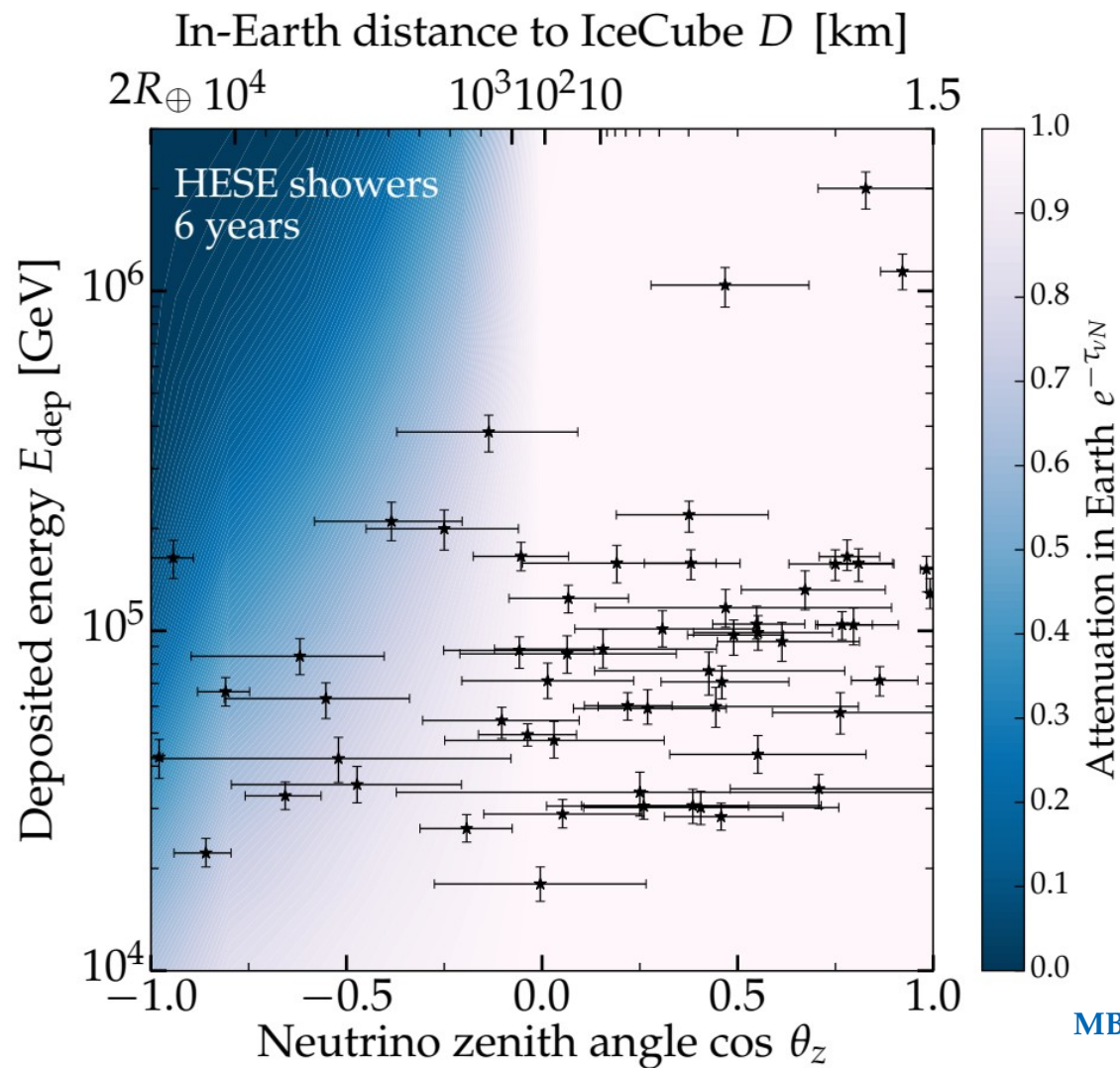


Angular resolution: $< 1^\circ$

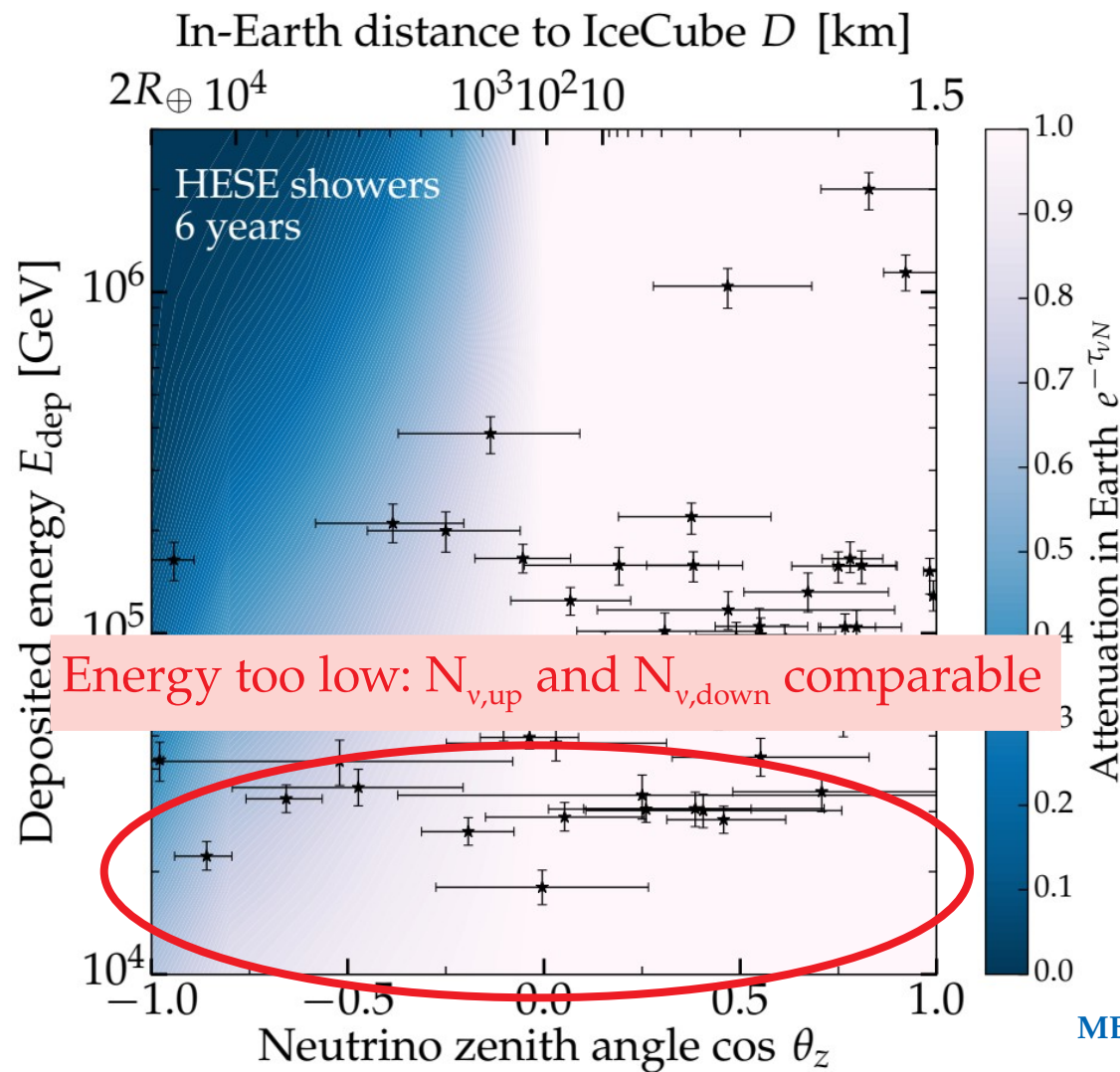
TeV–PeV:



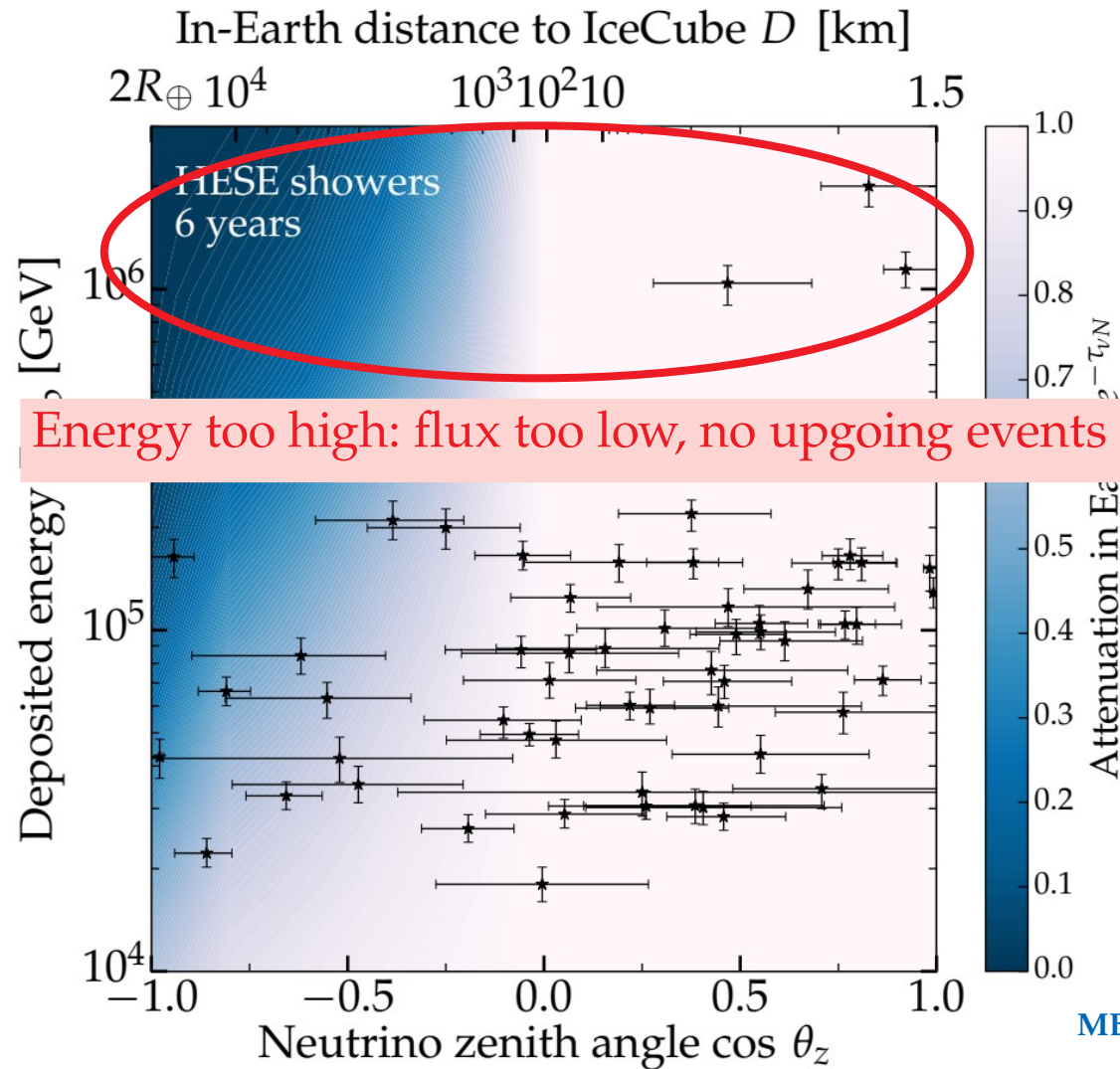
Earth is *almost fully* opaque,
some upgoing ν still make it through



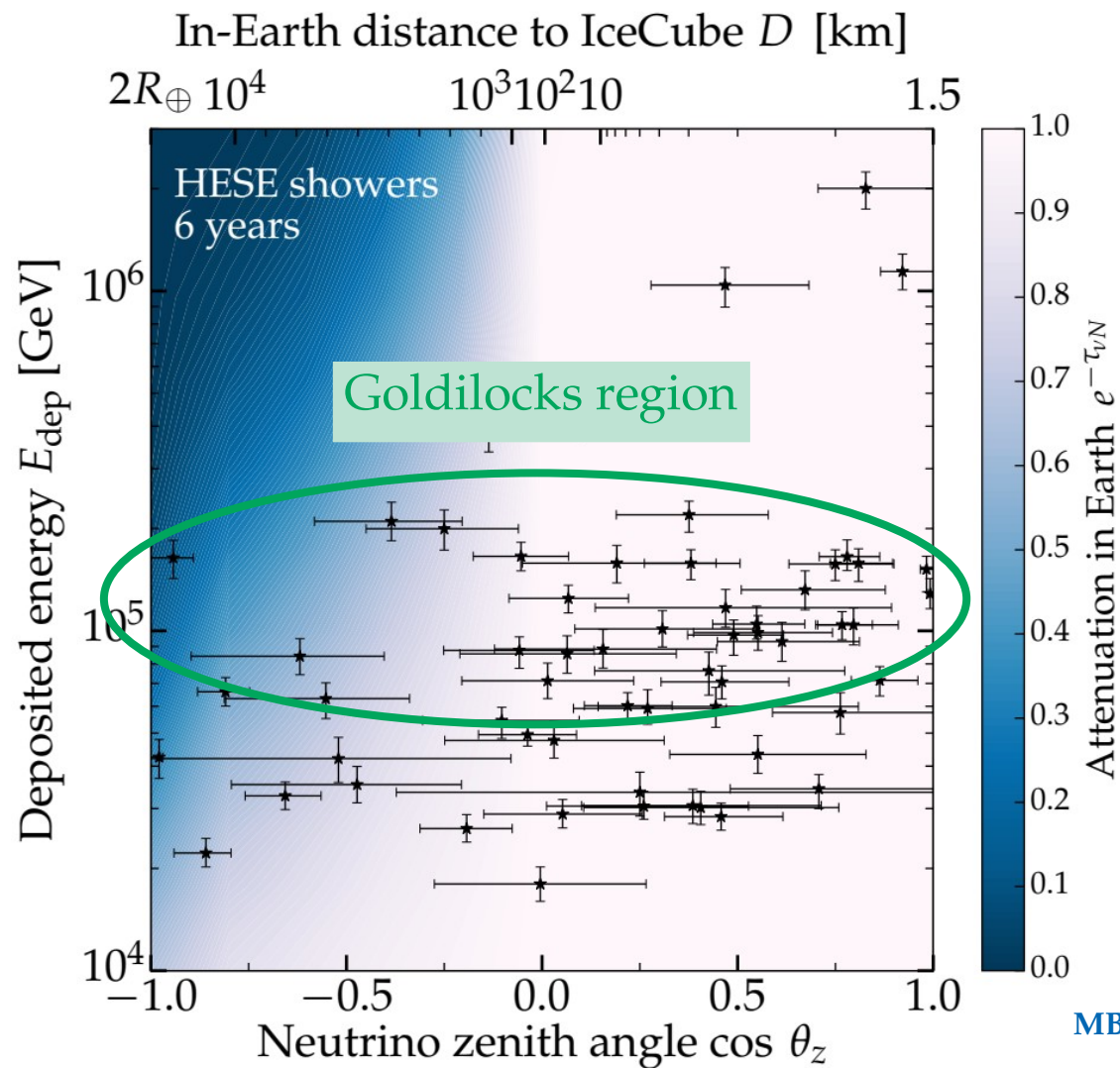
MB & Connolly, *PRL* 2019



MB & Connolly, *PRL* 2019

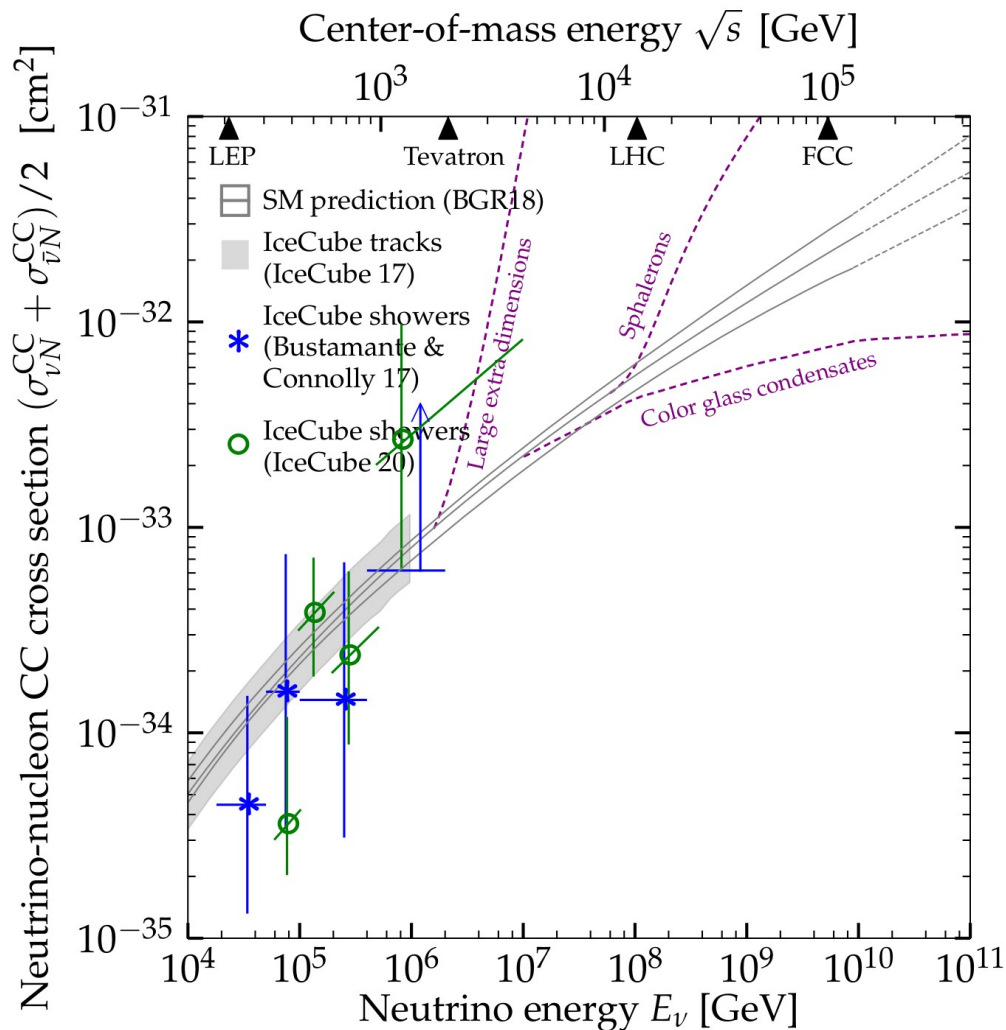


MB & Connolly, *PRL* 2019



MB & Connolly, *PRL* 2019

TeV–PeV νN cross section: *today*

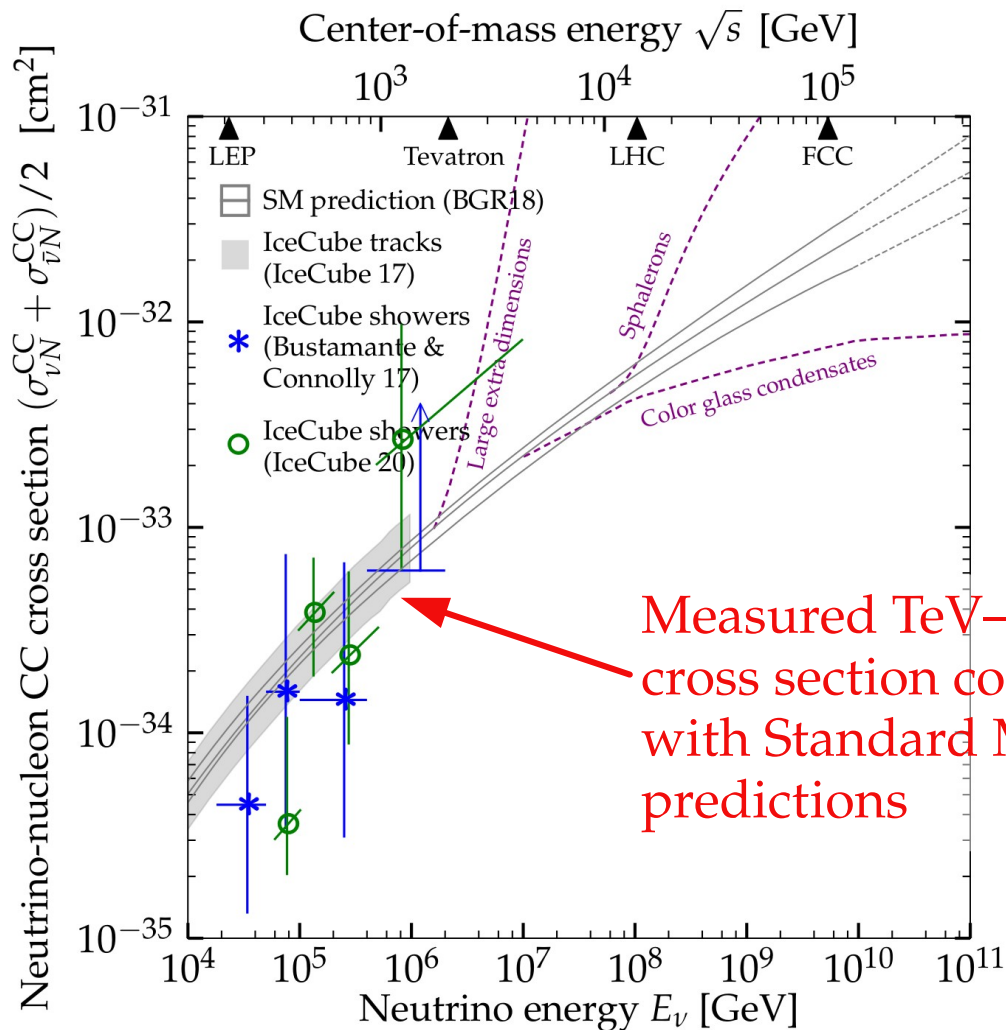


BGR18 prediction from:
[Bertone, Gauld, Rojo, JHEP 2019](#)

See also:
[García, Gauld, Heijboer, Rojo, JCAP 2020](#)

Measurements from:
[IceCube, 2011.03560](#)
[MB & Connolly, PRL 2019](#)
[IceCube, Nature 2017](#)

TeV–PeV νN cross section: *today*

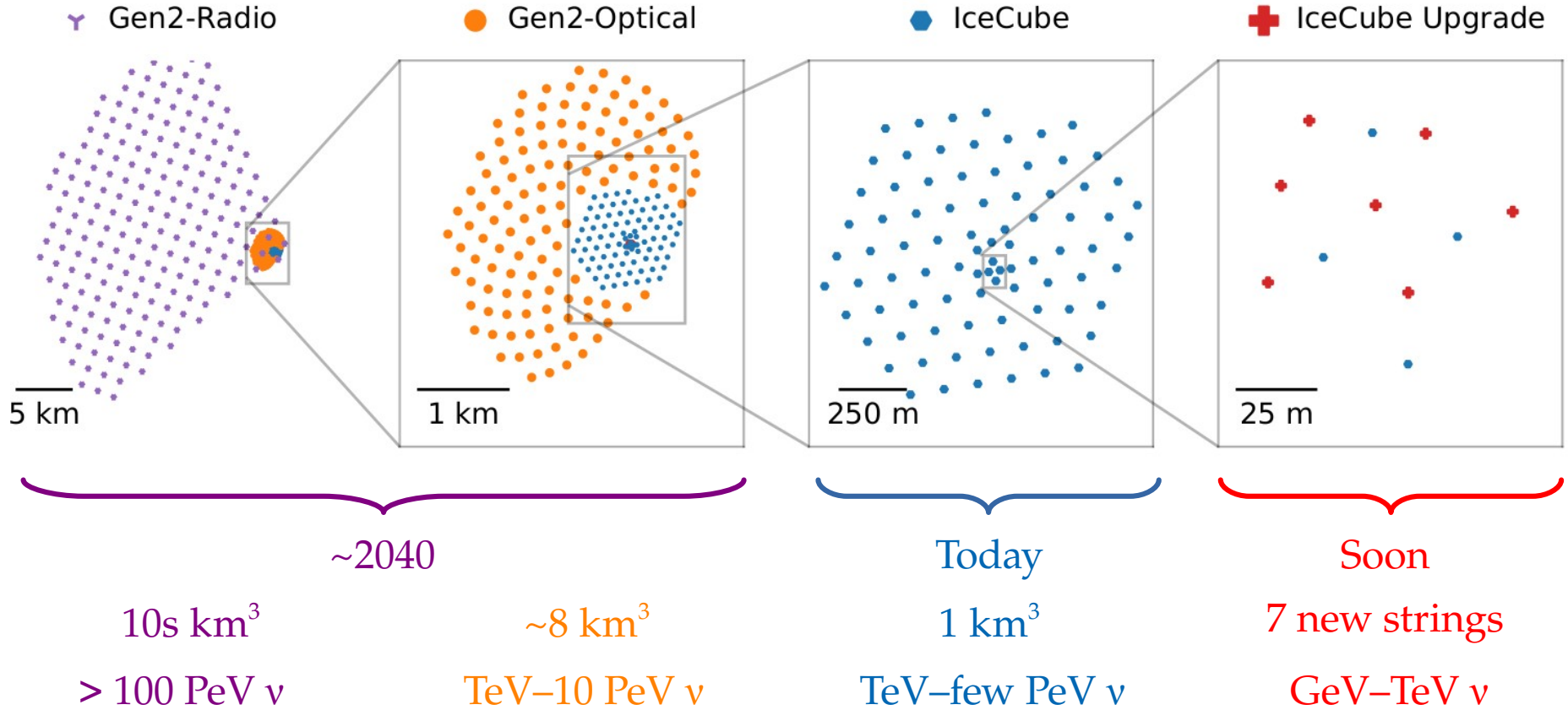


BGR18 prediction from:
[Bertone, Gauld, Rojo, JHEP 2019](#)

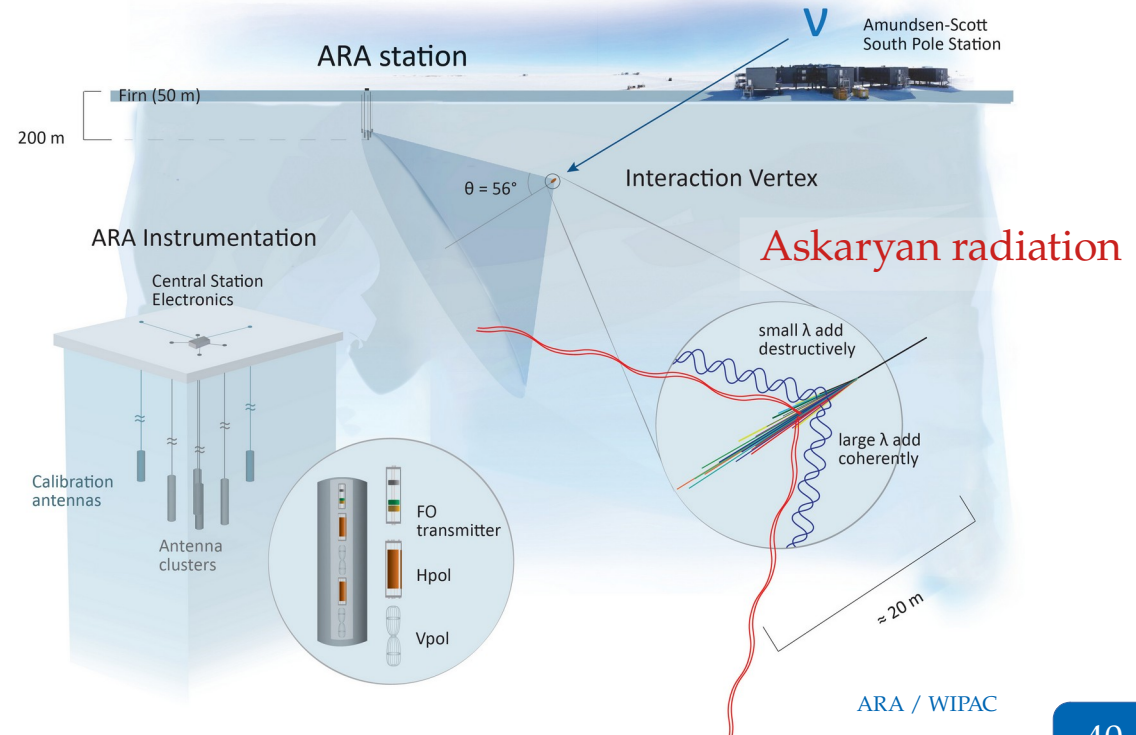
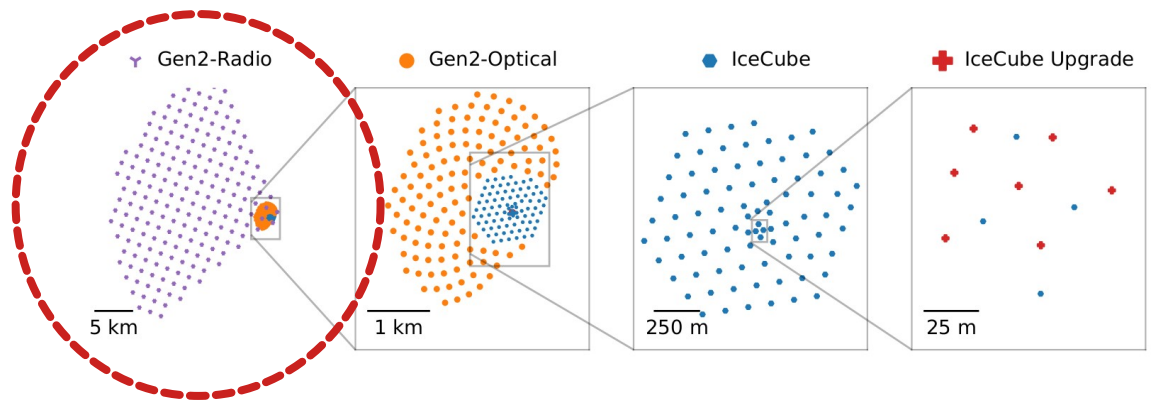
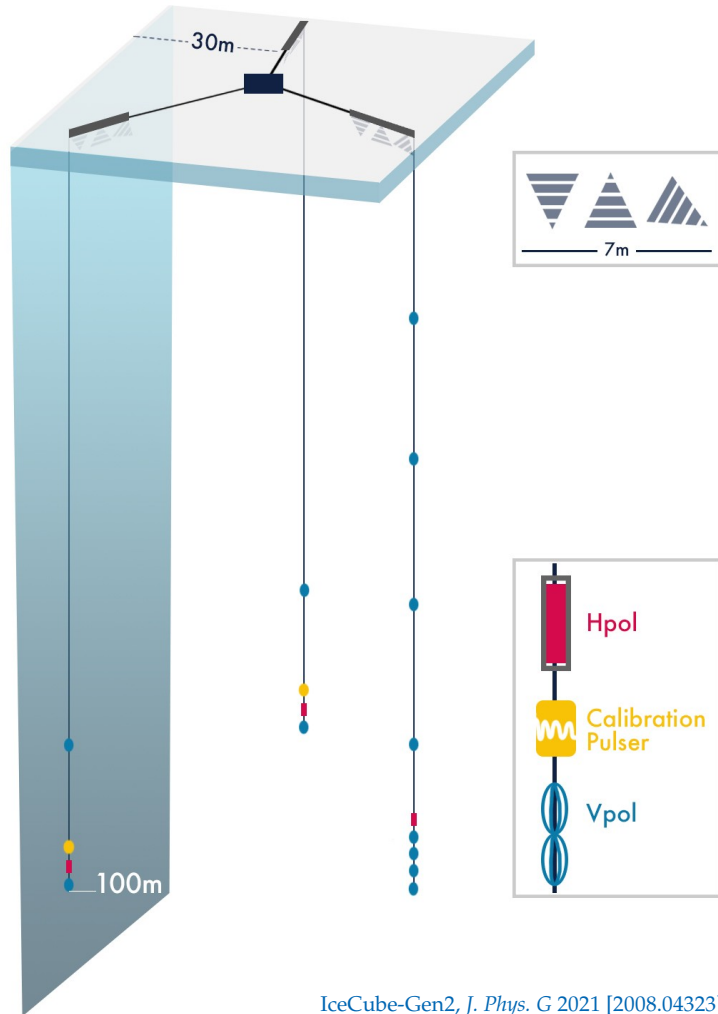
See also:
[García, Gauld, Heijboer, Rojo, JCAP 2020](#)

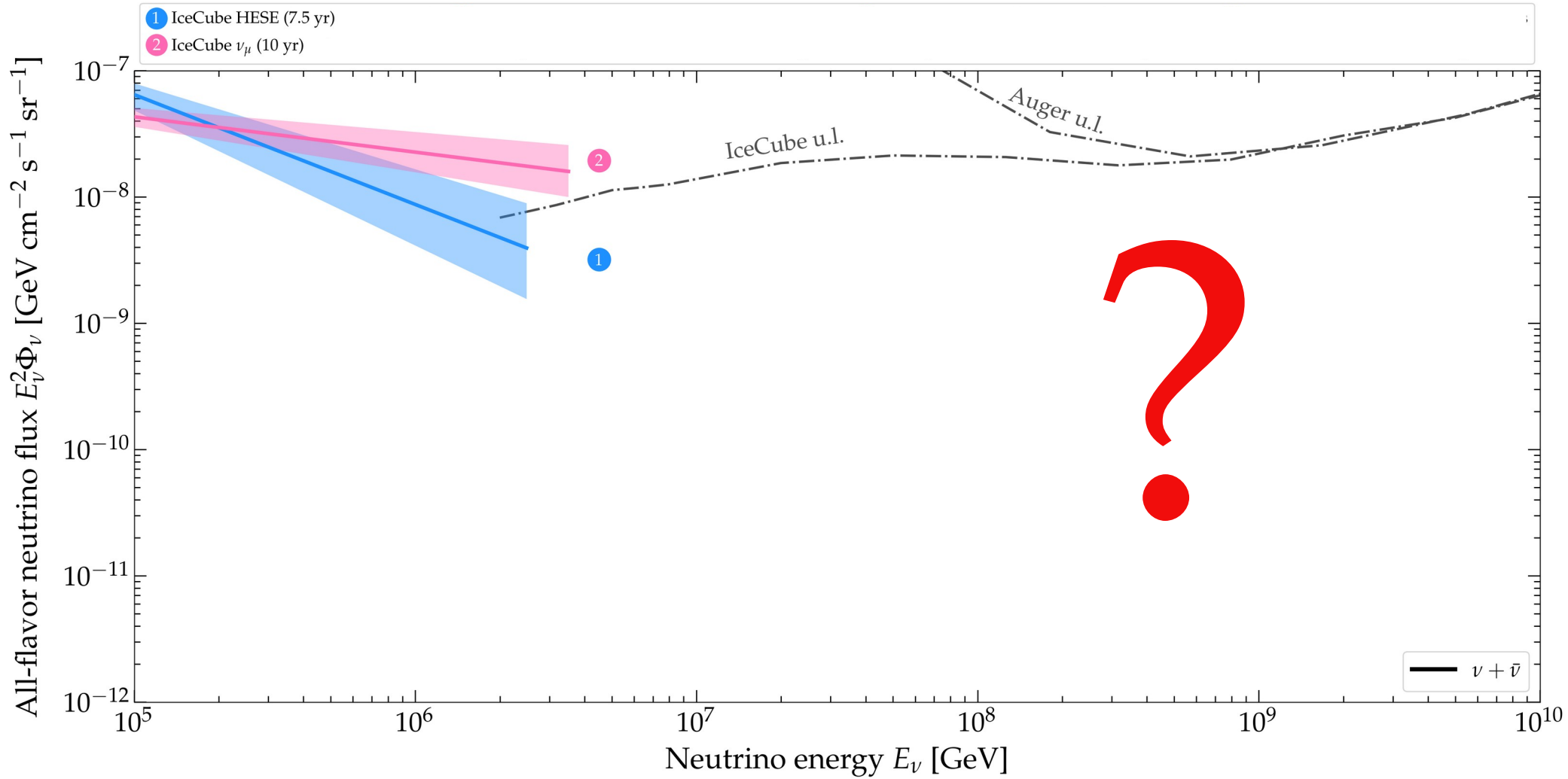
Measurements from:
[IceCube, 2011.03560](#)
[MB & Connolly, PRL 2019](#)
[IceCube, Nature 2017](#)

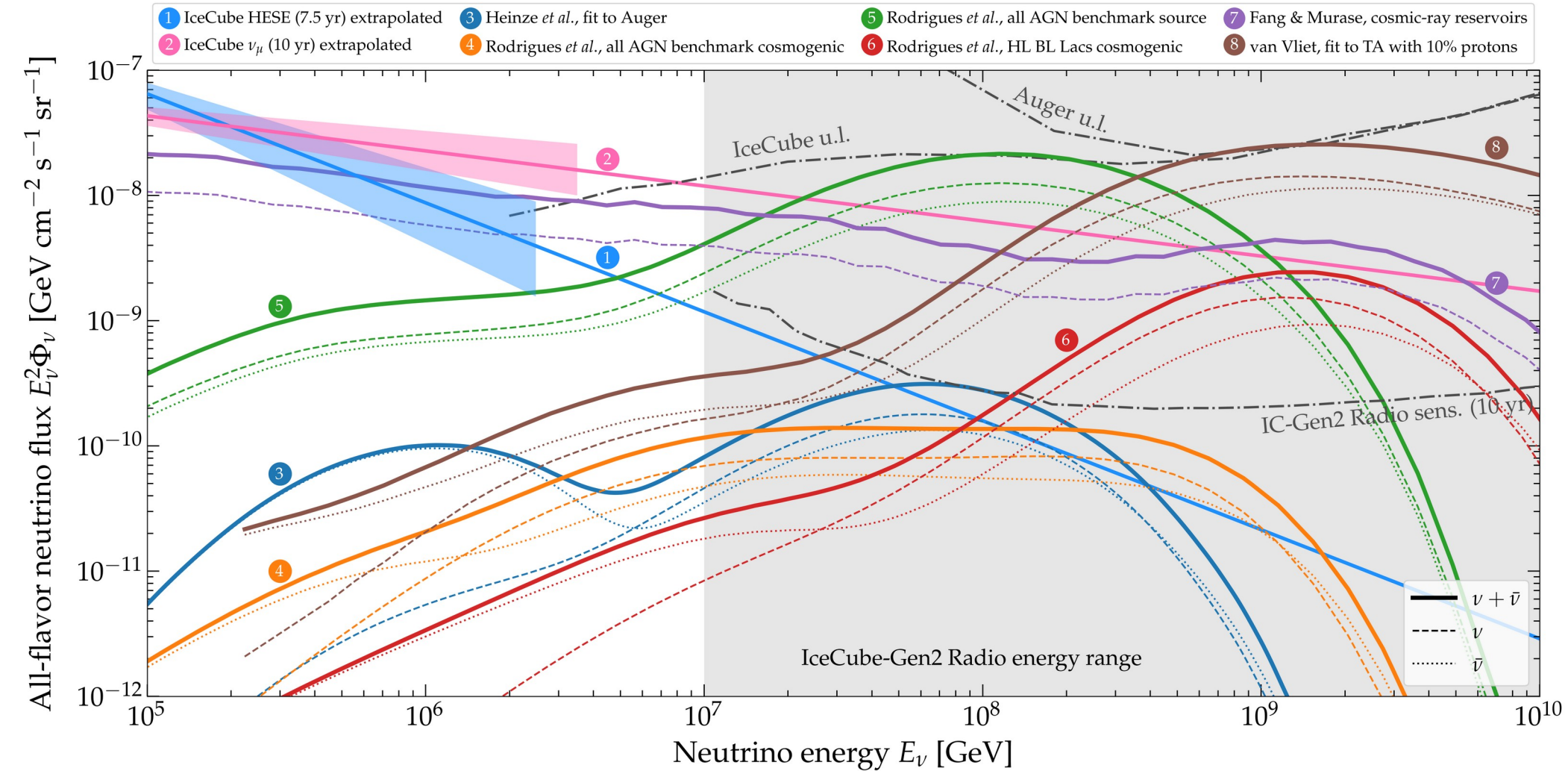
> 100 EeV ν : IceCube-Gen2



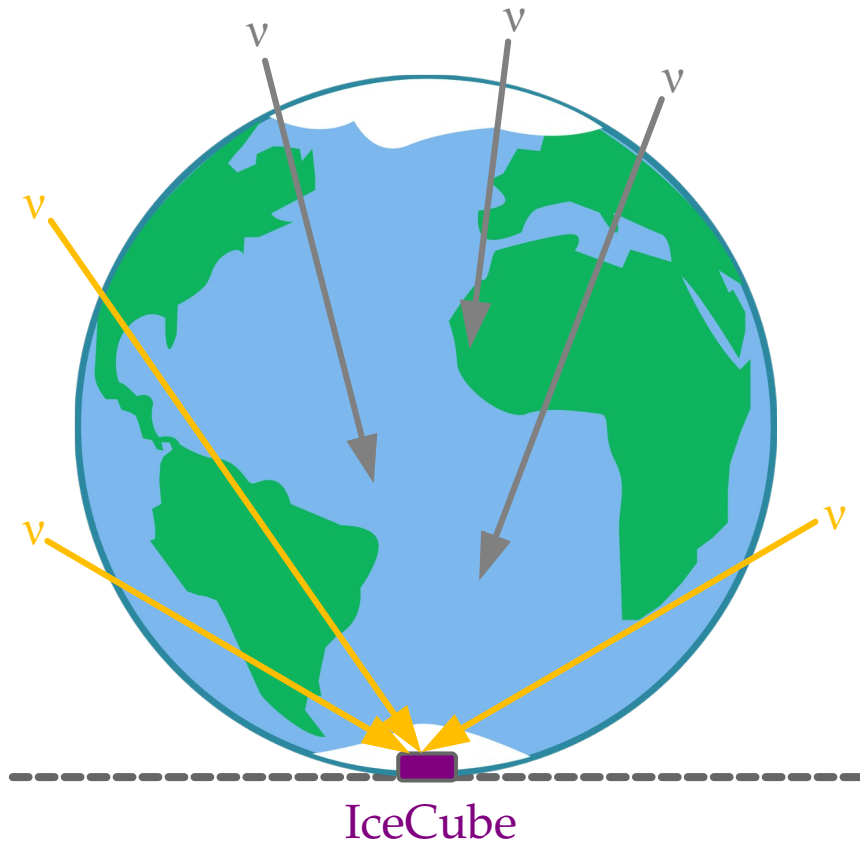
IceCube-Gen2 Radio





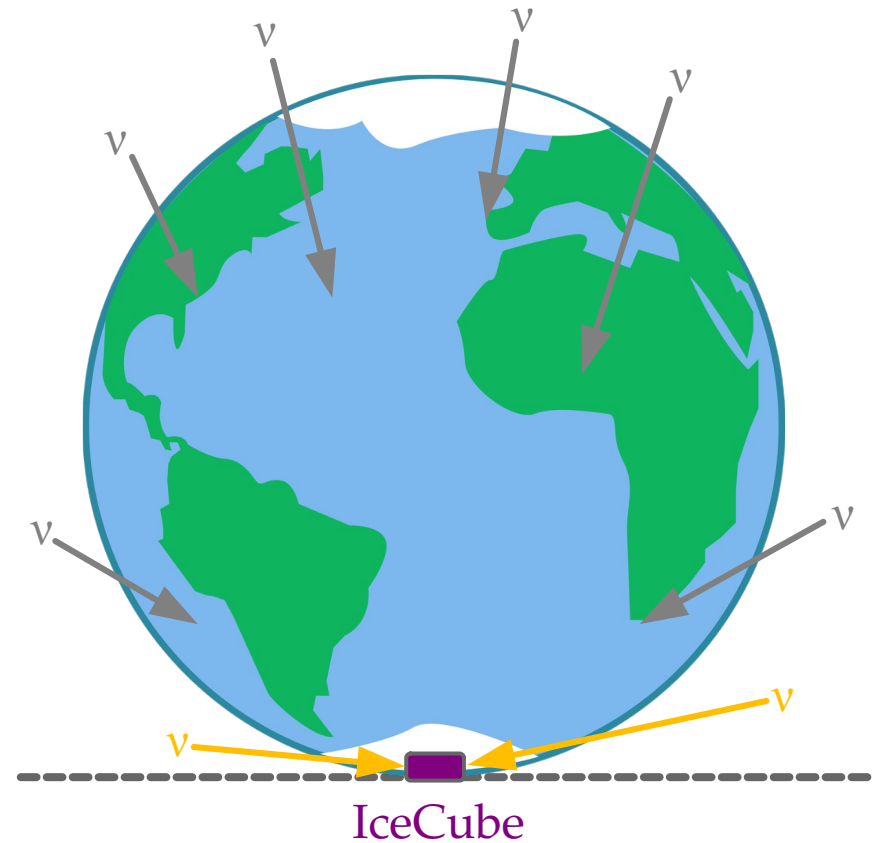


TeV–PeV:



