

# Pushing Neutrino Physics to the Cosmic Frontier

Mauricio Bustamante

Niels Bohr Institute, University of Copenhagen

TTK Theory Seminar, RWTH Aachen  
November 21, 2019

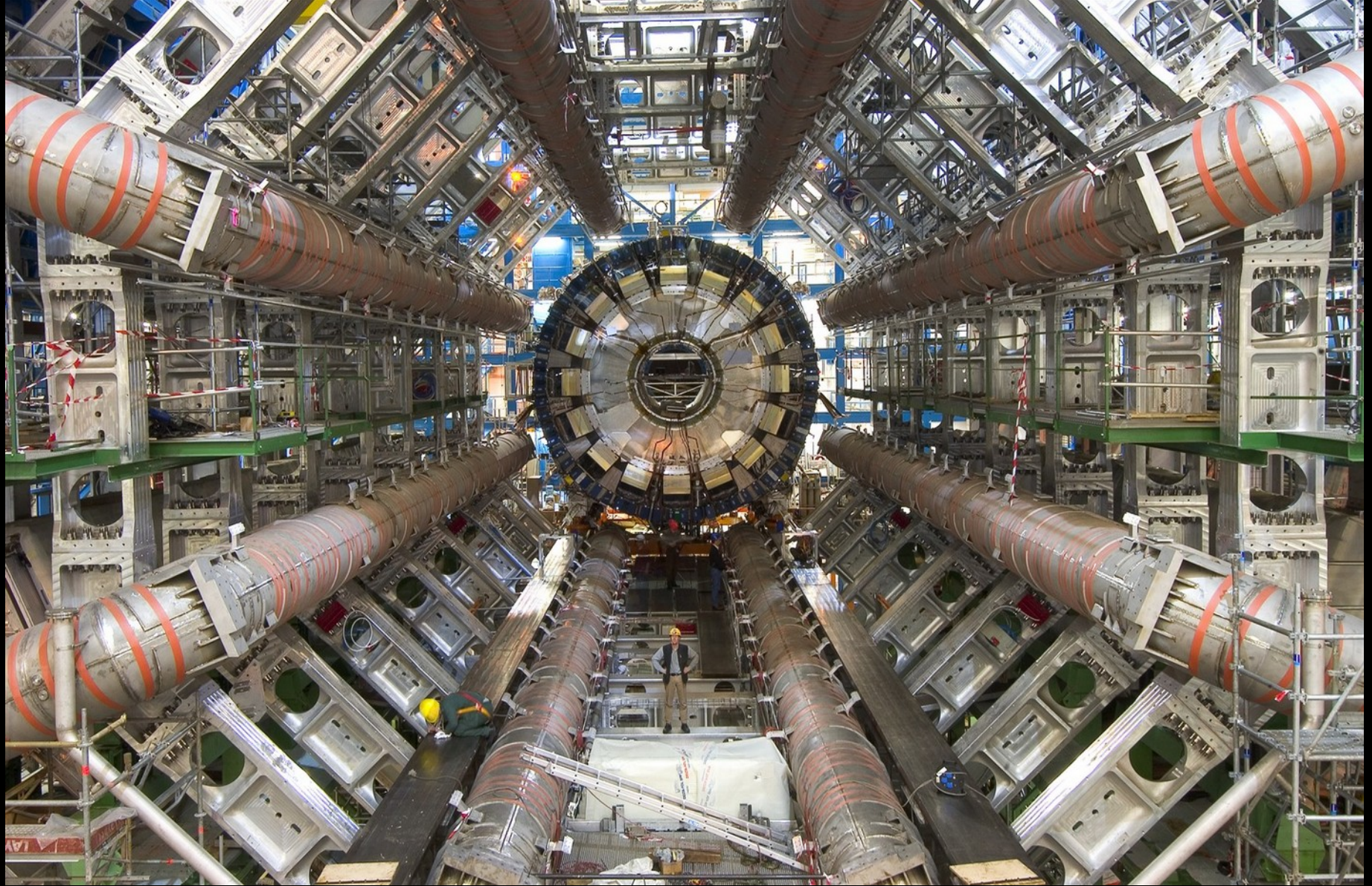
UNIVERSITY OF  
COPENHAGEN



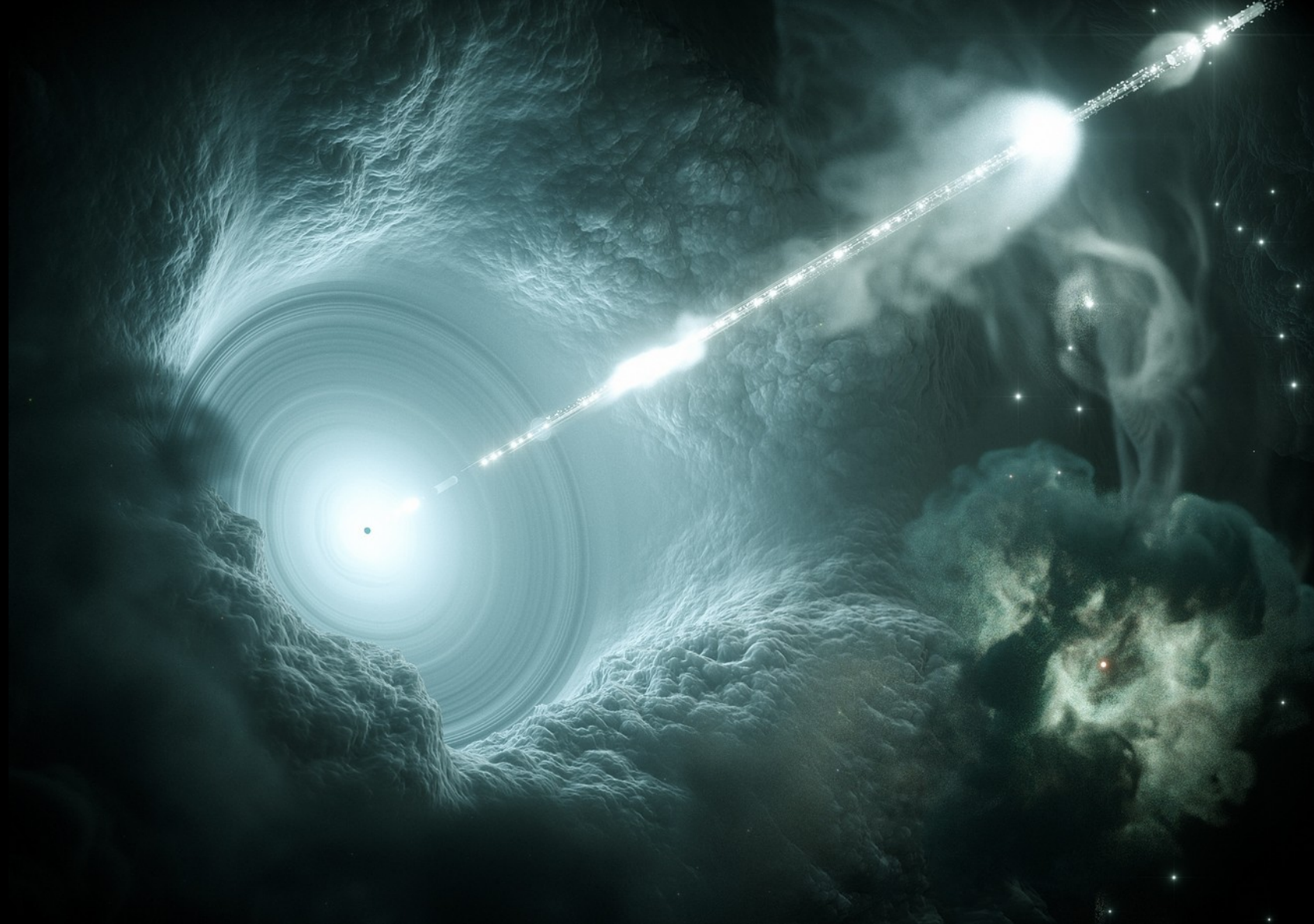
VILLUM FONDEN

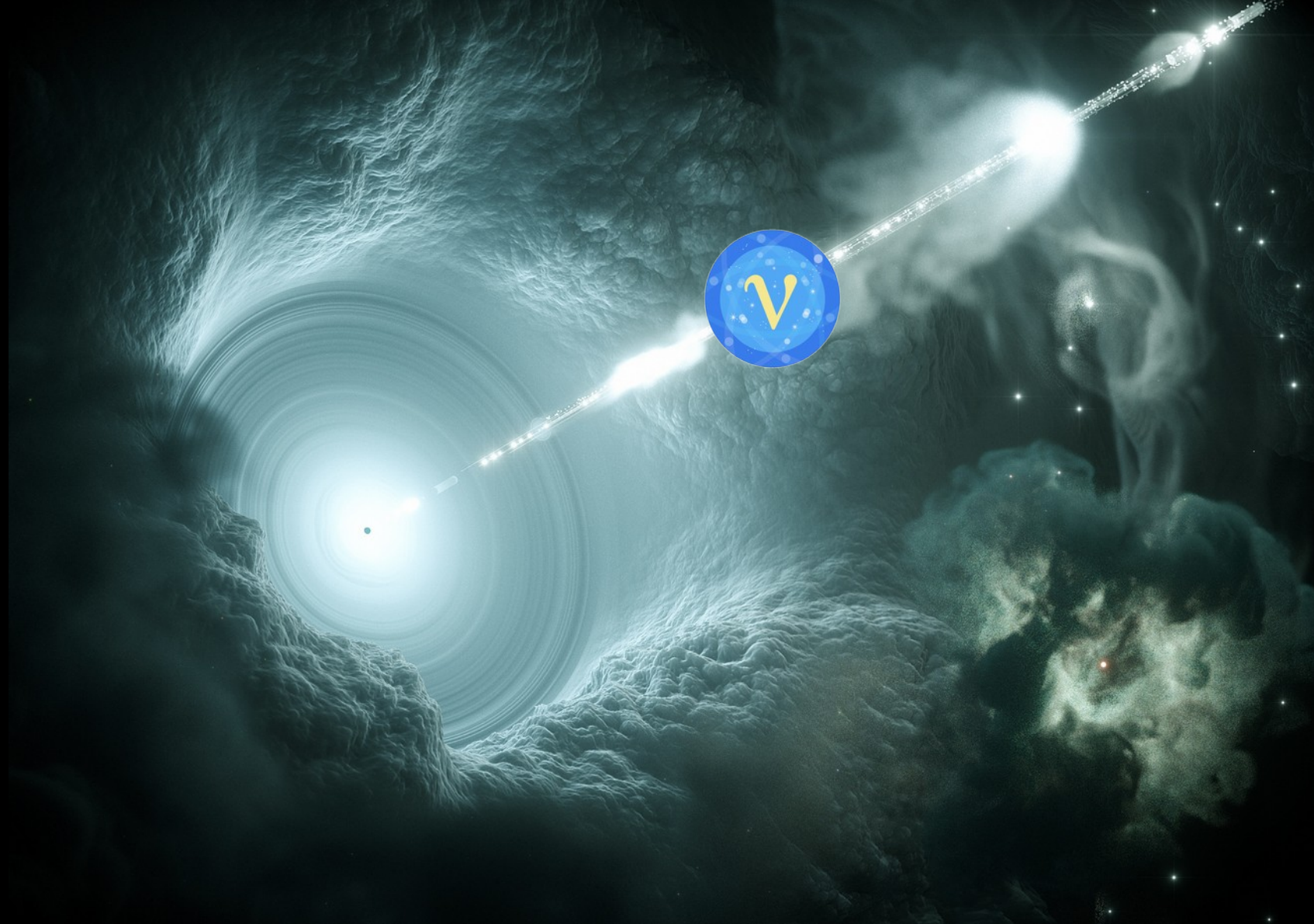














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→ Probe physics at new energy scales



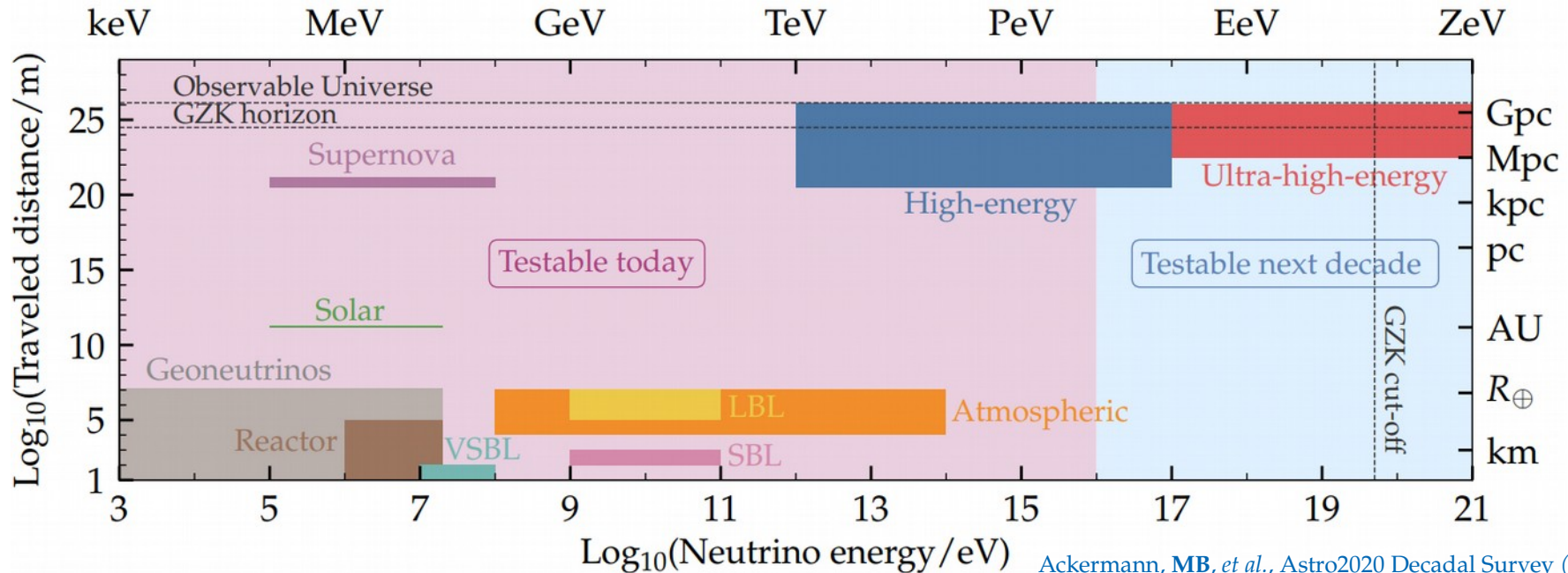
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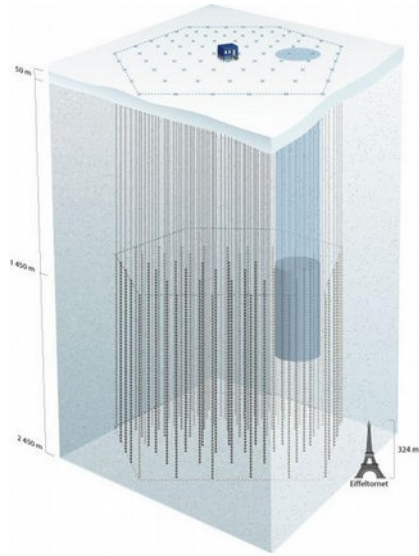


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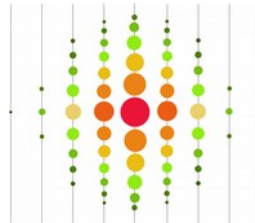
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- 5 It comes *for free*

# IceCube (8 years)

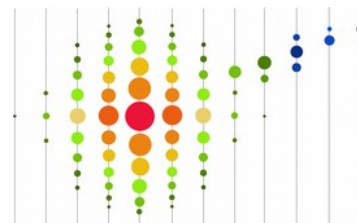
km<sup>3</sup> in-ice  
Cherenkov detector



Showers  
(mostly from  $\nu_e$ ,  $\nu_\tau$ )

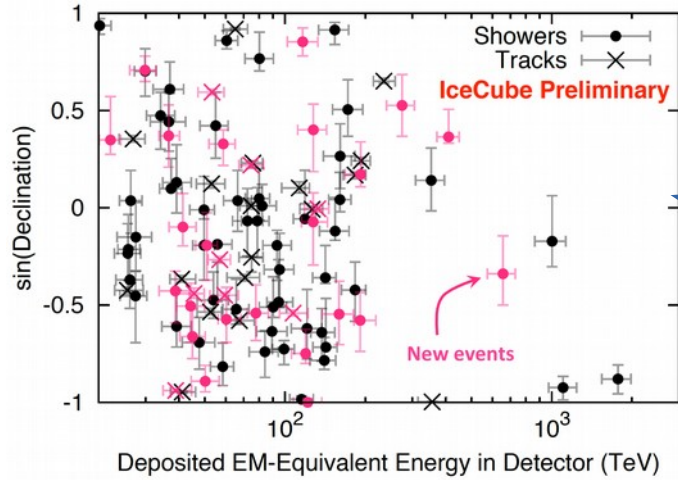


Tracks  
(from  $\nu_\mu$ )



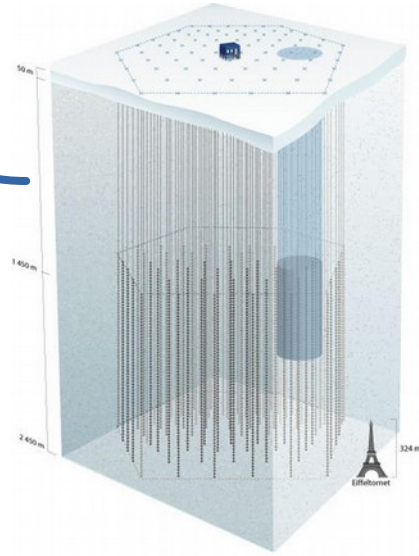


103 contained events, 15 TeV–2 PeV



IceCube (8 years)

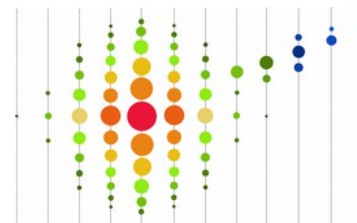
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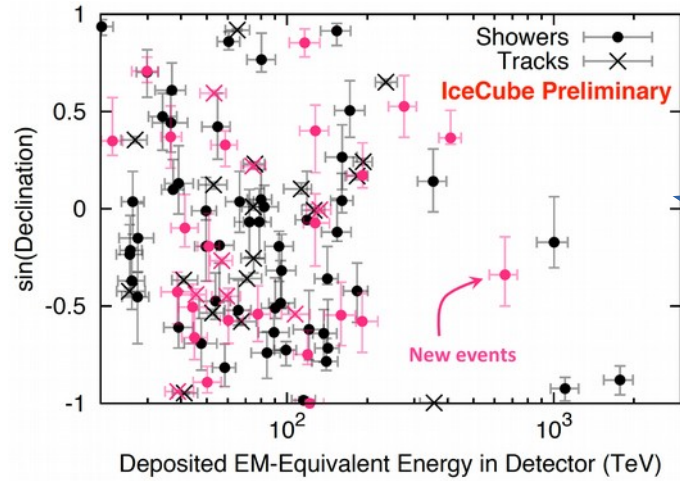
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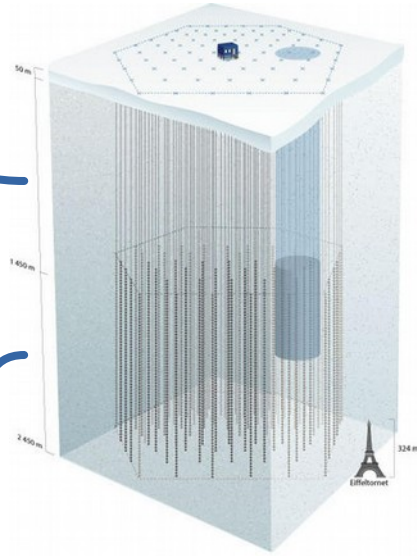


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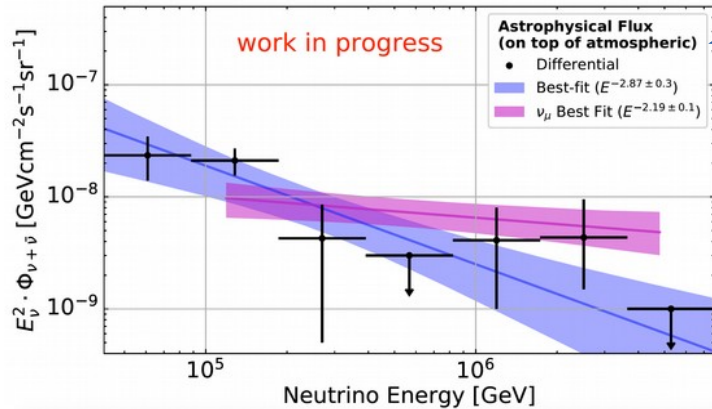


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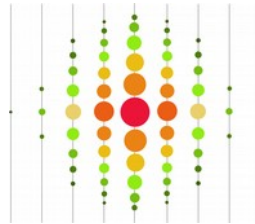
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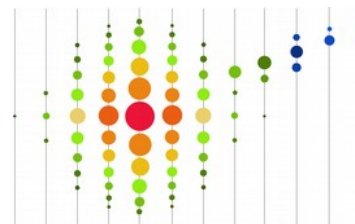
Astrophysical  $\nu$  flux detected at  $> 7\sigma$



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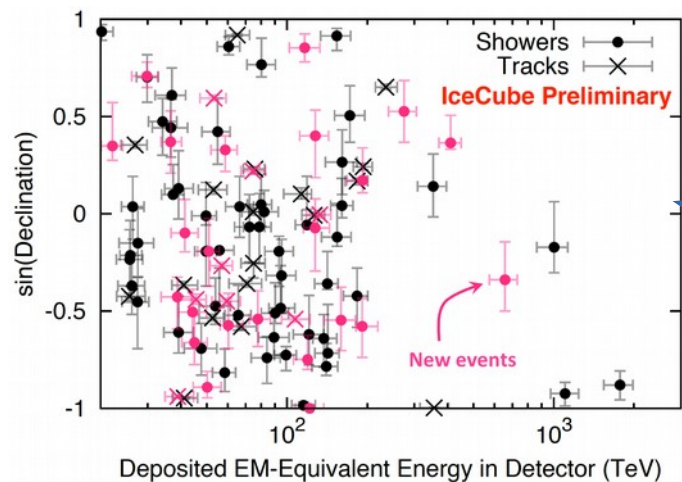


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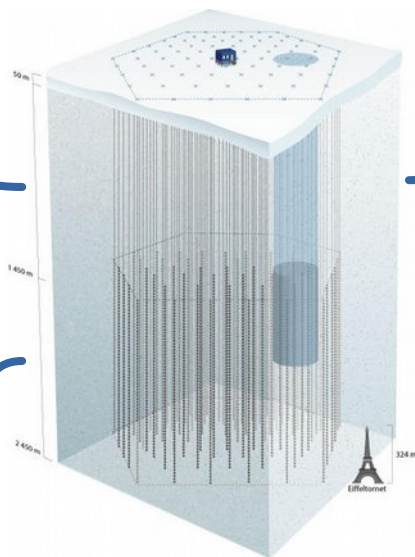


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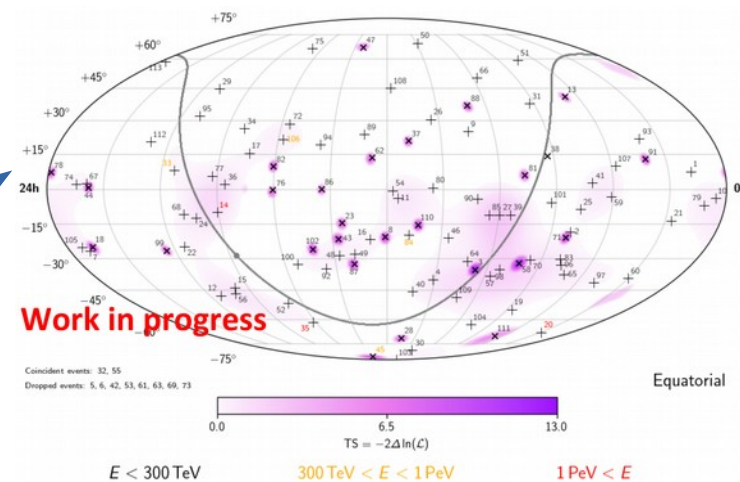


**IceCube (8 years)**

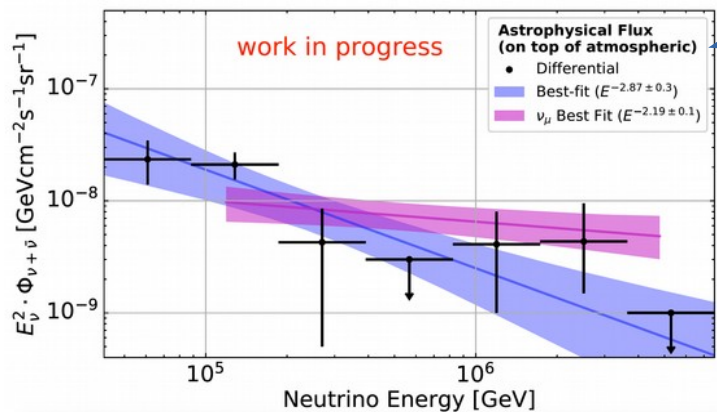
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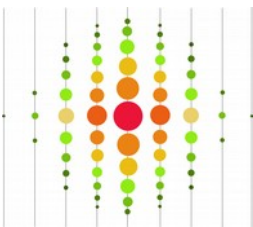
Arrival directions compatible with isotropy



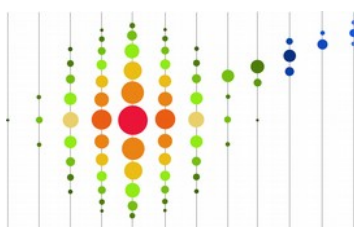
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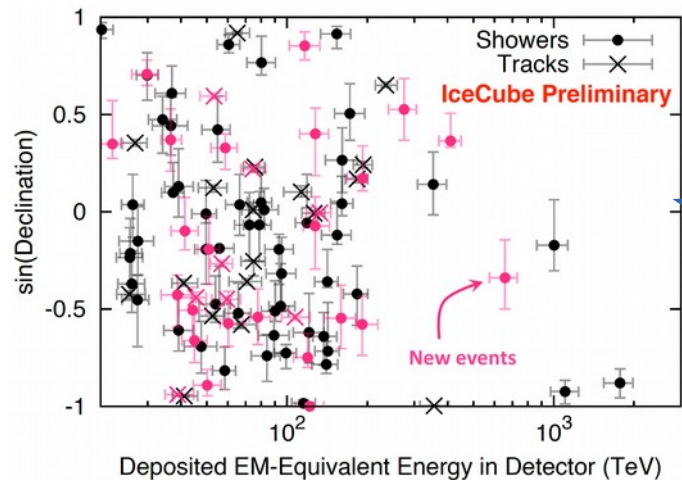
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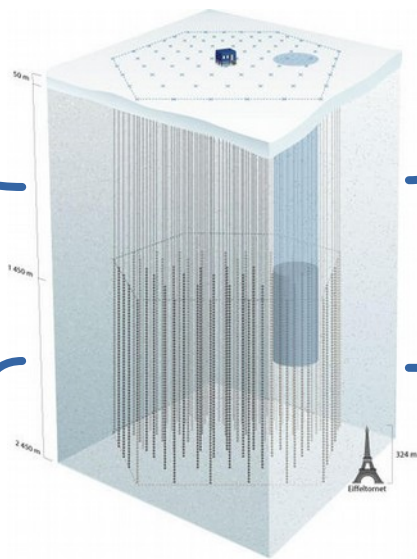


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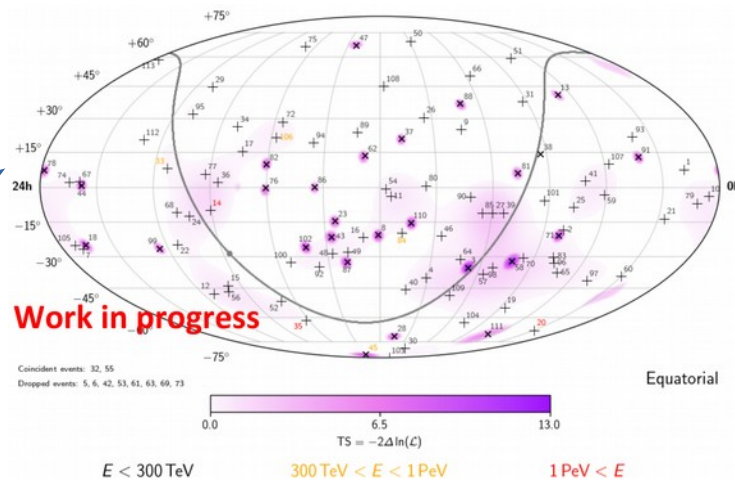


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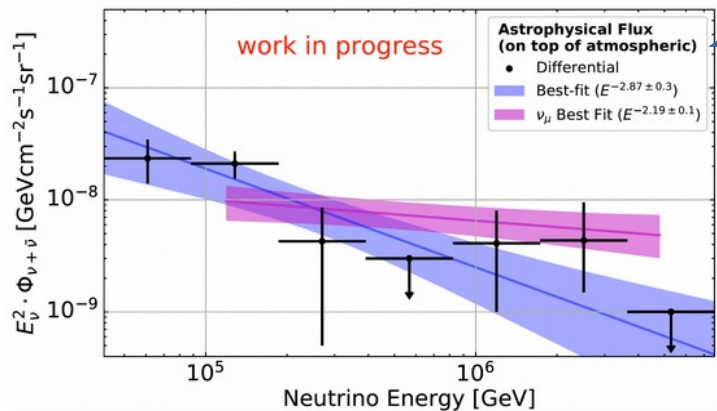
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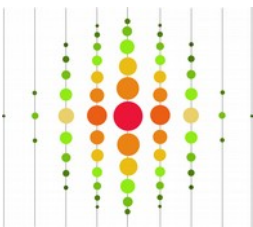
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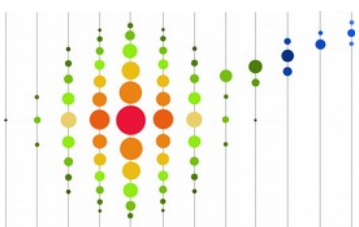
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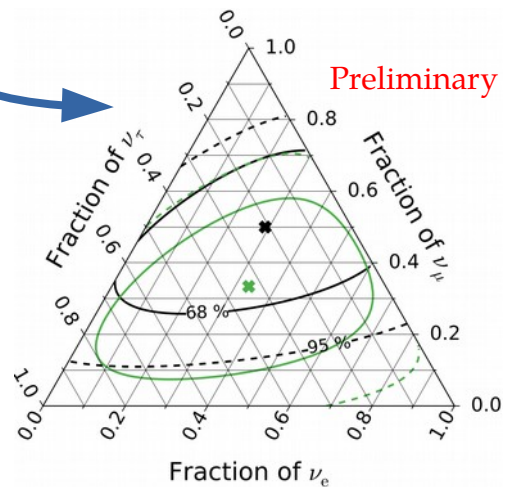
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Flavor composition



# *Status quo* of high-energy cosmic neutrinos

## What we know

- ▶ Isotropic distribution of sources
- ▶ Spectrum is a power law  $\propto E^{-p}$
- ▶ At least some sources are gamma-ray transients
- ▶ No correlation between directions of cosmic rays and neutrinos
- ▶ Flavor composition: compatible with equal number of  $\nu_e, \nu_\mu, \nu_\tau$
- ▶ No evident new physics

## What we don't know

- ▶ The sources of the diffuse  $\nu$  flux
- ▶ The  $\nu$  production mechanism
- ▶ The spectral index of the spectrum
- ▶ A spectral cut-off at a few PeV?
- ▶ Are there Galactic  $\nu$  sources?
- ▶ The precise flavor composition
- ▶ Is there new physics?



# Status quo of high-energy cosmic neutrinos

But we have solid theory expectations  
+ fast experimental progress

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*Already today.*



Astrophysical unknowns





Neutrino physicist



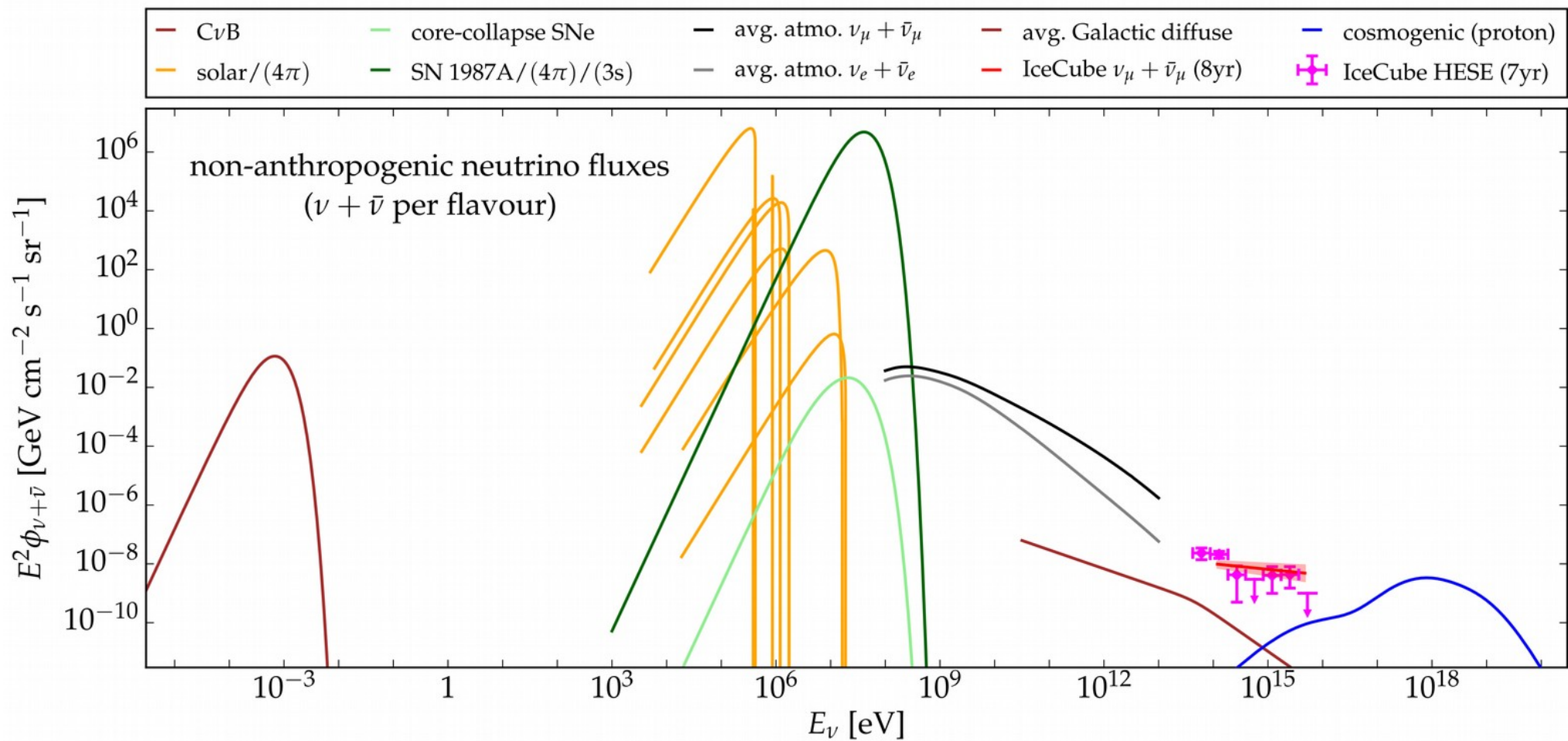


Figure courtesy of Markus Ahlers  
Also in: [Van Elewyck et al., PoS\(ICRC2019\), 1023](#)

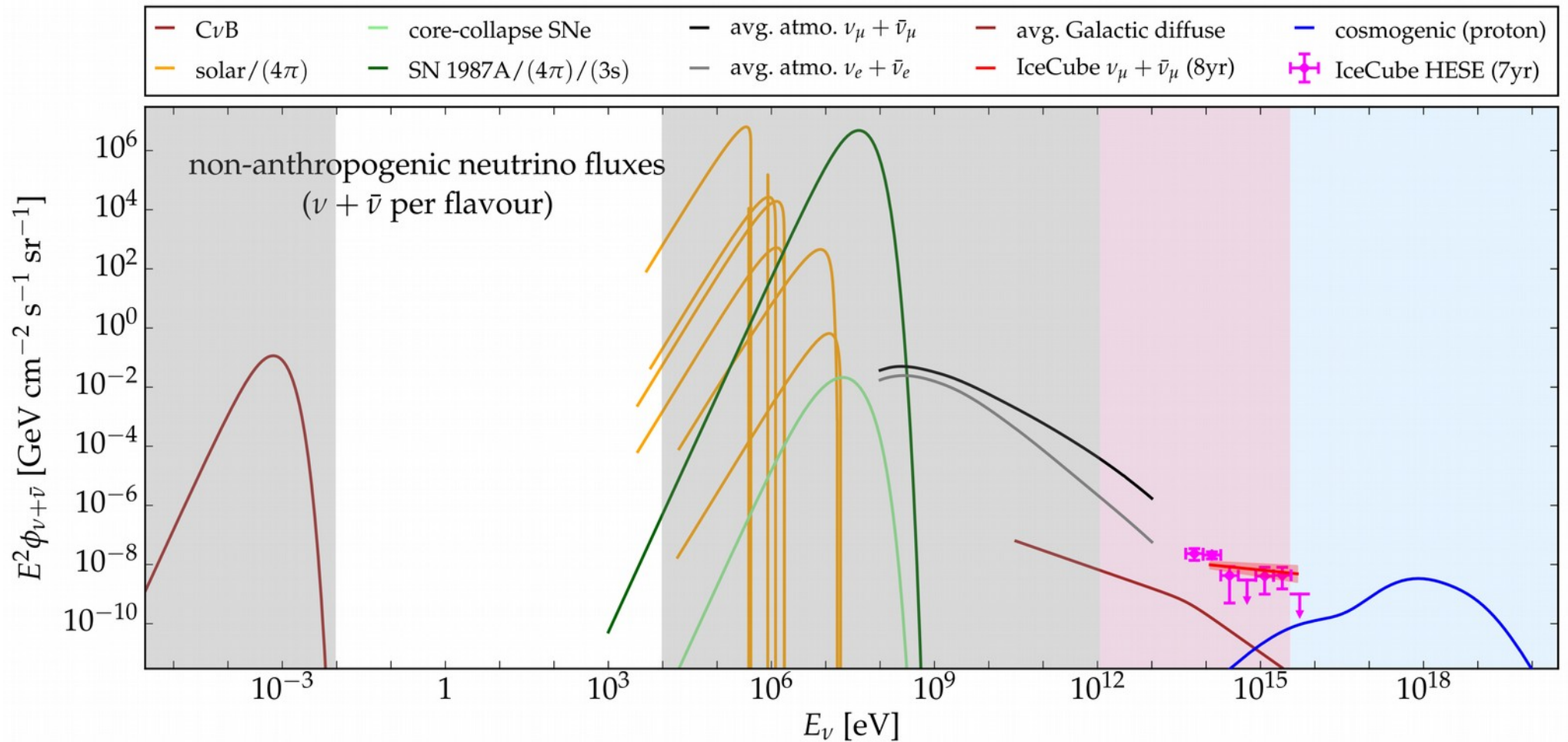


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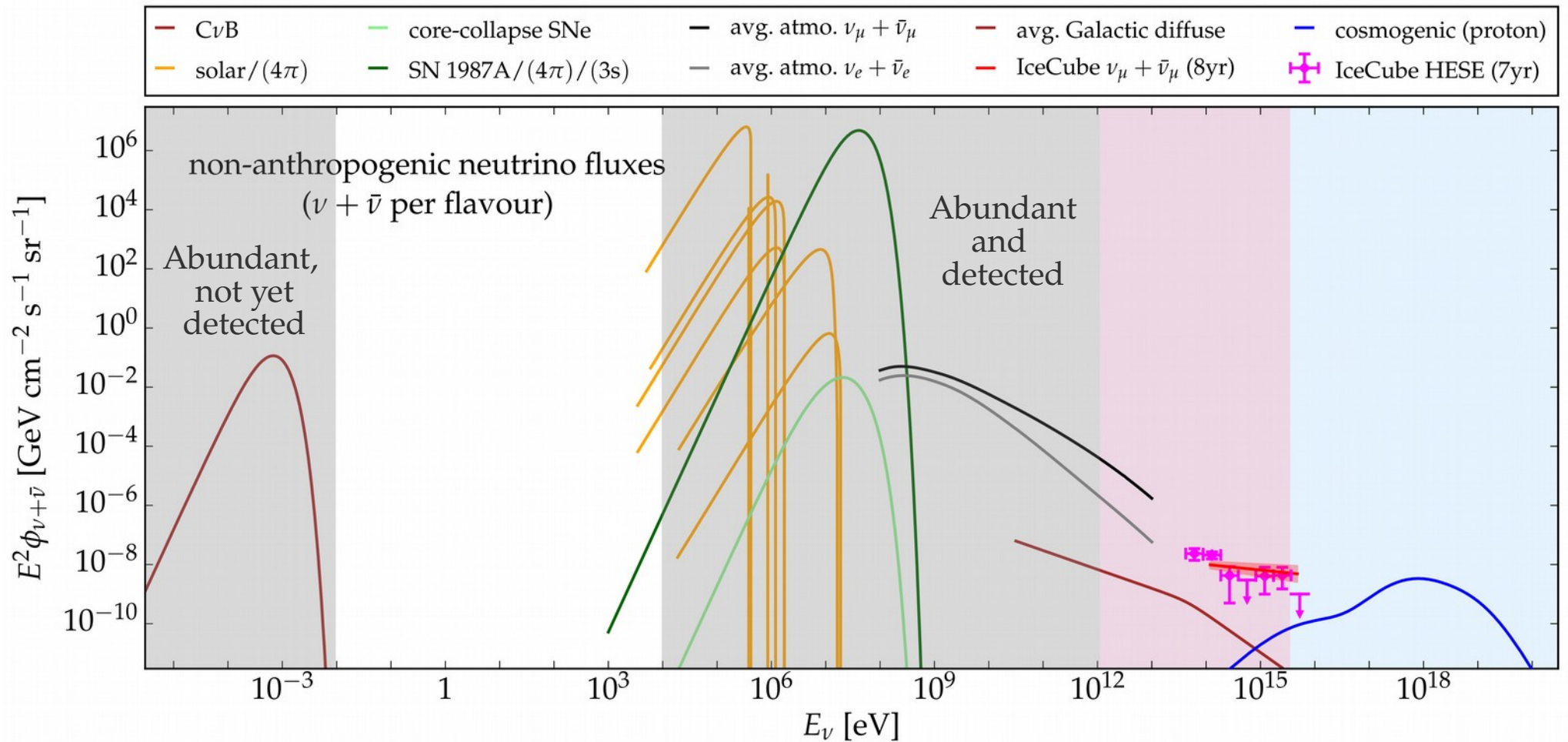


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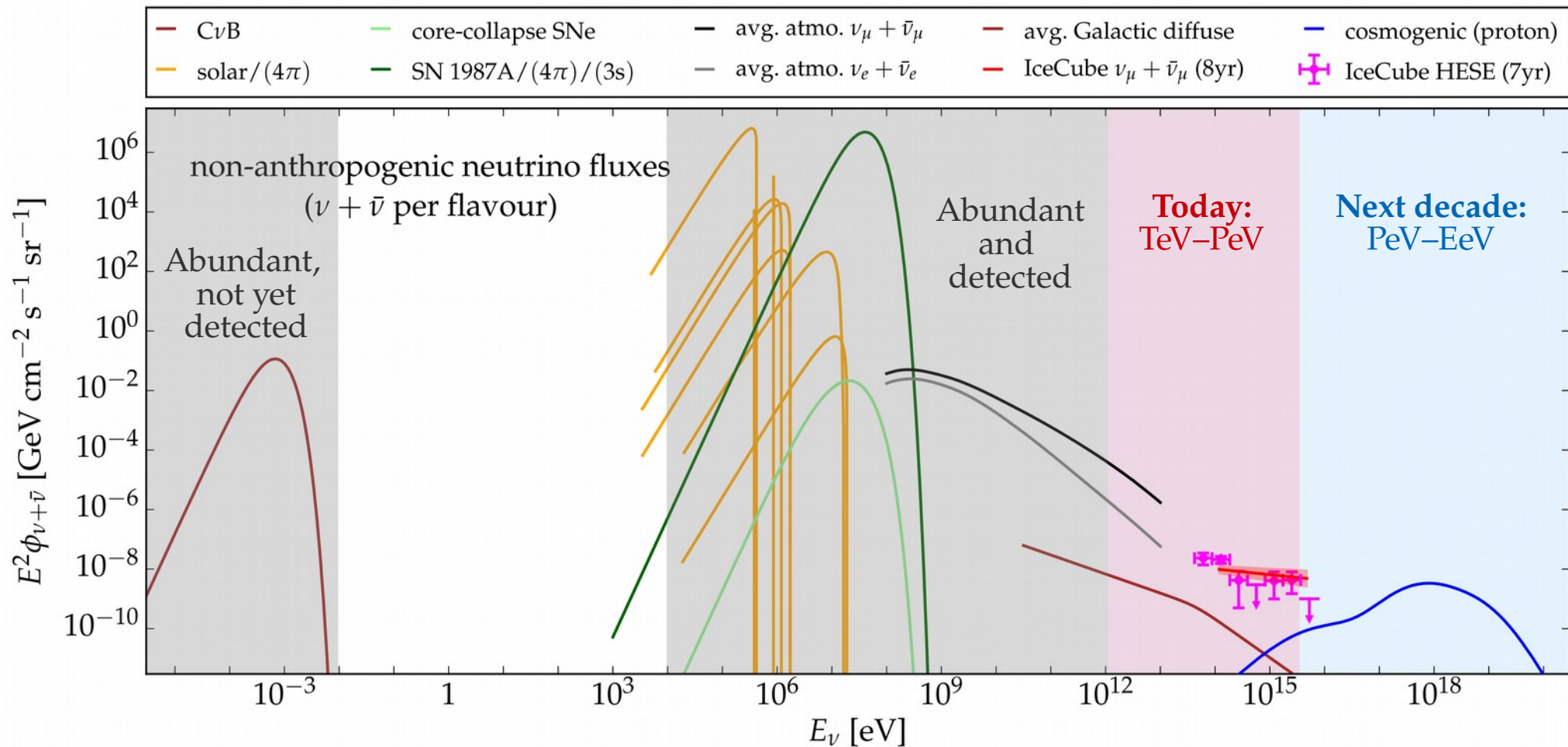
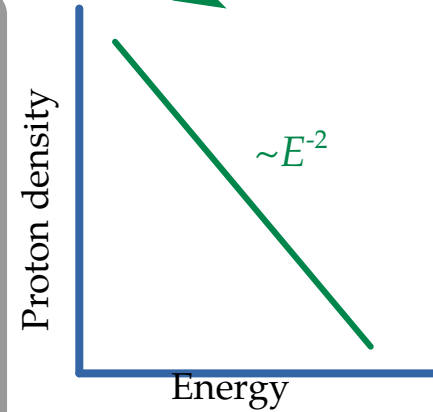
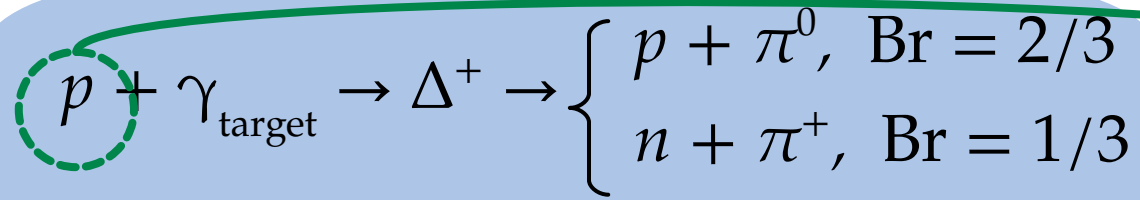


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# The multi-messenger connection: a simple picture

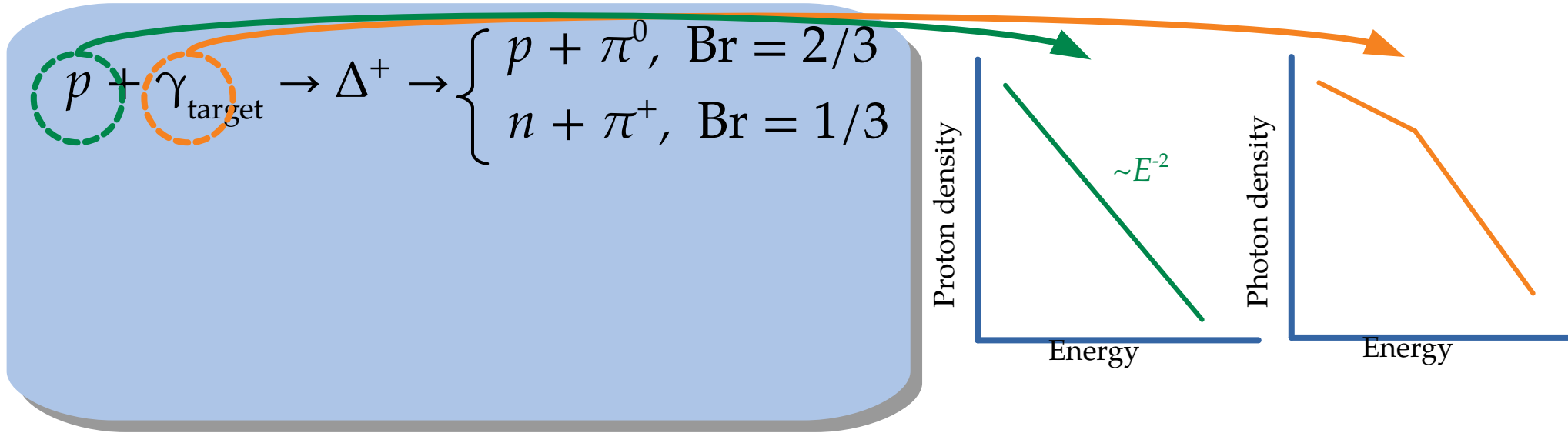
$$p + \gamma_{\text{target}} \rightarrow \Delta^+ \rightarrow \begin{cases} p + \pi^0, & \text{Br} = 2/3 \\ n + \pi^+, & \text{Br} = 1/3 \end{cases}$$

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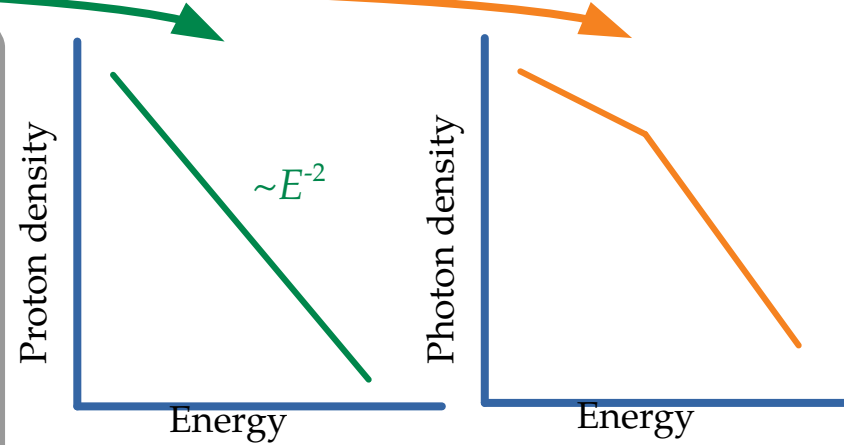
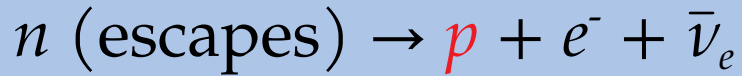
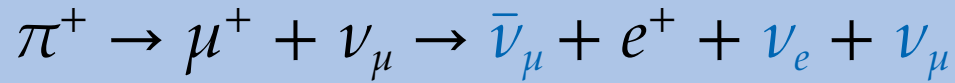
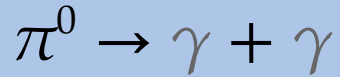
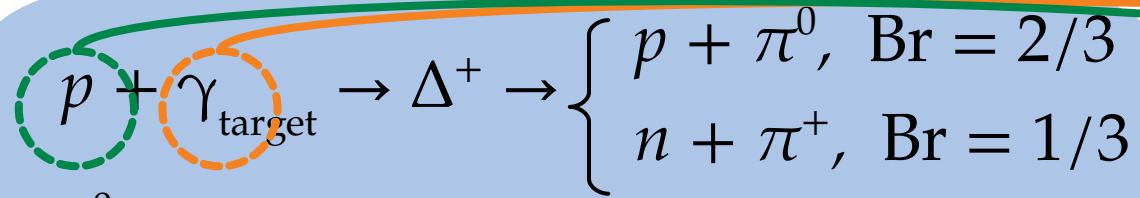




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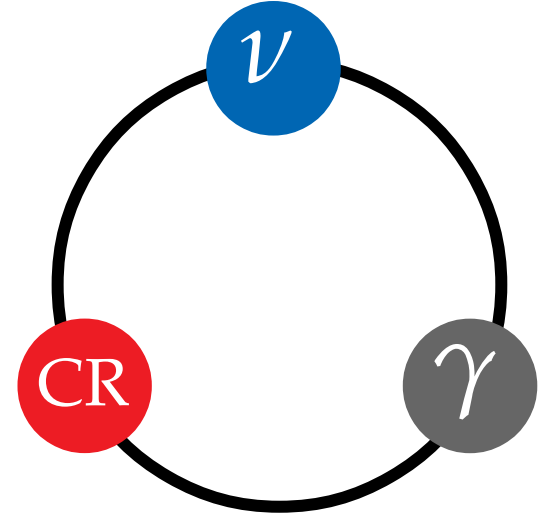
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$$\pi^0 \rightarrow \gamma + \gamma$$

$$\pi^+ \rightarrow \mu^+ + \nu_\mu \rightarrow \bar{\nu}_\mu + e^+ + \nu_e + \nu_\mu$$

$$n \text{ (escapes)} \rightarrow \textcolor{red}{p} + e^- + \bar{\nu}_e$$



Neutrino energy = Proton energy / 20

Gamma-ray energy = Proton energy / 10

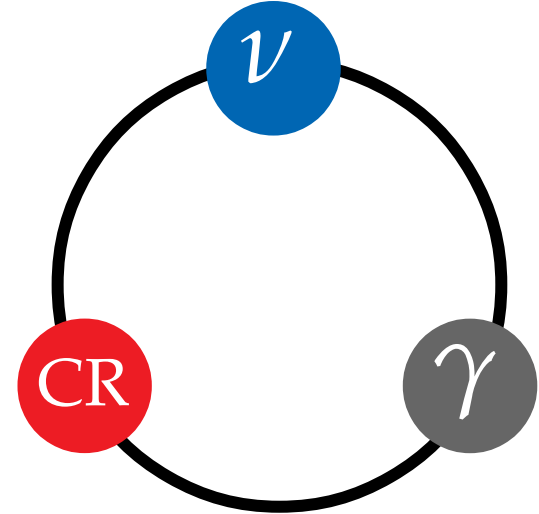
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1 PeV

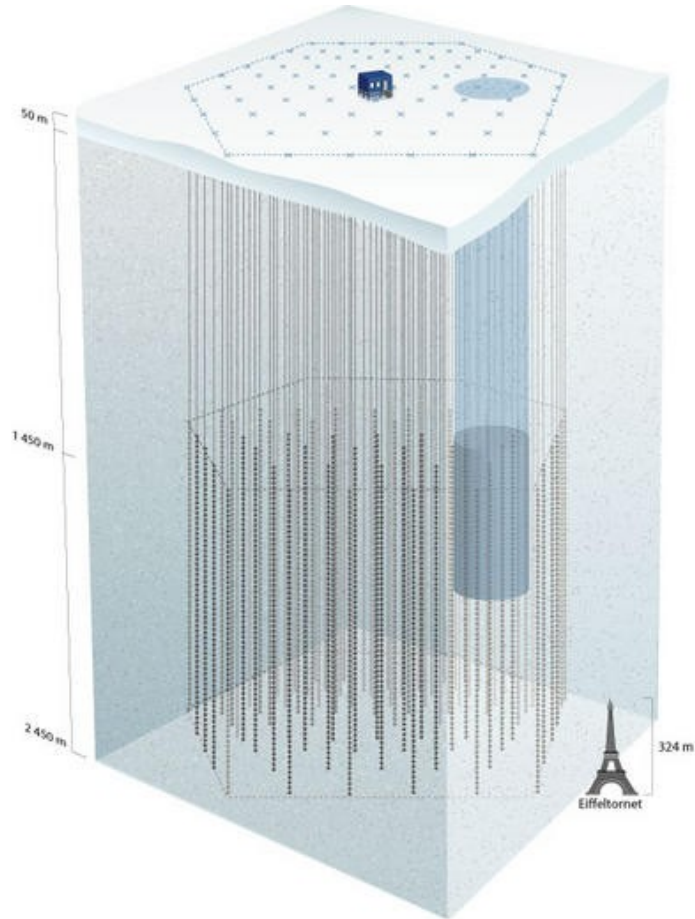
20 PeV

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# IceCube – What is it?