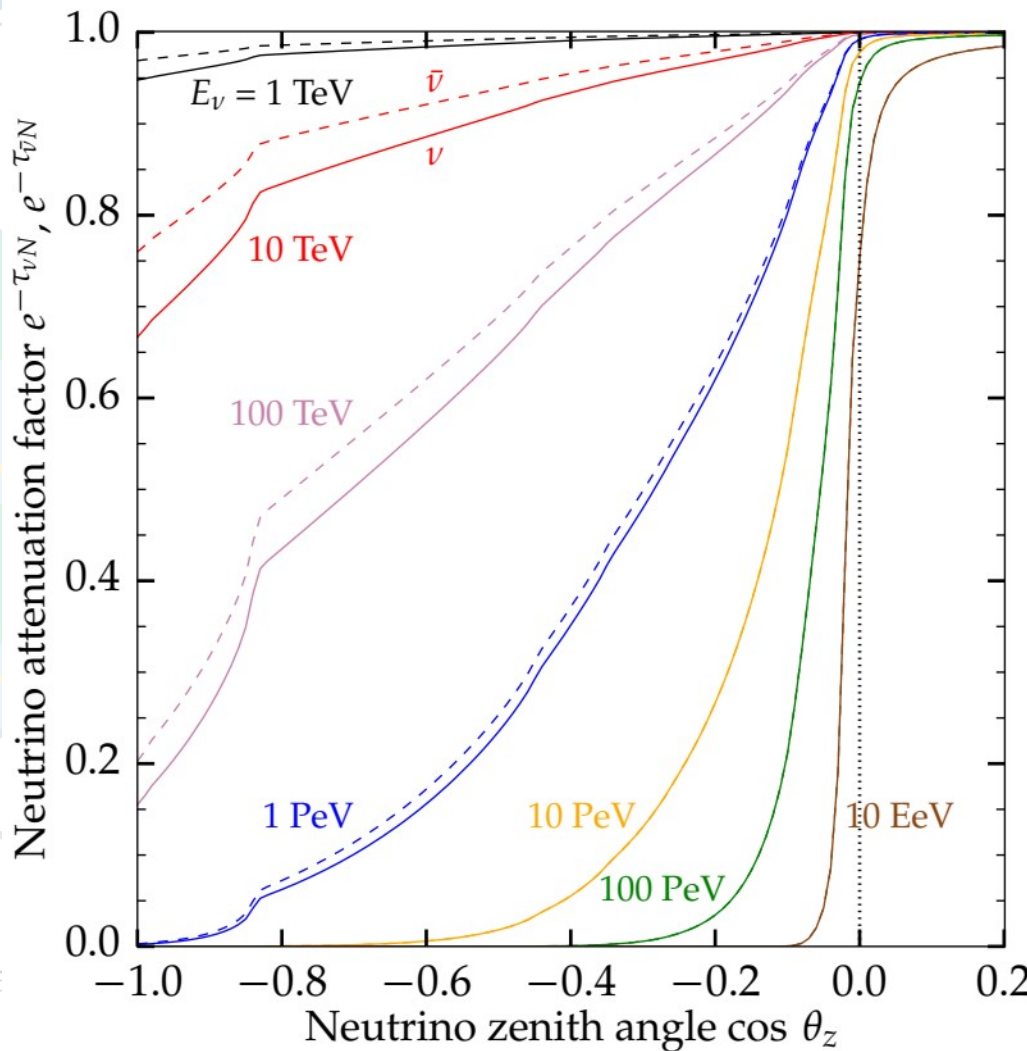
Earth is *almost fully* opaque,
some upgoing ν still make it through

> 100 PeV:

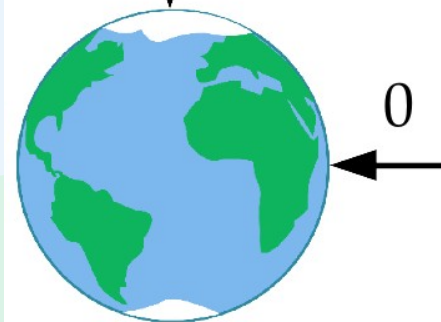


Earth is *completely* opaque,
but horizontal ν still make it through

TeV–PeV

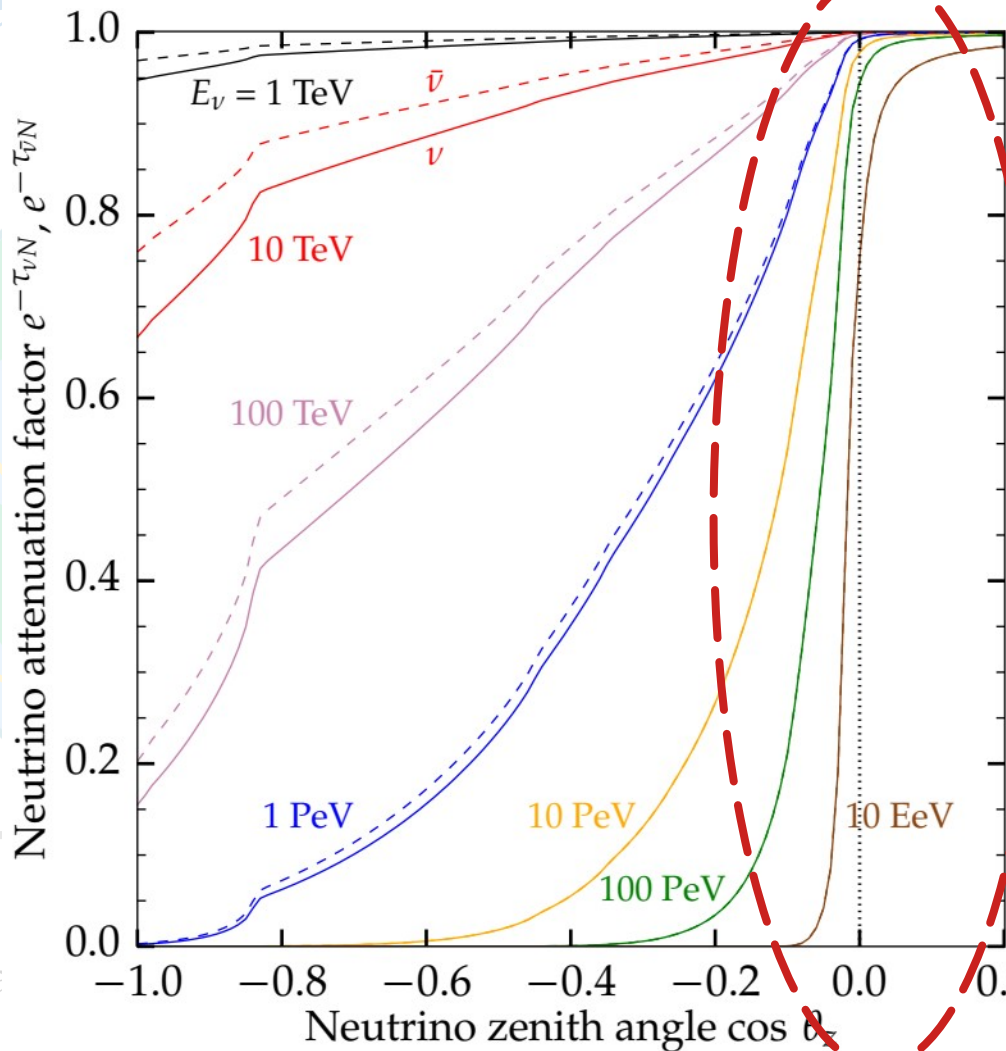


Upgoing
 $\cos \theta_z = -1$

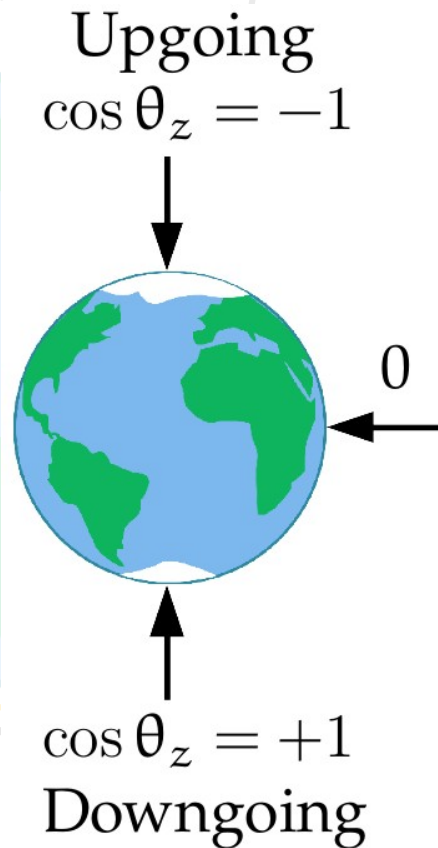


$\cos \theta_z = +1$
Downgoing

Earth is completely opaque,
horizontal ν still make it through



At UHE, we can only extract the cross section using horizontal ν



Earth is completely opaque, horizontal ν still make it through

Measuring neutrino-nucleon cross sections at UHE

Baseline Gen2 radio array design:

- ▶ 169 hybrid stations (shallow + deep) + 144 deep stations
- ▶ Detector angular resolution (zenith angle): 2°
- ▶ Detector shower energy resolution: 10%

*Ask about
alternative choices*

Detailed event-rate calculation scheme:

- ▶ V_{eff} vs. shower energy vs. angle, custom-generated in NuRadioMC
- ▶ In-Earth propagation, leading & sub-leading ν interactions in NuPropEarth
- ▶ Inelasticity distribution factored in
- ▶ Use recent cross-section predictions as baseline
- ▶ Background from atmospheric muons (< 0.1 event per year above 10^7 GeV)

Event rate at IC-Gen2 Radio

Event rate at IC-Gen2 Radio

Real event rate

$$\frac{d^3 N_{\nu_\alpha}^{\text{CC}}}{dE_\nu dy d\cos\theta_z}$$

E_ν : Neutrino energy

y : Inelasticity

$\cos\theta_z$: Neutrino direction

Includes:

- ▶ Flux
- ▶ In-Earth propagation
- ▶ Effective volume
- ▶ Inelasticity distribution

Event rate at IC-Gen2 Radio

Real event rate

$$\frac{d^3 N_{\nu_\alpha}^{\text{CC}}}{dE_\nu dy d\cos\theta_z}$$

E_ν : Neutrino energy

y : Inelasticity

$\cos\theta_z$: Neutrino direction

Detector effects

Each ν species
computed separately

Includes:

- Flux
- In-Earth propagation
- Effective volume
- Inelasticity distribution

Event rate at IC-Gen2 Radio

Real event rate

$$\frac{d^3 N_{\nu_\alpha}^{\text{CC}}}{dE_\nu dy d\cos\theta_z}$$

E_ν : Neutrino energy

y : Inelasticity

$\cos\theta_z$: Neutrino direction

Includes:

- Flux
- In-Earth propagation
- Effective volume
- Inelasticity distribution

Detector effects

Each ν species
computed separately

Detected event rate

$$\frac{d^2 N_{\nu_\alpha}^{\text{CC}}}{dE_{\text{sh}}^{\text{rec}} d\theta_z^{\text{rec}}}$$

$E_{\text{sh}}^{\text{rec}}$: Reconstructed *shower* energy

$\cos\theta_z^{\text{rec}}$: Reconstructed direction

Includes, in addition:

- Connection between ν energy and shower energy
- Energy resolution
- Angular resolution

Event rate at IC-Gen2 Radio

Note: Calculations are similar for CC and NC

Real event rate

$$\frac{d^3 N_{\nu_\alpha}^{\text{CC}}}{dE_\nu dy d\cos\theta_z}$$

E_ν : Neutrino energy

y : Inelasticity

$\cos\theta_z$: Neutrino direction

Includes:

- Flux
- In-Earth propagation
- Effective volume
- Inelasticity distribution

Detector effects

Each ν species
computed separately

Detected event rate

$$\frac{d^2 N_{\nu_\alpha}^{\text{CC}}}{dE_{\text{sh}}^{\text{rec}} d\theta_z^{\text{rec}}}$$

$E_{\text{sh}}^{\text{rec}}$: Reconstructed *shower* energy

$\cos\theta_z^{\text{rec}}$: Reconstructed direction

Includes, in addition:

- Connection between ν energy and shower energy
- Energy resolution
- Angular resolution

Detector effective volume

IC-Gen2 has stations containing:

- ▶ Shallow antennas
- ▶ Deep antennas

Detector effective volume

IC-Gen2 has stations containing:

- ▶ Shallow antennas
- ▶ Deep antennas

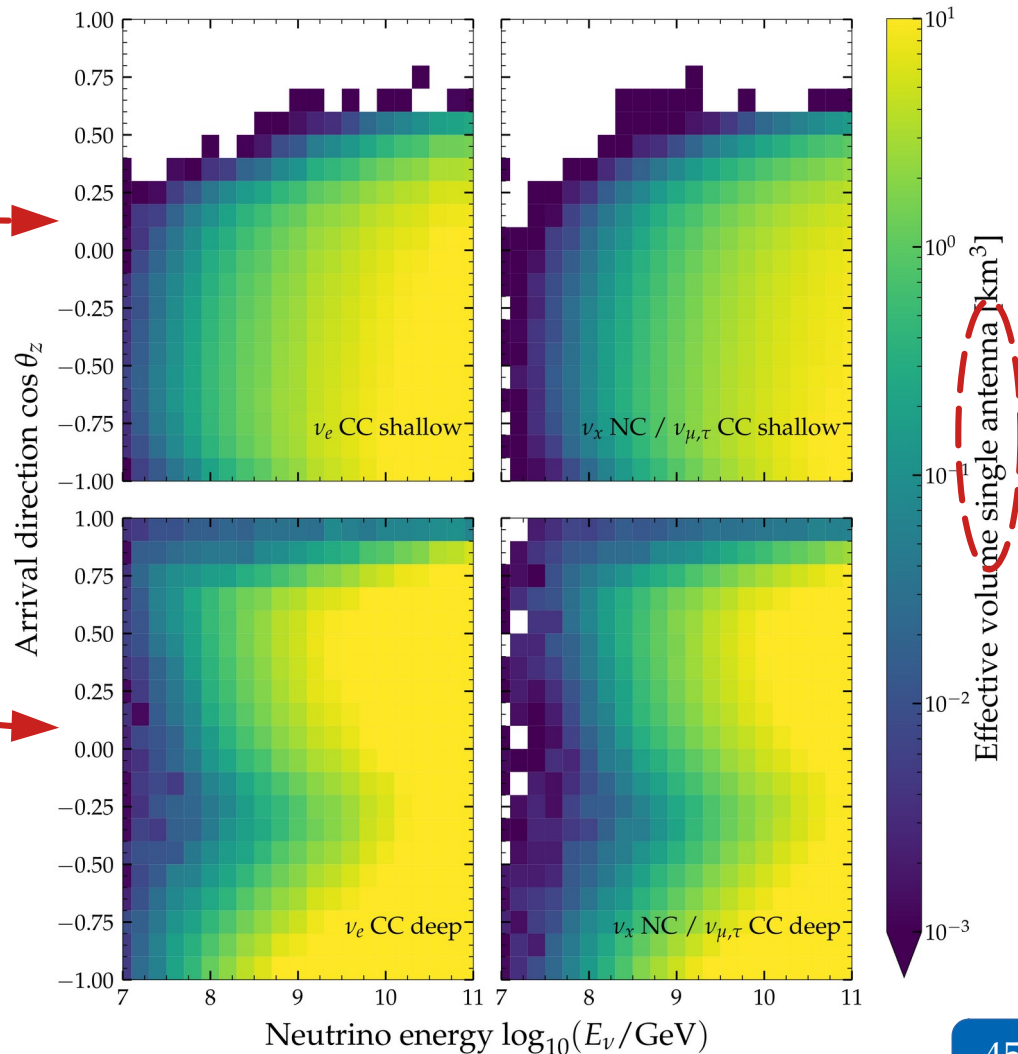
We simulate the effective volume of
with NuRadioMC & NuRadioReco

Detector effective volume

IC-Gen2 has stations containing:

- ▶ Shallow antennas
- ▶ Deep antennas

We simulate the effective volume of
with NuRadioMC & NuRadioReco



Detector effective volume

IC-Gen2 has stations containing:

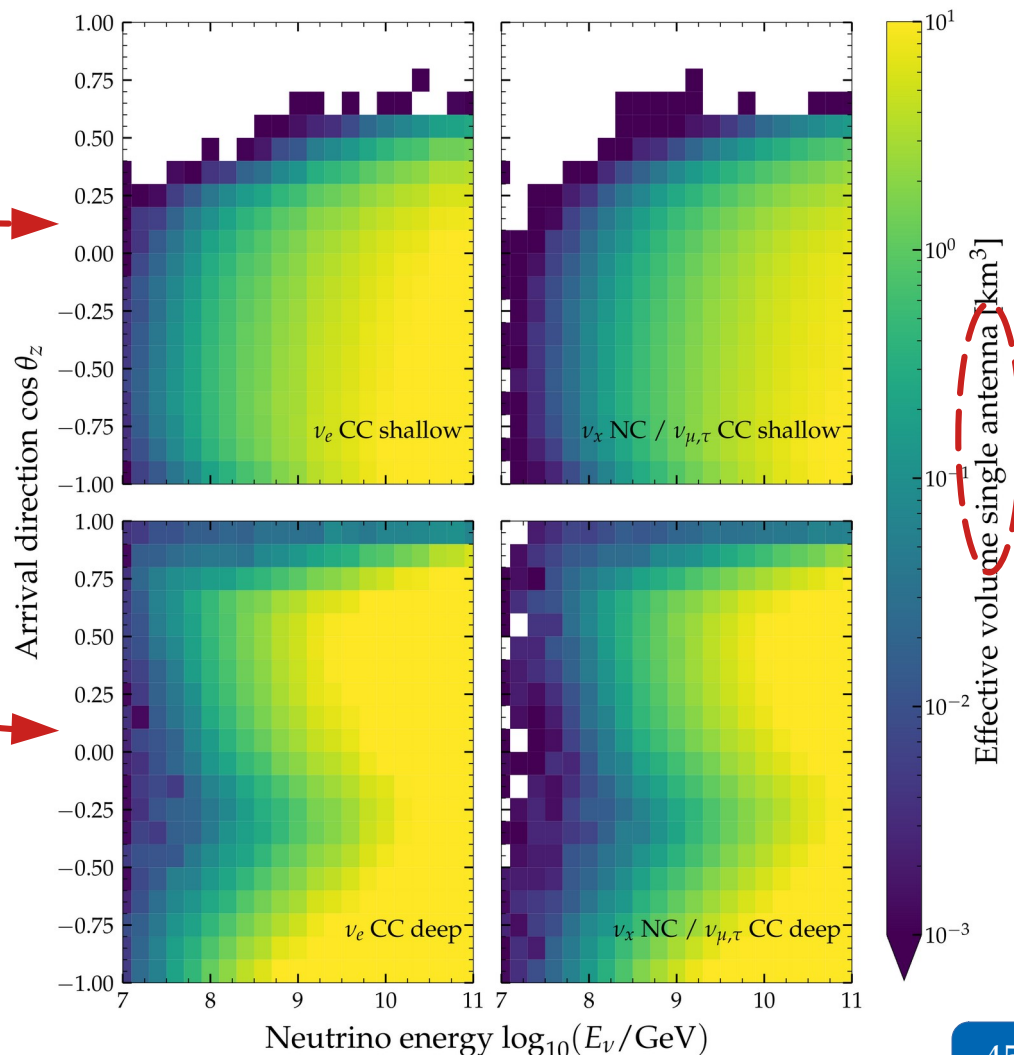
- ▶ Shallow antennas
- ▶ Deep antennas

We simulate the effective volume of
with NuRadioMC & NuRadioReco

Note: For now, we turned off the
contribution of secondary leptons

For ν_e CC: Use the CC V_{eff}

For ν_μ CC, ν_τ CC, ν_l NC: Use the NC V_{eff}



Detector effective volume

IC-Gen2 has stations containing:

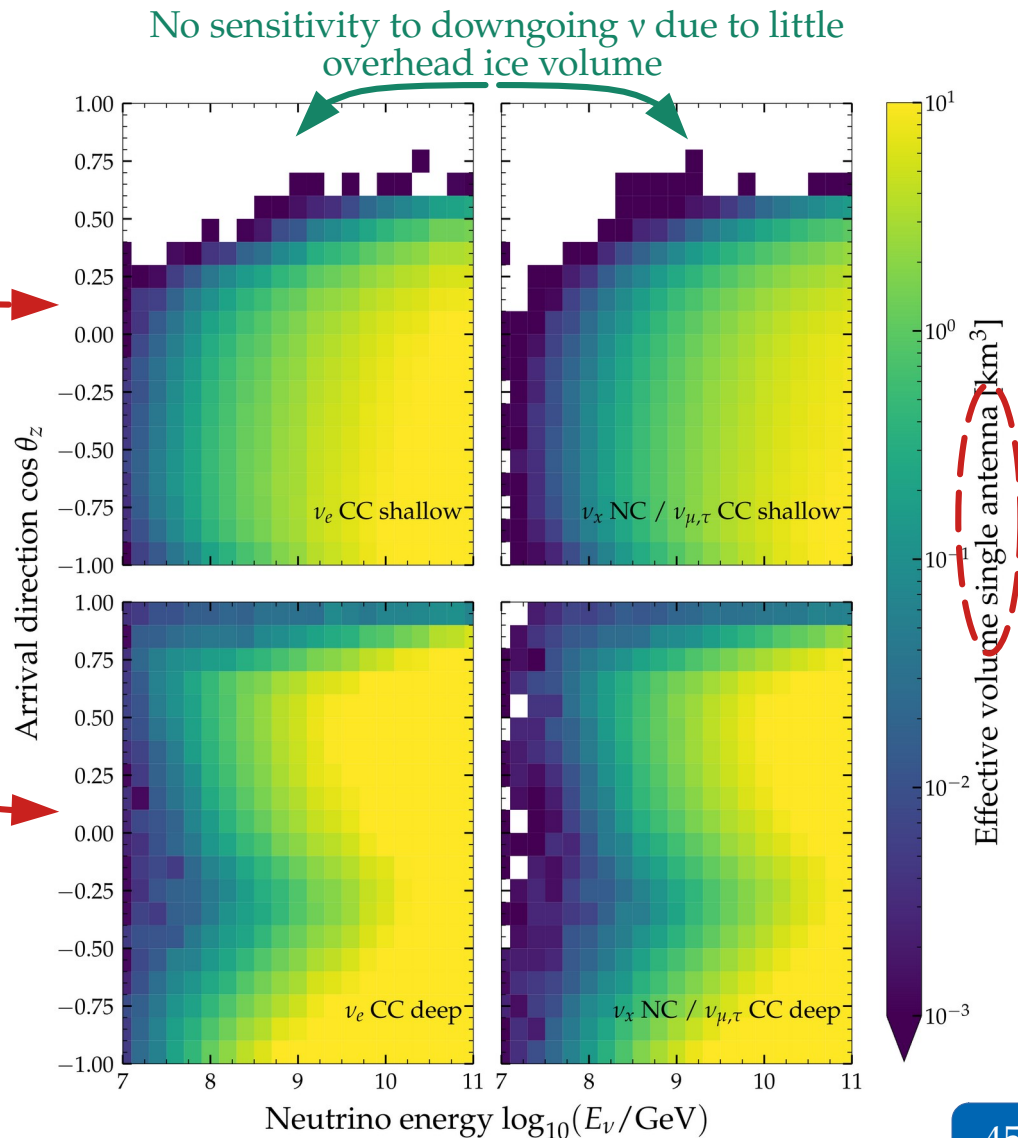
- ▶ Shallow antennas
- ▶ Deep antennas

We simulate the effective volume of
with NuRadioMC & NuRadioReco

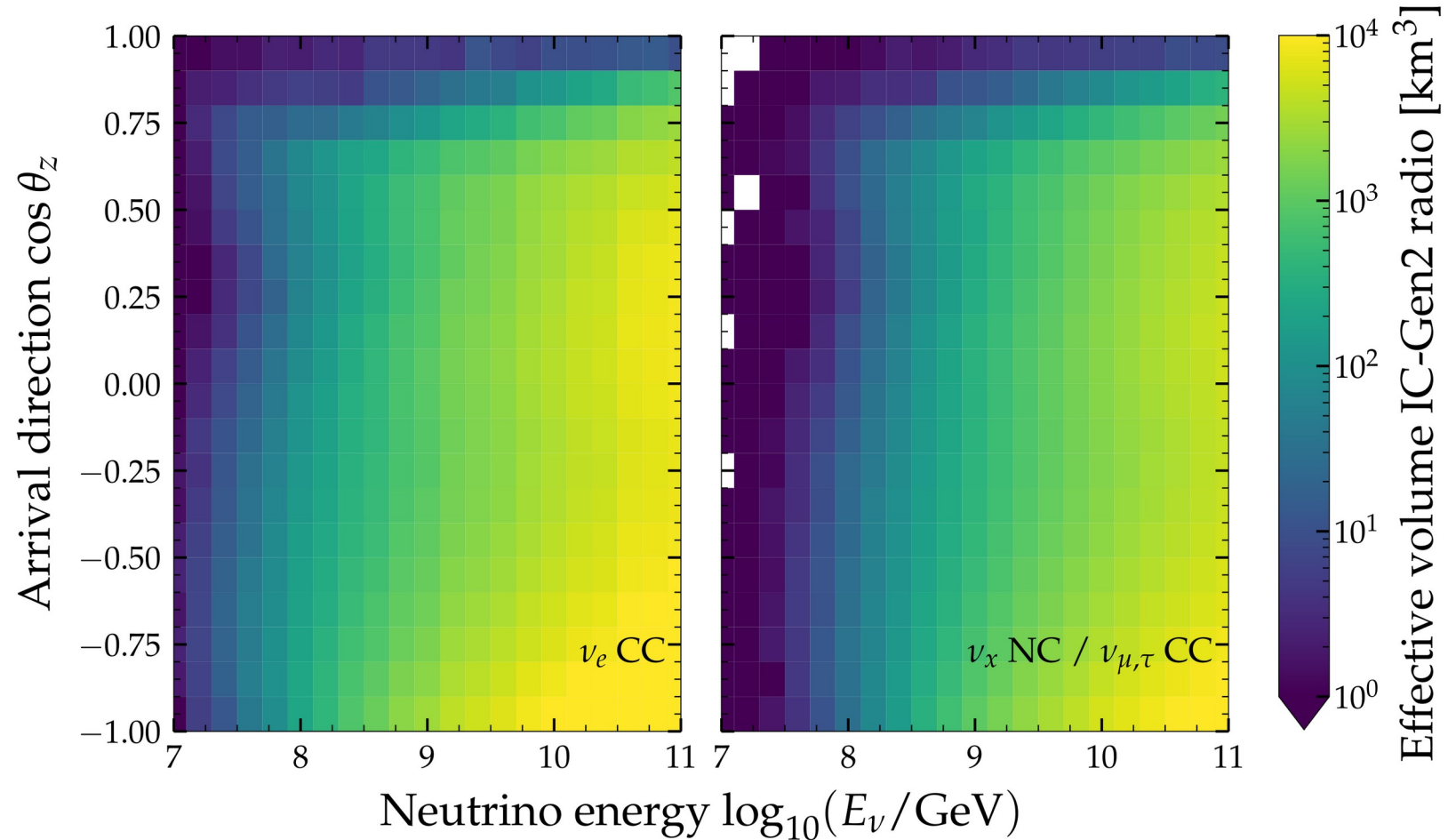
Note: For now, we turned off the
contribution of secondary leptons

For ν_e CC: Use the CC V_{eff}

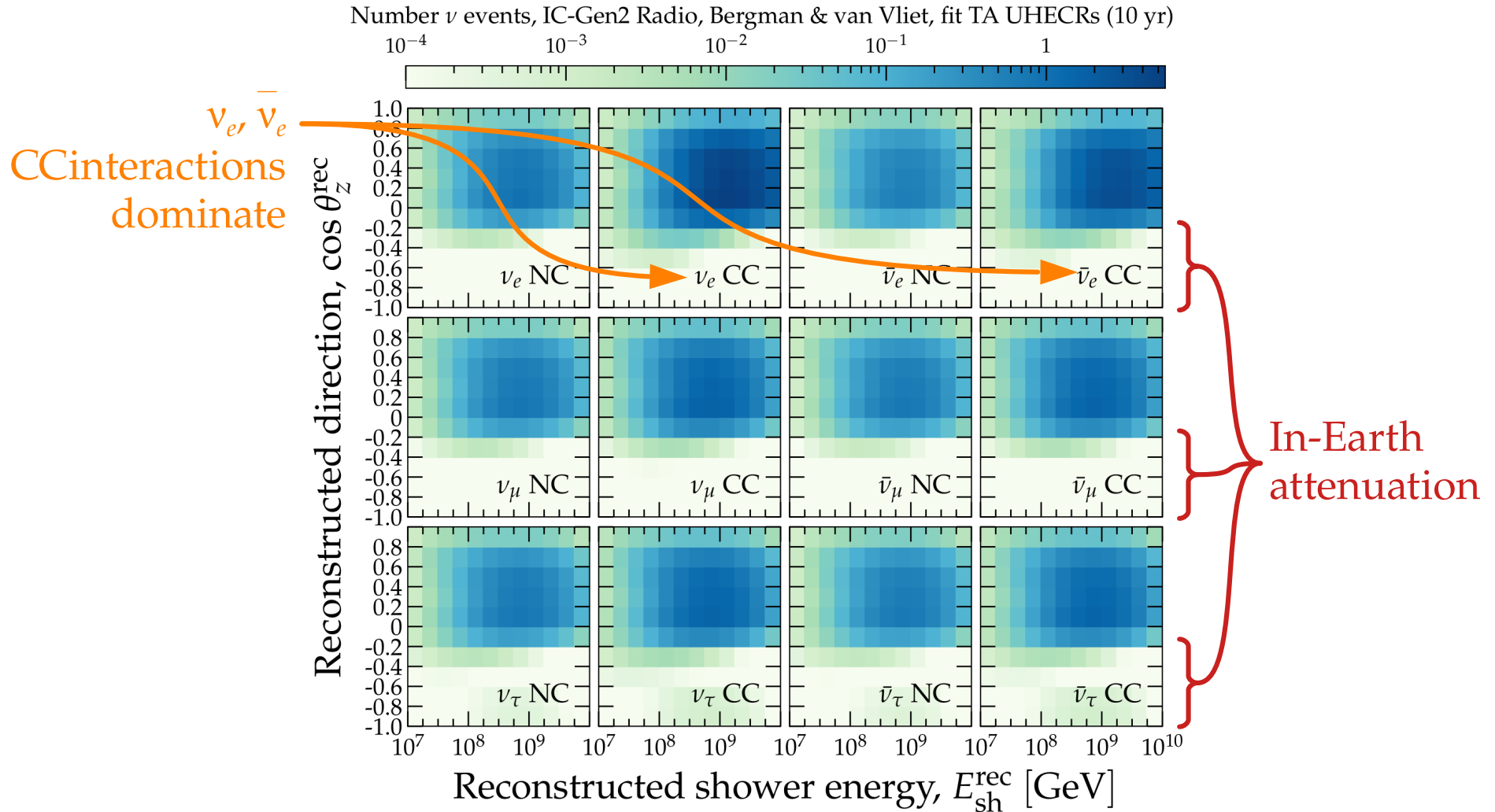
For ν_μ CC, ν_τ CC, ν_l NC: Use the NC V_{eff}

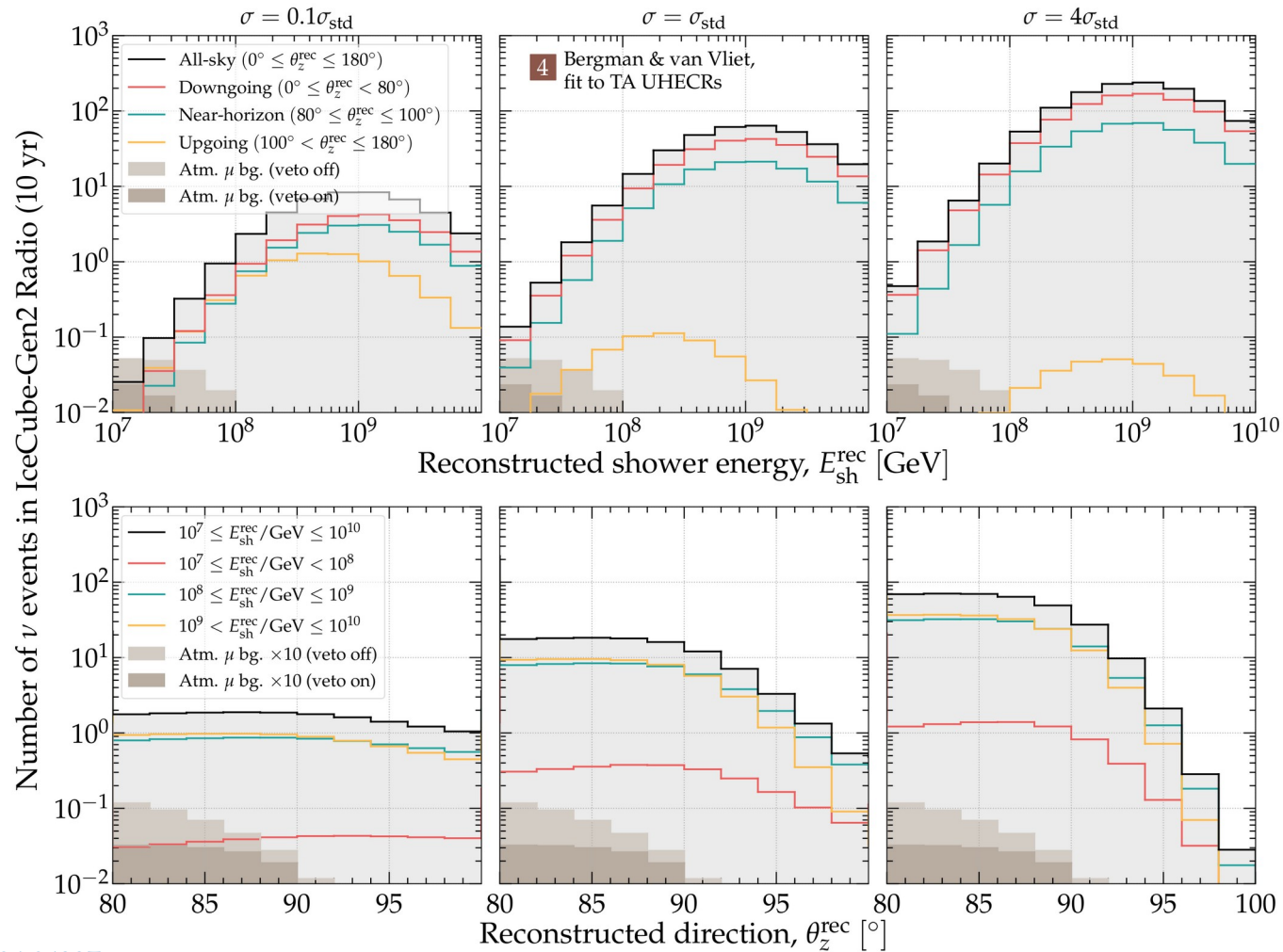


Total volume = 169 shallow-only stations + 144 hybrid (shallow+deep) stations

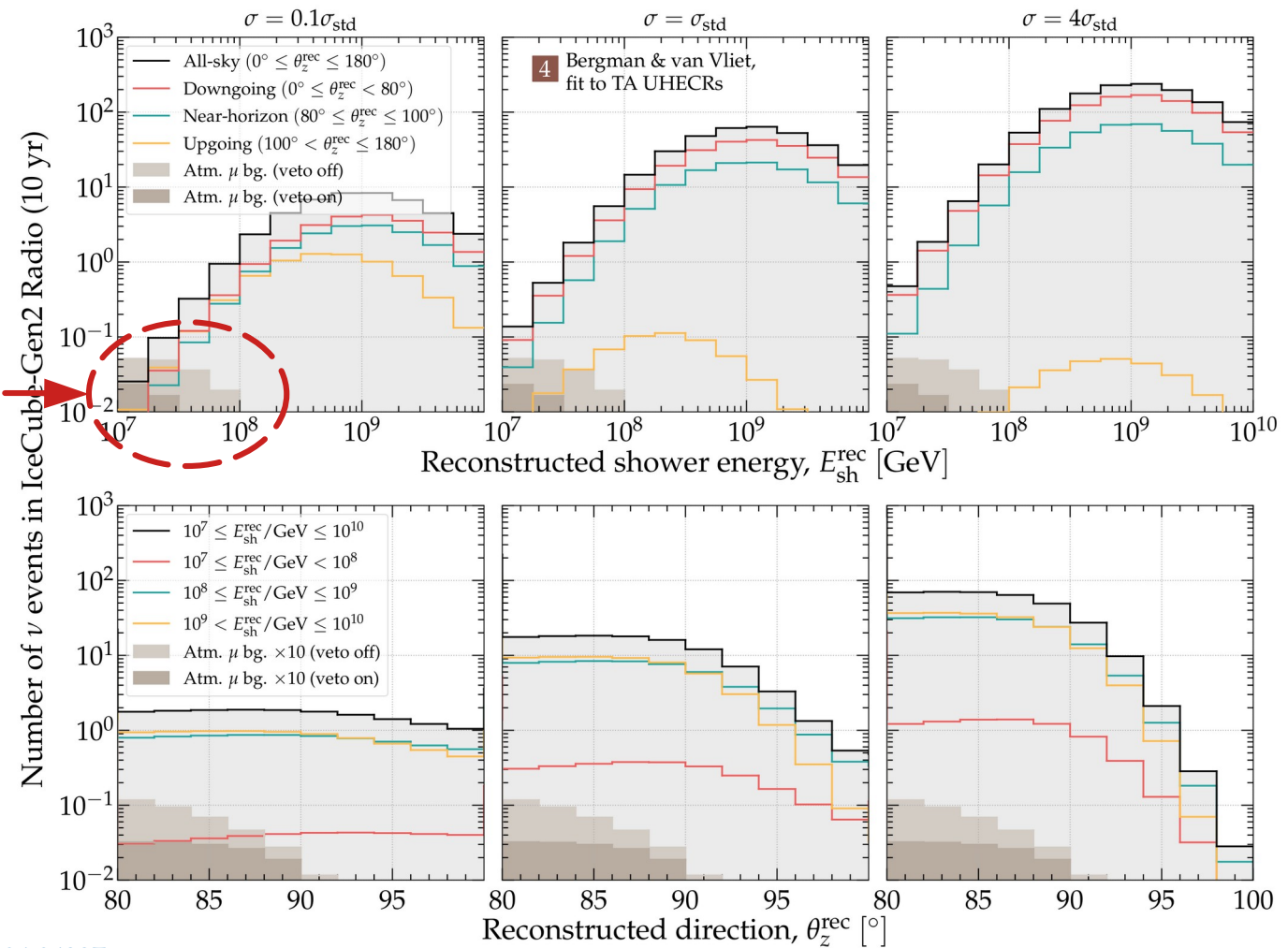


Event rates per channel

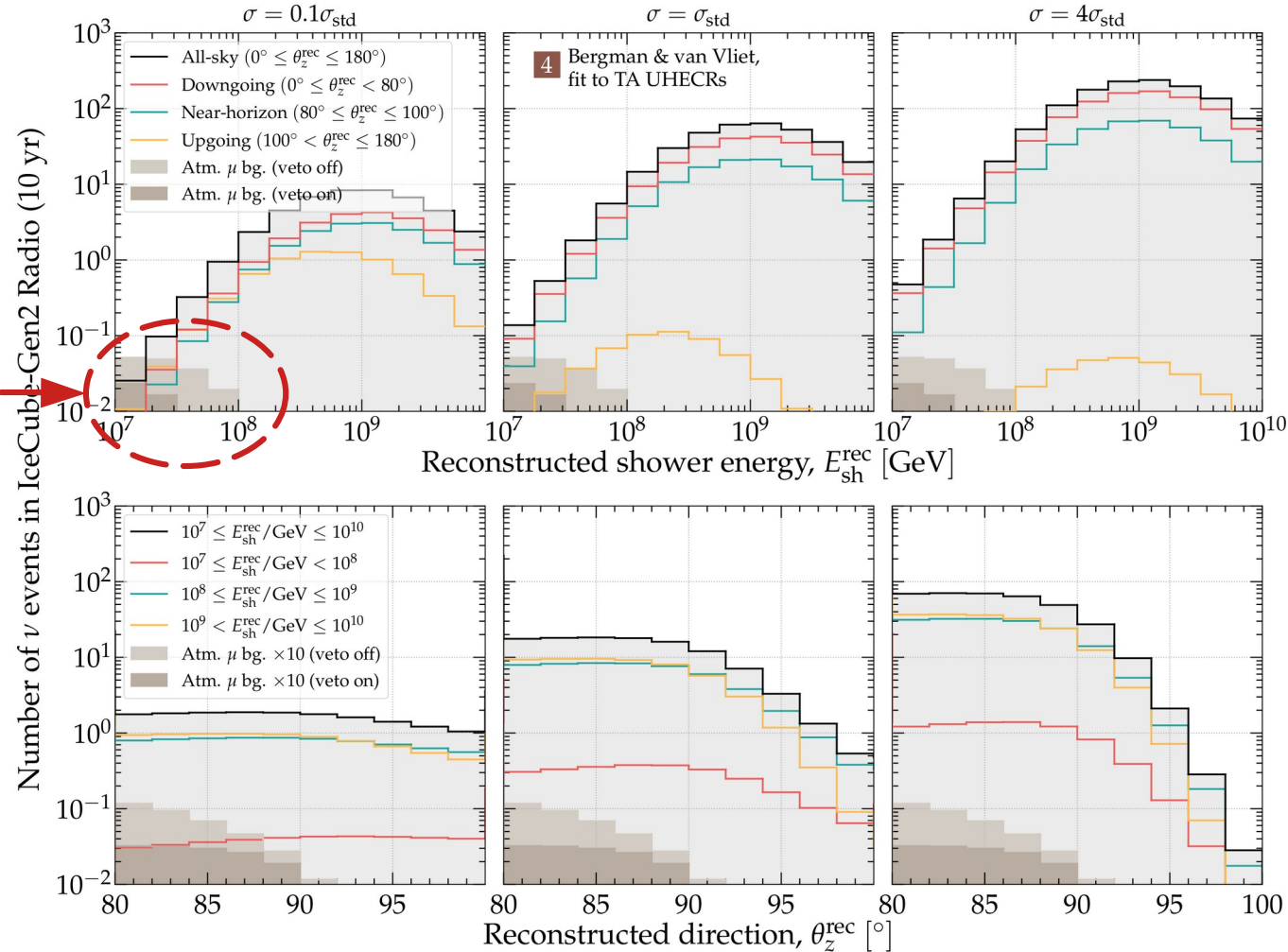




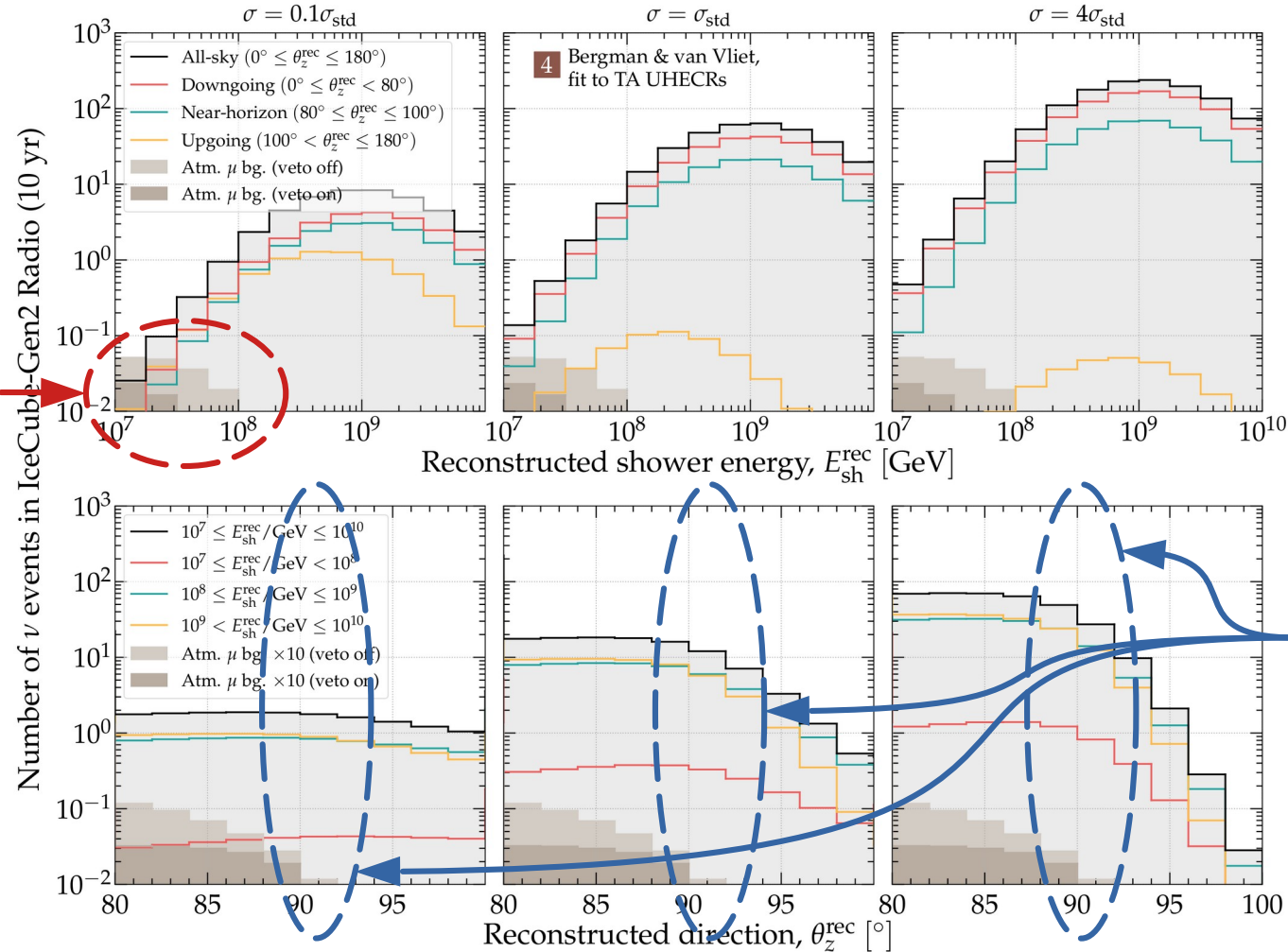
Atmospheric
muon
background



Larger neutrino-nucleon cross section



Larger neutrino-nucleon cross section



Measuring cross section *and* flux normalization

Two physical parameters:

Neutrino-nucleon cross section: $f_{\sigma} = \frac{\sigma}{\sigma_{\text{std}}}$

Neutrino flux normalization:
(Keep the spectral shape fixed for now) $f = \frac{\Phi_{\nu}(10^8 \text{ GeV})}{\Phi_{\nu,\text{std}}(10^8 \text{ GeV})}$

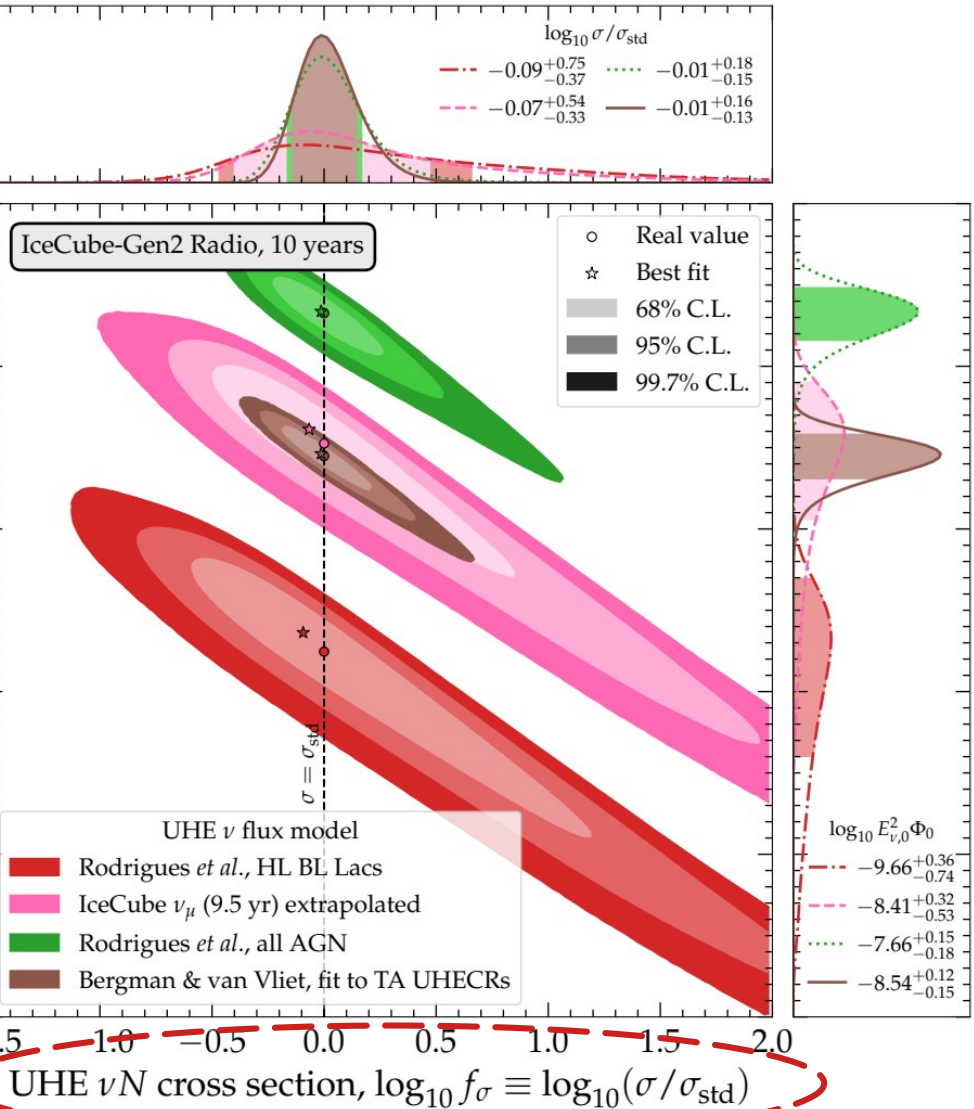
We vary and extract both simultaneously *always*,
and marginalize over each at a time

Flux normalization

Cross section

Note: We fix the spectral shape, but explore many alternatives

All-flavor ν flux (10^8 GeV), $\log_{10}(E_{\nu,0}^2 \Phi_0 / [\text{GeV cm}^{-2} \text{s}^{-1} \text{sr}^{-1}])$

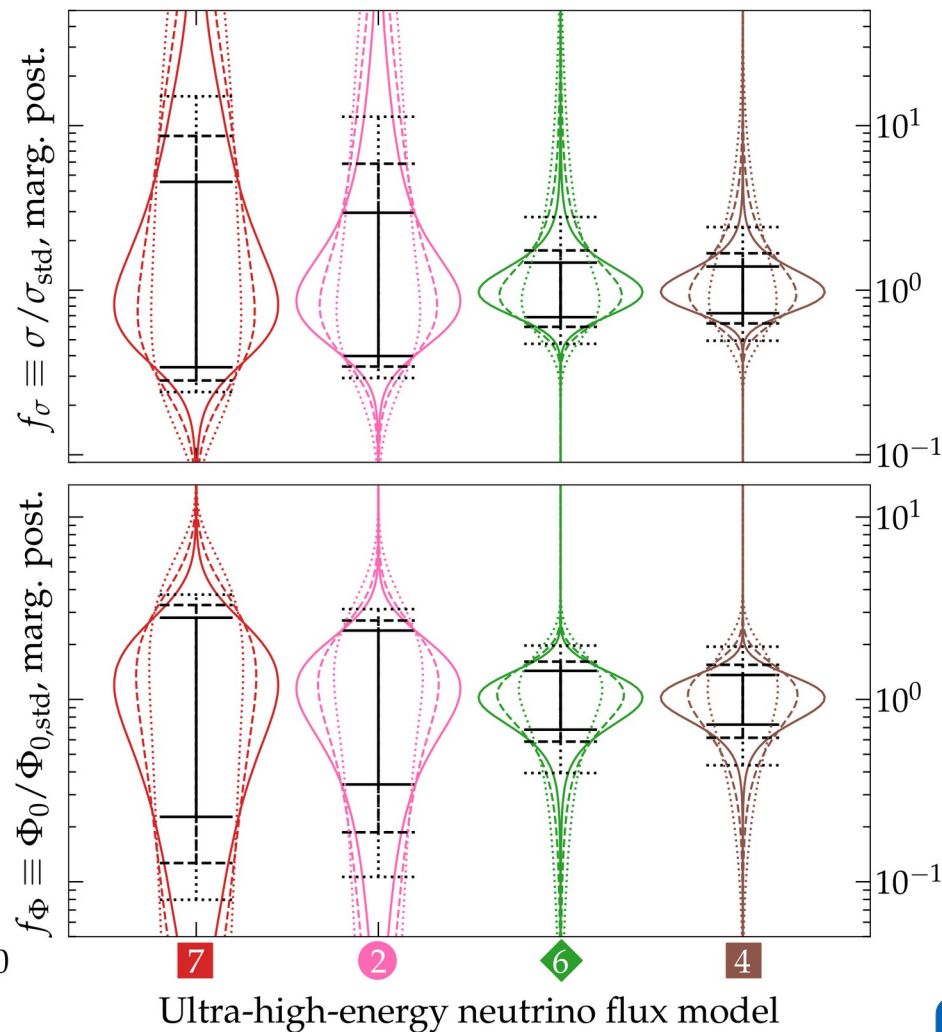
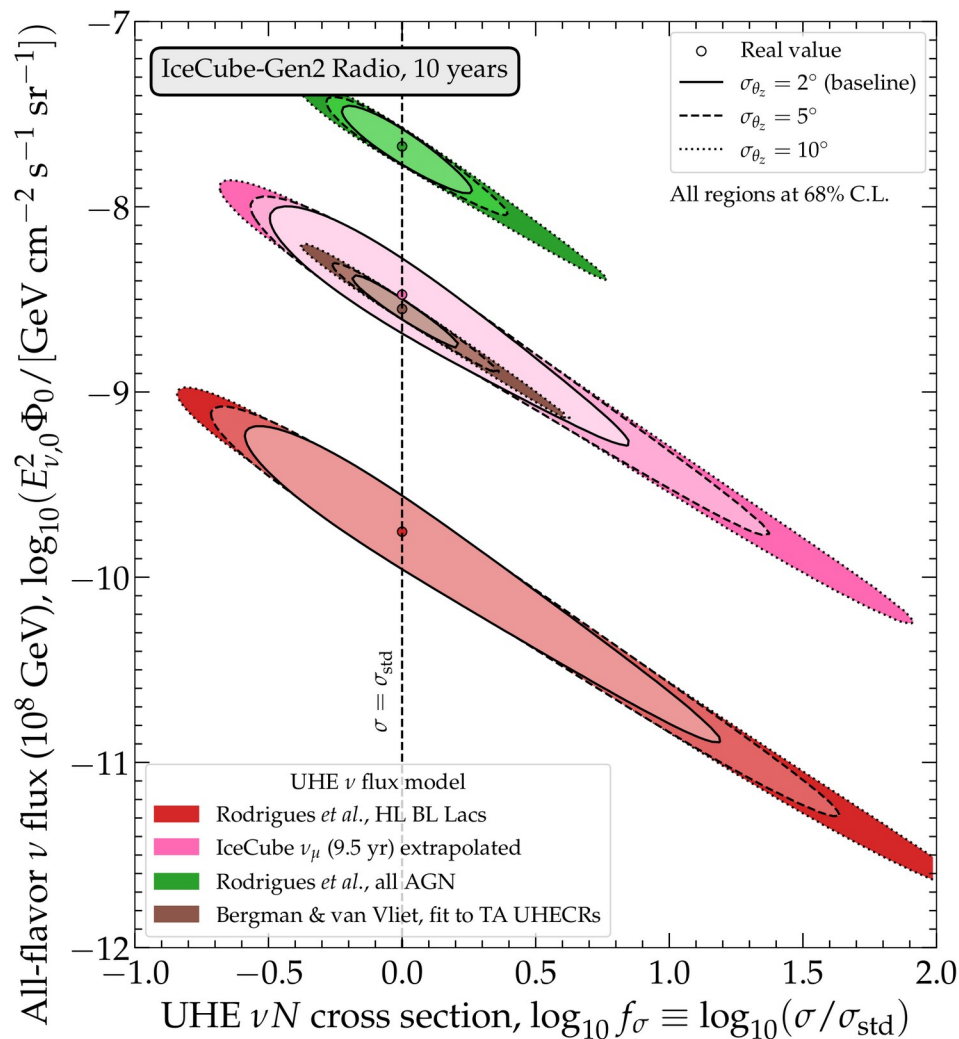


Needed to measure the cross section?

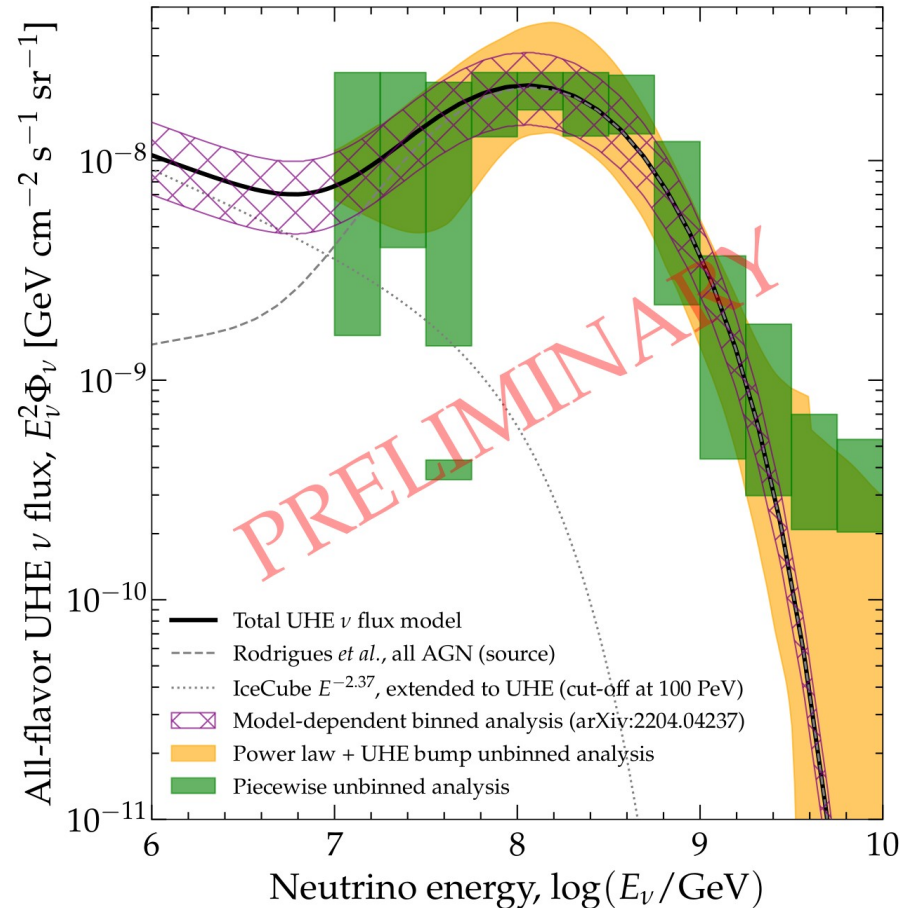
~30–300 events

Effect of angular resolution

Valera, MB, Glaser, 2204.04237



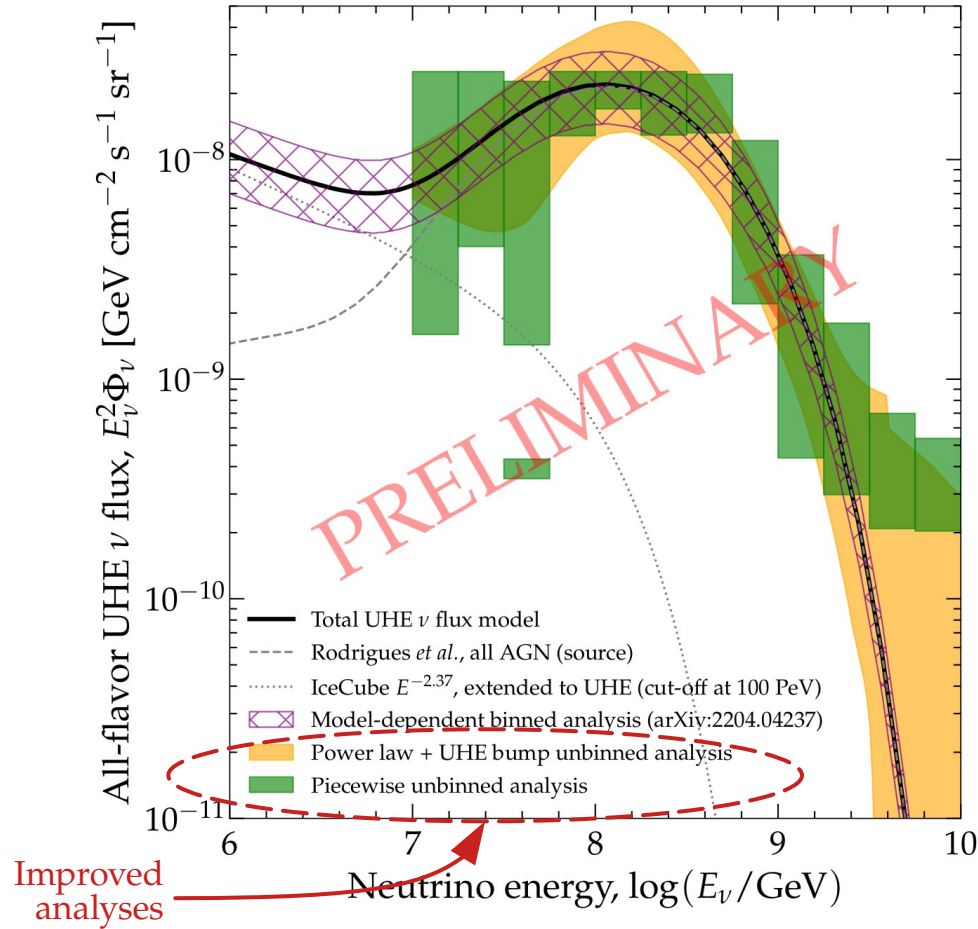
In the works: inferring the energy spectrum



Note: Preliminary results above are for a single event-rate realization

Valera, MB, In preparation

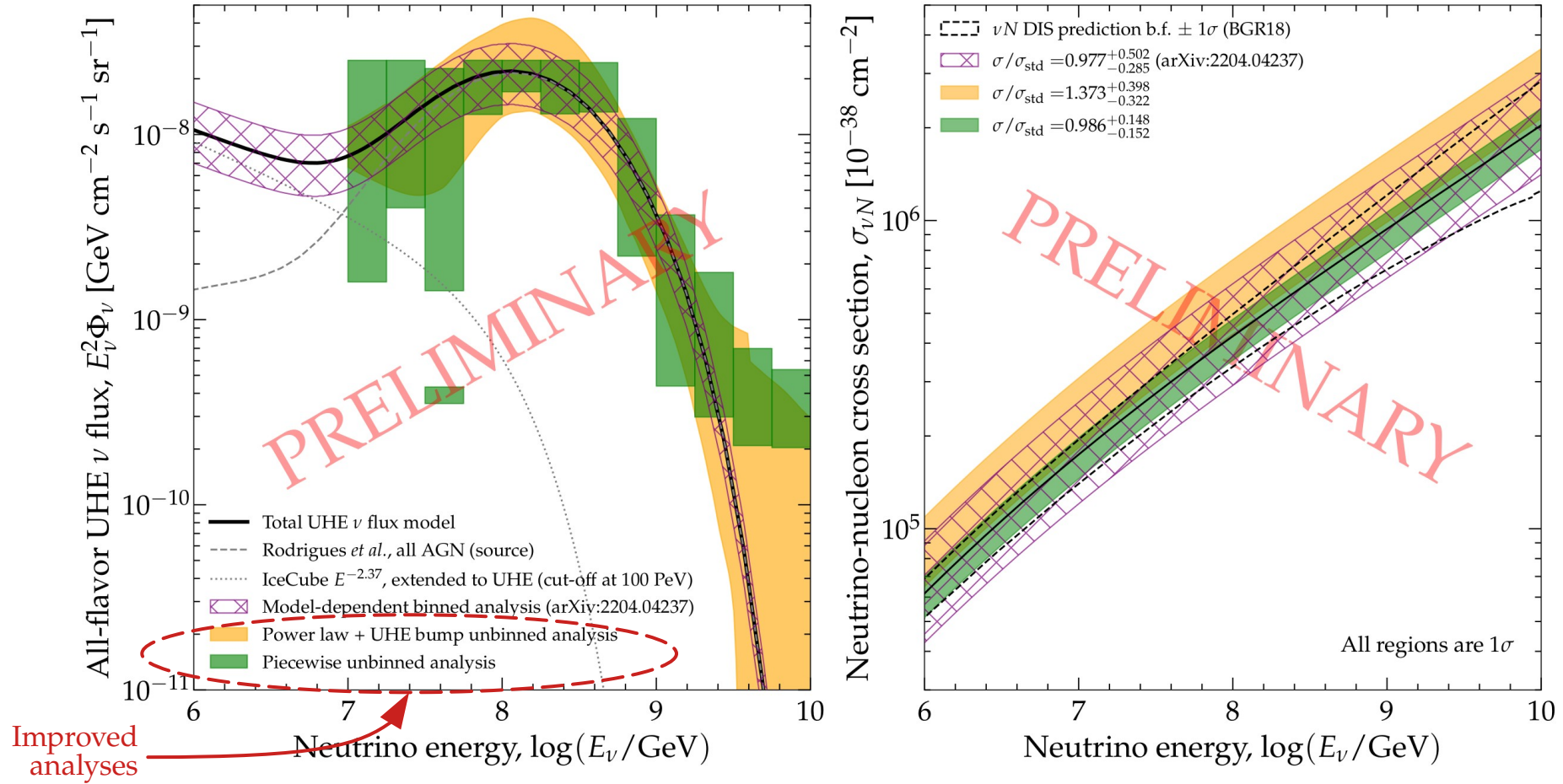
In the works: inferring the energy spectrum



Note: Preliminary results above are for a single event-rate realization

Valera, MB, In preparation

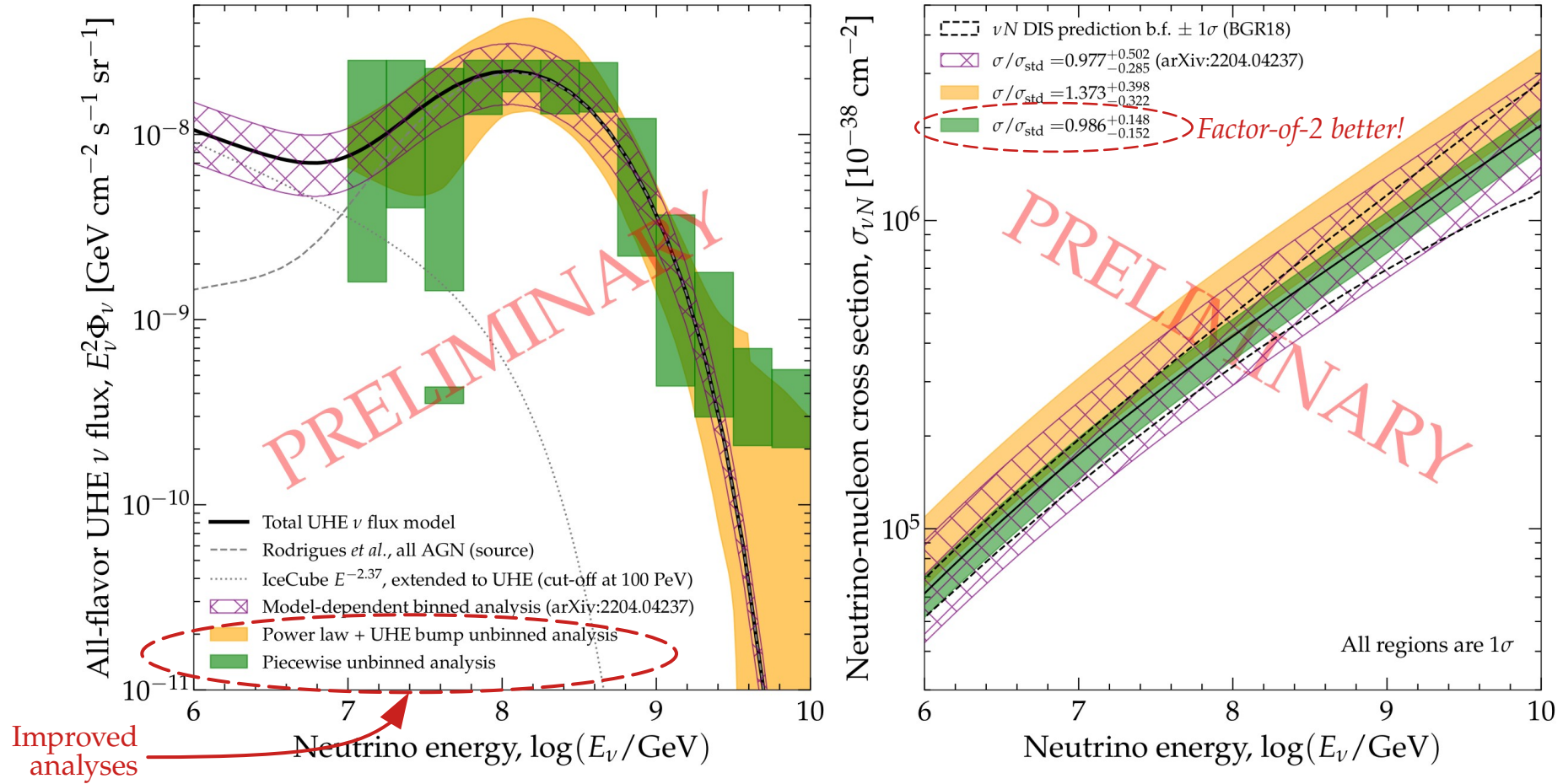
In the works: inferring the energy spectrum



Note: Preliminary results above are for a single event-rate realization

Valera, MB, In preparation

In the works: inferring the energy spectrum



Note: Preliminary results above are for a single event-rate realization

Valera, MB, In preparation

Coming attractions

Near-future improvements (see 2204.04237 for details):

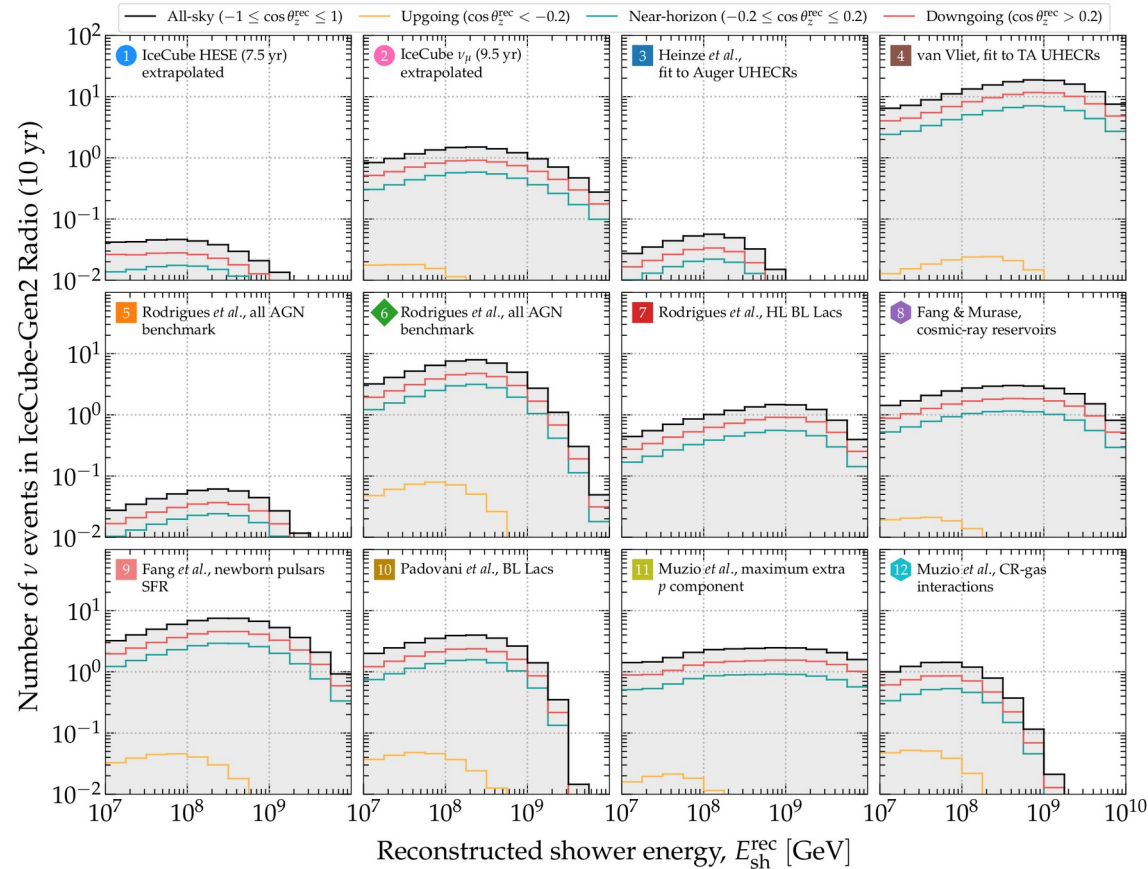
- ▶ Extract cross section, flux normalization, *and* energy spectrum shape (*ongoing*)
- ▶ Use unbinned likelihood (*ongoing*)
- ▶ Adding secondary lepton interactions to effective volume (*soon*)
- ▶ Improving effect of LPM effect in relation between neutrino and shower energy

Needs a bit more work:

- ▶ Forecast TeV–PeV cross section measurement in optical array
- ▶ Forecast UHE cross section for competing radio array designs (*ongoing*)
- ▶ **Urgent:** estimate background of reflect air-shower cores (*ongoing, not by us*)
(could be as high as 10 events per year!)

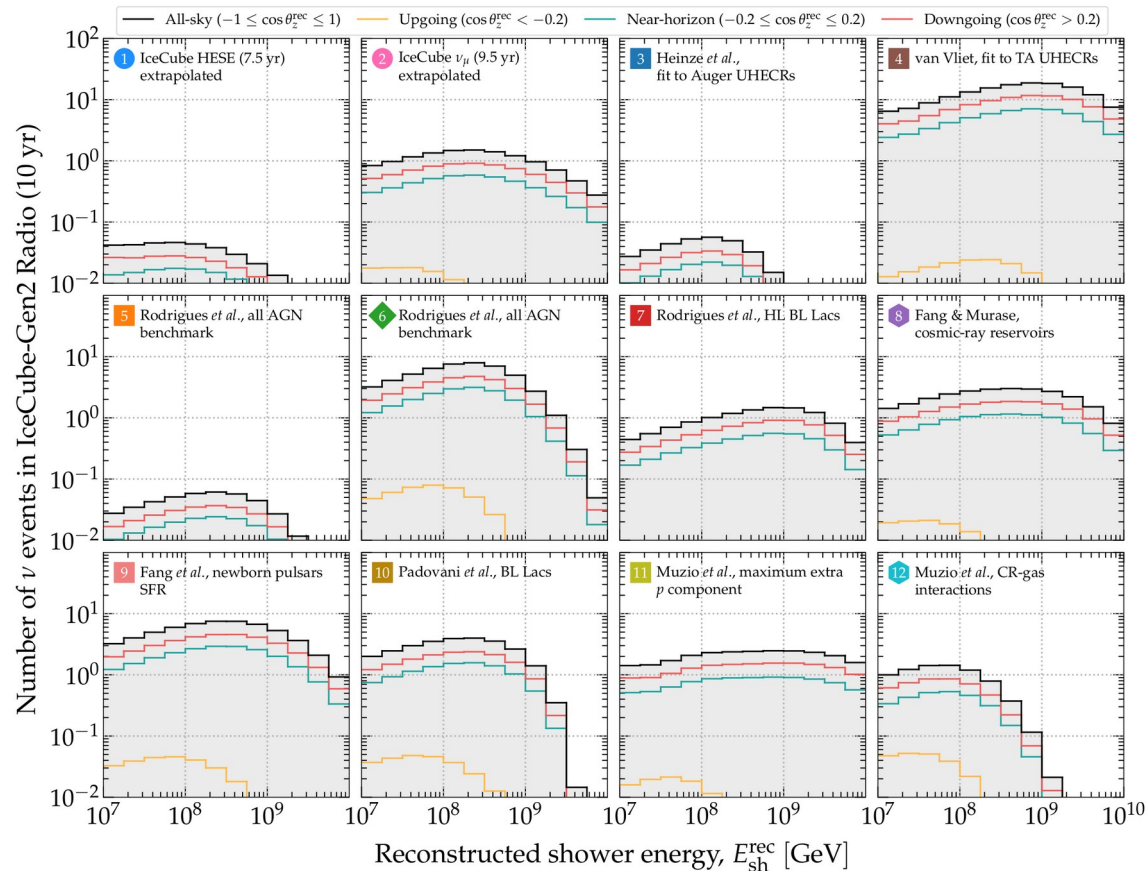
Beyond: Gen2 (radio) diffuse UHE ν flux discovery

Compute event rates for UHE ν flux predictions...