- ▶  $\text{Km}^3$  in-ice Cherenkov detector in Antarctica
- ▶ >5000 PMTs at 1.5–2.5 km of depth
- ▶ Sensitive to neutrino energies  $> 10 \text{ GeV}$





# How does IceCube see TeV–PeV neutrinos?

## Deep inelastic neutrino-nucleon scattering

Neutral current (NC)

$$\nu_x + N \rightarrow \nu_x + X$$

Charged current (CC)

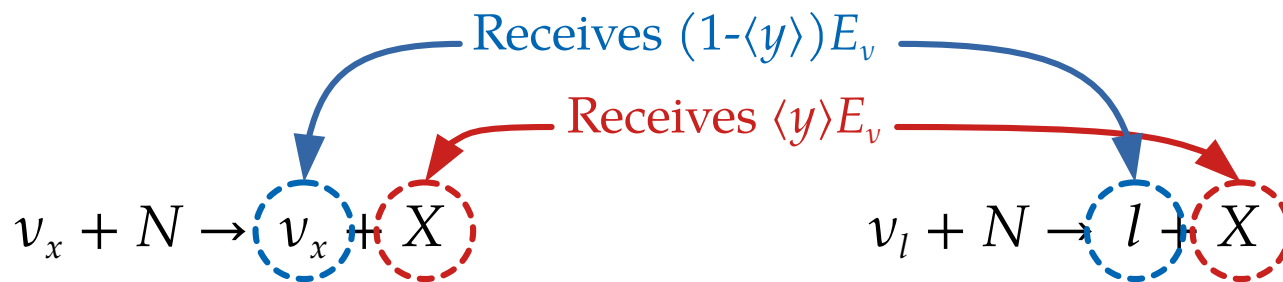
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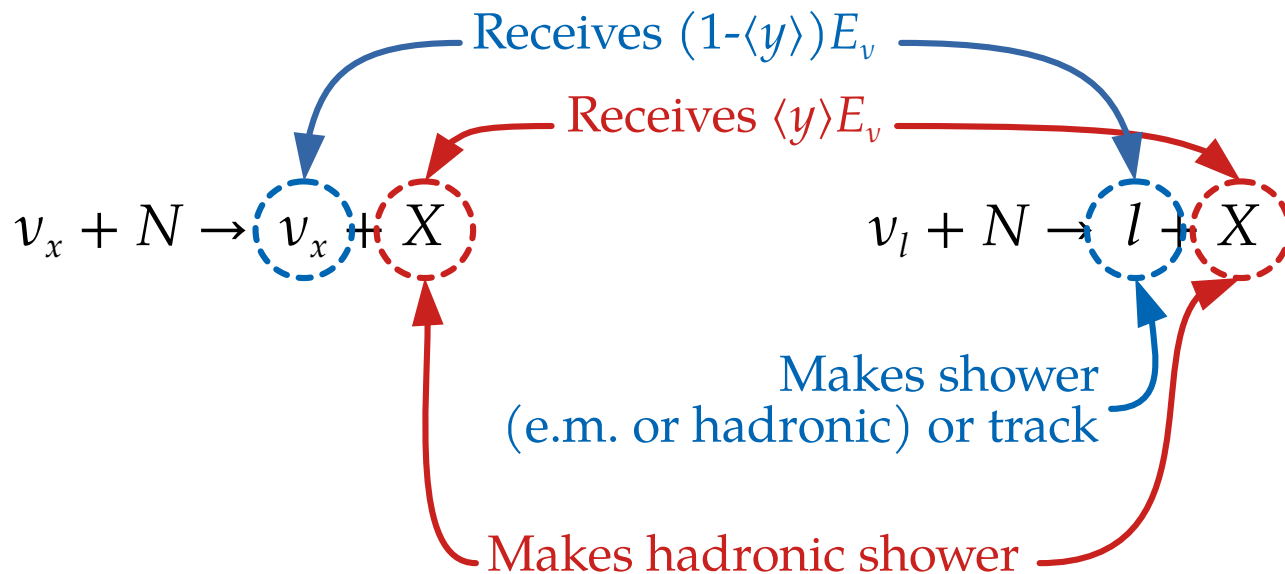
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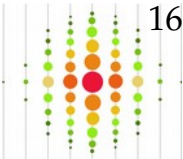
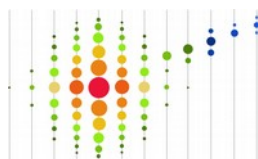
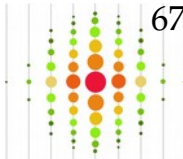
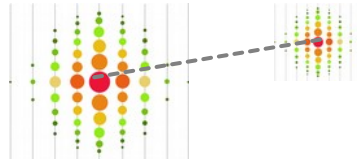
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Detected

To be confirmed

$\nu_x + \bar{\nu}_x$ NC									
$\nu_e + \bar{\nu}_e$ CC		+							
$\nu_\mu + \bar{\nu}_\mu$ CC		+							
$\nu_\tau + \bar{\nu}_\tau$ CC		+		16% or		17% or		67%	

# Fundamental physics with HE cosmic neutrinos

- ▶ Numerous new-physics effects grow as  $\sim \kappa_n \cdot E^n \cdot L$
- ▶ So we can probe  $\kappa_n \sim 4 \cdot 10^{-47} (E/\text{PeV})^{-n} (L/\text{Gpc})^{-1} \text{PeV}^{1-n}$
- ▶ Improvement over current limits:  $\kappa_0 < 10^{-29} \text{PeV}$ ,  $\kappa_1 < 10^{-33}$
- ▶ Fundamental physics can be extracted from four neutrino observables:
  - ▶ Spectral shape
  - ▶ Angular distribution
  - ▶ Flavor composition
  - ▶ Timing



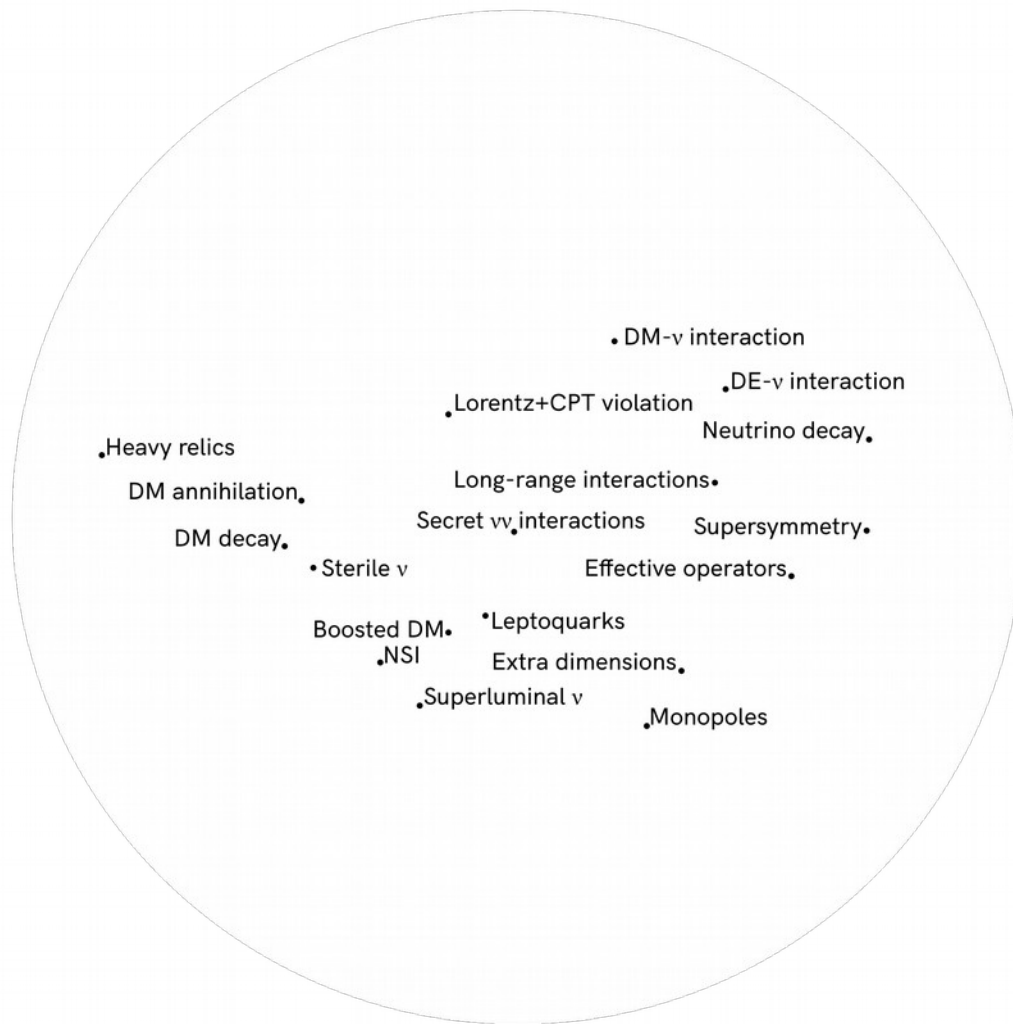
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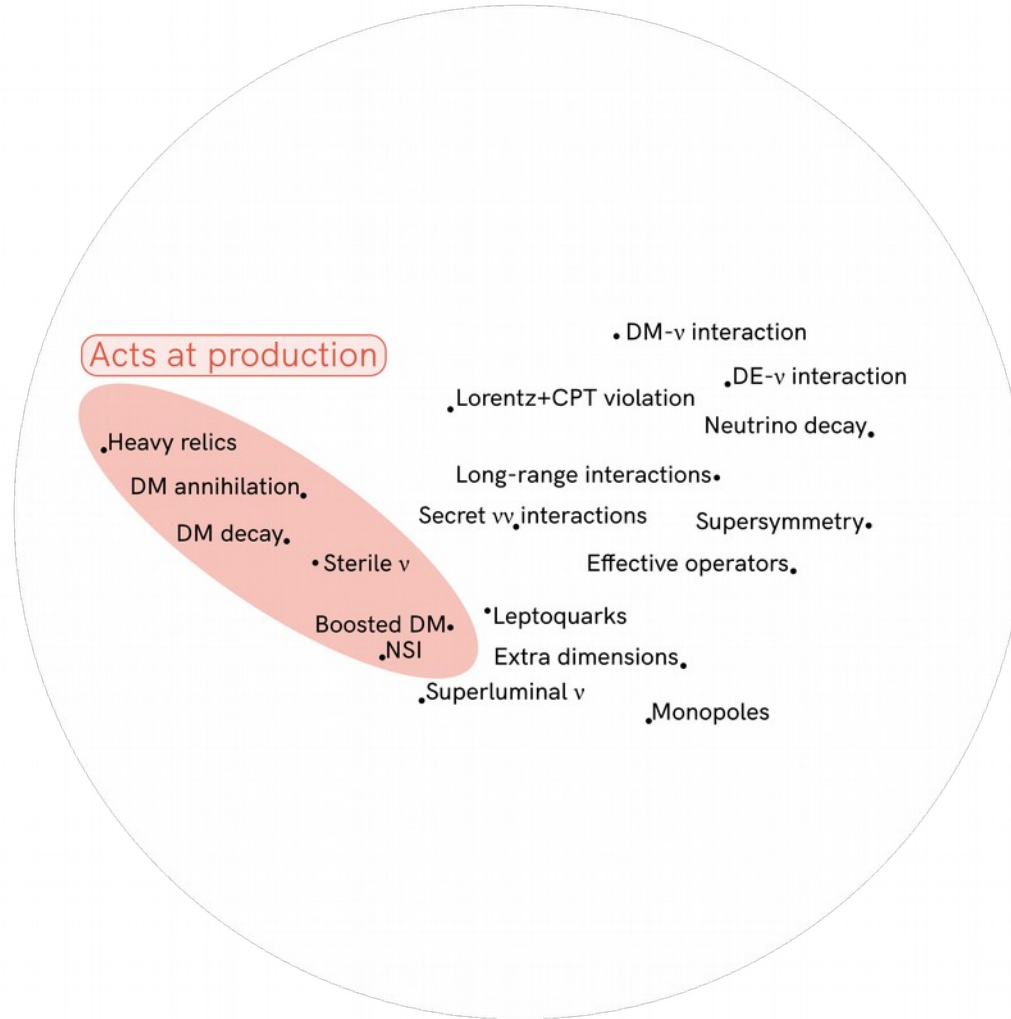
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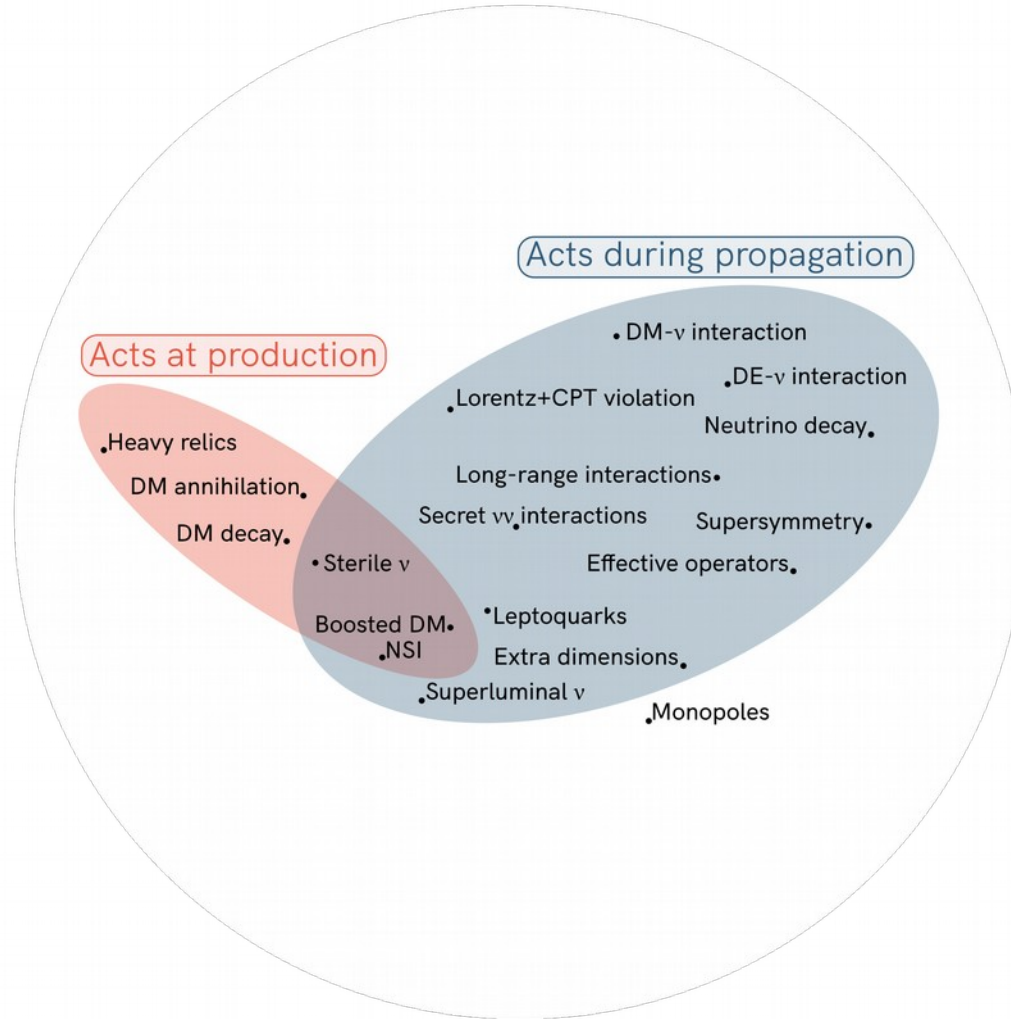
*In spite of poor energy, angular, flavor reconstruction & astrophysical unknowns*



*Note: Not an exhaustive list*

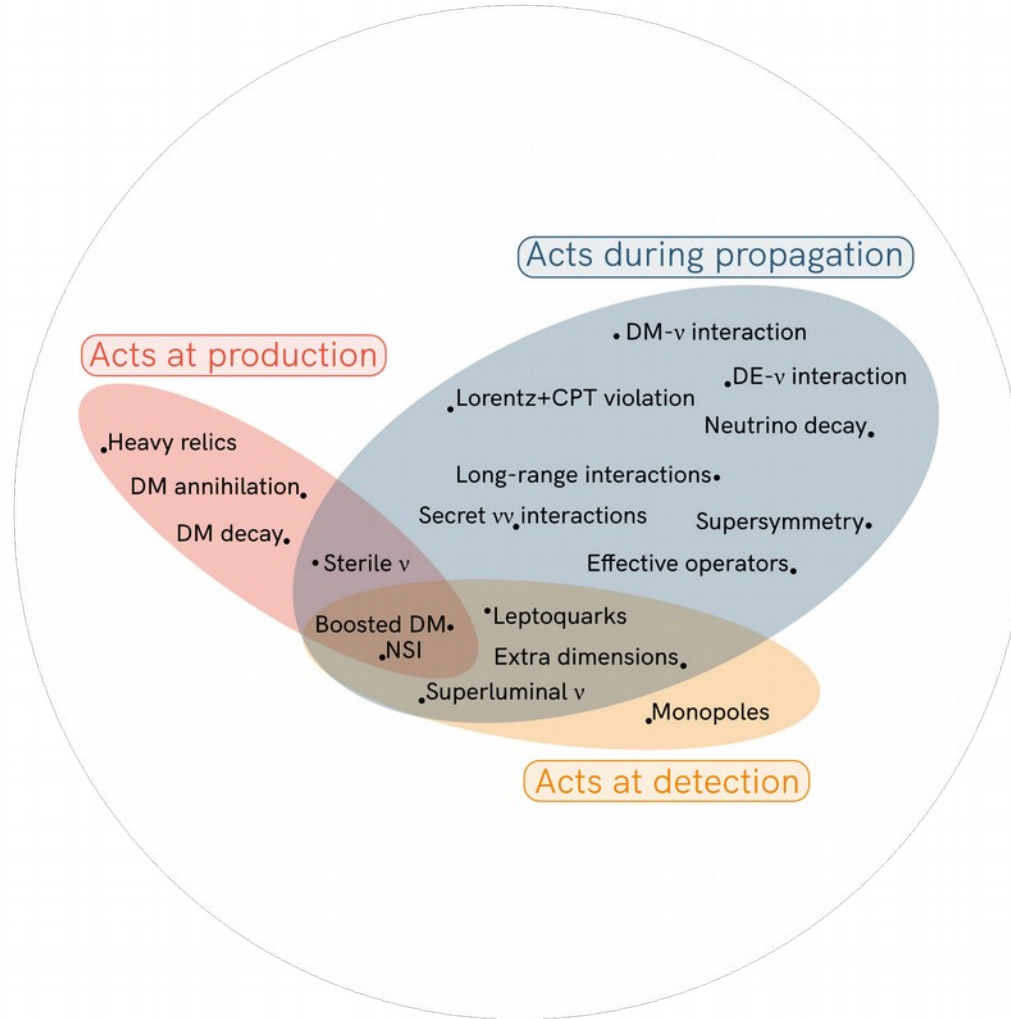


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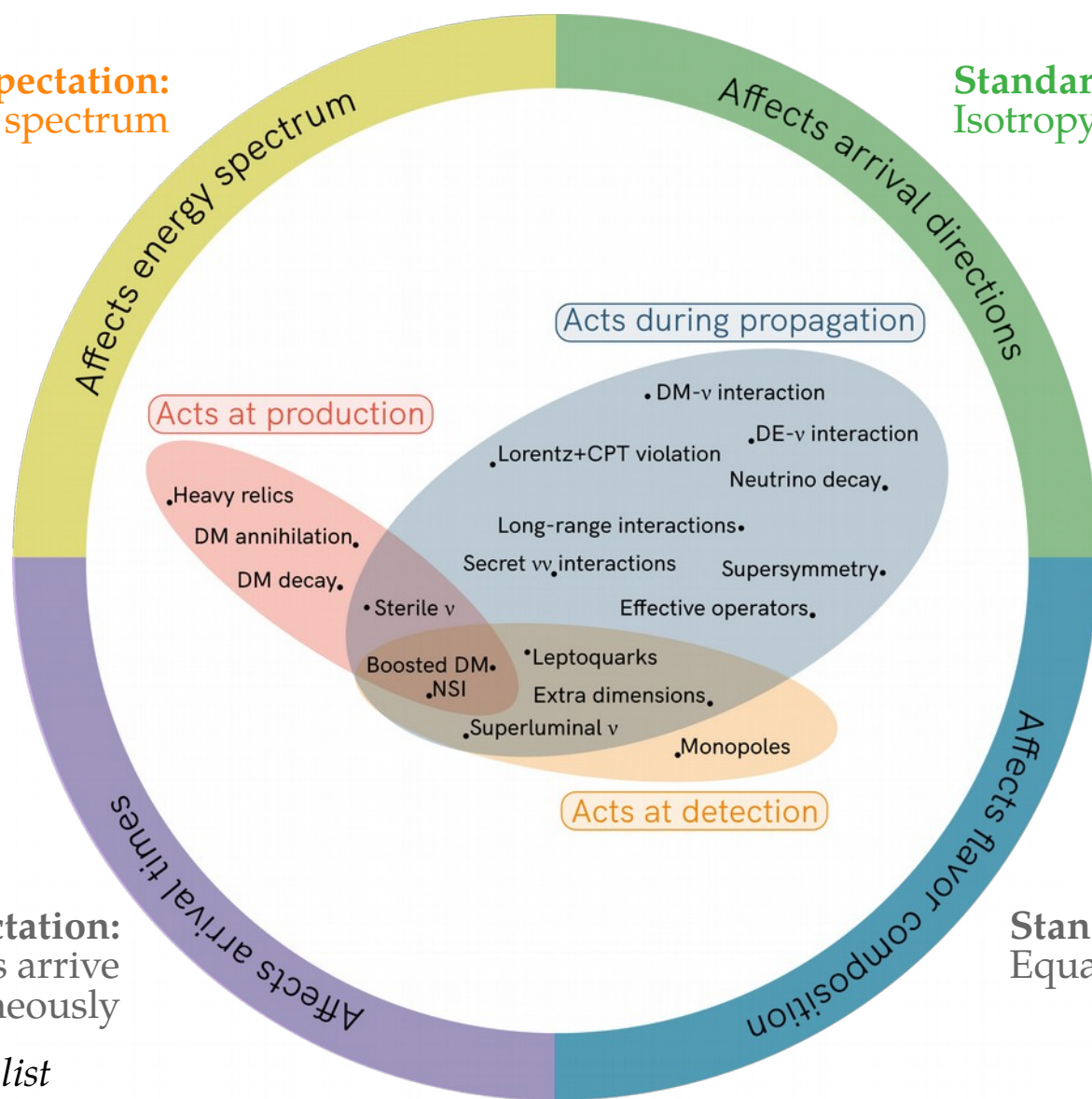




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Power-law energy spectrum

**Standard expectation:**  
Isotropy (for diffuse flux)



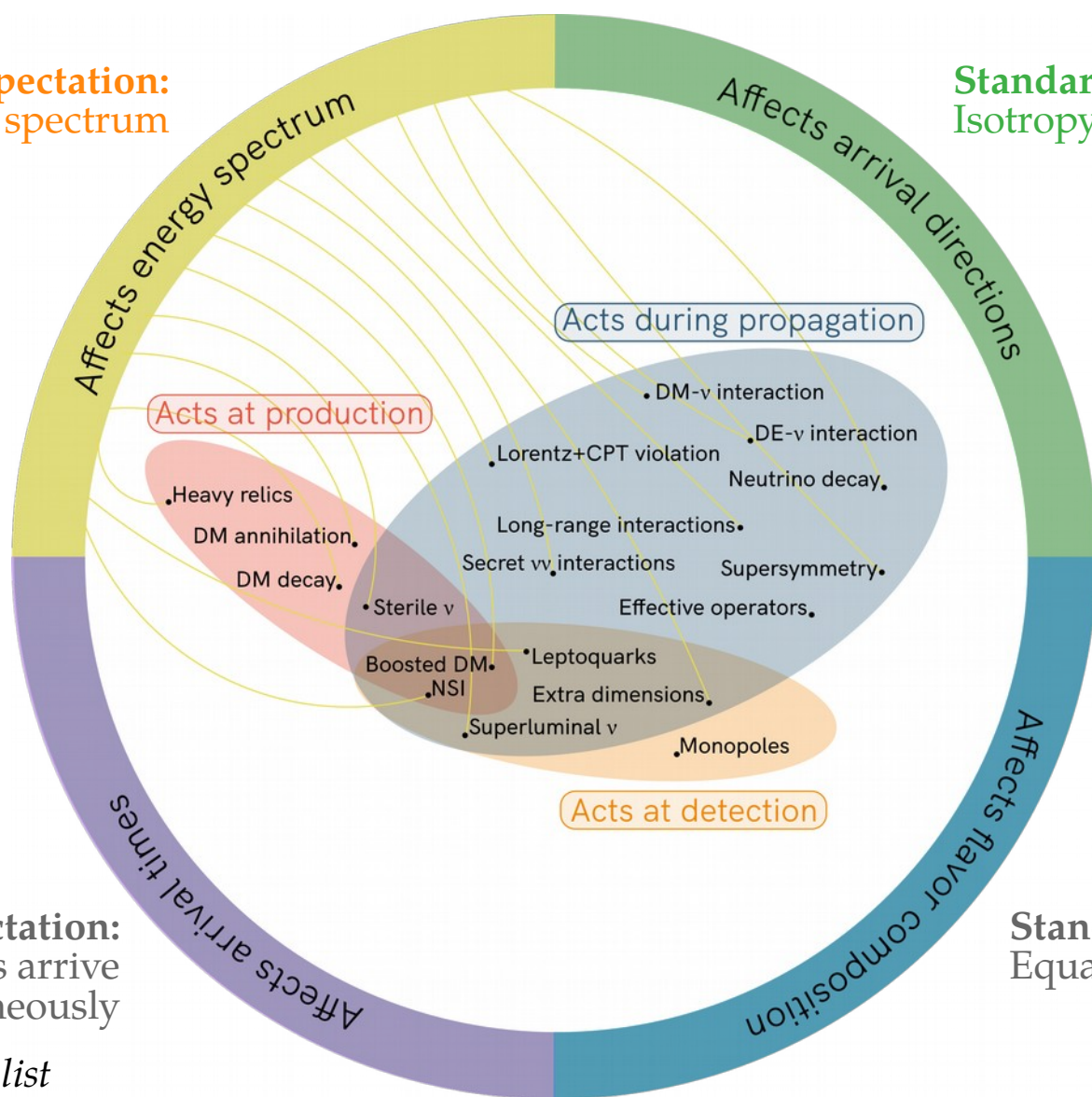
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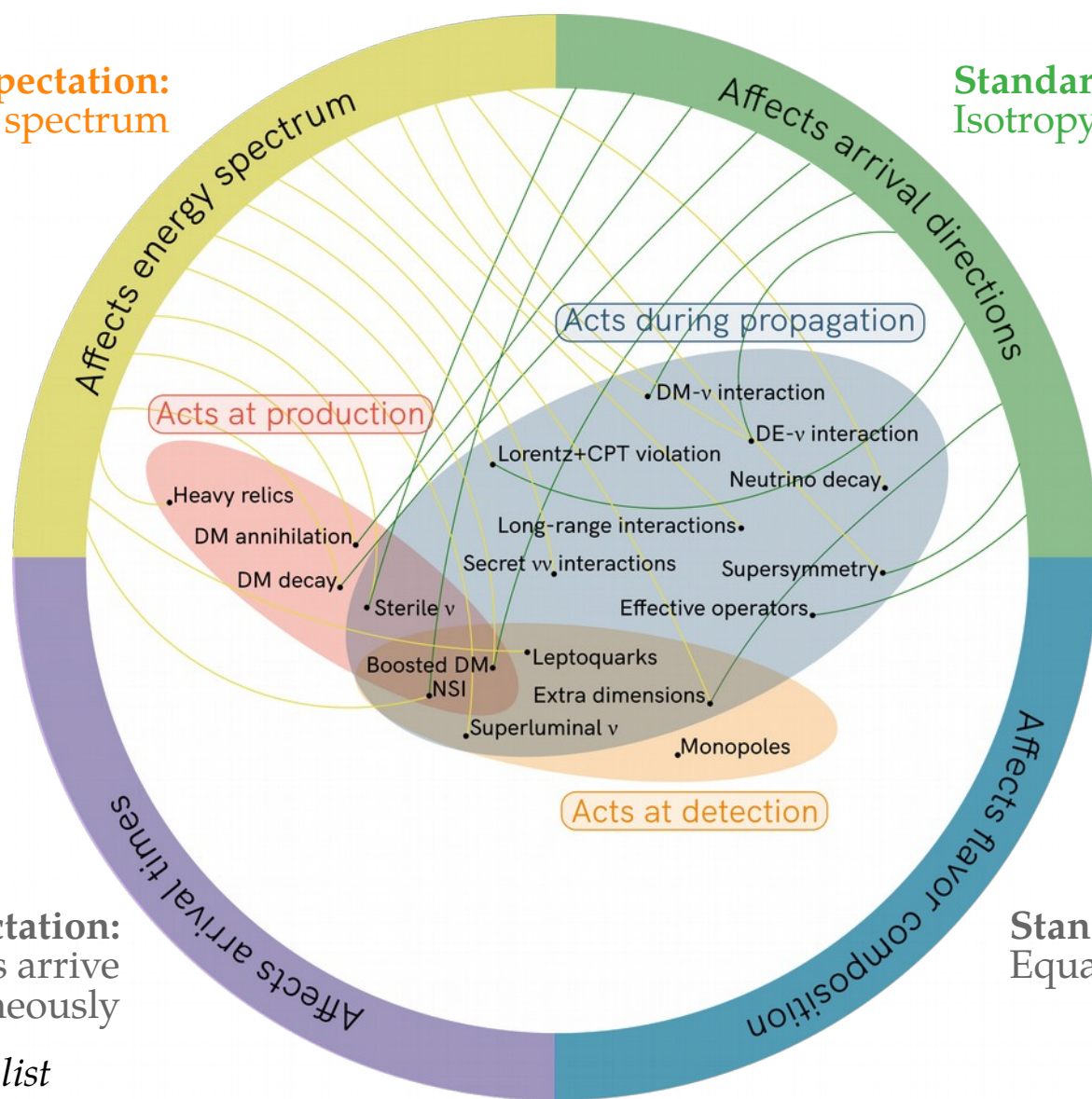
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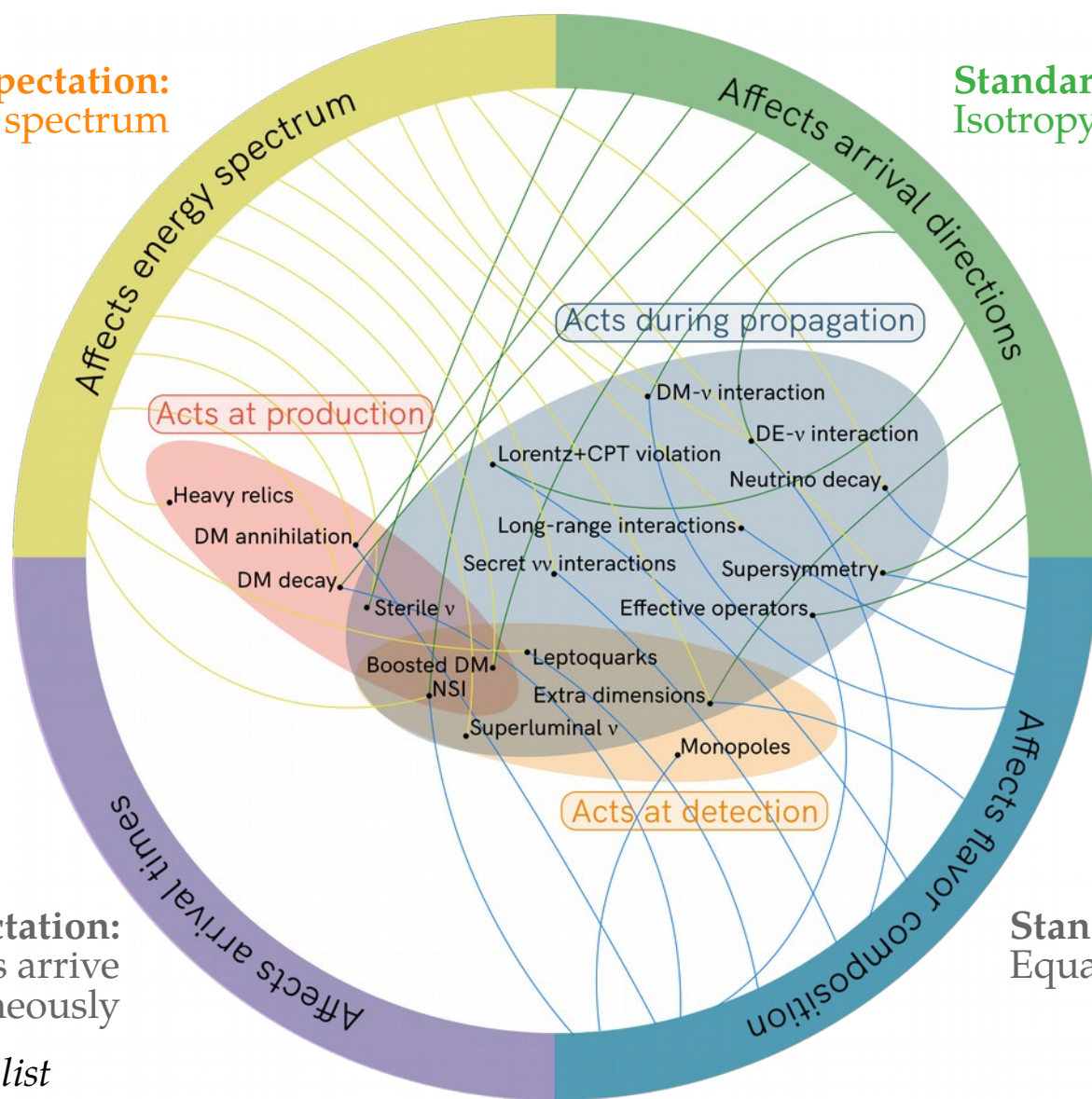
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**Standard expectation:**  
Isotropy (for diffuse flux)



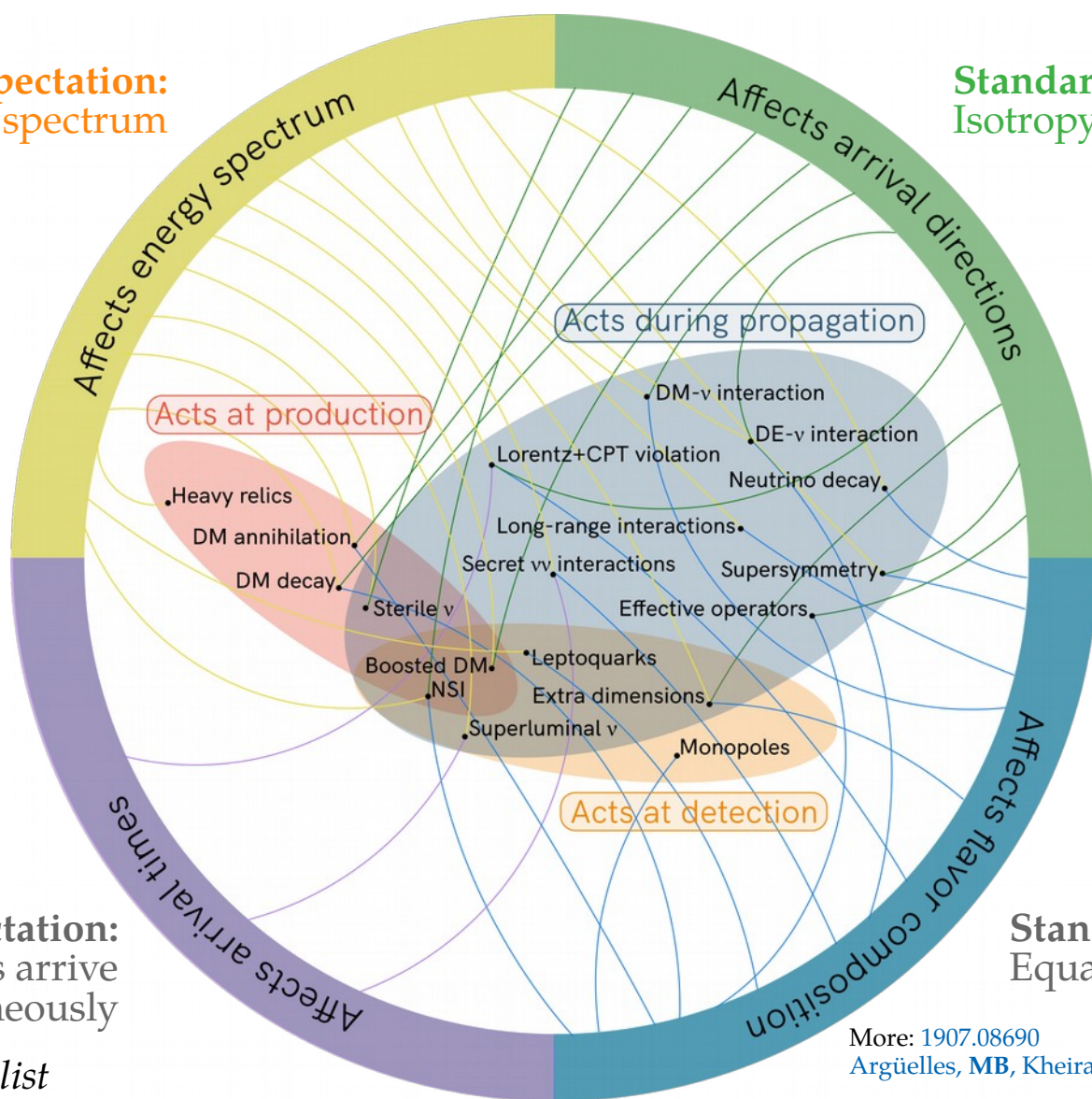
**Standard expectation:**  
 $\nu$  and  $\gamma$  from transients arrive simultaneously

**Standard expectation:**  
Equal number of  $\nu_e, \nu_\mu, \nu_\tau$

*Note: Not an exhaustive list*

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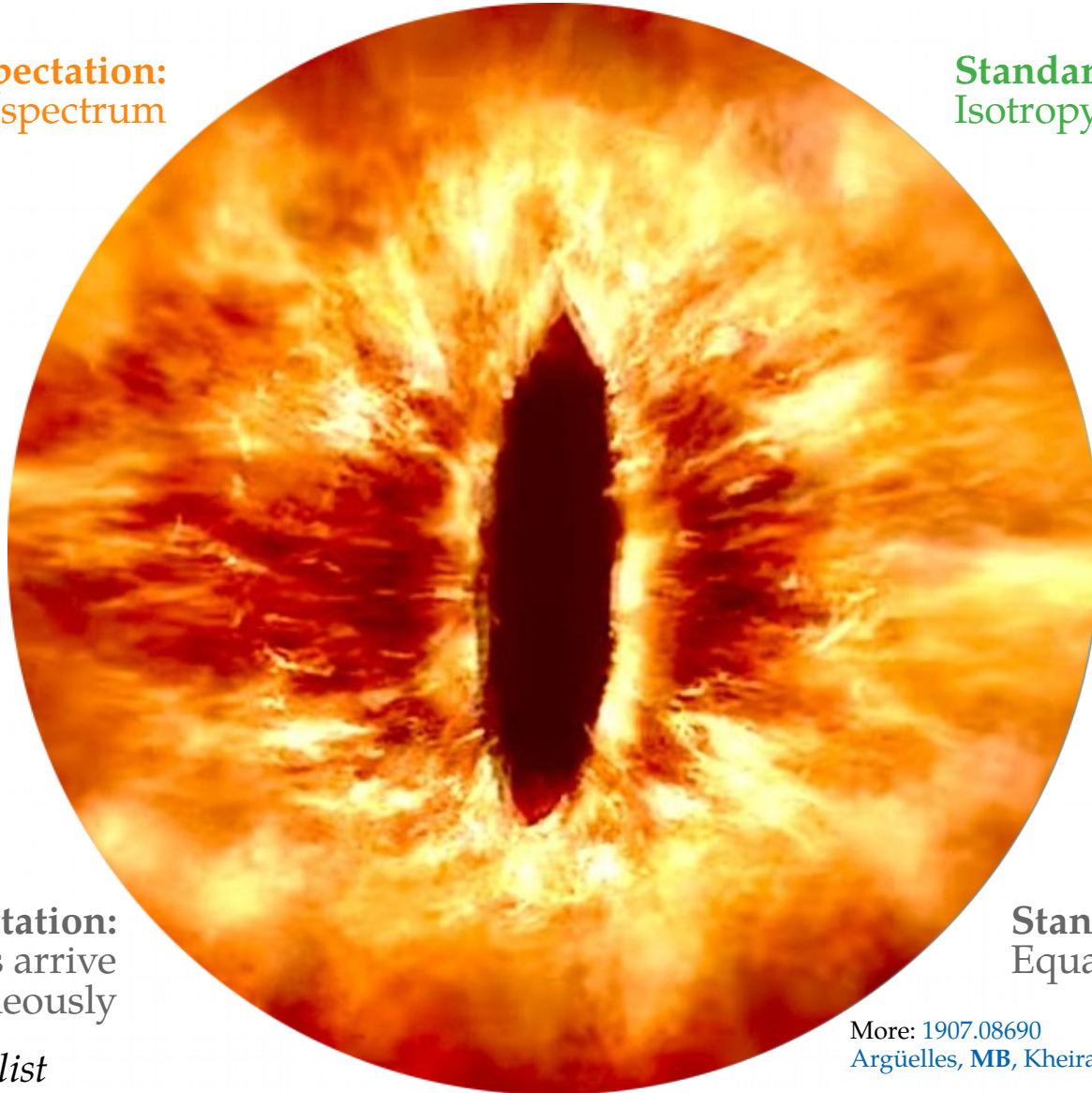
More: 1907.08690

Argüelles, MB, Kheirandish, Palomares-Ruiz, Salvadó, Vincent



**Standard expectation:**  
Power-law energy spectrum

**Standard expectation:**  
Isotropy (for diffuse flux)



**Standard expectation:**  
 $\nu$  and  $\gamma$  from transients arrive  
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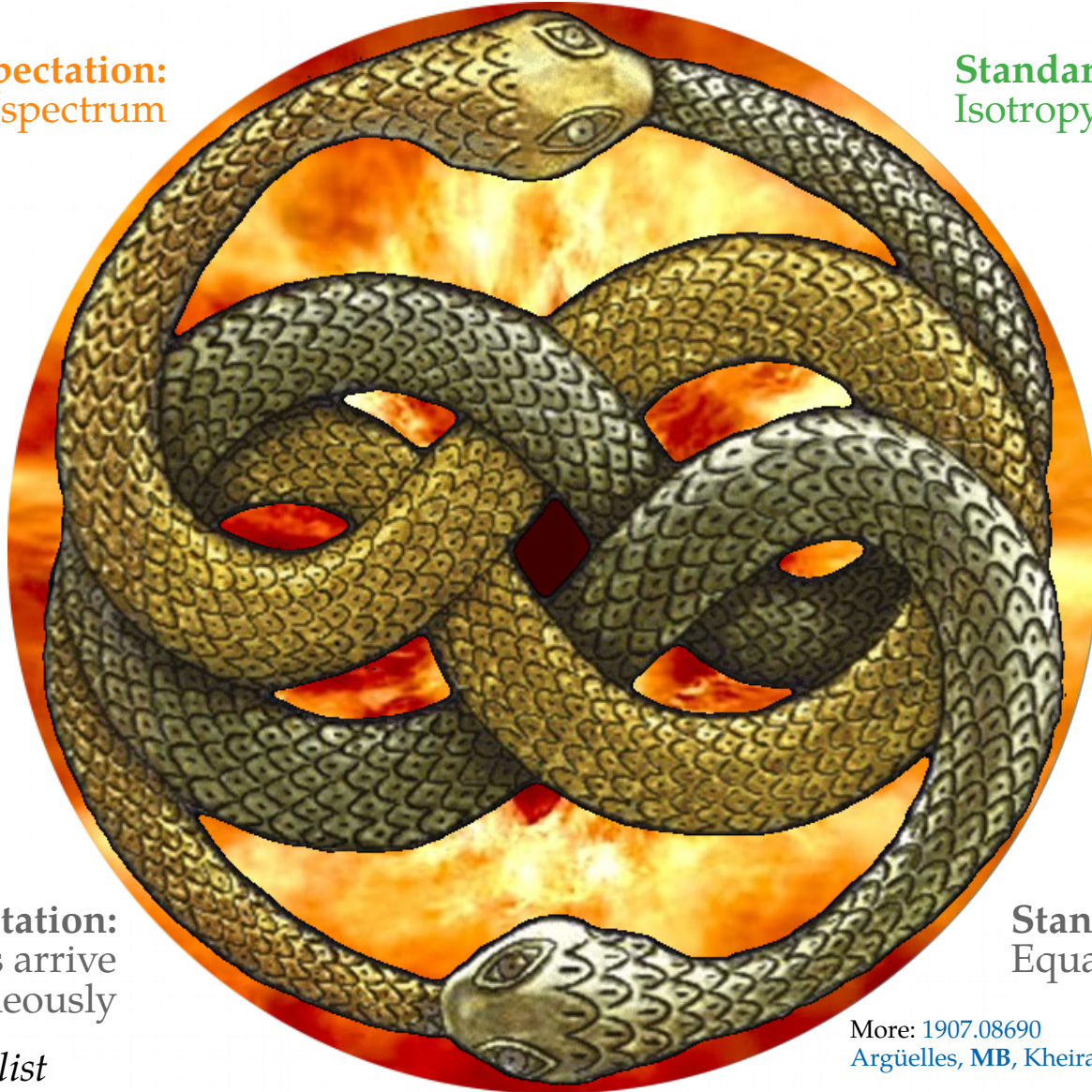
**Standard expectation:**  
Equal number of  $\nu_e$ ,  $\nu_\mu$ ,  $\nu_\tau$

*Note: Not an exhaustive list*

More: 1907.08690  
Argüelles, MB, Kheirandish, Palomares-Ruiz, Salvadó, Vincent

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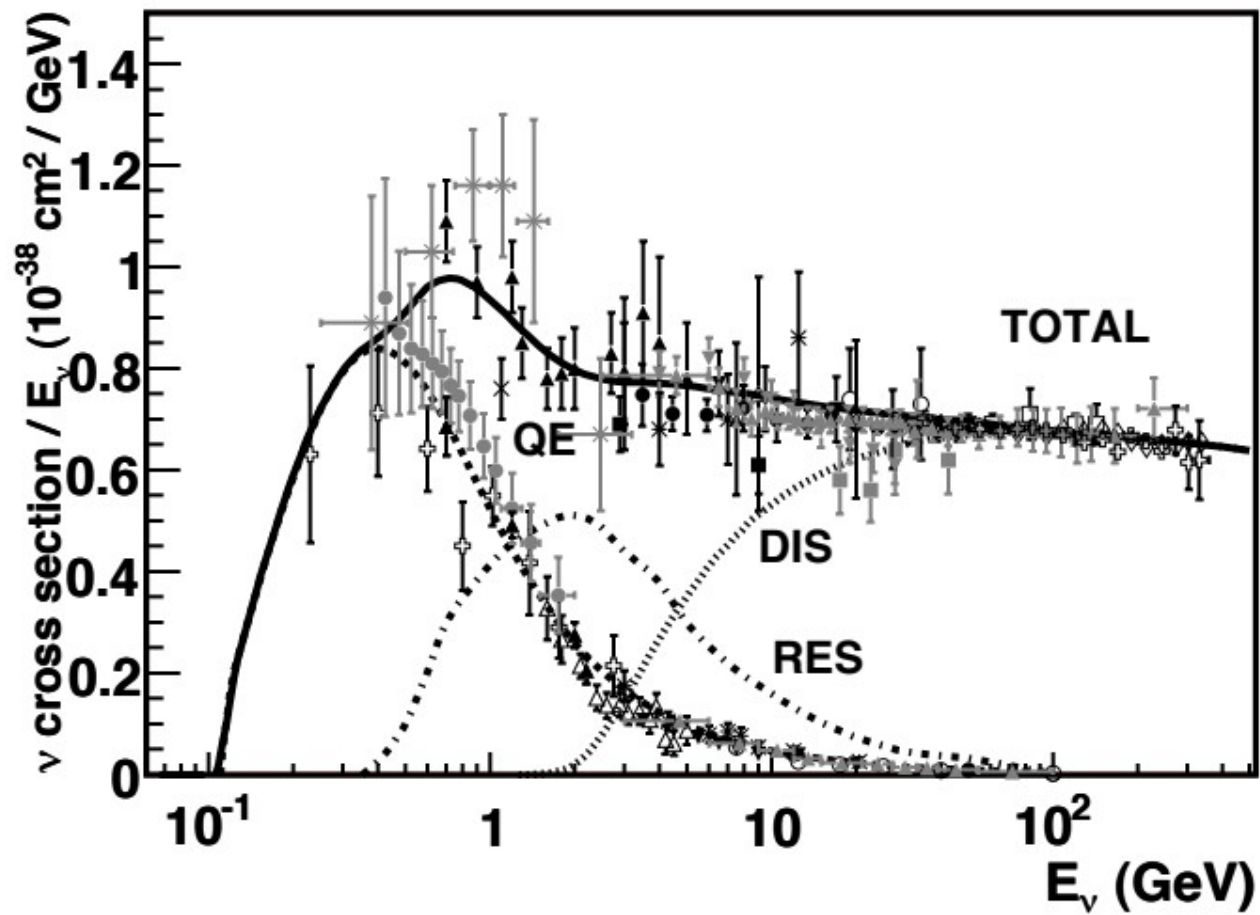


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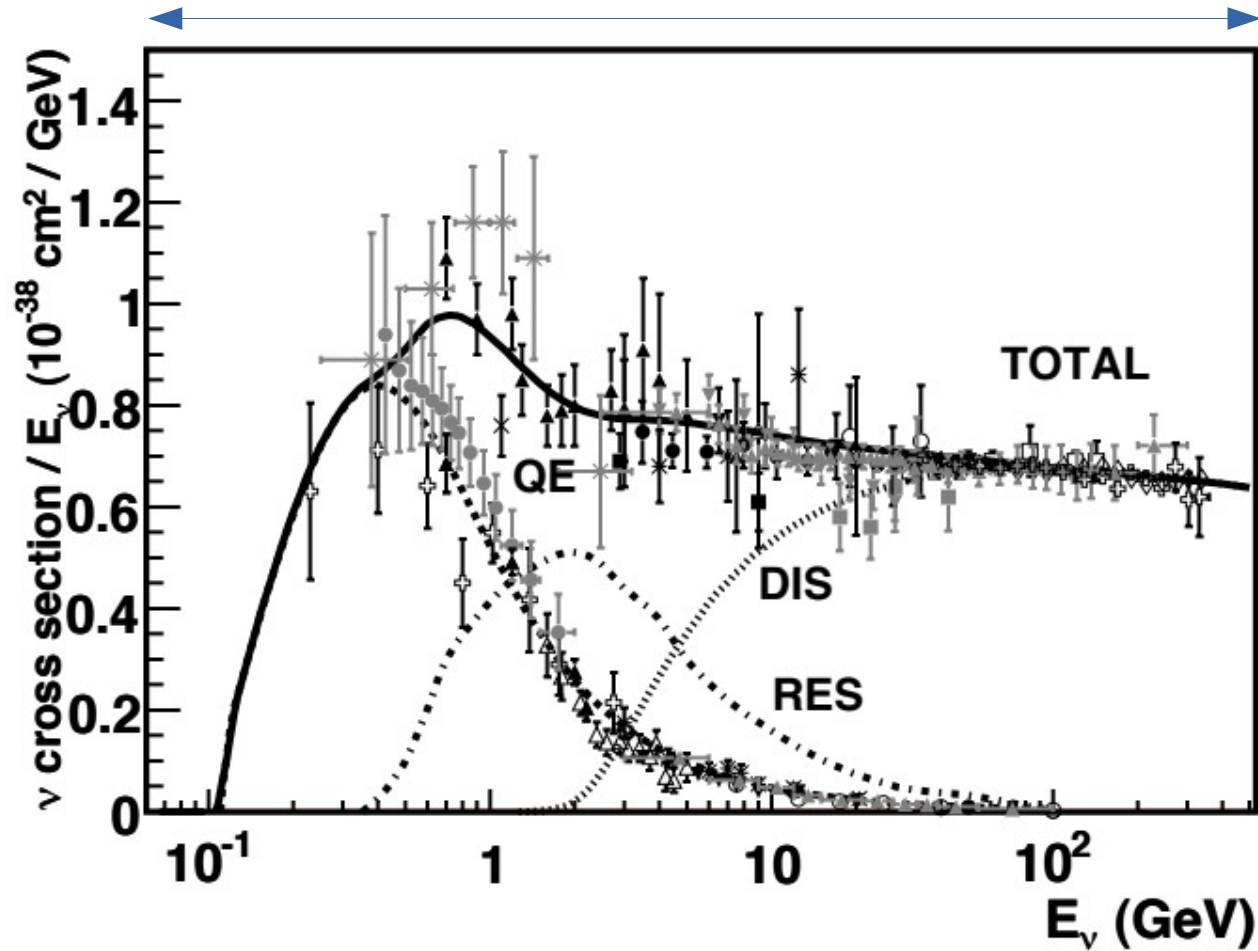
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More: 1907.08690  
Argüelles, MB, Kheirandish, Palomares-Ruiz, Salvadó, Vincent



Particle Data Group

## Accelerator experiments

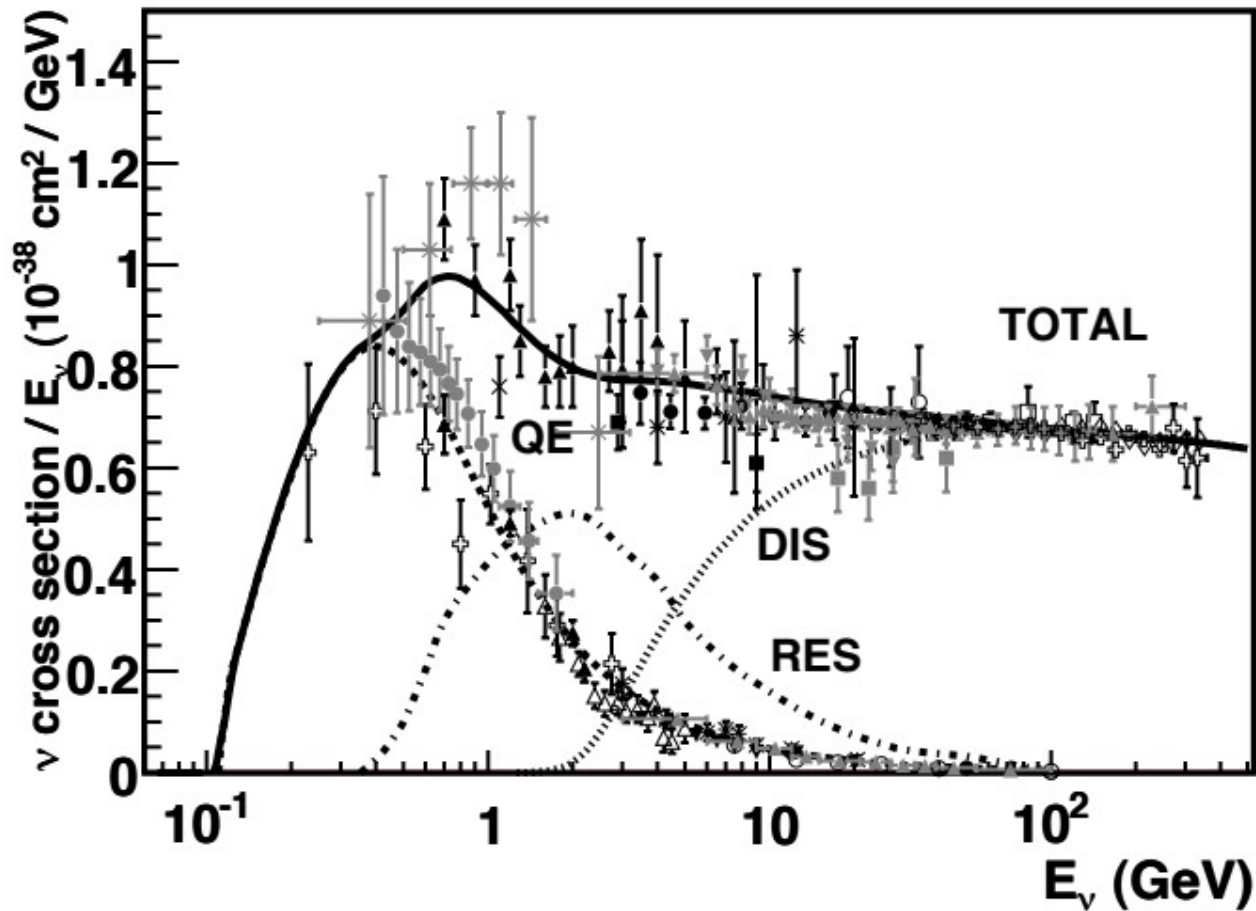


Particle Data Group



## Accelerator experiments

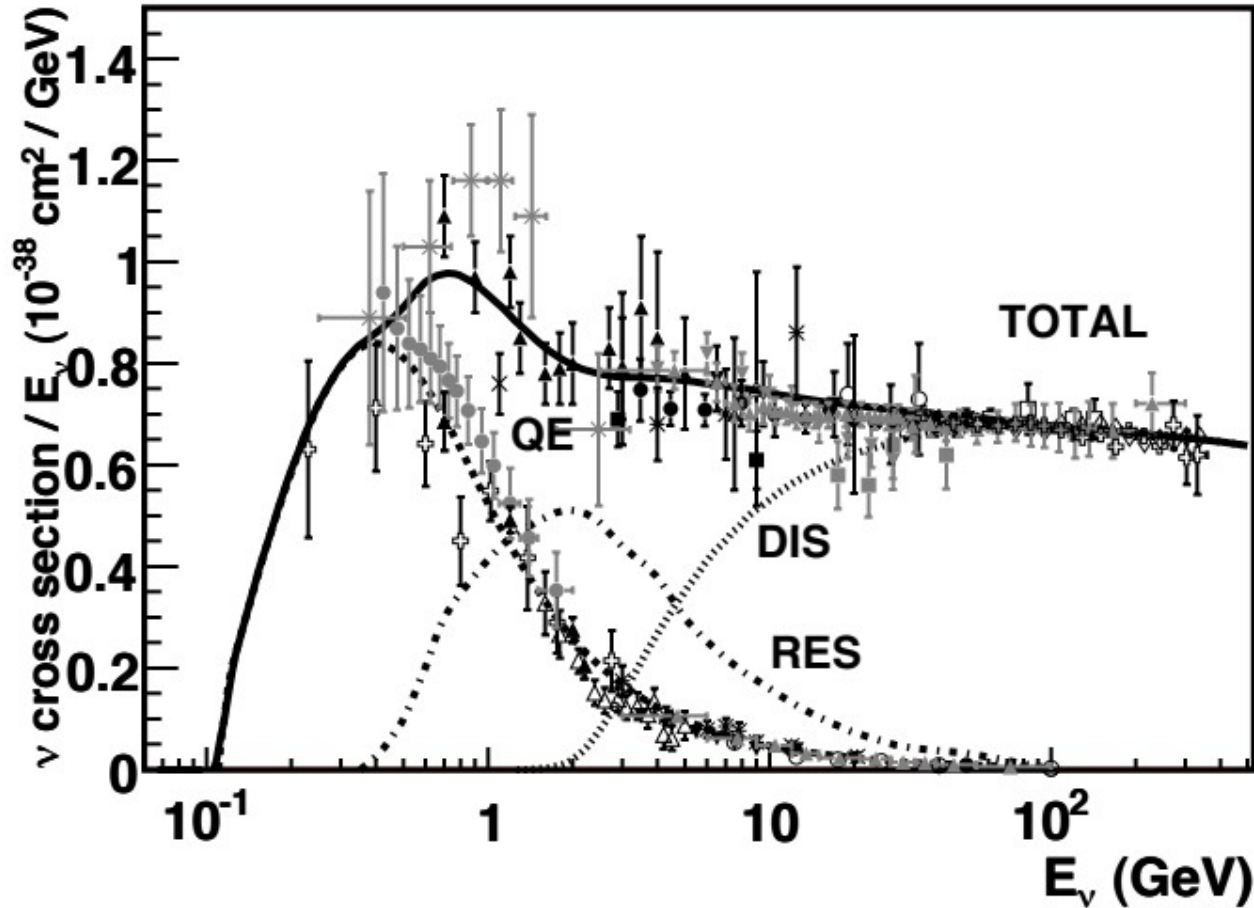
One recent  
measurement  
(COHERENT)



Particle Data Group

## Accelerator experiments

One recent  
measurement  
(COHERENT)

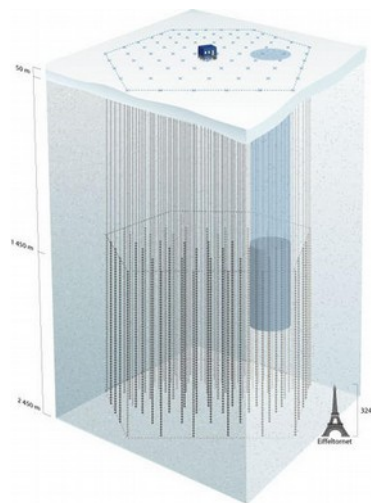
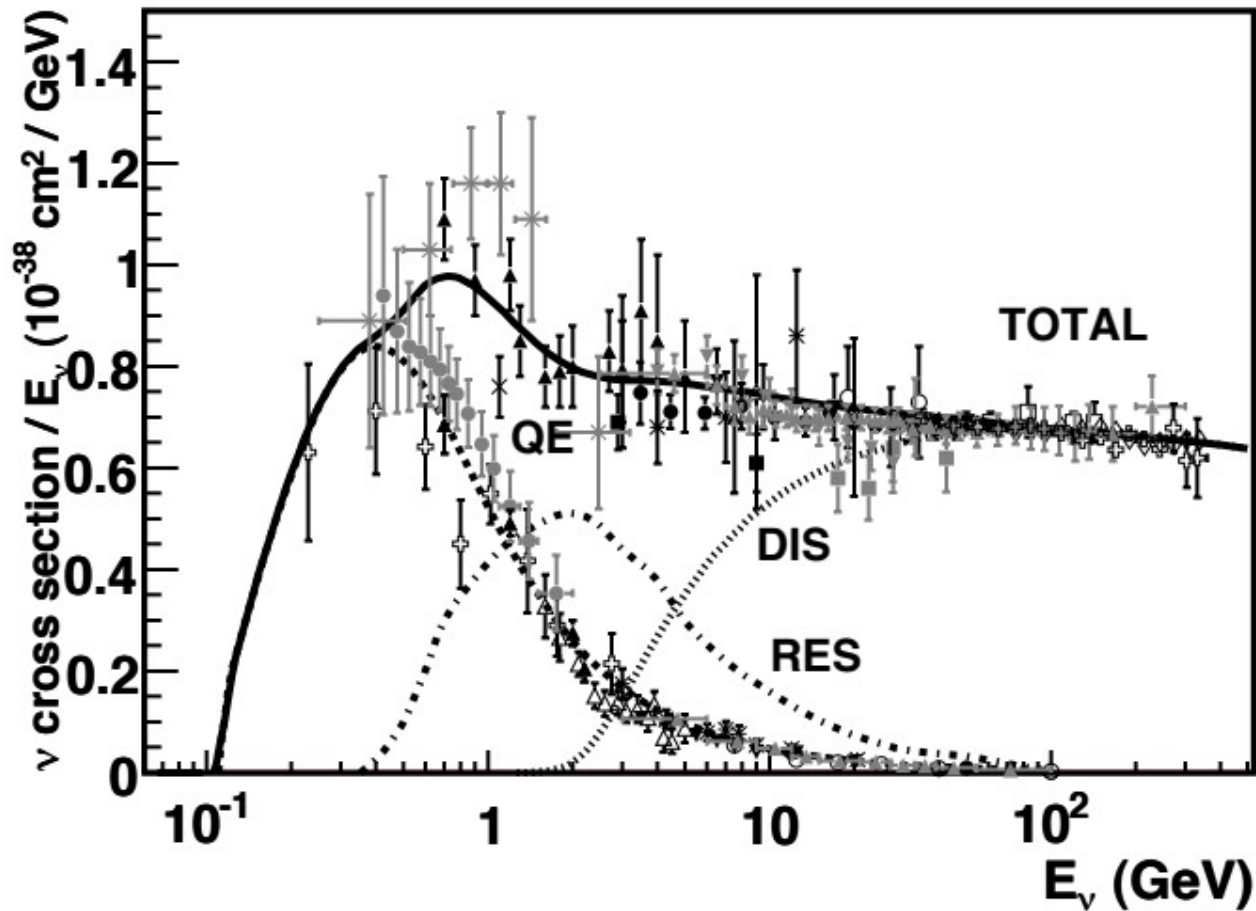


No  
measurements  
... until recently!

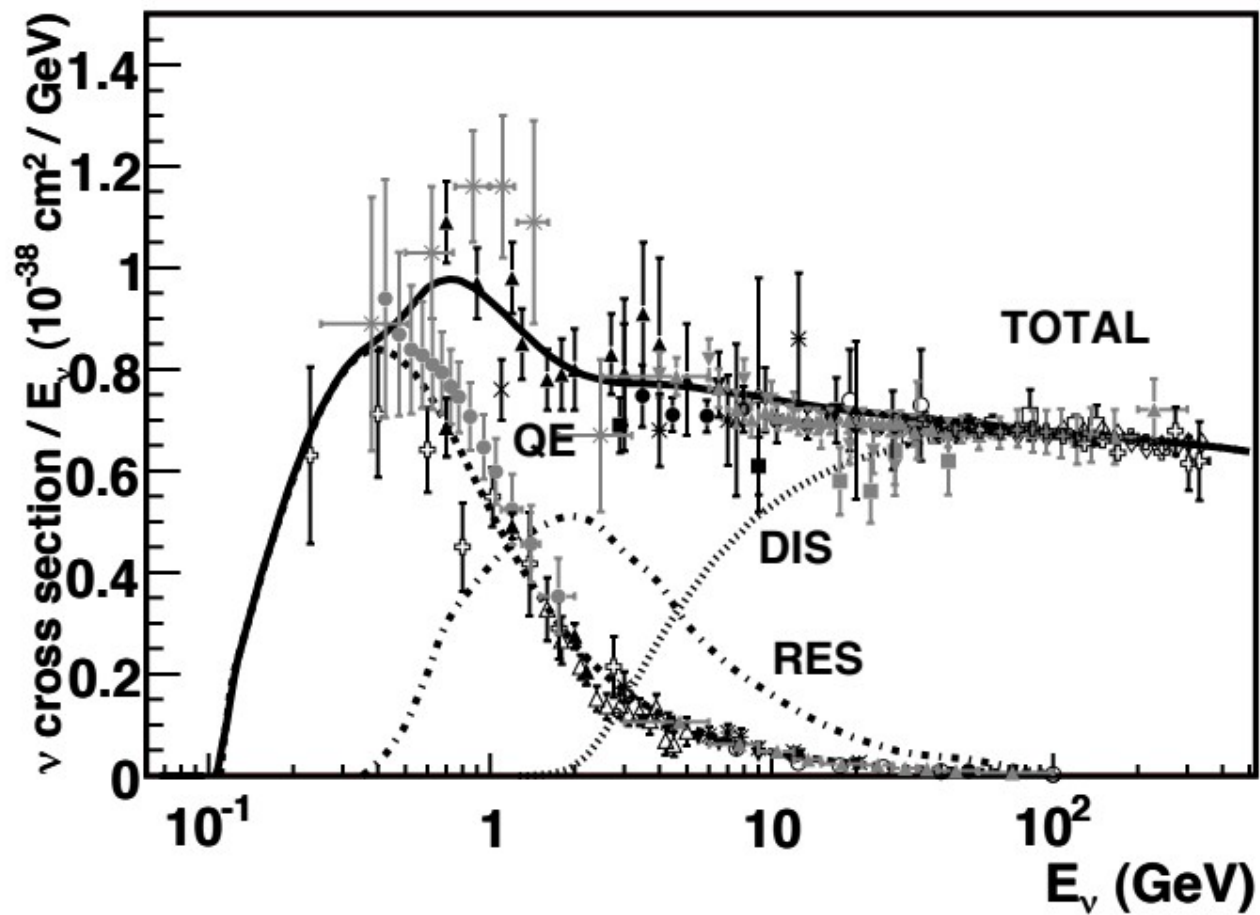


## Accelerator experiments

One recent  
measurement  
(COHERENT)



Particle Data Group

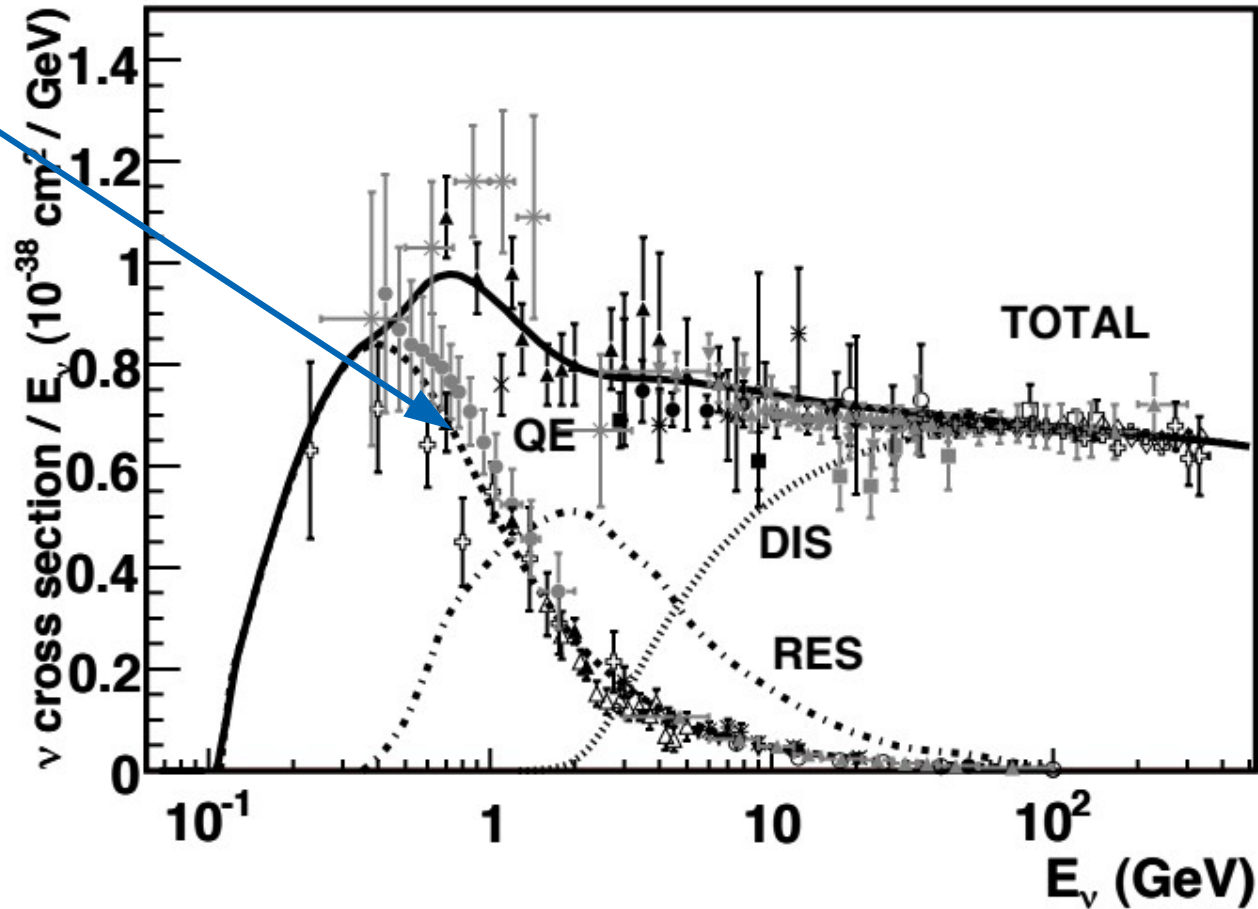


Particle Data Group

Quasi-elastic  
scattering:

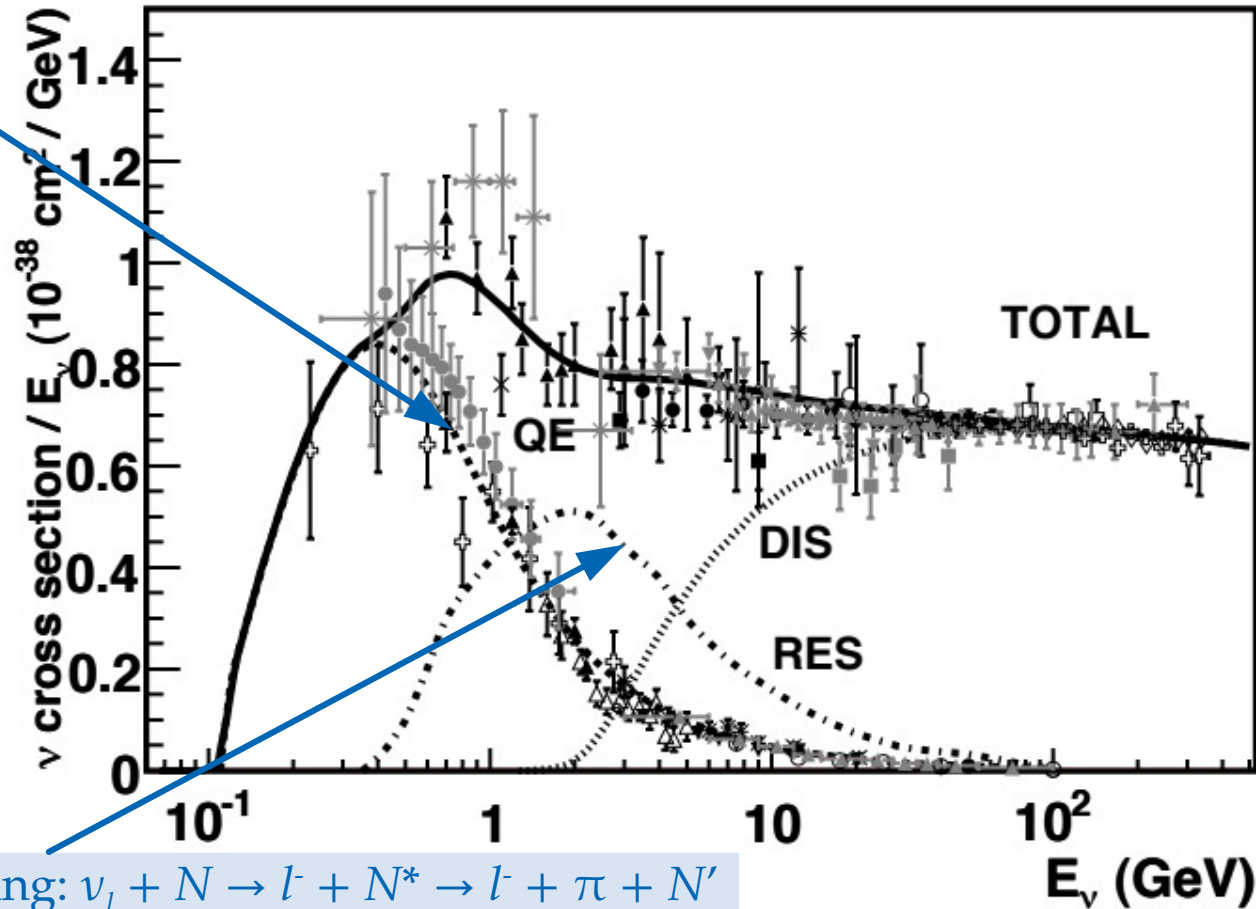
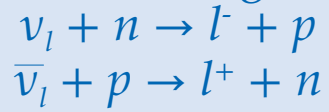
$$\nu_l + n \rightarrow l^- + p$$

$$\bar{\nu}_l + p \rightarrow l^+ + n$$



Particle Data Group

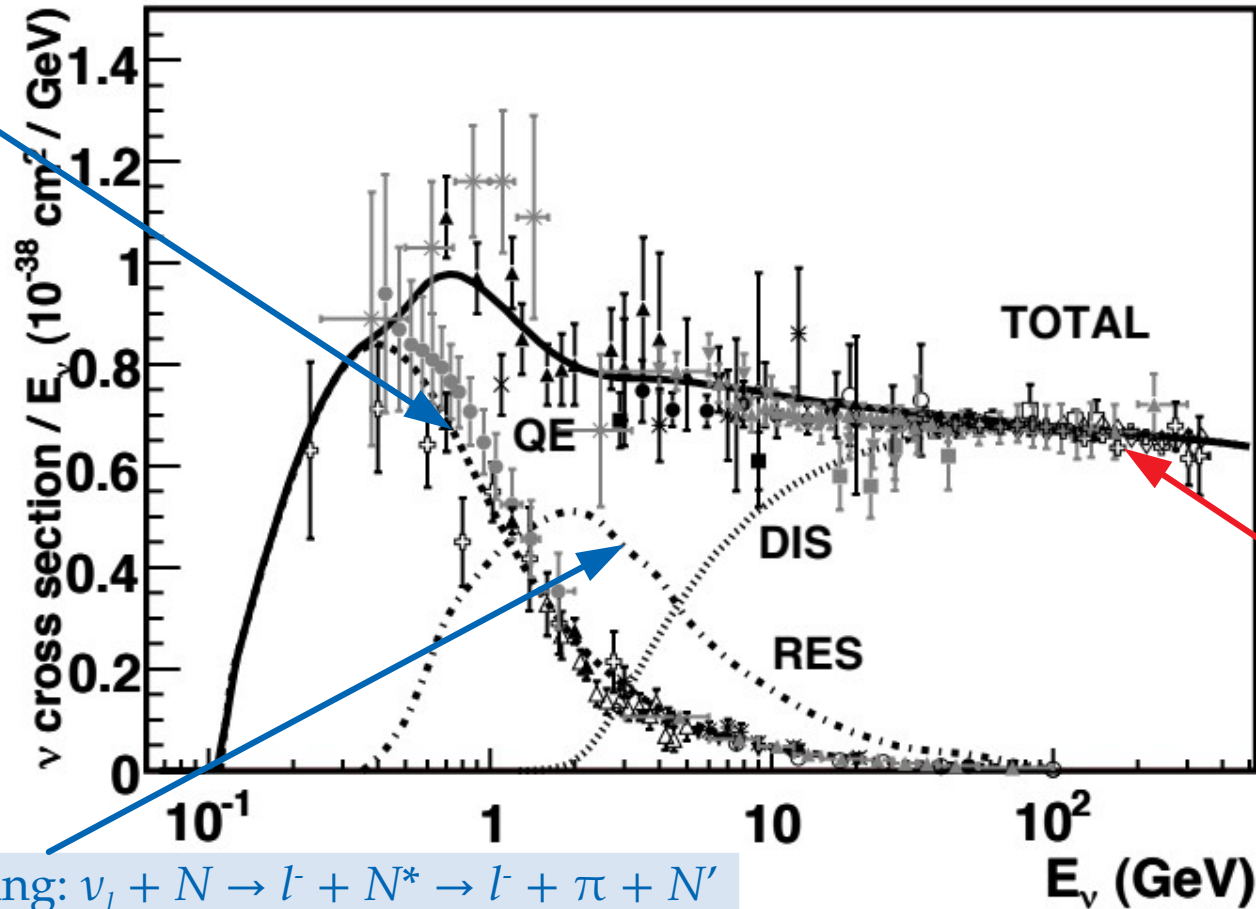
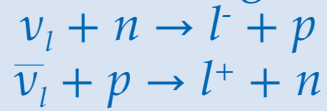
Quasi-elastic  
scattering:



Resonant scattering:  $\nu_l + N \rightarrow l^- + N^* \rightarrow l^- + \pi + N'$

Particle Data Group

Quasi-elastic  
scattering:



Deep inelastic  
scattering:  
 $\nu_l + N \rightarrow l^- + X$   
 $\bar{\nu}_l + N \rightarrow l^+ + X$

Resonant scattering:  $\nu_l + N \rightarrow l^- + N^* \rightarrow l^- + \pi + N'$

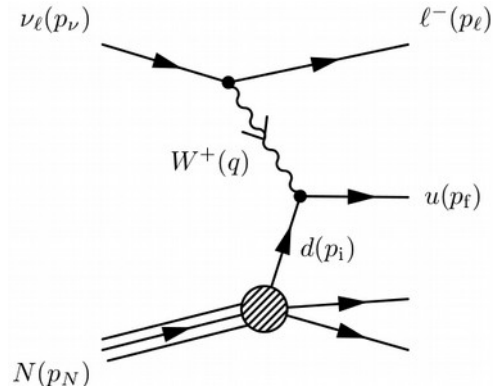
Particle Data Group

Extrapolating the cross section to high energies



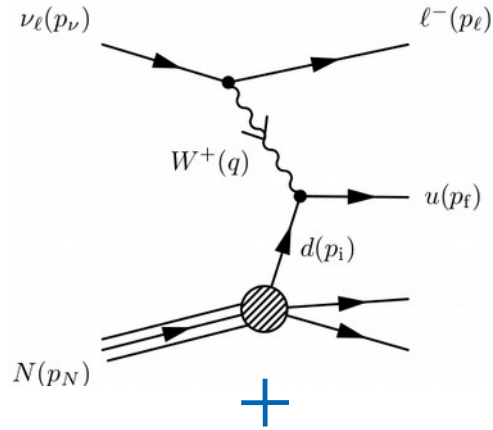
# Extrapolating the cross section to high energies

SM

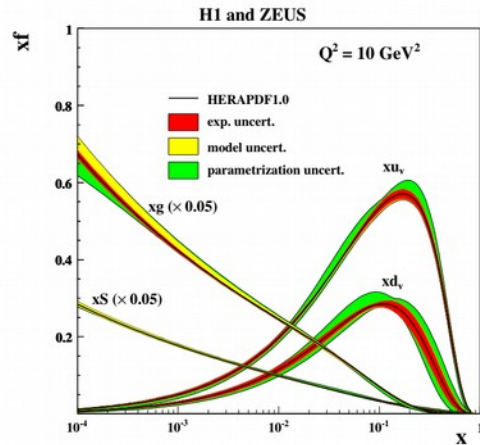


# Extrapolating the cross section to high energies

SM

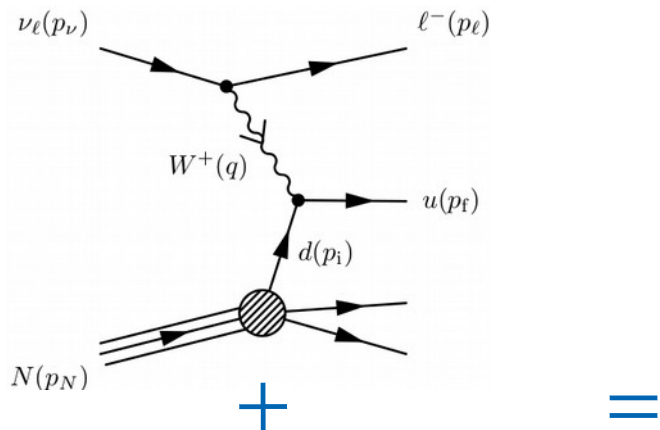


PDFs

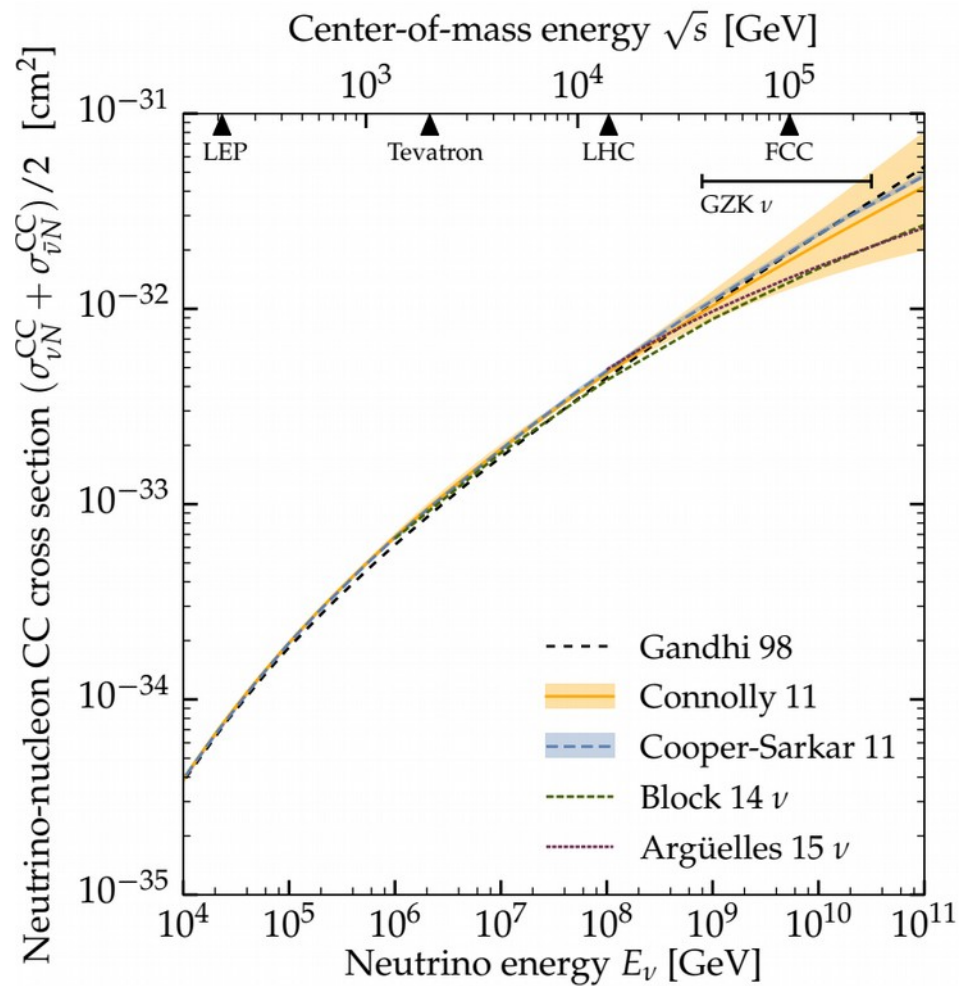
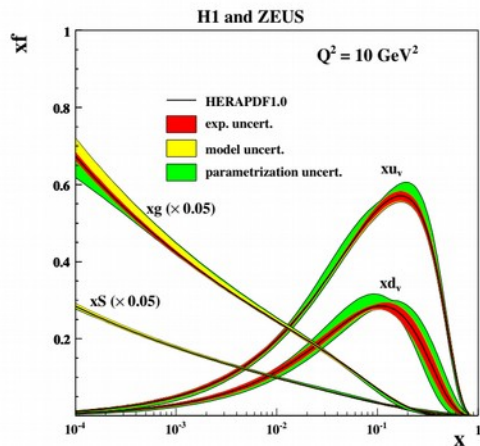


# Extrapolating the cross section to high energies

SM

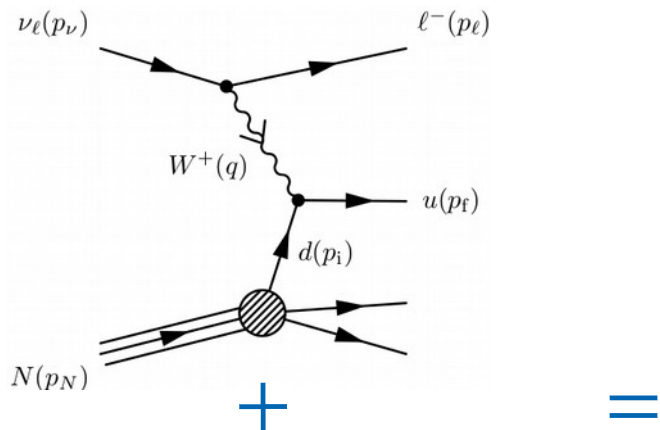


PDFs

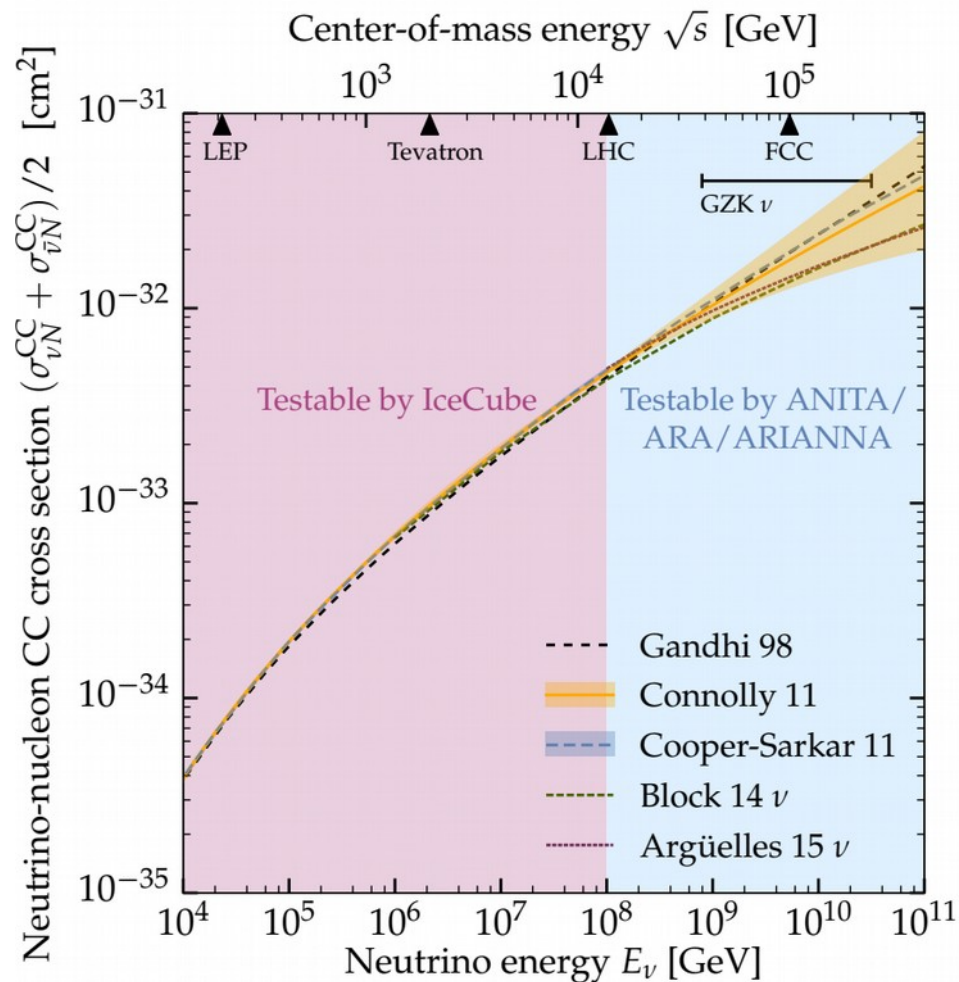
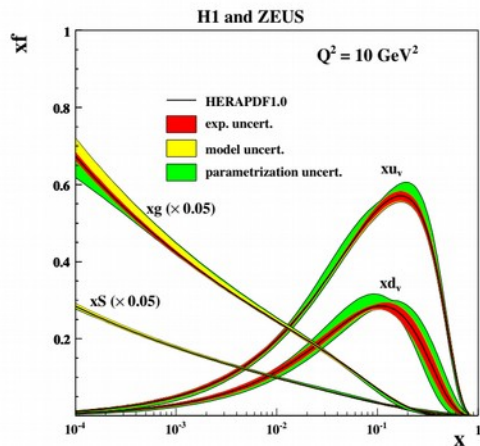


# Extrapolating the cross section to high energies

SM



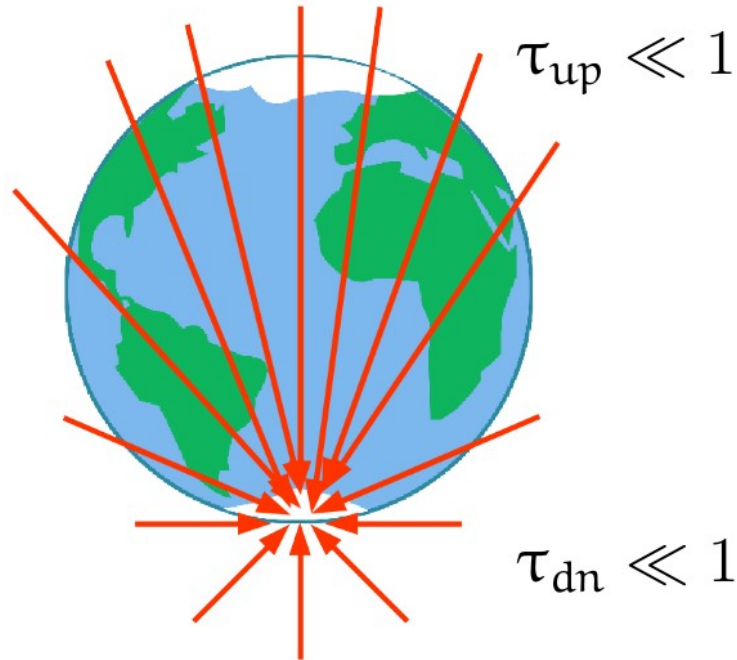
PDFs



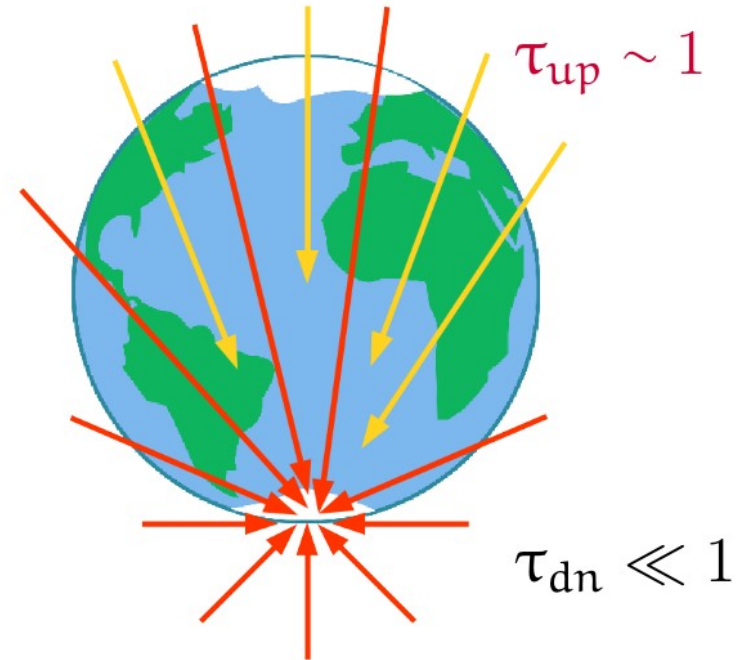
# Measuring the high-energy cross section

$$\text{Optical depth to } \nu N \text{ int's} = \frac{\text{Distance from Earth's surface to IceCube}}{\text{Mean free path inside Earth}} \equiv \tau(E_\nu, \theta_z) \propto \sigma_{\nu N}$$

Below  $\sim 10$  TeV: Earth is transparent



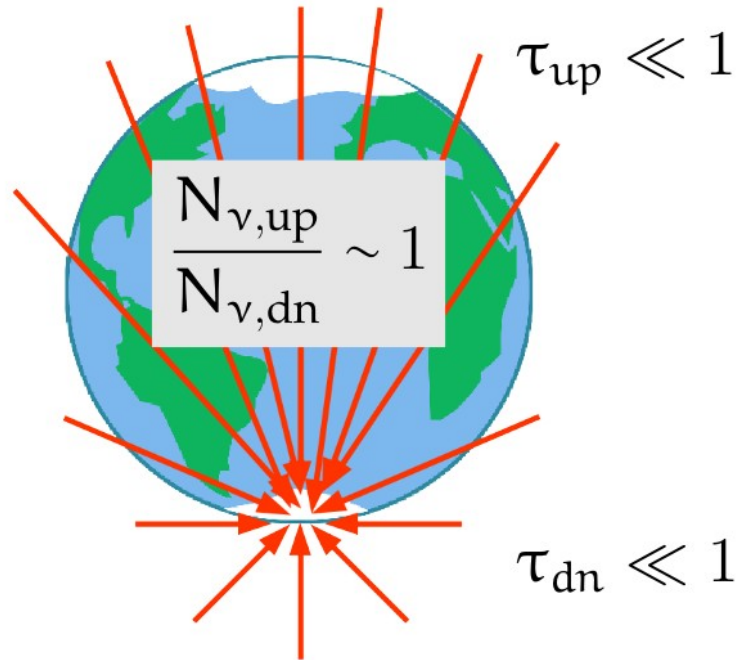
Above  $\sim 10$  TeV: Earth is opaque



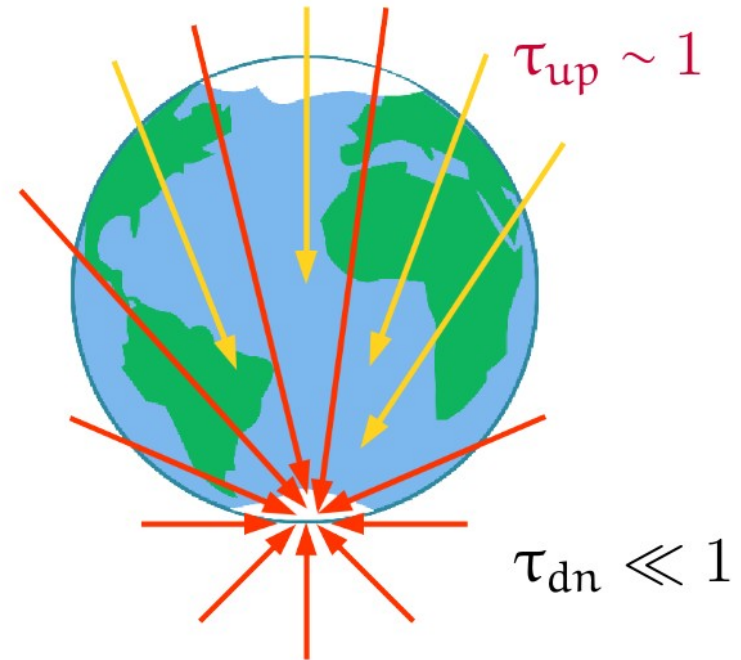
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Below  $\sim 10$  TeV: Earth is transparent



Above  $\sim 10$  TeV: Earth is opaque

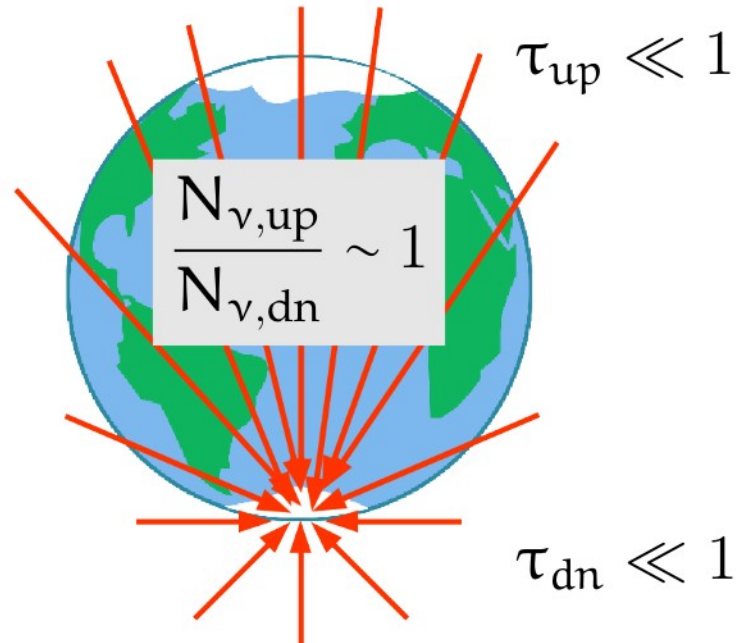




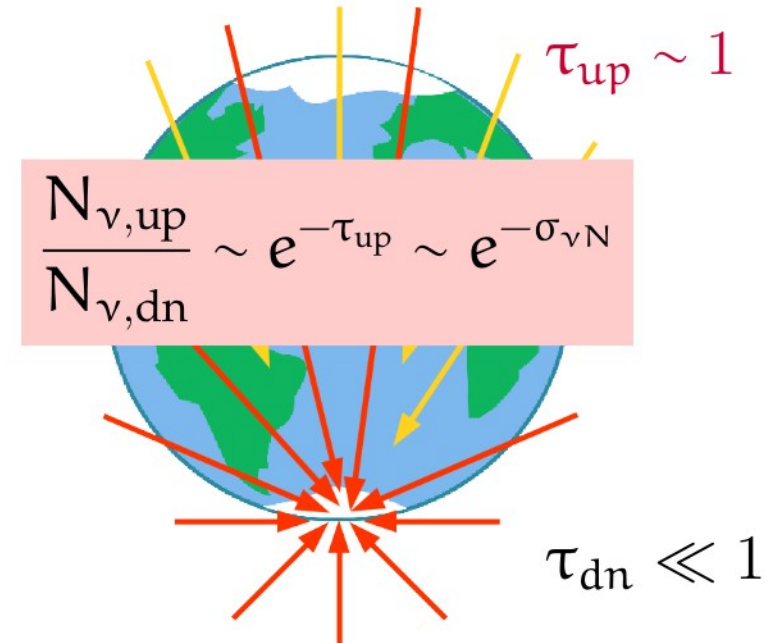
# Measuring the high-energy cross section

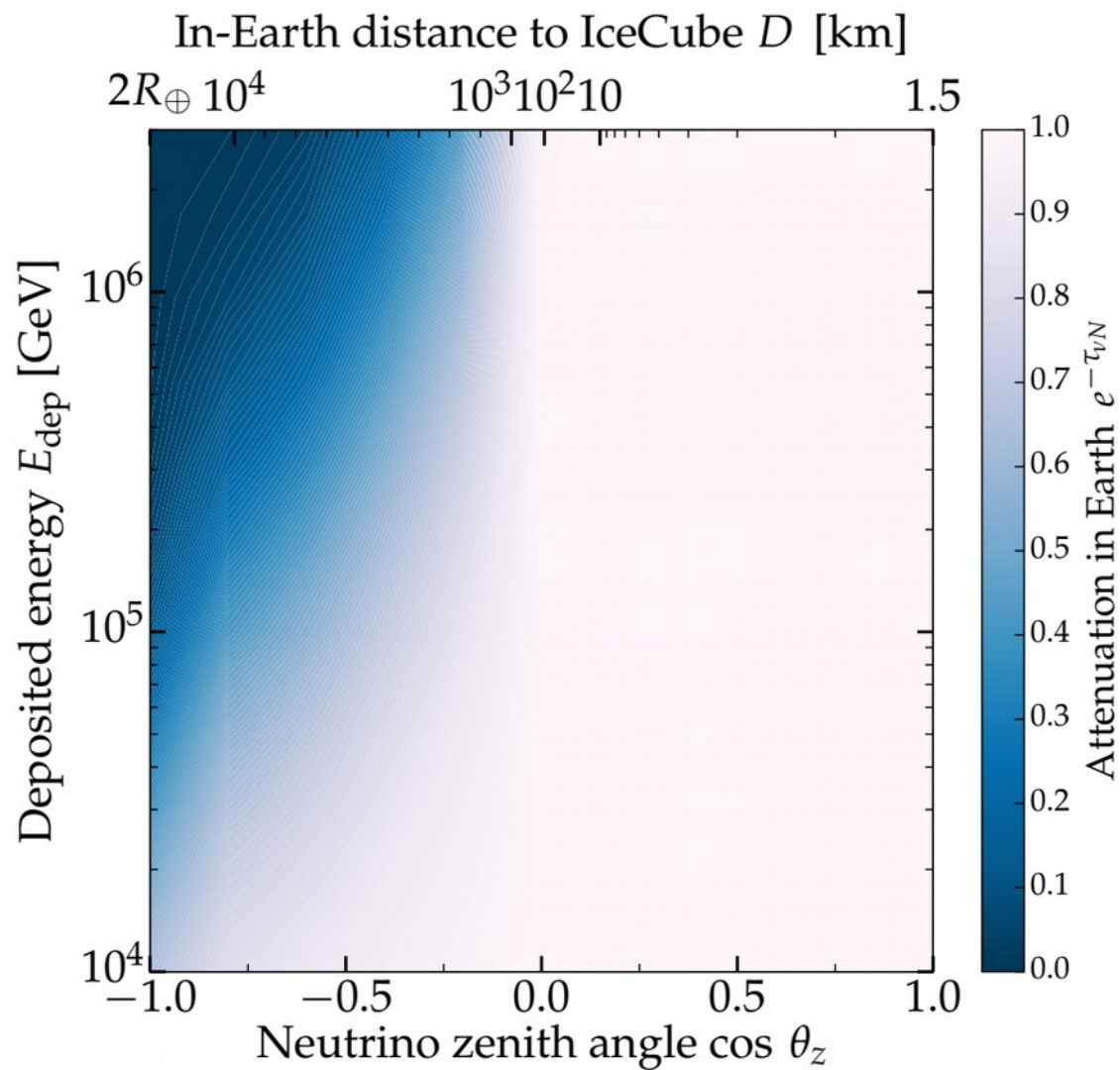
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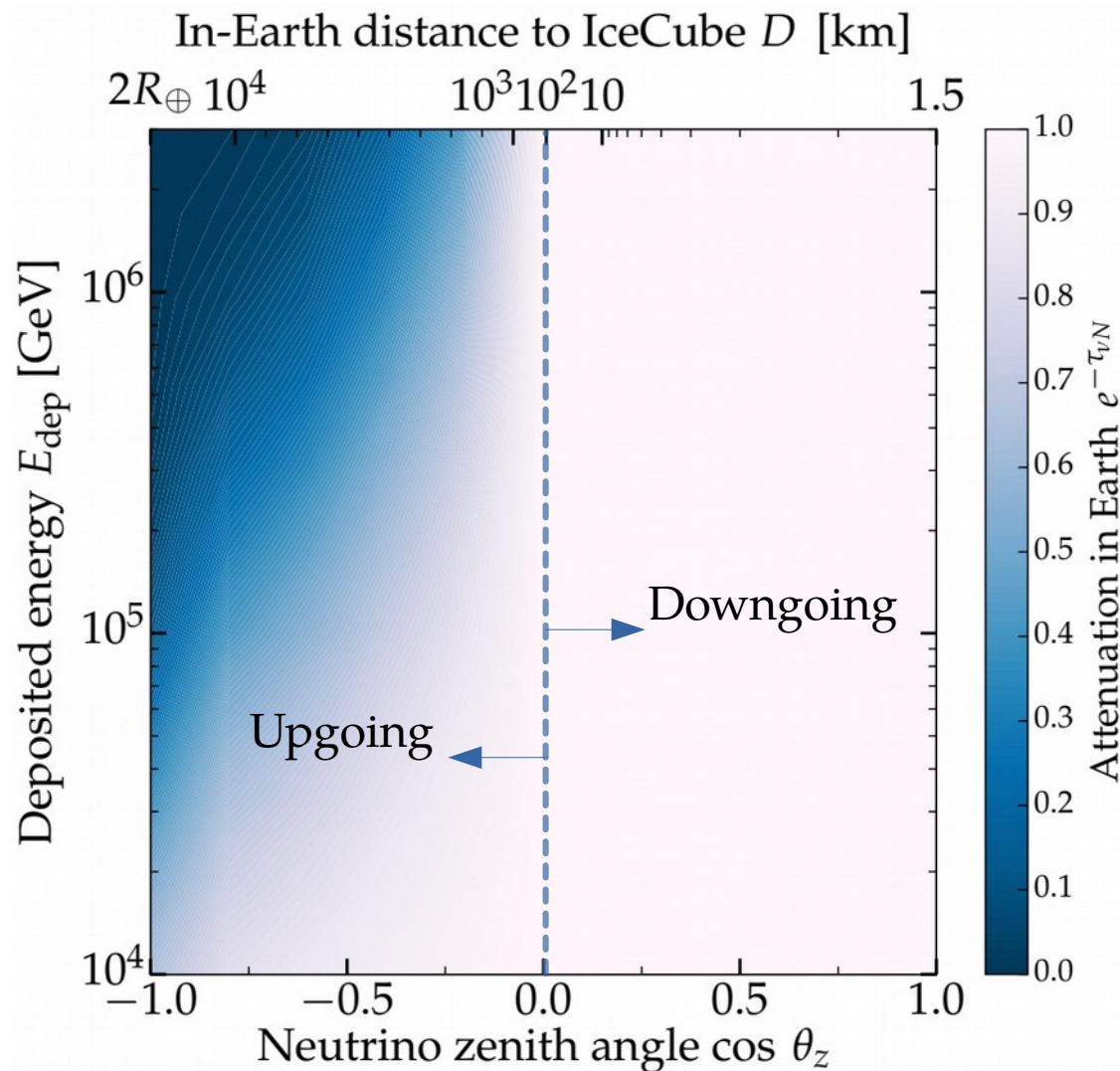
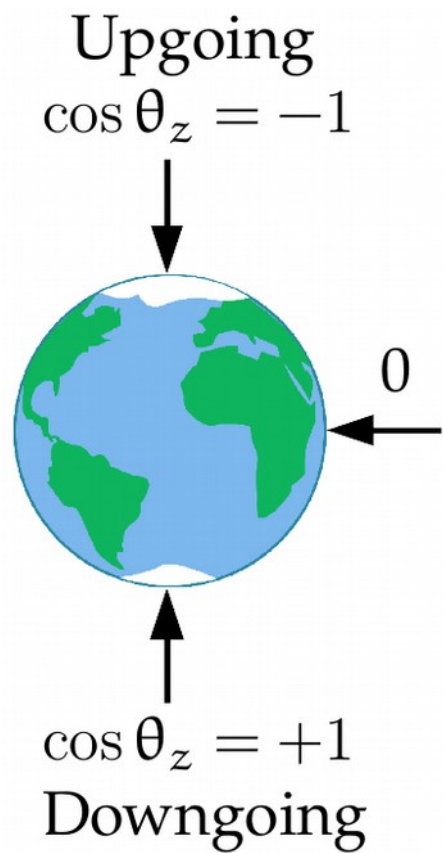
Below  $\sim 10$  TeV: Earth is transparent

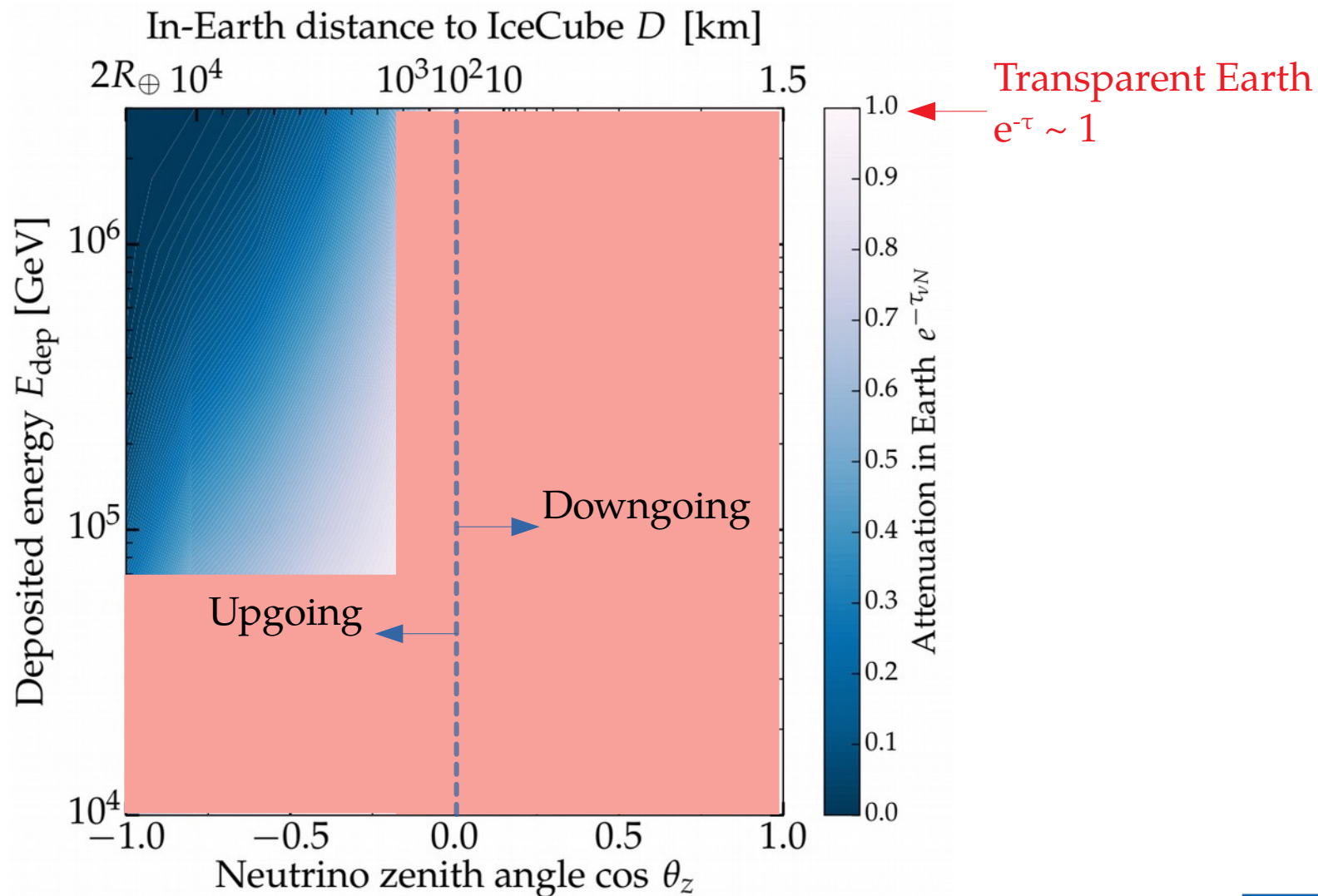
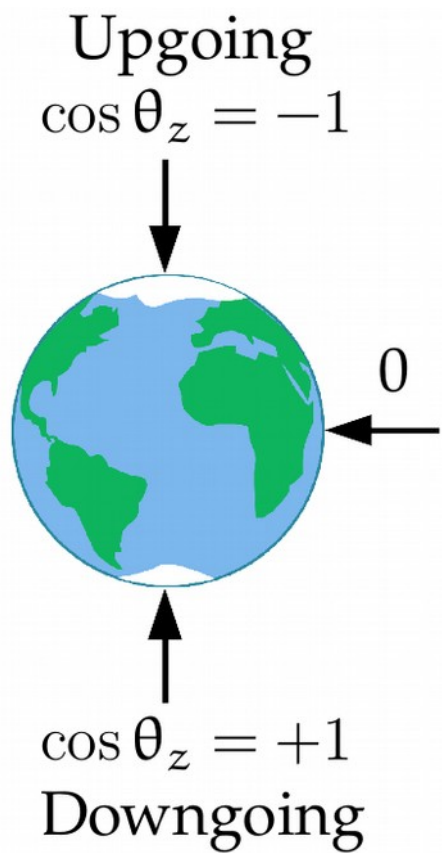


Above  $\sim 10$  TeV: Earth is opaque

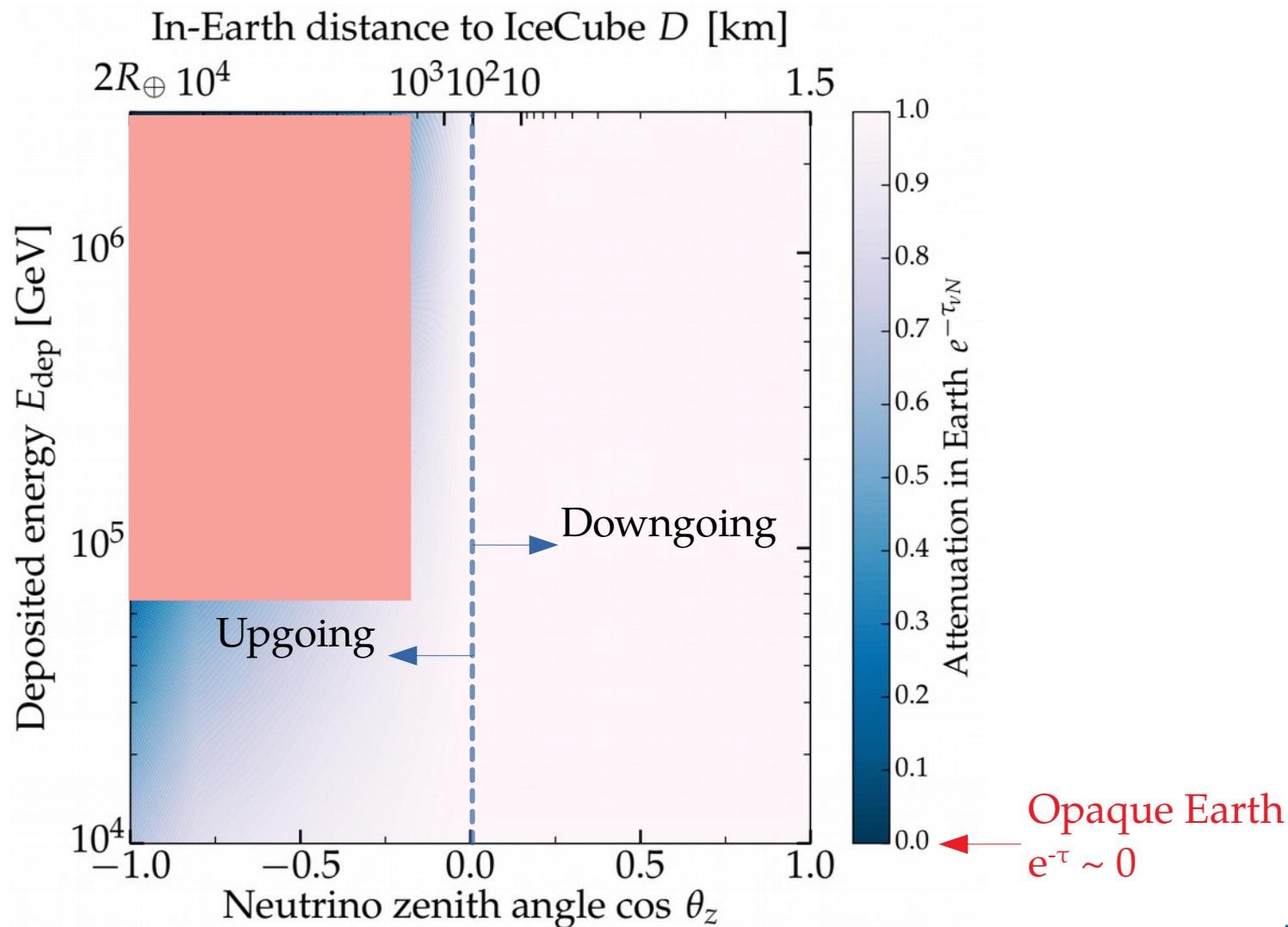
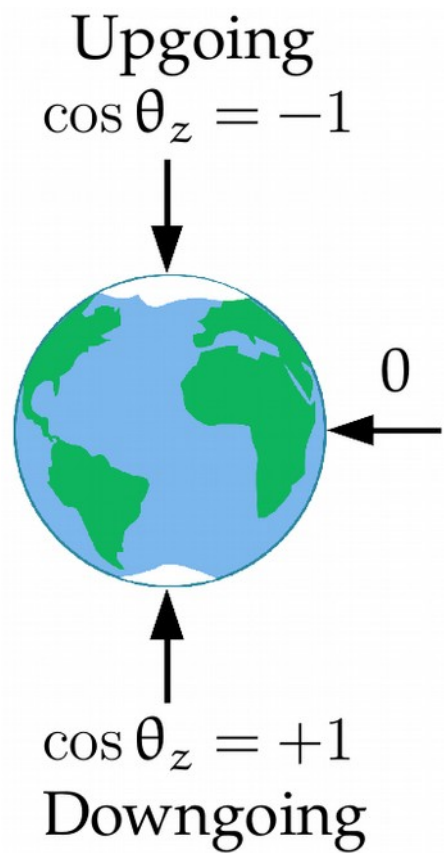


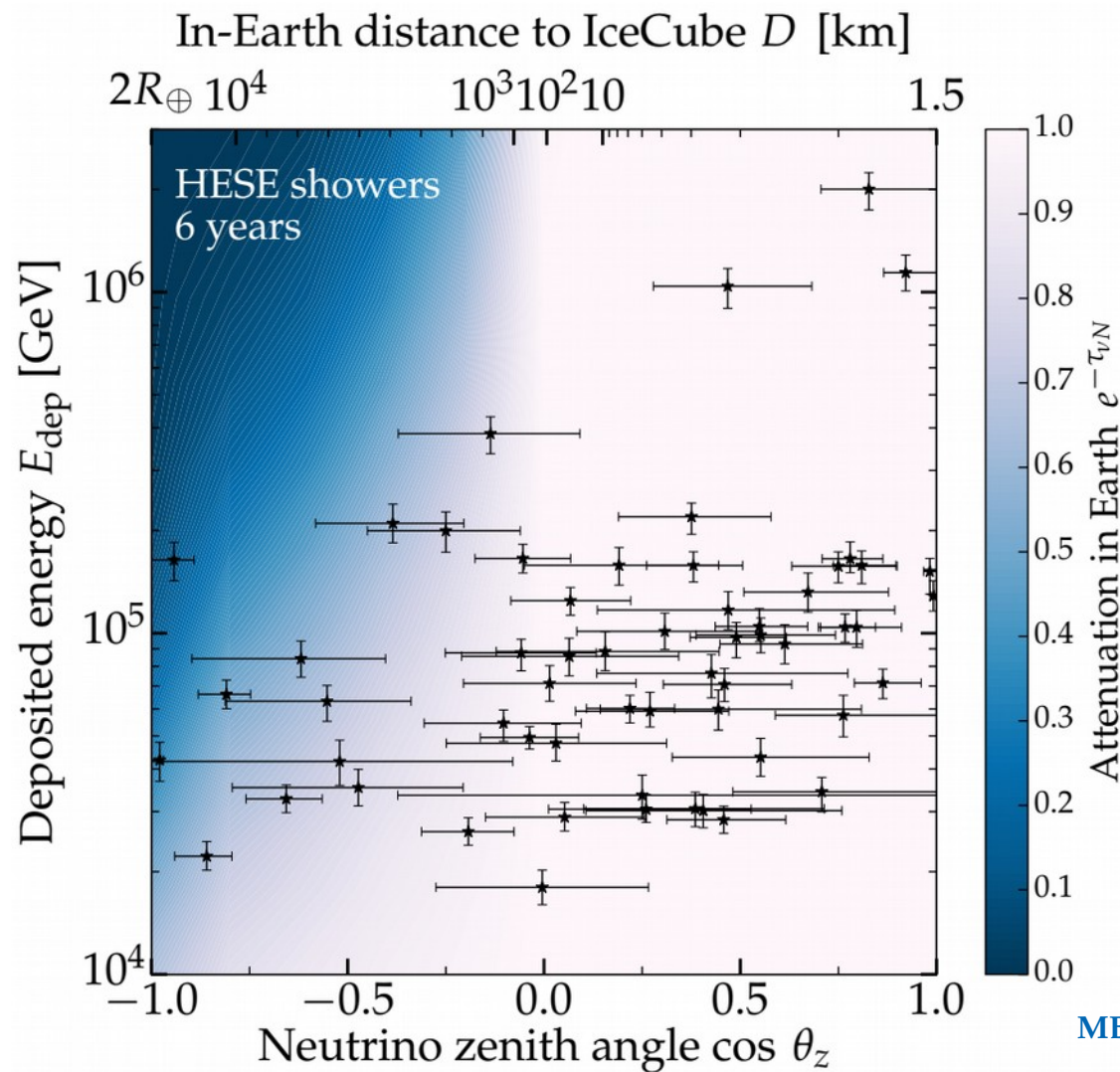






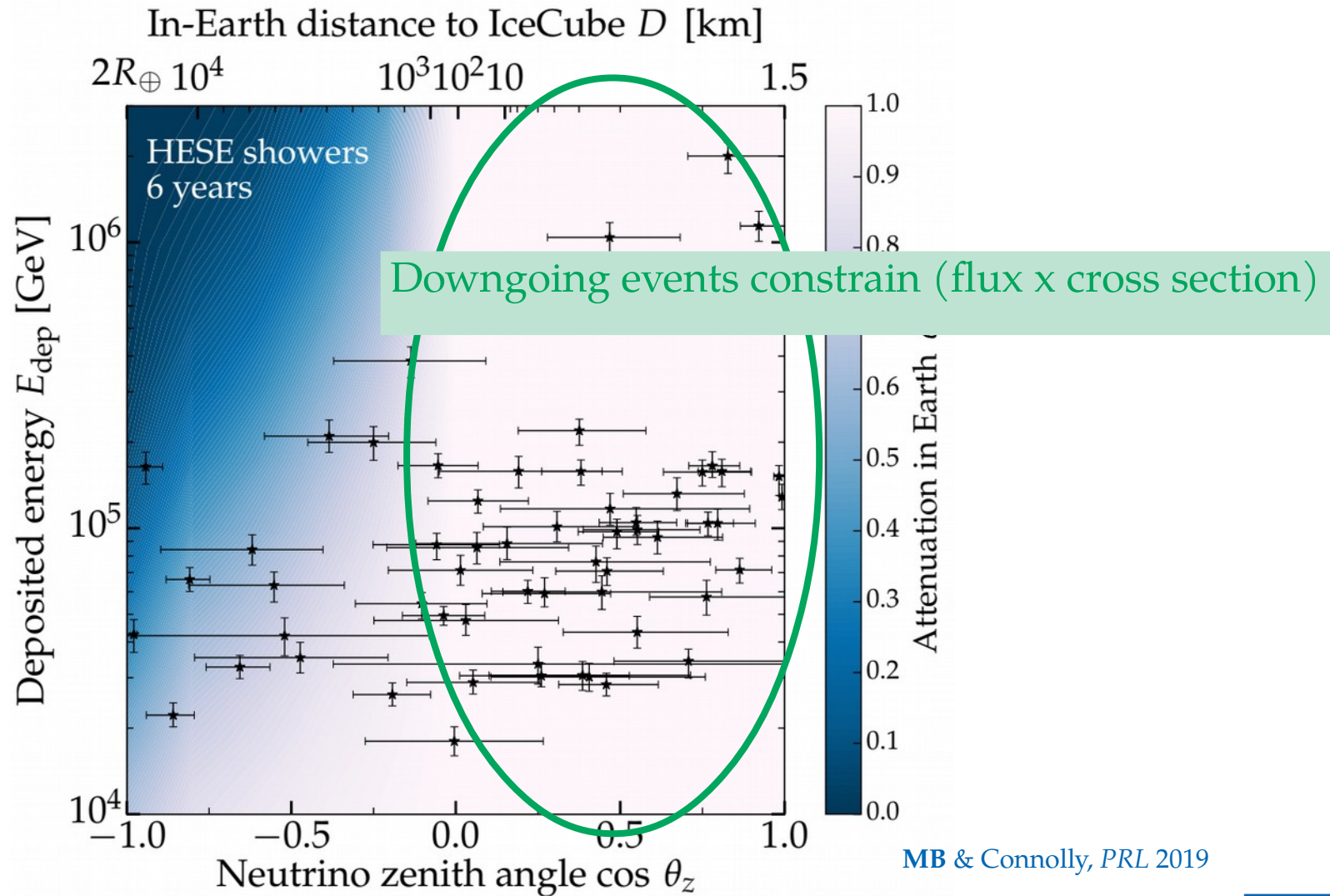






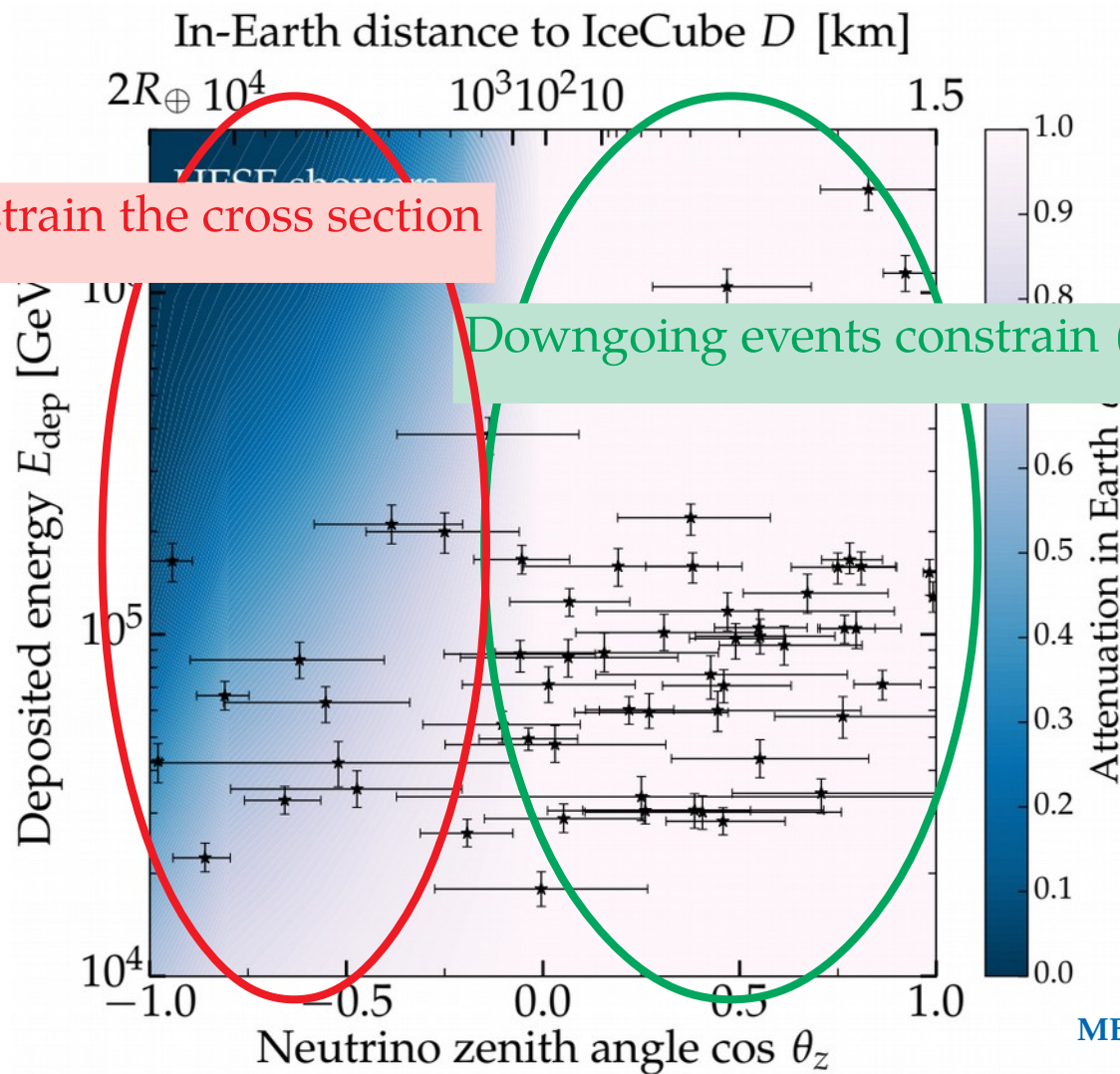
MB & Connolly, *PRL* 2019



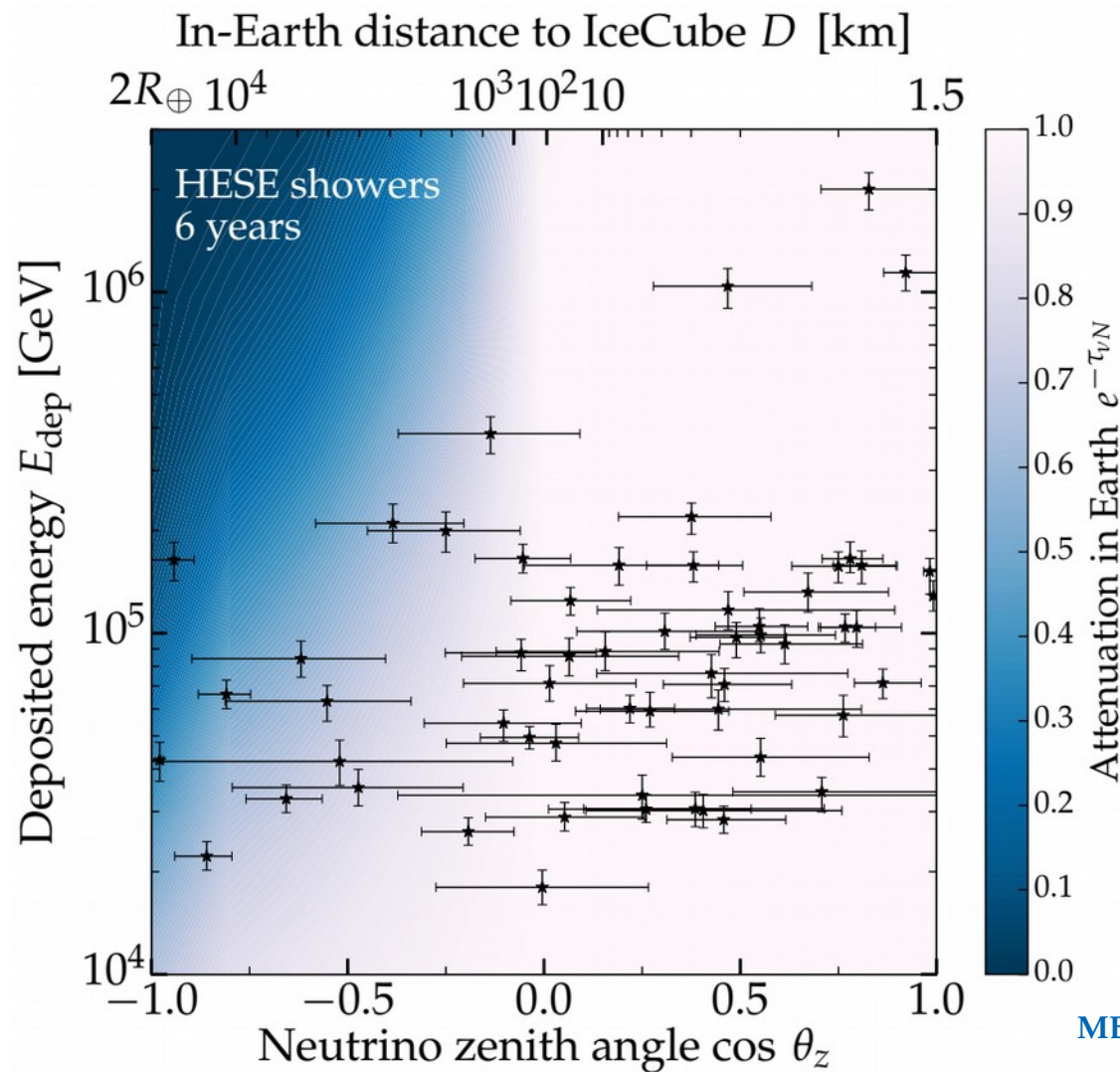


Upgoing events constrain the cross section

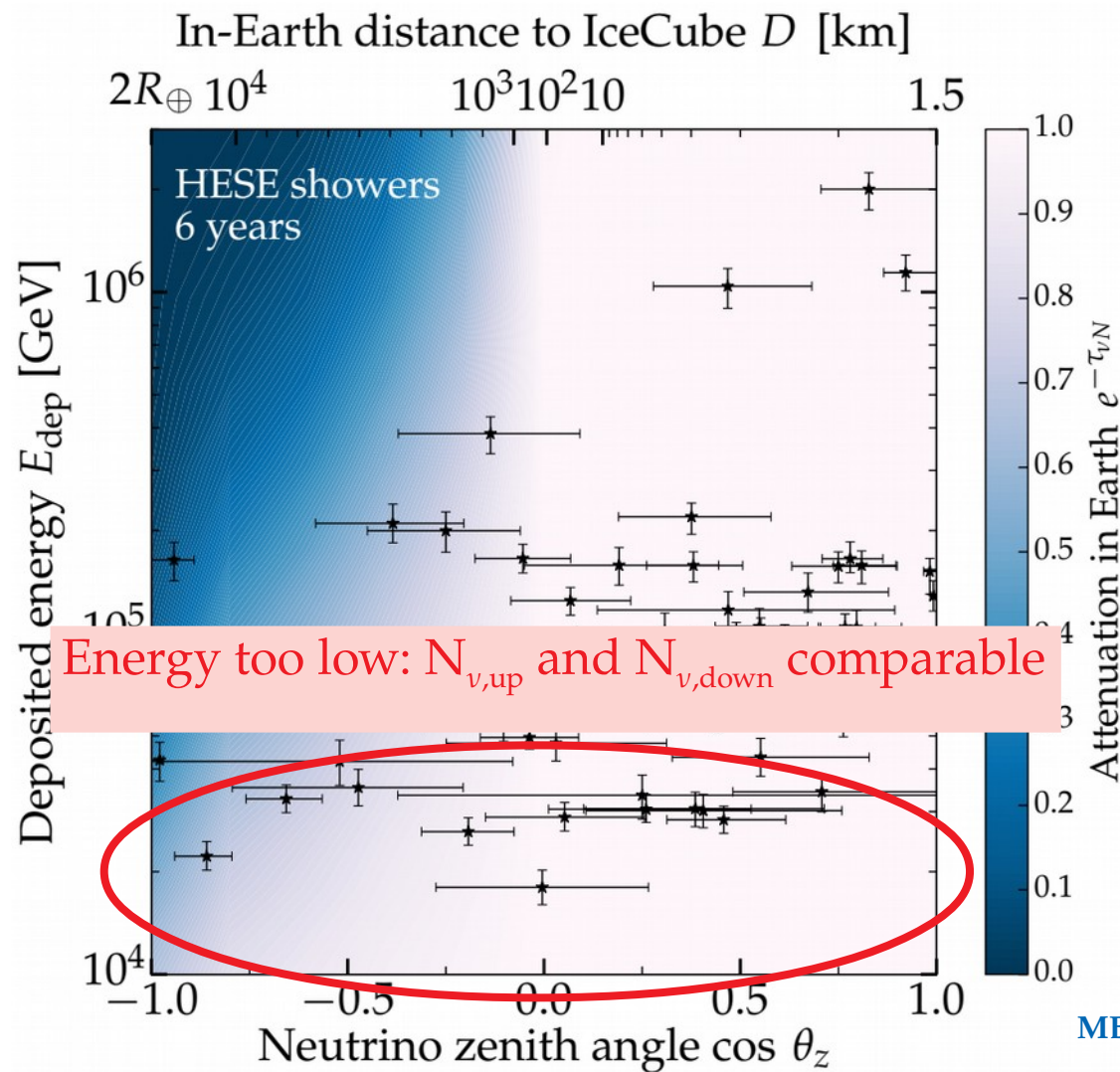
Downgoing events constrain (flux x cross section)