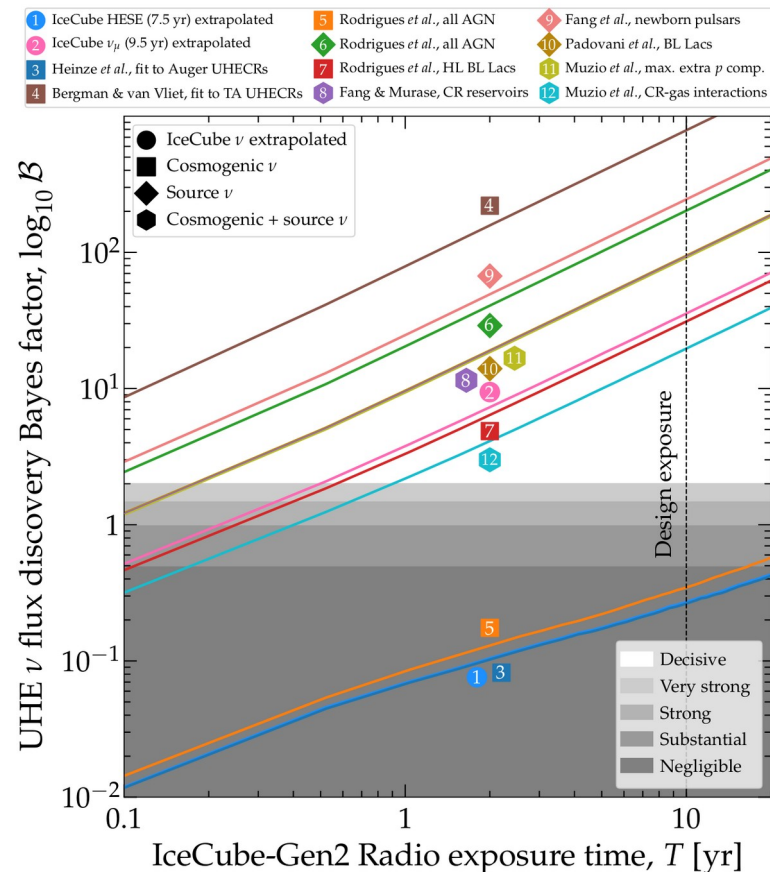


Beyond: Gen2 (radio) diffuse UHE ν flux discovery

Compute event rates for UHE ν flux predictions...



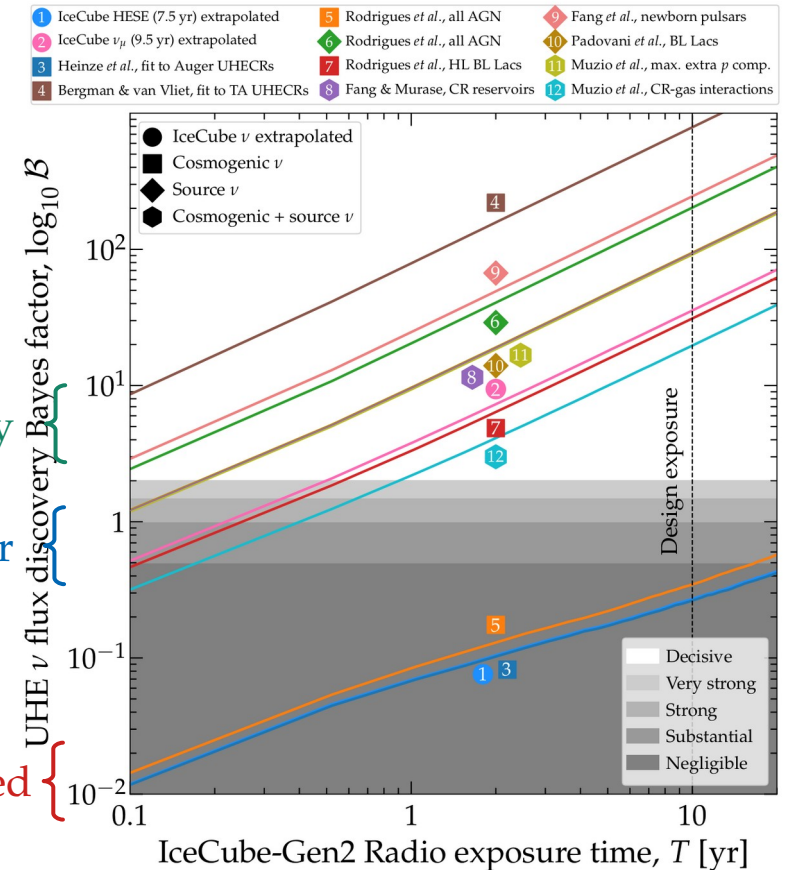
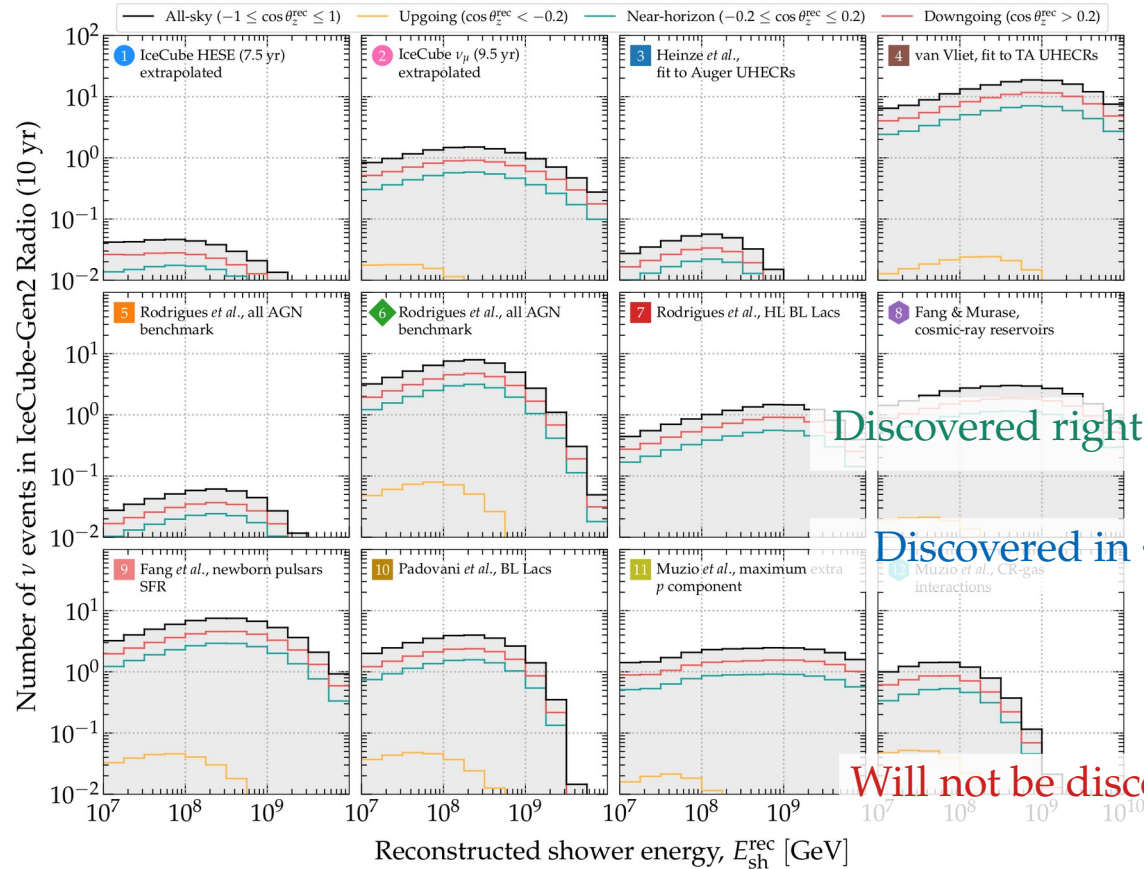
... and how long it will take to discover each



Beyond: Gen2 (radio) diffuse UHE ν flux discovery

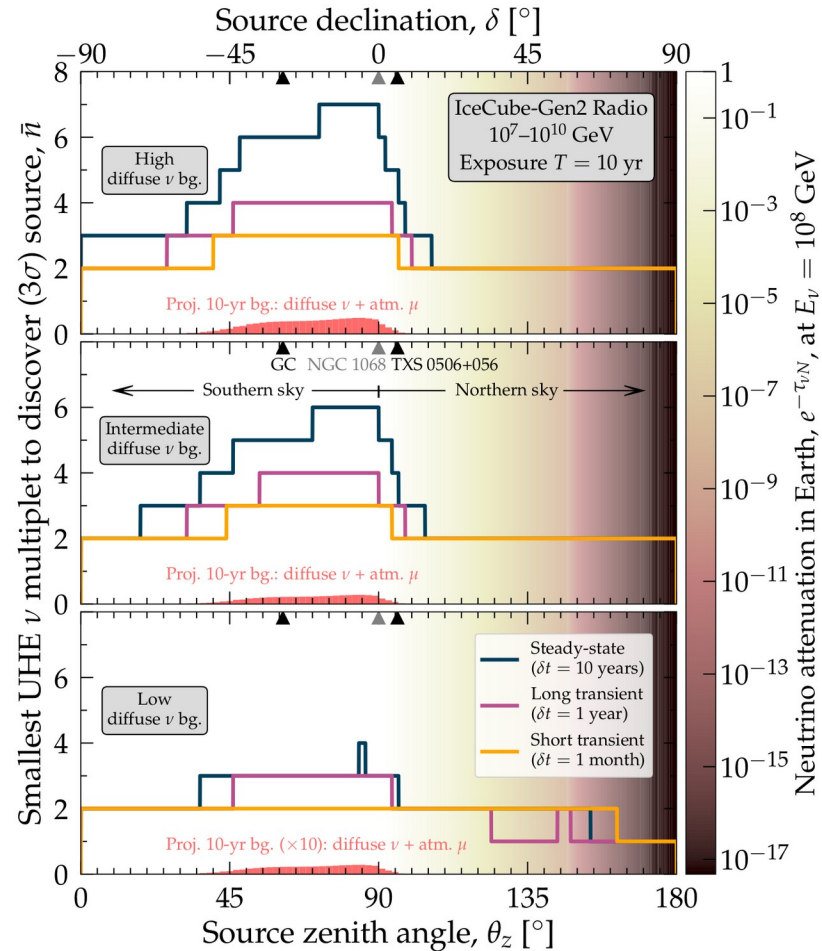
Compute event rates for UHE ν flux predictions...

... and how long it will take to discover each



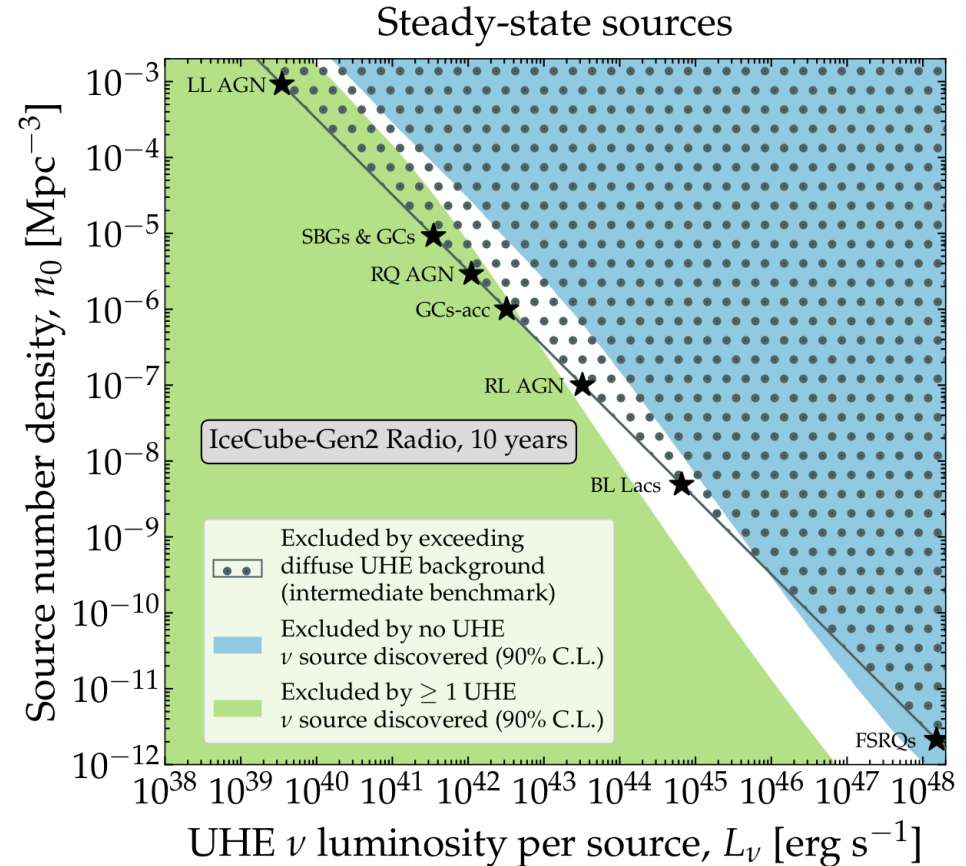
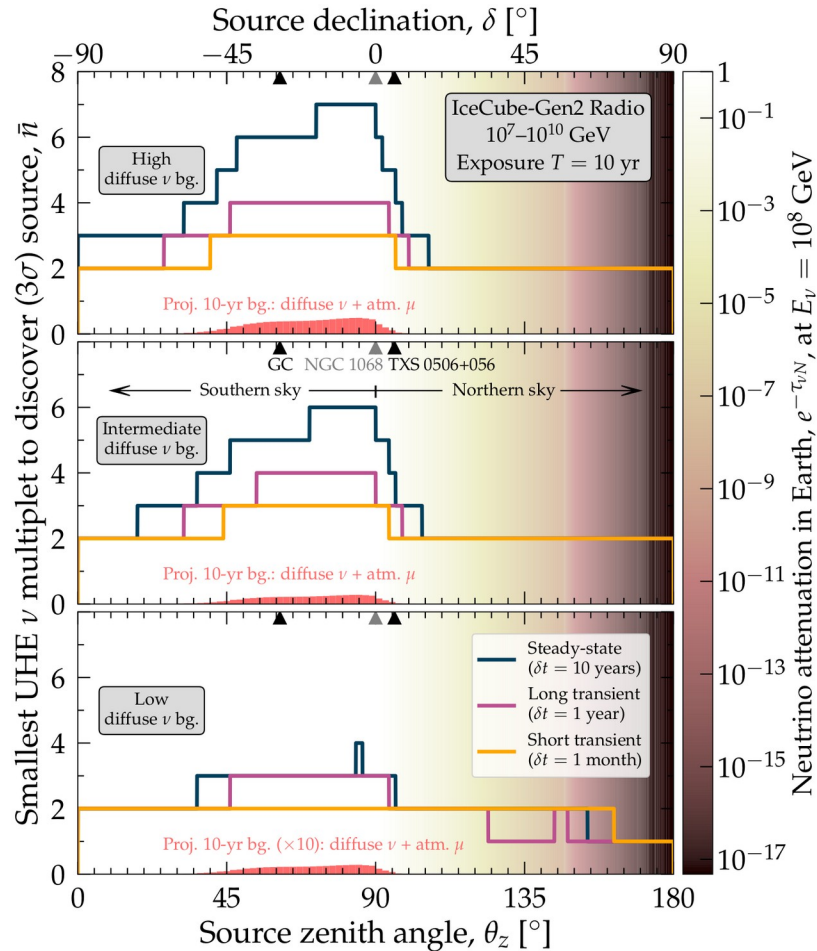
Beyond: Gen2 (radio) point-source UHE ν discovery

Find smallest UHE multiplet to claim source discovery...



Beyond: Gen2 (radio) point-source UHE ν discovery

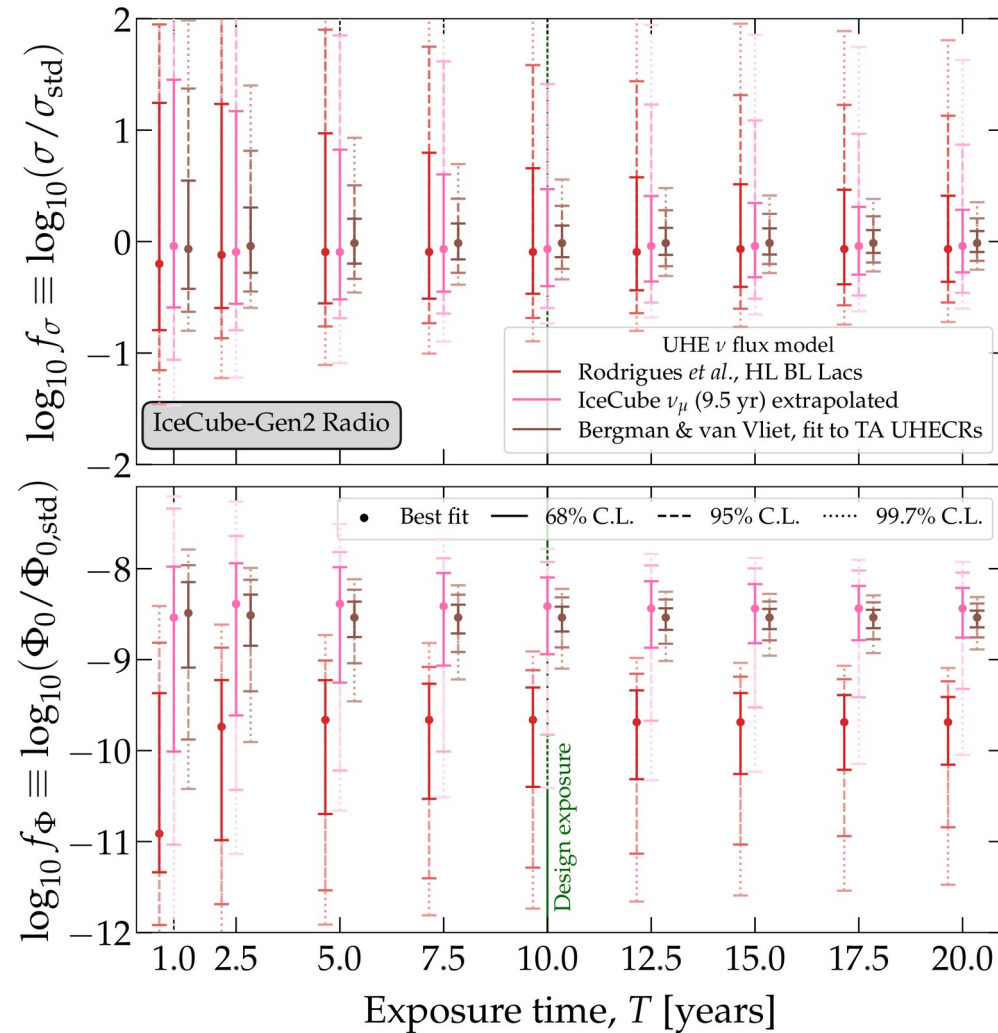
Find smallest UHE multiplet to claim source discovery... and what discovery says of the source population



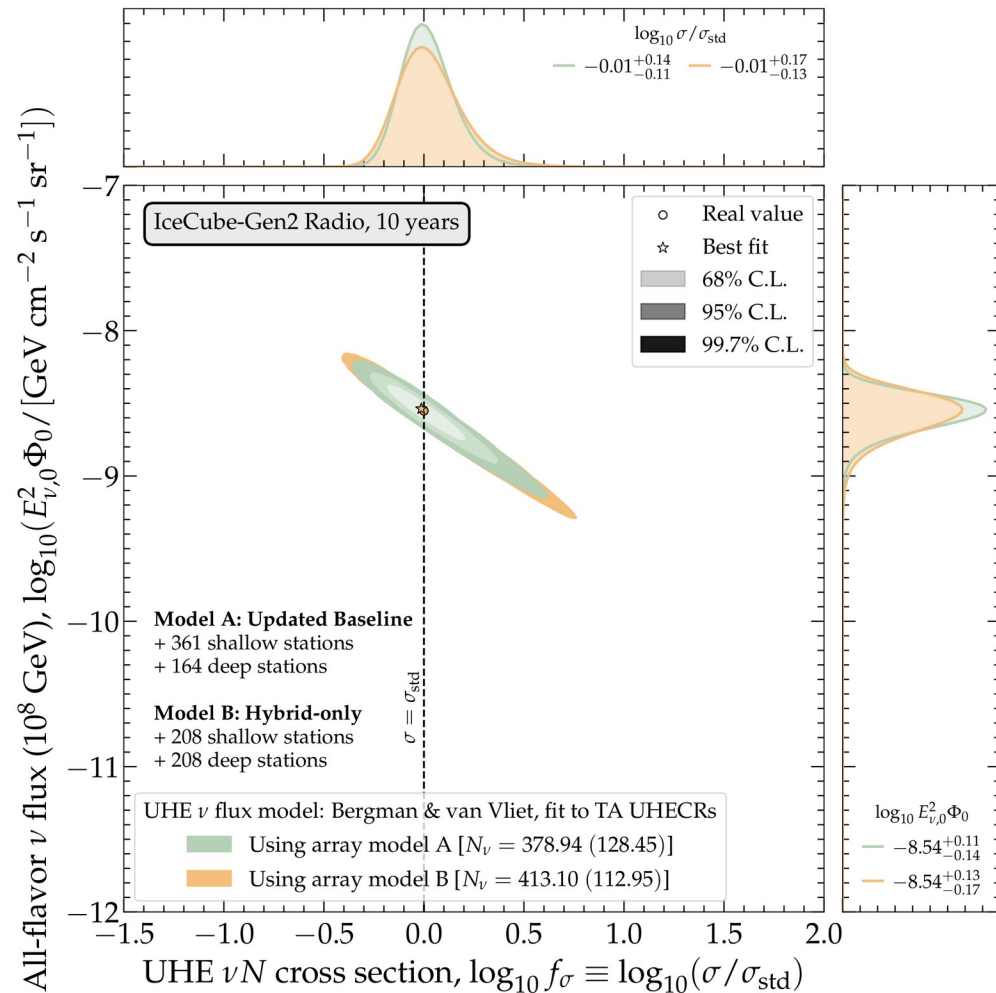
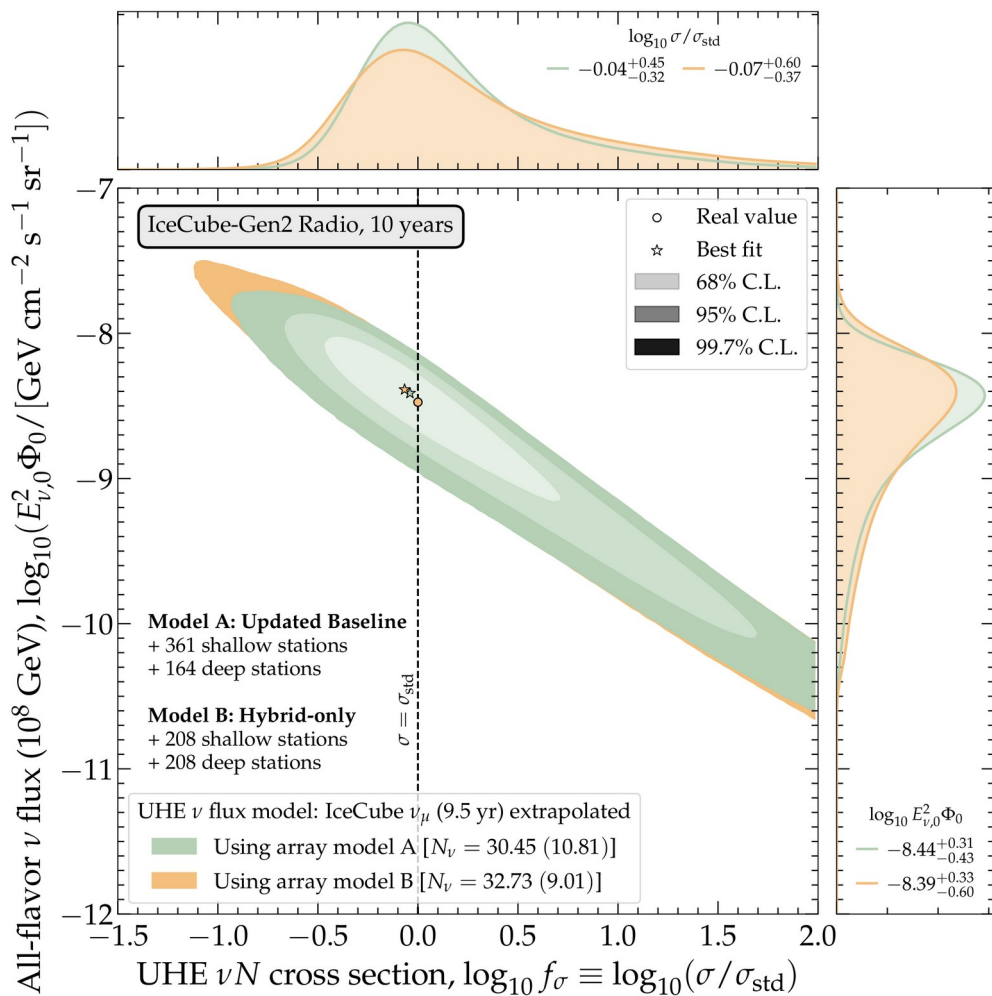
Thanks!

Backup slides

Precision *vs.* exposure time



Results for alternative radio array designs



Fundamental physics with high-energy cosmic neutrinos

- ▶ Numerous new ν physics effects grow as $\sim \kappa_n \cdot E^n \cdot L$
- ▶ So we can probe $\kappa_n \sim 4 \cdot 10^{-47} (E/\text{PeV})^{-n} (L/\text{Gpc})^{-1} \text{PeV}^{1-n}$
- ▶ Improvement over limits using atmospheric ν : $\kappa_0 < 10^{-29} \text{PeV}$, $\kappa_1 < 10^{-33}$
- ▶ Fundamental physics can be extracted from four neutrino observables:
 - ▶ Spectral shape
 - ▶ Angular distribution
 - ▶ Flavor composition
 - ▶ Timing

Fundamental physics with high-energy cosmic neutrinos

- ▶ Numerous new ν physics effects grow as $\sim \kappa_n \cdot E^n \cdot L$ $\left. \vphantom{\begin{matrix} \kappa_n \\ E^n \\ L \end{matrix}} \right\} \begin{array}{l} \text{E.g.,} \\ n = -1: \text{neutrino decay} \\ n = 0: \text{CPT-odd Lorentz violation} \\ n = +1: \text{CPT-even Lorentz violation} \end{array}$
- ▶ So we can probe $\kappa_n \sim 4 \cdot 10^{-47} (E/\text{PeV})^{-n} (L/\text{Gpc})^{-1} \text{PeV}^{1-n}$
- ▶ Improvement over limits using atmospheric ν : $\kappa_0 < 10^{-29} \text{PeV}$, $\kappa_1 < 10^{-33}$
- ▶ Fundamental physics can be extracted from four neutrino observables:
 - ▶ Spectral shape
 - ▶ Angular distribution
 - ▶ Flavor composition
 - ▶ Timing

Fundamental physics with high-energy cosmic neutrinos

- ▶ Numerous new ν physics effects grow as $\sim \kappa_n \cdot E^n \cdot L$ $\left. \vphantom{\begin{matrix} \kappa_n \\ E^n \\ L \end{matrix}} \right\} \begin{array}{l} \text{E.g.,} \\ n = -1: \text{neutrino decay} \\ n = 0: \text{CPT-odd Lorentz violation} \\ n = +1: \text{CPT-even Lorentz violation} \end{array}$
- ▶ So we can probe $\kappa_n \sim 4 \cdot 10^{-47} (E/\text{PeV})^{-n} (L/\text{Gpc})^{-1} \text{PeV}^{1-n}$
- ▶ Improvement over limits using atmospheric ν : $\kappa_0 < 10^{-29} \text{PeV}$, $\kappa_1 < 10^{-33}$
- ▶ Fundamental physics can be extracted from four neutrino observables:
 - ▶ Spectral shape
 - ▶ Angular distribution
 - ▶ Flavor composition
 - ▶ Timing $\left. \vphantom{\begin{matrix} \text{Spectral shape} \\ \text{Angular distribution} \\ \text{Flavor composition} \\ \text{Timing} \end{matrix}} \right\} \begin{array}{l} \text{In spite of} \\ \text{poor energy, angular, flavor reconstruction} \\ \text{\& astrophysical unknowns} \end{array}$

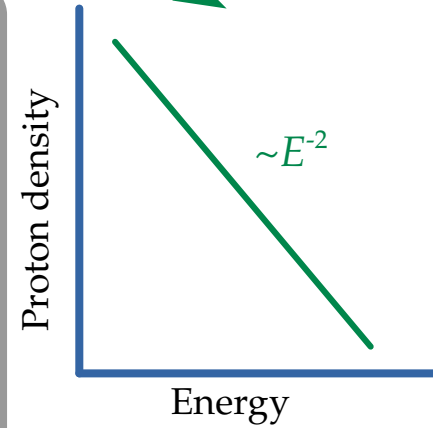
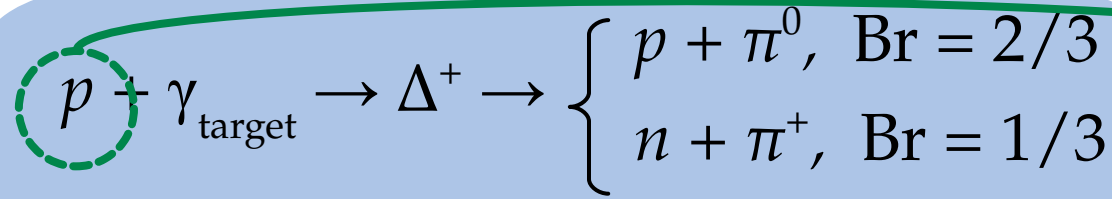
Making high-energy astrophysical neutrinos

(or $p + p$)

$$p + \gamma_{\text{target}} \rightarrow \Delta^+ \rightarrow \begin{cases} p + \pi^0, & \text{Br} = 2/3 \\ n + \pi^+, & \text{Br} = 1/3 \end{cases}$$

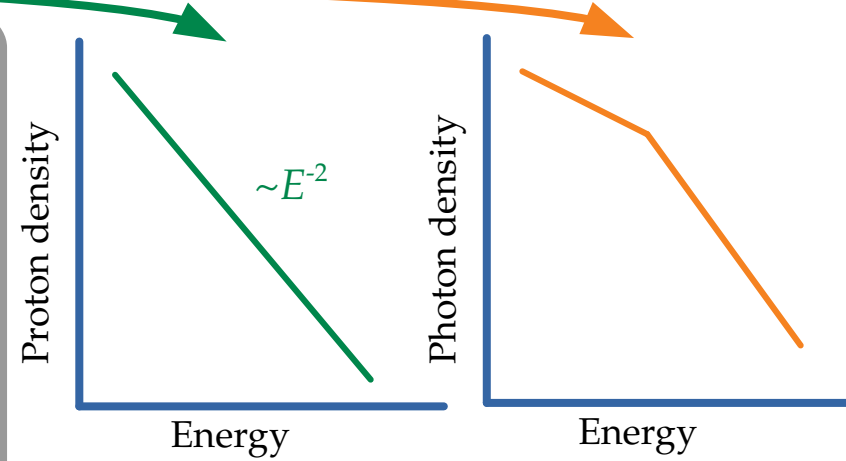
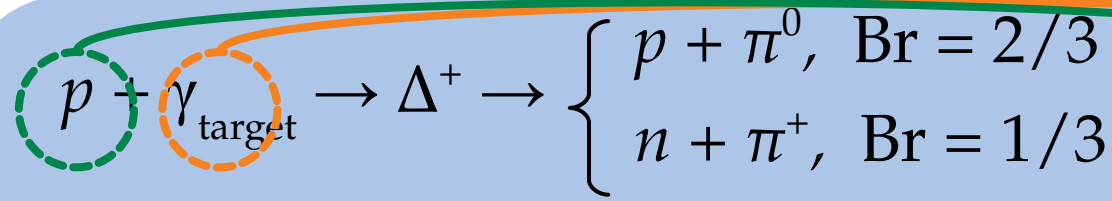
Making high-energy astrophysical neutrinos

(or $p + p$)



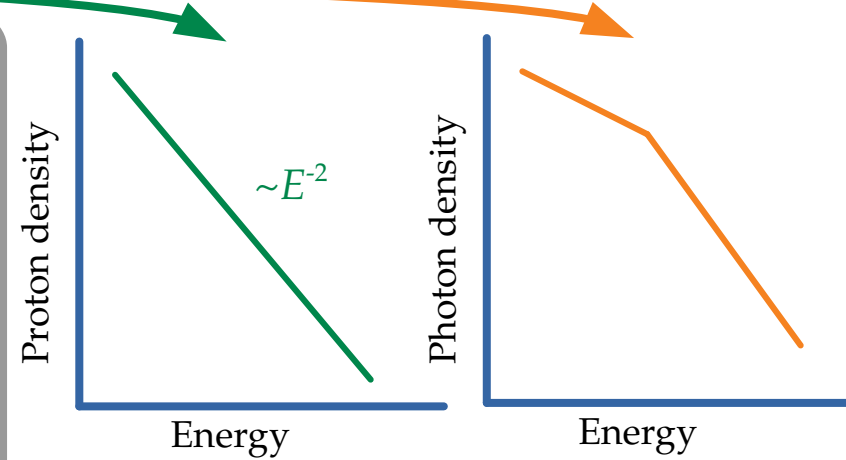
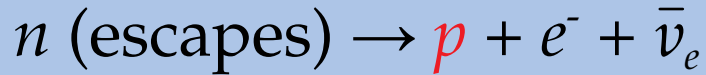
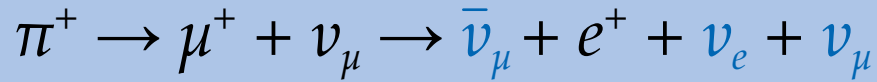
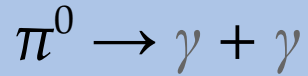
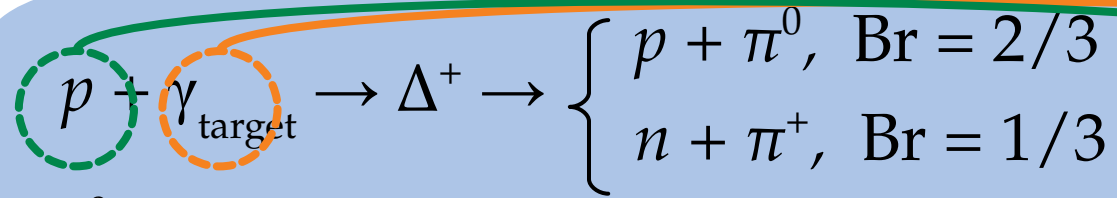
Making high-energy astrophysical neutrinos

(or $p + p$)



Making high-energy astrophysical neutrinos

(or $p + p$)



Making high-energy astrophysical neutrinos

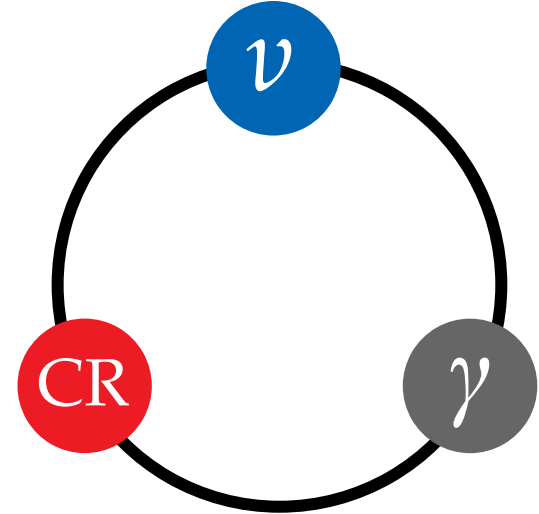
(or $p + p$)

$$p + \gamma_{\text{target}} \rightarrow \Delta^+ \rightarrow \begin{cases} p + \pi^0, & \text{Br} = 2/3 \\ n + \pi^+, & \text{Br} = 1/3 \end{cases}$$

$$\pi^0 \rightarrow \gamma + \gamma$$

$$\pi^+ \rightarrow \mu^+ + \nu_\mu \rightarrow \bar{\nu}_\mu + e^+ + \nu_e + \nu_\mu$$

$$n \text{ (escapes)} \rightarrow \textcolor{red}{p} + e^- + \bar{\nu}_e$$



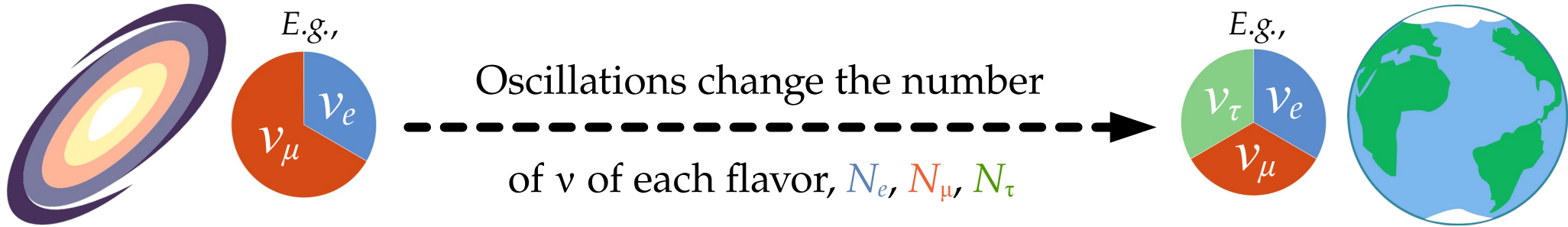
Neutrino energy = Proton energy / 20

Gamma-ray energy = Proton energy / 10

Astrophysical sources

Earth

Up to a few Gpc



Different production mechanisms yield different flavor ratios:

$$(f_{e,S}, f_{\mu,S}, f_{\tau,S}) \equiv (N_{e,S}, N_{\mu,S}, N_{\tau,S}) / N_{\text{tot}}$$

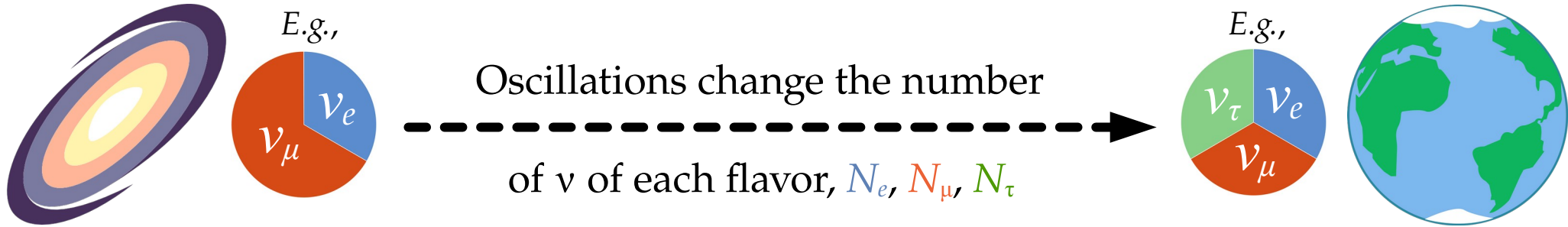
Flavor ratios at Earth ($\alpha = e, \mu, \tau$):

$$f_{\alpha,\oplus} = \sum_{\beta=e,\mu,\tau} P_{\nu_\beta \rightarrow \nu_\alpha} f_{\beta,S}$$