MB & Connolly, *PRL* 2019

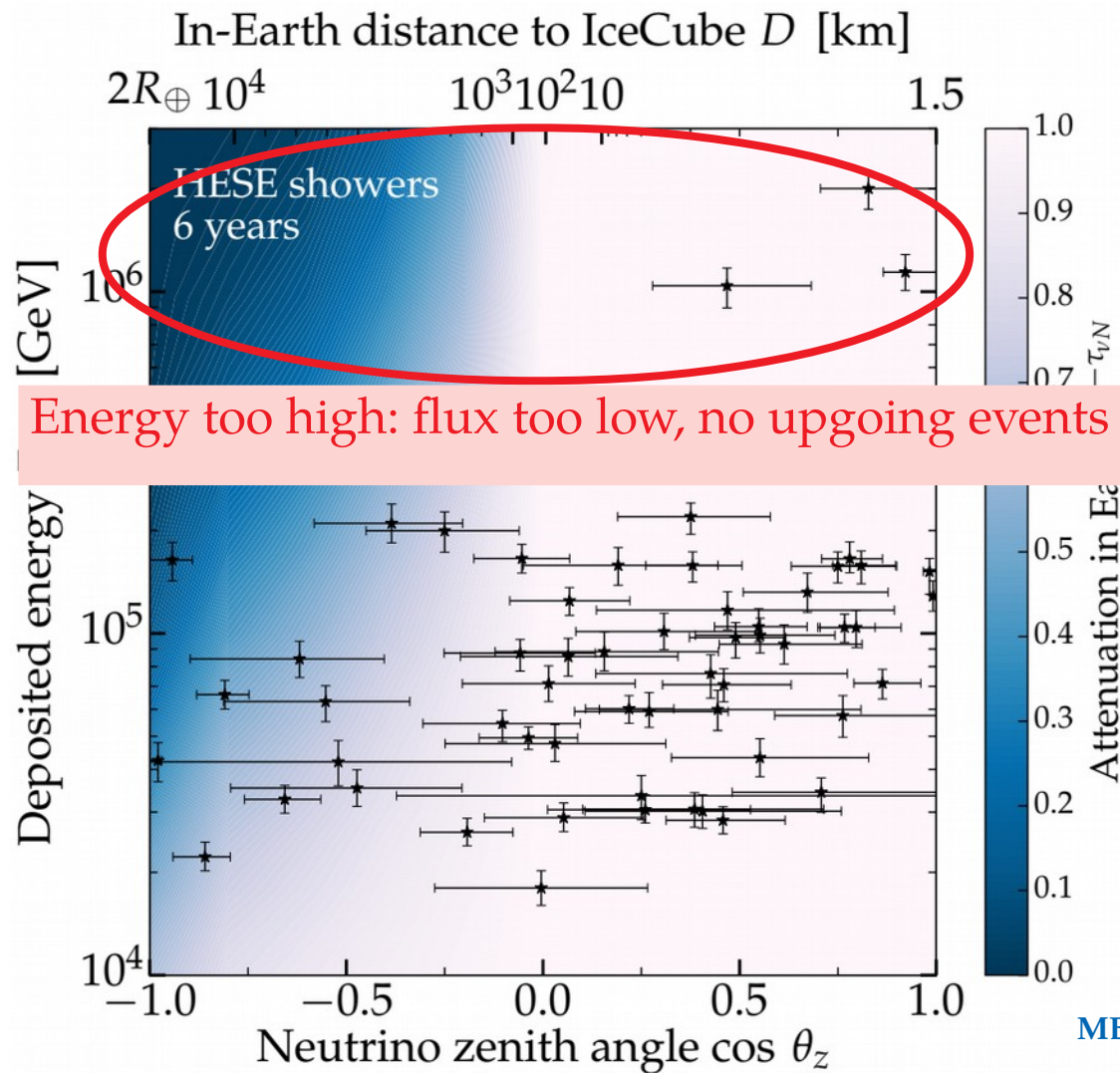


MB & Connolly, *PRL* 2019

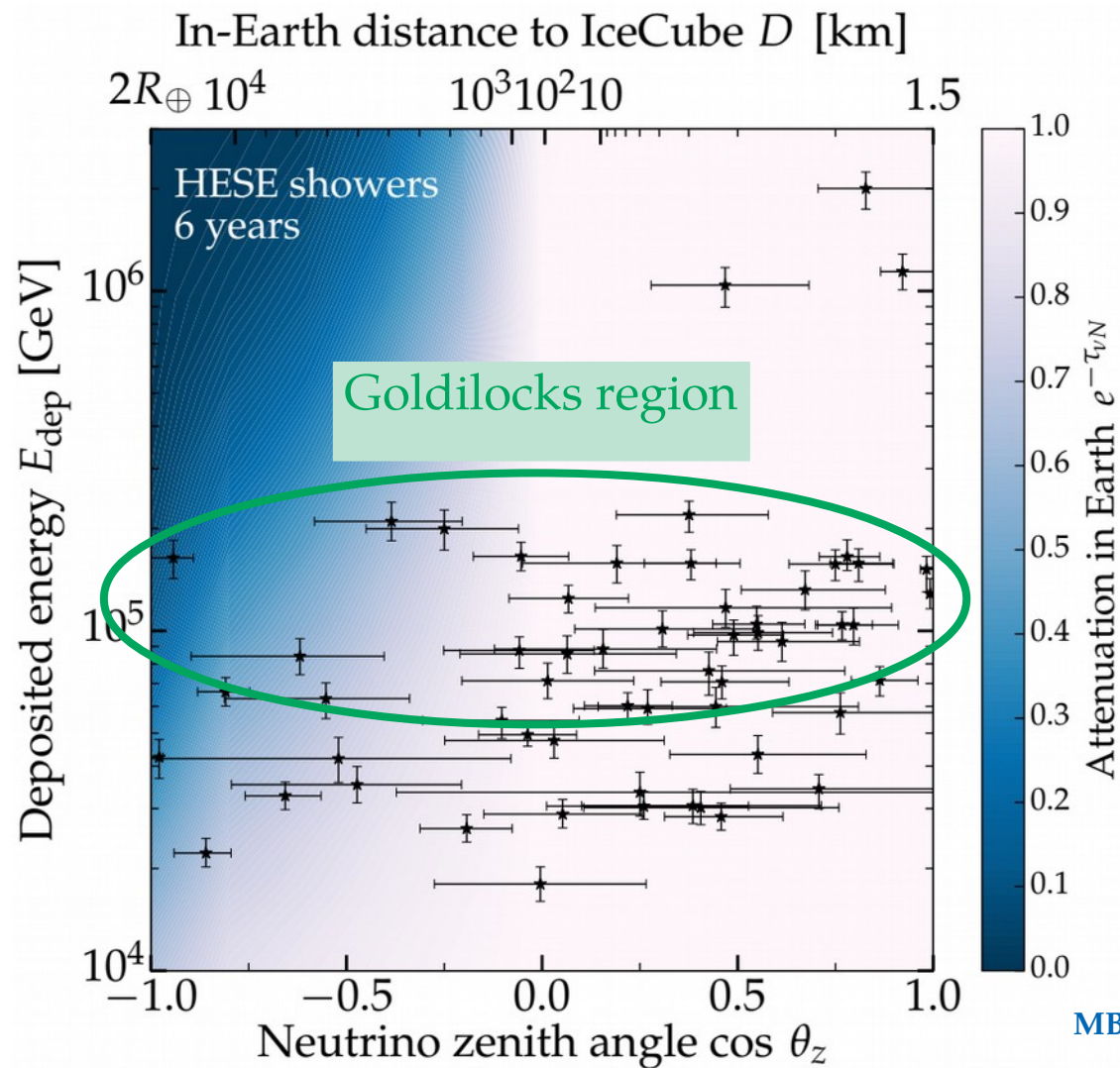


MB & Connolly, *PRL* 2019





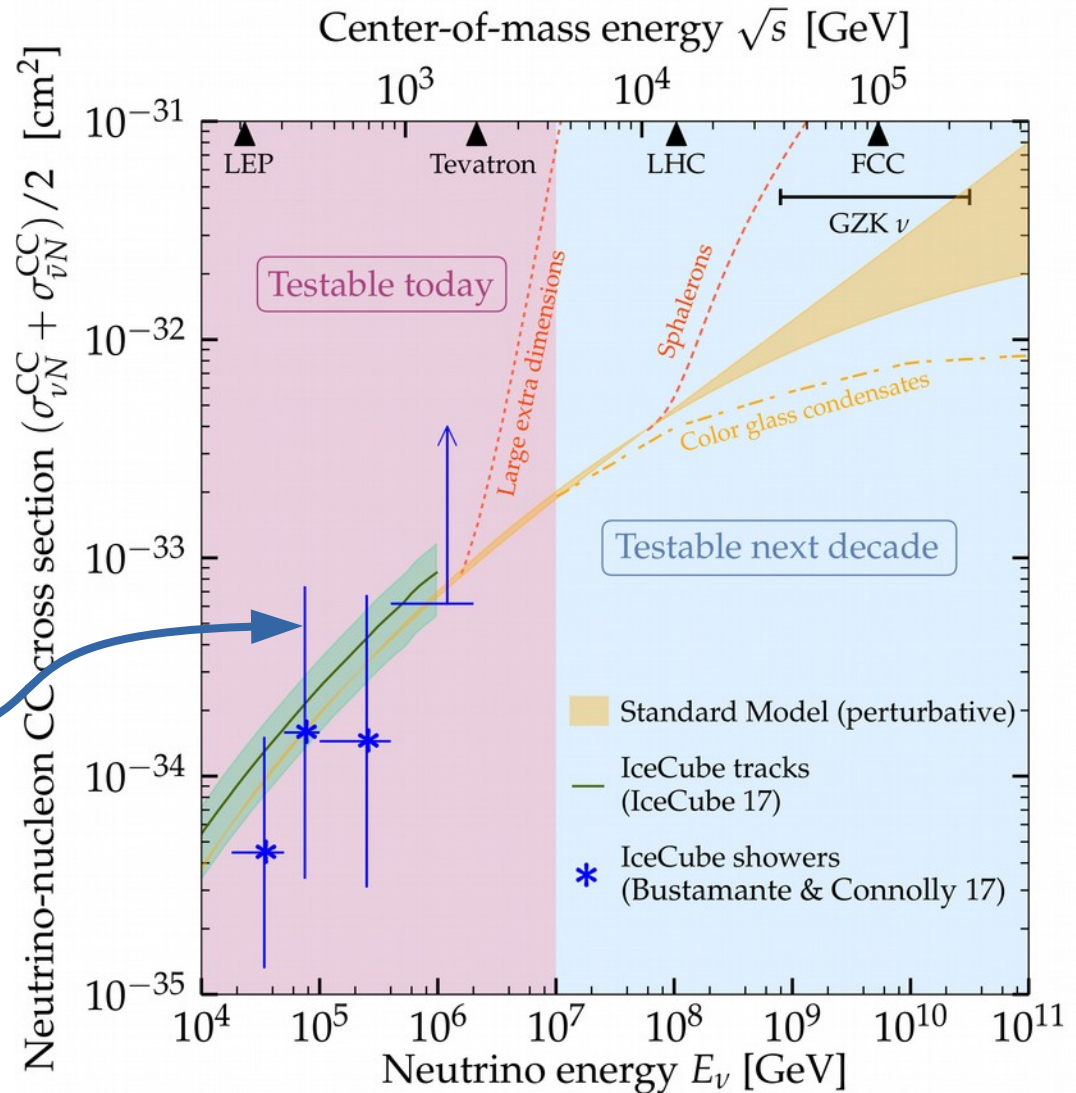
MB & Connolly, *PRL* 2019



MB & Connolly, *PRL* 2019



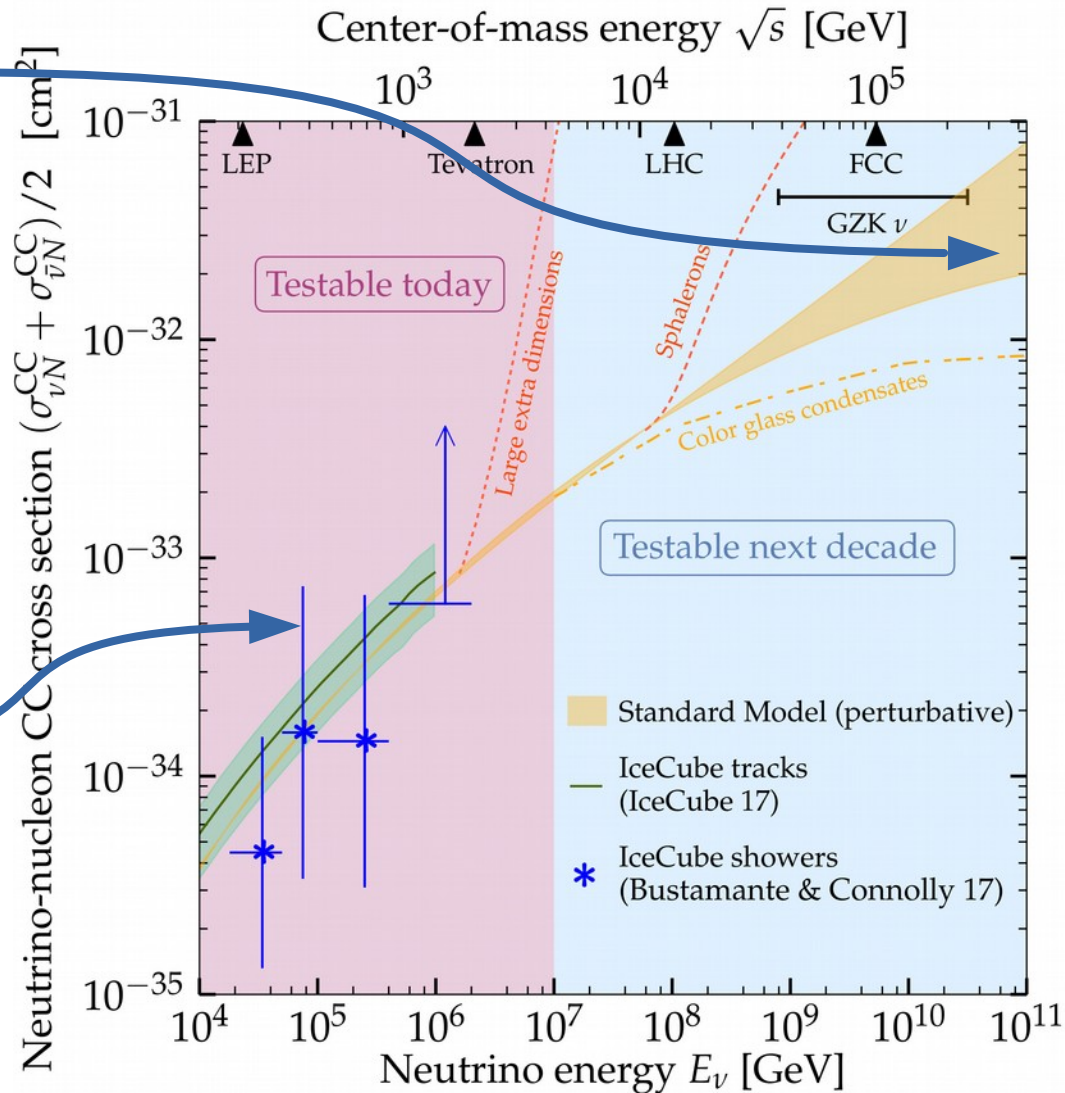
- ▶ Fold in astrophysical unknowns (spectral index, normalization)
- ▶ Compatible with SM predictions
- ▶ Still room for new physics
- ▶ Today, using IceCube:
  - ▶ Extracted from ~60 showers in 6 yr
  - ▶ Limited by statistics
- ▶ Future, using IceCube-Gen2:
  - ▶  $\times 5$  volume  $\Rightarrow$  300 showers in 6 yr
  - ▶ Reduce statistical error by 40%



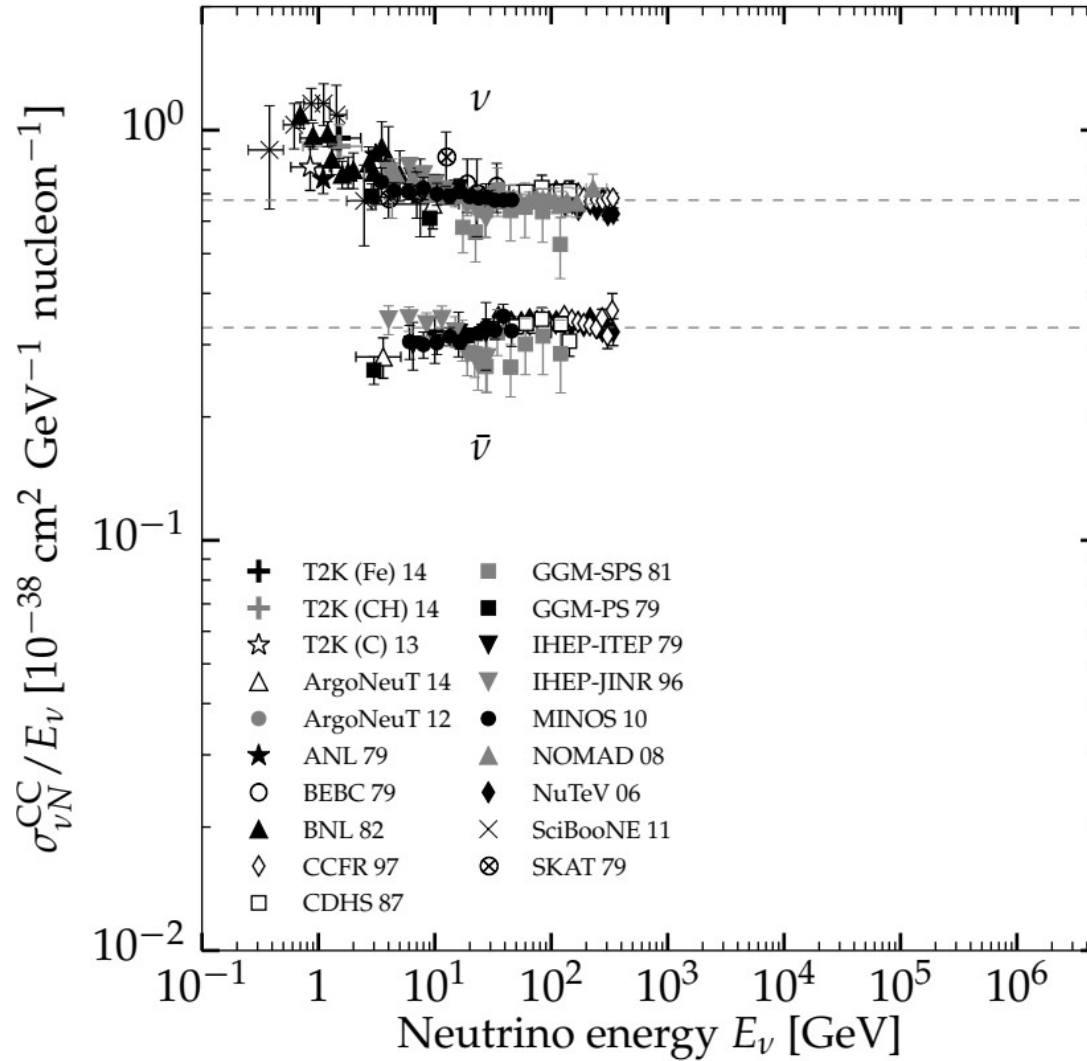
UHE uncertainties can be smaller:  
Cooper-Sarkar, Mertsch, Sarkar *et al.*, *JHEP* 2011

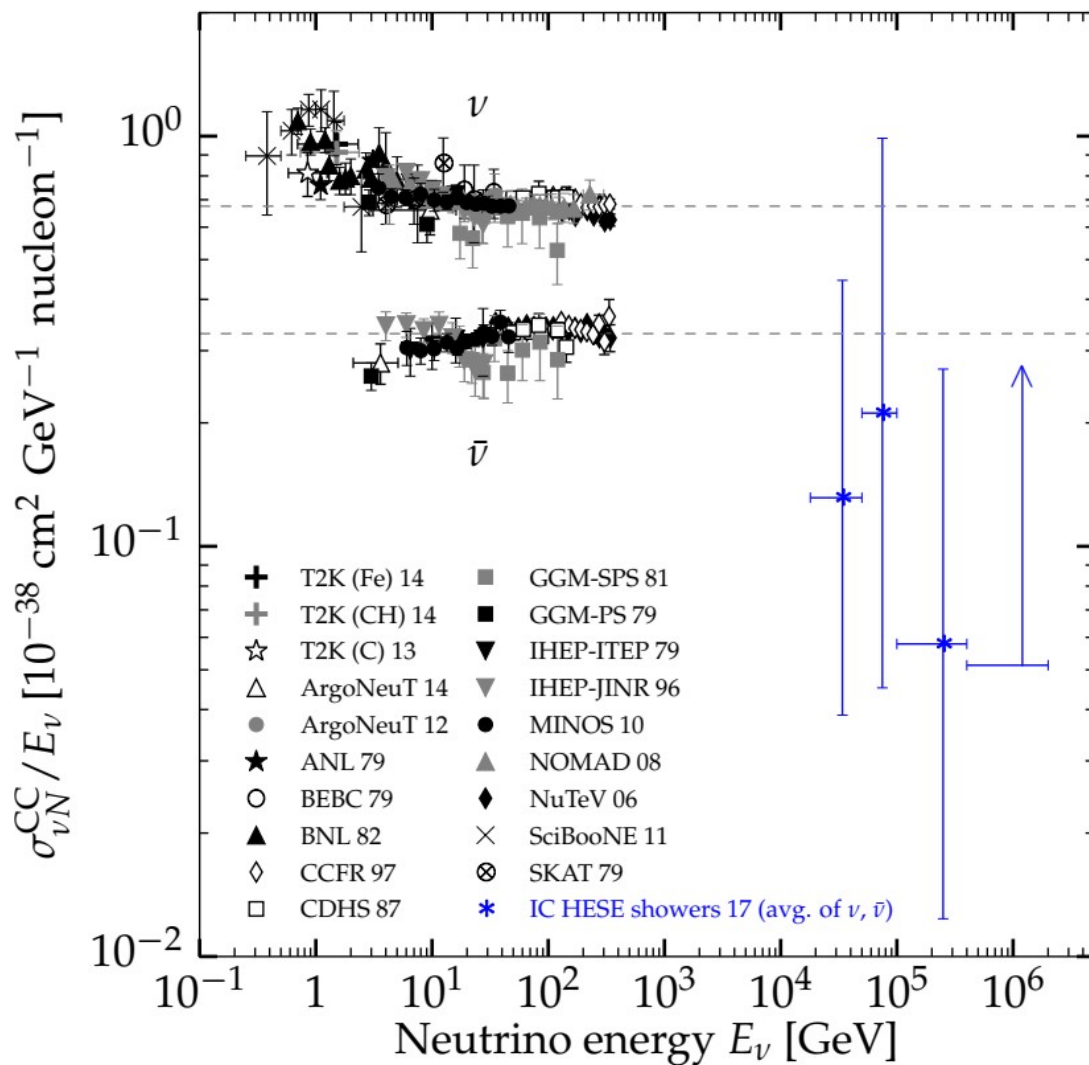
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Cross sections from:  
MB & Connolly *PRL* 2019  
IceCube, *Nature* 2017

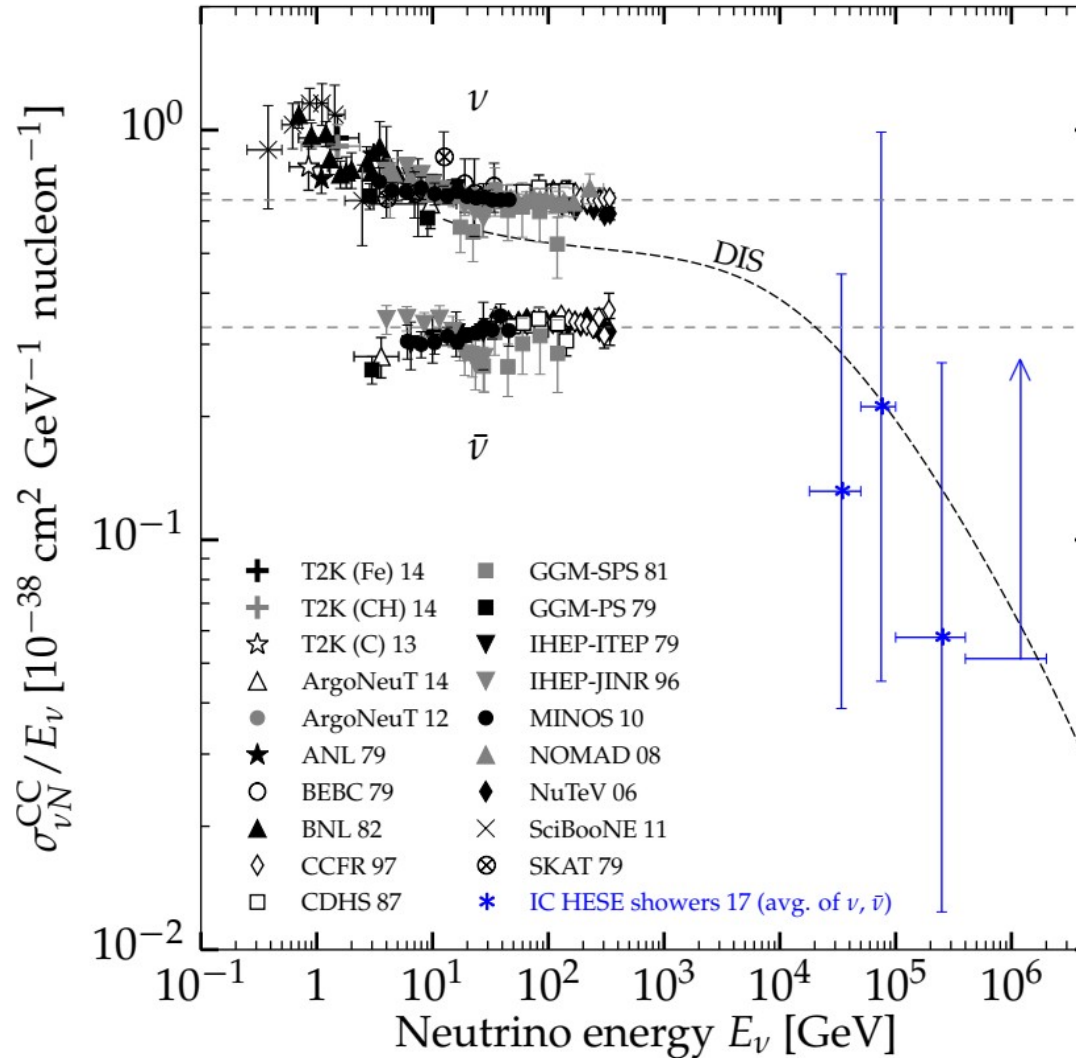


Ackermann, MB, *et al.*, *Astro2020 Decadal Survey* (1903.04333)

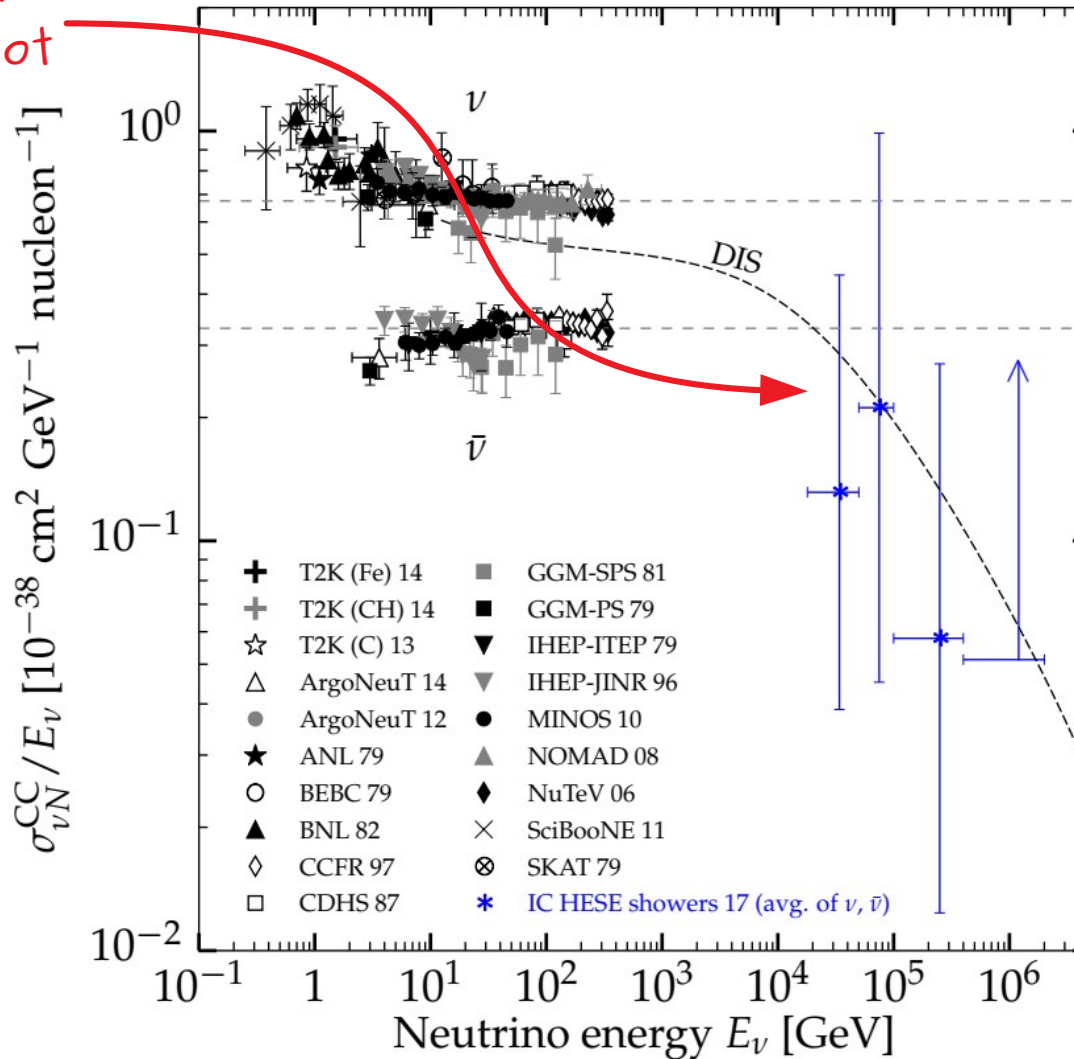




MB & A. Connolly PRL 2019  
See also: IceCube, Nature 2017



Extending the PDG  
cross-section plot



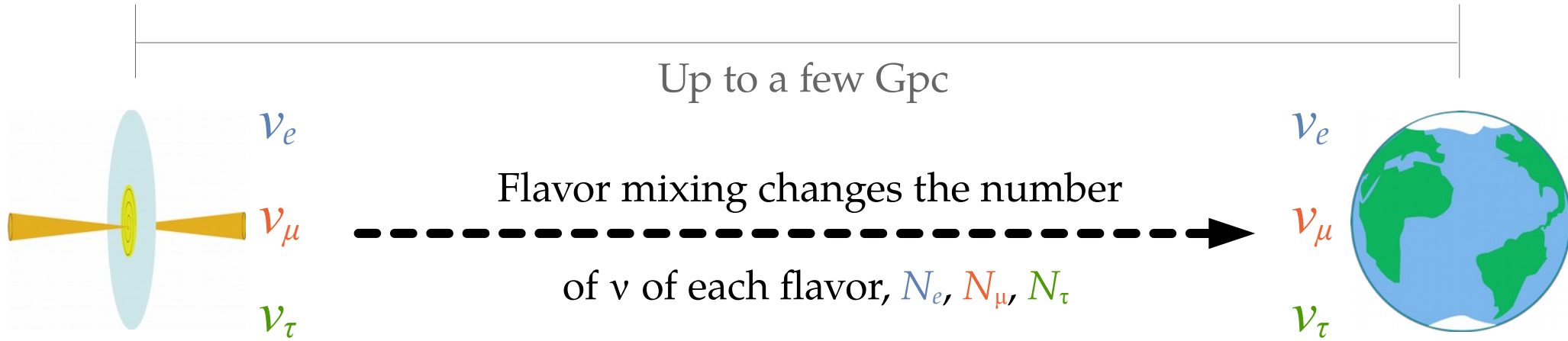
MB & A. Connolly PRL 2019  
See also: IceCube, Nature 2017



# Flavor composition

Astrophysical neutrino sources

Earth



- Different processes yield different ratios of neutrinos of each flavor:

$$(f_{e,S}, f_{\mu,S}, f_{\tau,S}) \equiv (N_{e,S}, N_{\mu,S}, N_{\tau,S}) / N_{\text{tot}}$$

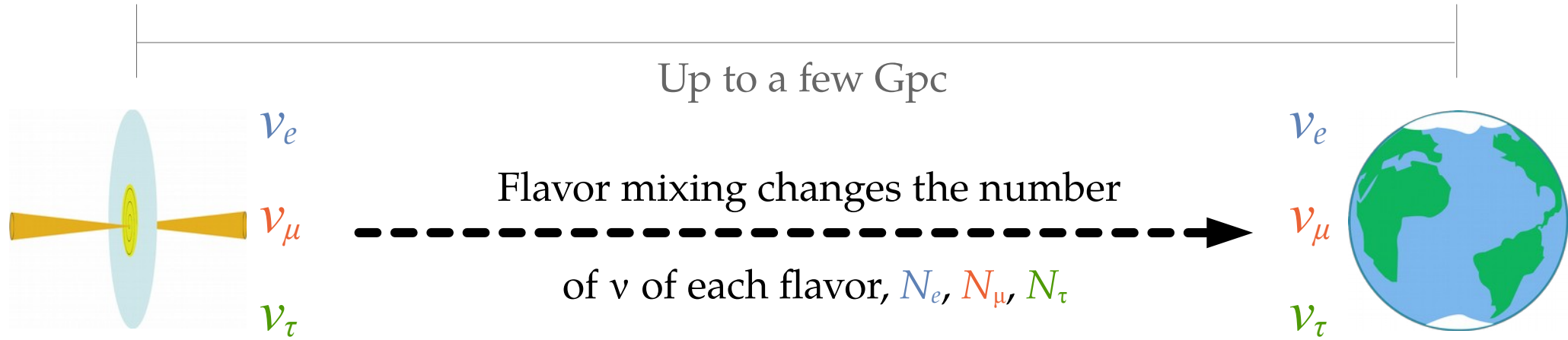
- Flavor ratios at Earth ( $\alpha = e, \mu, \tau$ ):

$$f_{\alpha,\oplus} = \sum_{\beta=e,\mu,\tau} P_{\nu_\beta \rightarrow \nu_\alpha} f_{\beta,S}$$

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Astrophysical neutrino sources

Earth



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$$f_{\alpha,\oplus} = \sum_{\beta=e,\mu,\tau} P_{\nu_\beta \rightarrow \nu_\alpha} f_{\beta,S}$$

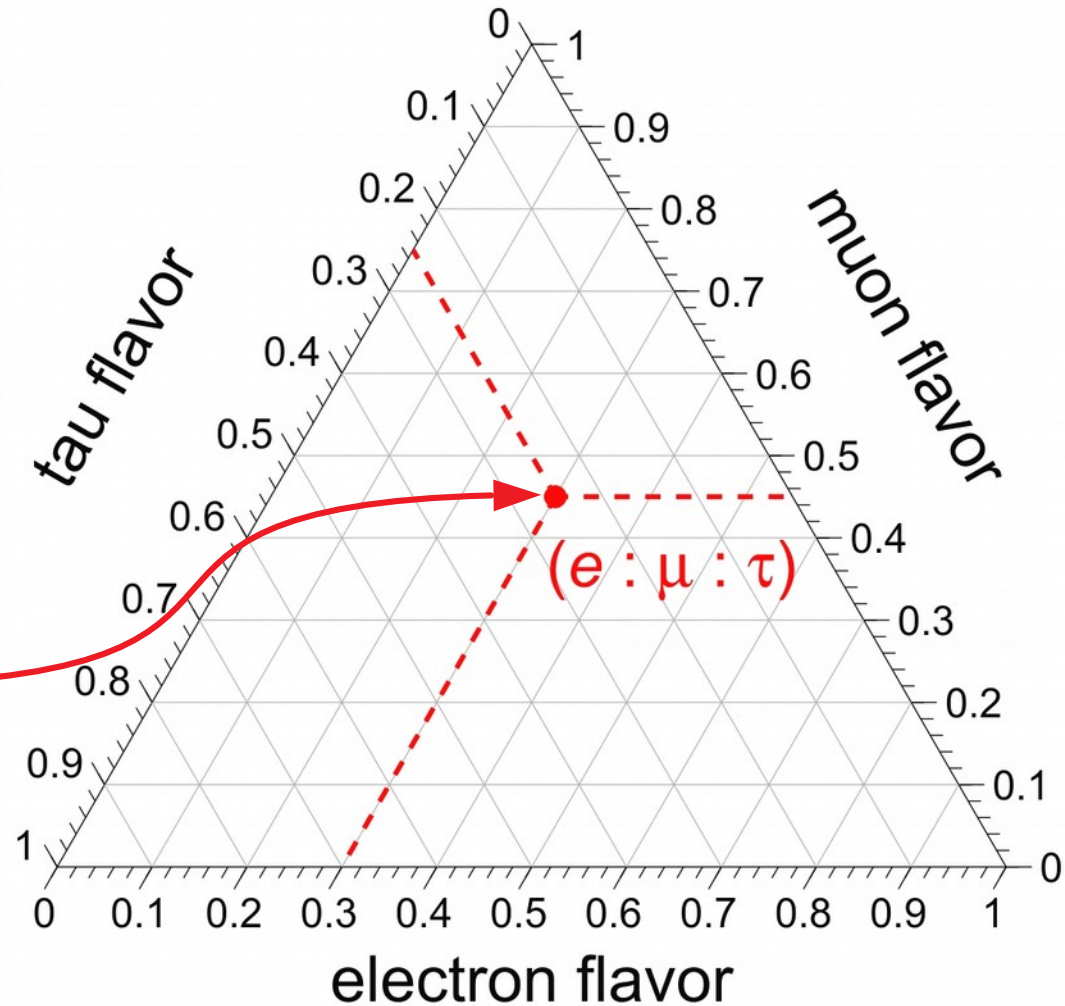
Standard oscillations  
or  
new physics

# Reading a ternary plot

Assumes underlying unitarity –  
sum of projections on each axis is 1

**How to read it:** Follow the tilt of  
the tick marks, *e.g.*,

$$(e:\mu:\tau) = (0.30:0.45:0.25)$$



One likely TeV–PeV  $\nu$  production scenario:

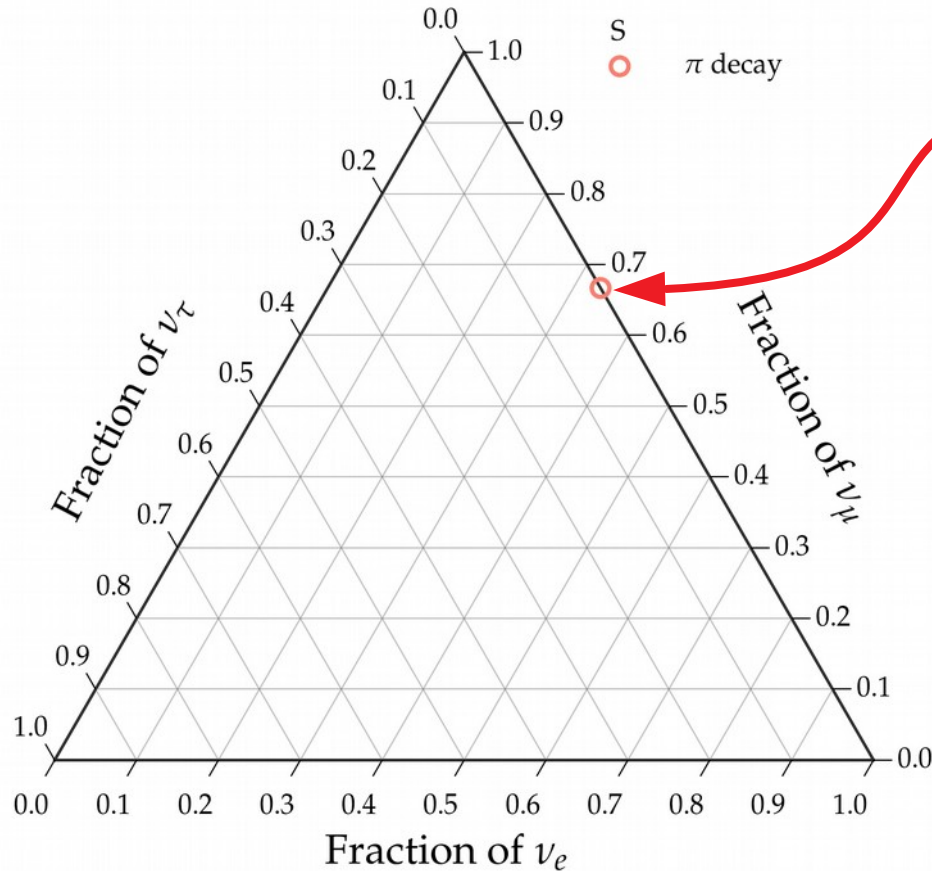
$$p + \gamma \rightarrow \pi^+ \rightarrow \mu^+ + \nu_\mu \text{ followed by } \mu^+ \rightarrow e^+ + \nu_e + \bar{\nu}_\mu$$

Full  $\pi$  decay chain

$$(1/3:2/3:0)_S$$

*Note:*  $\nu$  and  $\bar{\nu}$  are (so far) indistinguishable  
in neutrino telescopes

One likely TeV–PeV  $\nu$  production scenario:

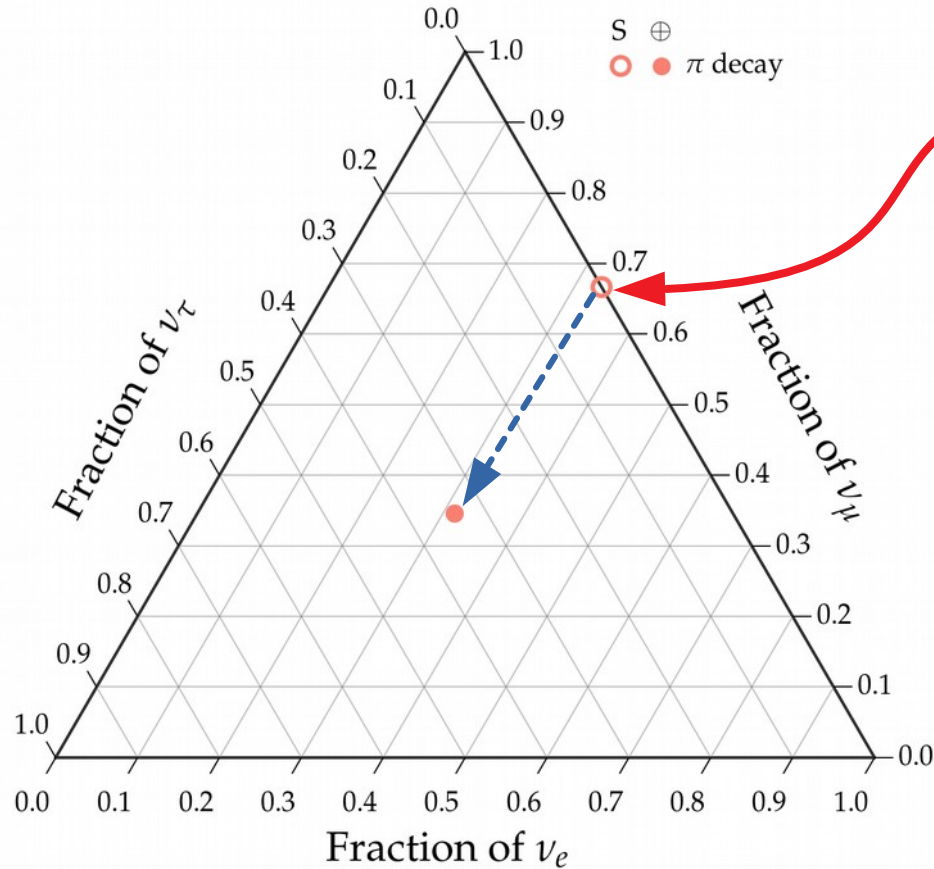


Full  $\pi$  decay chain

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One likely TeV–PeV  $\nu$  production scenario:



Full  $\pi$  decay chain

$(1/3:2/3:0)_S$

Note:  $\nu$  and  $\bar{\nu}$  are (so far) indistinguishable in neutrino telescopes



$$p + \gamma \rightarrow \pi^+ \rightarrow \mu^+ + \nu_\mu \quad \text{followed by} \quad \mu^+ \rightarrow e^+ + \nu_e + \bar{\nu}_\mu$$

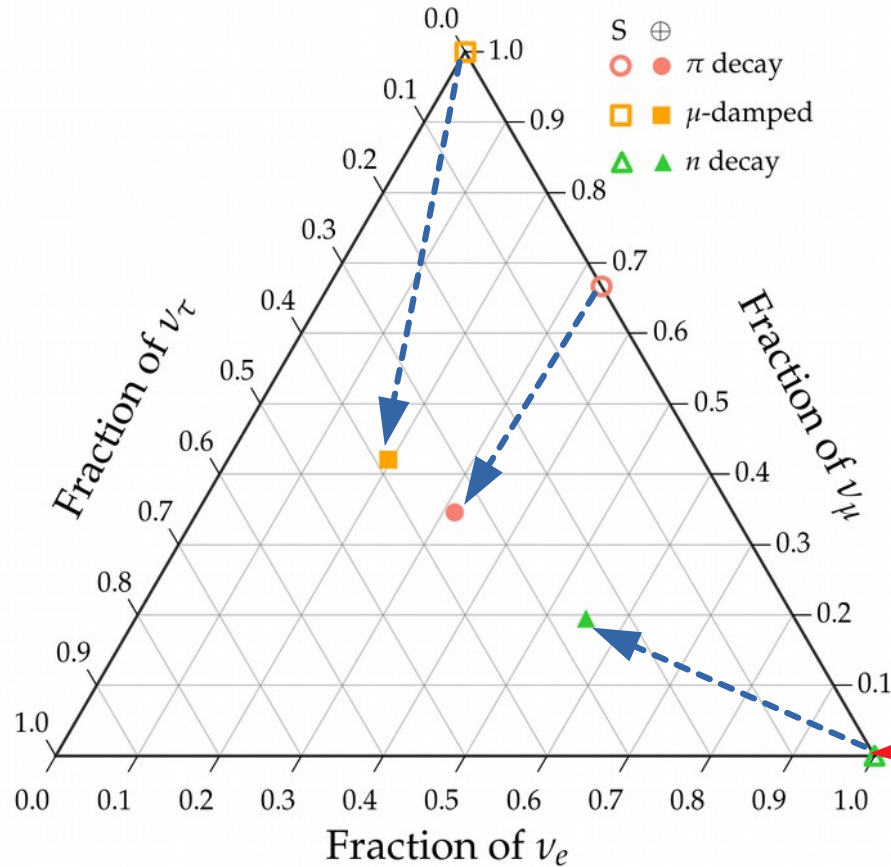
$$(1/3:2/3:0)_S$$

- Muon damped

$$(0:1:0)_S$$

*Note:  $\nu$  and  $\bar{\nu}$  are (so far) indistinguishable  
in neutrino telescopes*

One likely TeV–PeV  $\nu$  production scenario:



Full  $\pi$  decay chain

$(1/3:2/3:0)_S$

Muon damped

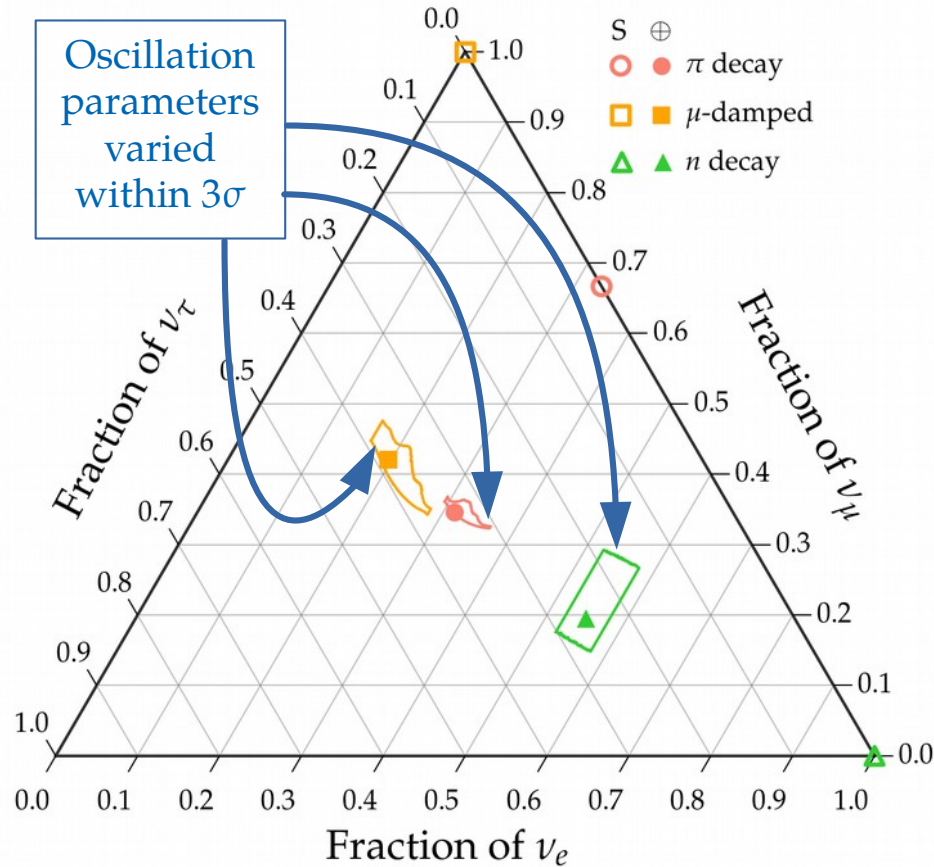
$(0:1:0)_S$

Neutron decay

$(1:0:0)_S$

Note:  $\nu$  and  $\bar{\nu}$  are (so far) indistinguishable in neutrino telescopes

One likely TeV–PeV  $\nu$  production scenario:



Full  $\pi$  decay chain

$$(1/3:2/3:0)_S$$

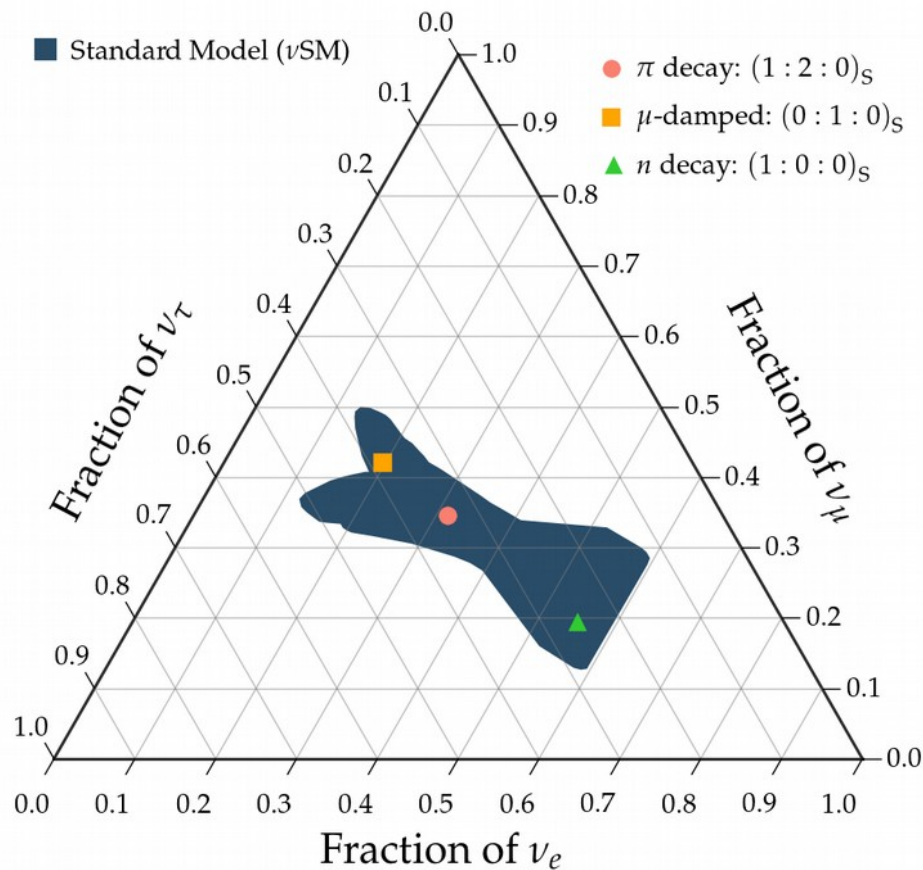
Muon damped

$$(0:1:0)_S$$

Neutron decay

$$(1:0:0)_S$$

Note:  $\nu$  and  $\bar{\nu}$  are (so far) indistinguishable in neutrino telescopes



All possible flavor  
ratios at the sources

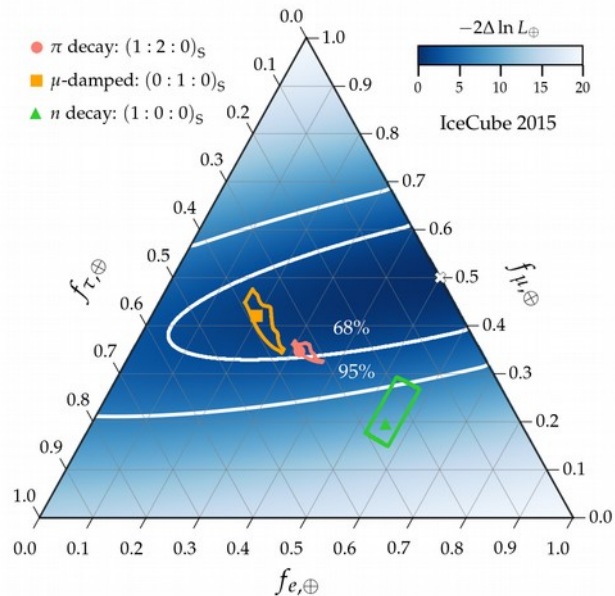
+

Vary oscillation  
parameters within  $3\sigma$

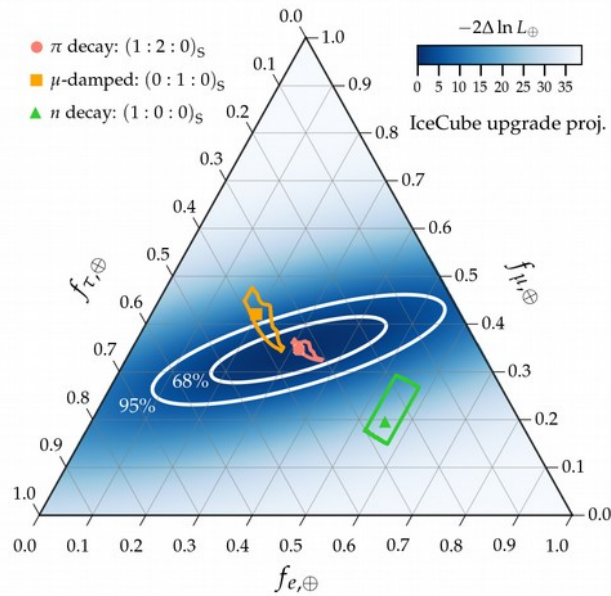
*Note:*  $\nu$  and  $\bar{\nu}$  are (so far) indistinguishable  
in neutrino telescopes

# IceCube flavor composition

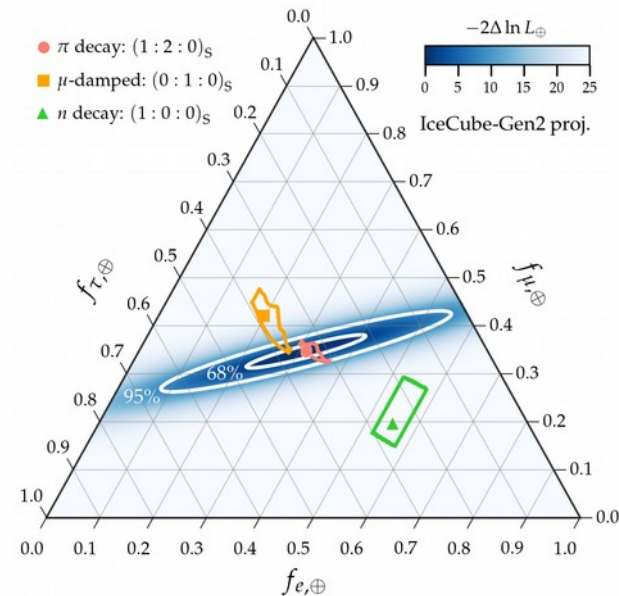
Today  
IceCube



Near future (2022)  
IceCube upgrade



In 10 years (2030s)  
IceCube-Gen2



- ▶ Best fit:  
 $(f_e:f_\mu:f_\tau)_\oplus = (0.49:0.51:0)_\oplus$
- ▶ Compatible with standard source compositions
- ▶ Hints of one  $\nu_\tau$  (not shown)

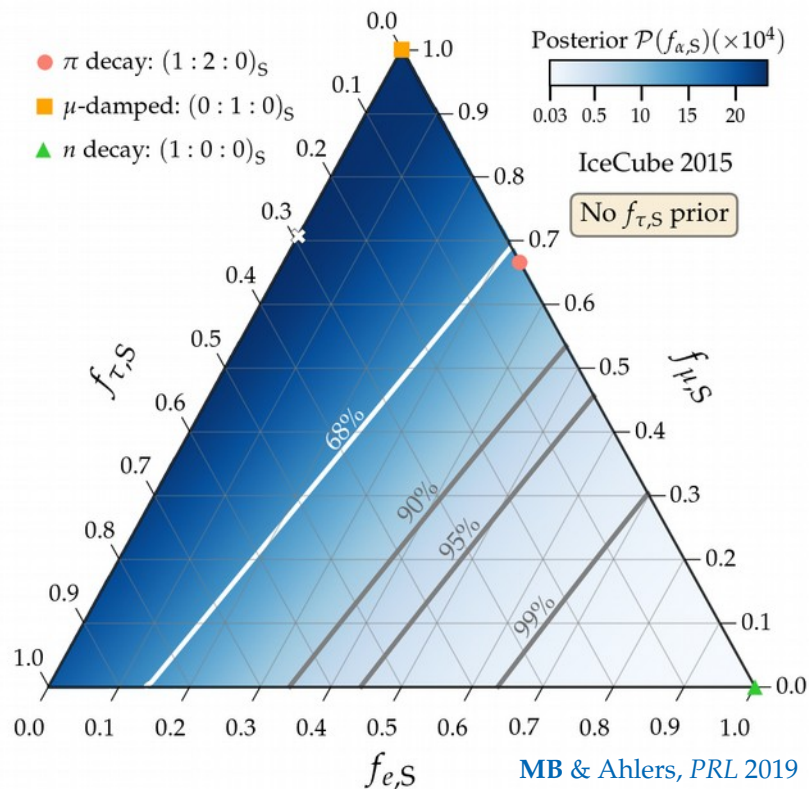
Assuming production by the full pion decay chain

Plus possibly better flavor-tagging, *e.g.*, muon and neutron echoes  
[Li, MB, Beacom PRL 2019]

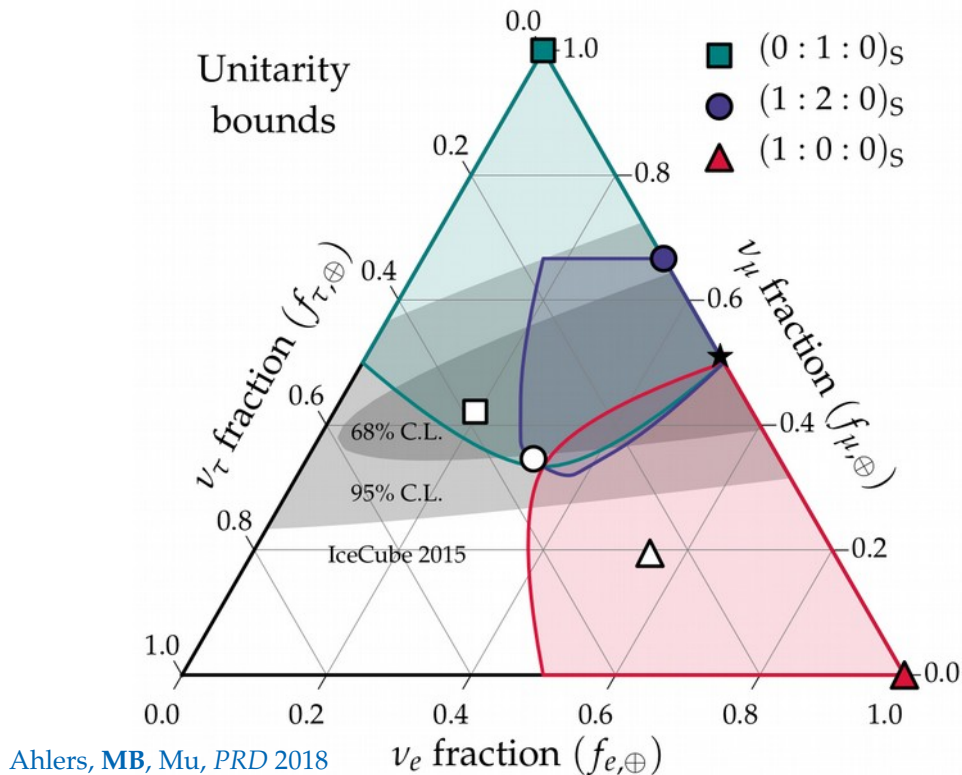


# Flavor – What is it good for?

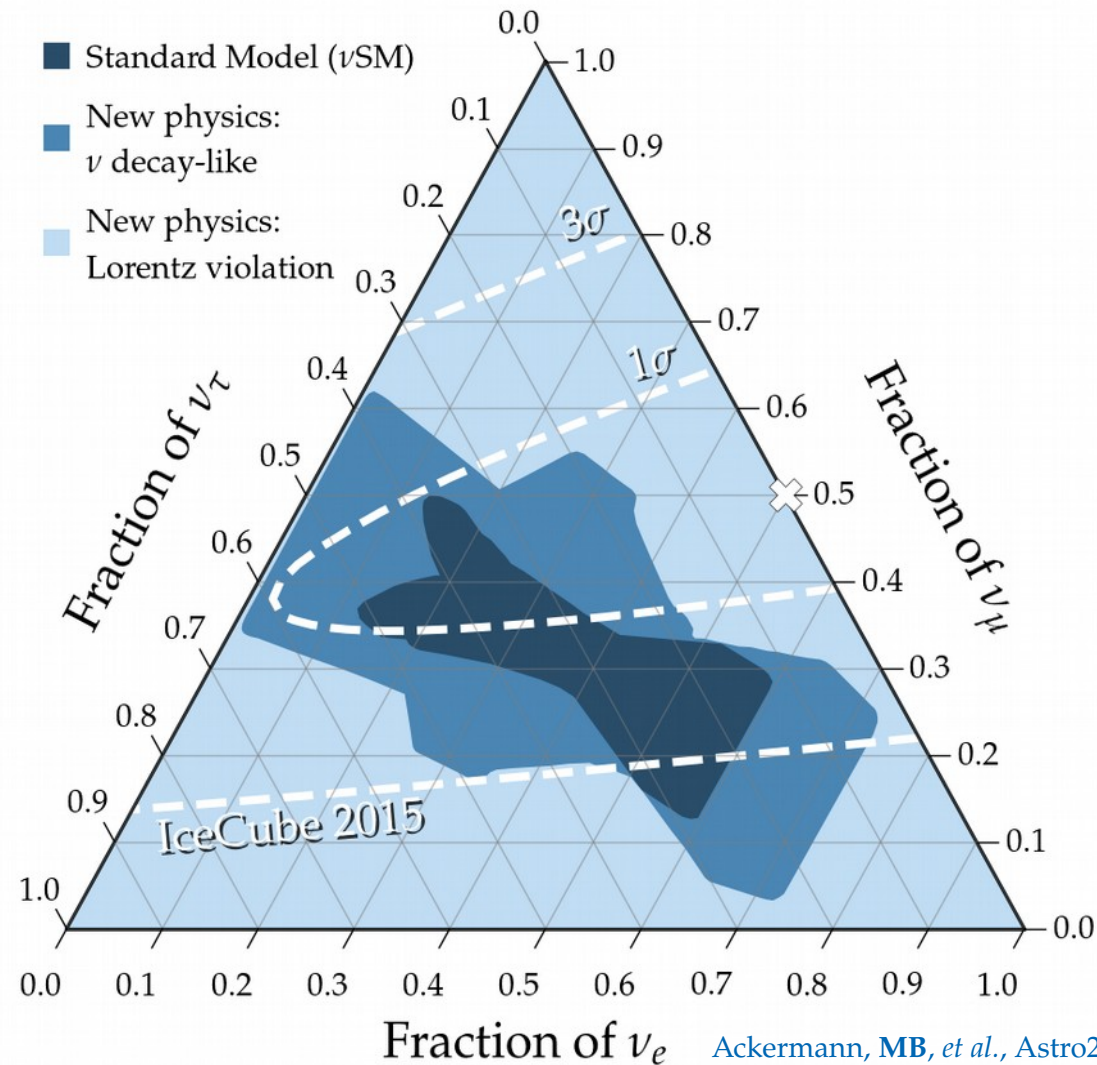
Trusting **particle physics**  
and learning about **astrophysics**



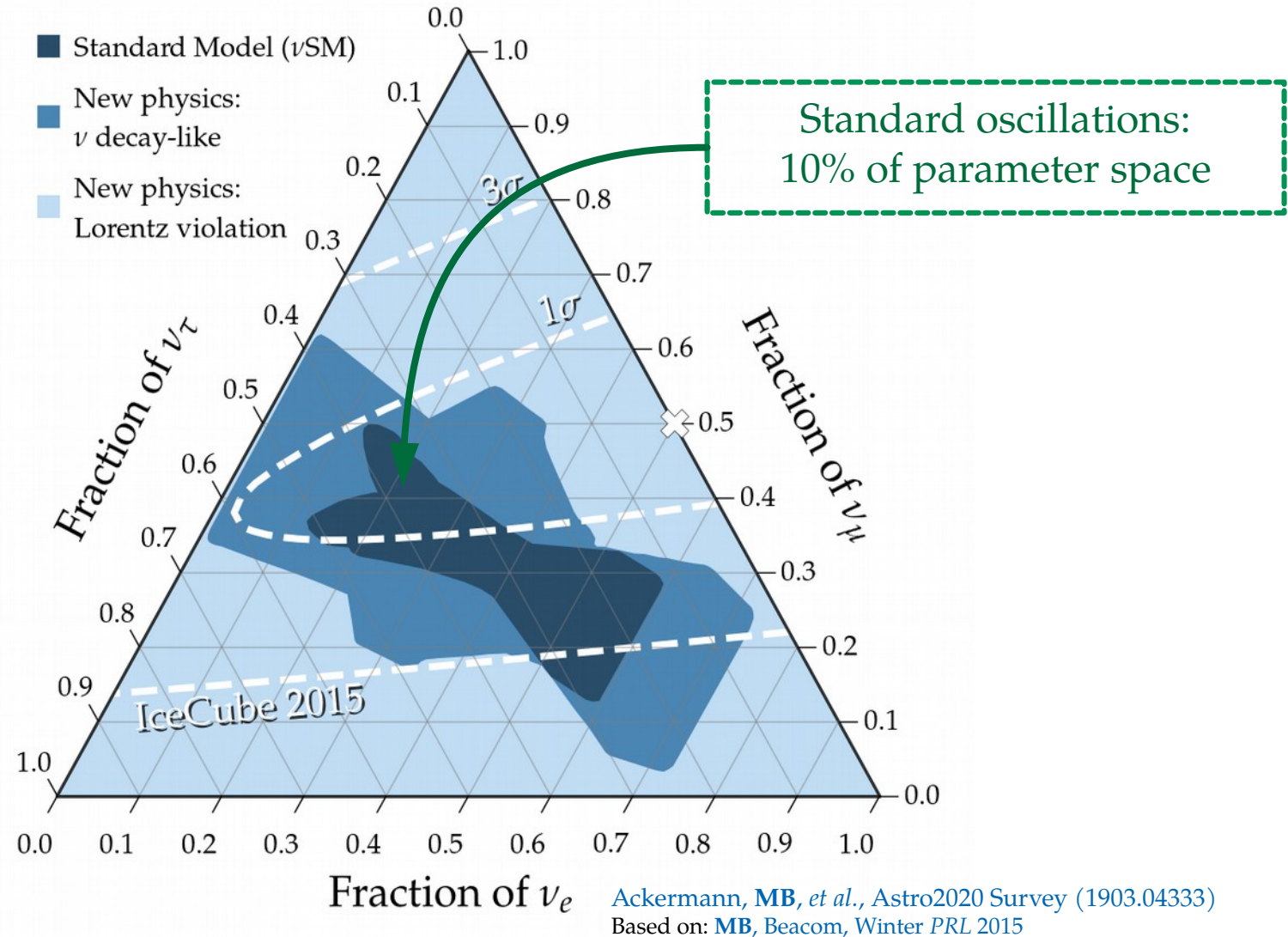
Trusting **astrophysics**  
and learning about **particle physics**





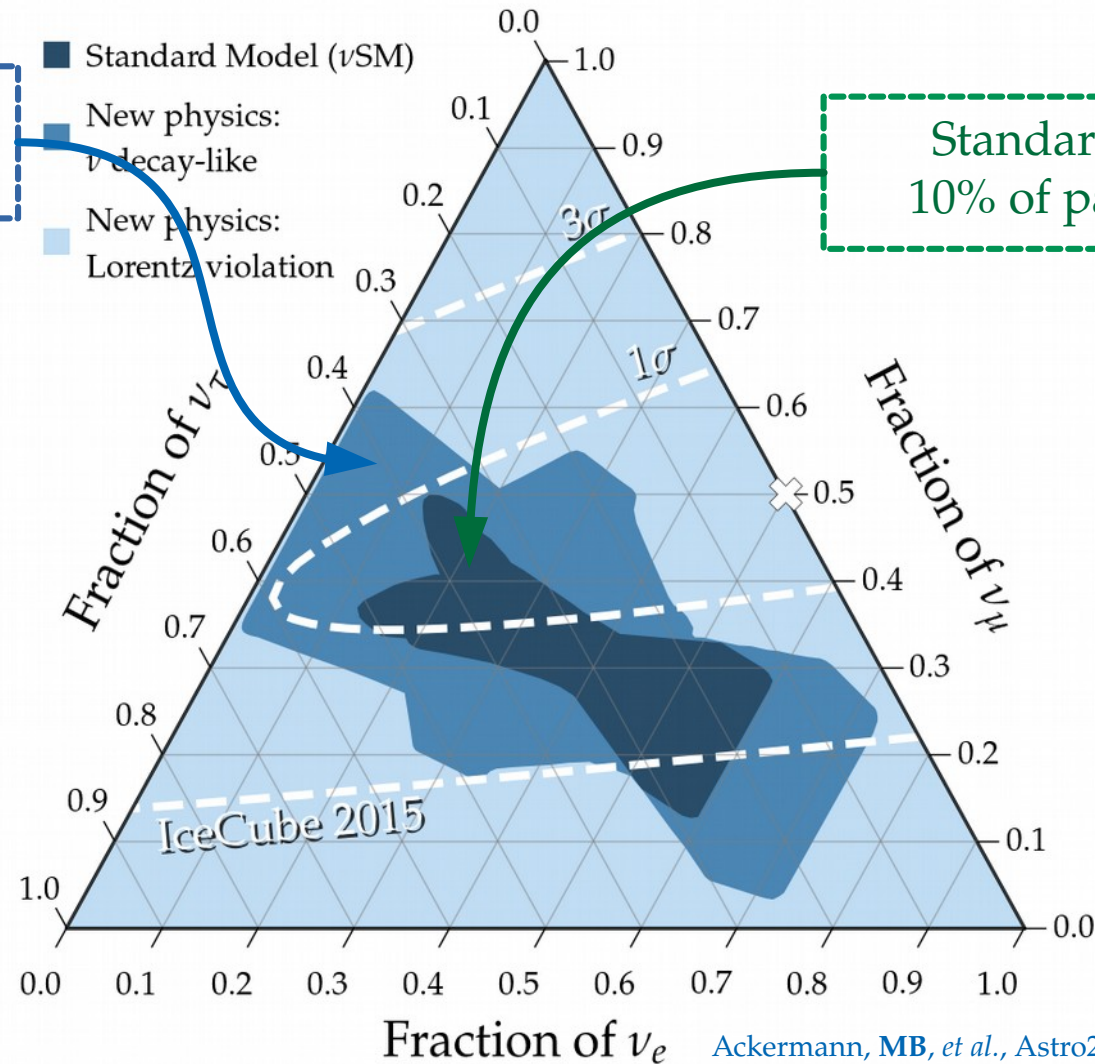


Ackermann, MB, et al., Astro2020 Survey (1903.04333)  
Based on: MB, Beacom, Winter PRL 2015



Neutrino decay  
30% of parameter space

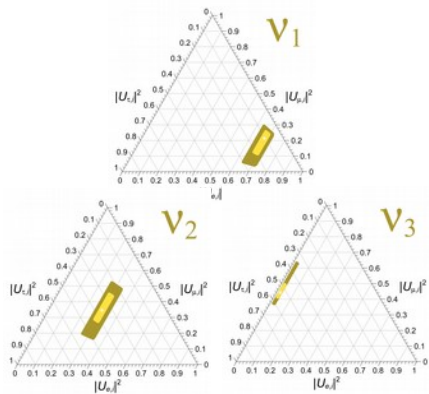
Standard oscillations:  
10% of parameter space



Neutrino decay  
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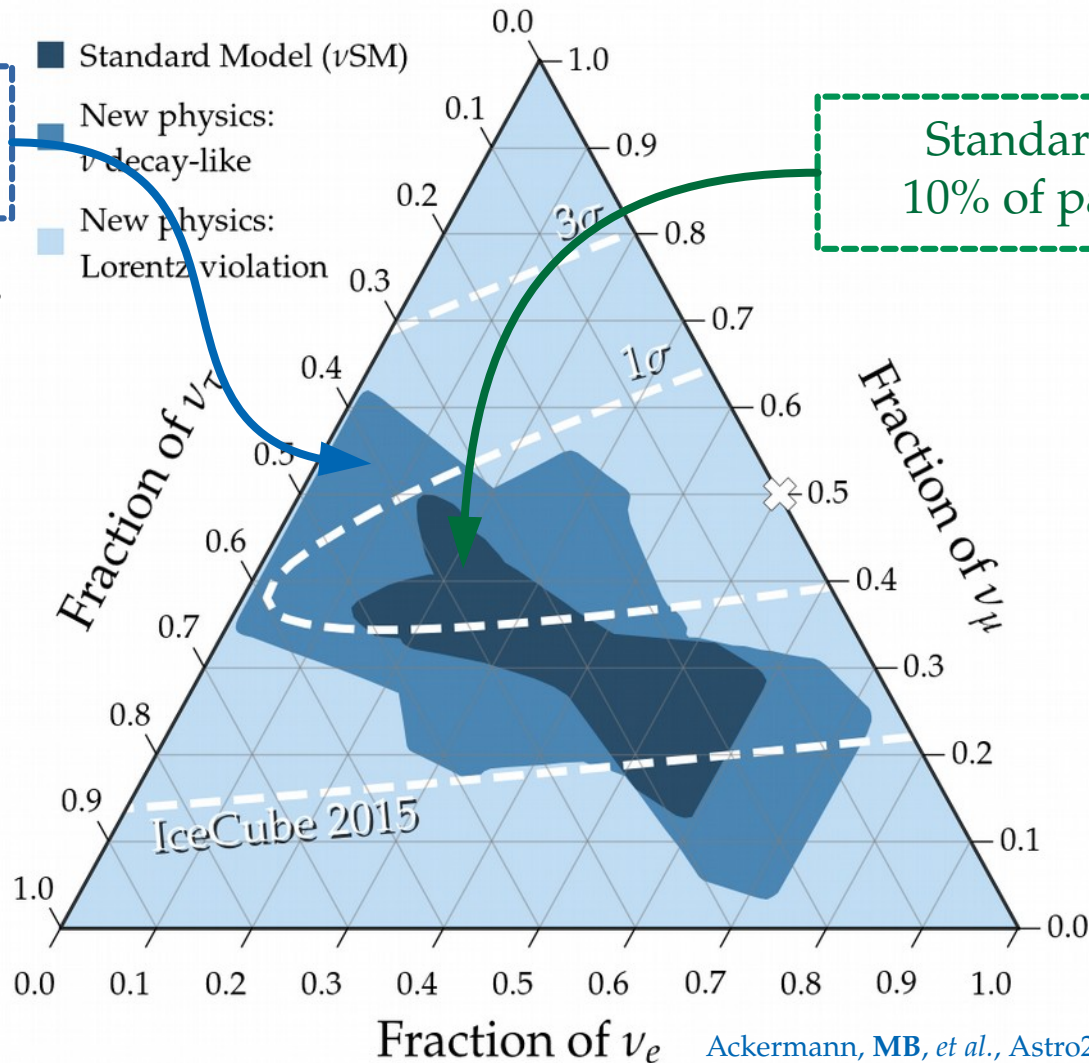
$\nu_2, \nu_3 \rightarrow \nu_1$  OR  $\nu_1, \nu_2 \rightarrow \nu_3$

Flavor ratios determined by  
how many  $\nu_1, \nu_2, \nu_3$  survive:



$\tau_2/m_2, \tau_3/m_3 > 10 \text{ s eV}^{-1}$

MB, Beacom, Murase PRD 2017  
Baerwald, MB, Winter JCAP 2012



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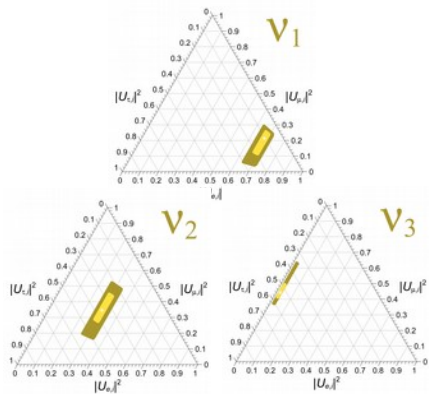
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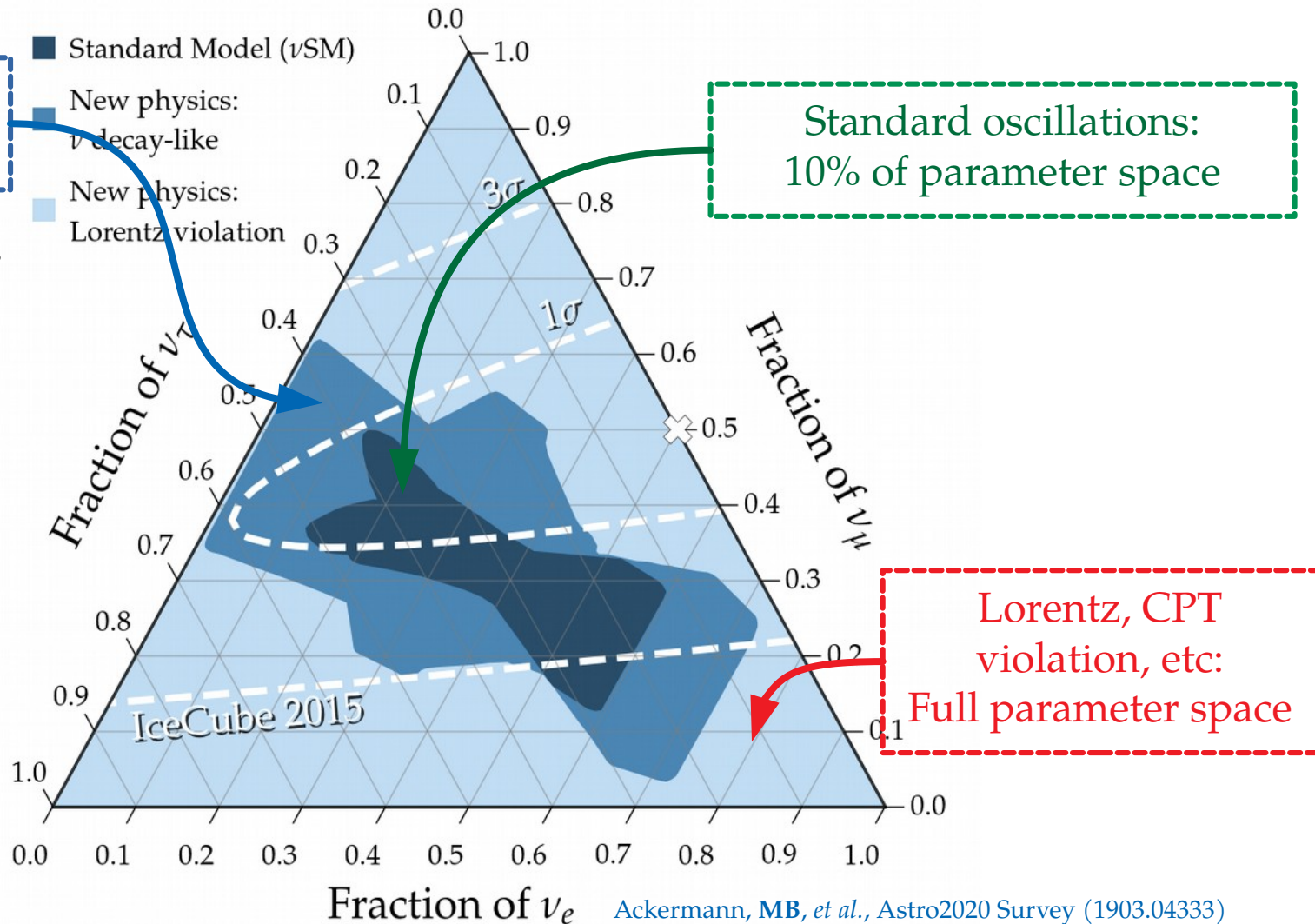
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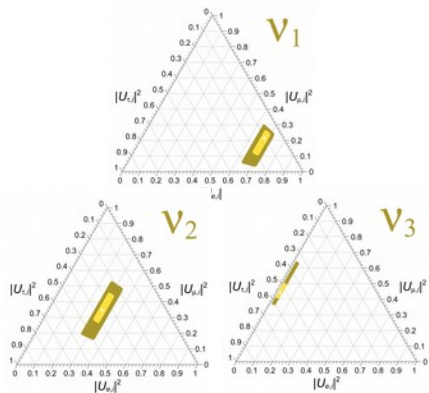
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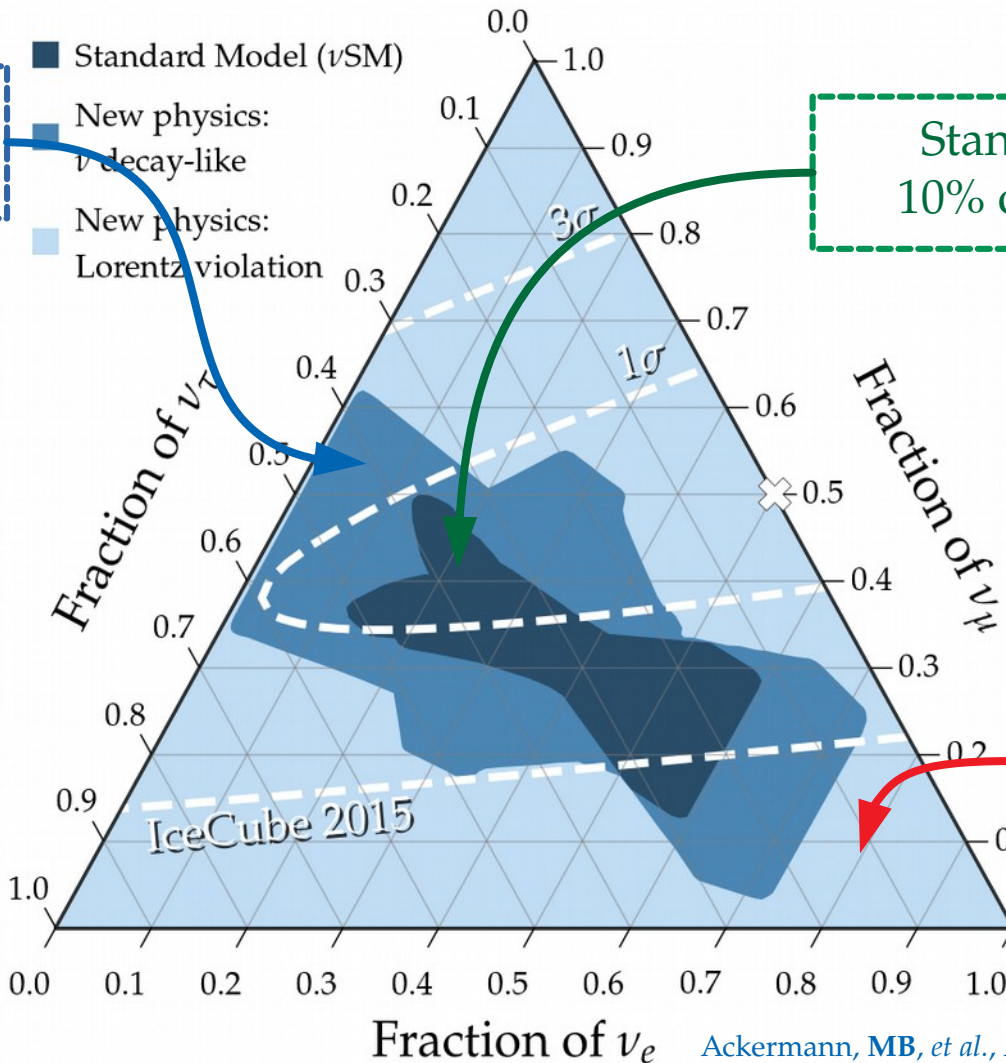
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Standard oscillations:  
10% of parameter space

Lorentz, CPT  
violation, etc:  
Full parameter space



Ackermann, MB, et al., Astro2020 Survey (1903.04333)  
Based on: MB, Beacom, Winter PRL 2015

# What lies beyond? *Take your pick*

- ▶ High-energy effective field theories
  - ▶ Violation of Lorentz and CPT invariance  
[Barenboim & Quigg, *PRD* 2003; MB, Gago, Peña-Garay, *JHEP* 2010; Kostelecky & Mewes 2004]
  - ▶ Violation of equivalence principle  
[Gasperini, *PRD* 1989; Glashow *et al.*, *PRD* 1997]
  - ▶ Coupling to a gravitational torsion field  
[De Sabbata & Gasperini, *Nuovo Cim.* 1981]
  - ▶ Renormalization-group-running of mixing parameters  
[MB, Gago, Jones, *JHEP* 2011]
  - ▶ General non-unitary propagation  
[Ahlers, MB, Mu, *PRD* 2018]
- ▶ Active-sterile mixing  
[Aeikens *et al.*, *JCAP* 2015; Brdar, *JCAP* 2017]
- ▶ Flavor-violating physics
  - ▶ New neutrino-electron interactions  
[MB & Agarwalla, *PRL* 2019]
  - ▶ New  $\nu\nu$  interactions  
[Ng & Beacom, *PRD* 2014; Cherry, Friedland, Shoemaker, 1411.1071; Blum, Hook, Murase, 1408.3799]
- ▶ ...



Toho Company Ltd.

# New physics – High-energy effects

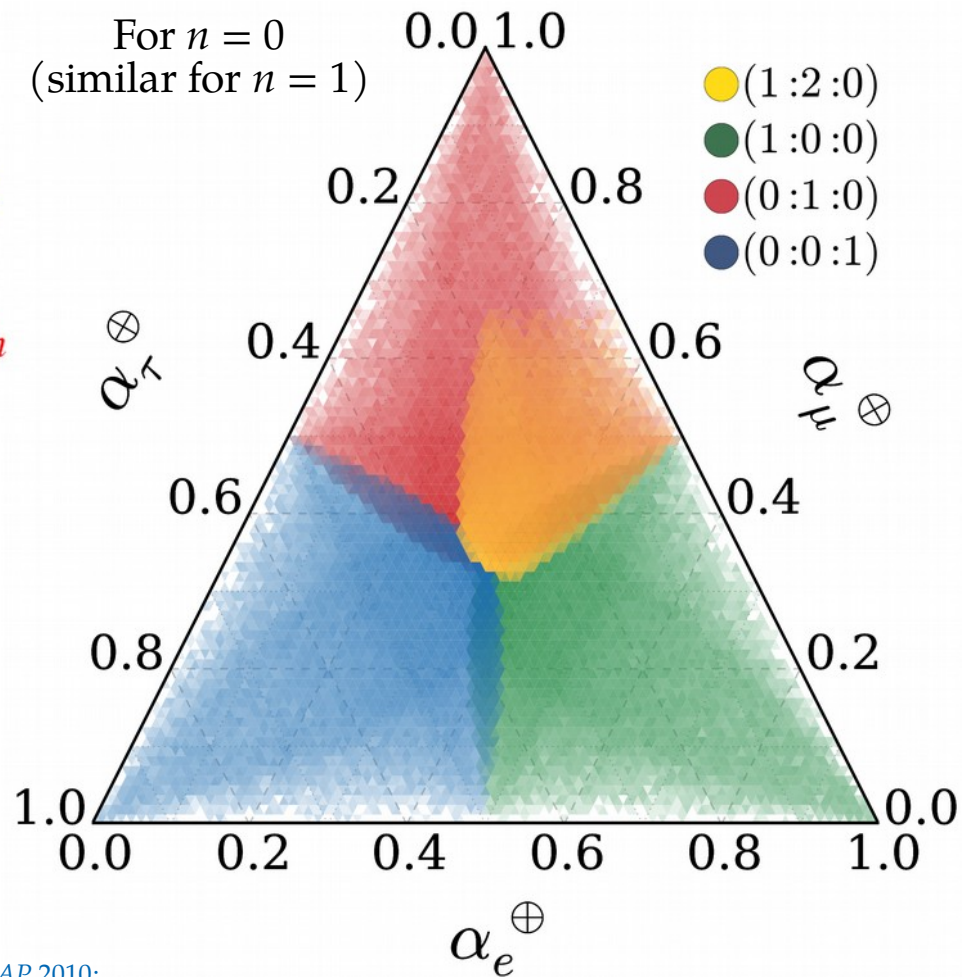
$$H_{\text{tot}} = H_{\text{std}} + H_{\text{NP}}$$

$$H_{\text{std}} = \frac{1}{2E} U_{\text{PMNS}}^\dagger \text{diag} (0, \Delta m_{21}^2, \Delta m_{31}^2) U_{\text{PMNS}}$$

$$H_{\text{NP}} = \sum_n \left( \frac{E}{\Lambda_n} \right)^n U_n^\dagger \text{diag} (O_{n,1}, O_{n,2}, O_{n,3}) U_n$$

This can populate *all* of the triangle –

- Use current atmospheric bounds on  $O_{n,i}$ :  
 $O_0 < 10^{-23} \text{ GeV}$ ,  $O_1/\Lambda_1 < 10^{-27} \text{ GeV}$
- Sample the unknown new mixing angles



See also: [Rasmusen et al., PRD 2017](#); [MB, Beacom, Winter PRL 2015](#); [MB, Gago, Peña-Garay JCAP 2010](#); [Bazo, MB, Gago, Miranda IJMPA 2009](#); + many others

Argüelles, Katori, Salvadó, PRL 2015



# New physics – High-energy effects

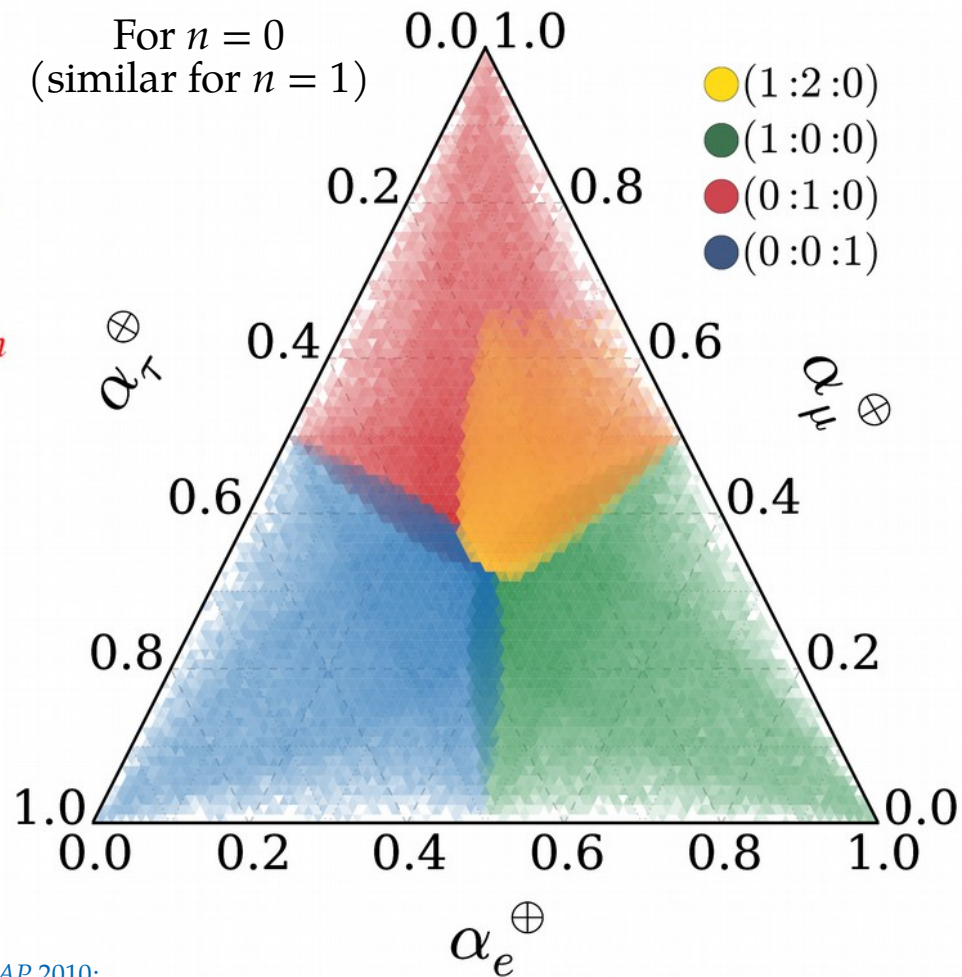
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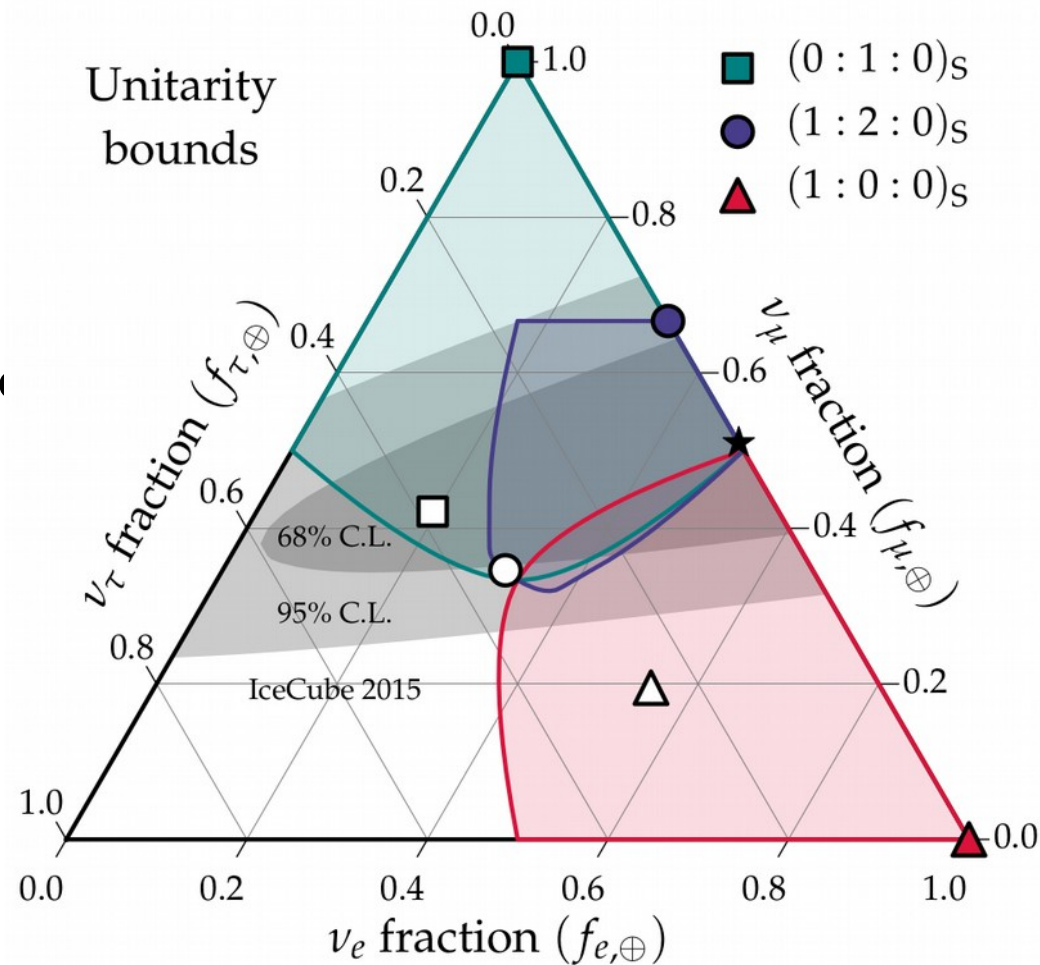
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# Using unitarity to constrain new physics

$$H_{\text{tot}} = H_{\text{std}} + H_{\text{NP}}$$

- ▶ New mixing angles unconstrained
- ▶ Use unitarity ( $U_{\text{NP}} U_{\text{NP}}^\dagger = 1$ ) to bound all possible flavor ratios at Earth
- ▶ Can be used as prior in new-physics searches in IceCube





# Ultra-long-range flavorful interactions

- ▶ **Simple extension of the SM:** Promote the global lepton-number symmetries  $L_e-L_\mu$ ,  $L_e-L_\tau$  to local symmetries
- ▶ They introduce new interaction between electrons and  $\nu_e$  and  $\nu_\mu$  or  $\nu_\tau$  mediated by a new neutral vector boson ( $Z'$ ):
  - ▶ Affects oscillations
  - ▶ If the  $Z'$  is *very* light, *many* electrons can contribute

X.-G. He, G.C. Joshi, H. Lew, R. R. Volkas, *PRD* 1991 / R. Foot, X.-G. He, H. Lew, R. R. Volkas, *PRD* 1994  
A. Joshipura, S. Mohanty, *PLB* 2004 / J. Grifols & E. Massó, *PLB* 2004 / A. Bandyopadhyay, A. Dighe, A. Joshipura, *PRD* 2007  
M.C. González-García, P.C. de Holanda, E. Massó, R. Zukanovich Funchal, *JCAP* 2007 / A. Samanta, *JCAP* 2011  
S.-S. Chatterjee, A. Dasgupta, S. Agarwalla, *JHEP* 2015

# The new potential sourced by an electron

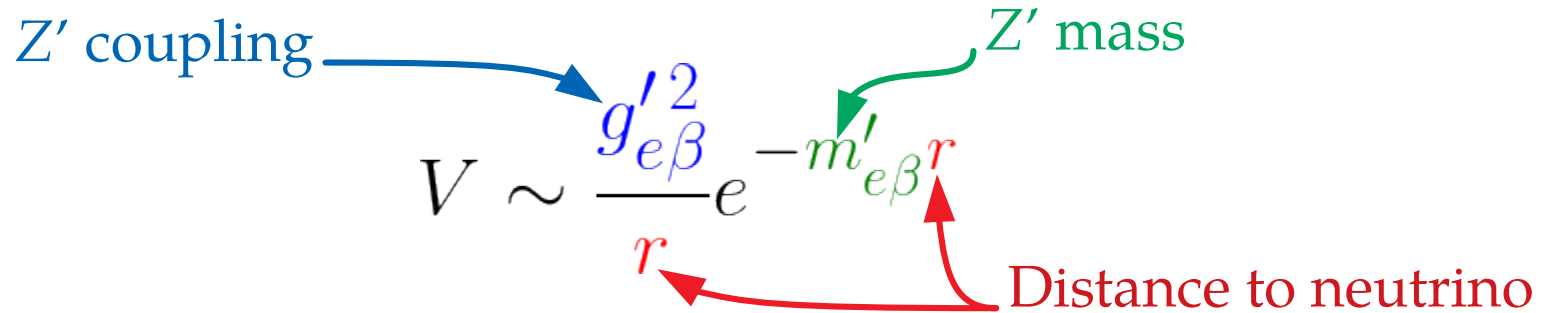
Under the  $L_e$ - $L_\mu$  or  $L_e$ - $L_\tau$  symmetry, an electron sources a Yukawa potential —

$$V \sim \frac{g_{e\beta}'^2}{r} e^{-m'_{e\beta} r}$$

A neutrino “feels” all the electrons within the interaction range  $\sim (1/m')$

# The new potential sourced by an electron

Under the  $L_e-L_\mu$  or  $L_e-L_\tau$  symmetry, an electron sources a Yukawa potential —



The diagram shows the Yukawa potential equation  $V \sim \frac{g'^2_{e\beta}}{r} e^{-m'_{e\beta} r}$  with three color-coded annotations: a blue arrow points from the text "Z' coupling" to the  $g'^2_{e\beta}$  term; a green arrow points from the text "Z' mass" to the  $m'_{e\beta}$  term; and a red arrow points from the text "Distance to neutrino" to the  $r$  term in the denominator.

$$V \sim \frac{g'^2_{e\beta}}{r} e^{-m'_{e\beta} r}$$

A neutrino “feels” all the electrons within the interaction range  $\sim (1/m')$

# Electron-neutrino interactions can kill oscillations


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$$H_{\text{tot}} = \underbrace{H_{\text{vac}}}$$

**Standard oscillations:**  
Neutrinos change flavor  
because this is non-diagonal



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$$P_{\nu_\alpha \rightarrow \nu_\beta}(\theta_{ij}, \delta_{\text{CP}})$$

# Electron-neutrino interactions can kill oscillations

$$H_{\text{tot}} = H_{\text{vac}} + \underbrace{V_{e\beta}}_{= \text{diag}(V_{e\mu}, -V_{e\mu}, 0)}$$

**New neutrino-electron interaction:**  
This is diagonal

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↓

$$P_{\nu_\alpha \rightarrow \nu_\beta} \left( \theta_{ij}, \delta_{\text{CP}}, \Delta m_{ij}^2, E_\nu, \overbrace{g'_{e\mu}, m'_{e\mu}}^{\text{Z' parameters}} \right)$$

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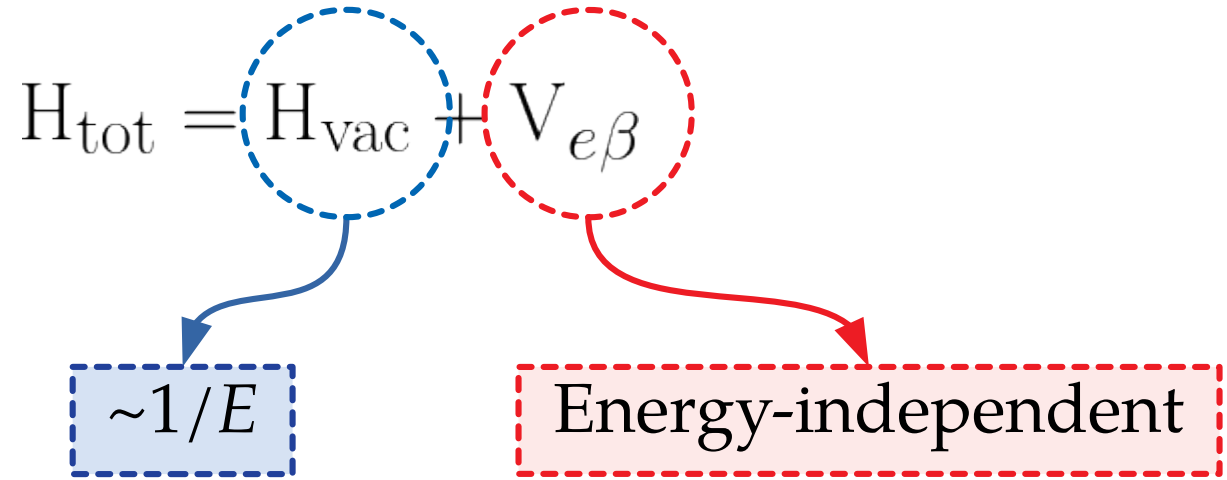
If  $V_{e\beta}$  dominates ( $g' \gg 1, m' \ll 1$ ), oscillations turn off

# Electron-neutrino interactions can kill oscillations

$$H_{\text{tot}} = H_{\text{vac}} + V_{e\beta}$$



# Electron-neutrino interactions can kill oscillations



# Electron-neutrino interactions can kill oscillations

$$H_{\text{tot}} = H_{\text{vac}} + V_{e\beta}$$

$\sim 1/E$

Energy-independent

$\therefore$  We can use high-energy astrophysical neutrinos

# The total potential

Cosmological electrons ( $10^{79} e$ )

Sun ( $10^{57} e$ )

Moon ( $10^{49} e$ )

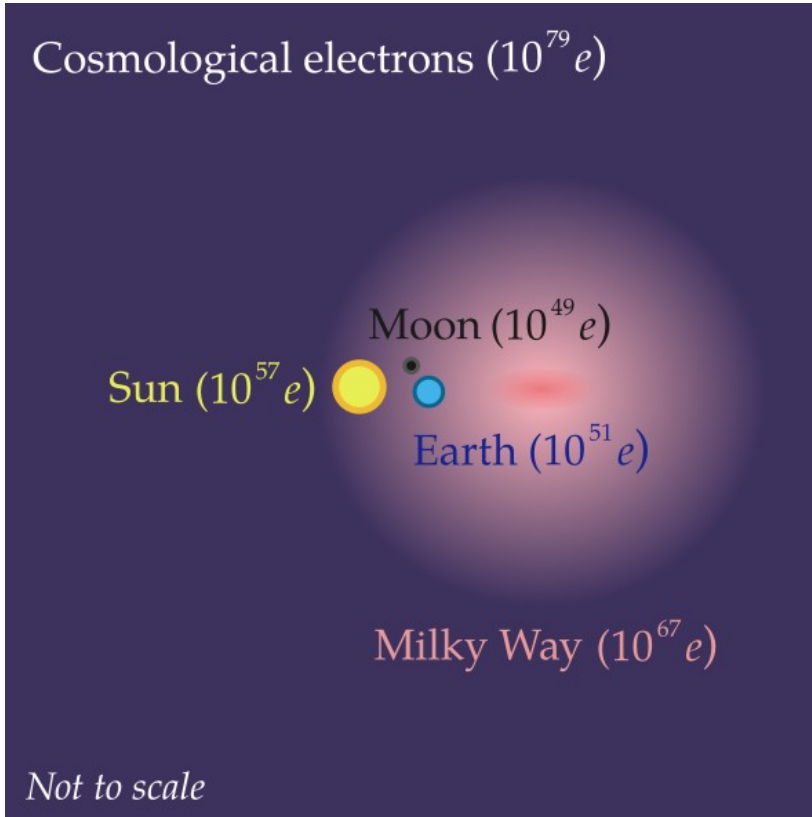
Earth ( $10^{51} e$ )



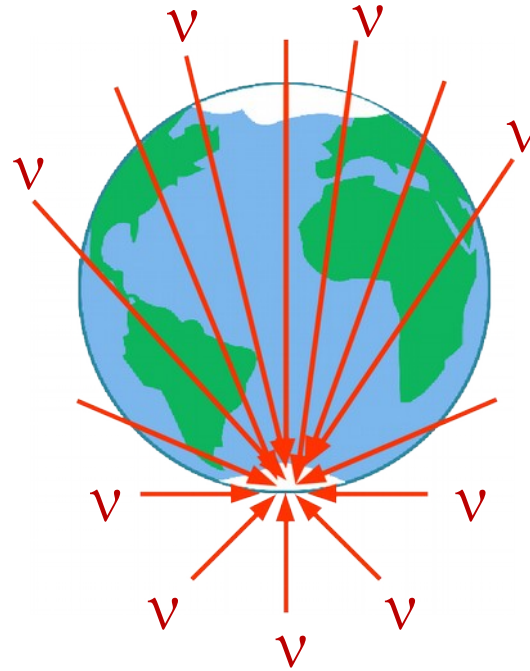
Milky Way ( $10^{67} e$ )

*Not to scale*

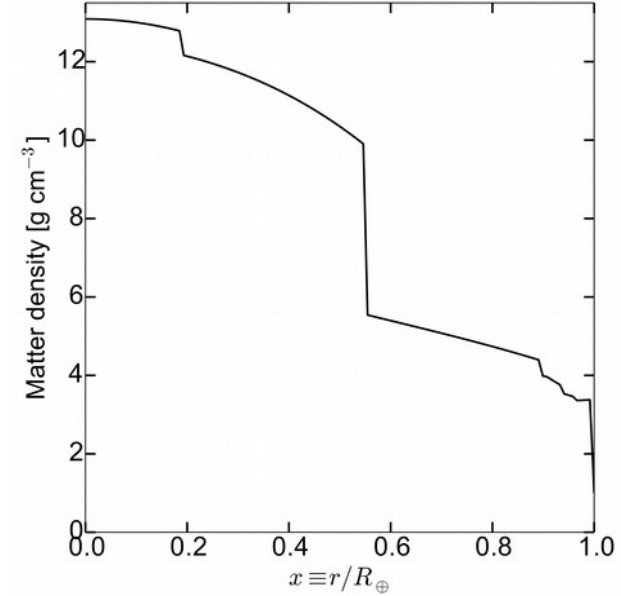
# The total potential



## Earth:



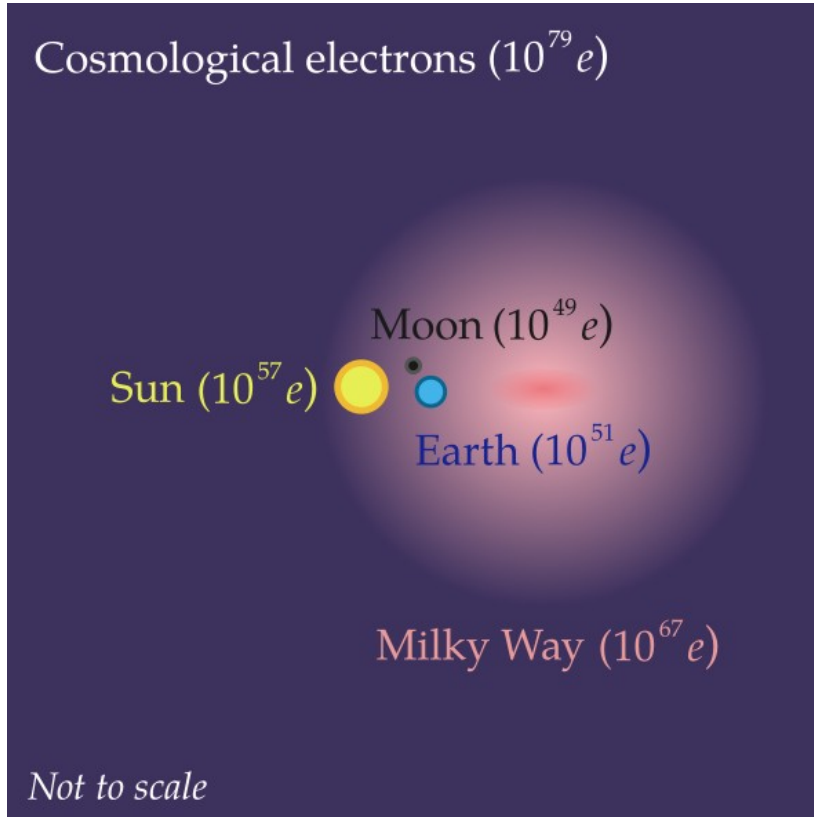
Preliminary Reference Earth Model  
Dziewonski & Anderson 1981



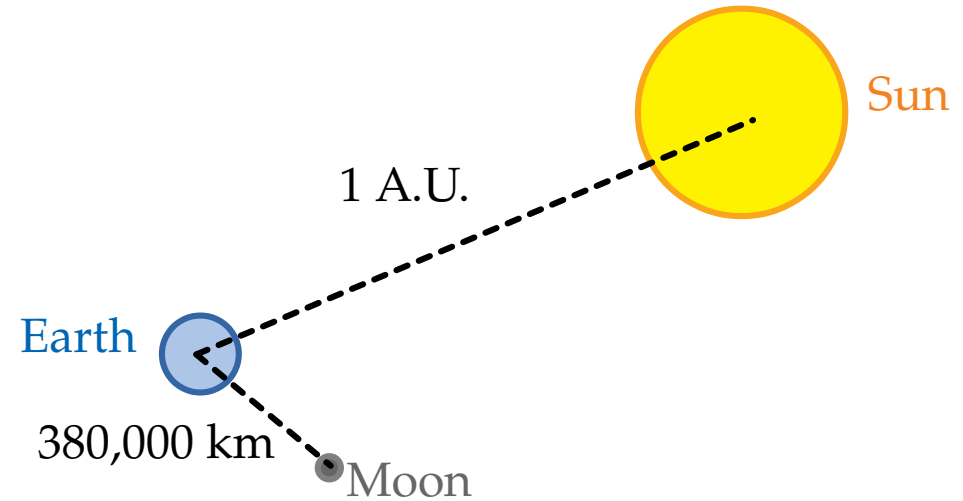
Neutrinos traverse different electron column depths

$$V_{e\beta} = V_{e\beta}^{\oplus}$$

# The total potential



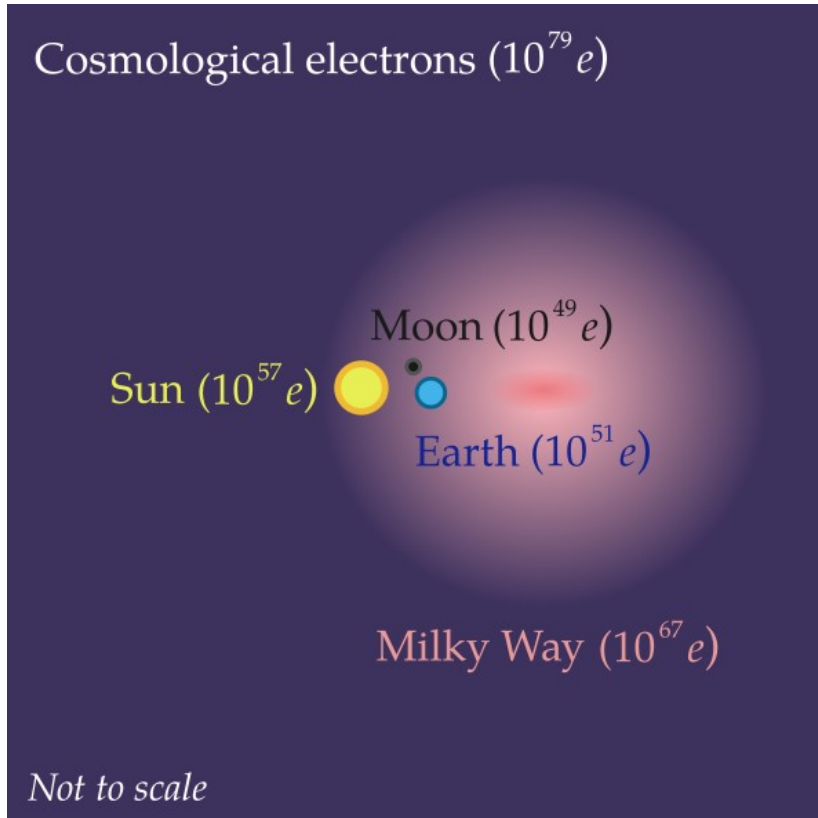
## Moon and Sun:



Treated as point sources of electrons

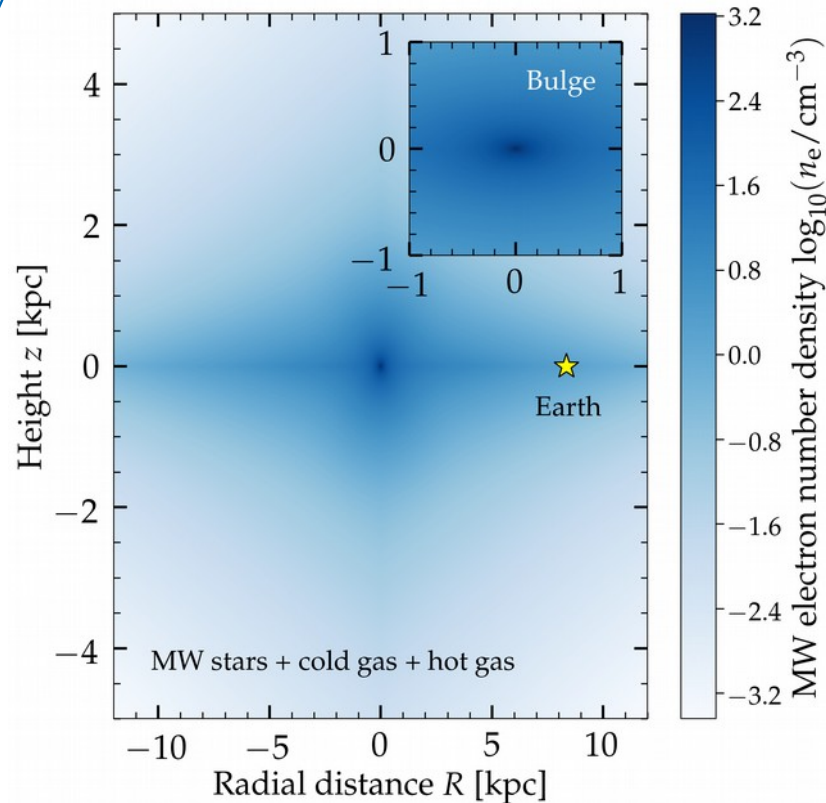
$$V_{e\beta} = V_{e\beta}^{\oplus} + V_{e\beta}^{\text{Moon}} + V_{e\beta}^{\odot}$$

# The total potential



## Milky Way:

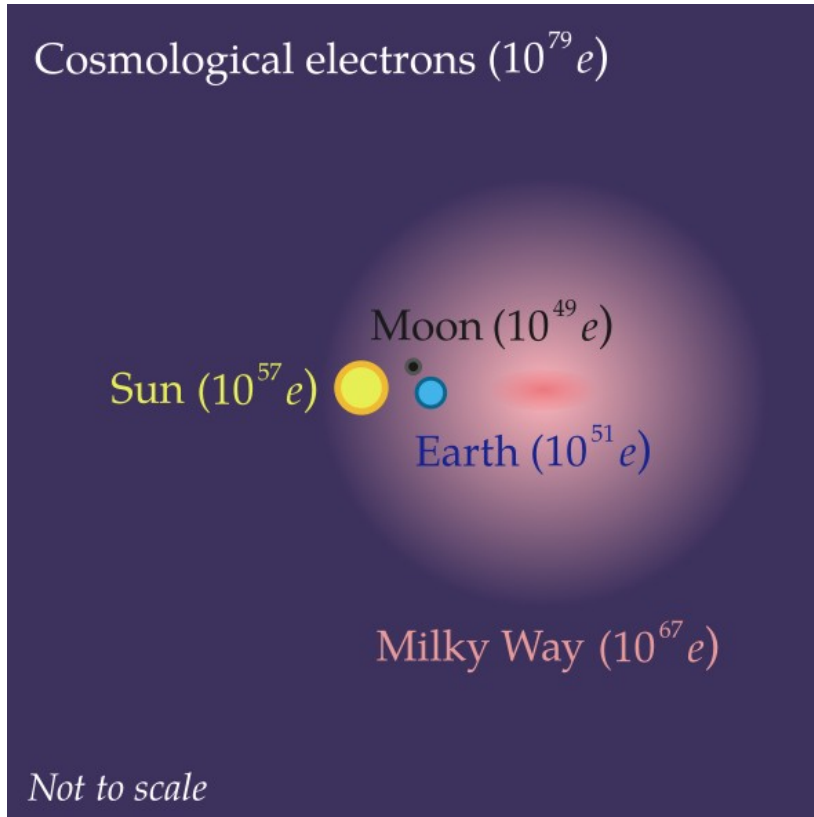
P. McMillan 2011  
M.J. Miller & J.N. Bregman 2013



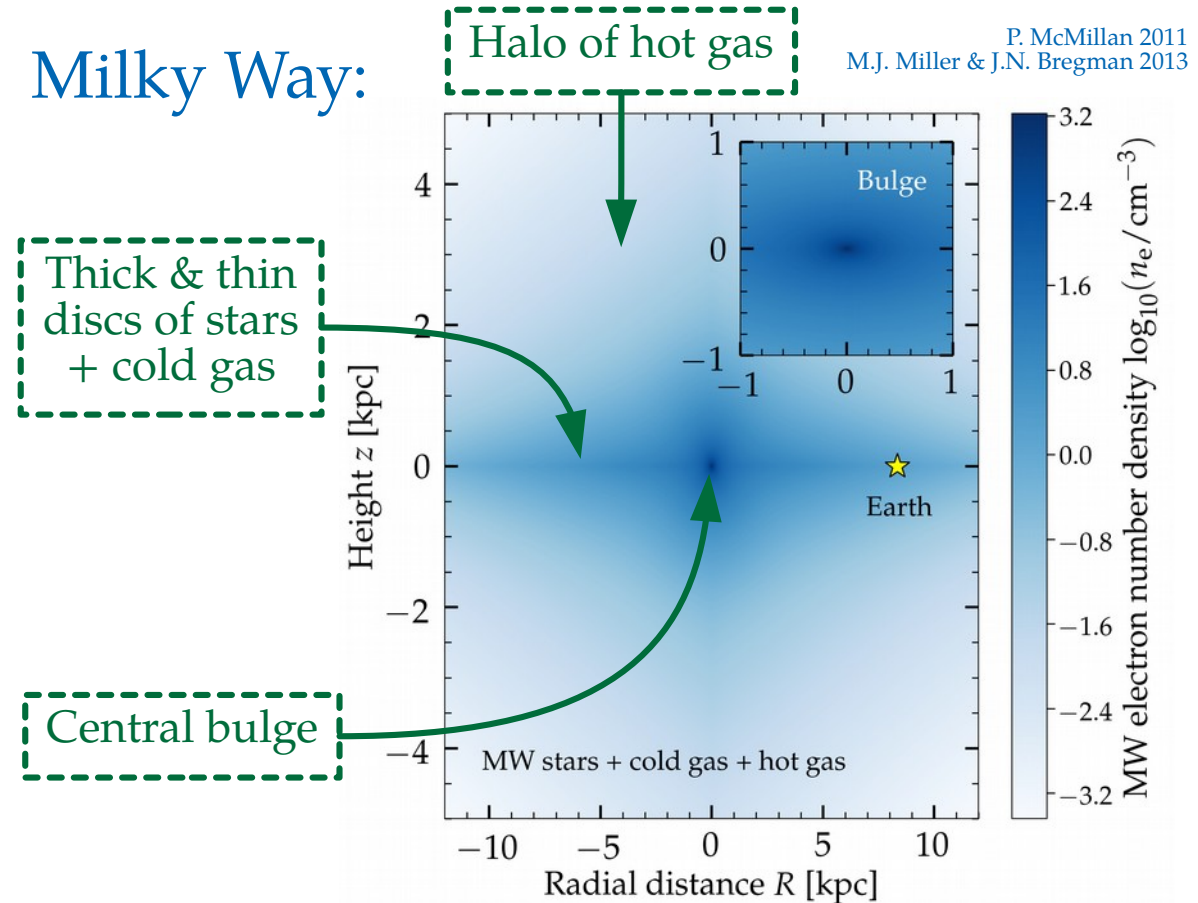
$$V_{e\beta} = V_{e\beta}^{\oplus} + V_{e\beta}^{\text{Moon}} + V_{e\beta}^{\odot} + V_{e\beta}^{\text{MW}}$$



# The total potential



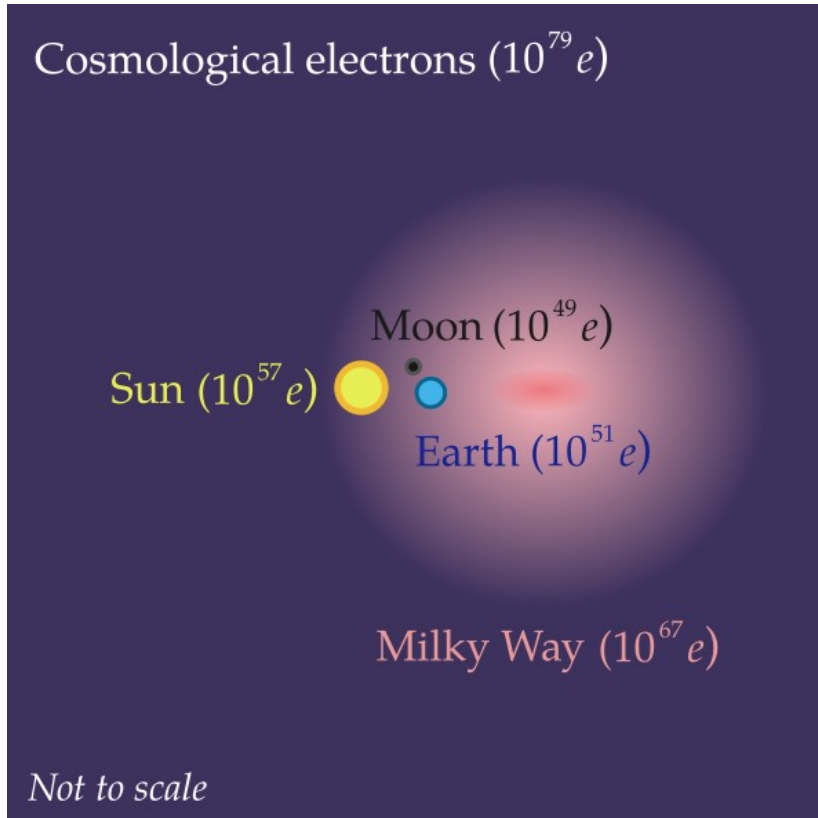
Milky Way:



P. McMillan 2011  
M.J. Miller & J.N. Bregman 2013

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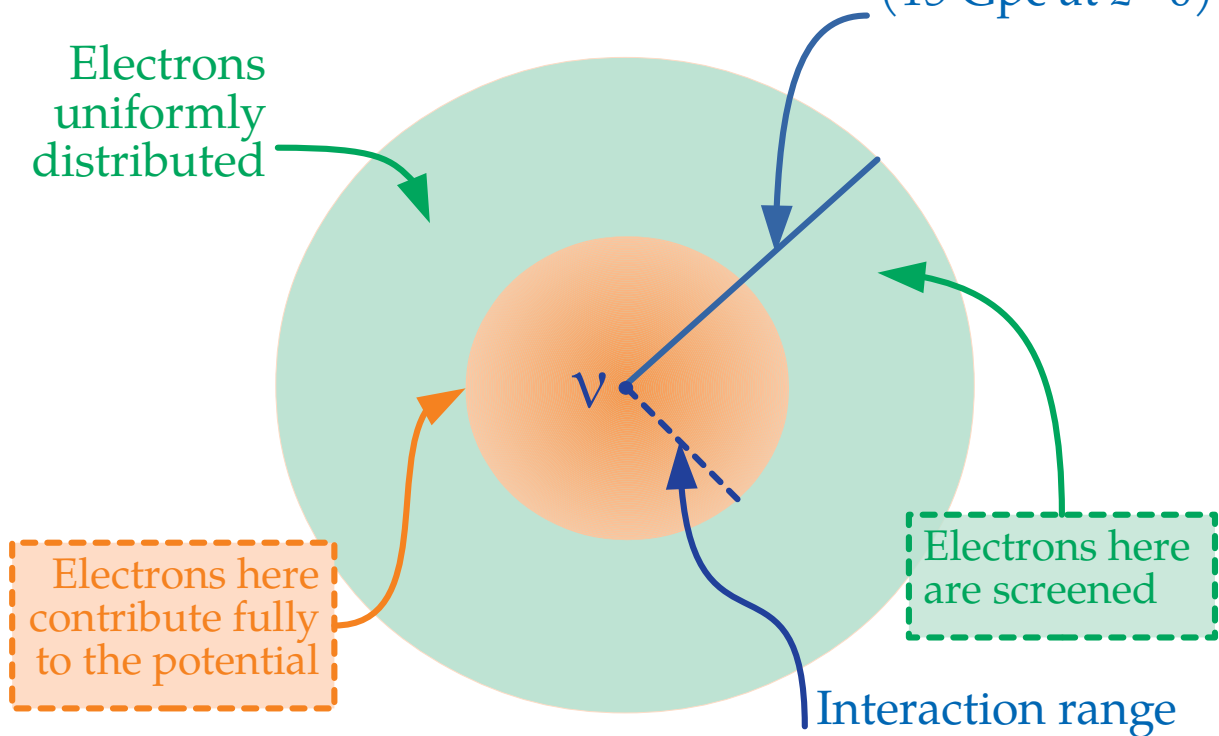
# The total potential