Astrophysical sources

Earth

Up to a few Gpc



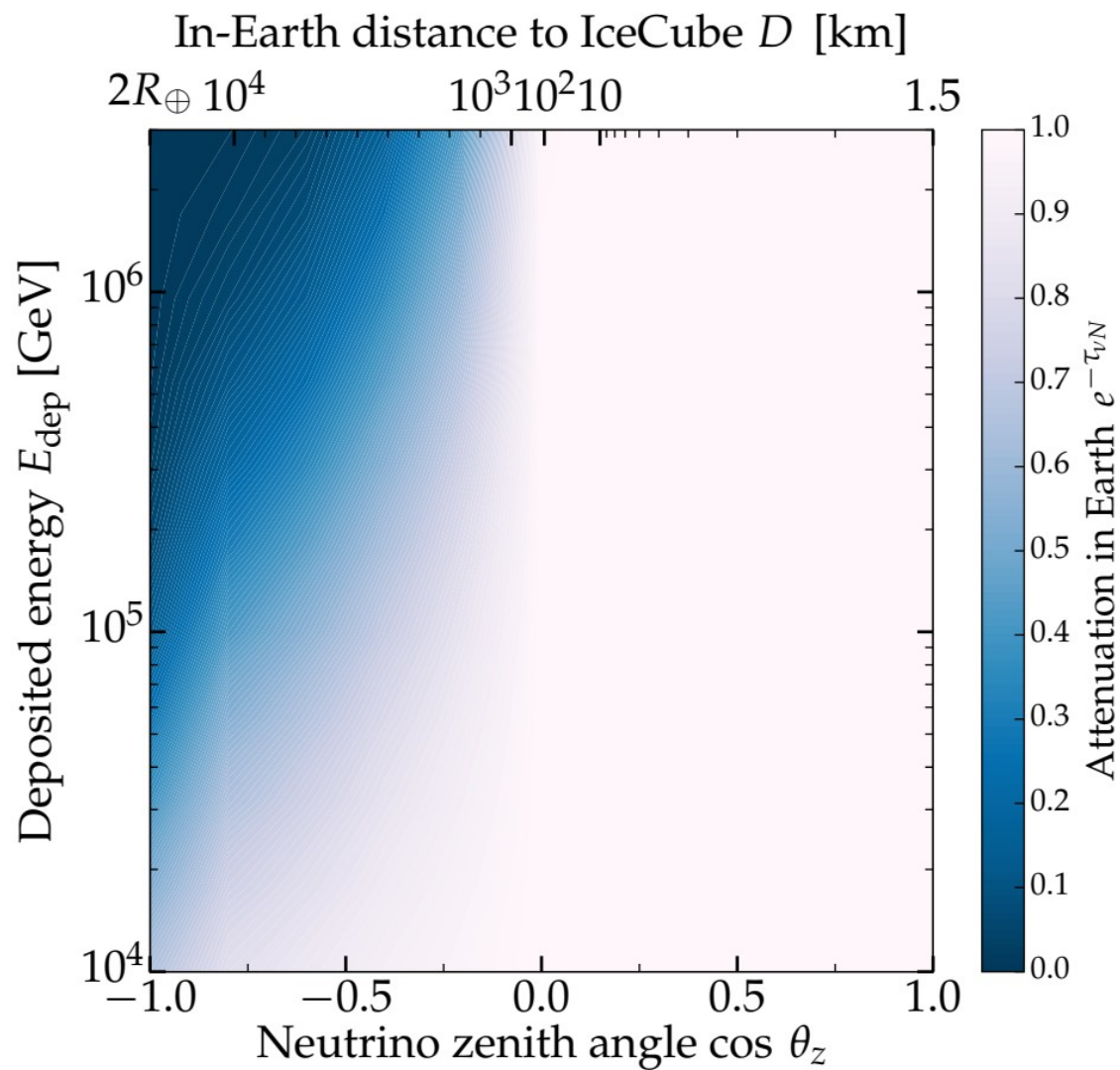
Different production mechanisms yield different flavor ratios:

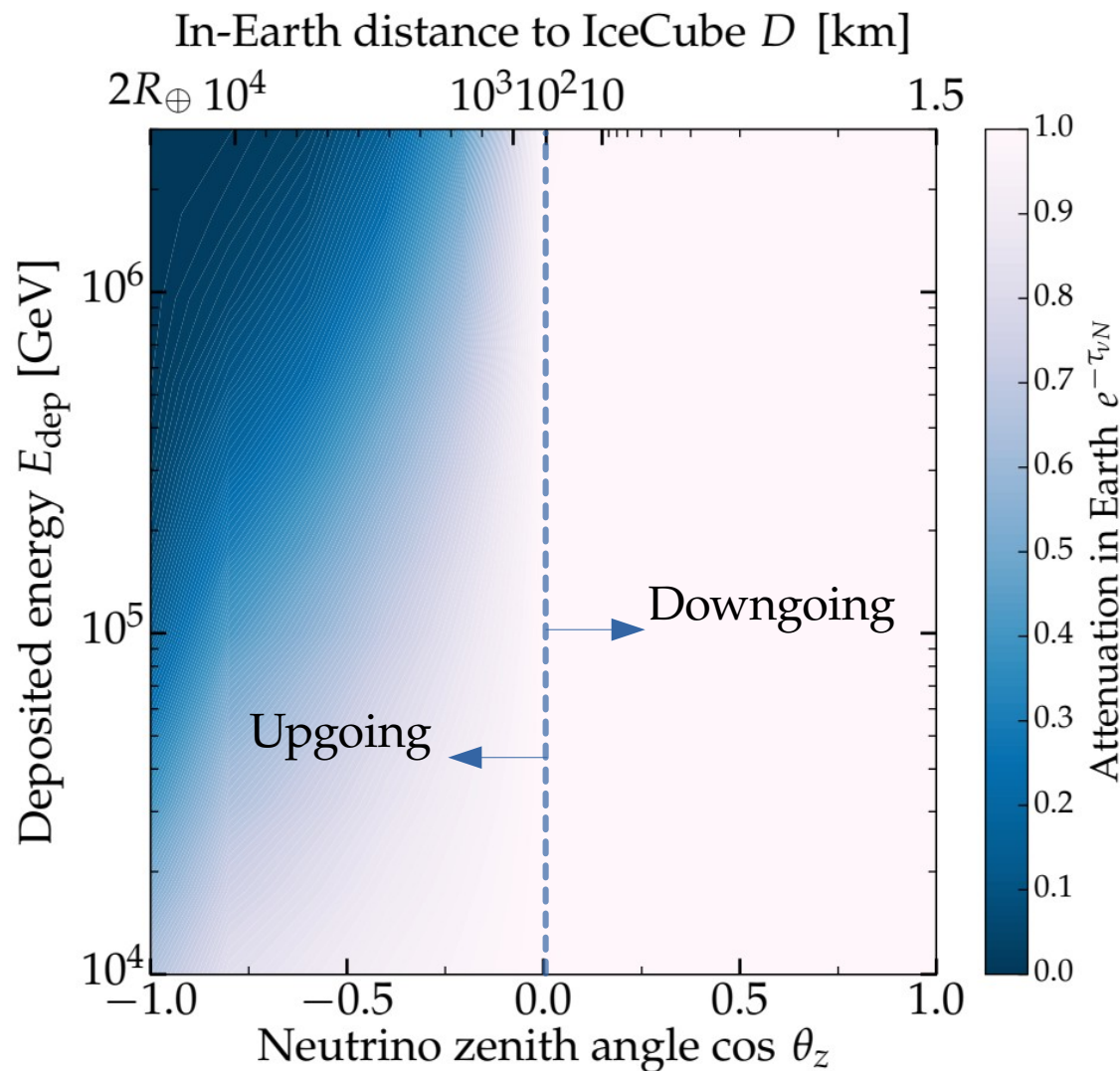
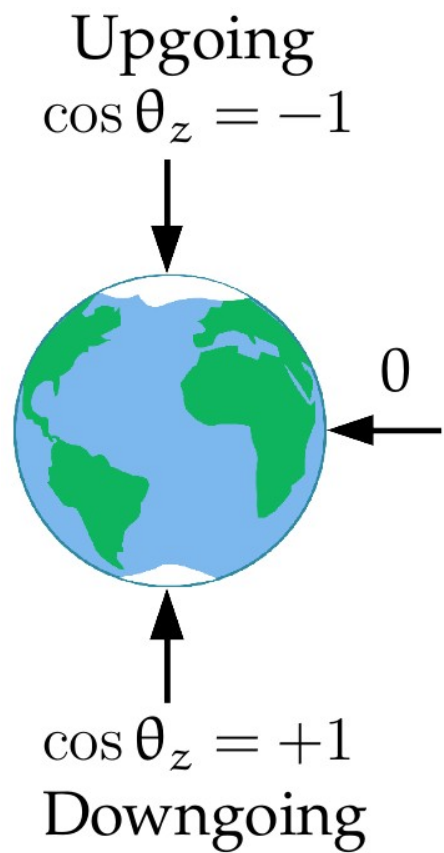
$$(f_{e,S}, f_{\mu,S}, f_{\tau,S}) \equiv (N_{e,S}, N_{\mu,S}, N_{\tau,S}) / N_{\text{tot}}$$

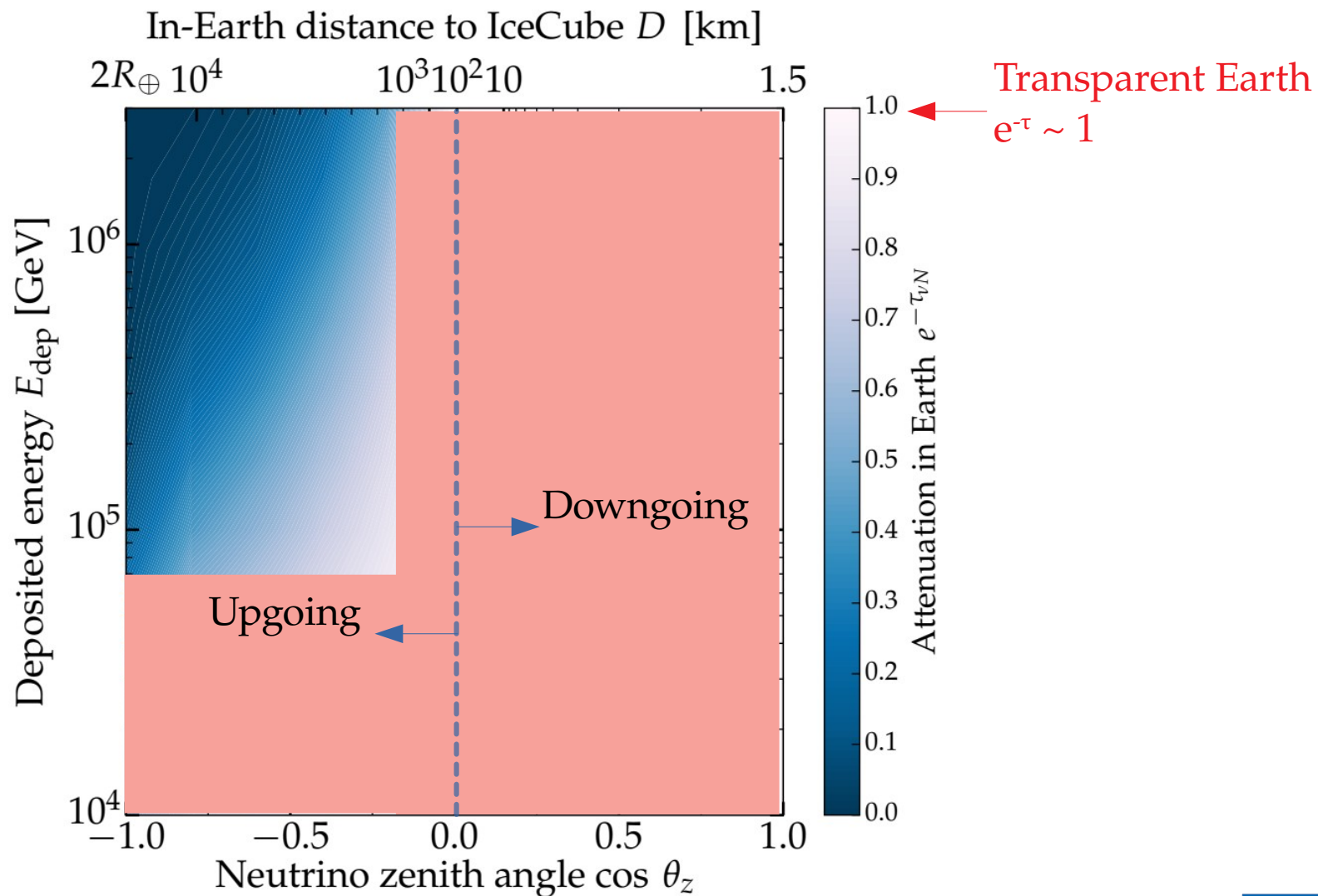
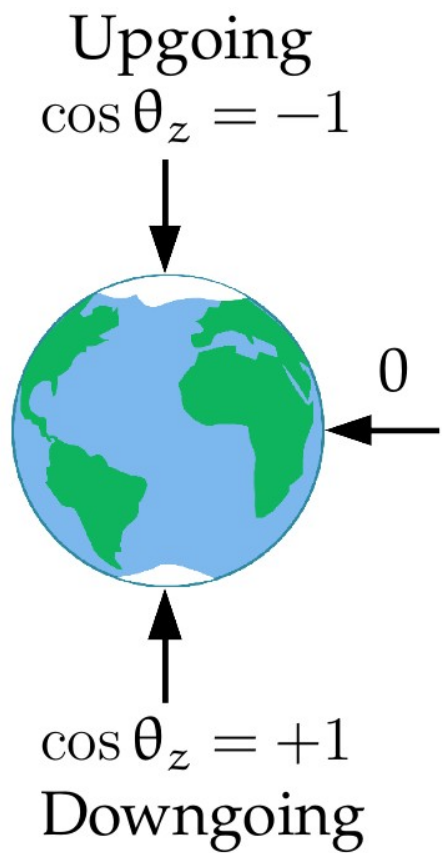
Flavor ratios at Earth ($\alpha = e, \mu, \tau$):

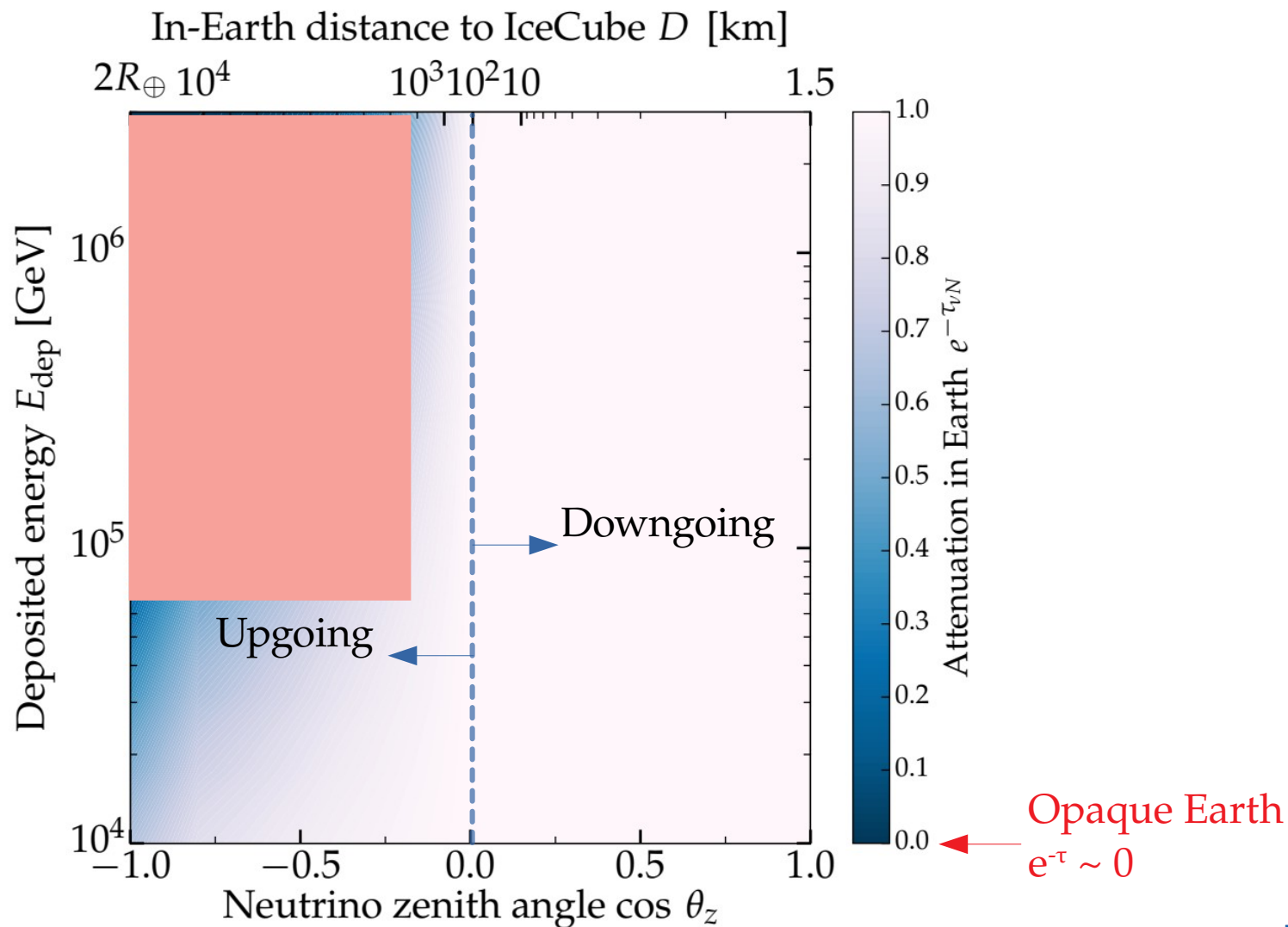
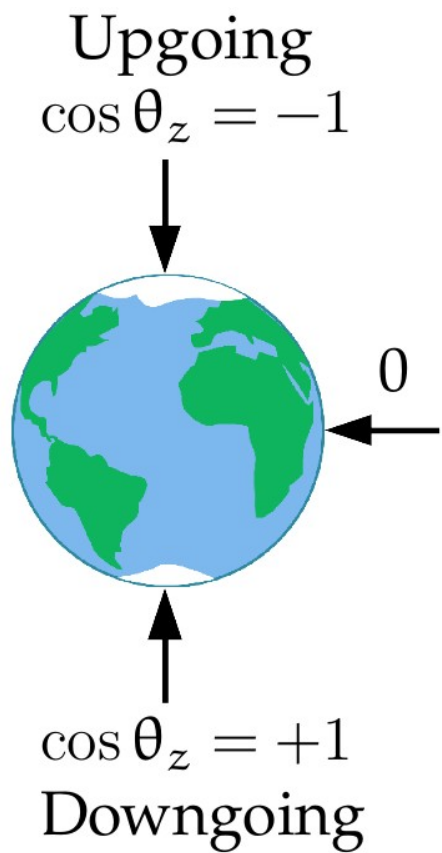
$$f_{\alpha,\oplus} = \sum_{\beta=e,\mu,\tau} P_{\nu_\beta \rightarrow \nu_\alpha} f_{\beta,S}$$

Standard oscillations
or
new physics





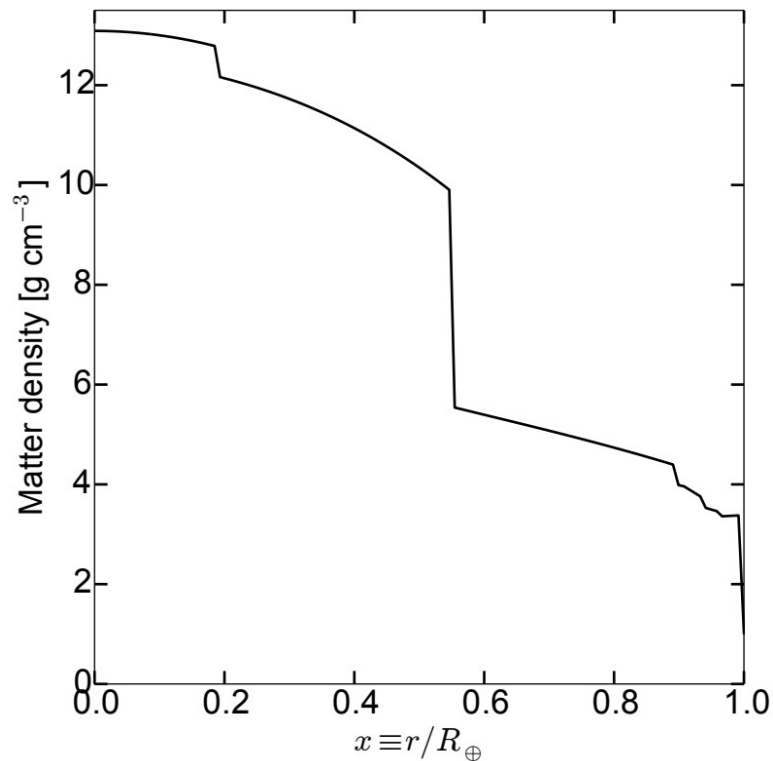




A feel for the in-Earth attenuation

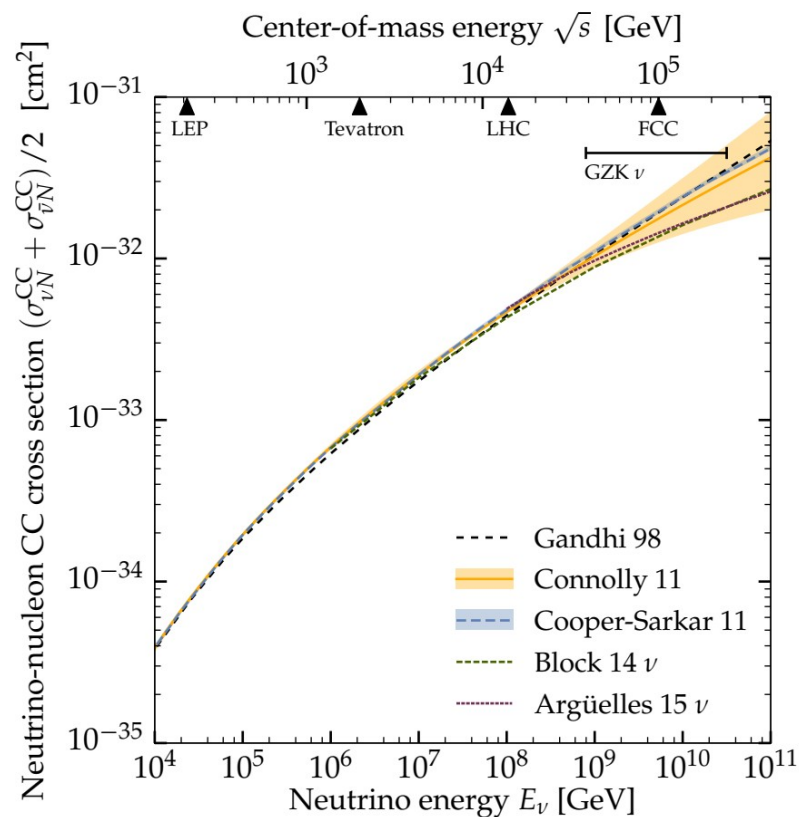
Earth matter density

(Preliminary Reference Earth Model)

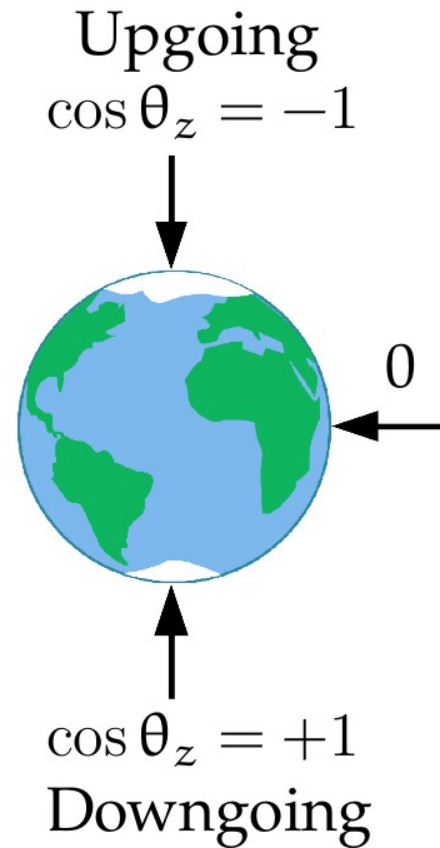
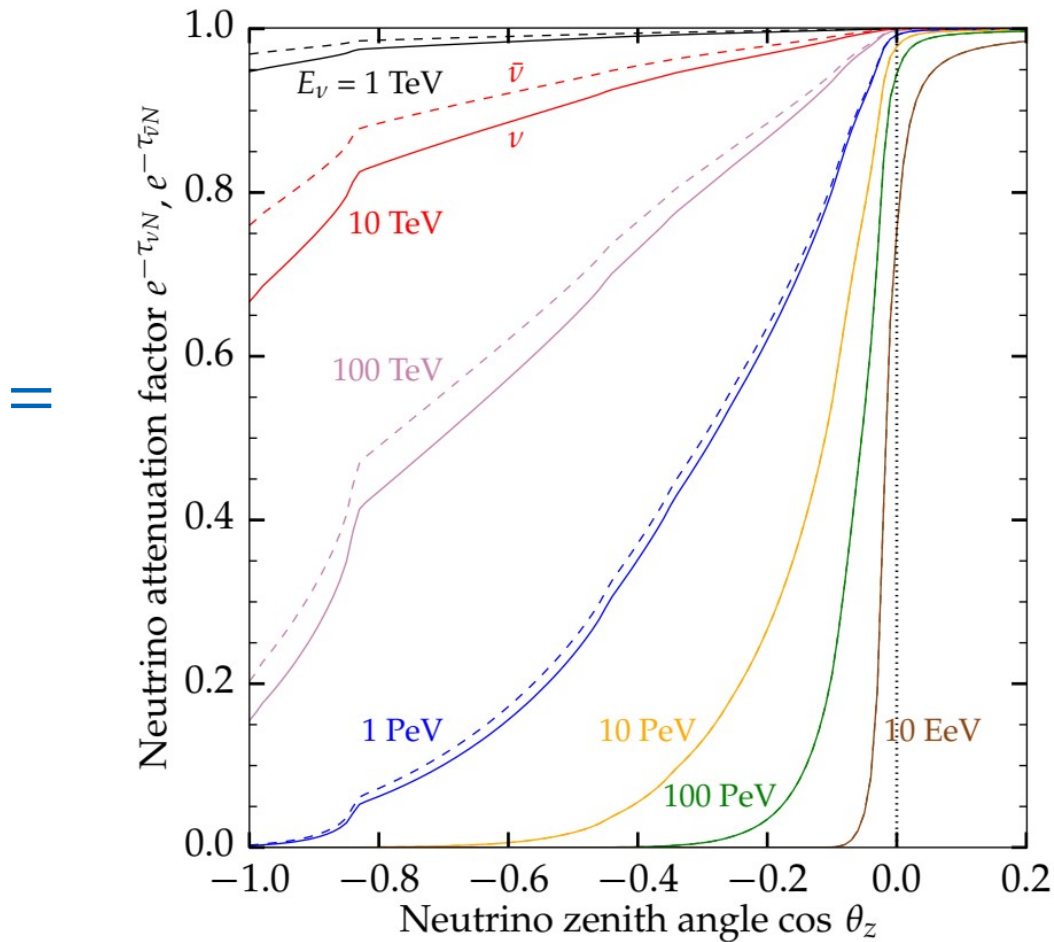


+

Neutrino-nucleon cross section



A feel for the in-Earth attenuation



What goes into the (likelihood) mix?

- ▶ Inside each energy bin, we freely vary
 - ▶ N_{ast} (showers from astrophysical neutrinos)
 - ▶ N_{atm} (showers from atmospheric neutrinos)
 - ▶ γ (astrophysical spectral index)
 - ▶ σ_{CC} (neutrino-nucleon charged-current cross section)
- ▶ For each combination, we generate the angular and energy shower spectrum...
- ▶ ... and compare it to the observed HESE spectrum via a likelihood
- ▶ Maximum likelihood yields σ_{CC} (marginalized over nuisance parameters)
- ▶ Bins are independent of each other – there are no (significant) cross-bin correlations

What goes into the (likelihood) mix?

- ▶ Inside each energy bin, we freely vary
 - ▶ N_{ast} (showers from astrophysical neutrinos)
 - ▶ N_{atm} (showers from atmospheric neutrinos)
 - ▶ γ (astrophysical spectral index)
 - ▶ σ_{CC} (neutrino-nucleon charged-current cross section)
- ▶ For each combination, we generate the angular and energy shower spectrum...
- ▶ ... and compare it to the observed HESE spectrum via a likelihood
- ▶ Maximum likelihood yields σ_{CC} (marginalized over nuisance parameters)
- ▶ Bins are independent of each other – there are no (significant) cross-bin correlations

Including detector resolution
(10% in energy, 15° in direction)

Marginalized cross section in each bin

TABLE I. Neutrino-nucleon charged-current inclusive cross sections, averaged between neutrinos ($\sigma_{\nu N}^{\text{CC}}$) and anti-neutrinos ($\sigma_{\bar{\nu} N}^{\text{CC}}$), extracted from 6 years of IceCube HESE showers. To obtain these results, we fixed $\sigma_{\bar{\nu} N}^{\text{CC}} = \langle \sigma_{\bar{\nu} N}^{\text{CC}} / \sigma_{\nu N}^{\text{CC}} \rangle \cdot \sigma_{\nu N}^{\text{CC}}$ — where $\langle \sigma_{\bar{\nu} N}^{\text{CC}} / \sigma_{\nu N}^{\text{CC}} \rangle$ is the average ratio of $\bar{\nu}$ to ν cross sections calculated using the standard prediction from Ref. [60](#) — and $\sigma_{\nu N}^{\text{NC}} = \sigma_{\nu N}^{\text{CC}}/3$, $\sigma_{\bar{\nu} N}^{\text{NC}} = \sigma_{\bar{\nu} N}^{\text{CC}}/3$. Uncertainties are statistical plus systematic, added in quadrature.

E_ν [TeV]	$\langle E_\nu \rangle$ [TeV]	$\langle \sigma_{\bar{\nu} N}^{\text{CC}} / \sigma_{\nu N}^{\text{CC}} \rangle$	$\log_{10}[\frac{1}{2}(\sigma_{\nu N}^{\text{CC}} + \sigma_{\bar{\nu} N}^{\text{CC}})/\text{cm}^2]$
18–50	32	0.752	-34.35 ± 0.53
50–100	75	0.825	-33.80 ± 0.67
100–400	250	0.888	-33.84 ± 0.67
400–2004	1202	0.957	$> -33.21 (1\sigma)$

Energy and angular shower spectra

Rate from all flavors, CC + NC:

$$\frac{d^2 N_{\text{sh}}}{dE_{\text{sh}} d \cos \theta_z} = \frac{d^2 N_{\text{sh},e}^{\text{CC}}}{dE_{\text{sh}} d \cos \theta_z} + \text{Br}_{\tau \rightarrow \text{sh}} \frac{d^2 N_{\text{sh},\tau}^{\text{CC}}}{dE_{\text{sh}} d \cos \theta_z} + \sum_{l=e,\mu,\tau} \frac{d^2 N_{\text{sh},l}^{\text{NC}}}{dE_{\text{sh}} d \cos \theta_z}$$

$\text{Br}_{\tau \rightarrow \text{sh}} = 0.83$

Contribution from one flavor CC:

$$\frac{d^2 N_{\text{sh},l}^{\text{CC}}}{dE_{\text{sh}} d \cos \theta_z}(E_{\text{sh}}, \cos \theta_z) \simeq -2\pi \rho_{\text{ice}} N_A V T \left\{ \Phi_l(E_\nu) \sigma_{\nu N}^{\text{CC}}(E_\nu) e^{-\tau_{\nu N}(E_\nu, \theta_z)} + \Phi_{\bar{l}}(E_\nu) \sigma_{\bar{\nu} N}^{\text{CC}}(E_\nu) e^{-\tau_{\bar{\nu} N}(E_\nu, \theta_z)} \right\} \Big|_{E_\nu = E_{\text{sh}}/f_{l,\text{CC}}}$$

Conversion between shower energy and neutrino energy:

$$f_{l,t} \equiv \frac{E_{\text{sh}}}{E_\nu} \simeq \begin{cases} 1 & \text{for } l = e \text{ and } t = \text{CC} \\ [\langle y \rangle + 0.7(1 - \langle y \rangle)] \simeq 0.8 & \text{for } l = \tau \text{ and } t = \text{CC} \\ \langle y \rangle \simeq 0.25 & \text{for } l = e, \mu, \tau \text{ and } t = \text{NC} \end{cases}$$

Detector resolution

Number of contained showers:

$$\frac{d^2 N_{\text{sh}}}{dE_{\text{dep}} d \cos \theta_z} = \int dE_{\text{sh}} \int d \cos \theta'_z \frac{d^2 N_{\text{sh}}}{dE_{\text{sh}} d \cos \theta'_z} R_E(E_{\text{sh}}, E_{\text{dep}}, \sigma_E(E_{\text{sh}})) R_\theta(\cos \theta'_z, \cos \theta_z, \sigma_{\cos \theta_z})$$

Energy resolution: [Palomares-Ruiz, Vincent, Mena *PRD* 2015; Vincent, Palomares-Ruiz, Mena *PRD* 2016; MB, Beacom, Murase, *PRD* 2016]

$$R_E(E_{\text{sh}}, E_{\text{dep}}, \sigma_E(E_{\text{sh}})) = \frac{1}{\sqrt{2\pi\sigma_E^2(E_{\text{sh}})}} \exp \left[-\frac{(E_{\text{sh}} - E_{\text{dep}})^2}{2\sigma_E^2(E_{\text{sh}})} \right] \quad \text{with } \sigma_E(E_{\text{sh}}) = 0.1 E_{\text{sh}}$$

IceCube, *JINST* 2014

Angular resolution:

$$R_\theta(\cos \theta'_z, \cos \theta_z, \sigma_{\cos \theta_z}) = \frac{1}{\sqrt{2\pi\sigma_{\cos \theta_z}^2}} \exp \left[-\frac{(\cos \theta'_z - \cos \theta_z)^2}{2\sigma_{\cos \theta_z}^2} \right]$$

with $\sigma_{\cos \theta_z} \equiv \frac{1}{2} [|\cos(\theta_z + \sigma_{\theta_z}) - \cos \theta_z| + |\cos(\theta_z - \sigma_{\theta_z}) - \cos \theta_z|]$ and $\sigma_{\theta_z} = 15^\circ$

MB & A. Connolly, 1711.11043

Likelihood

In an energy bin containing $N_{\text{sh}}^{\text{obs}}$ observed showers, the likelihood is

Each energy bin is independent

$$\mathcal{L} = \frac{e^{-(N_{\text{sh}}^{\text{atm}} + N_{\text{sh}}^{\text{ast}})}}{N_{\text{sh}}^{\text{obs}}!} \prod_{i=1}^{N_{\text{sh}}^{\text{obs}}} \mathcal{L}_i$$

Partial likelihood, *i.e.*, relative probability of the i -th shower being from an atmospheric neutrino or an astrophysical neutrino:

Depends on σ_{vN}

$$\mathcal{L}_i = N_{\text{sh}}^{\text{atm}} \mathcal{P}_i^{\text{atm}} + N_{\text{sh}}^{\text{ast}} \mathcal{P}_i^{\text{ast}}$$

$$\mathcal{P}_i^{\text{atm}} = \left(\int_{E_{\text{dep}}^{\text{min}}}^{E_{\text{dep}}^{\text{max}}} dE_{\text{dep}} \int_{-1}^1 d \cos \theta_z \frac{d^2 N_{\text{sh}}^{\text{atm}}}{dE_{\text{dep}} d \cos \theta_z} \right)^{-1} \left(\frac{d^2 N_{\text{sh}}^{\text{atm}}}{dE_{\text{dep}} d \cos \theta_z} \Big|_{E_{\text{dep},i}, \cos \theta_{z,i}} \right)$$

PDF for this shower to be made by an atmospheric ν

$$\mathcal{P}_i^{\text{ast}} = \left(\int_{E_{\text{dep}}^{\text{min}}}^{E_{\text{dep}}^{\text{max}}} dE_{\text{dep}} \int_{-1}^1 d \cos \theta_z \frac{d^2 N_{\text{sh}}^{\text{ast}}}{dE_{\text{dep}} d \cos \theta_z} \right)^{-1} \left(\frac{d^2 N_{\text{sh}}^{\text{ast}}}{dE_{\text{dep}} d \cos \theta_z} \Big|_{E_{\text{dep},i}, \cos \theta_{z,i}} \right)$$

PDF for this shower to be made by an astrophysical ν

Depends on γ and σ_{vN}

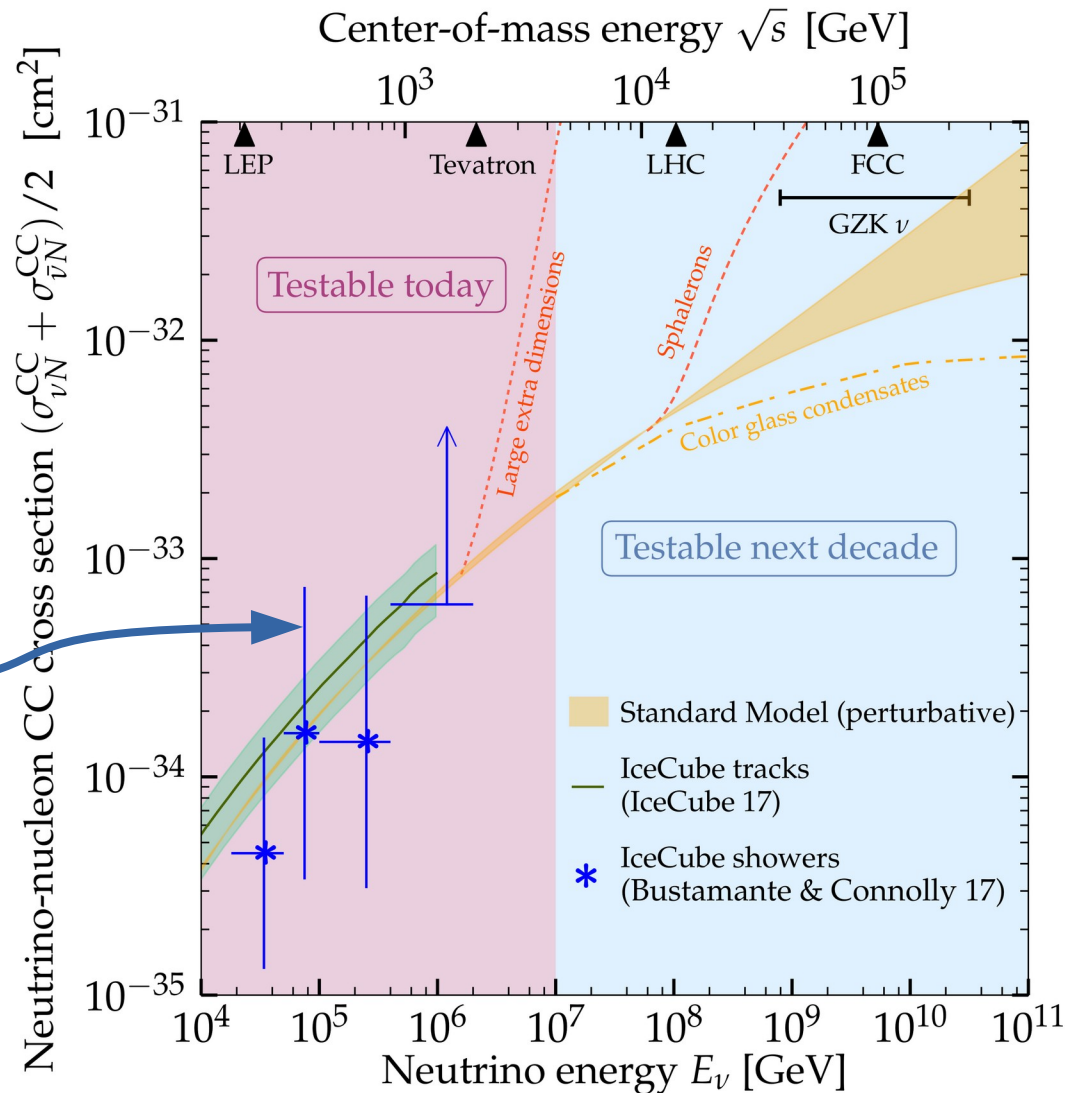
MB & A. Connolly, 1711.11043

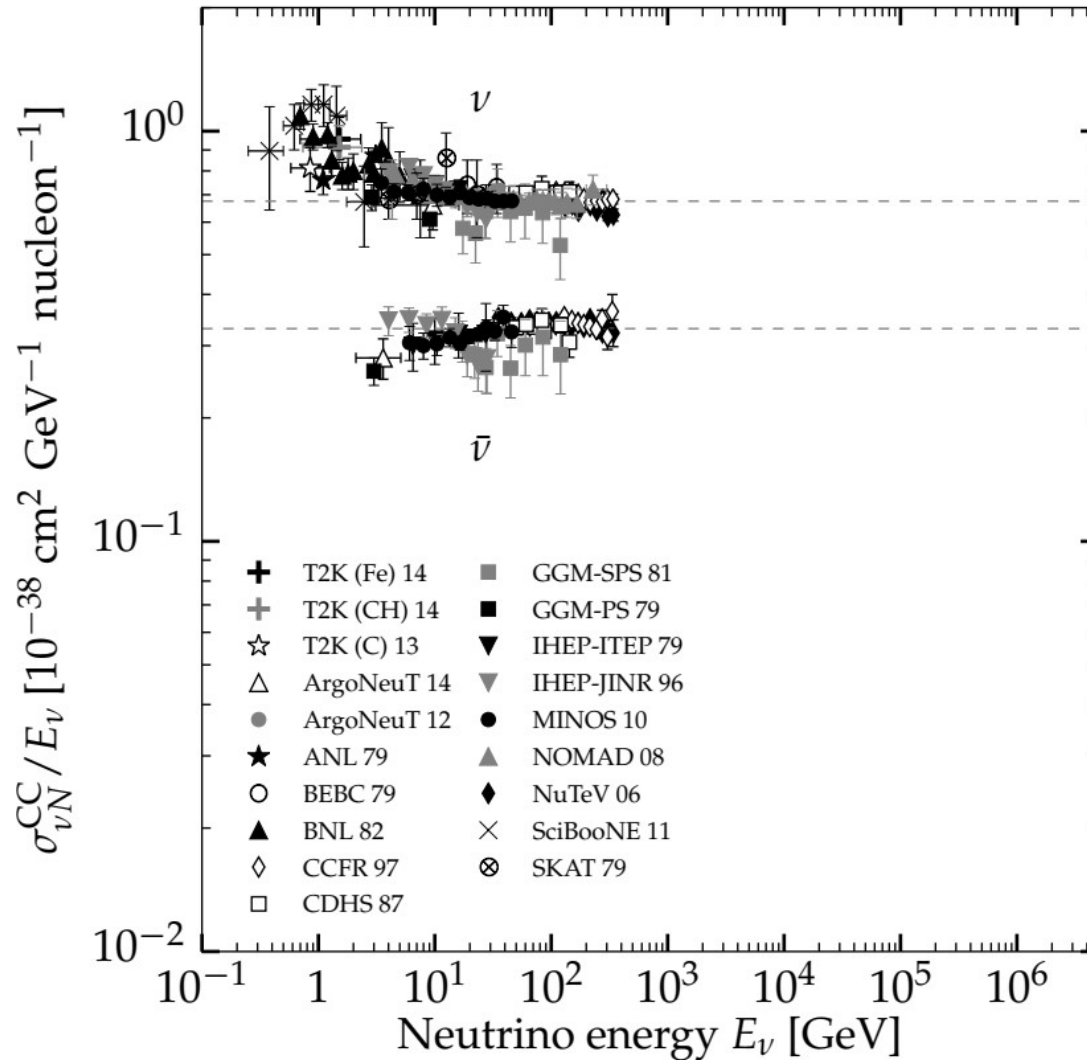
See also: Palomares-Ruiz, Vincent, Mena *PRD* 2015; Vincent, Palomares-Ruiz, Mena *PRD* 2016