## Cosmological electrons:

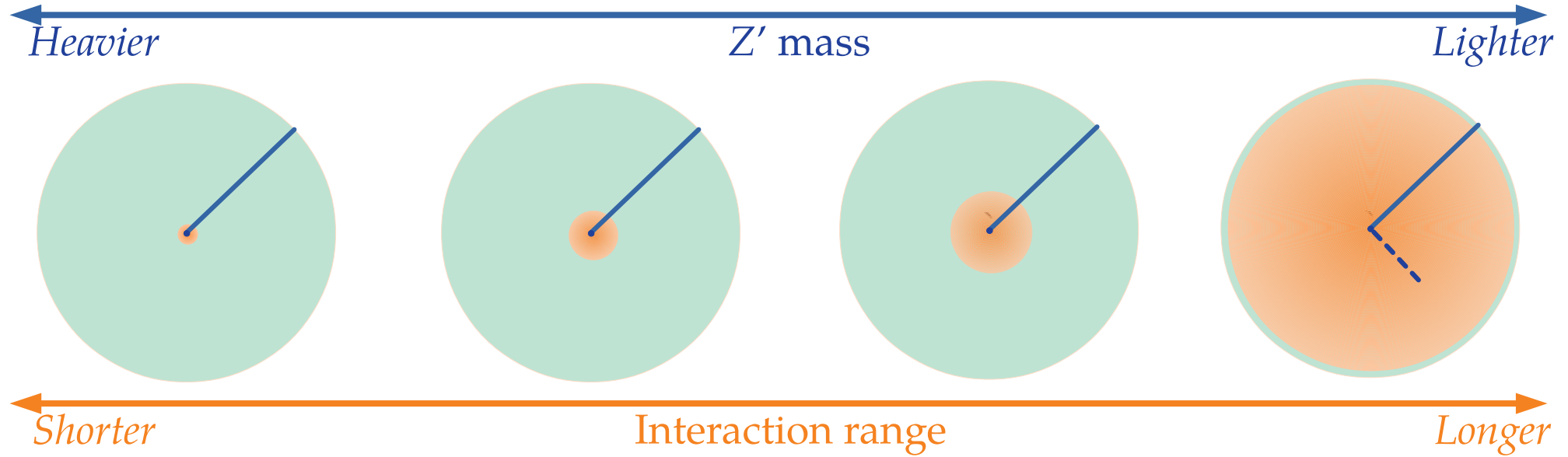
Electrons  
uniformly  
distributed

Causal horizon  
(15 Gpc at  $z=0$ )



$$V_{e\beta} = V_{e\beta}^{\oplus} + V_{e\beta}^{\text{Moon}} + V_{e\beta}^{\odot} + V_{e\beta}^{\text{MW}} + V_{e\beta}^{\text{cos}}$$

# The total potential



$$V_{e\beta} = V_{e\beta}^{\oplus} + V_{e\beta}^{\text{Moon}} + V_{e\beta}^{\odot} + V_{e\beta}^{\text{MW}} + V_{e\beta}^{\cos}$$

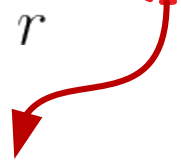
# Electrons in the local and distant Universe

Potential:

$$V_{e\beta} \propto \frac{1}{r} e^{-m'_{e\beta} r}$$

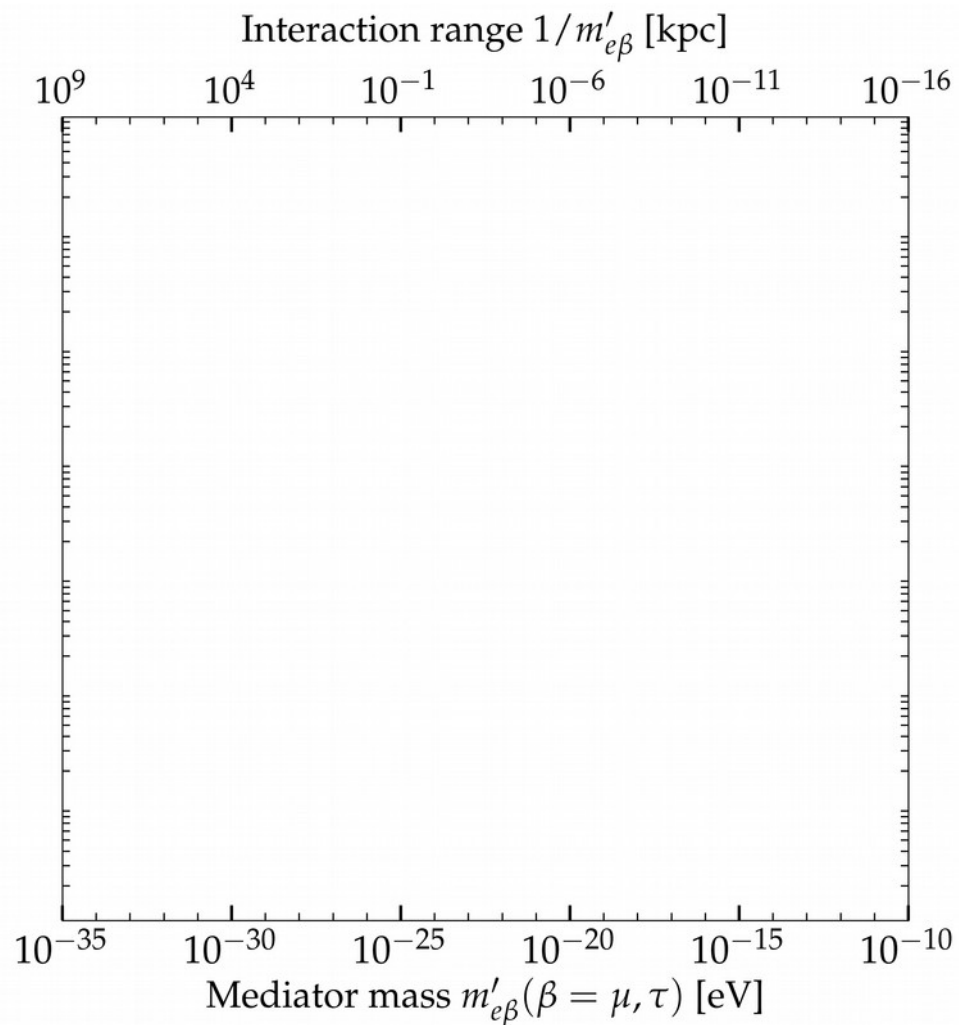
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# Electrons in the local and distant Universe



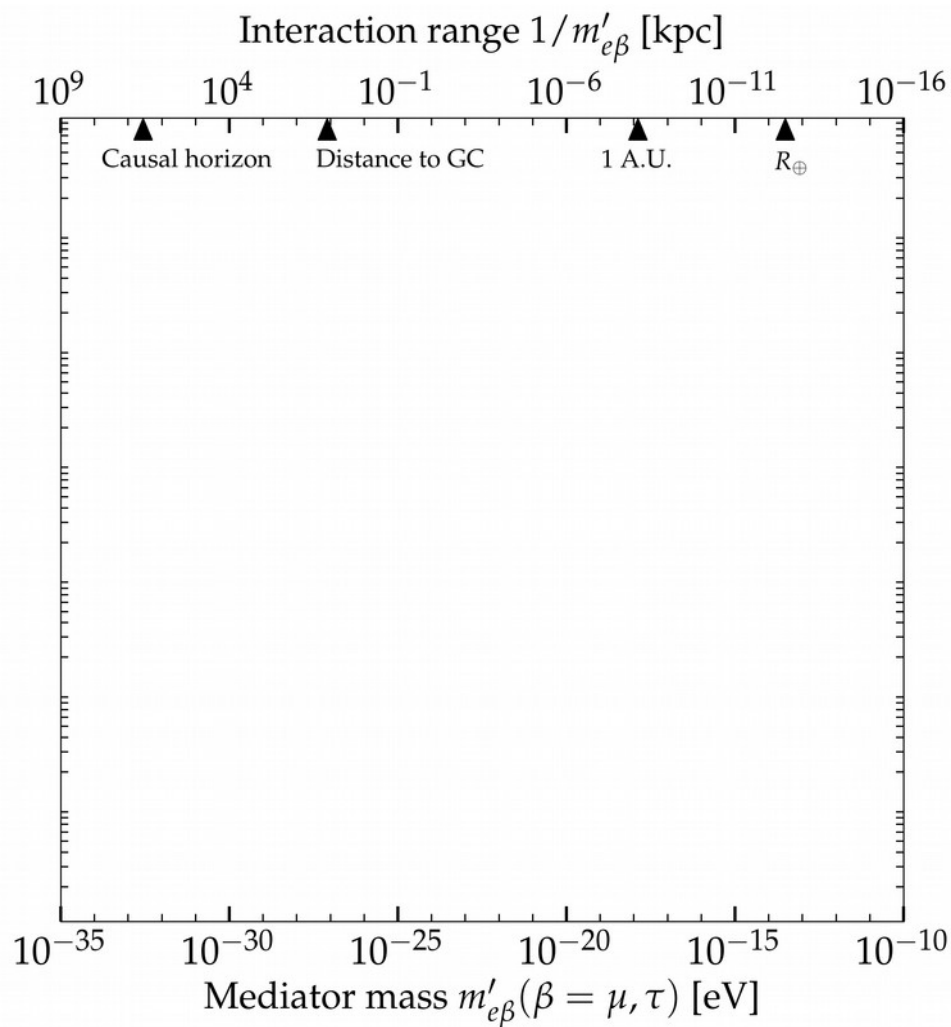
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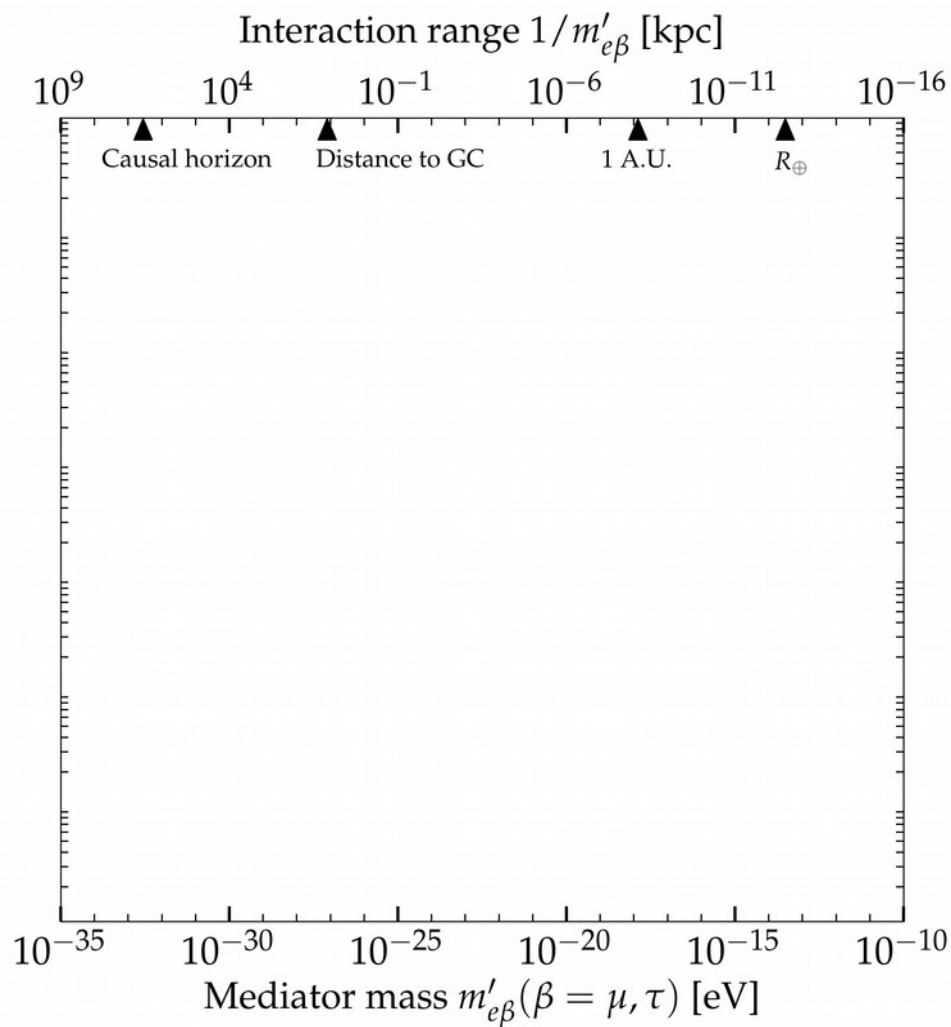


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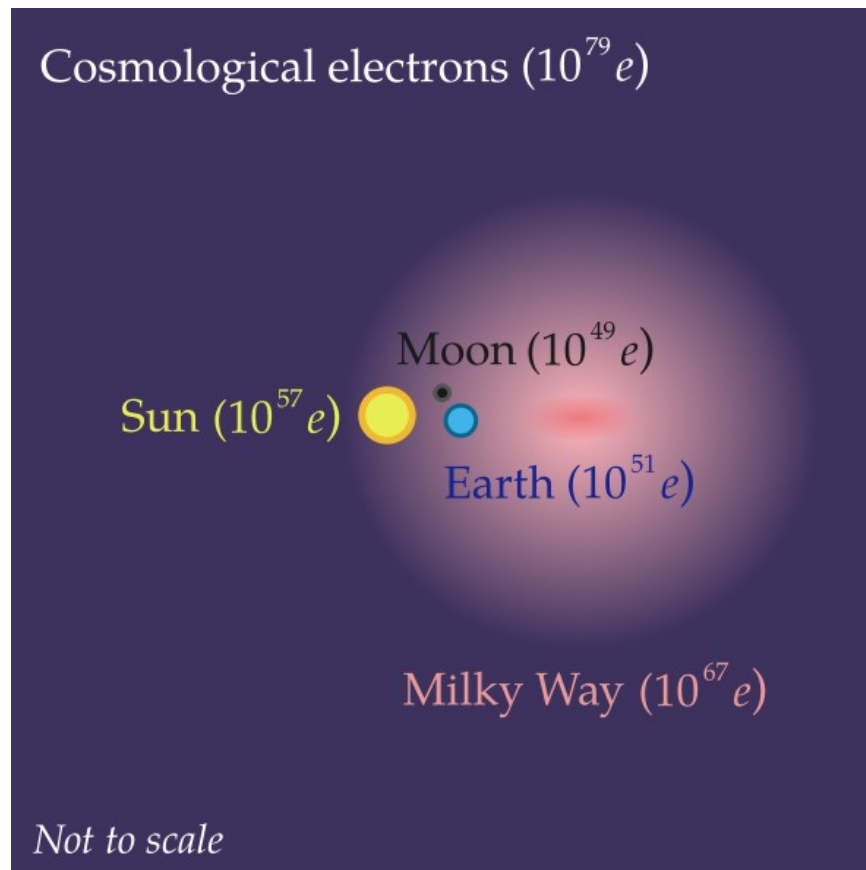
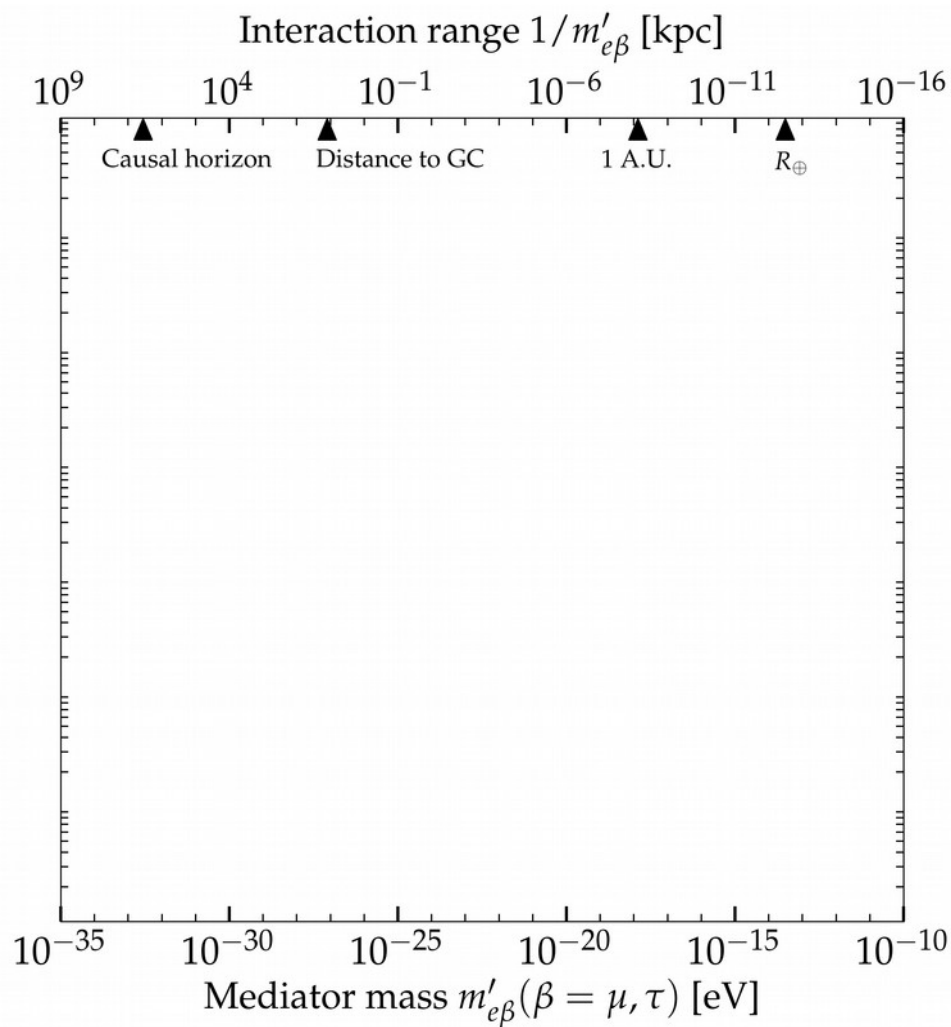
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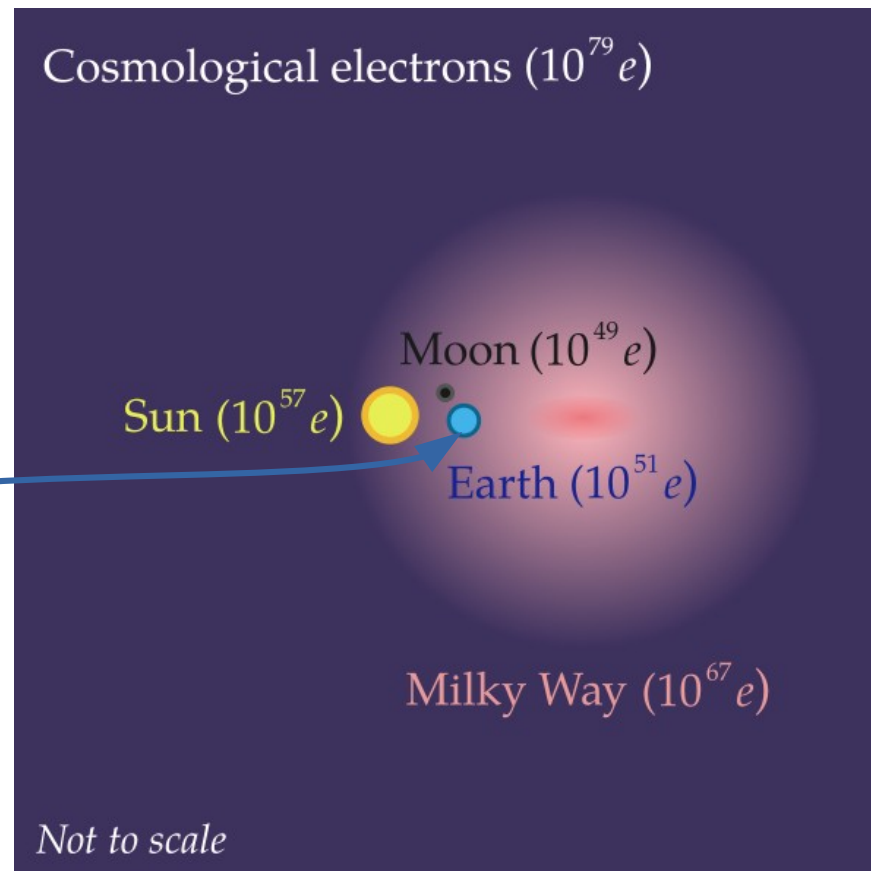
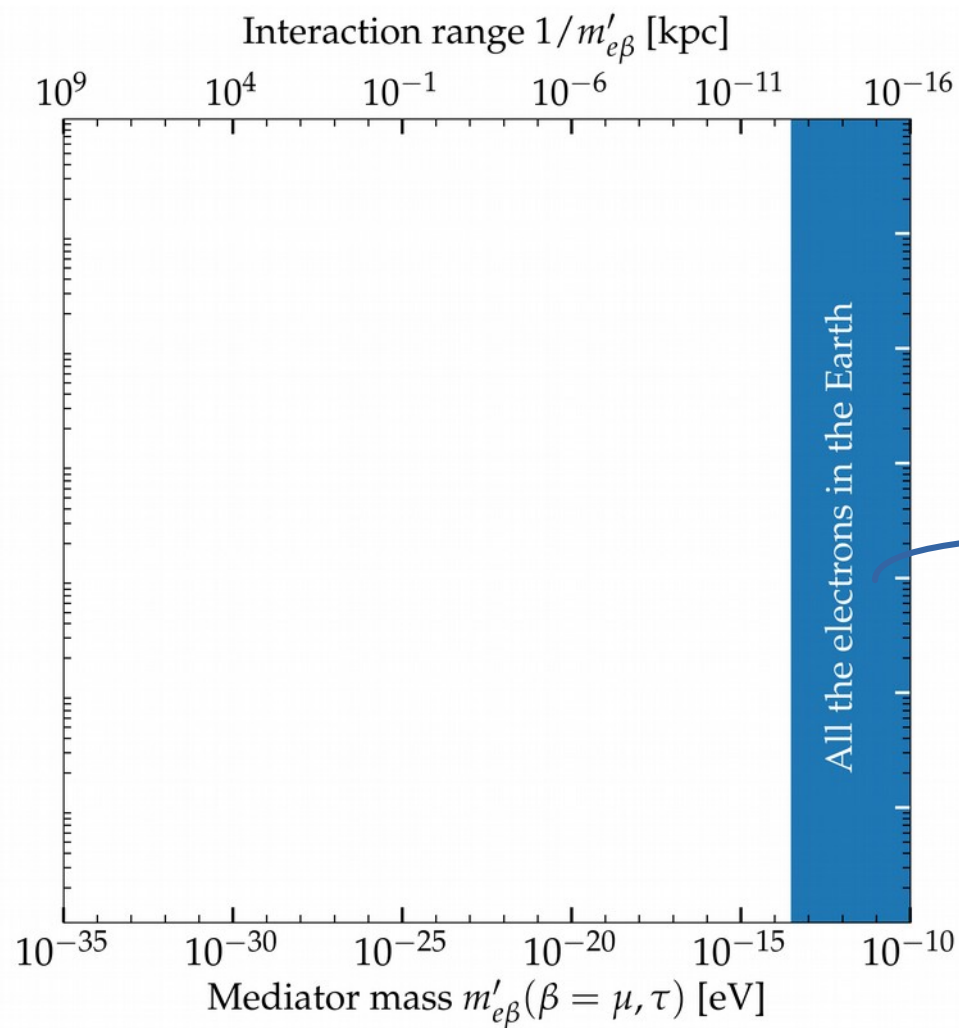
Interaction range:  $\frac{1}{m'_{e\beta}}$

Light mediators  
 $\Rightarrow$  Long interaction ranges

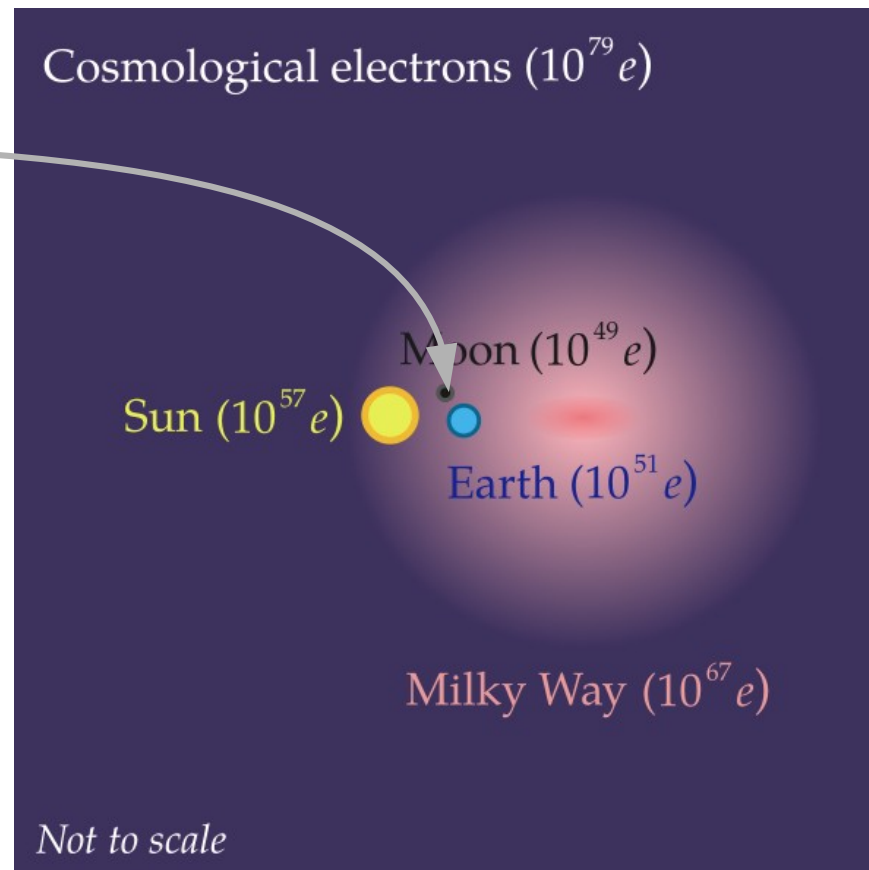
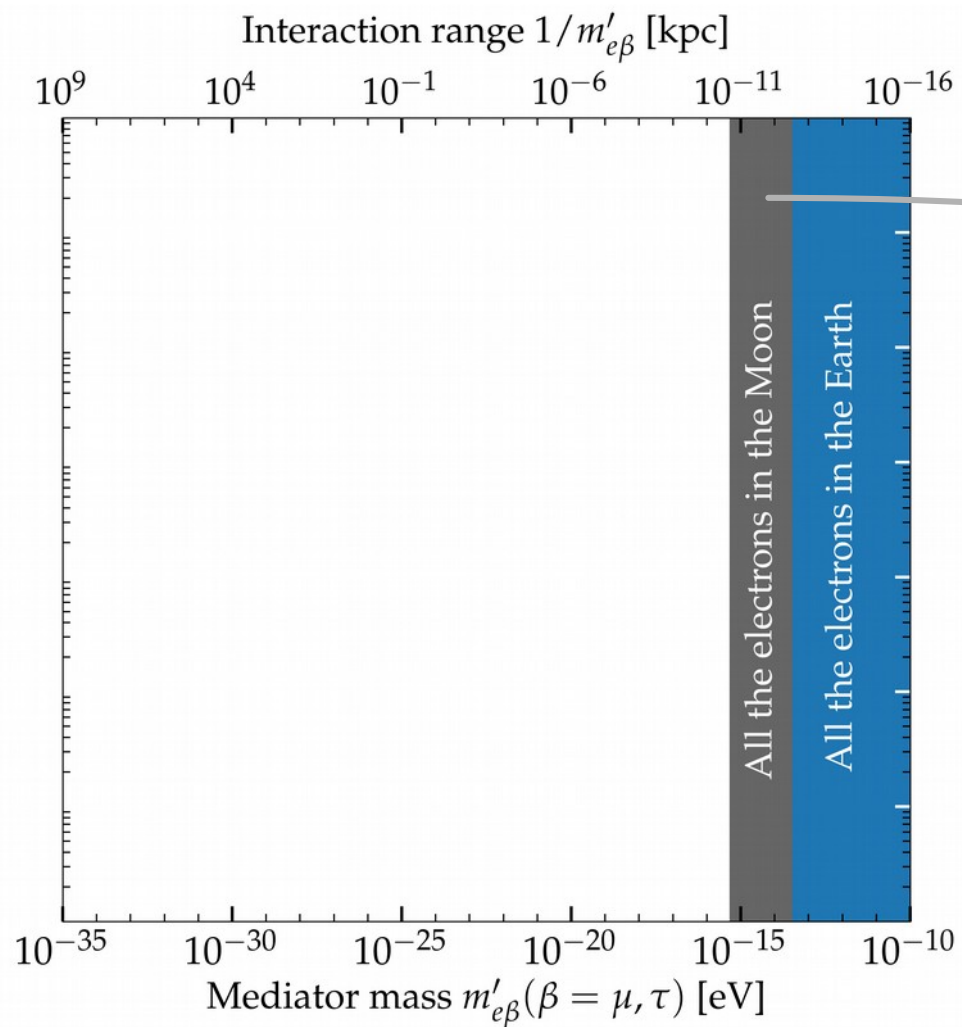
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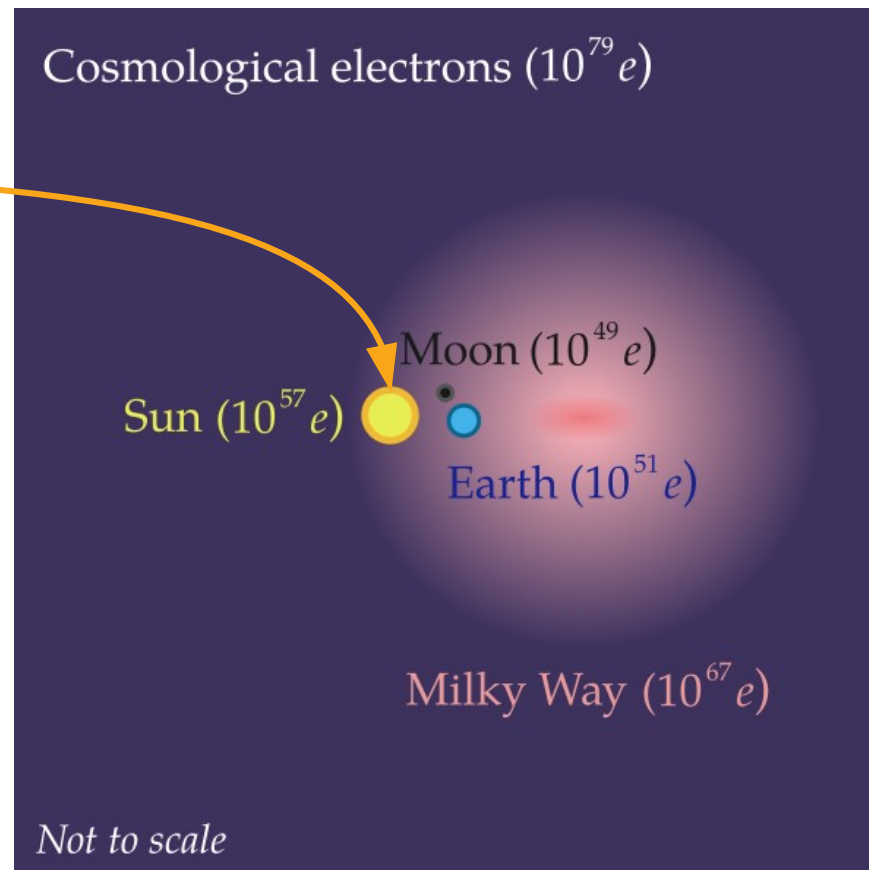
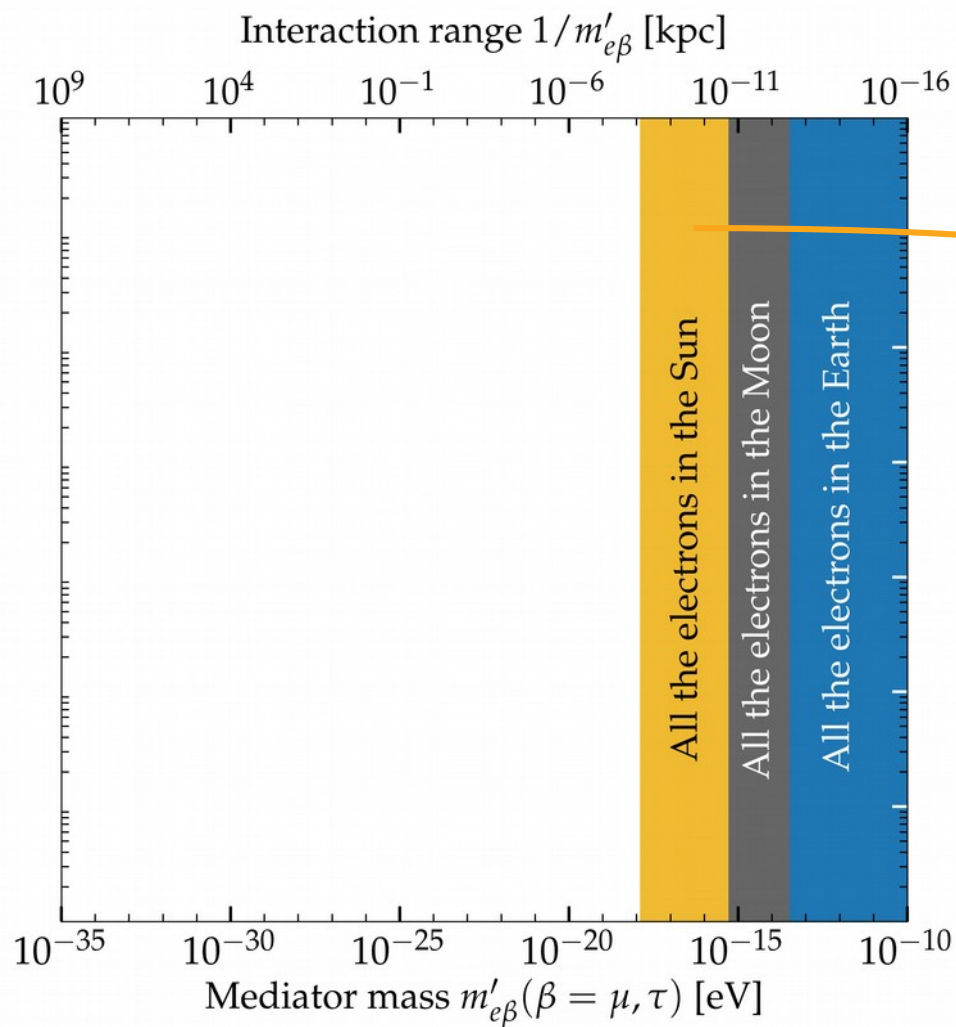
# Electrons in the local and distant Universe



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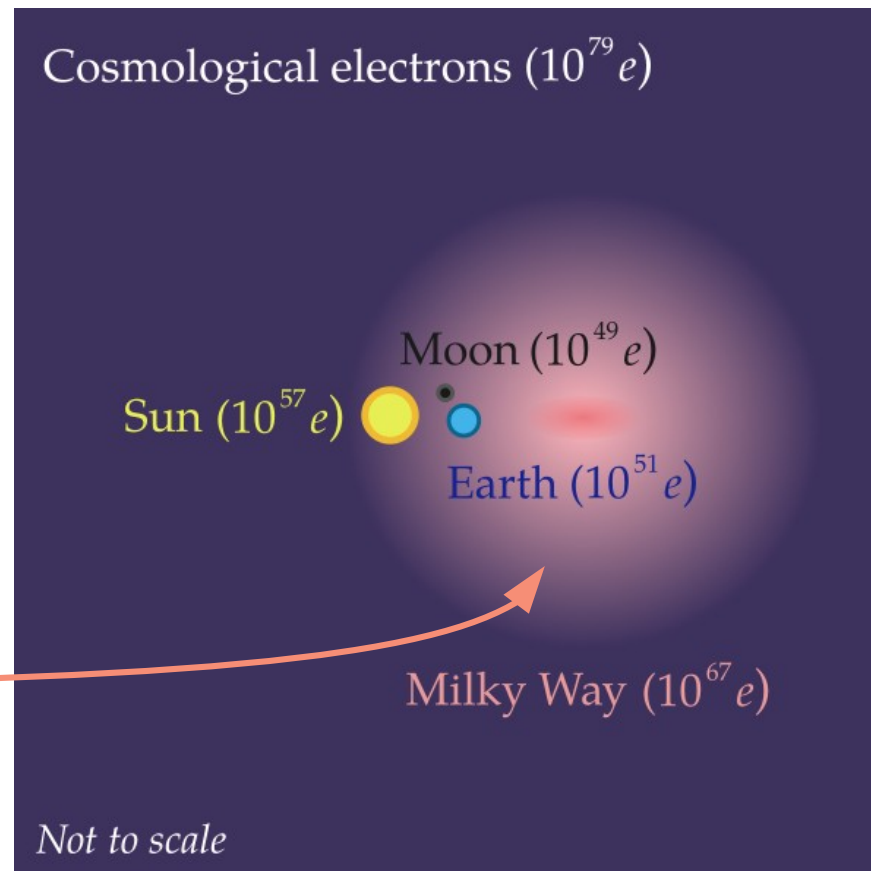
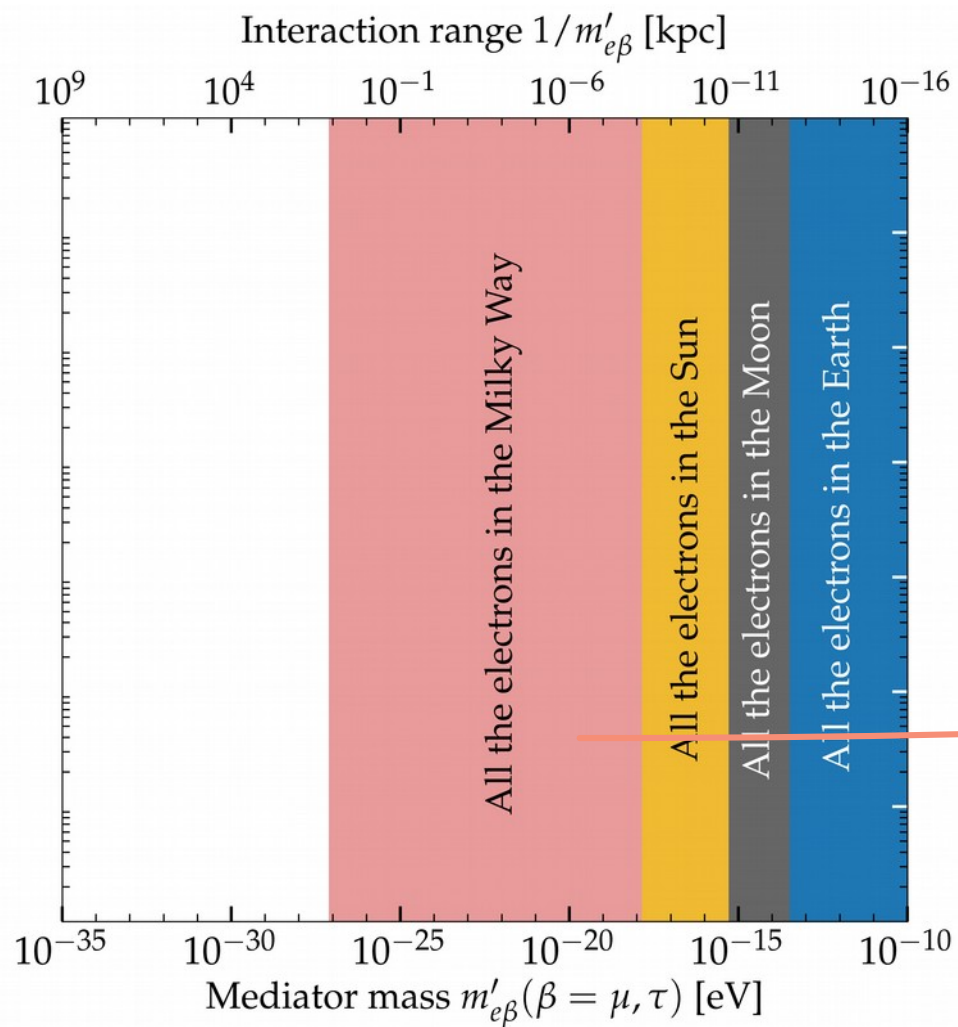


# Electrons in the local and distant Universe

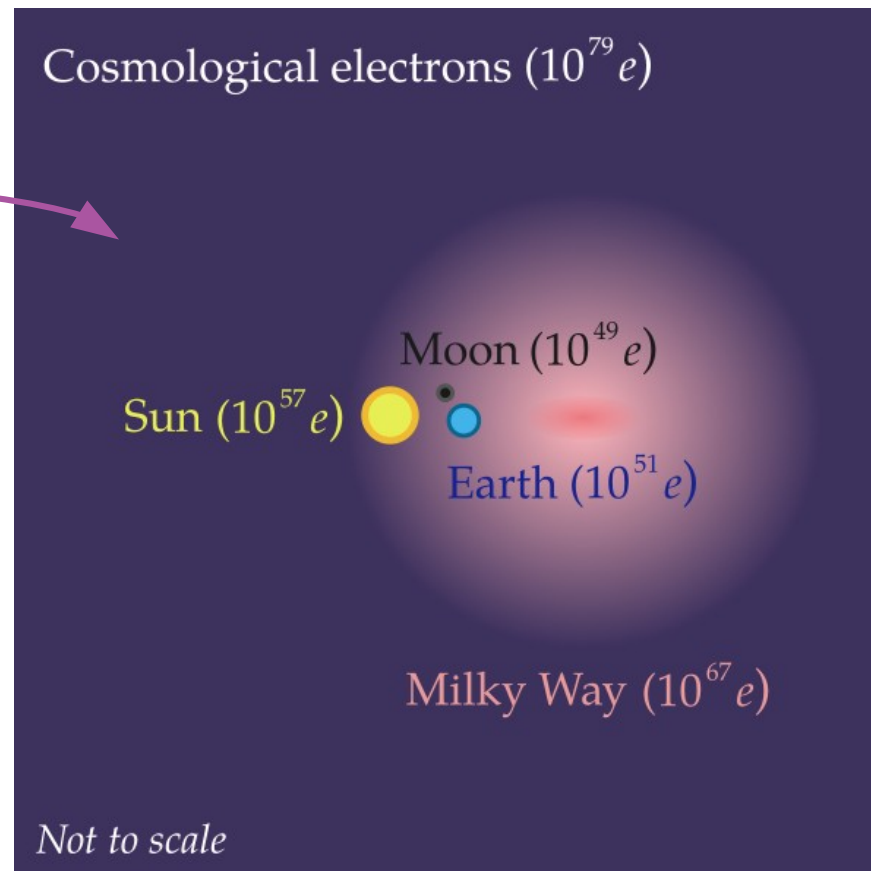
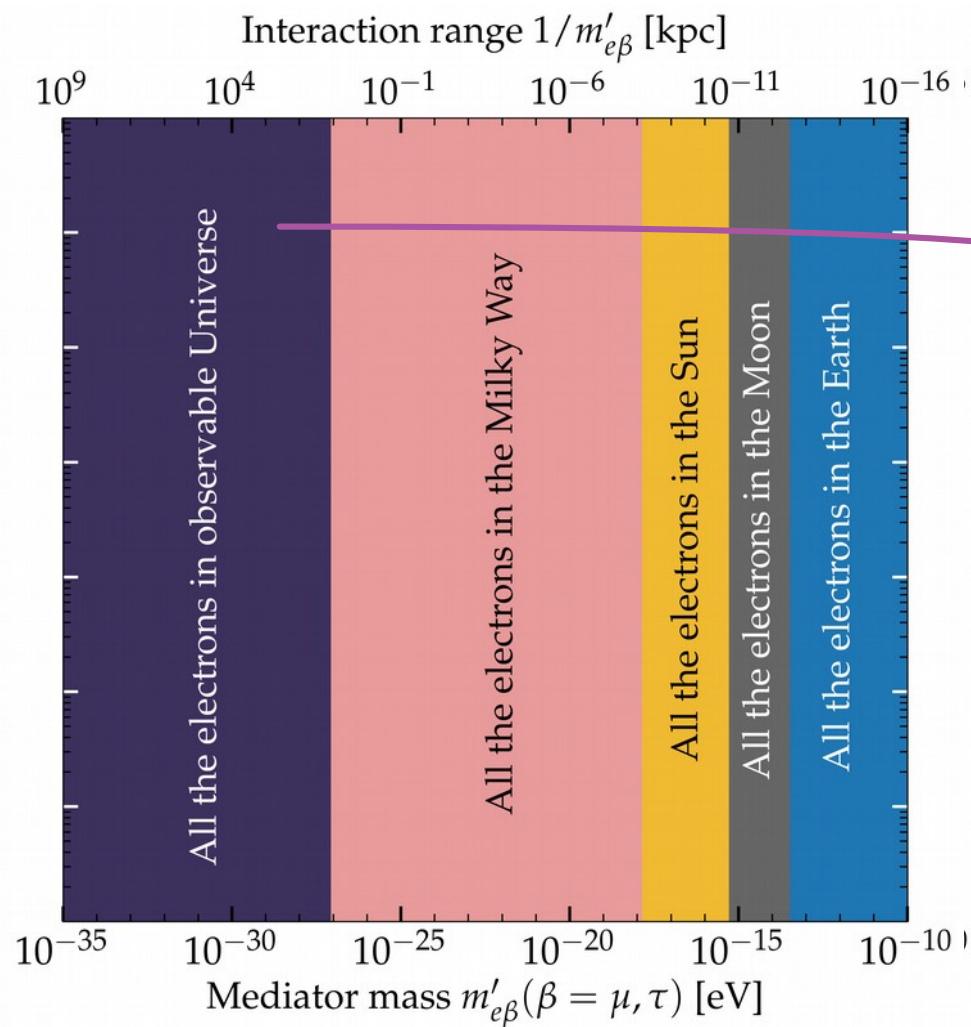




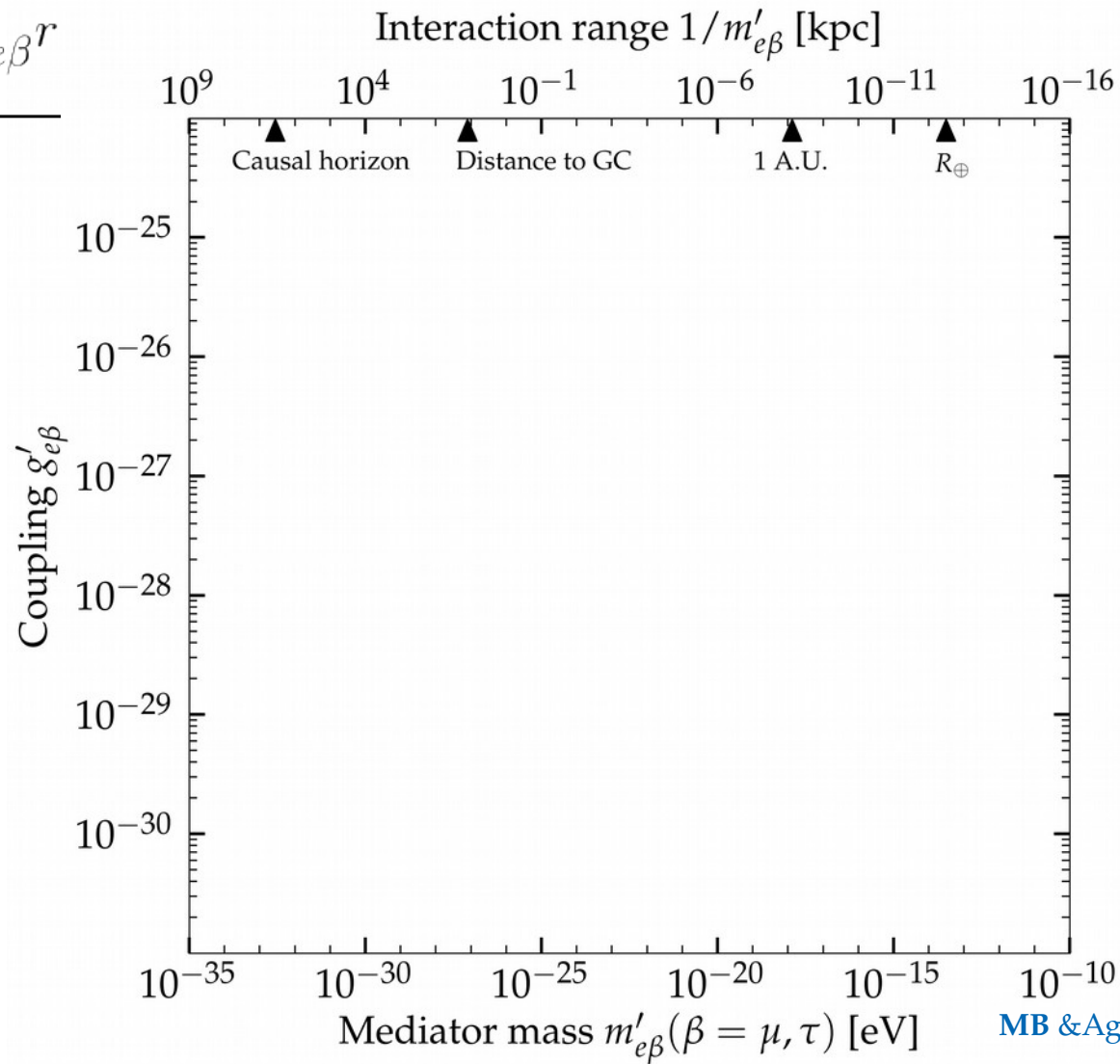
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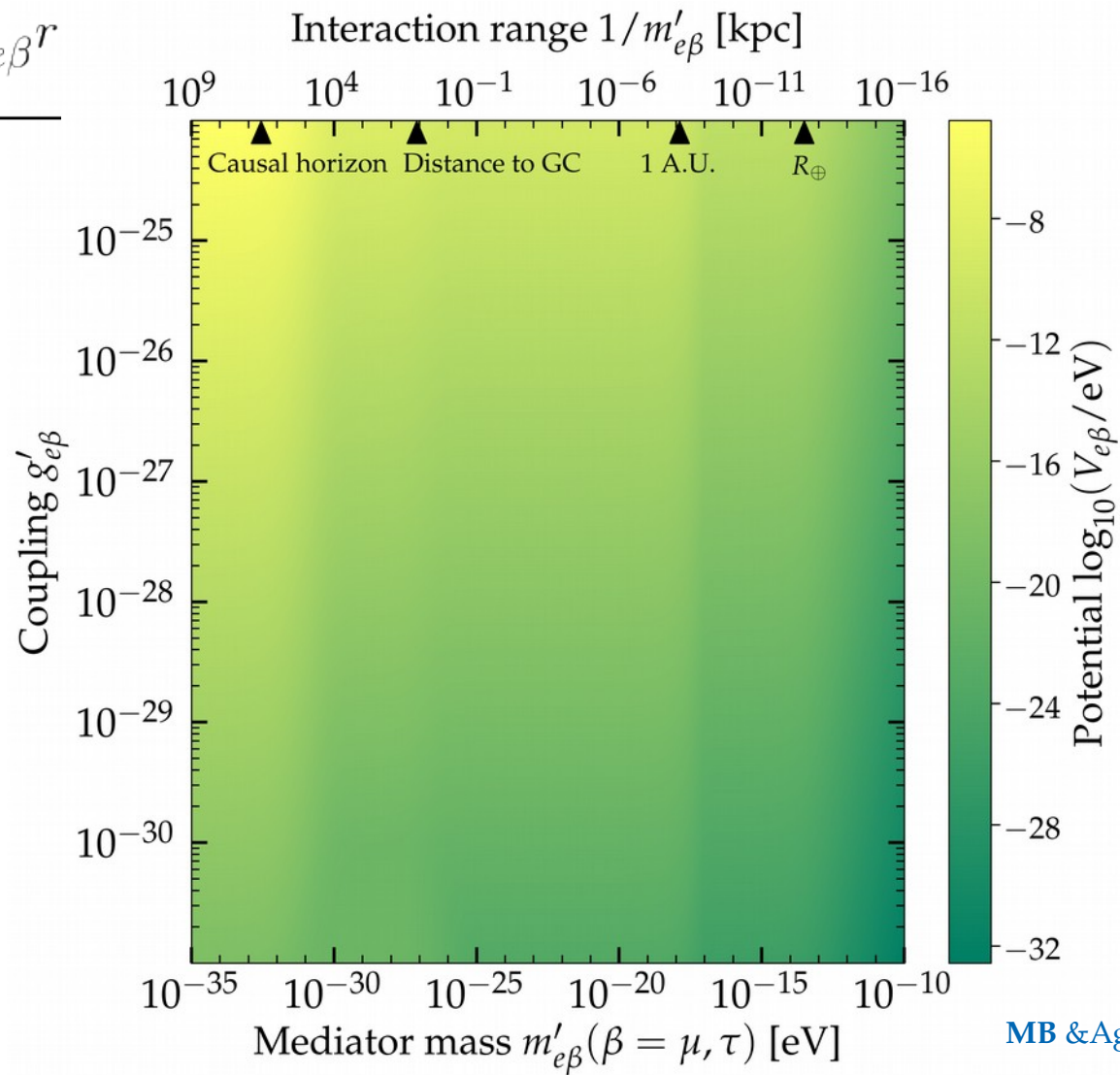


$$V_{e\beta} = \frac{g_{e\beta}'^2}{4\pi} \frac{e^{-m'_{e\beta} r}}{r}$$



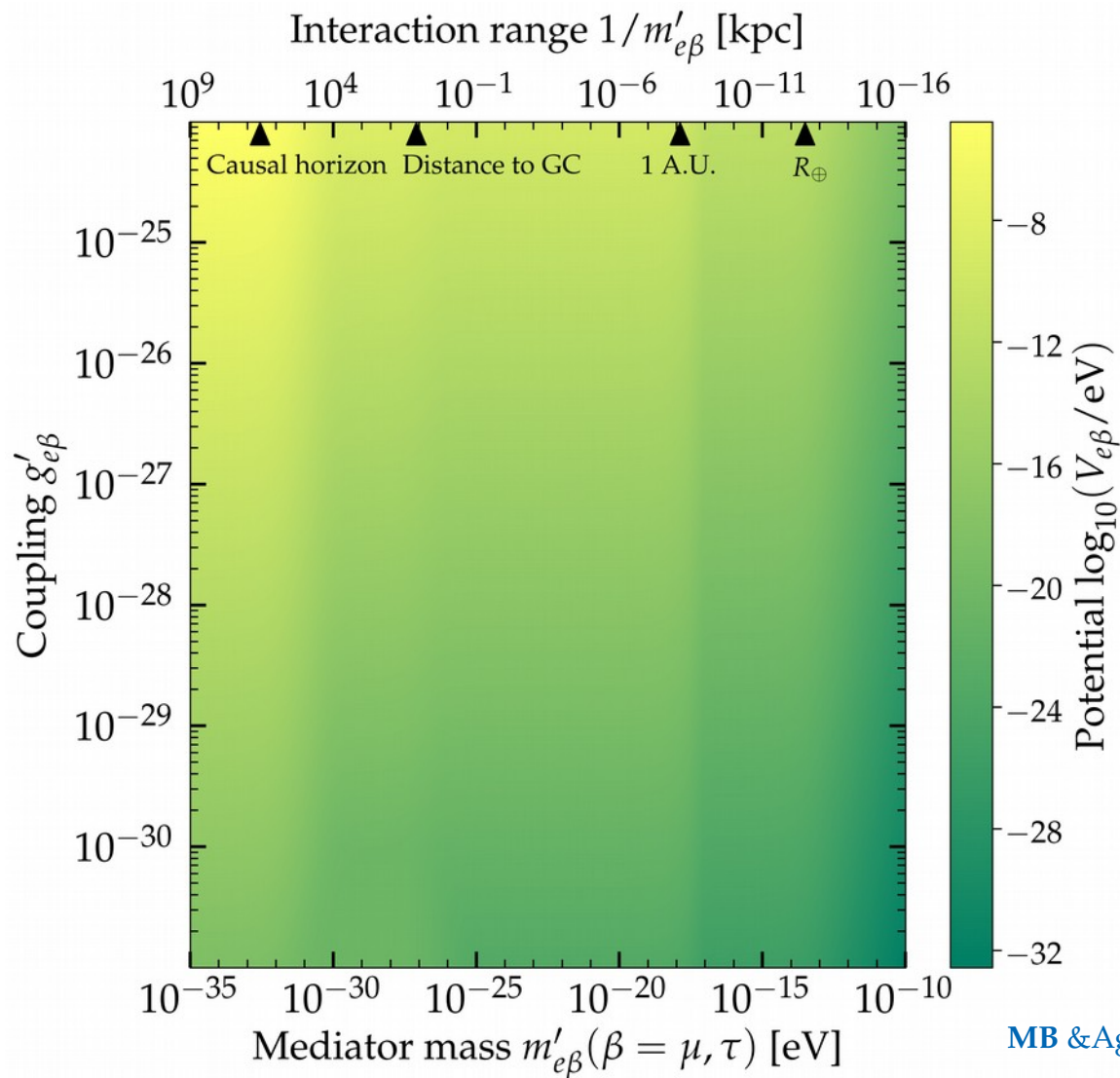
MB & Agarwalla, *PRL* 2019

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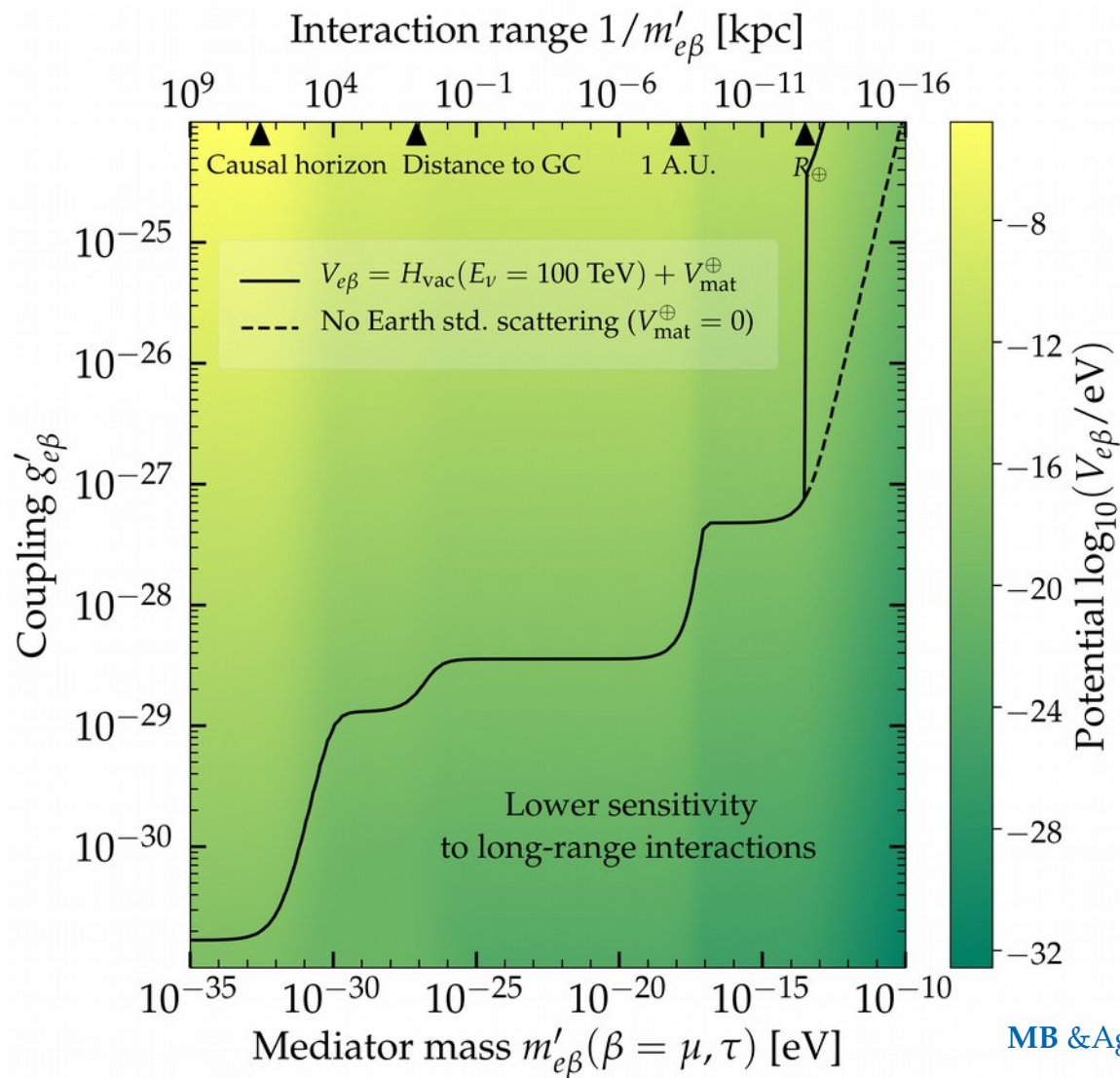
MB & Agarwalla, *PRL* 2019

$$\begin{aligned}
 g_{\text{strong}} &\sim 13.5 \\
 g_{\text{e.m.}} &\sim 0.3 \\
 g_{\text{weak}} &\sim 0.01 \\
 g_{\text{gravity}} &\sim 10^{-19}
 \end{aligned}$$



MB & Agarwalla, *PRL* 2019

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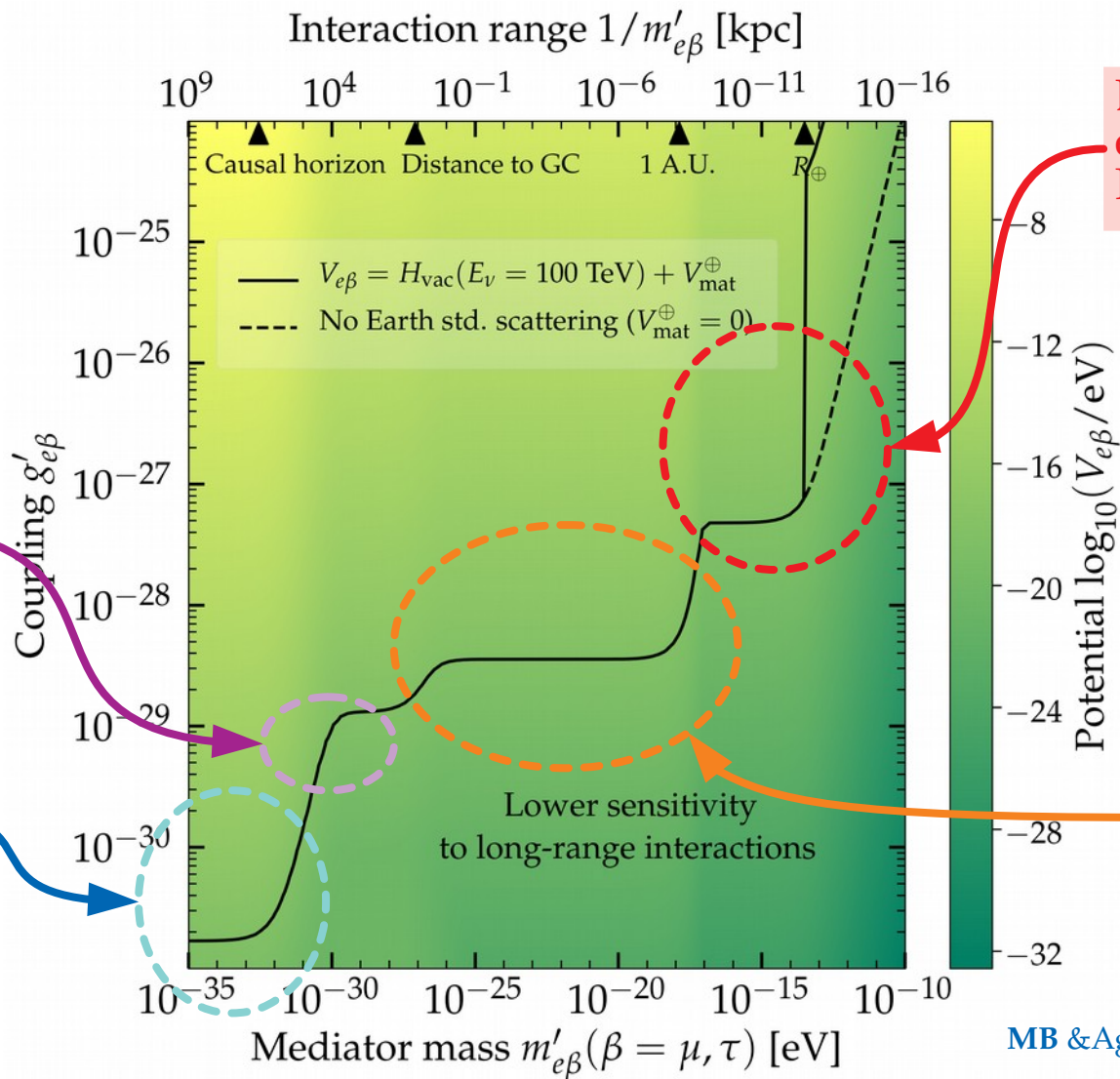