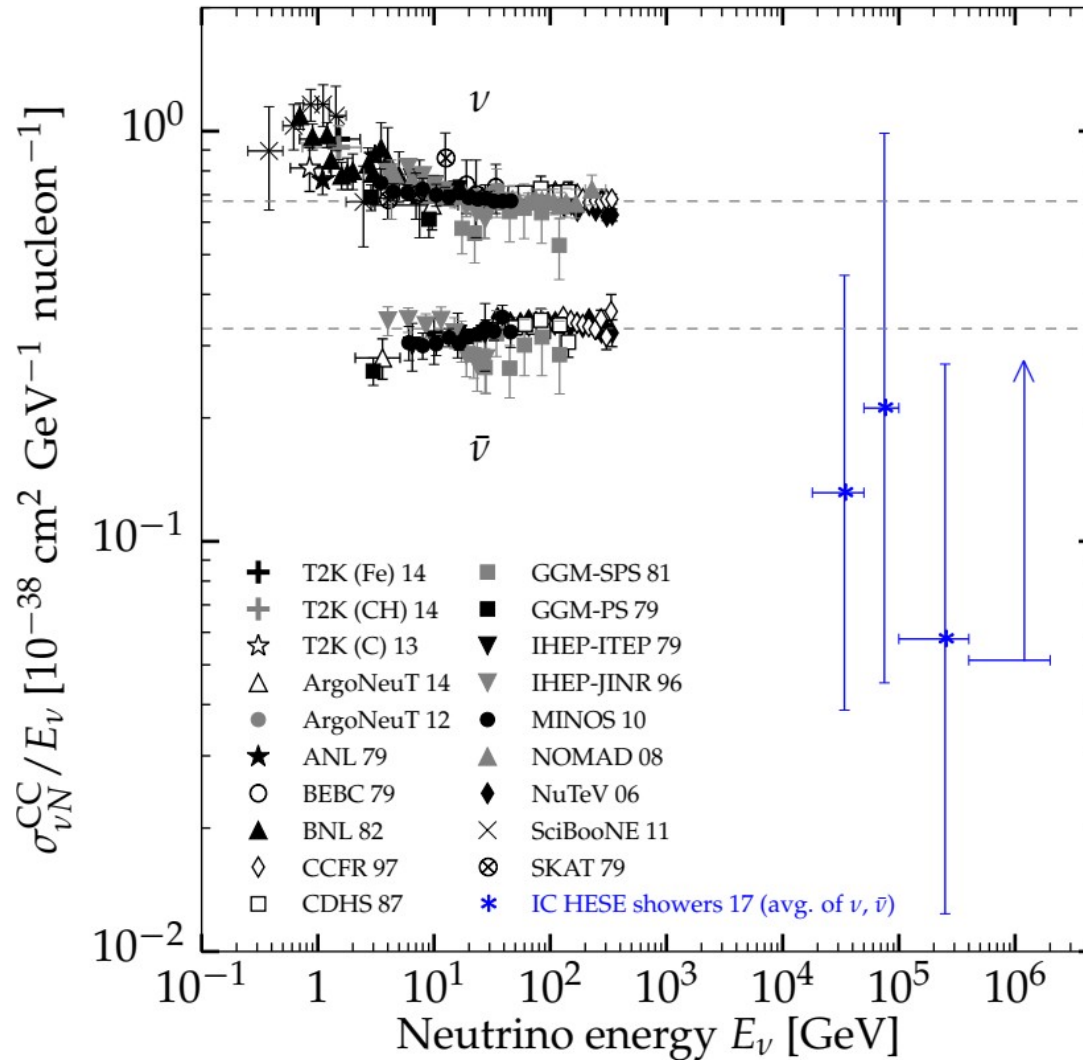
The fine print

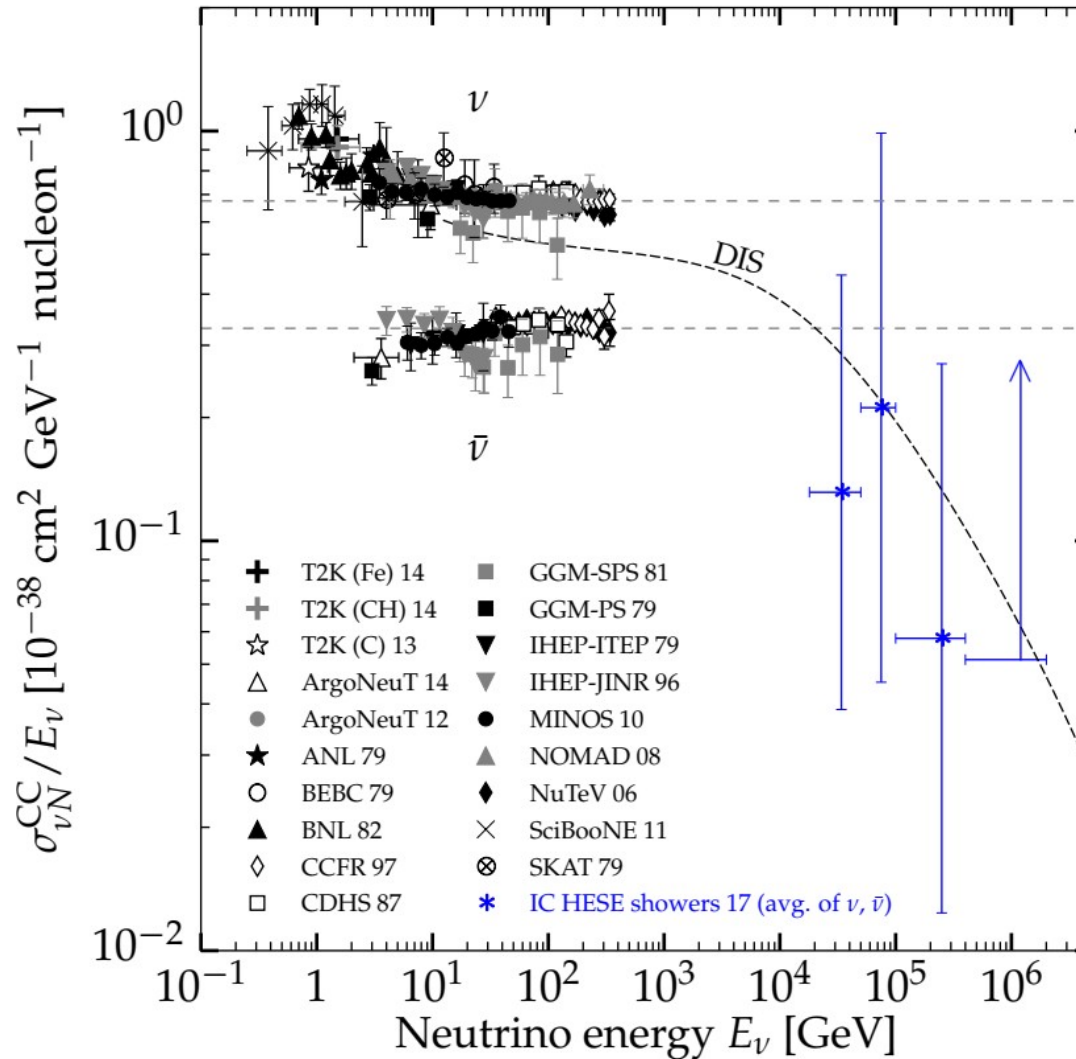
- ▶ High-energy ν 's: astrophysical (isotropic) + atmospheric (**anisotropic**)
→ We take into account the shape of the atmospheric contribution
- ▶ The shape of the astrophysical ν **energy spectrum** is still uncertain
→ We take a $E^{-\gamma}$ spectrum in *narrow* energy bins
- ▶ **NC showers** are sub-dominant to **CC showers**, but they are indistinguishable
→ Following Standard-Model predictions, we take $\sigma_{\text{NC}} = \sigma_{\text{CC}}/3$
- ▶ IceCube does not **distinguish ν from $\bar{\nu}$** , and their cross-sections are different
→ We assume equal fluxes, expected from production via pp collisions
→ We assume the avg. ratio $\langle \sigma_{\nu N} / \sigma_{\bar{\nu} N} \rangle$ in each bin known, from SM predictions
- ▶ The **flavor composition** of astrophysical neutrinos is still uncertain
→ We assume equal flux of each flavor, compatible with theory and observations

- ▶ Fold in astrophysical unknowns (spectral index, normalization)
- ▶ Compatible with SM predictions
- ▶ Still room for new physics
- ▶ Today, using IceCube:
 - ▶ Extracted from ~60 showers in 6 yr
 - ▶ Limited by statistics
- ▶ Future, using IceCube-Gen2:
 - ▶ $\times 5$ volume \Rightarrow 300 showers in 6 yr
 - ▶ Reduce statistical error by 40%

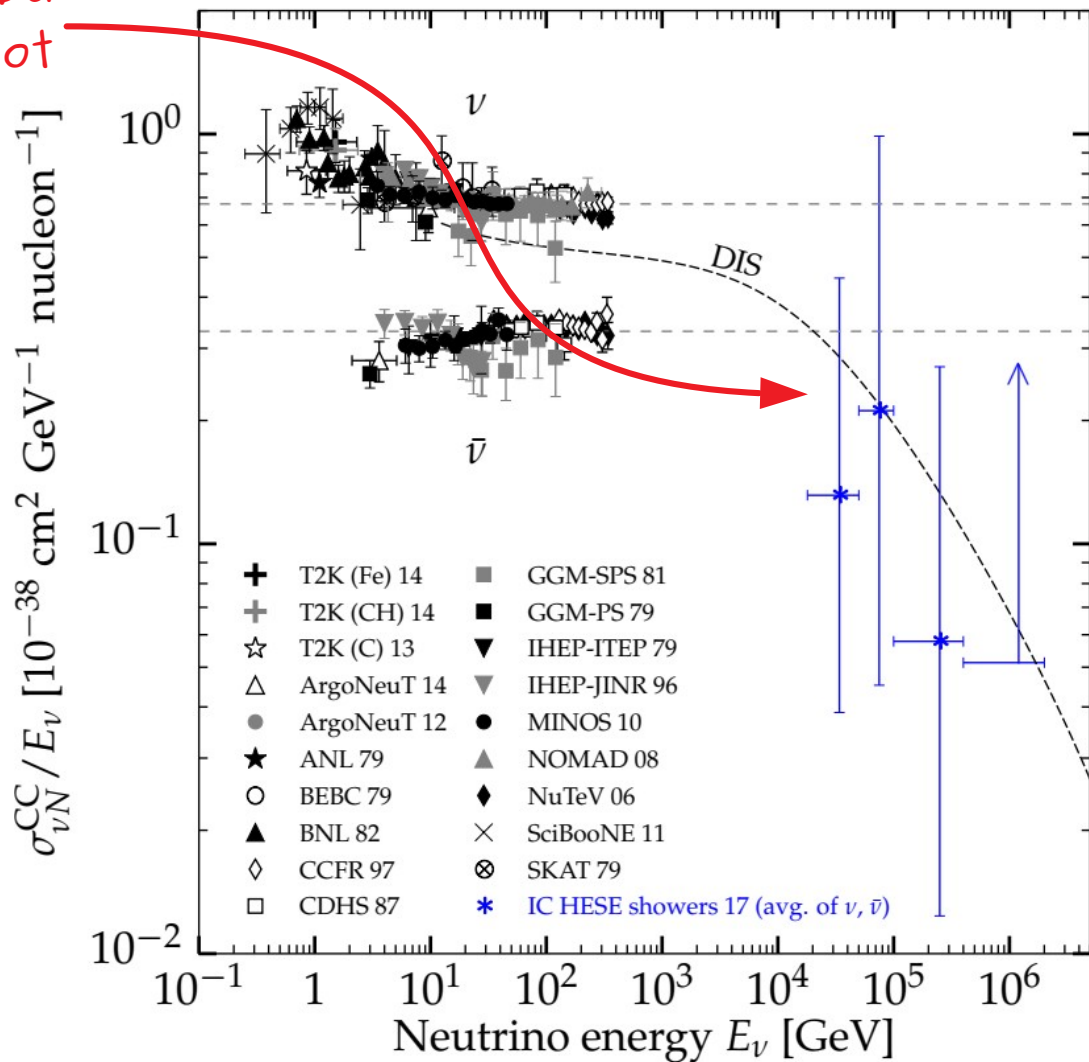








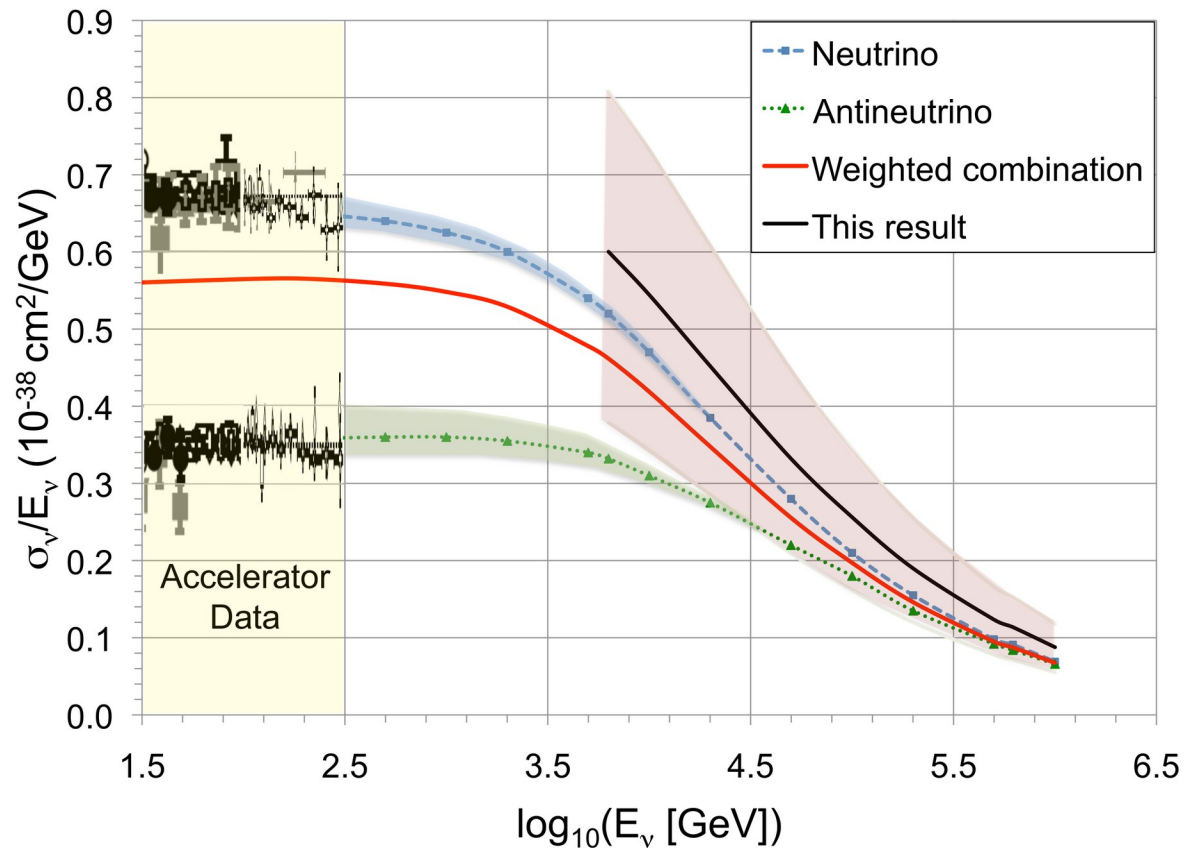
Extending the PDG
cross-section plot



MB & Connolly PRL 2019
See also: IceCube, Nature 2017

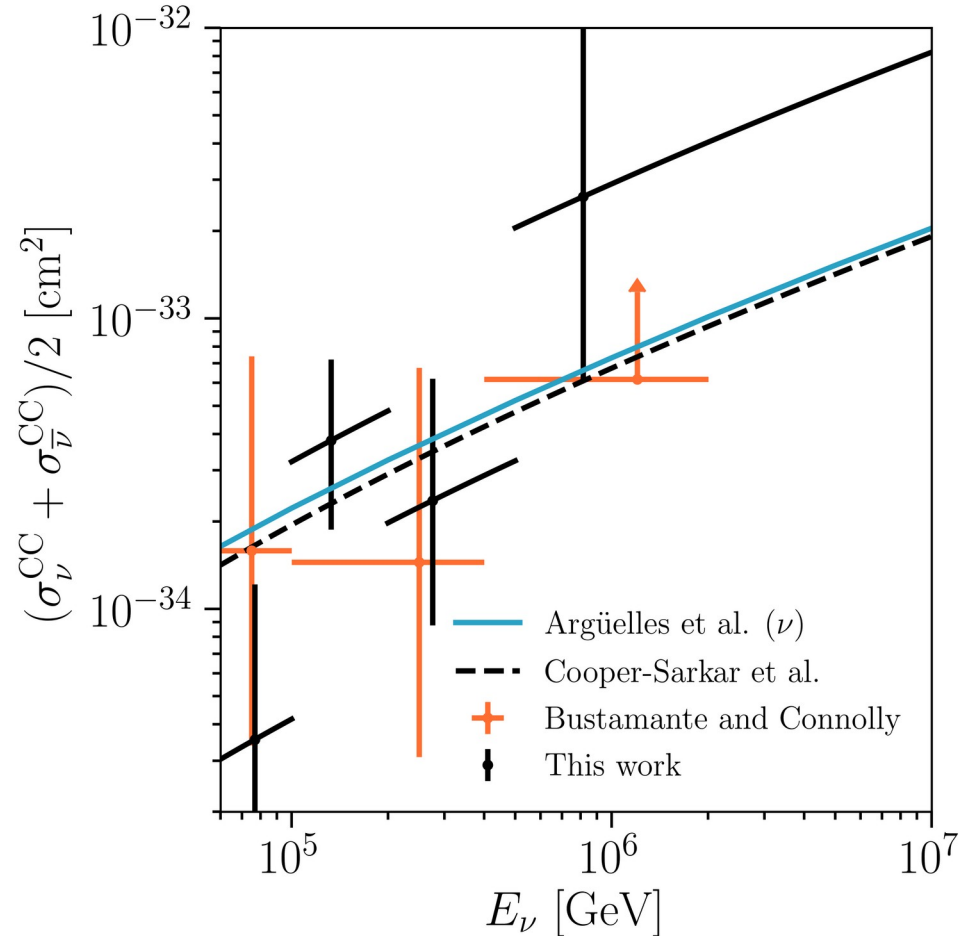
Using through-going muons instead

- ▶ Use $\sim 10^4$ through-going muons
- ▶ Measured: dE_μ/dx
- ▶ Inferred: $E_\mu \approx dE_\mu/dx$
- ▶ From simulations (uncertain):
most likely E_ν given E_μ
- ▶ Fit the ratio $\sigma_{\text{obs}}/\sigma_{\text{SM}}$
 $1.30^{+0.21}_{-0.19}(\text{stat.})^{+0.39}_{-0.43}(\text{syst.})$
- ▶ All events grouped in a single
energy bin 6–980 TeV



Updated cross section measurement

- ▶ Uses 7.5 years of IceCube data
- ▶ Uses starting showers + tracks
 - ▶ Vs. starting showers only in Bustamante & Connolly 2017
 - ▶ Vs. throughgoing muons in IceCube 2017
- ▶ Extends measurement to 10 PeV
- ▶ Still compatible with Standard Model predictions
- ▶ Higher energies? Work in progress by Valera & MB



Bonus: Measuring the inelasticity $\langle y \rangle$

- ▶ Inelasticity in CC ν_μ interaction $\nu_\mu + N \rightarrow \mu + X$:

$$E_X = y E_\nu \quad \text{and} \quad E_\mu = (1-y) E_\nu \Rightarrow y = (1 + E_\mu/E_X)^{-1}$$

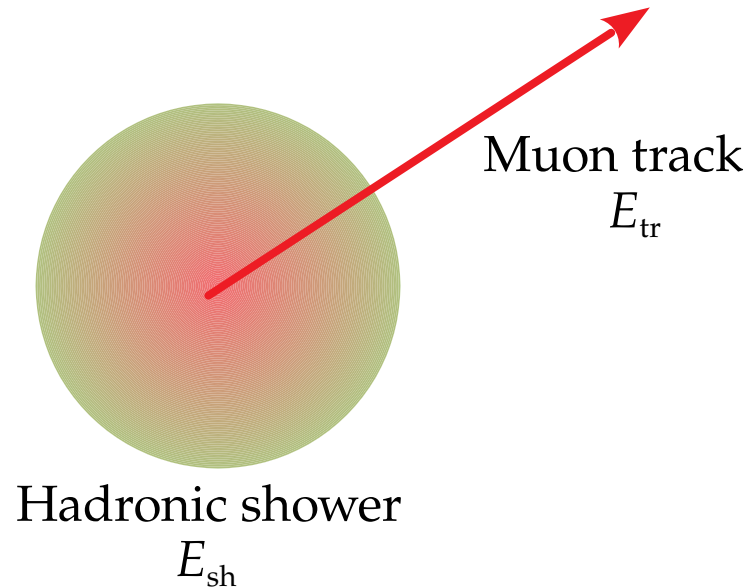
- ▶ The value of y follows a distribution $d\sigma/dy$

- ▶ In a HESE starting track:

$$\left. \begin{array}{l} E_X = E_{\text{sh}} \text{ (energy of shower)} \\ E_\mu = E_{\text{tr}} \text{ (energy of track)} \end{array} \right\} y = (1 + E_{\text{tr}}/E_{\text{sh}})^{-1}$$

- ▶ New IceCube analysis:

- ▶ 5 years of starting-track data (2650 tracks)
- ▶ Machine learning separates shower from track
- ▶ Different y distributions for ν and $\bar{\nu}$



Bonus: Measuring the inelasticity $\langle y \rangle$

- ▶ Inelasticity in CC ν_μ interaction $\nu_\mu + N \rightarrow \mu + X$:

$$E_X = y E_\nu \quad \text{and} \quad E_\mu = (1-y) E_\nu \Rightarrow y = (1 + E_\mu/E_X)^{-1}$$

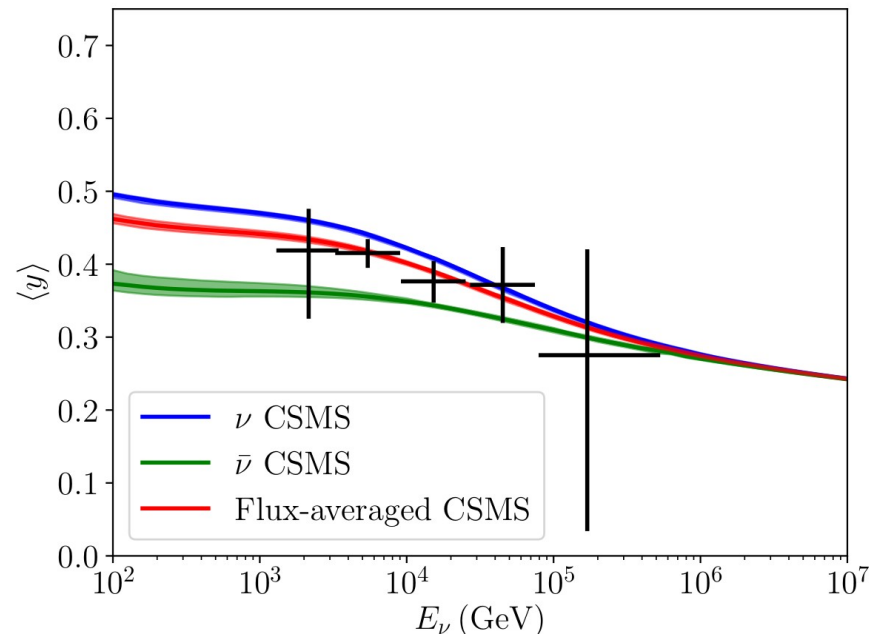
- ▶ The value of y follows a distribution $d\sigma/dy$

- ▶ In a HESE starting track:

$$\left. \begin{array}{l} E_X = E_{\text{sh}} \text{ (energy of shower)} \\ E_\mu = E_{\text{tr}} \text{ (energy of track)} \end{array} \right\} y = (1 + E_{\text{tr}}/E_{\text{sh}})^{-1}$$

- ▶ New IceCube analysis:

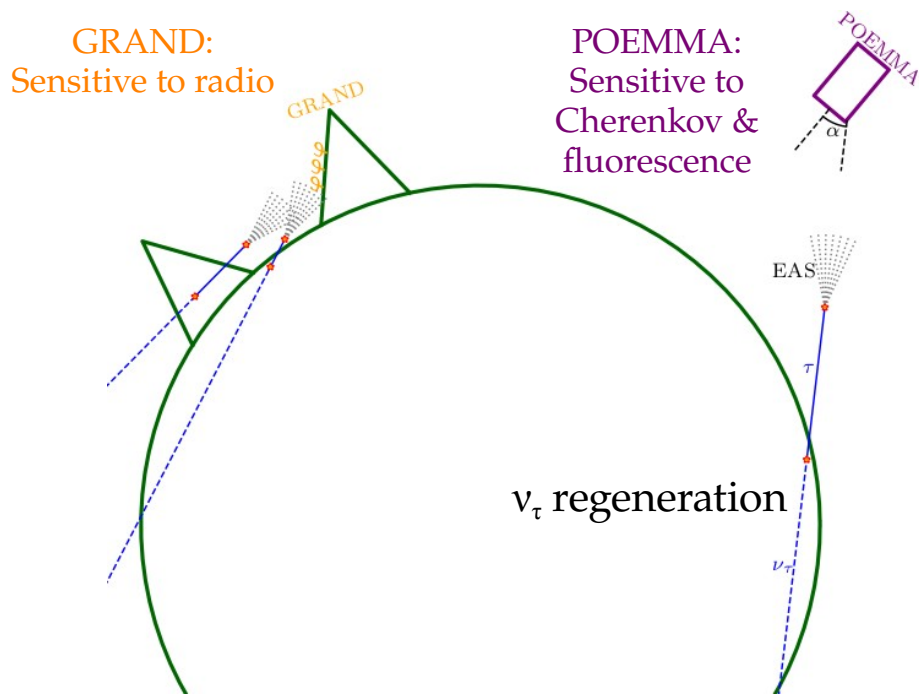
- ▶ 5 years of starting-track data (2650 tracks)
- ▶ Machine learning separates shower from track
- ▶ Different y distributions for ν and $\bar{\nu}$



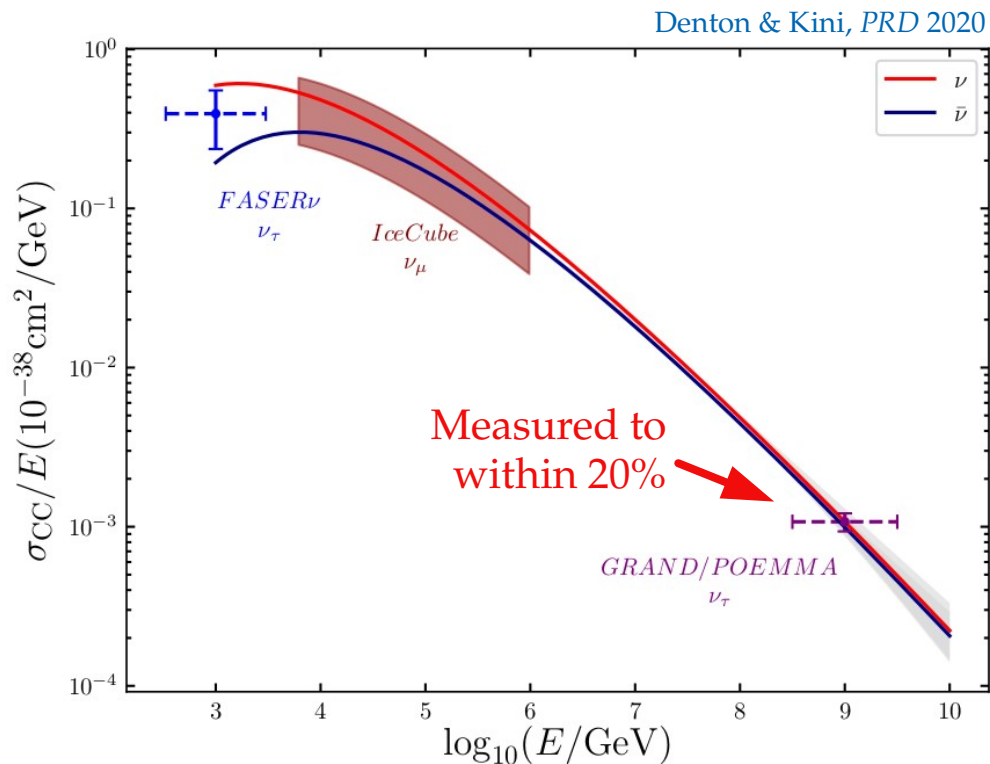
IceCube, PRD 2019

GRAND & POEMMA

Both sensitive to extensive air showers
induced by Earth-skimming UHE ν_τ



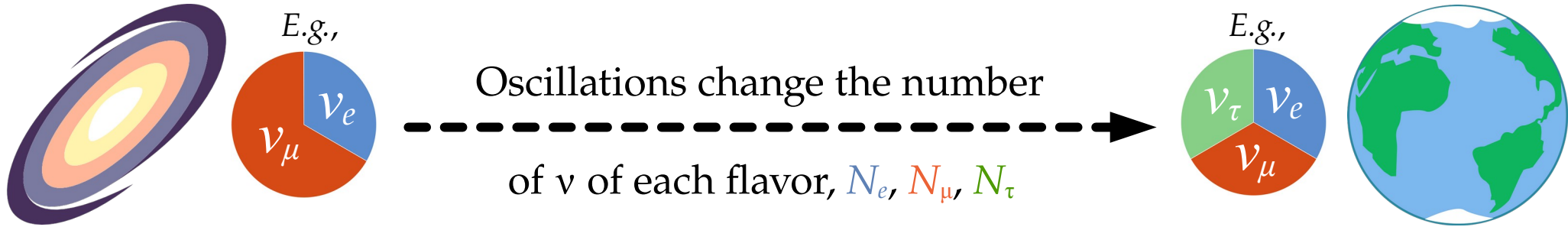
If they see 100 events from ν_τ with initial energy of 10^9 GeV (pre-attenuation):



Astrophysical sources

Earth

Up to a few Gpc



Different production mechanisms yield different flavor ratios:

$$(f_{e,S}, f_{\mu,S}, f_{\tau,S}) \equiv (N_{e,S}, N_{\mu,S}, N_{\tau,S}) / N_{\text{tot}}$$

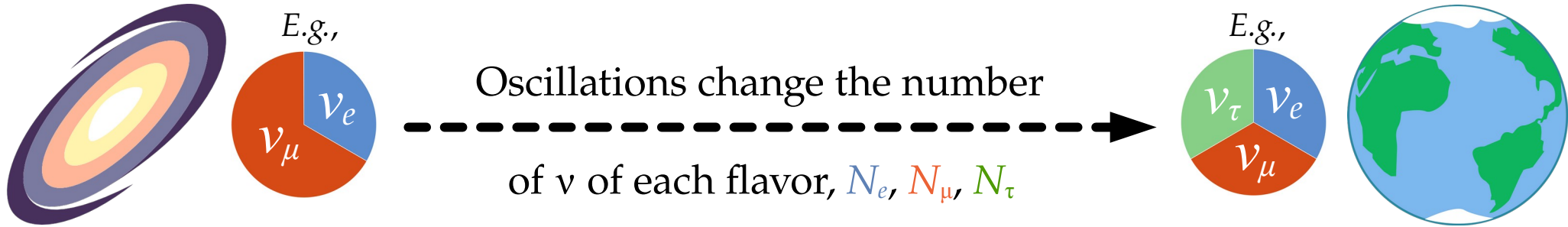
Flavor ratios at Earth ($\alpha = e, \mu, \tau$):

$$f_{\alpha,\oplus} = \sum_{\beta=e,\mu,\tau} P_{\nu_\beta \rightarrow \nu_\alpha} f_{\beta,S}$$

Astrophysical sources

Earth

Up to a few Gpc



Different production mechanisms yield different flavor ratios:

$$(f_{e,S}, f_{\mu,S}, f_{\tau,S}) \equiv (N_{e,S}, N_{\mu,S}, N_{\tau,S}) / N_{\text{tot}}$$

Flavor ratios at Earth ($\alpha = e, \mu, \tau$):

$$f_{\alpha,\oplus} = \sum_{\beta=e,\mu,\tau} P_{\nu_\beta \rightarrow \nu_\alpha} f_{\beta,S}$$

Standard oscillations
or
new physics

Flavor at the Earth: *theoretically palatable regions*

Theoretically palatable flavor regions

≡

MB, Beacom, Winter, PRL 2015

Allowed regions of flavor ratios at Earth derived from oscillations

Note:

The original palatable regions were
frequentist [MB, Beacom, Winter, PRL 2015];
the new ones are Bayesian

Flavor at the Earth: *theoretically palatable regions*

Theoretically palatable flavor regions

≡

MB, Beacom, Winter, PRL 2015

Allowed regions of flavor ratios at Earth derived from oscillations

Ingredient #1:

Flavor ratios at the source,

$$(f_{e,S}, f_{\mu,S}, f_{\tau,S})$$

Fix at one of the benchmarks
(pion decay, muon-damped, neutron decay)

or

Explore all possible combinations

Note:

The original palatable regions were
frequentist [MB, Beacom, Winter, PRL 2015];
the new ones are Bayesian

Flavor at the Earth: *theoretically palatable regions*

Theoretically palatable flavor regions

≡

MB, Beacom, Winter, PRL 2015

Allowed regions of flavor ratios at Earth derived from oscillations

Ingredient #1:

Flavor ratios at the source,

$$(f_{e,S}, f_{\mu,S}, f_{\tau,S})$$

Ingredient #2:

Fix at one of the benchmarks
(pion decay, muon-damped, neutron decay)

or

Explore all possible combinations

Note:

The original palatable regions were
frequentist [MB, Beacom, Winter, PRL 2015];
the new ones are Bayesian

Flavor at the Earth: *theoretically palatable regions*

Theoretically palatable flavor regions

≡

MB, Beacom, Winter, PRL 2015

Allowed regions of flavor ratios at Earth derived from oscillations

Ingredient #1:

Flavor ratios at the source,

$(f_{e,S}, f_{\mu,S}, f_{\tau,S})$

Ingredient #2:

Probability density of mixing
parameters $(\theta_{12}, \theta_{23}, \theta_{13}, \delta_{CP})$

Fix at one of the benchmarks
(pion decay, muon-damped, neutron decay)

or

Explore all possible combinations

Note:

The original palatable regions were
frequentist [MB, Beacom, Winter, PRL 2015];
the new ones are Bayesian

Flavor at the Earth: *theoretically palatable regions*

Theoretically palatable flavor regions

≡

MB, Beacom, Winter, *PRL* 2015

Allowed regions of flavor ratios at Earth derived from oscillations

Ingredient #1:

Flavor ratios at the source,

$$(f_{e,S}, f_{\mu,S}, f_{\tau,S})$$

Ingredient #2:

Probability density of mixing parameters $(\theta_{12}, \theta_{23}, \theta_{13}, \delta_{\text{CP}})$

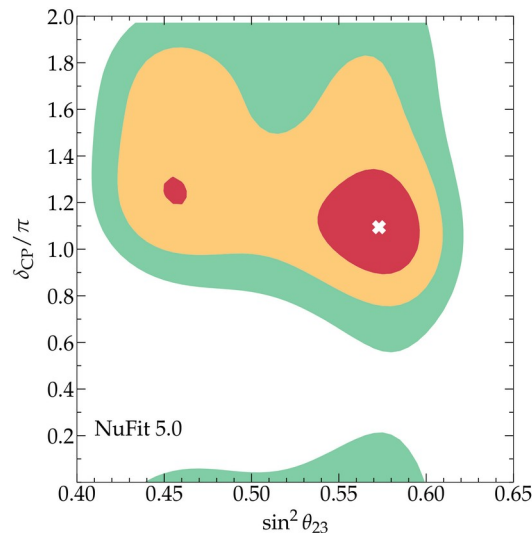
Fix at one of the benchmarks
(pion decay, muon-damped, neutron decay)

or

Explore all possible combinations

2020: Use χ^2 profiles from
the NuFit 5.0 global fit
(solar + atmospheric
+ reactor + accelerator)

Esteban *et al.*, *JHEP* 2020
www.nu-fit.org



Note:

The original palatable regions were
frequentist [MB, Beacom, Winter, *PRL* 2015];
the new ones are Bayesian

Flavor at the Earth: *theoretically palatable regions*

Theoretically palatable flavor regions

≡

MB, Beacom, Winter, *PRL* 2015

Allowed regions of flavor ratios at Earth derived from oscillations

Ingredient #1:

Flavor ratios at the source,

$$(f_{e,S}, f_{\mu,S}, f_{\tau,S})$$

Ingredient #2:

Probability density of mixing parameters $(\theta_{12}, \theta_{23}, \theta_{13}, \delta_{CP})$

Fix at one of the benchmarks
(pion decay, muon-damped, neutron decay)

or

Explore all possible combinations

Note:

The original palatable regions were frequentist [MB, Beacom, Winter, *PRL* 2015]; the new ones are Bayesian

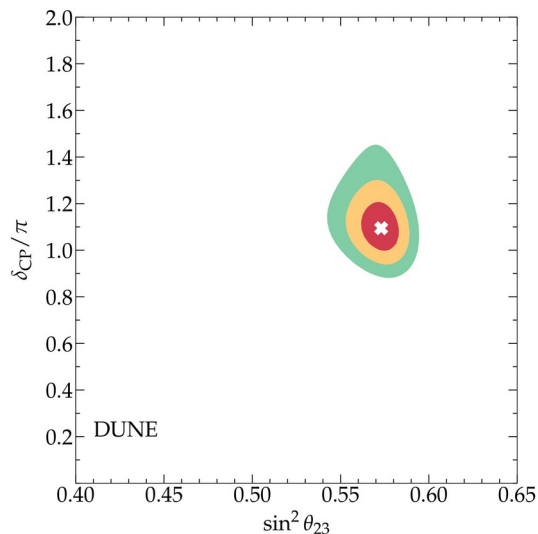
2020: Use χ^2 profiles from the NuFit 5.0 global fit (solar + atmospheric + reactor + accelerator)

Esteban *et al.*, *JHEP* 2020
www.nu-fit.org

Post-2020: Build our own profiles using simulations of JUNO, DUNE, Hyper-K

An *et al.*, *J. Phys. G* 2016
DUNE, 2002.03005

Huber, Lindner, Winter, *Nucl. Phys. B* 2002



One likely TeV–PeV ν production scenario:

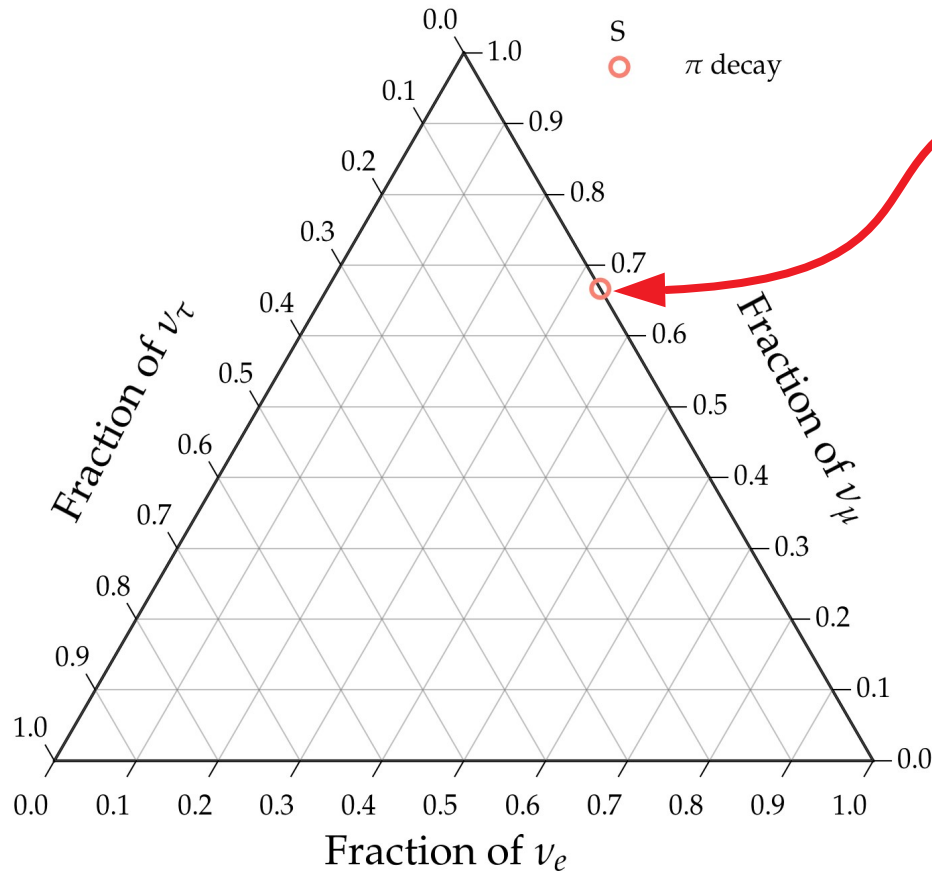
$$p + \gamma \rightarrow \pi^+ \rightarrow \mu^+ + \nu_\mu \text{ followed by } \mu^+ \rightarrow e^+ + \nu_e + \bar{\nu}_\mu$$

Full π decay chain

$$(1/3:2/3:0)_S$$

Note: ν and $\bar{\nu}$ are (so far) indistinguishable
in neutrino telescopes

One likely TeV–PeV ν production scenario:



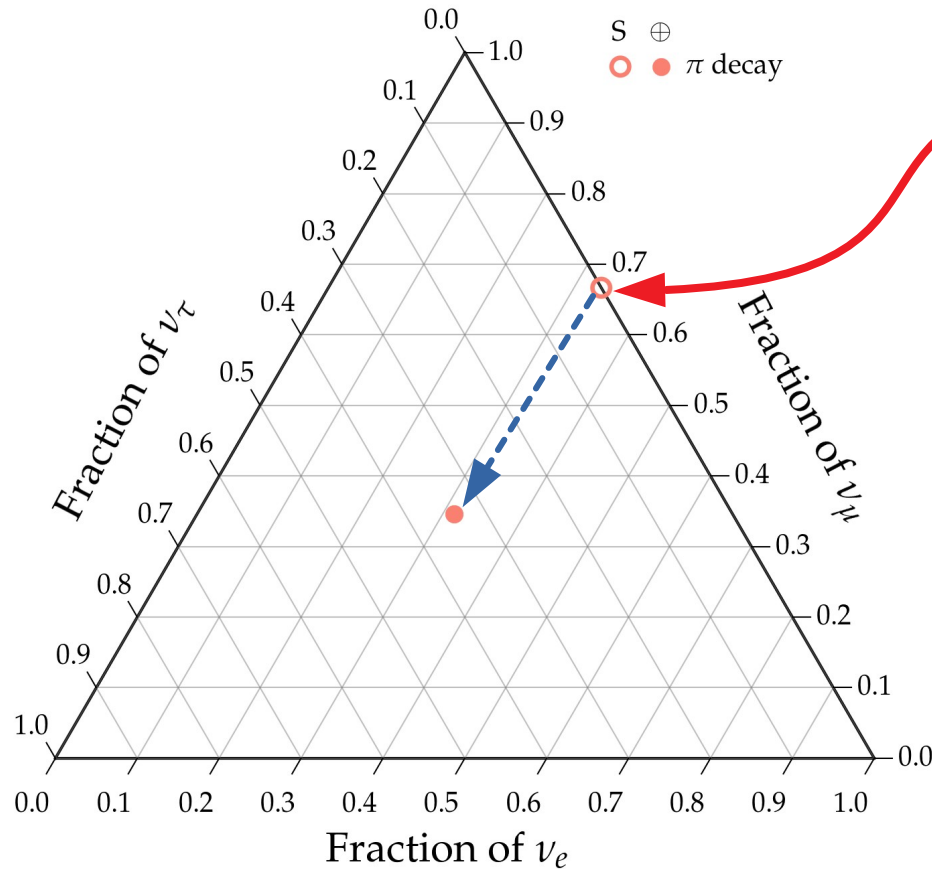
Full π decay chain

$(1/3:2/3:0)_S$

Note: ν and $\bar{\nu}$ are (so far) indistinguishable in neutrino telescopes

One likely TeV–PeV ν production scenario:

$p + \gamma \rightarrow \pi^+ \rightarrow \mu^+ + \nu_\mu$ followed by $\mu^+ \rightarrow e^+ + \nu_e + \bar{\nu}_\mu$

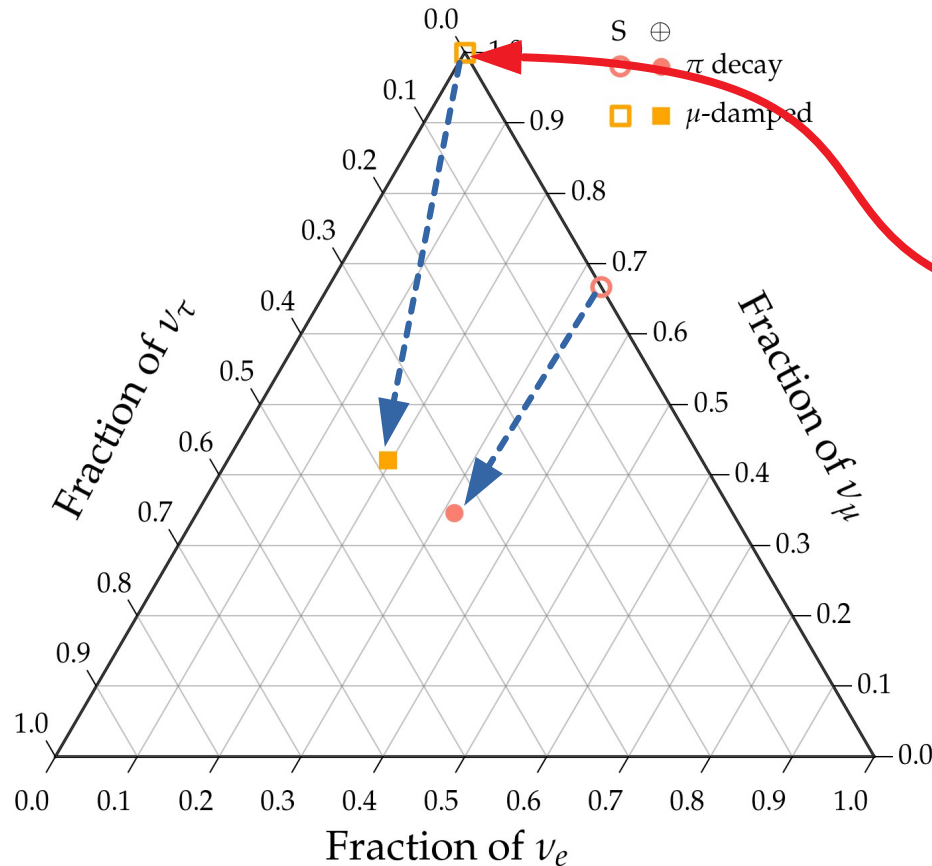


Full π decay chain

(1/3:2/3:0)_S

Note: ν and $\bar{\nu}$ are (so far) indistinguishable in neutrino telescopes

One likely TeV–PeV ν production scenario:



Full π decay chain

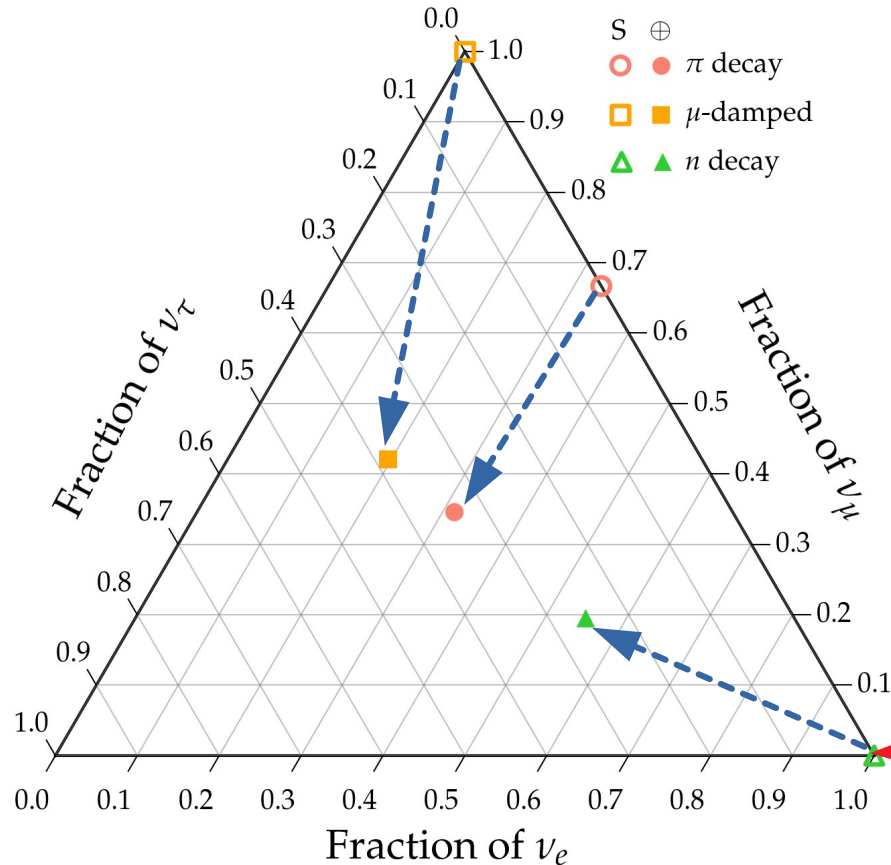
$(1/3:2/3:0)_S$

Muon damped

$(0:1:0)_S$

Note: ν and $\bar{\nu}$ are (so far) indistinguishable in neutrino telescopes

One likely TeV–PeV ν production scenario:



Full π decay chain

$(1/3:2/3:0)_S$

Muon damped

$(0:1:0)_S$

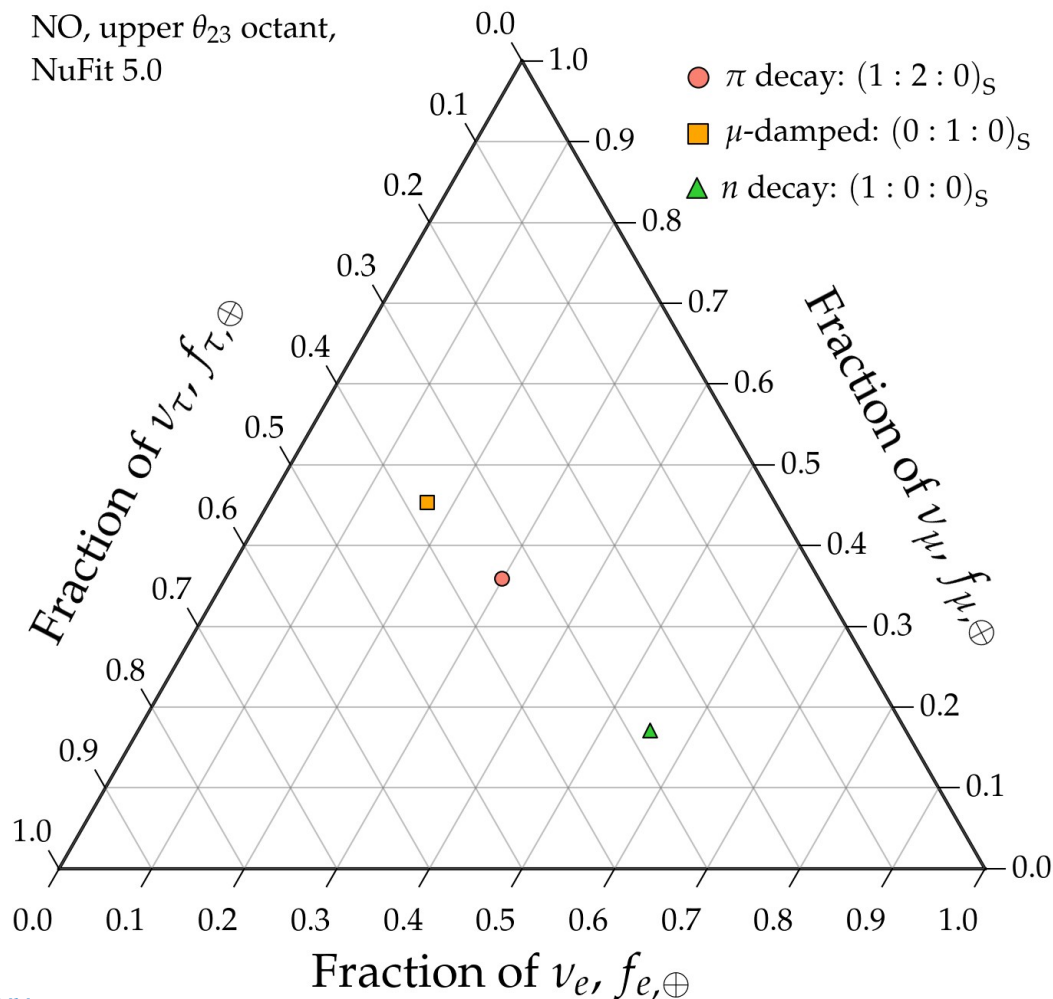
Neutron decay

$(1:0:0)_S$

Note: ν and $\bar{\nu}$ are (so far) indistinguishable in neutrino telescopes

Theoretically palatable regions: today (2020)

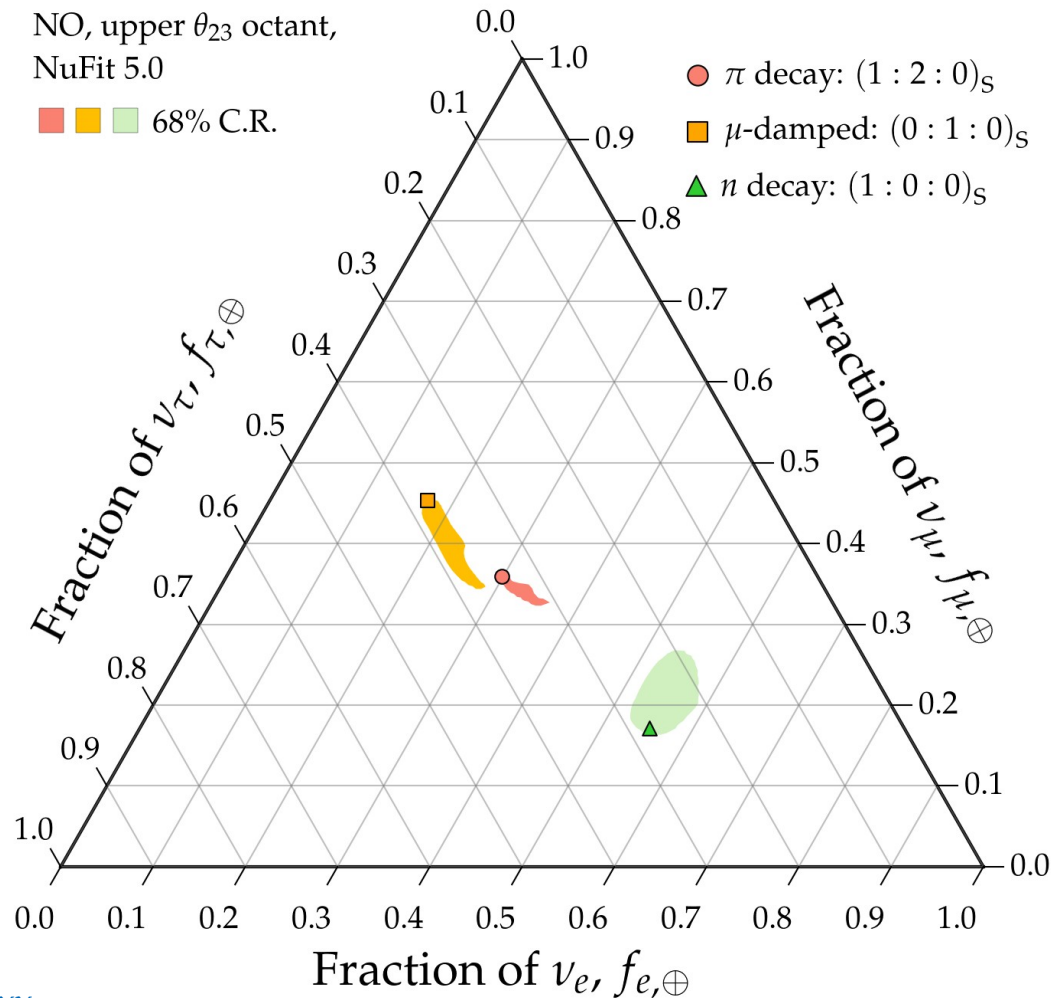
NO, upper θ_{23} octant,
NuFit 5.0



Note:

All plots shown are for normal
neutrino mass ordering (NO);
inverted ordering looks similar

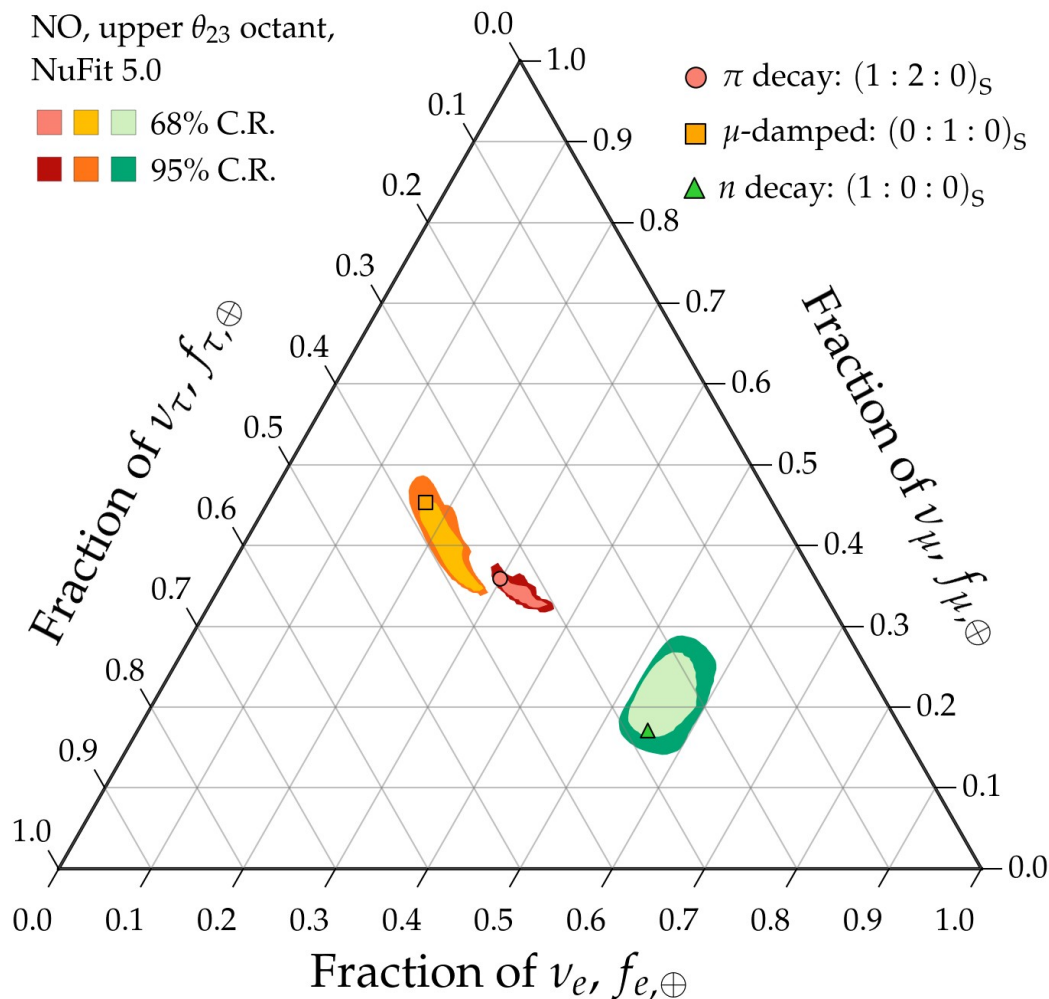
Theoretically palatable regions: today (2020)



Note:

All plots shown are for normal
neutrino mass ordering (NO);
inverted ordering looks similar

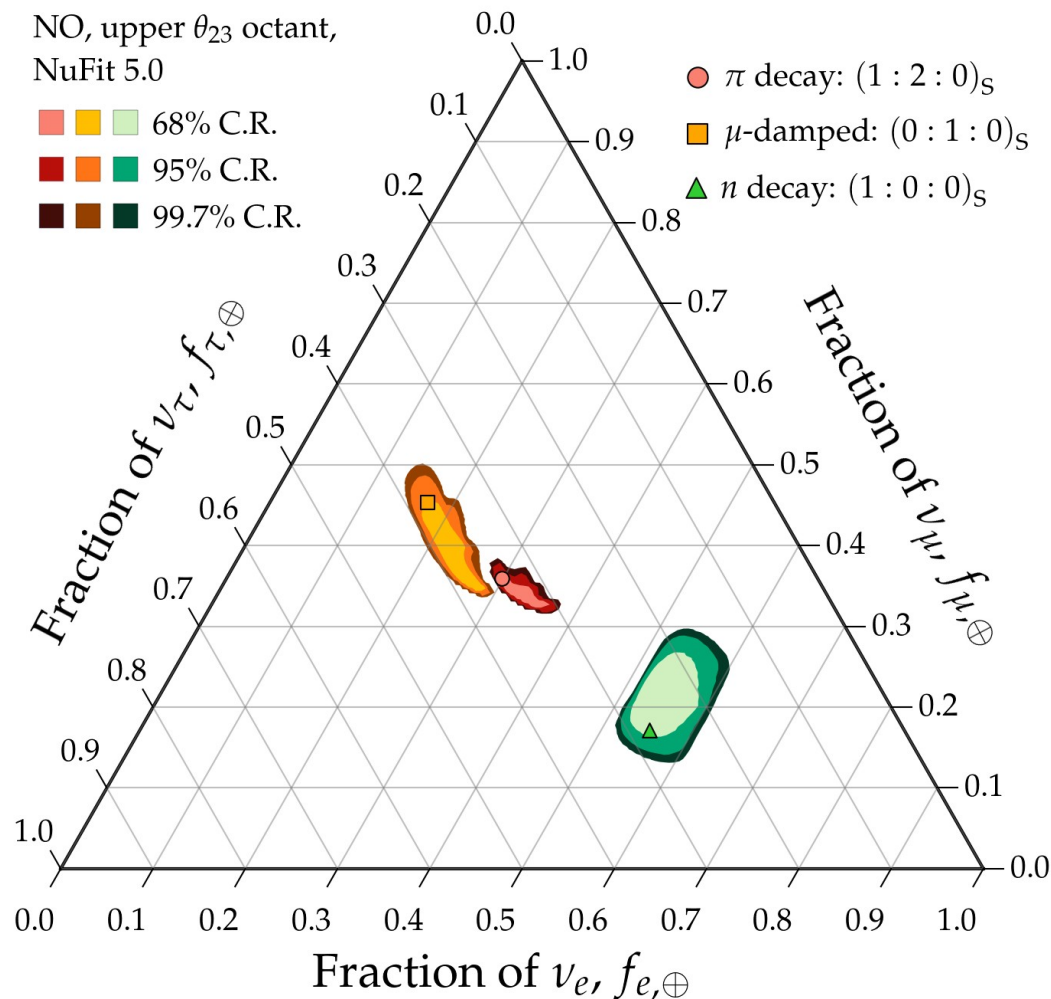
Theoretically palatable regions: today (2020)



Note:

All plots shown are for normal
neutrino mass ordering (NO);
inverted ordering looks similar

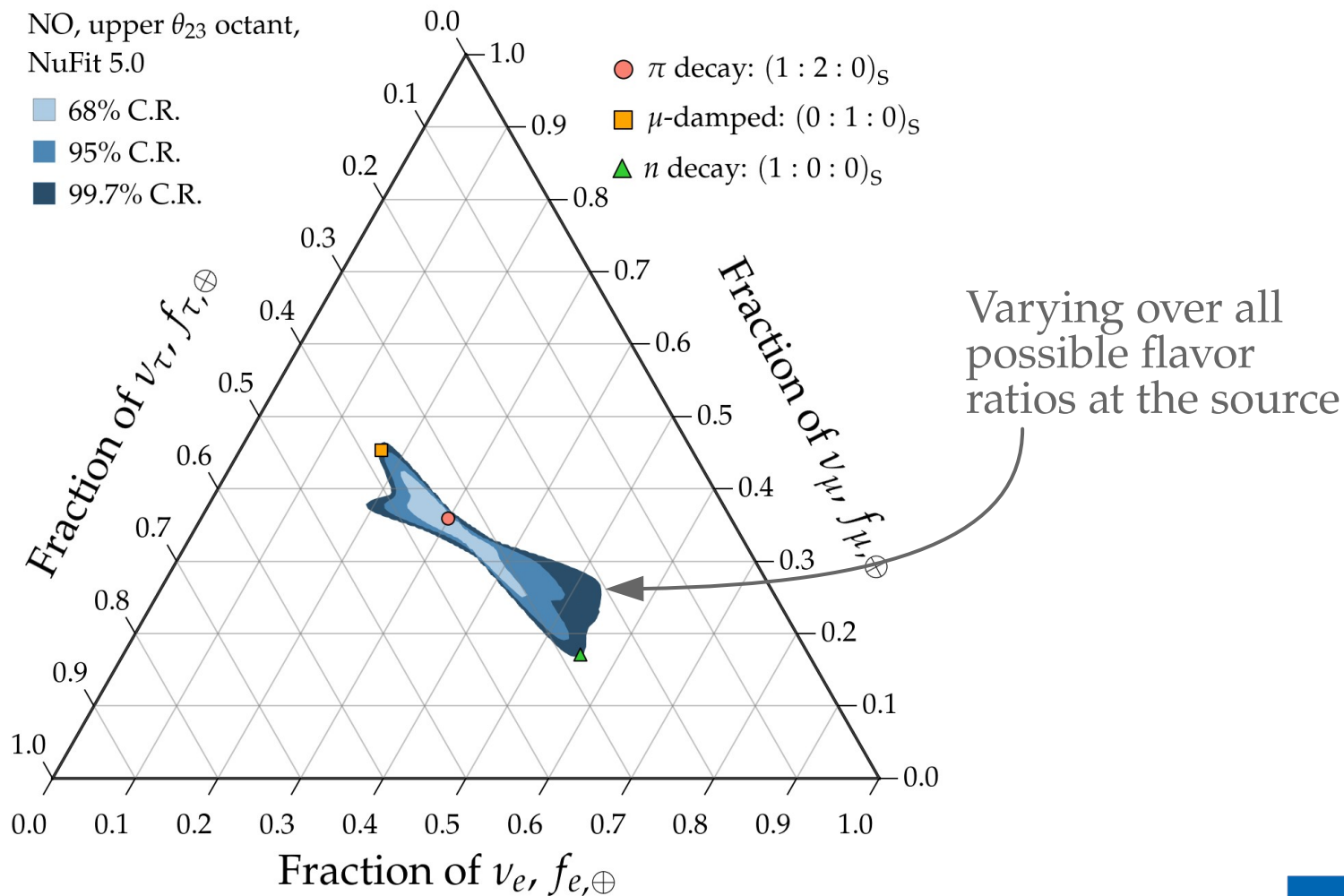
Theoretically palatable regions: today (2020)



Note:

All plots shown are for normal
neutrino mass ordering (NO);
inverted ordering looks similar

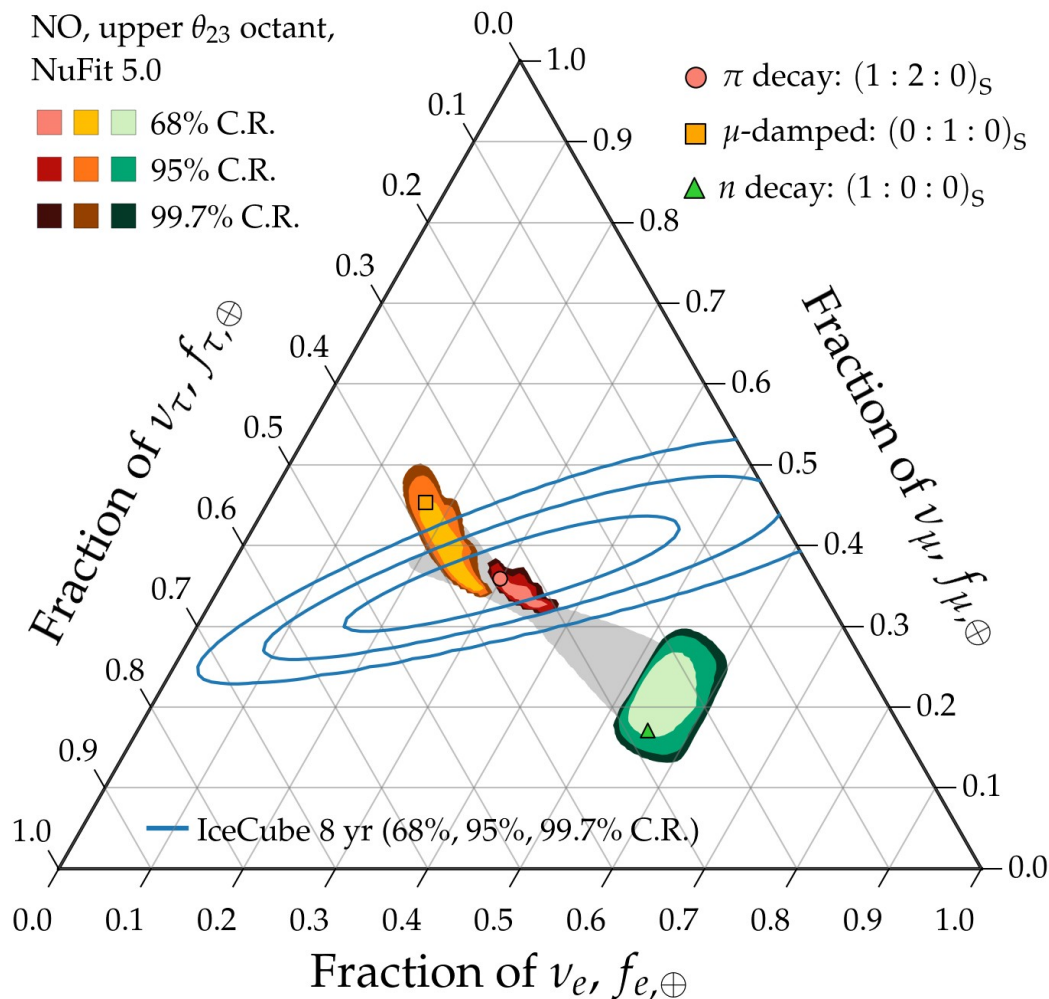
Theoretically palatable regions: today (2020)



Note:

All plots shown are for normal neutrino mass ordering (NO);
inverted ordering looks similar

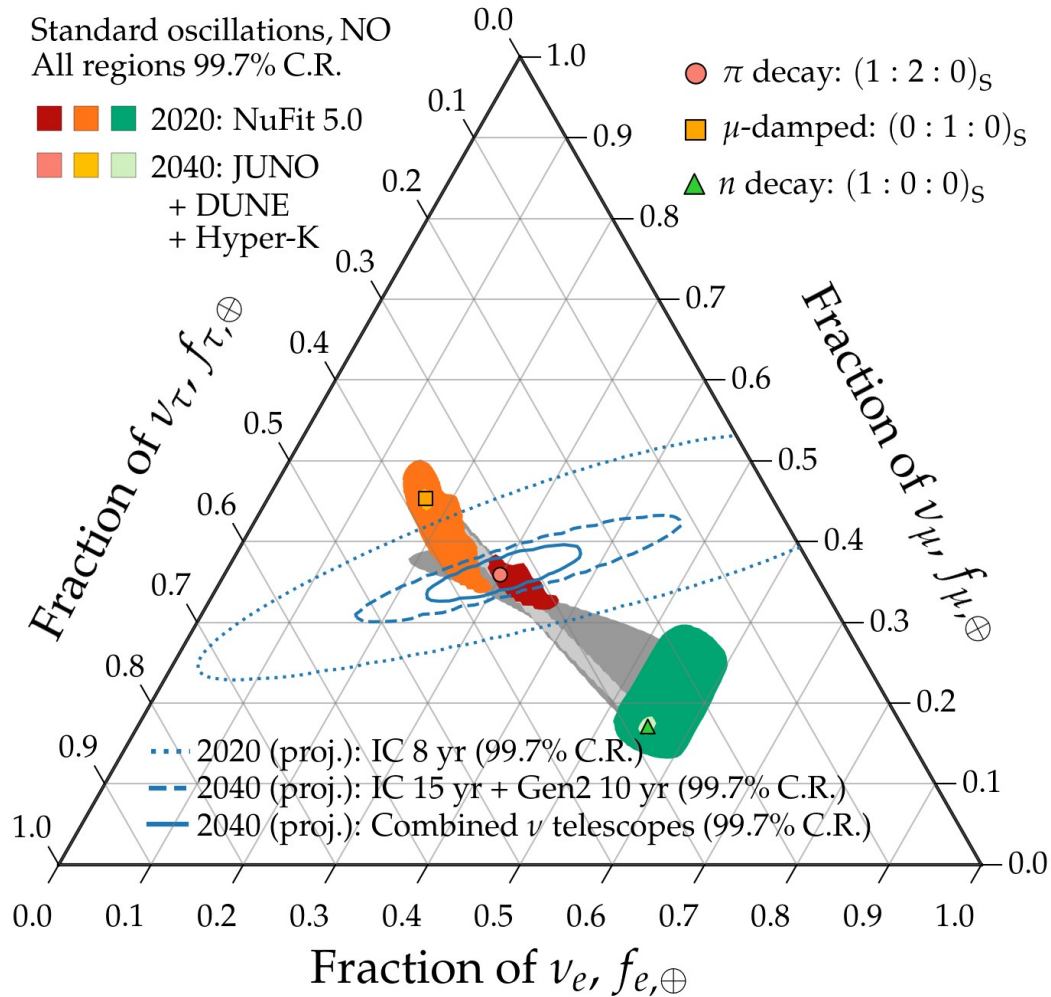
Theoretically palatable regions: today (2020)



Note:

All plots shown are for normal
neutrino mass ordering (NO);
inverted ordering looks similar

Theoretically palatable regions: 2020 *vs.* 2040



By 2040:

Theory –

Mixing parameters known
precisely: allowed flavor regions
are *almost* points (already by 2030)

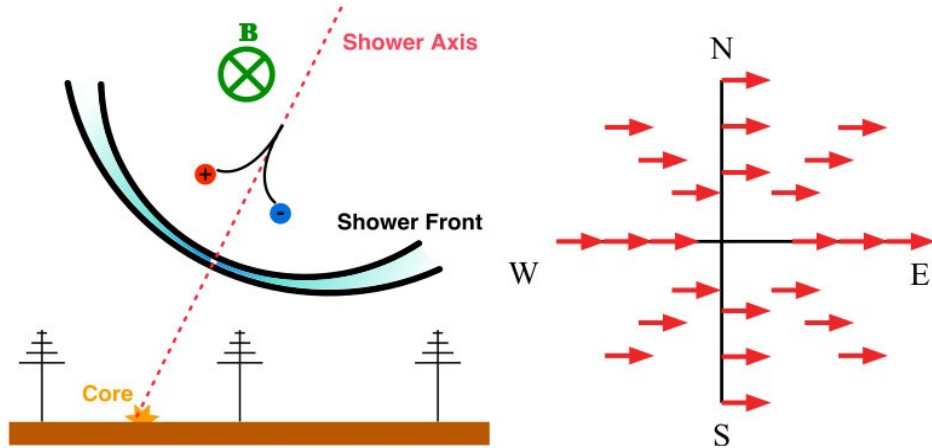
Measurement of flavor ratios –

Can distinguish between similar
predictions at 99.7% C.R. (3σ)

*Can finally use the full power of
flavor composition for astrophysics
and neutrino physics*

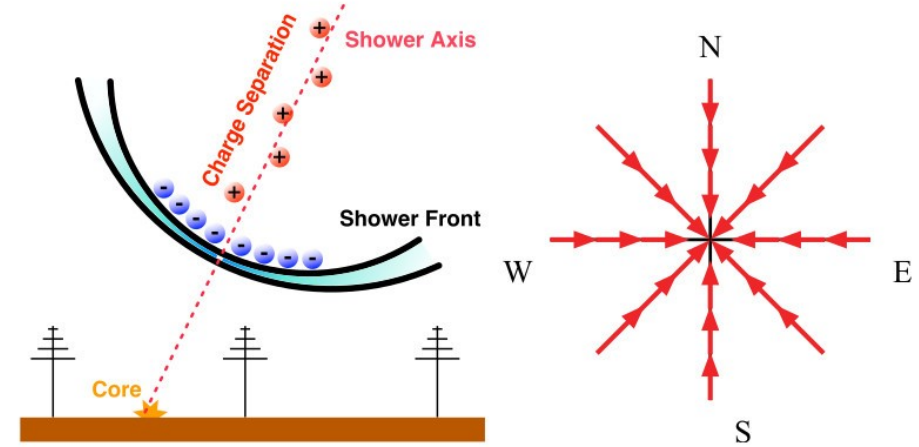
Radio emission: geomagnetic and Askaryan

Geomagnetic



- ▶ Time-varying transverse current
- ▶ Linearly polarized parallel to Lorentz force
- ▶ Dominant in air showers