$g_{\text{strong}} \sim 13.5$   
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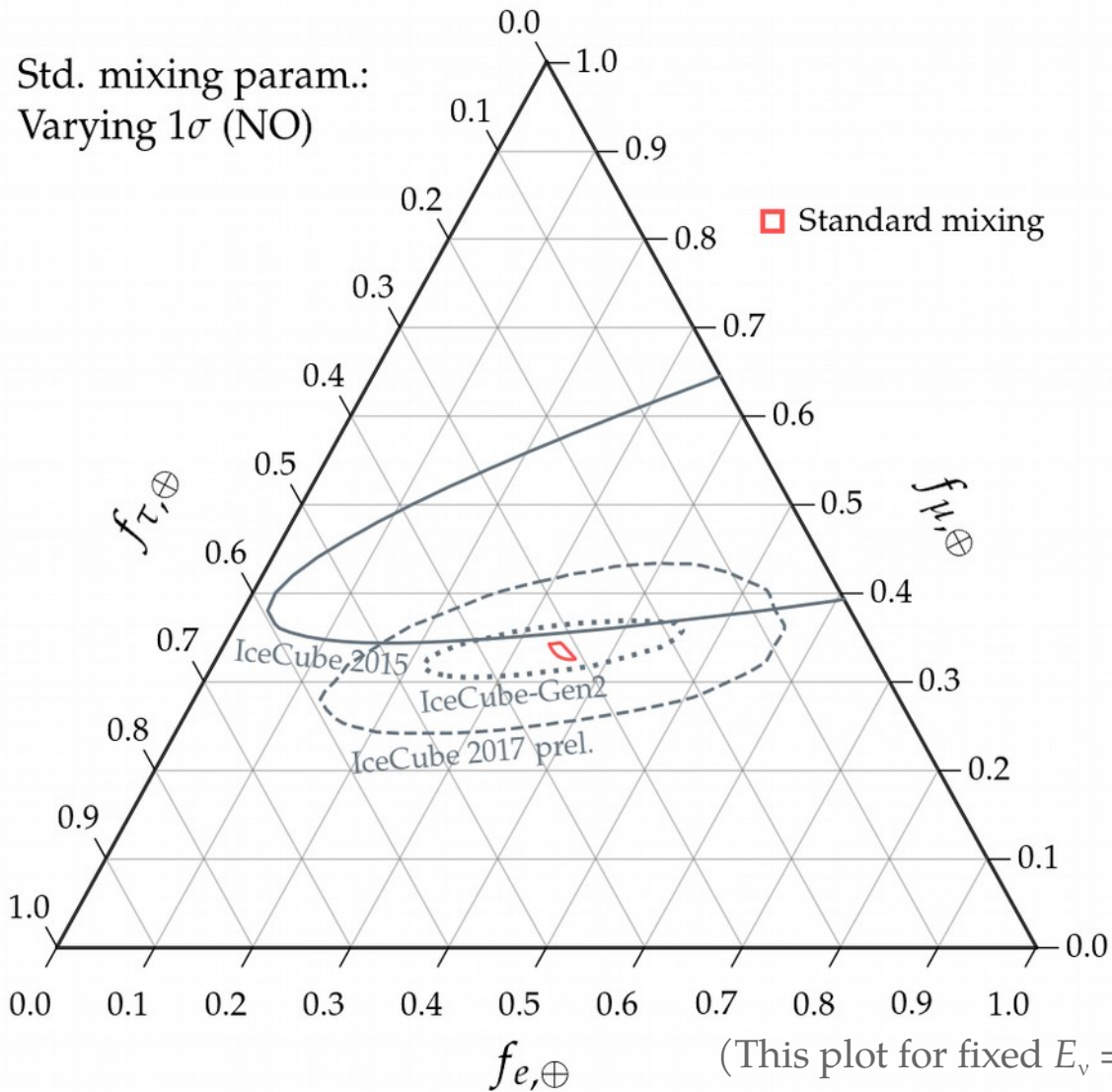
Dominated by Milky-Way  $e$

Dominated by cosmological  $e$

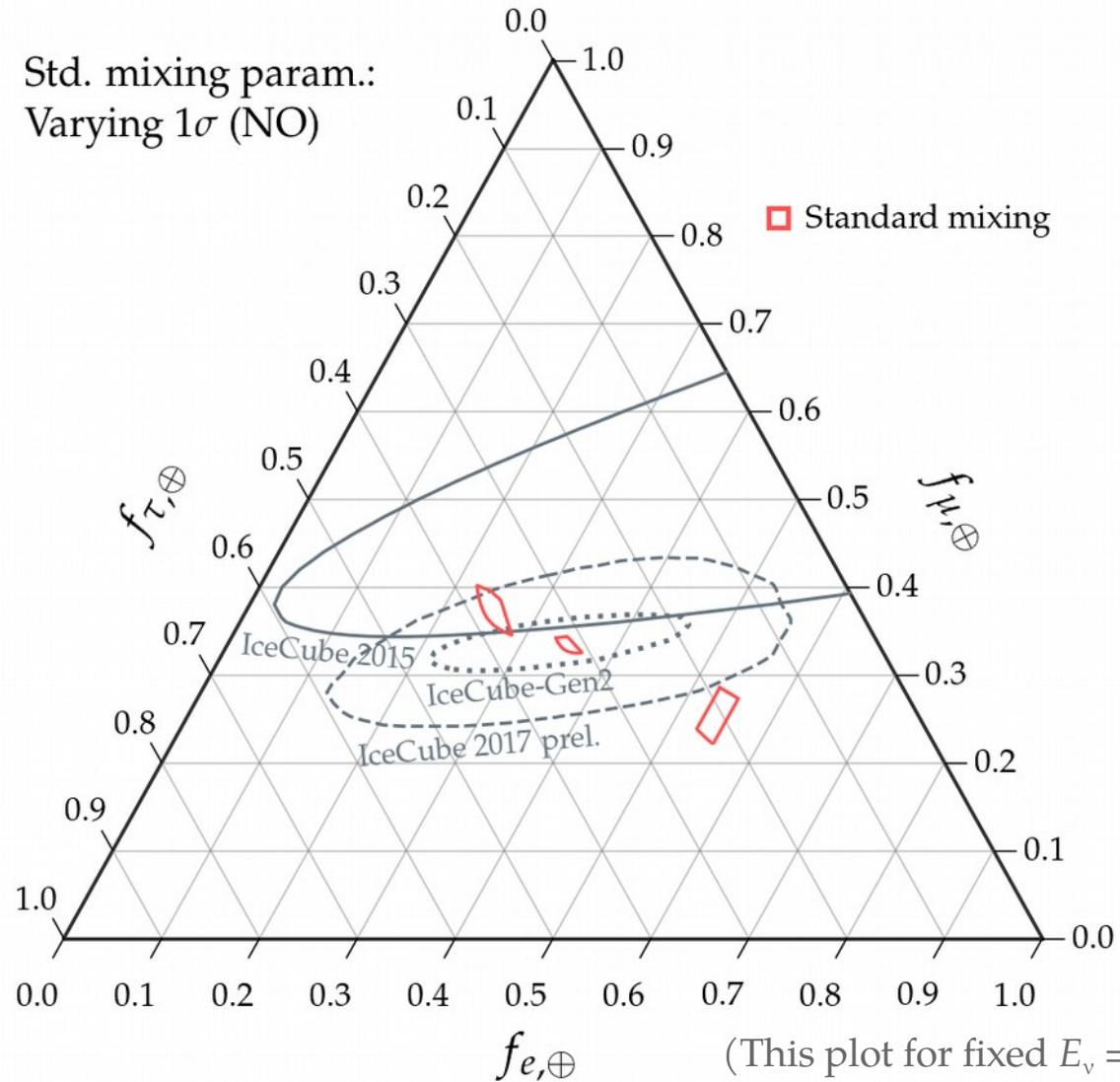


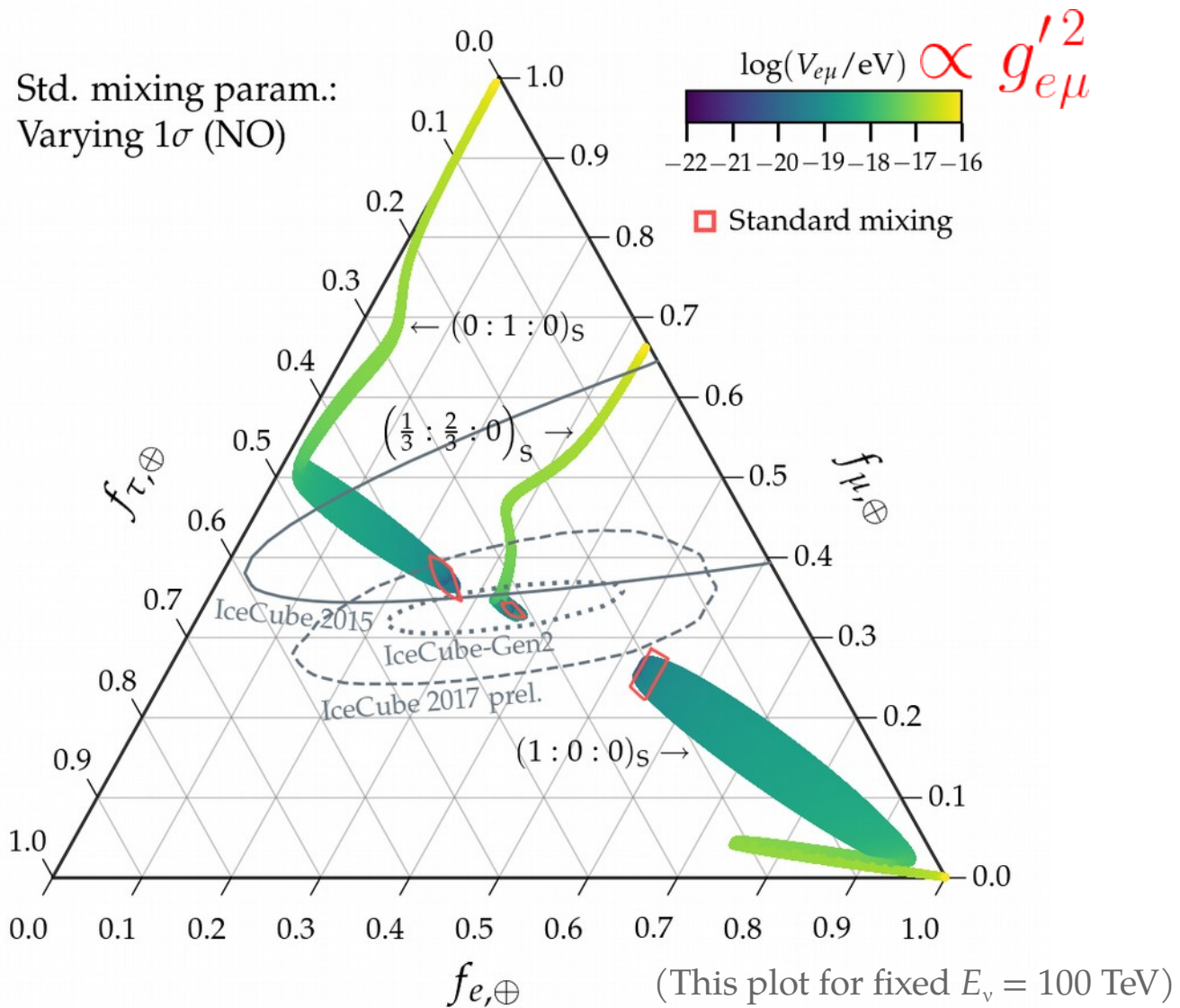
Dominated by electrons in the Earth + Moon

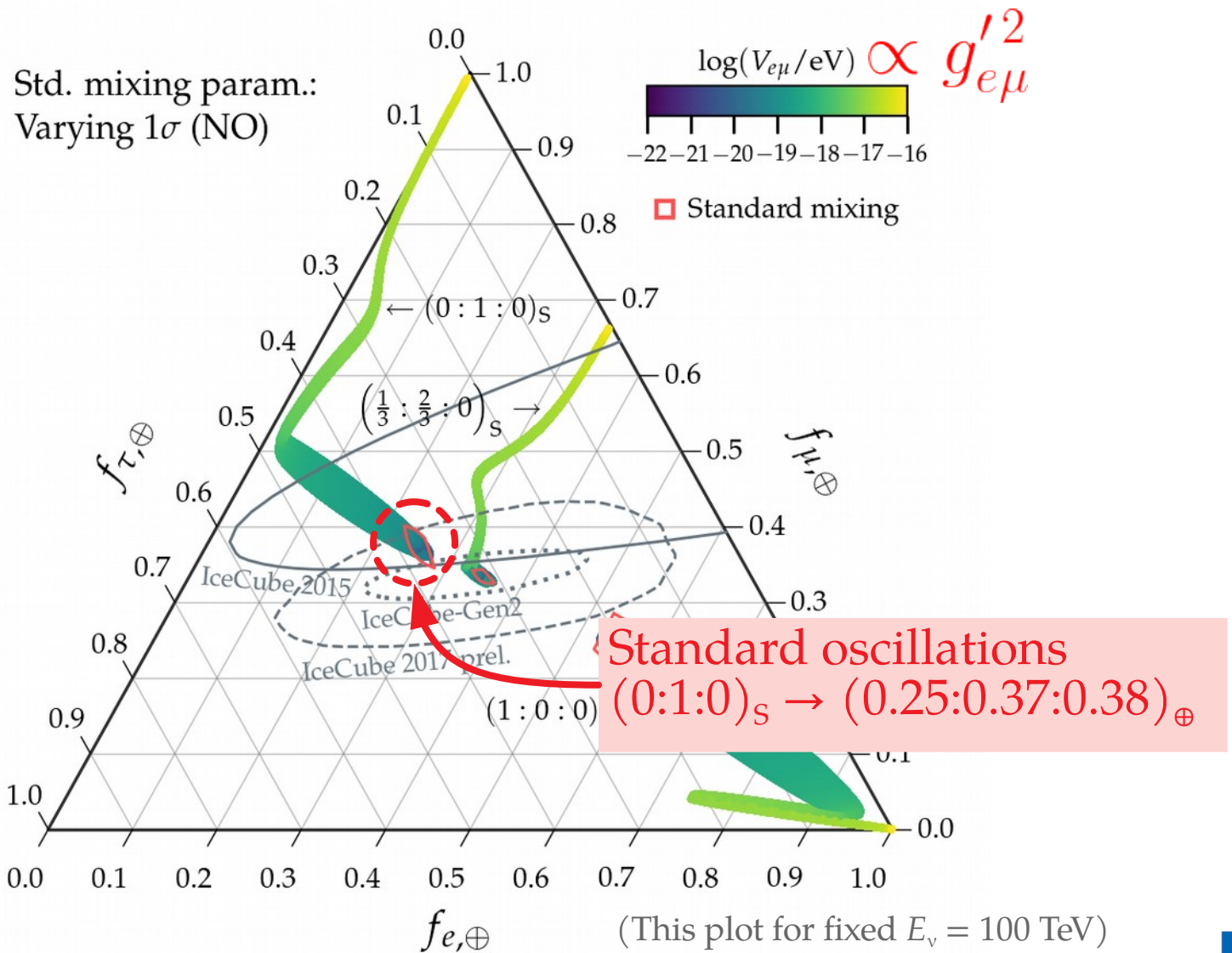
Dominated by solar electrons (+ Milky-Way  $e$ )



Std. mixing param.:  
Varying  $1\sigma$  (NO)



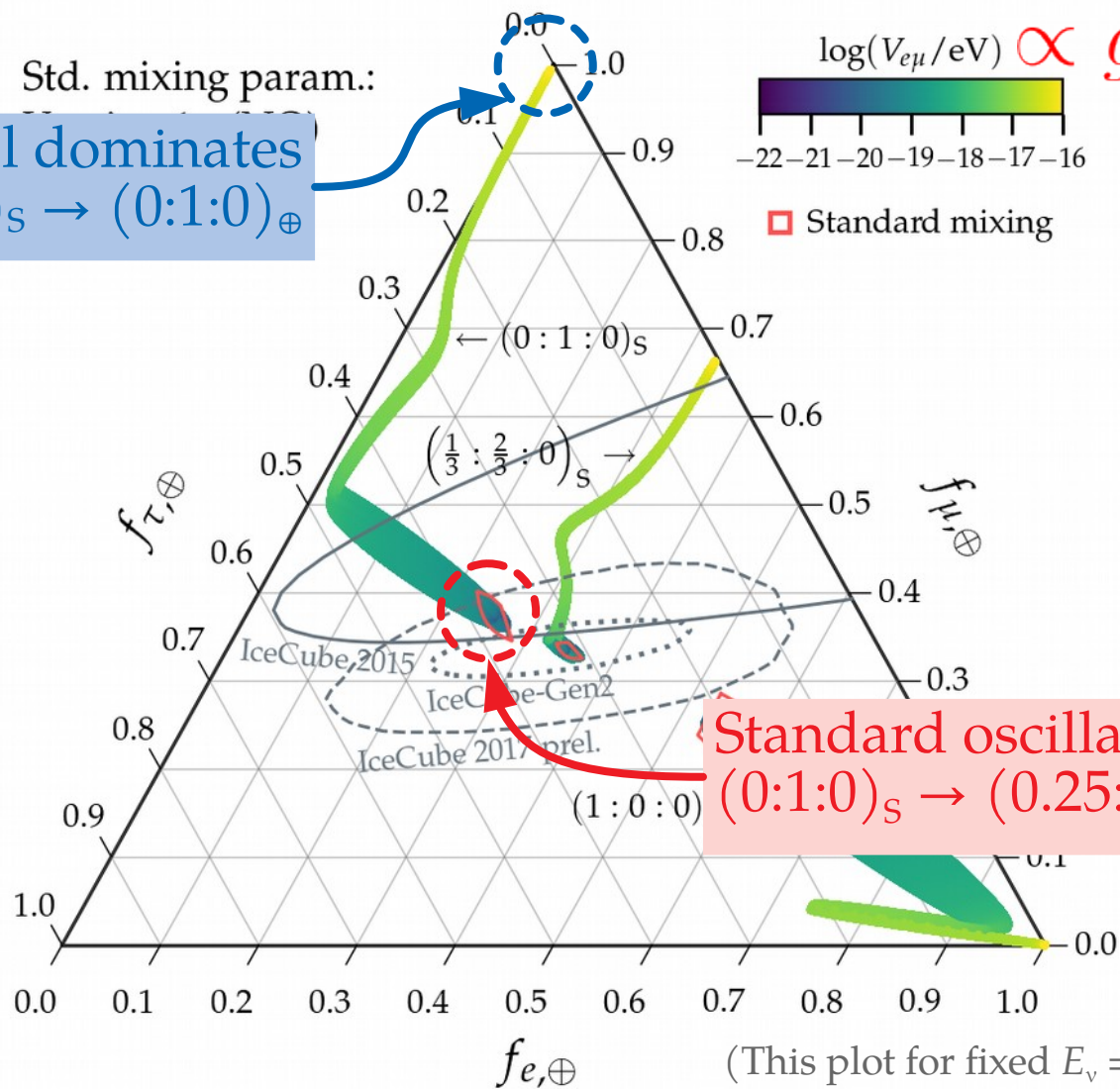
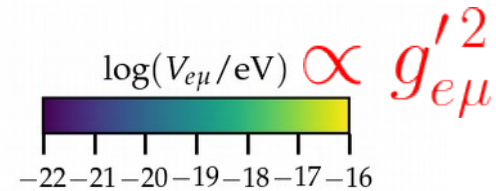






New potential dominates  
 $(0:1:0)_S \rightarrow (0:1:0)_\oplus$

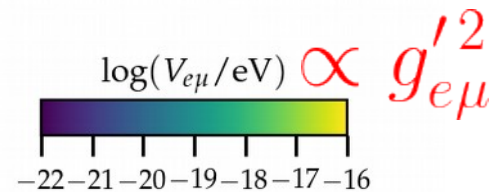
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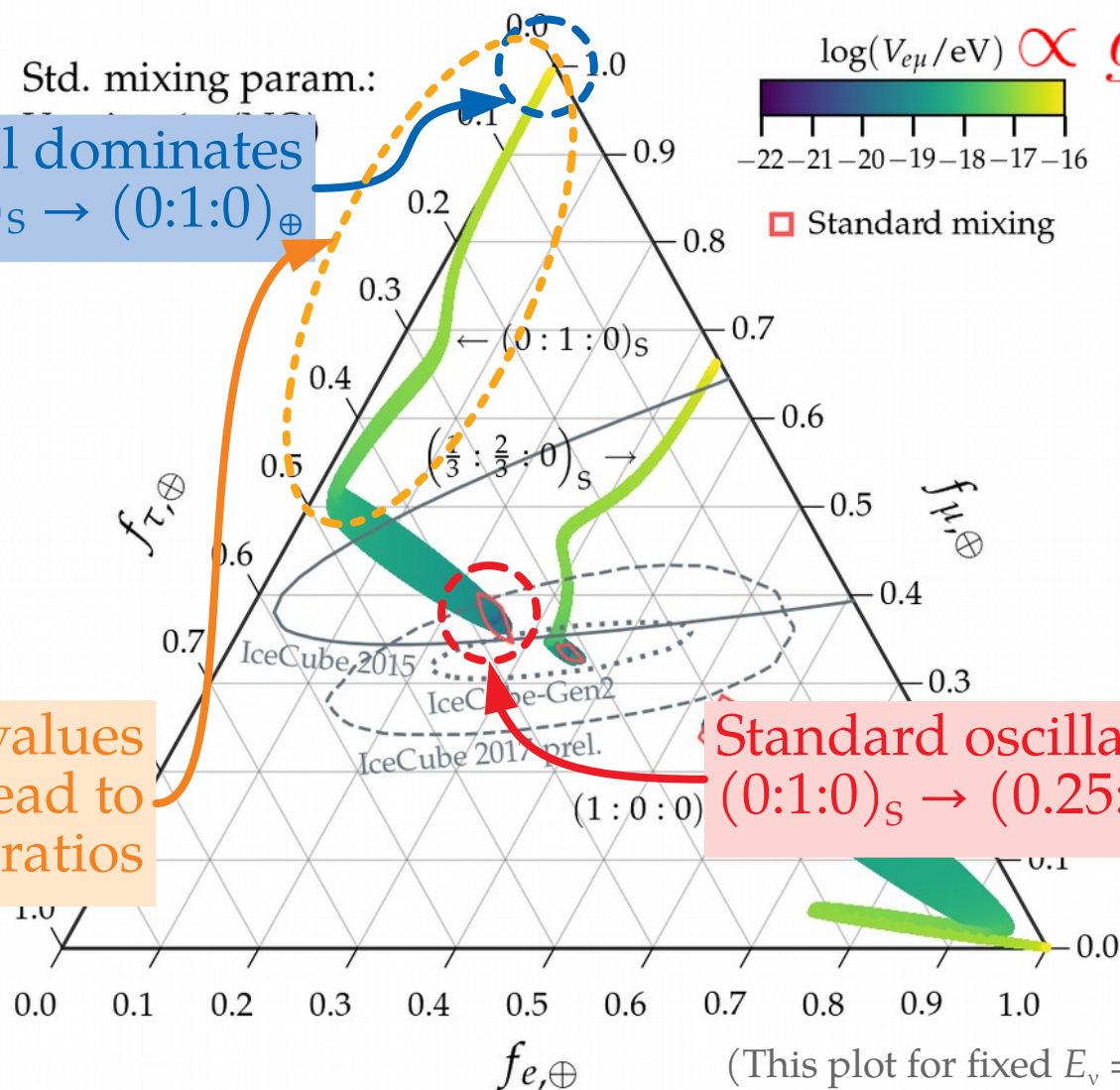
Std. mixing param.:

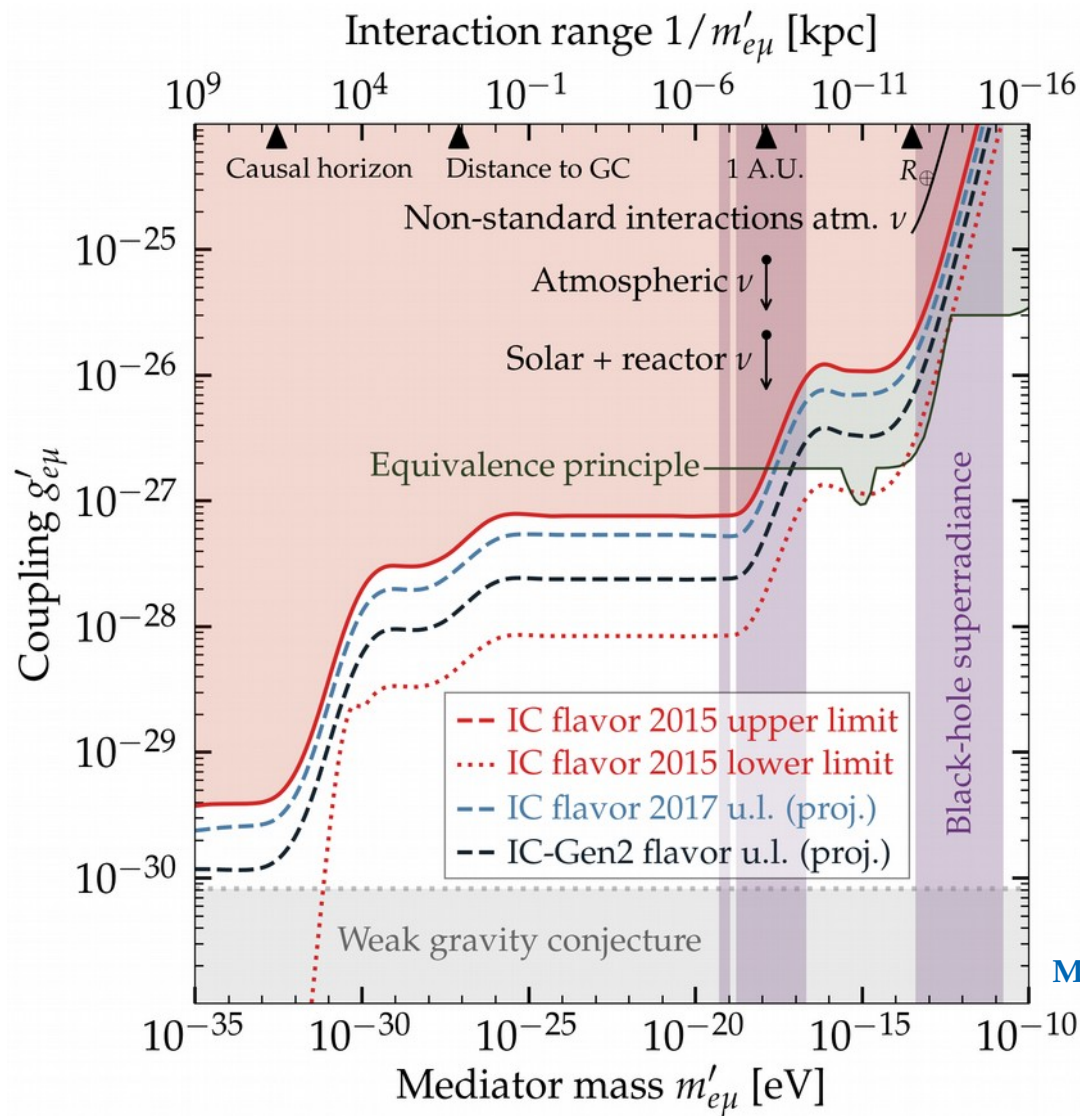


Standard mixing

We can disfavor all values  
of  $m'$  and  $g'$  that lead to  
these flavor ratios

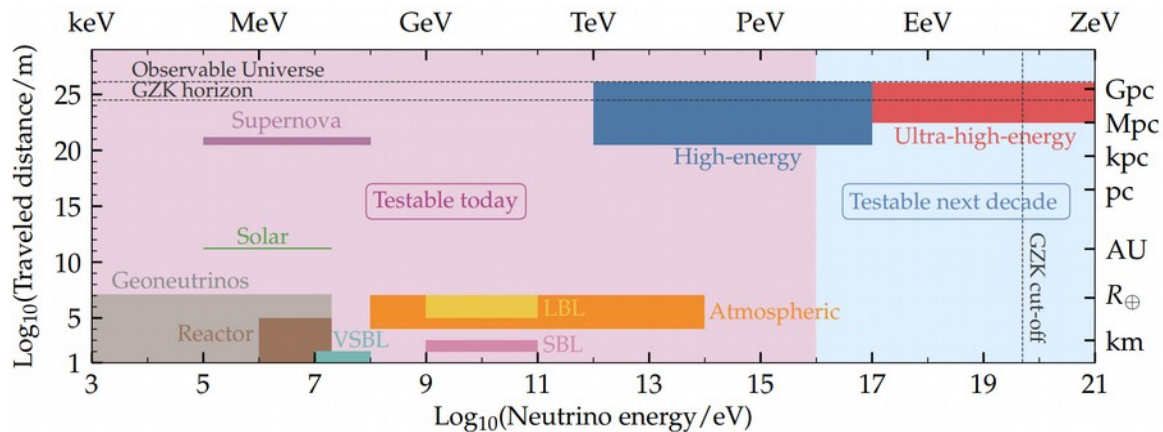
Standard oscillations  
 $(0:1:0)_s \rightarrow (0.25:0.37:0.38)_\oplus$





MB & Agarwalla, PRL 2019

# An exciting decade ahead



**Today: TeV–PeV astrophysical  $\nu$**

$$\kappa_n \sim 4 \cdot 10^{-47} (E/\text{PeV})^{-n} (L/\text{Gpc})^{-1} \text{PeV}^{1-n}$$

IceCube + ANTARES + Baikal

+ Growing statistics

+ Improved systematics

**Next decade: EeV cosmogenic  $\nu$**

$$\kappa_n \sim 4 \cdot 10^{-50} (E/\text{EeV})^{-n} (L/\text{Gpc})^{-1} \text{EeV}^{1-n}$$

IceCube upgrade

IceCube-Gen2

KM3NeT

ANITA

ARA

ARIANNA

Baikal-GVD

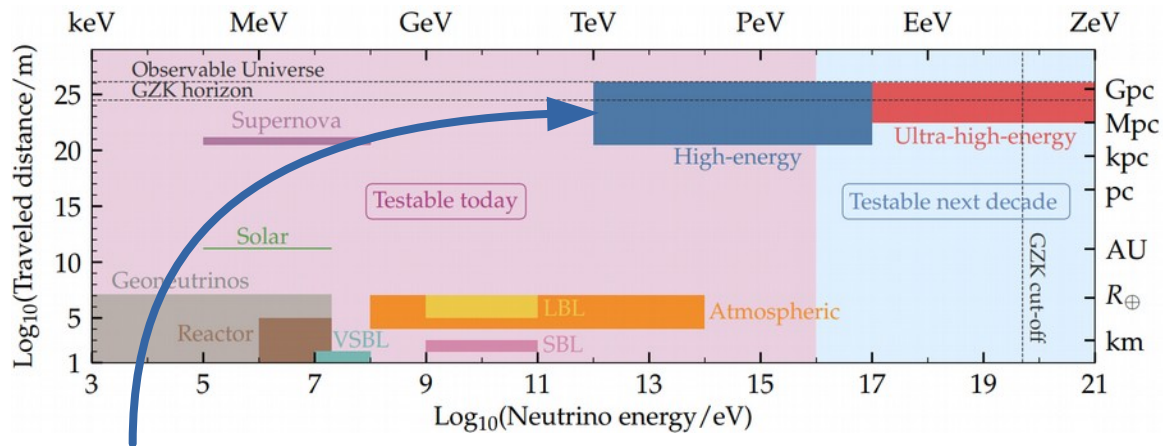
BEACON

GRAND

POEMMA

TRINITY

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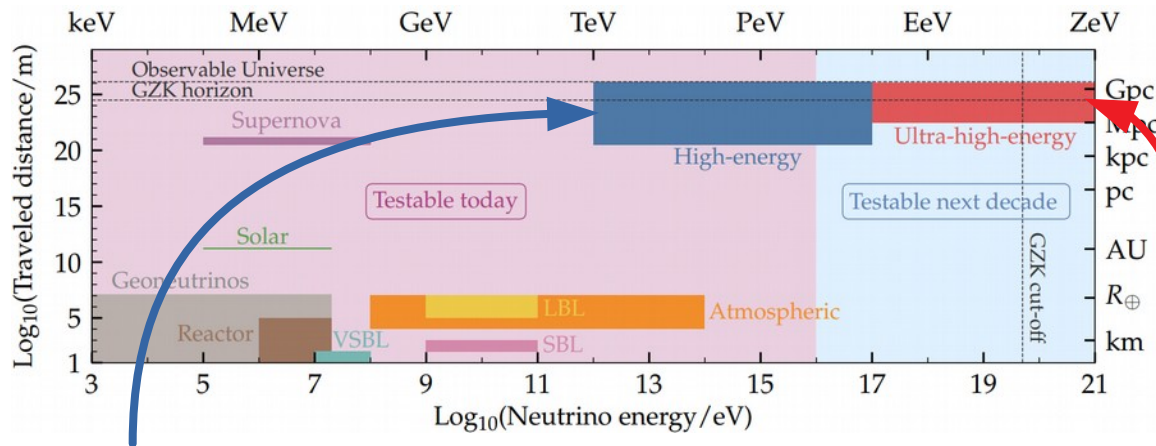
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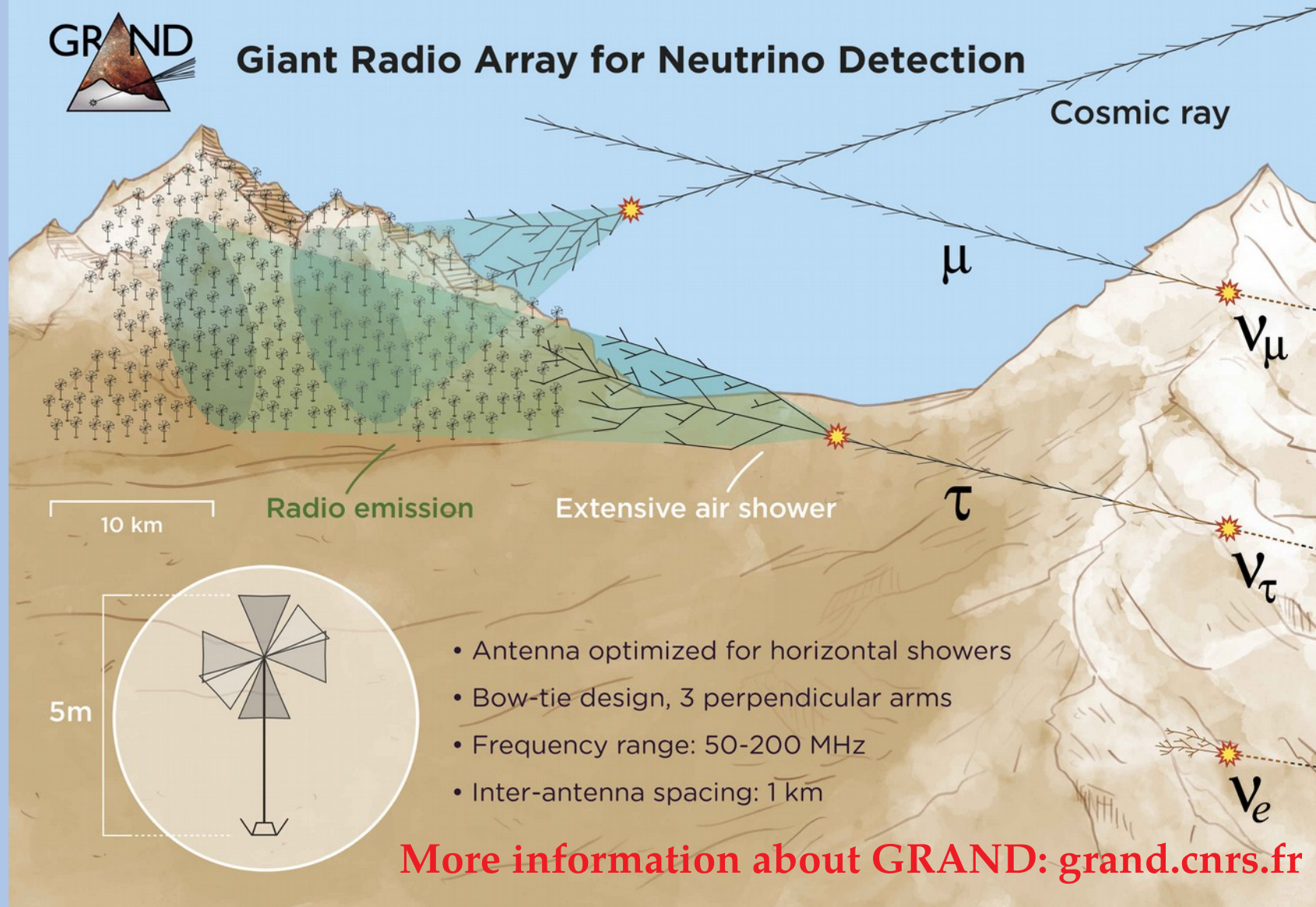
POEMMA

TRINITY





# Giant Radio Array for Neutrino Detection





# What are you taking home?

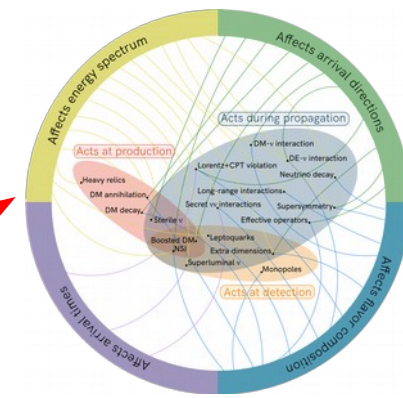
- ▶ Cosmic neutrinos are incisive probes of TeV–PeV physics
- ▶ We can do this *now*, in spite of astrophysical unknowns
- ▶ New physics comes in many shapes — so we need to be thorough
- ▶ Exciting prospects: larger statistics, better reconstruction, higher energies

## More?

- ▶ *Fundamental physics with high-energy cosmic neutrinos today and in the future*, [1907.08690](#)
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- ▶ *Astro2020: Astrophysics uniquely enabled by observations of high-energy cosmic neutrinos*, [1903.04334](#)

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Backup slides

# Flavor-transition probability: the quick and dirty of it

► In matrix form: 
$$\begin{pmatrix} \nu_e \\ \nu_\mu \\ \nu_\tau \end{pmatrix} = \begin{pmatrix} U_{e1}^* & U_{e2}^* & U_{e3}^* \\ U_{\mu 1}^* & U_{\mu 2}^* & U_{\mu 3}^* \\ U_{\tau 1}^* & U_{\tau 2}^* & U_{\tau 3}^* \end{pmatrix} \begin{pmatrix} \nu_1 \\ \nu_2 \\ \nu_3 \end{pmatrix}$$

► Pontecorvo-Maki-Nakagawa-Sakata matrix ( $c_{ij} = \cos \theta_{ij}$ ,  $s_{ij} = \sin \theta_{ij}$ ):

$$U = \underbrace{\begin{pmatrix} 1 & 0 & 0 \\ 0 & c_{23} & s_{23} \\ 0 & -s_{23} & c_{23} \end{pmatrix}}_{\text{Atmospheric}} \underbrace{\begin{pmatrix} c_{13} & 0 & s_{13}e^{-i\delta} \\ 0 & 1 & 0 \\ -s_{13}e^{i\delta} & 0 & c_{13} \end{pmatrix}}_{\text{Cross mixing}} \underbrace{\begin{pmatrix} c_{12} & s_{12} & 0 \\ -s_{12} & c_{12} & 0 \\ 0 & 0 & 1 \end{pmatrix}}_{\text{Solar}} \underbrace{\begin{pmatrix} e^{i\alpha_1/2} & 0 & 0 \\ 0 & e^{i\alpha_2/2} & 0 \\ 0 & 0 & 1 \end{pmatrix}}_{\text{Majorana CP phases}}$$

► Probability for  $\nu_\alpha \rightarrow \nu_\beta$ : 
$$P_{\nu_\alpha \rightarrow \nu_\beta} = \delta_{\alpha\beta} - 4 \sum_{i>j} \text{Re}(U_{\alpha i}^* U_{\beta i} U_{\alpha j} U_{\beta j}^*) \sin^2 \left( \Delta m_{ij}^2 \frac{L}{4E} \right) + 2 \sum_{i>j} \text{Im}(U_{\alpha i}^* U_{\beta i} U_{\alpha j} U_{\beta j}^*) \sin \left( \Delta m_{ij}^2 \frac{L}{2E} \right)$$

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$\theta_{23} \approx 48^\circ$   
 $\theta_{13} \approx 9^\circ$   
 $\theta_{12} \approx 34^\circ$   
 $\delta \approx 222^\circ$

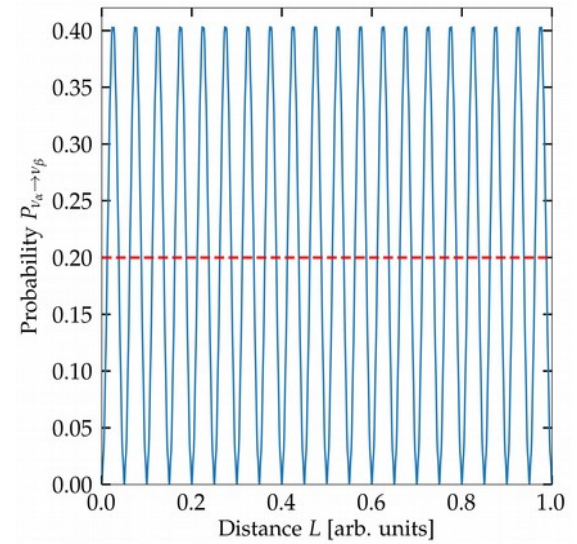
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Oscillation length for 1-TeV  $\nu$ :  $2\pi \times 2E/\Delta m^2 \sim 0.1$  pc

$\sim 8\%$  of the way to Proxima Centauri  
 $\ll$  Distance to Galactic Center (8 kpc)  
 $\ll$  Distance to Andromeda (1 Mpc)  
 $\ll$  Cosmological distances (few Gpc)

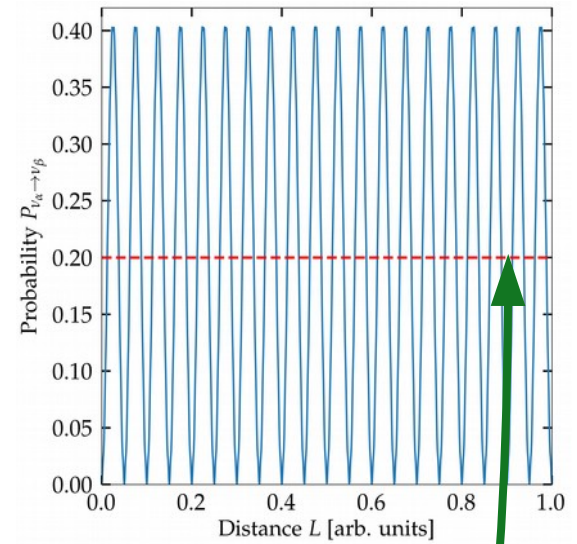
We cannot resolve oscillations, so we use instead the average probability:

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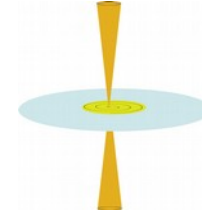
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# Inferring the flavor composition at the sources

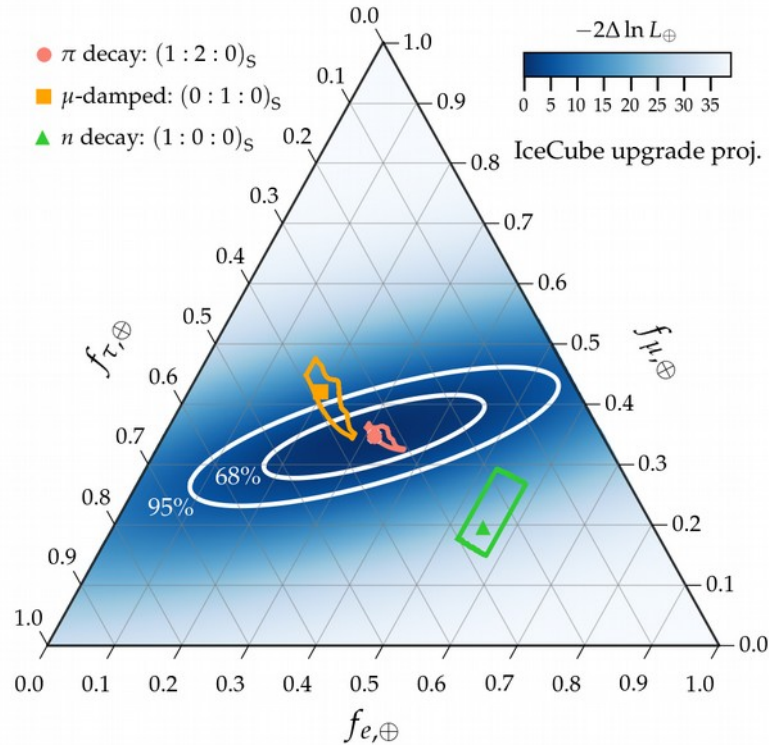
**Measured:**  
Flavor ratios at Earth



Invert flavor oscillations



**Inferred:**  
Flavor ratios at  
astrophysical sources

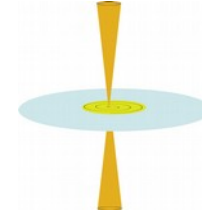


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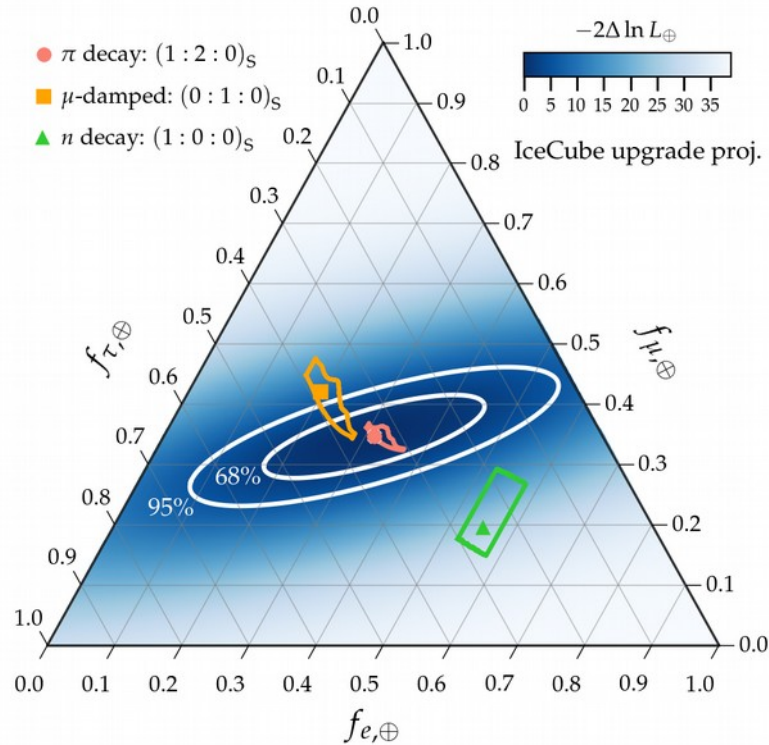
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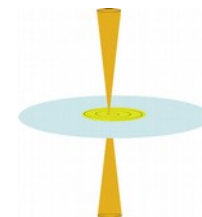


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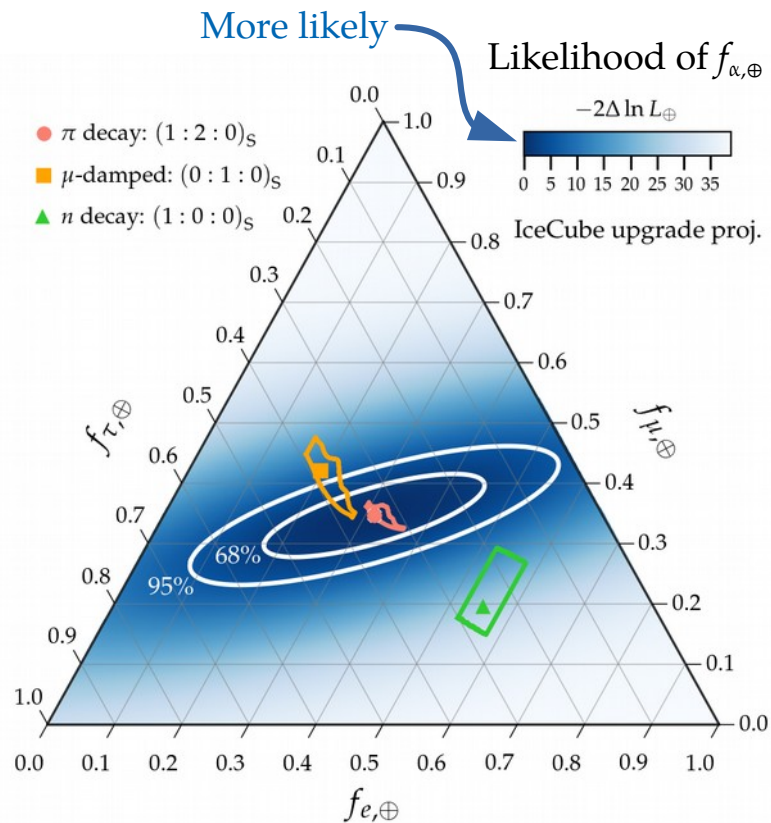
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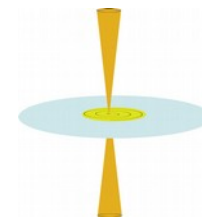


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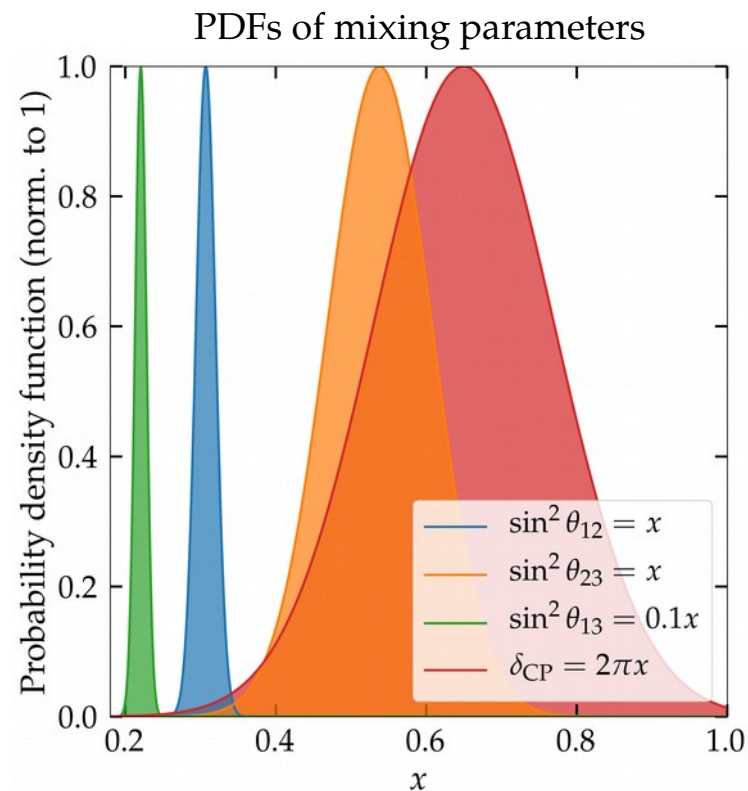
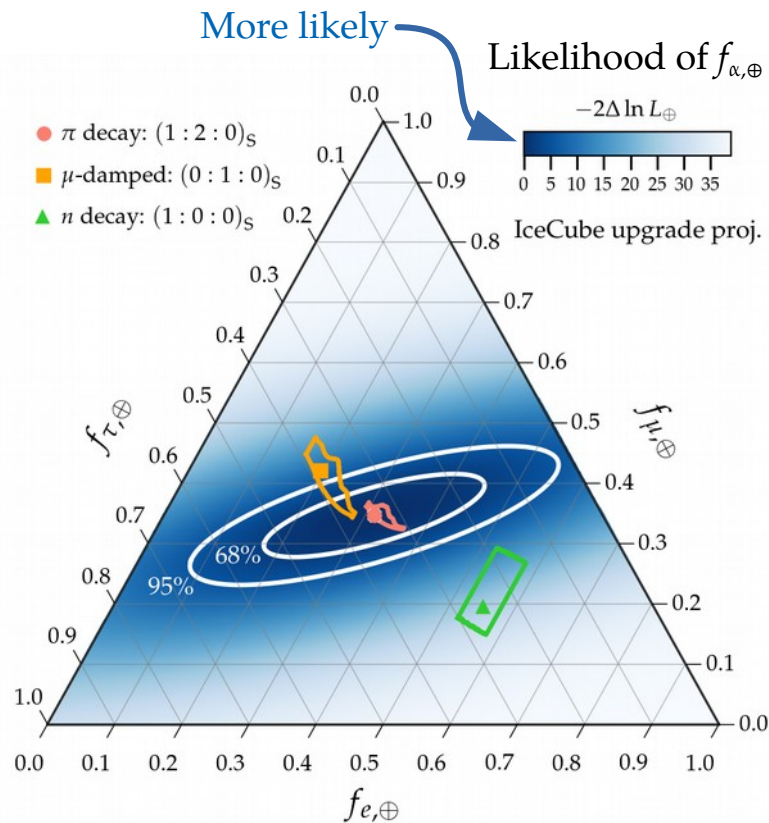
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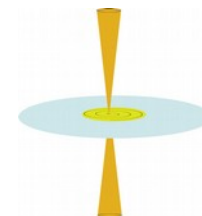


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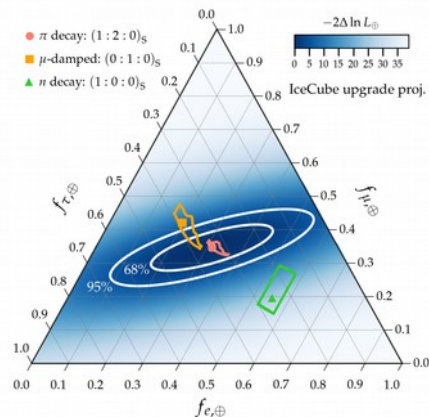
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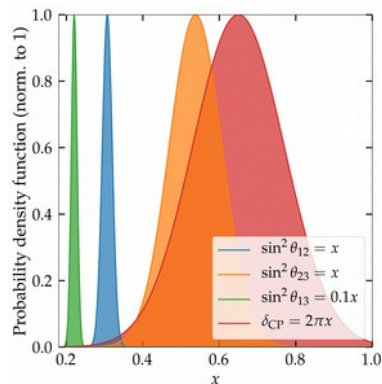
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Posterior probability density of  $f_{\alpha,S}$  being the flavor ratios at the sources:

$$\mathcal{P}(f_{\alpha,S}) \equiv \int d\theta \frac{\mathcal{P}(\theta)}{\mathcal{N}(\theta)} \mathcal{L}_{\oplus} [f_{e,\oplus}(f_{\alpha,S}, \theta), f_{\mu,\oplus}(f_{\alpha,S}, \theta)]$$

$$\theta \equiv (\theta_{12}, \theta_{23}, \theta_{13}, \delta_{CP})$$



$$\left[ \text{Normalization: } \mathcal{N}(\theta) \equiv \int_0^1 df_{e,S} \int_0^{1-f_{e,S}} df_{\mu,S} \mathcal{L}_{\oplus} [f_{e,\oplus}(f_{\alpha,S}, \theta), f_{\mu,\oplus}(f_{\alpha,S}, \theta)] \right]$$

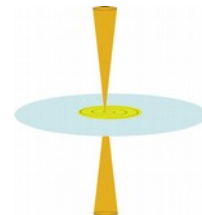


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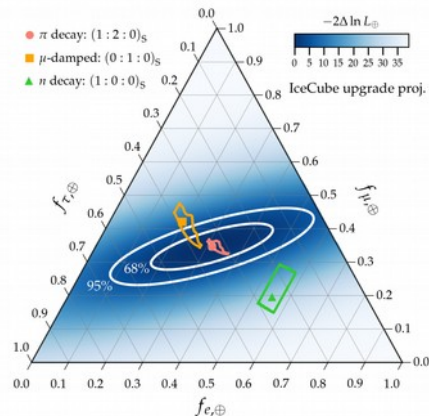
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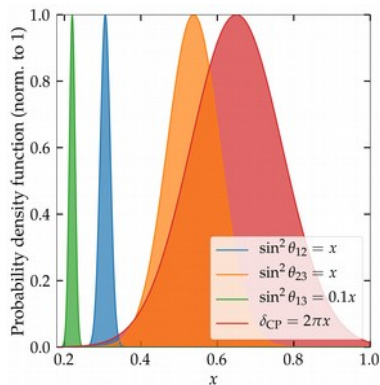
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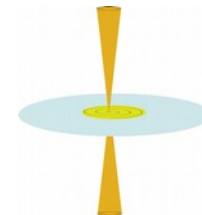
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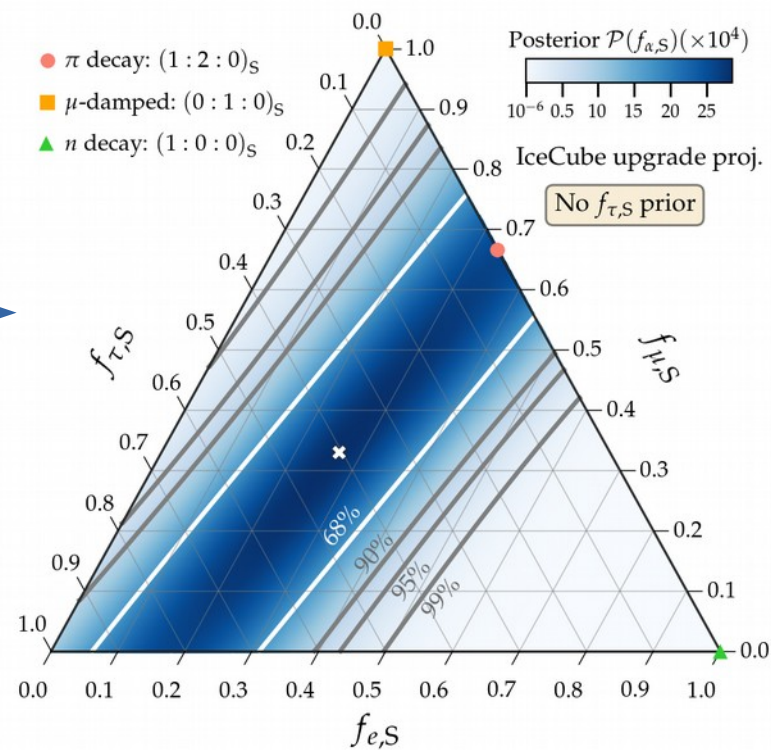
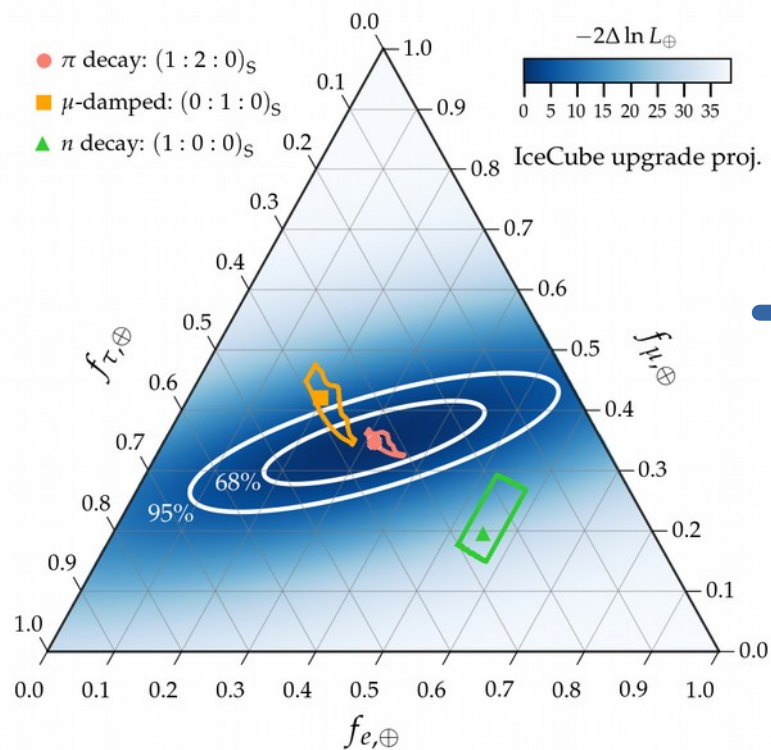
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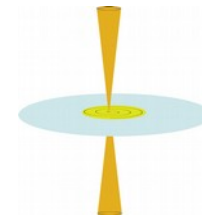


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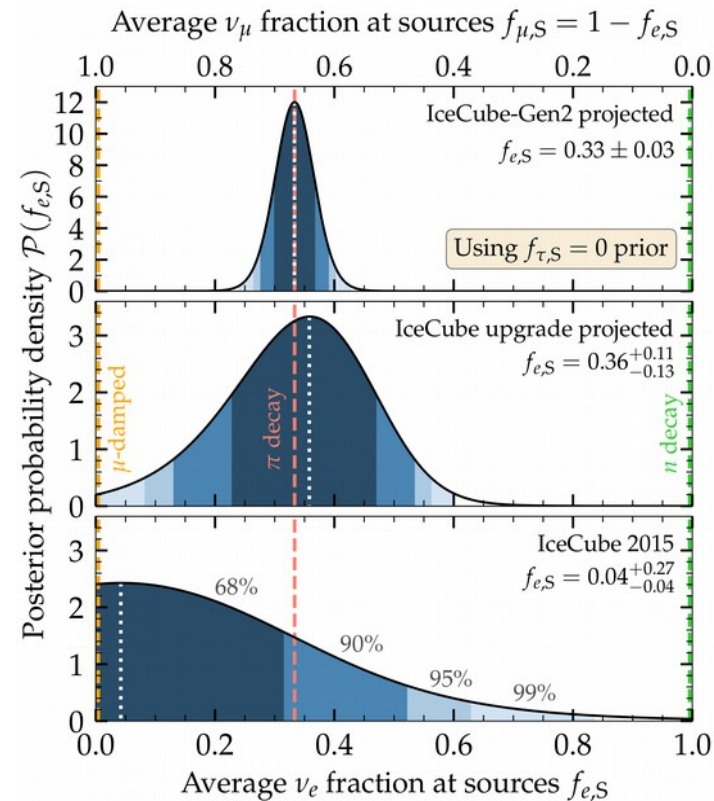
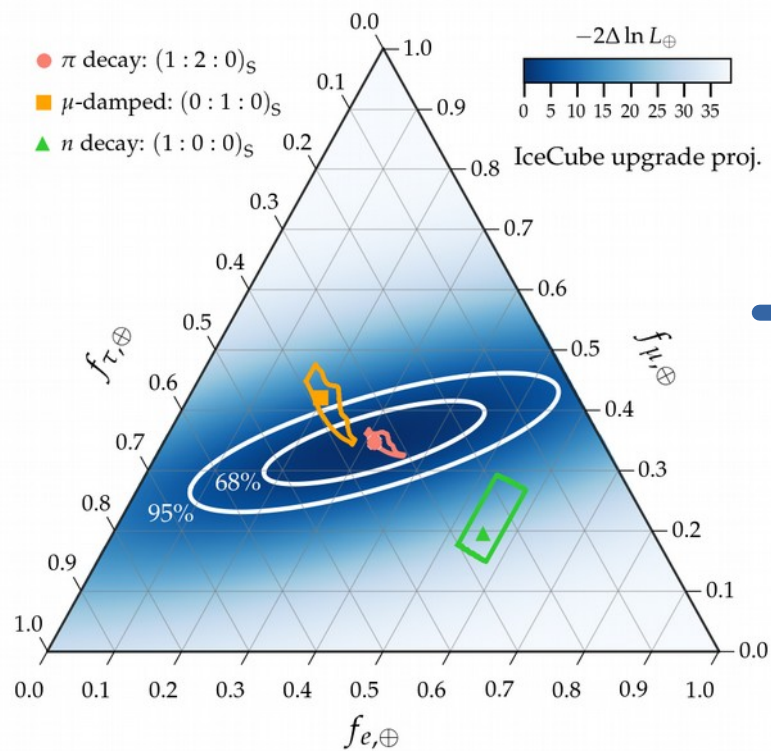
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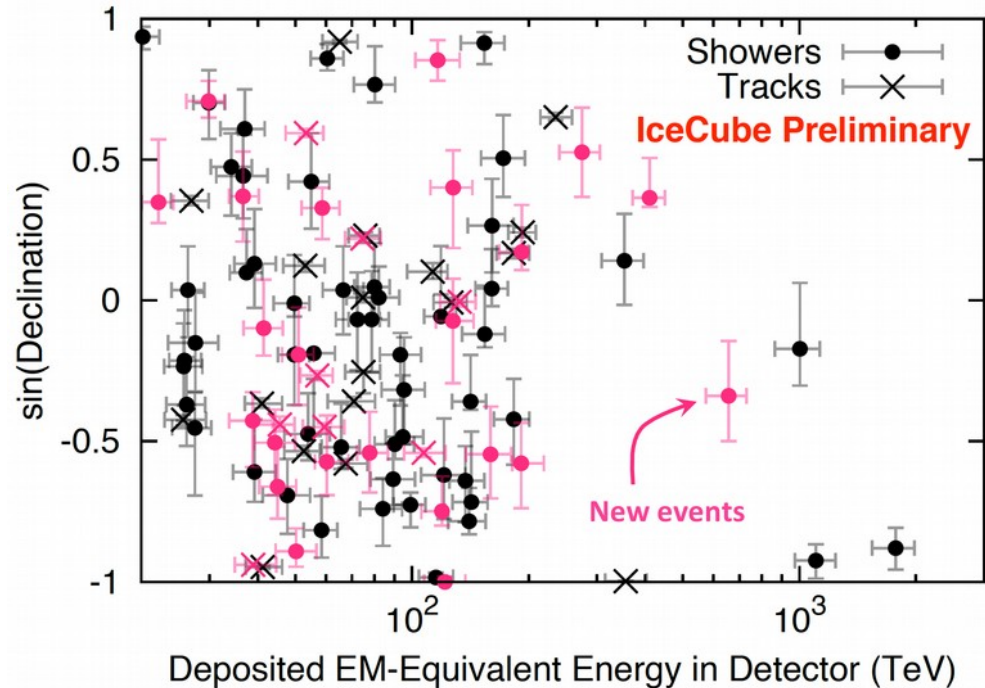


What has IceCube found so far (7.5 years)?