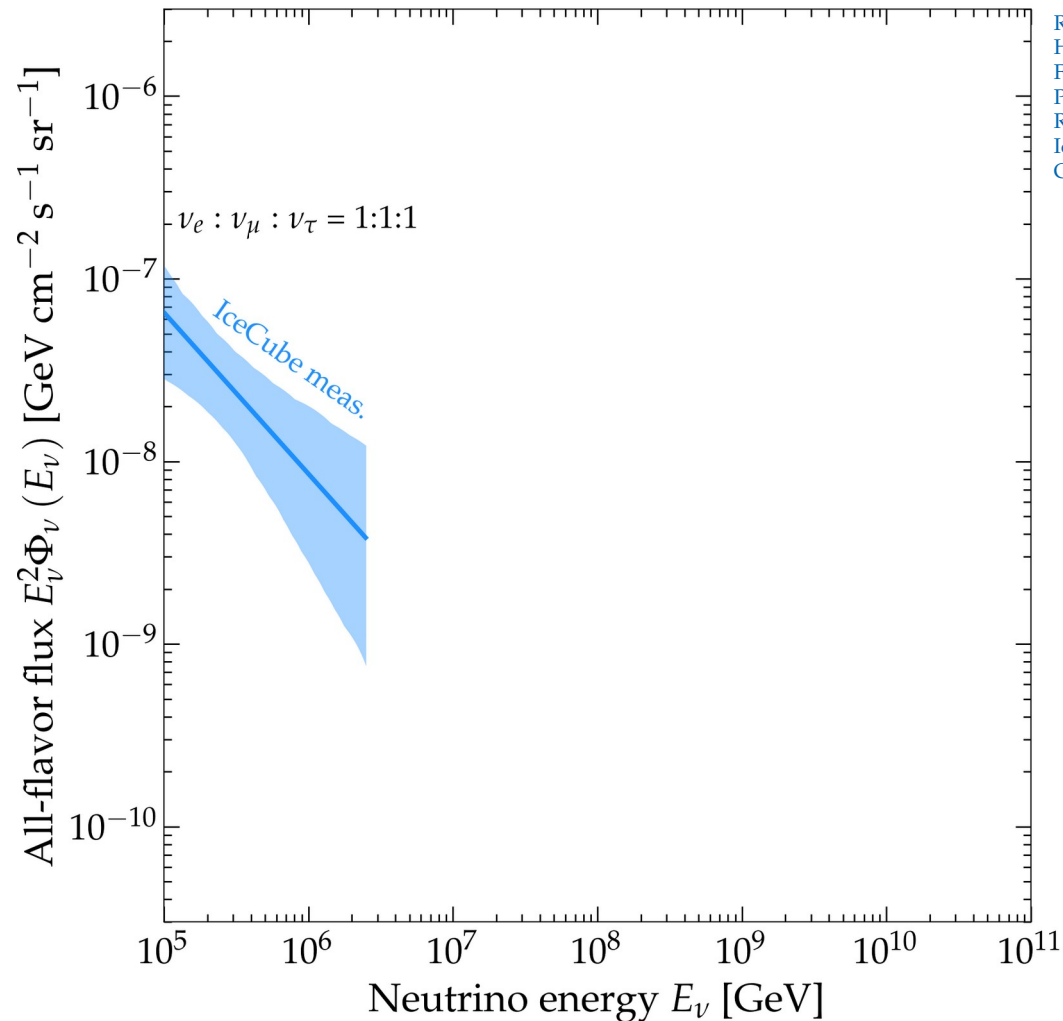
Askaryan



- ▶ Time-varying negative-charge ~20% excess
- ▶ Linearly polarized towards axis
- ▶ Sub-dominant in air showers

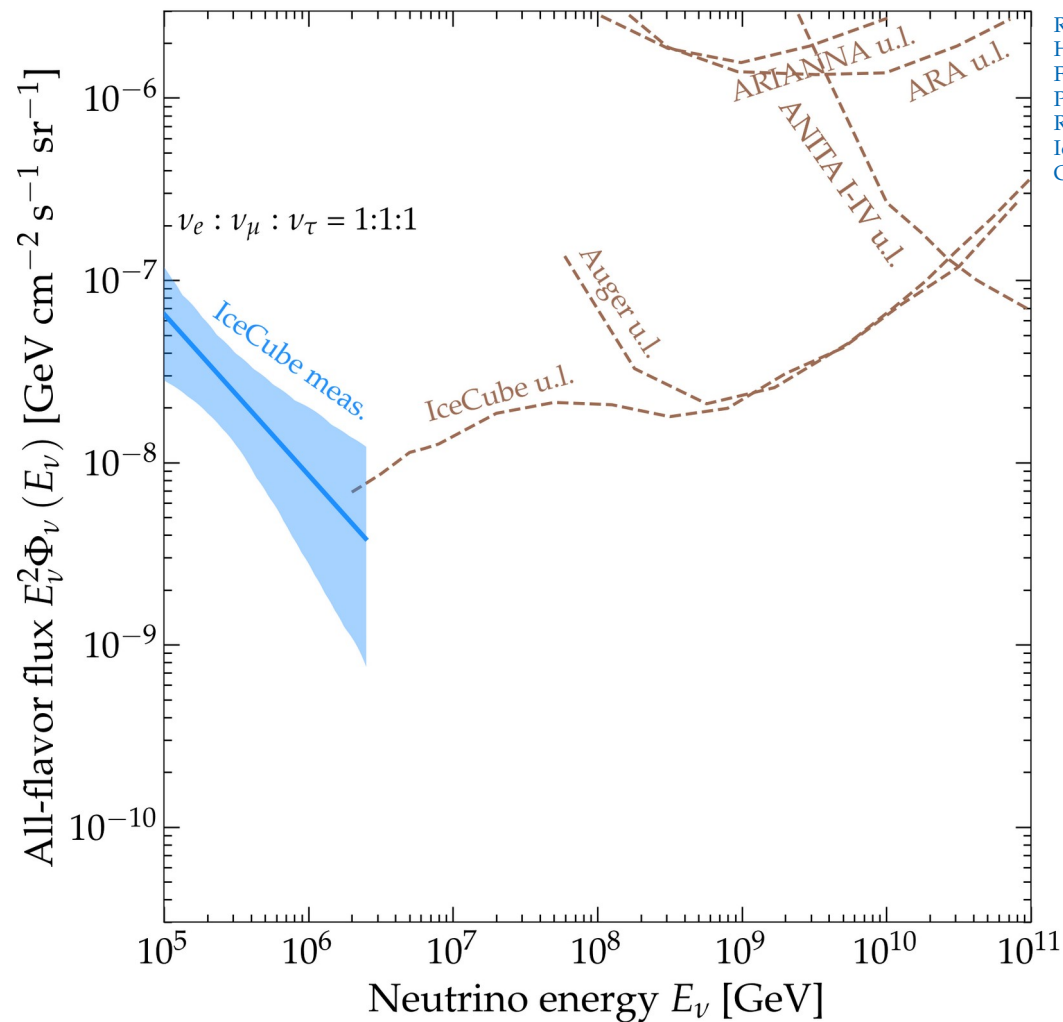
Radio emission: geomagnetic and Askaryan

UHE neutrinos: *steady-state sources*



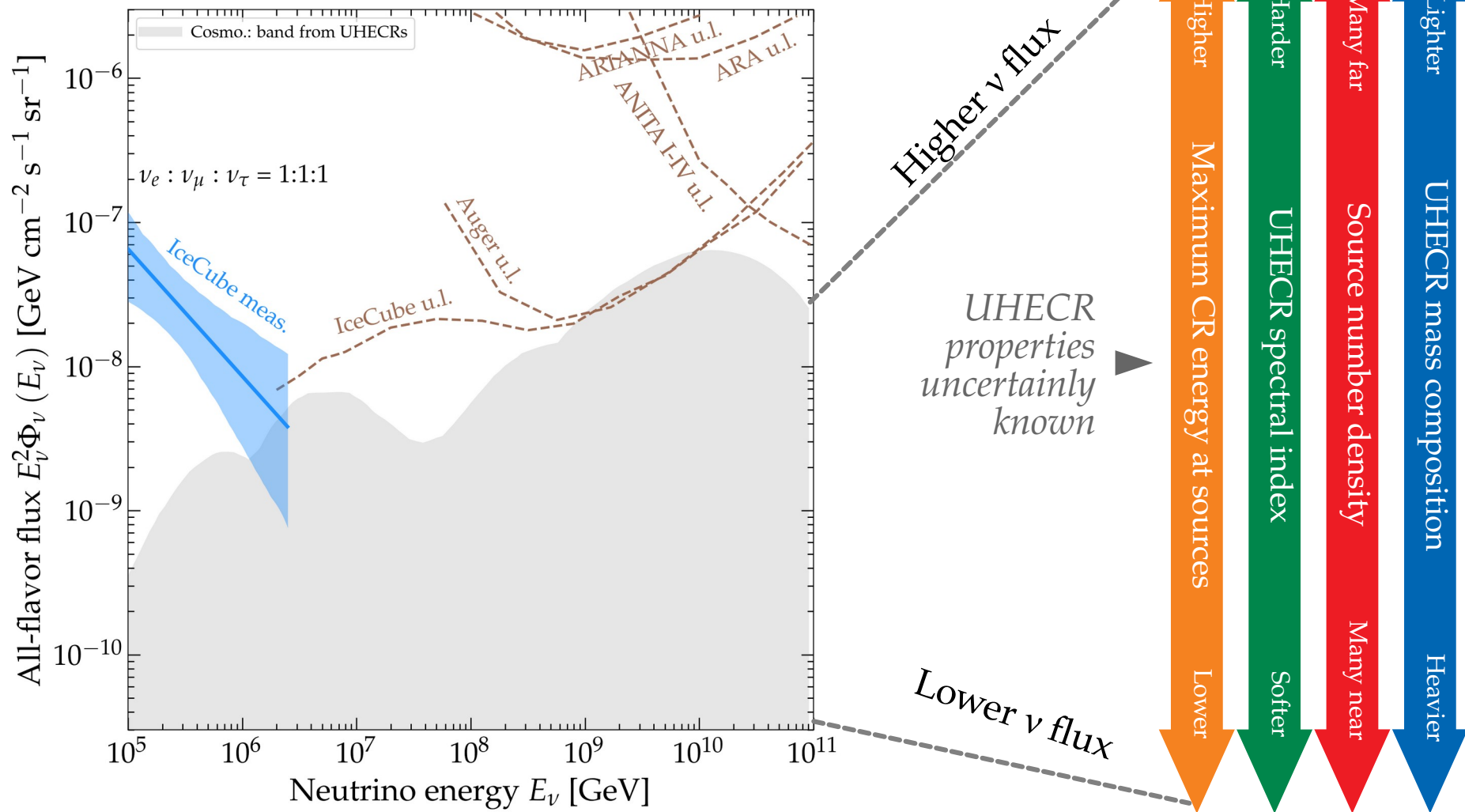
Rodrigues, Heinze, Palladino, van Vliet, Winter, 2003.08392
Heinze, Fedynitch, Boncioli, Winter *ApJ* 2019
Fang & Murase, *Nature Phys.* 2018
POEMMA, 2012.07945
RNO-G, *JINST* 2021
IceCube-Gen2, *J. Phys. G* 2021
GRAND, *Sci. China Phys. Mech. Astron.* 2020

UHE neutrinos: *steady-state sources*

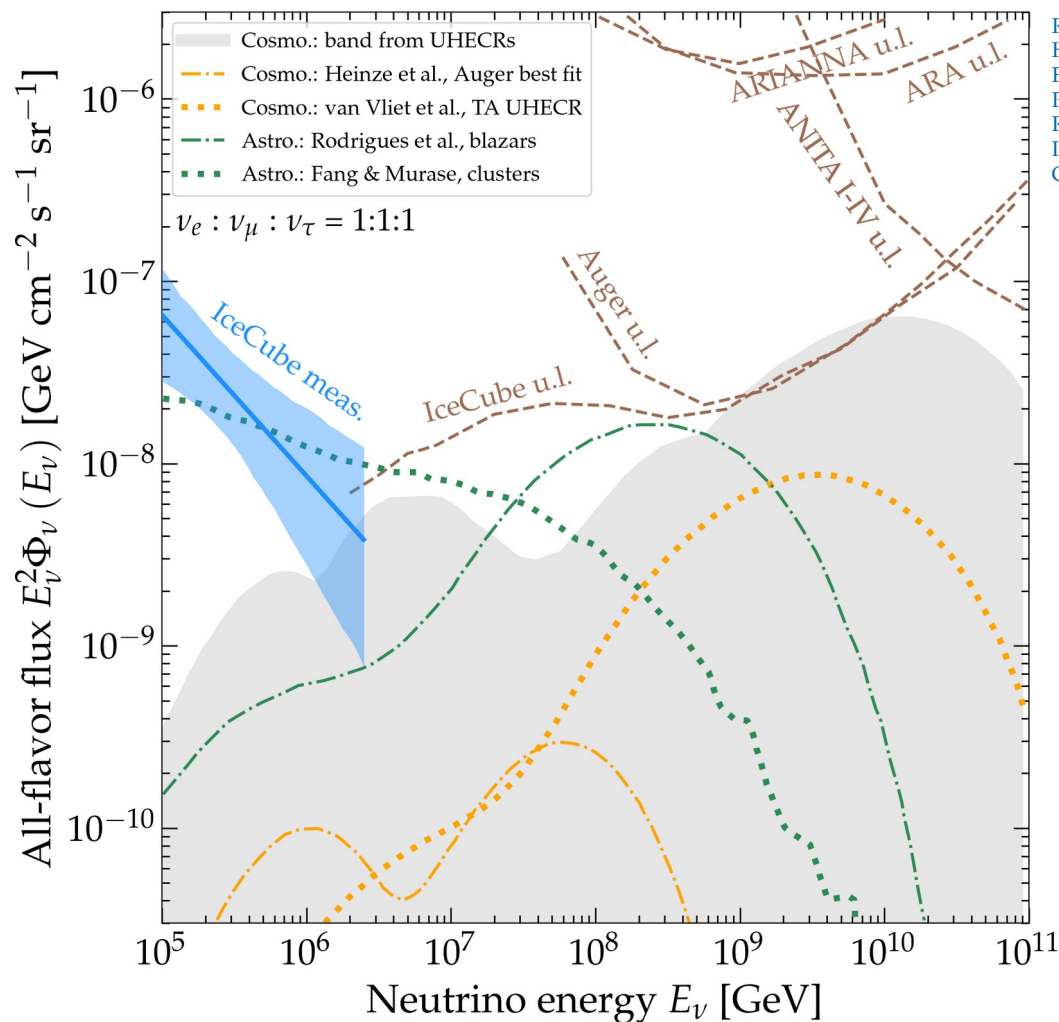


Rodrigues, Heinze, Palladino, van Vliet, Winter, 2003.08392
Heinze, Fedynitch, Boncioli, Winter *ApJ* 2019
Fang & Murase, *Nature Phys.* 2018
POEMMA, 2012.07945
RNO-G, *JINST* 2021
IceCube-Gen2, *J. Phys. G* 2021
GRAND, *Sci. China Phys. Mech. Astron.* 2020

UHE neutrinos: *steady-state sources*

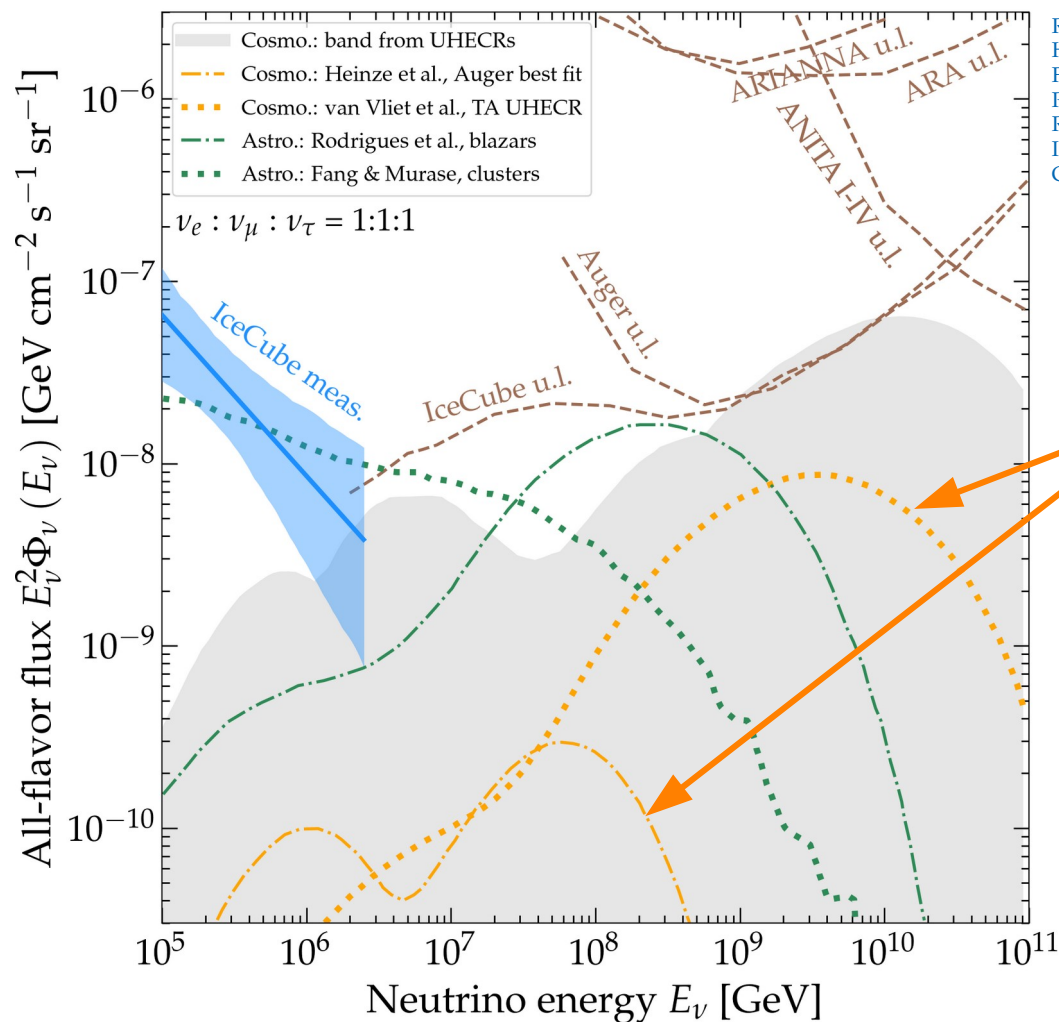


UHE neutrinos: *steady-state sources*



Rodrigues, Heinze, Palladino, van Vliet, Winter, 2003.08392
 Heinze, Fedynitch, Boncioli, Winter *ApJ* 2019
 Fang & Murase, *Nature Phys.* 2018
 POEMMA, 2012.07945
 RNO-G, *JINST* 2021
 IceCube-Gen2, *J. Phys. G* 2021
 GRAND, *Sci. China Phys. Mech. Astron.* 2020

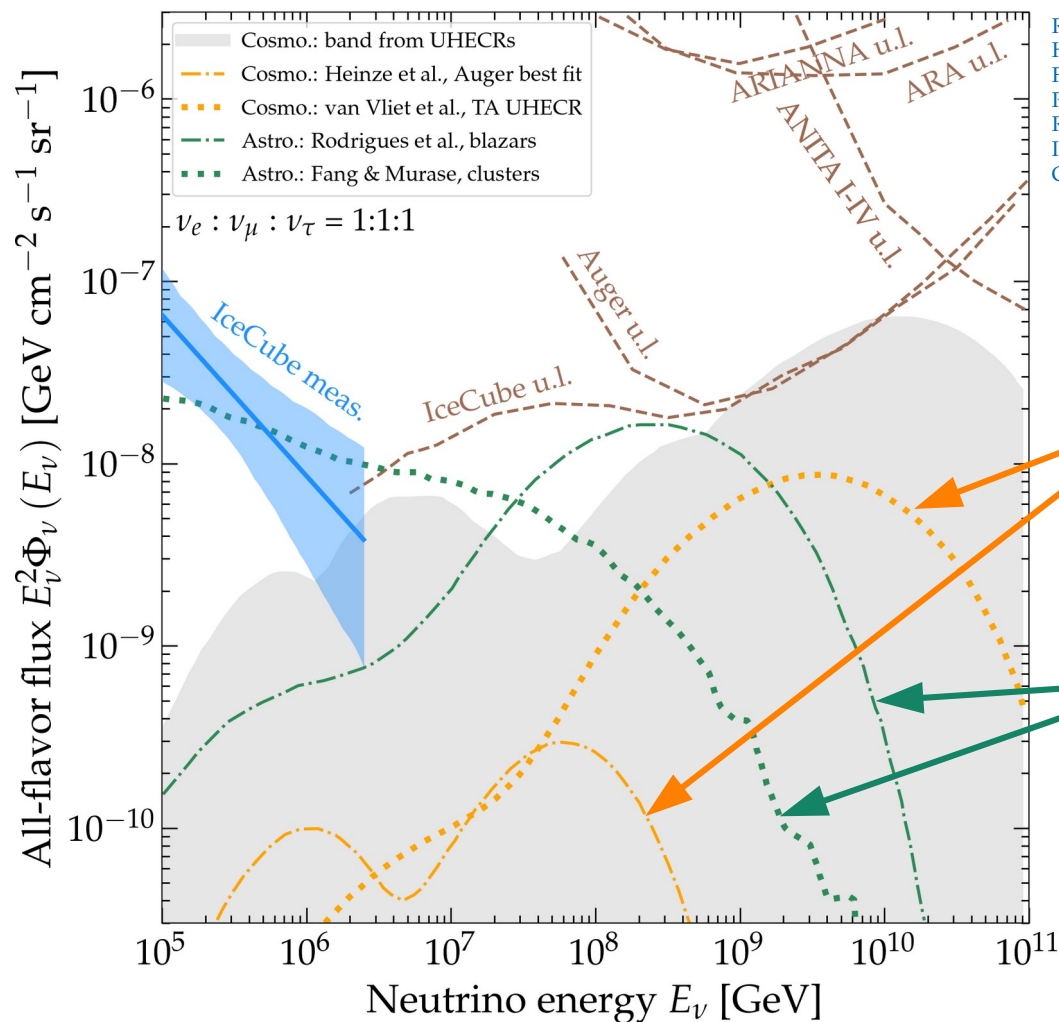
UHE neutrinos: *steady-state sources*



Rodrigues, Heinze, Palladino, van Vliet, Winter, 2003.08392
 Heinze, Fedynitch, Boncioli, Winter *ApJ* 2019
 Fang & Murase, *Nature Phys.* 2018
 POEMMA, 2012.07945
 RNO-G, *JINST* 2021
 IceCube-Gen2, *J. Phys. G* 2021
 GRAND, *Sci. China Phys. Mech. Astron.* 2020

Cosmogenic neutrinos

UHE neutrinos: *steady-state sources*

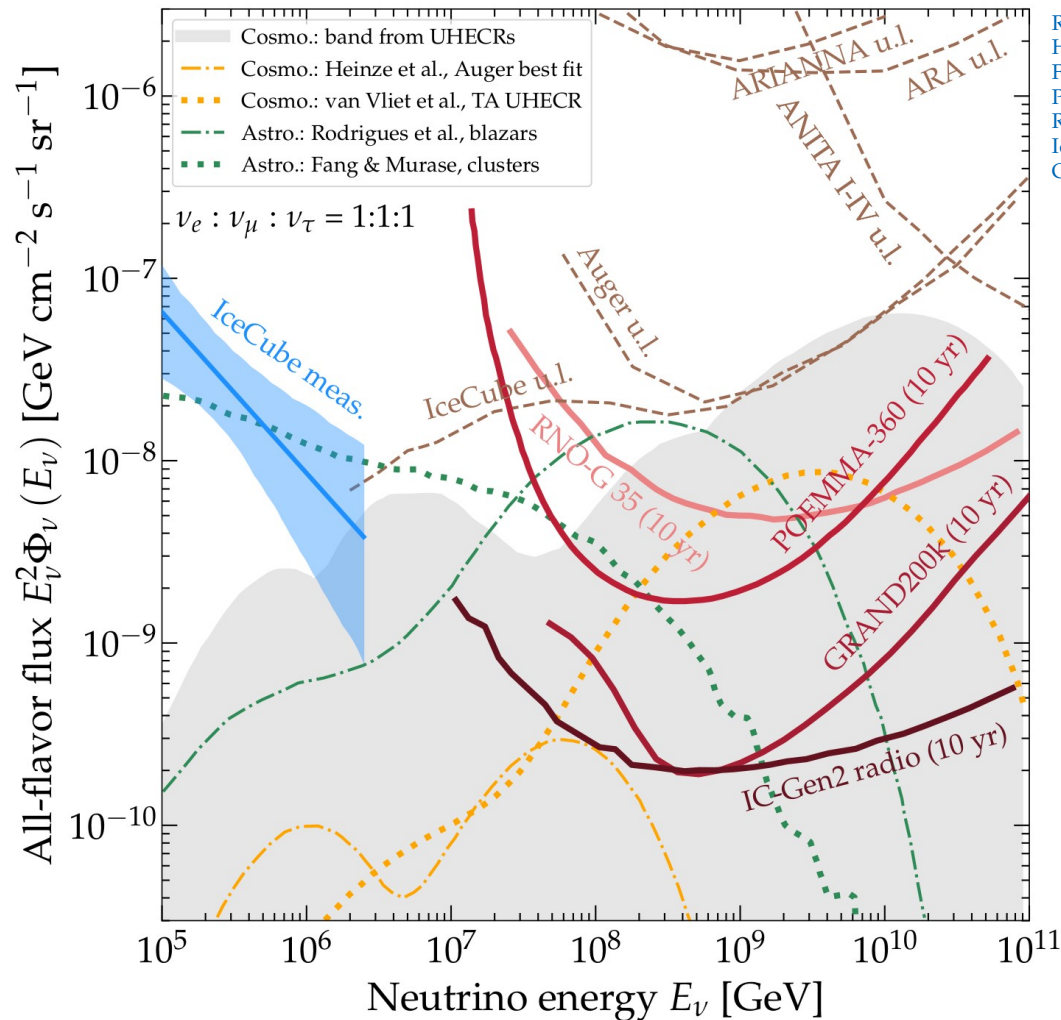


Rodrigues, Heinze, Palladino, van Vliet, Winter, 2003.08392
Heinze, Fedynitch, Boncioli, Winter *ApJ* 2019
Fang & Murase, *Nature Phys.* 2018
POEMMA, 2012.07945
RNO-G, *JINST* 2021
IceCube-Gen2, *J. Phys. G* 2021
GRAND, *Sci. China Phys. Mech. Astron.* 2020

Cosmogenic neutrinos

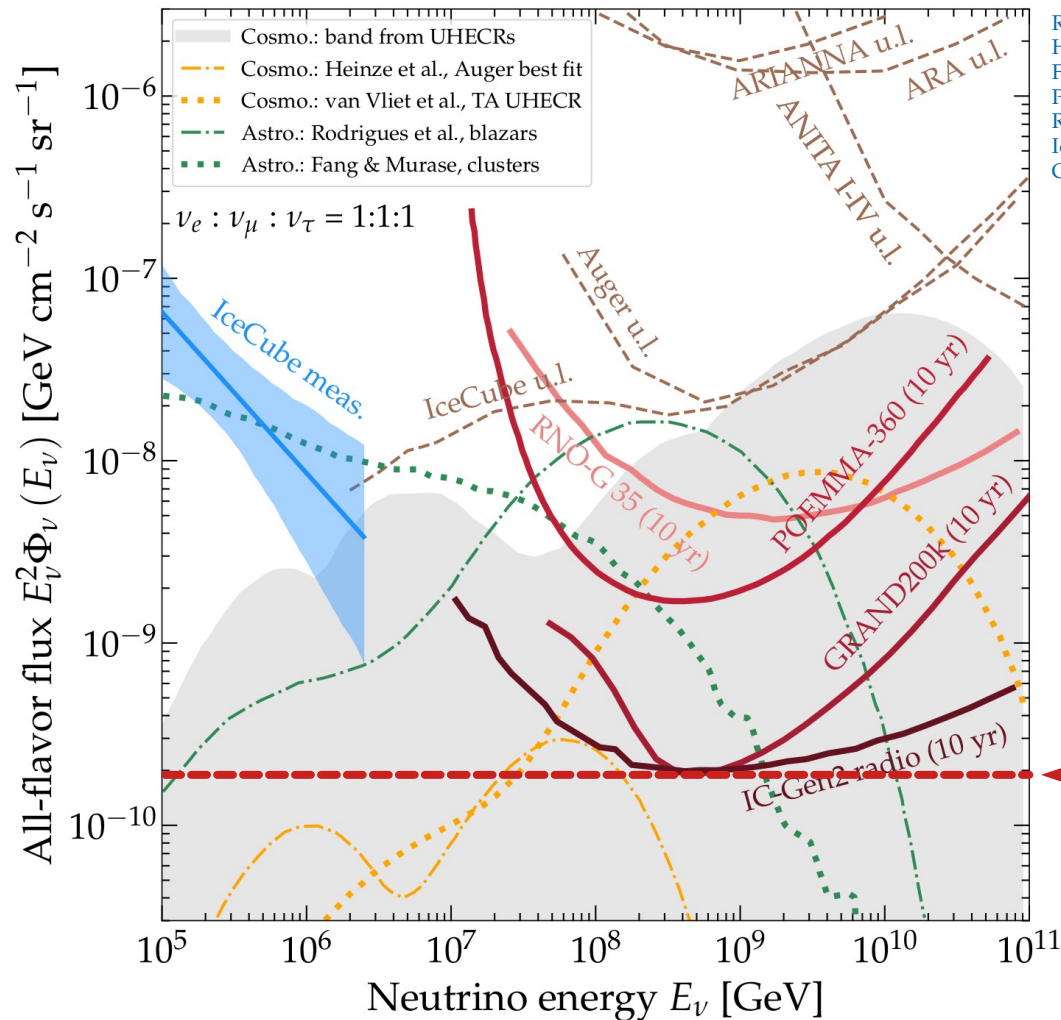
Neutrinos from the sources
(possibly dominant flux!)

UHE neutrinos: *steady-state sources*



Rodrigues, Heinze, Palladino, van Vliet, Winter, 2003.08392
 Heinze, Fedynitch, Boncioli, Winter *ApJ* 2019
 Fang & Murase, *Nature Phys.* 2018
 POEMMA, 2012.07945
 RNO-G, *JINST* 2021
 IceCube-Gen2, *J. Phys. G* 2021
 GRAND, *Sci. China Phys. Mech. Astron.* 2020

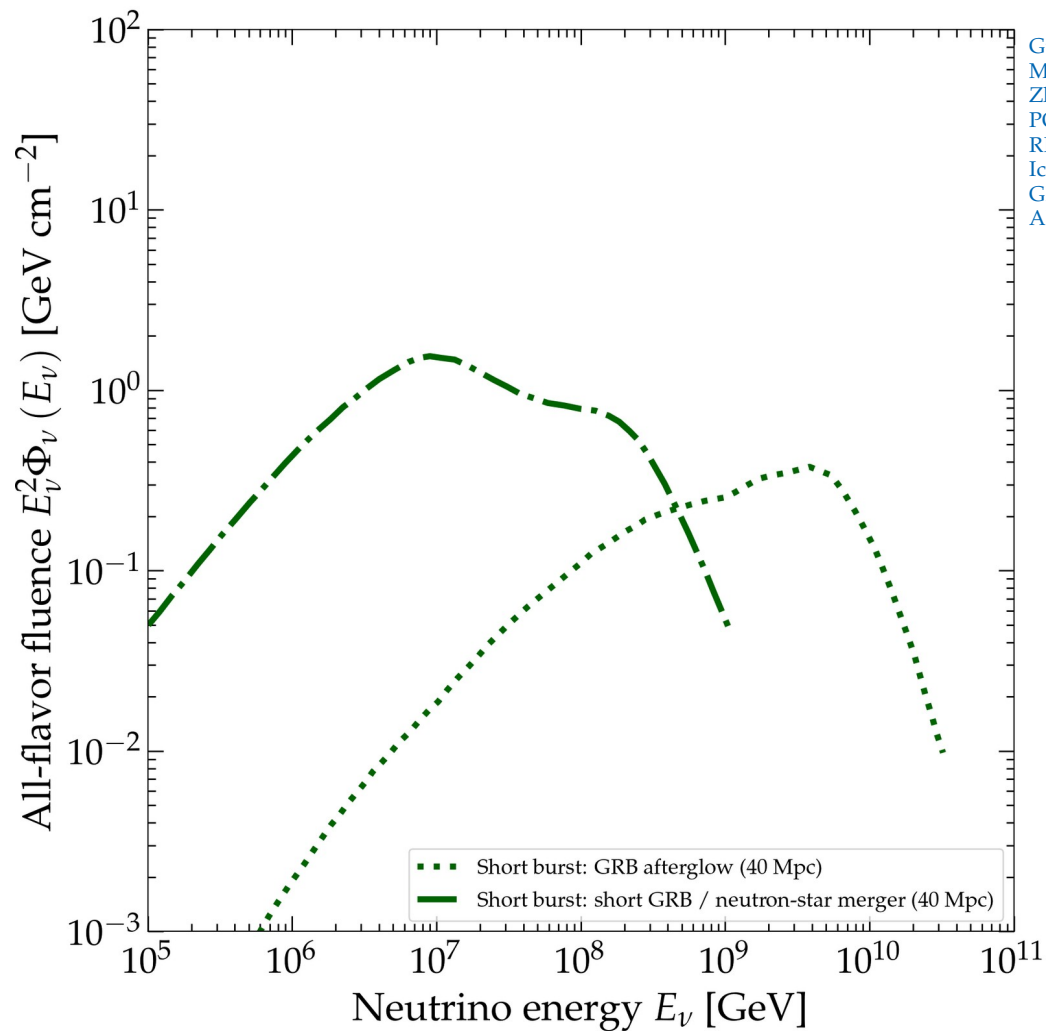
UHE neutrinos: *steady-state sources*



Rodrigues, Heinze, Palladino, van Vliet, Winter, 2003.08392
 Heinze, Fedynitch, Boncioli, Winter *ApJ* 2019
 Fang & Murase, *Nature Phys.* 2018
 POEMMA, 2012.07945
 RNO-G, *JINST* 2021
 IceCube-Gen2, *J. Phys. G* 2021
 GRAND, *Sci. China Phys. Mech. Astron.* 2020

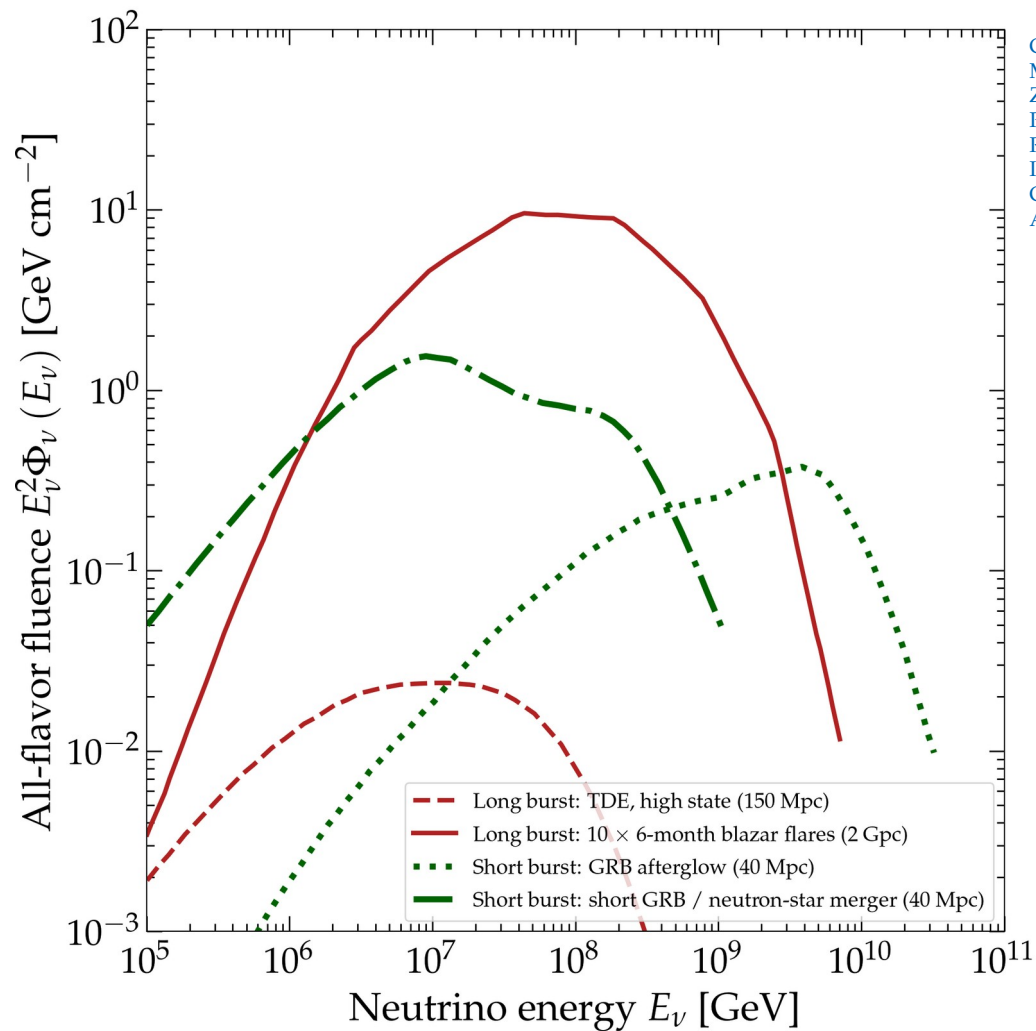
Ultimate target sensitivity
 for next-gen detectors
 (if protons are ~10% of the
 highest-energy UHECRs)

UHE neutrinos: *transient sources*



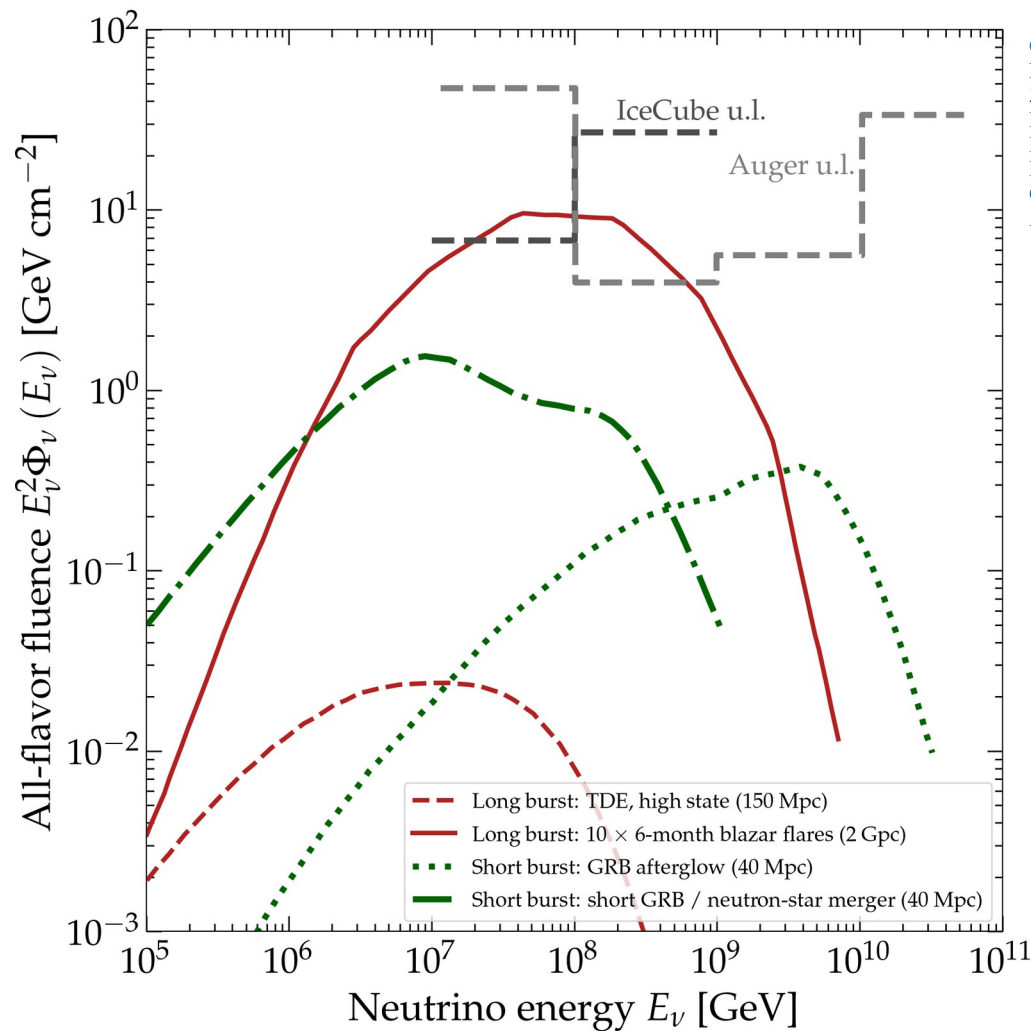
Guépin, Kotera, Barausse, Fang, Murase, *A&A* 2018
Murase, *PRD* 2017
Zhang *et al.*, *Nature Commun.* 2018
POEMMA, 2012.07945
RNO-G, *JINST* 2021
IceCube-Gen2, *J. Phys. G* 2021
GRAND, *Sci. China Phys. Mech. Astron.* 2020
ANTARES, IceCube, Auger, LIGO, Virgo, *ApJ* 2017

UHE neutrinos: *transient sources*



Guépin, Kotera, Barausse, Fang, Murase, *A&A* 2018
Murase, *PRD* 2017
Zhang *et al.*, *Nature Commun.* 2018
POEMMA, 2012.07945
RNO-G, *JINST* 2021
IceCube-Gen2, *J. Phys. G* 2021
GRAND, *Sci. China Phys. Mech. Astron.* 2020
ANTARES, IceCube, Auger, LIGO, Virgo, *ApJ* 2017

UHE neutrinos: *transient sources*



Guépin, Kotera, Barausse, Fang, Murase, *A&A* 2018
Murase, *PRD* 2017
Zhang *et al.*, *Nature Commun.* 2018
POEMMA, 2012.07945
RNO-G, *JINST* 2021
IceCube-Gen2, *J. Phys. G* 2021
GRAND, *Sci. China Phys. Mech. Astron.* 2020
ANTARES, IceCube, Auger, LIGO, Virgo, *ApJ* 2017