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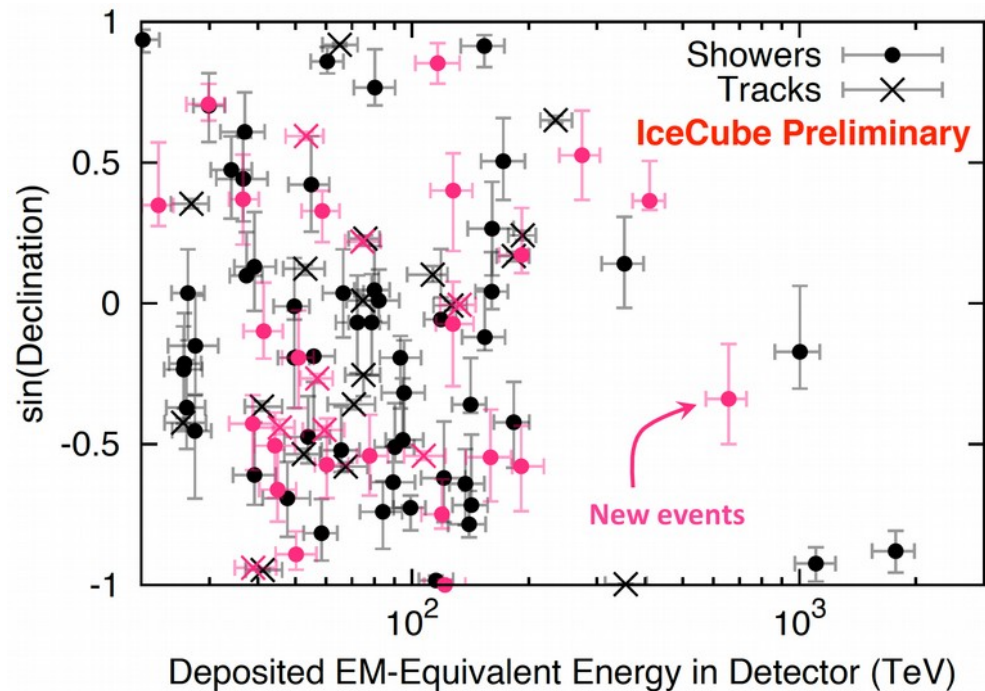
103 contained events between 15 TeV – 2 PeV



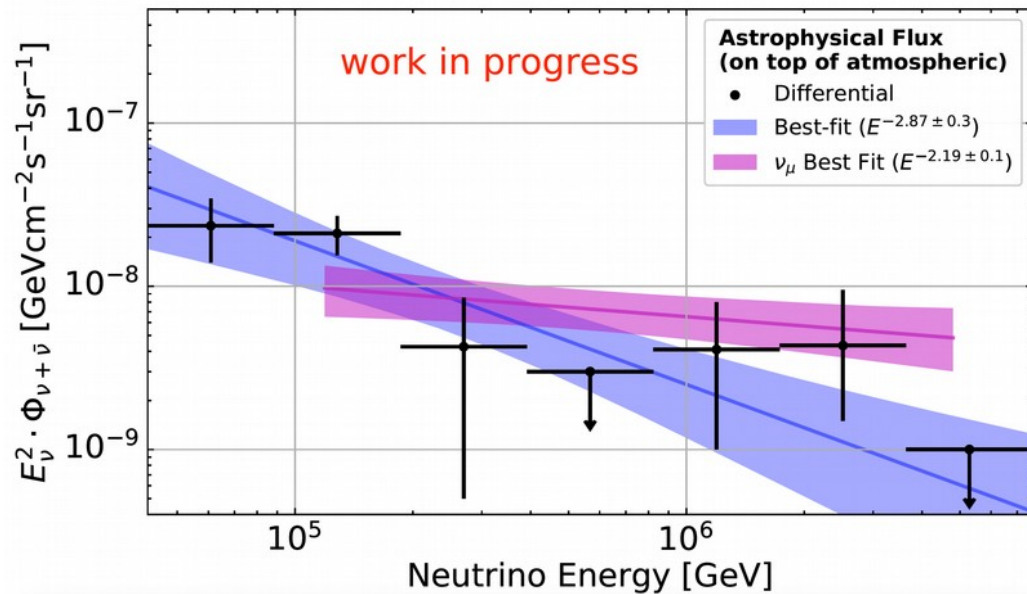


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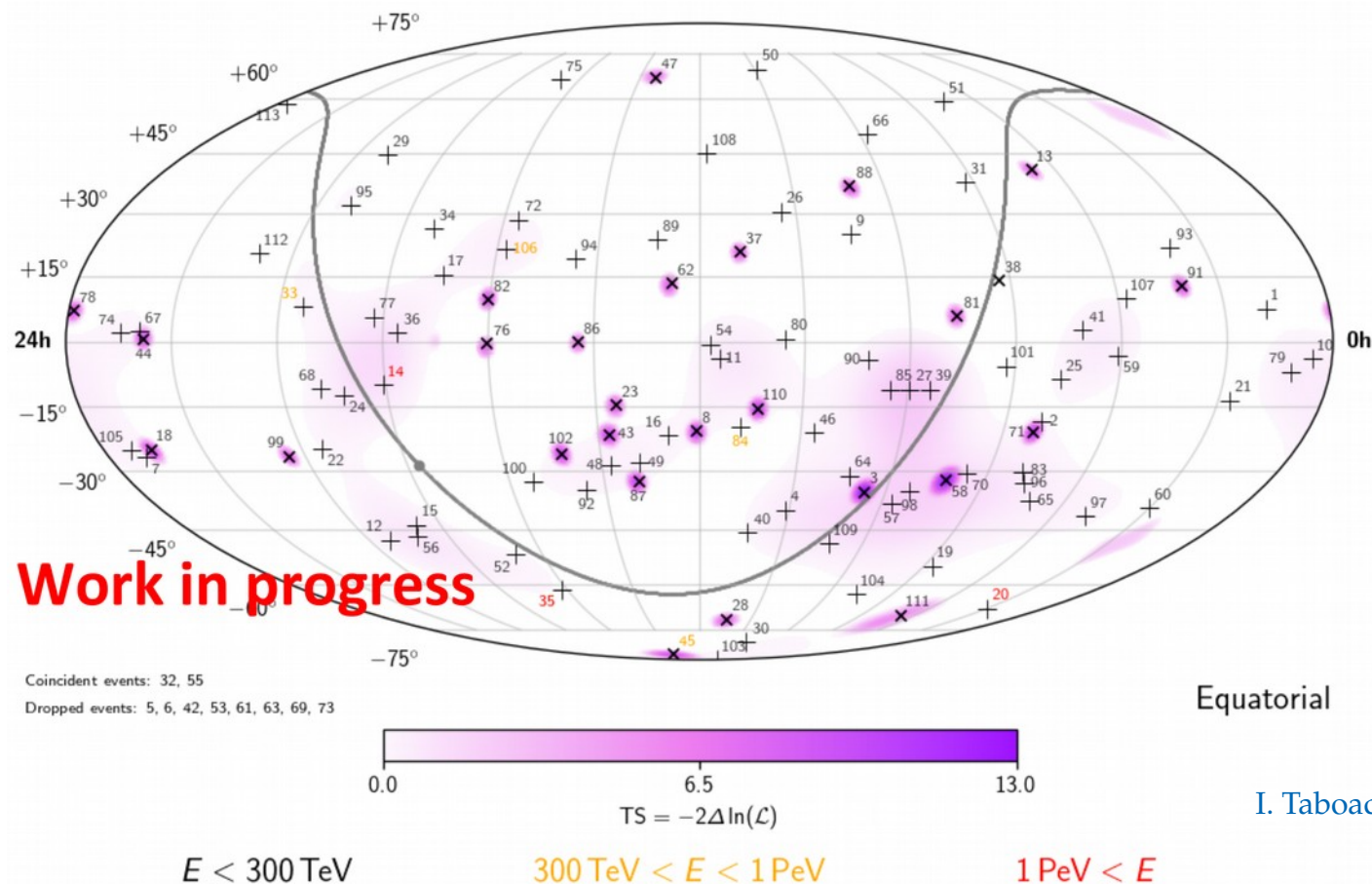


Astrophysical  $\nu$  flux detected at  $> 7\sigma$   
(Normalization ok, but steep spectrum)



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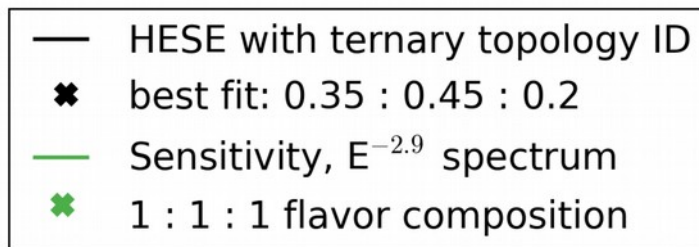
Arrival directions compatible with isotropy



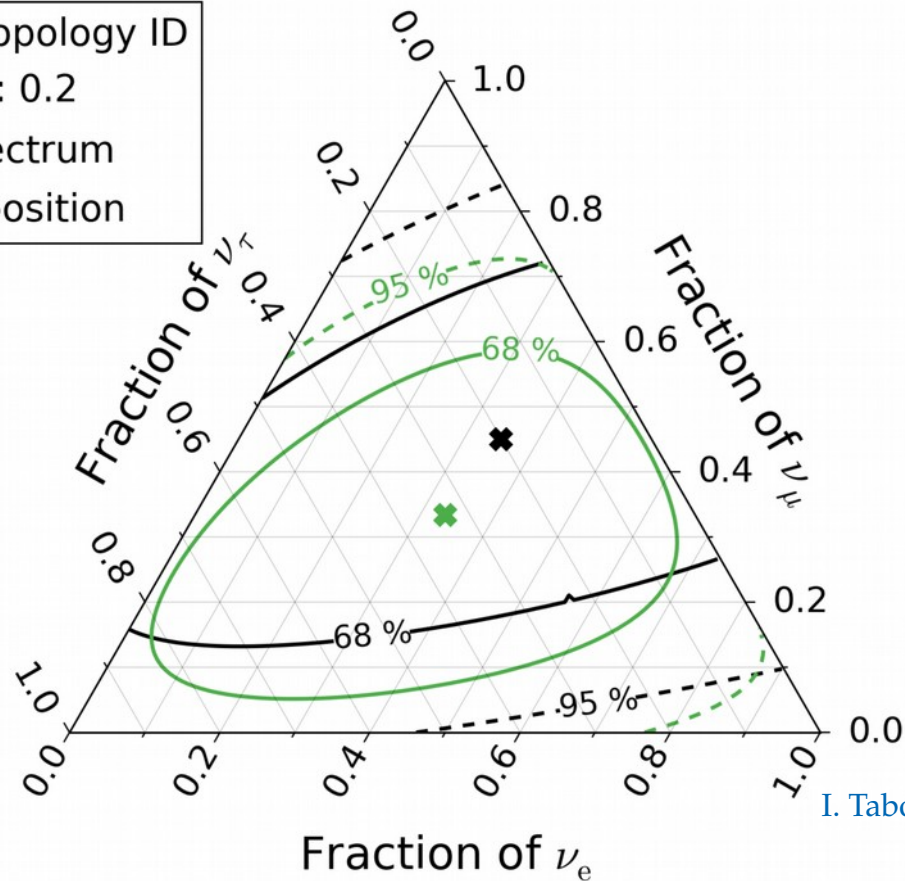
I. Taboada, Neutrino 2018

# What has IceCube found so far (7.5 years)?

Flavor composition compatible with equal proportion of each flavor



WORK IN PROGRESS



# Bonus: Measuring the inelasticity $\langle y \rangle$

- ▶ Inelasticity in CC  $\nu_\mu$  interaction  $\nu_\mu + N \rightarrow \mu + X$ :

$$E_X = y E_\nu \quad \text{and} \quad E_\mu = (1-y) E_\nu \Rightarrow y = (1 + E_\mu/E_X)^{-1}$$

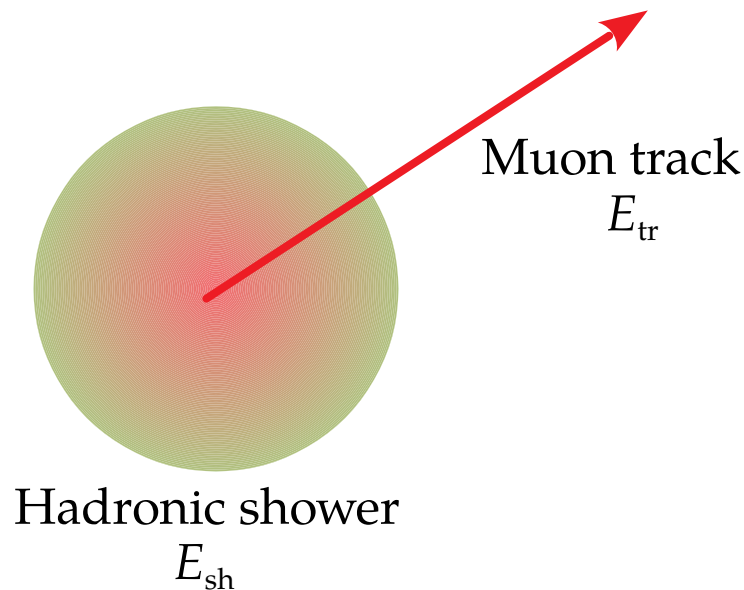
- ▶ The value of  $y$  follows a distribution  $d\sigma/dy$

- ▶ In a HESE starting track:

$$\left. \begin{array}{l} E_X = E_{\text{sh}} \text{ (energy of shower)} \\ E_\mu = E_{\text{tr}} \text{ (energy of track)} \end{array} \right\} y = (1 + E_{\text{tr}}/E_{\text{sh}})^{-1}$$

- ▶ New IceCube analysis:

- ▶ 5 years of starting-track data (2650 tracks)
- ▶ Machine learning separates shower from track
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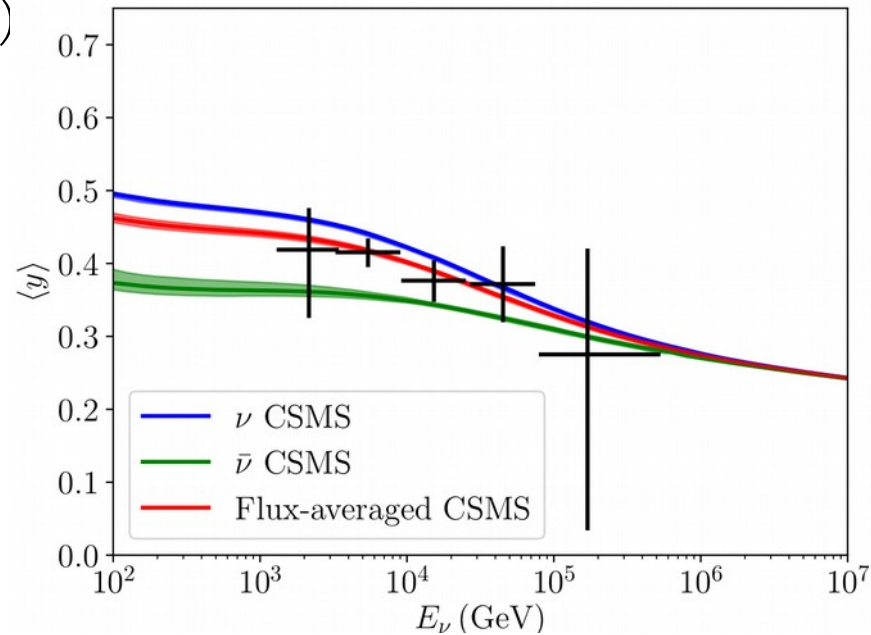
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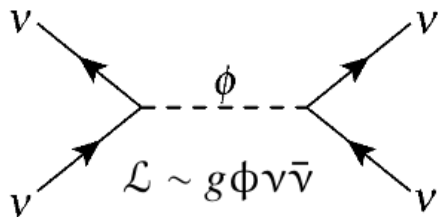
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- ▶ Different  $y$  distributions for  $\nu$  and  $\bar{\nu}$



IceCube, PRD 2019

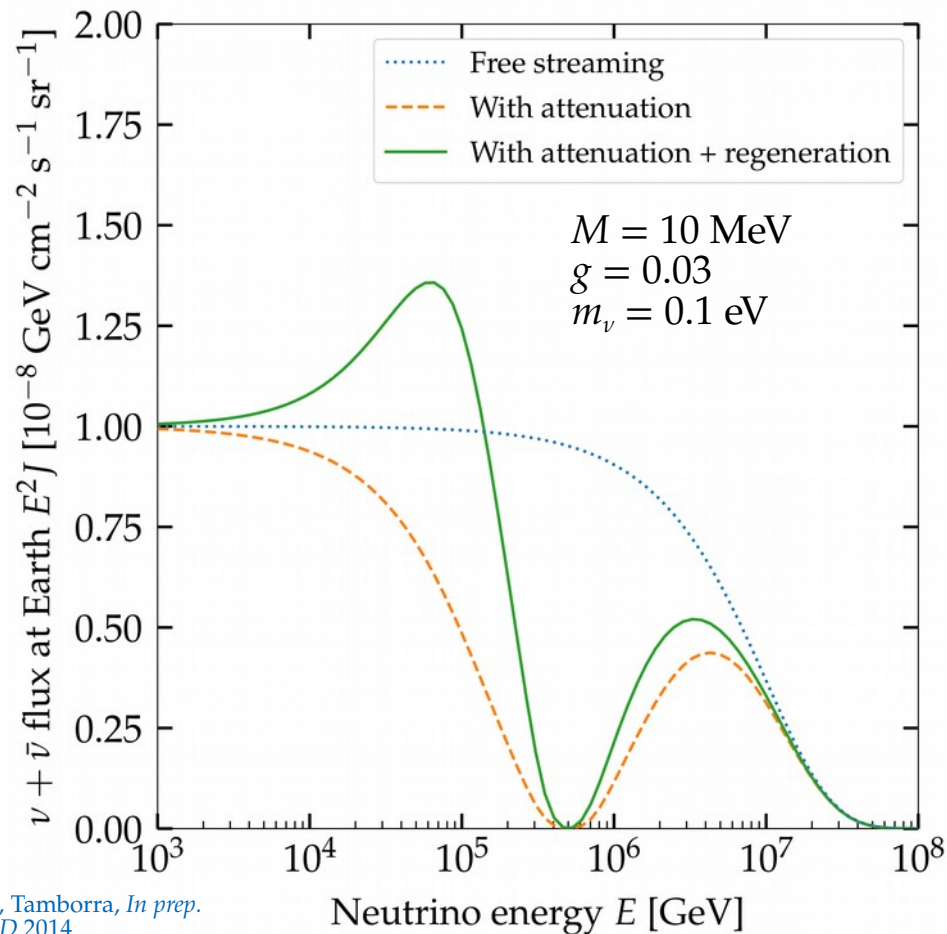
# New physics in the spectral shape: $\nu\nu$ interactions

“Secret” neutrino interactions between astrophysical  $\nu$  (PeV) and relic  $\nu$  (0.1 meV):



Cross section: 
$$\sigma = \frac{g^4}{4\pi} \frac{s}{(s - M^2)^2 + M^2\Gamma^2}$$

Resonance energy: 
$$E_{\text{res}} = \frac{M^2}{2m_\nu}$$

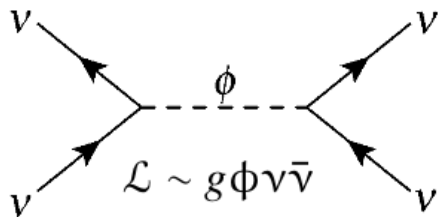


MB, Rosenstroem, Tamborra, *In prep.*  
Ng & Beacom, *PRD* 2014  
Cherry, Friedland, Shoemaker, 1411.1071  
Blum, Hook, Murase, 1408.3799



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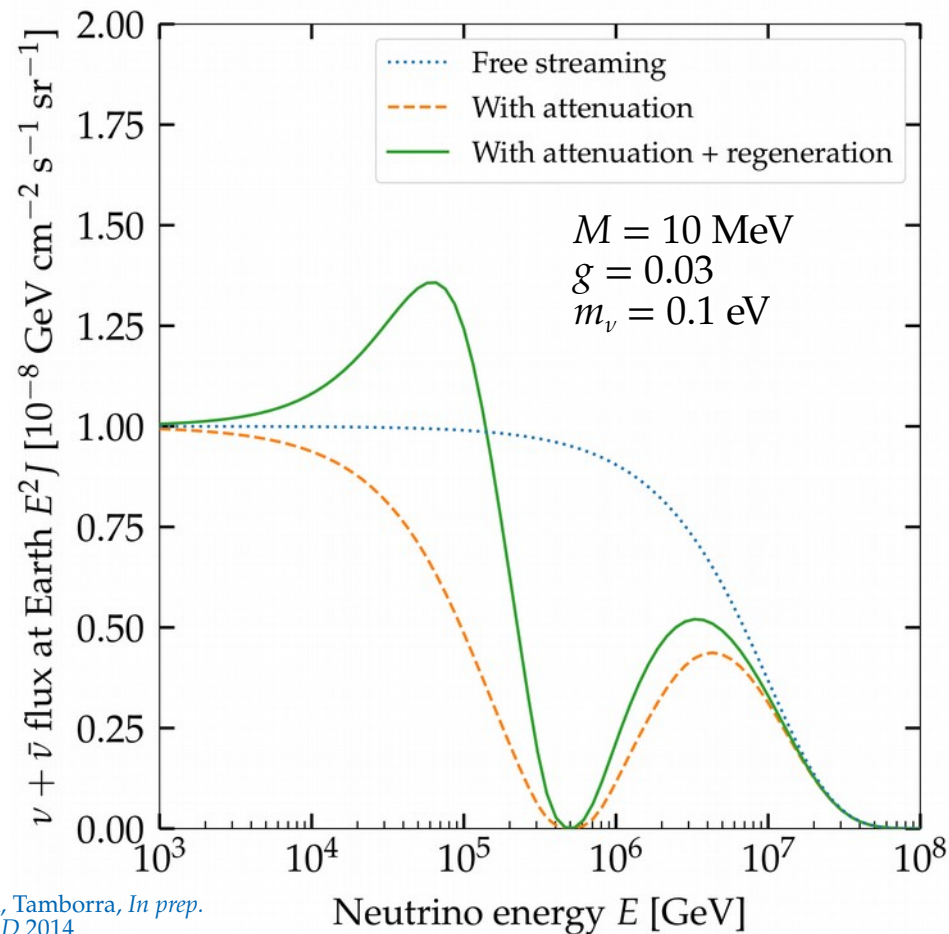
$$\sigma = \frac{g^4 s}{4\pi (s - M^2)^2 + M^2\Gamma^2}$$

New coupling

Mediator mass

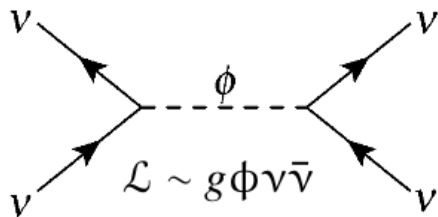
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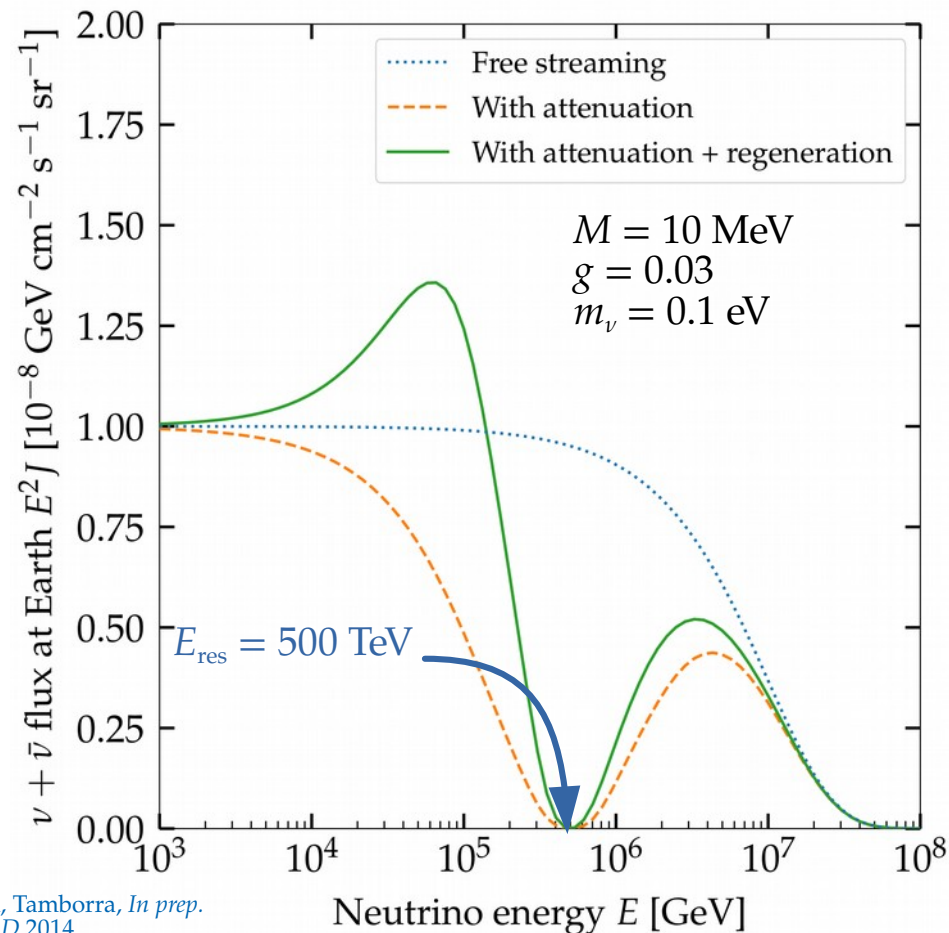
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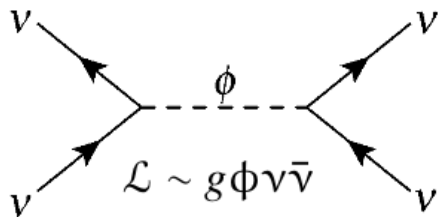
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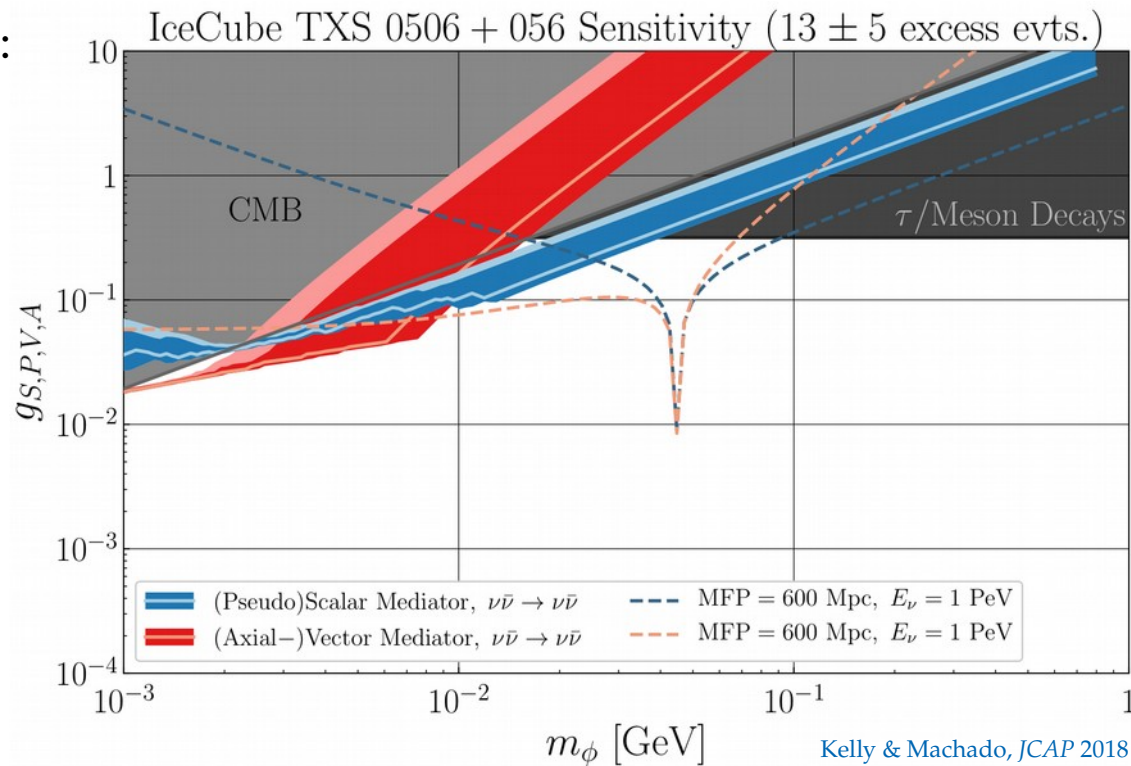
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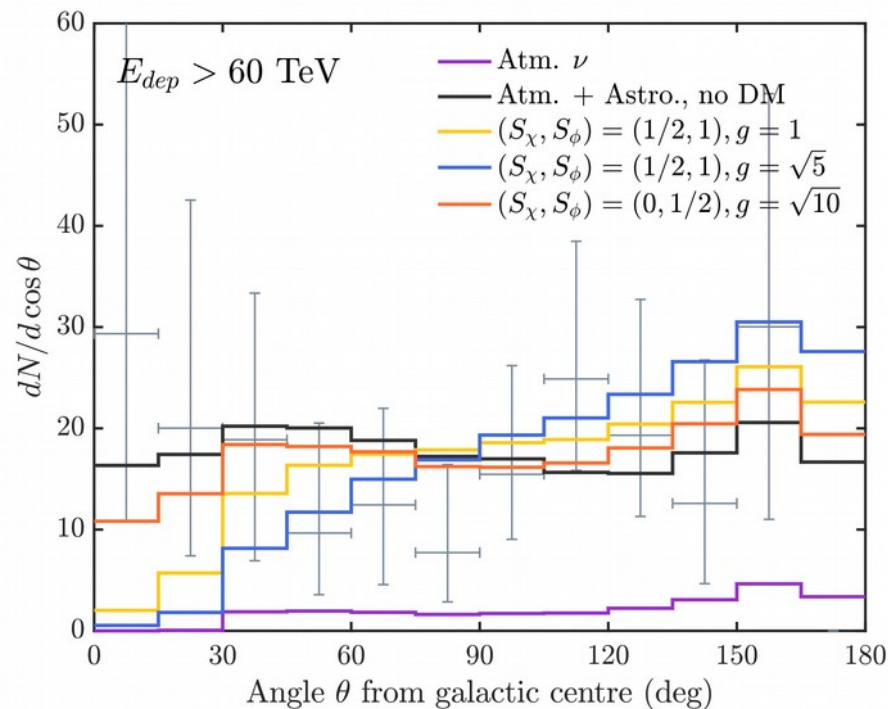
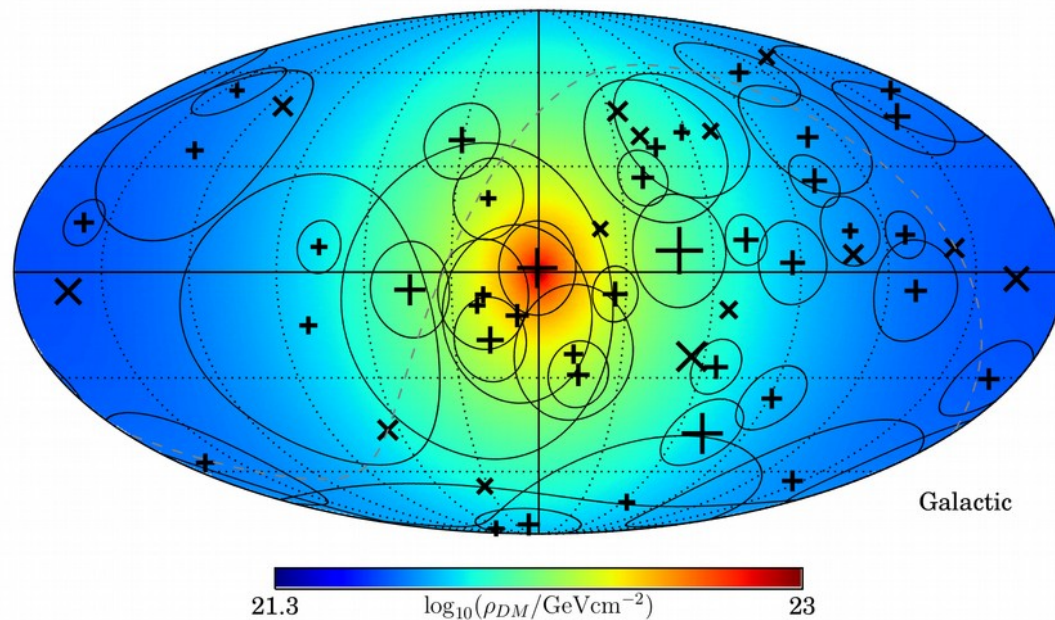
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$$\sigma = \frac{g^4}{4\pi} \frac{s}{(s - M^2)^2 + M^2\Gamma^2}$$

Resonance energy: 
$$E_{\text{res}} = \frac{M^2}{2m_\nu}$$



# New physics in the angular distribution: $\nu$ -DM interactions

Interaction between astrophysical neutrinos and the Galactic dark matter profile —



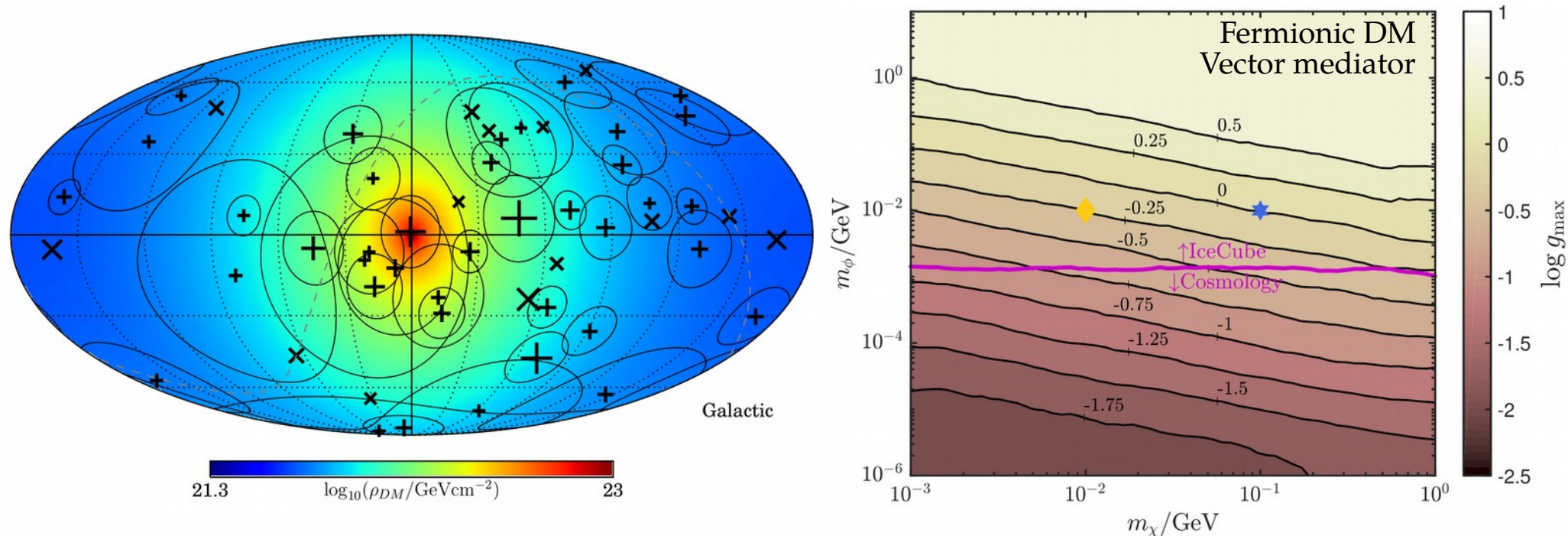
**Expected:** Fewer neutrinos coming from the Galactic Center

**Observed:** Isotropy



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Interaction between astrophysical neutrinos and the Galactic dark matter profile —

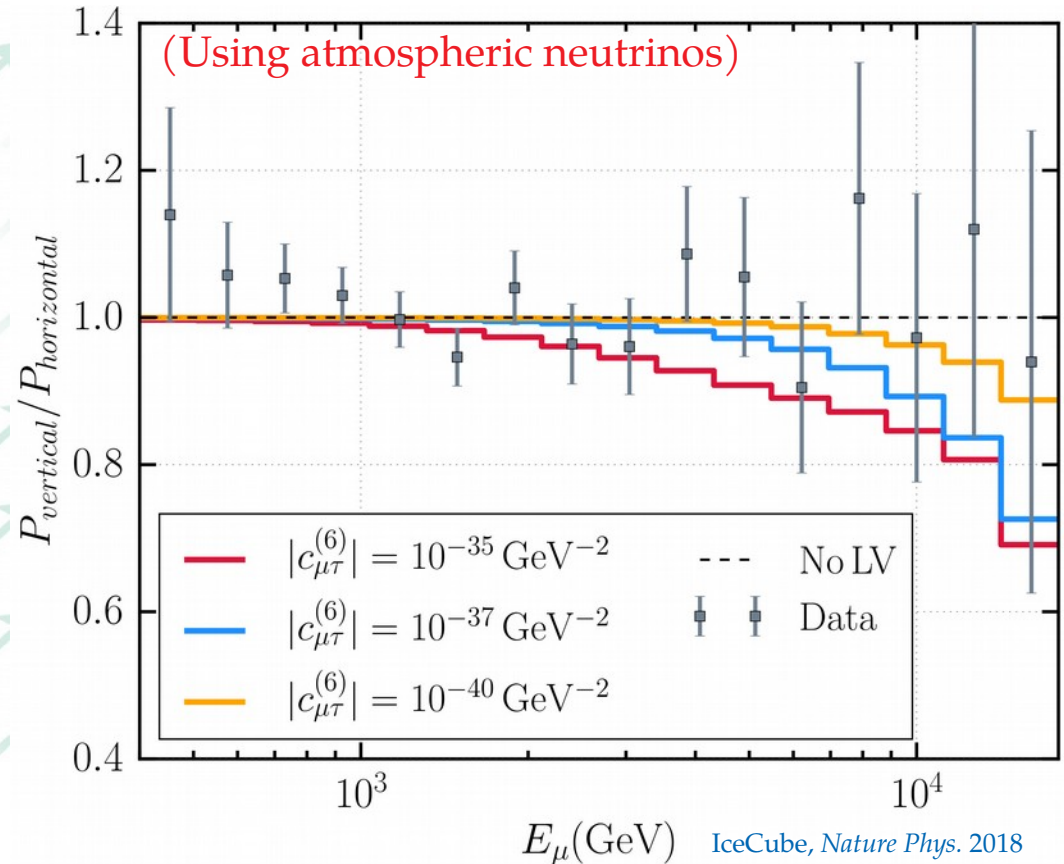
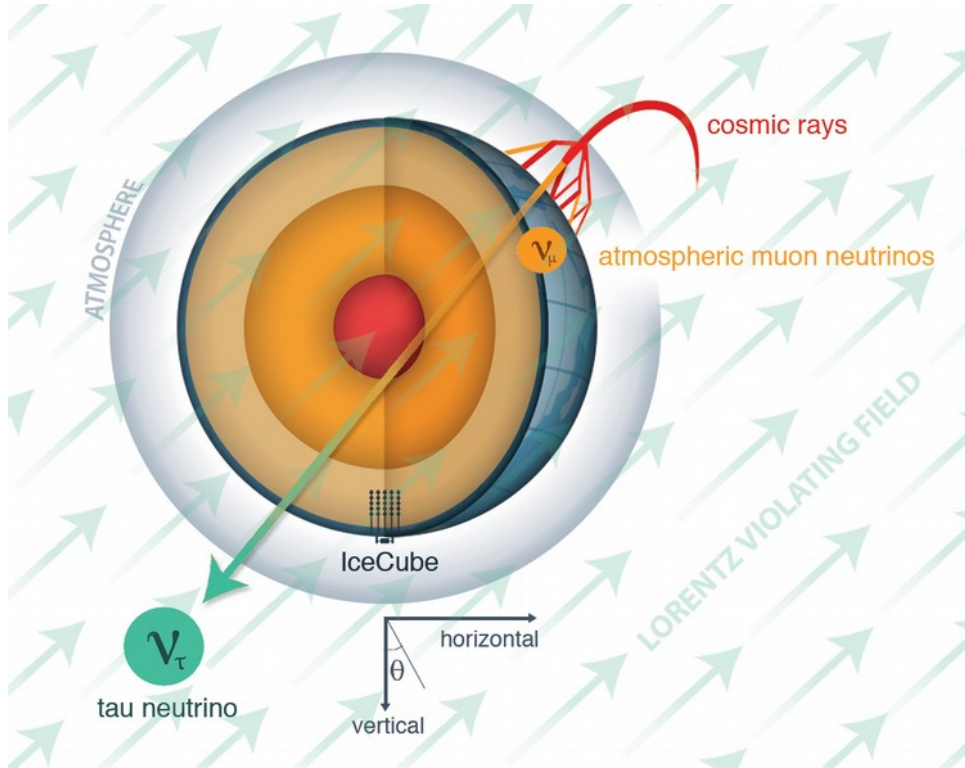


**Expected:** Fewer neutrinos coming from the Galactic Center

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# New physics in the energy & angular distribution

Lorentz invariance violation – Hamiltonian:  $H \sim m^2/(2E) + \hat{a}^{(3)} - E \cdot \hat{c}^{(4)} + E^2 \cdot \hat{a}^{(5)} - E^3 \cdot \hat{c}^{(6)}$



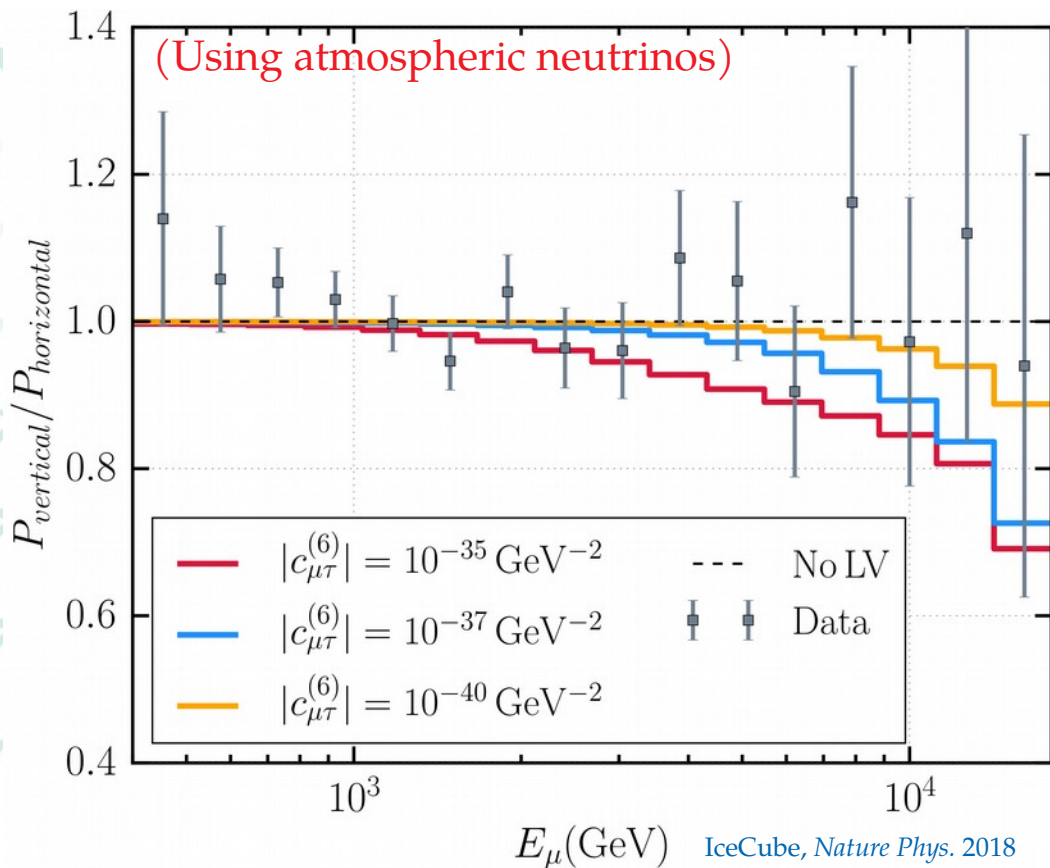
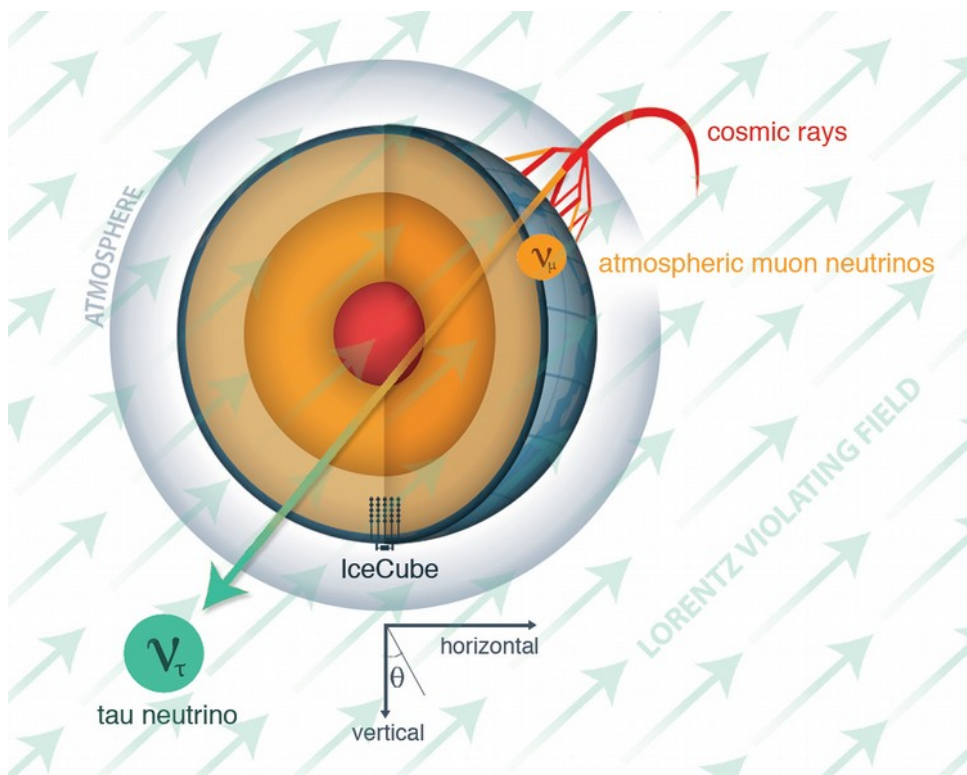


# New physics in the energy & angular distribution

Lorentz violation

Standard oscillations

Lorentz invariance violation – Hamiltonian:  $H \sim m^2/(2E) + \hat{a}^{(3)} - E \cdot \hat{c}^{(4)} + E^2 \cdot \hat{a}^{(5)} - E^3 \cdot \hat{c}^{(6)}$



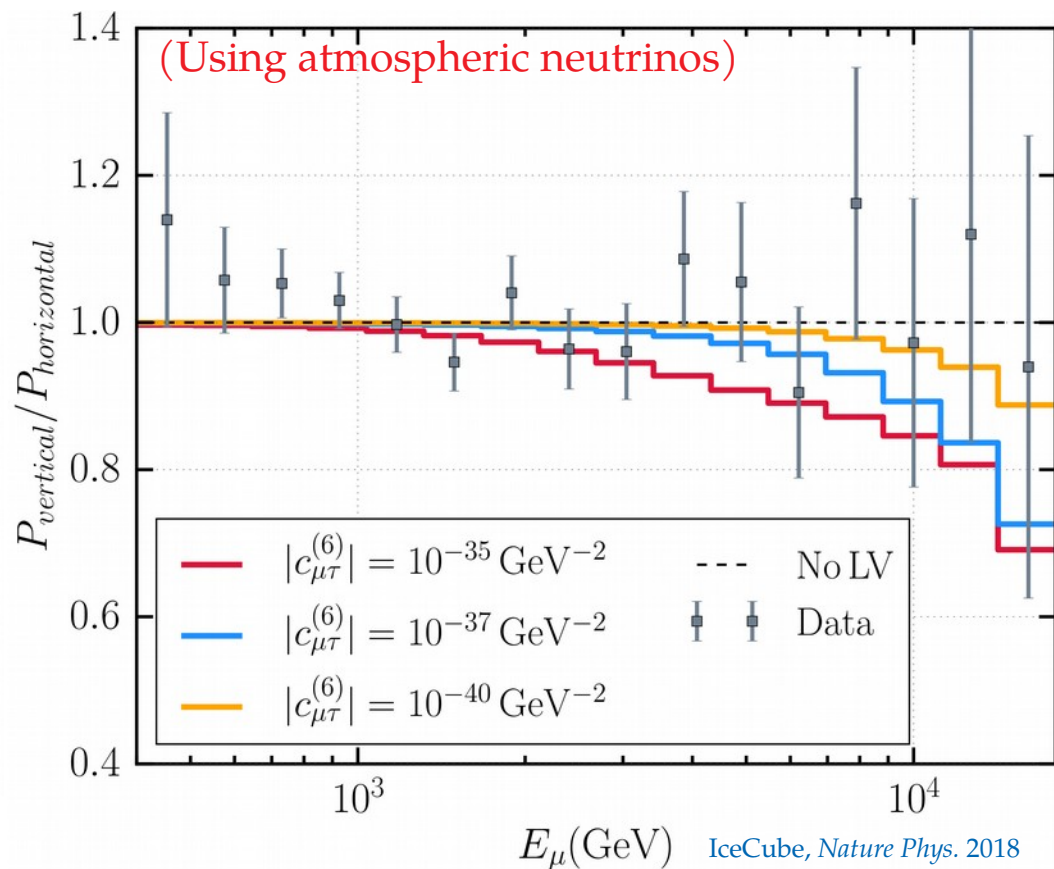
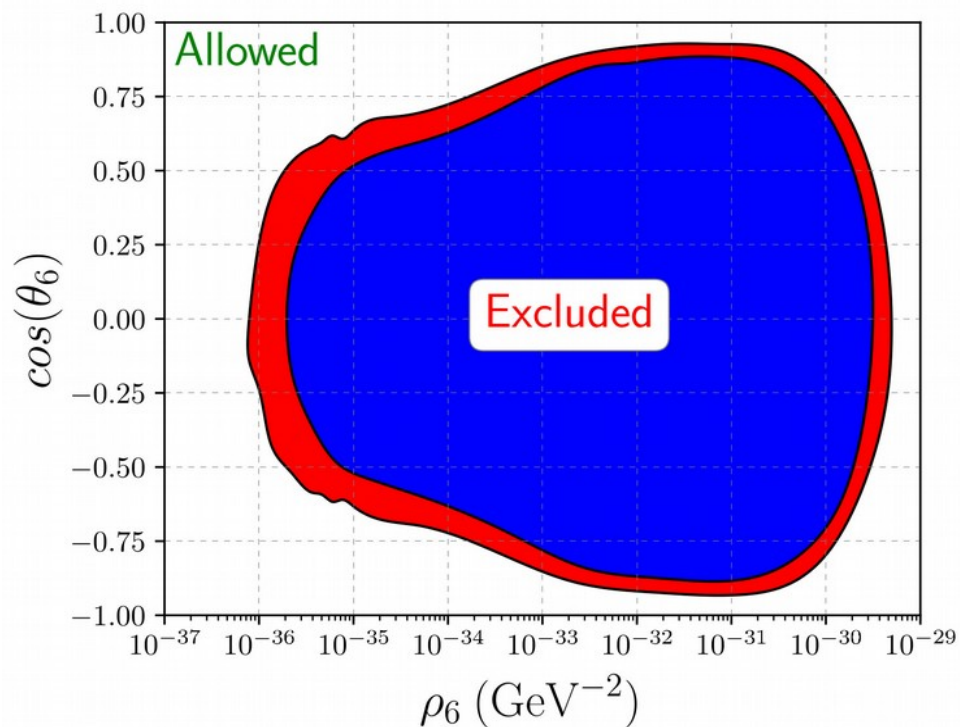
# New physics in the energy & angular distribution

Lorentz violation

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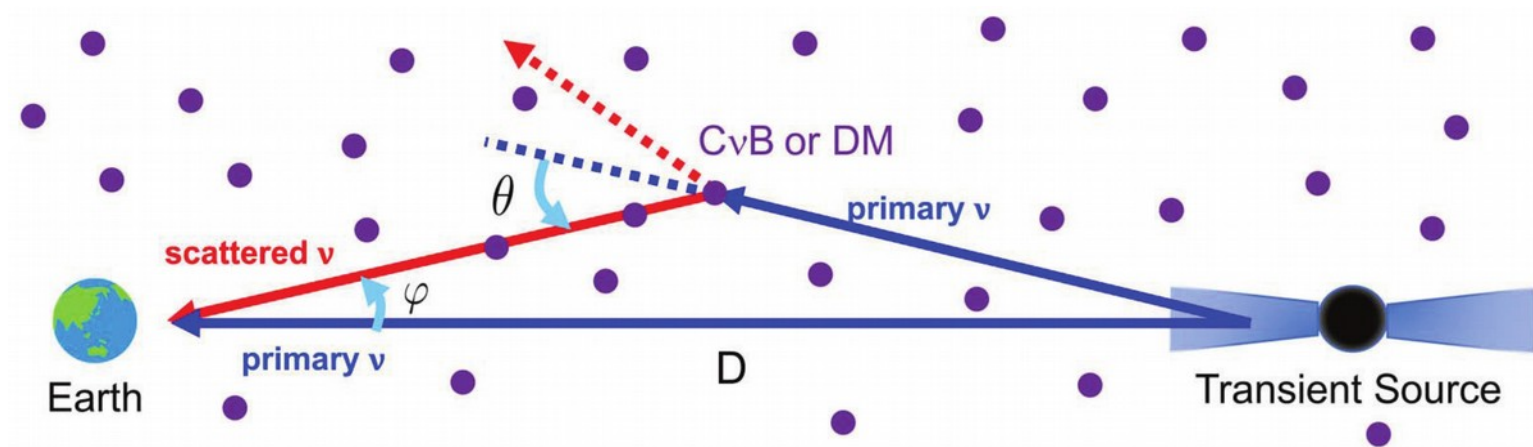
Lorentz invariance violation – Hamiltonian:  $H \sim \underbrace{m^2/(2E)}_{\text{Standard oscillations}} + \underbrace{\hat{a}^{(3)} - E \cdot \hat{c}^{(4)} + E^2 \cdot \hat{a}^{(5)} - E^3 \cdot \hat{c}^{(6)}}_{\text{Lorentz violation}}$

Best bounds come from IceCube



# New physics in timing — TeV–PeV

Multiple secret  $\nu\nu$  scatterings may delay the arrival of neutrinos from a transient



Shoemaker & Murase, 1903.08607

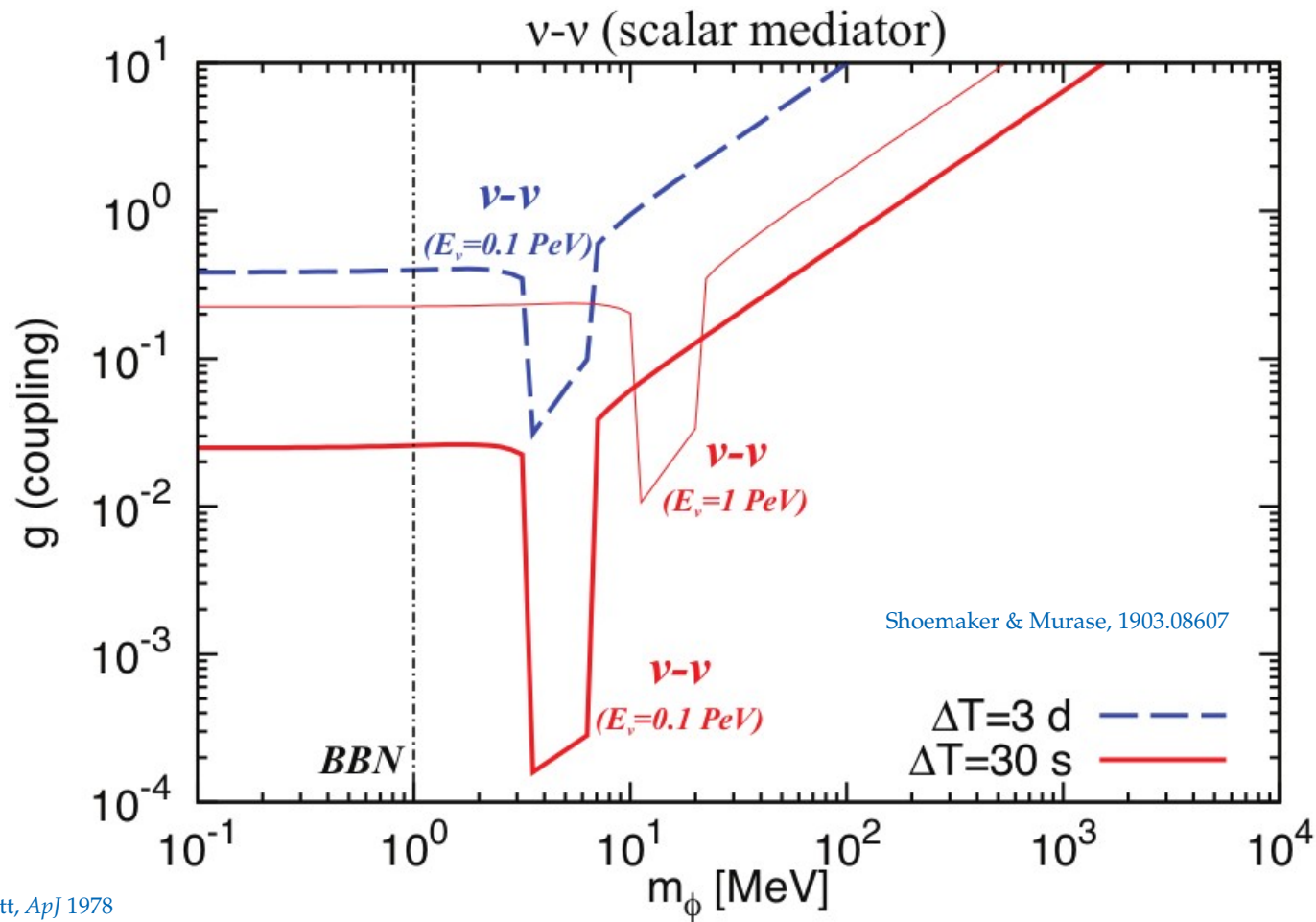
Characteristic time delay —

Optical depth to  $\nu\nu$ :  $\tau_{\nu\nu} = n_\nu \sigma_{\nu\nu} D$

$$\Delta t \approx 1500 \text{ s} \left( \frac{\tau_{\nu\nu}}{30} \right) \left( \frac{D}{3 \text{ Gpc}} \right) \left( \frac{m_\nu}{0.1 \text{ eV}} \right) \left( \frac{0.1 \text{ PeV}}{E_\nu} \right)$$

See also: Alcock & Hatchett, *ApJ* 1978

# New physics in timing — TeV–PeV



See also: Alcock & Hatchett, *ApJ* 1978

# Neutrino zenith angle distribution

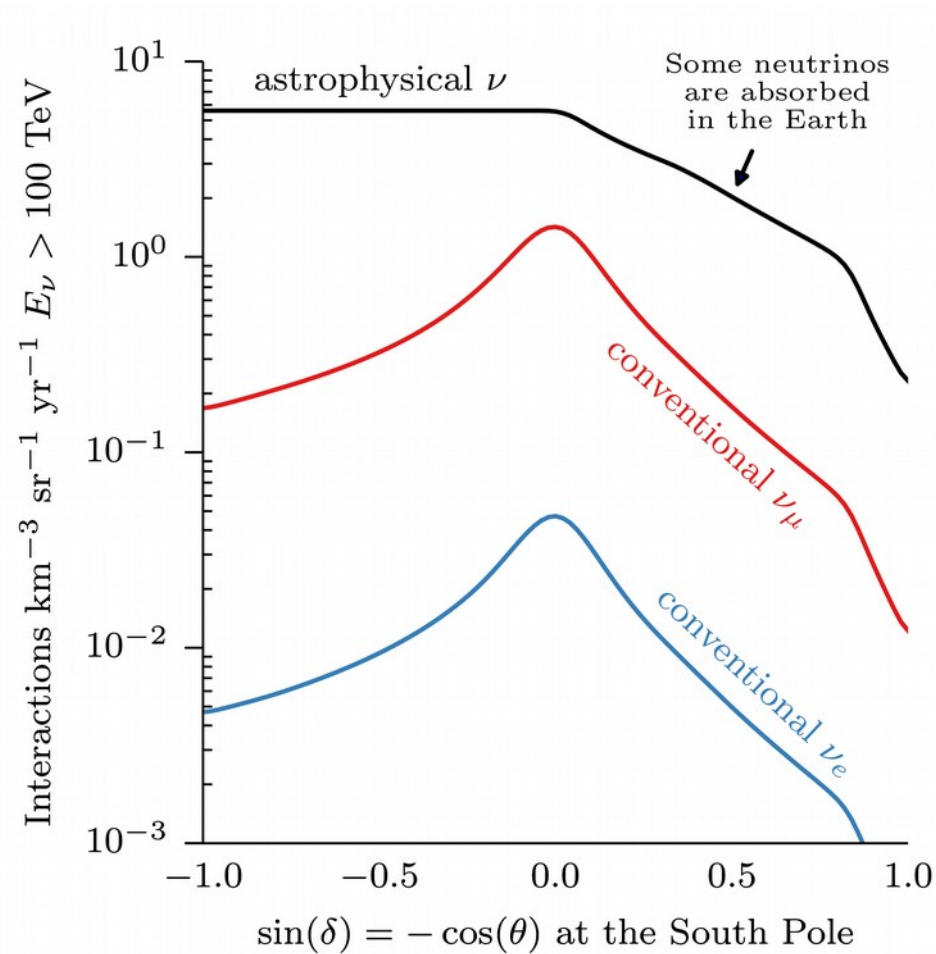
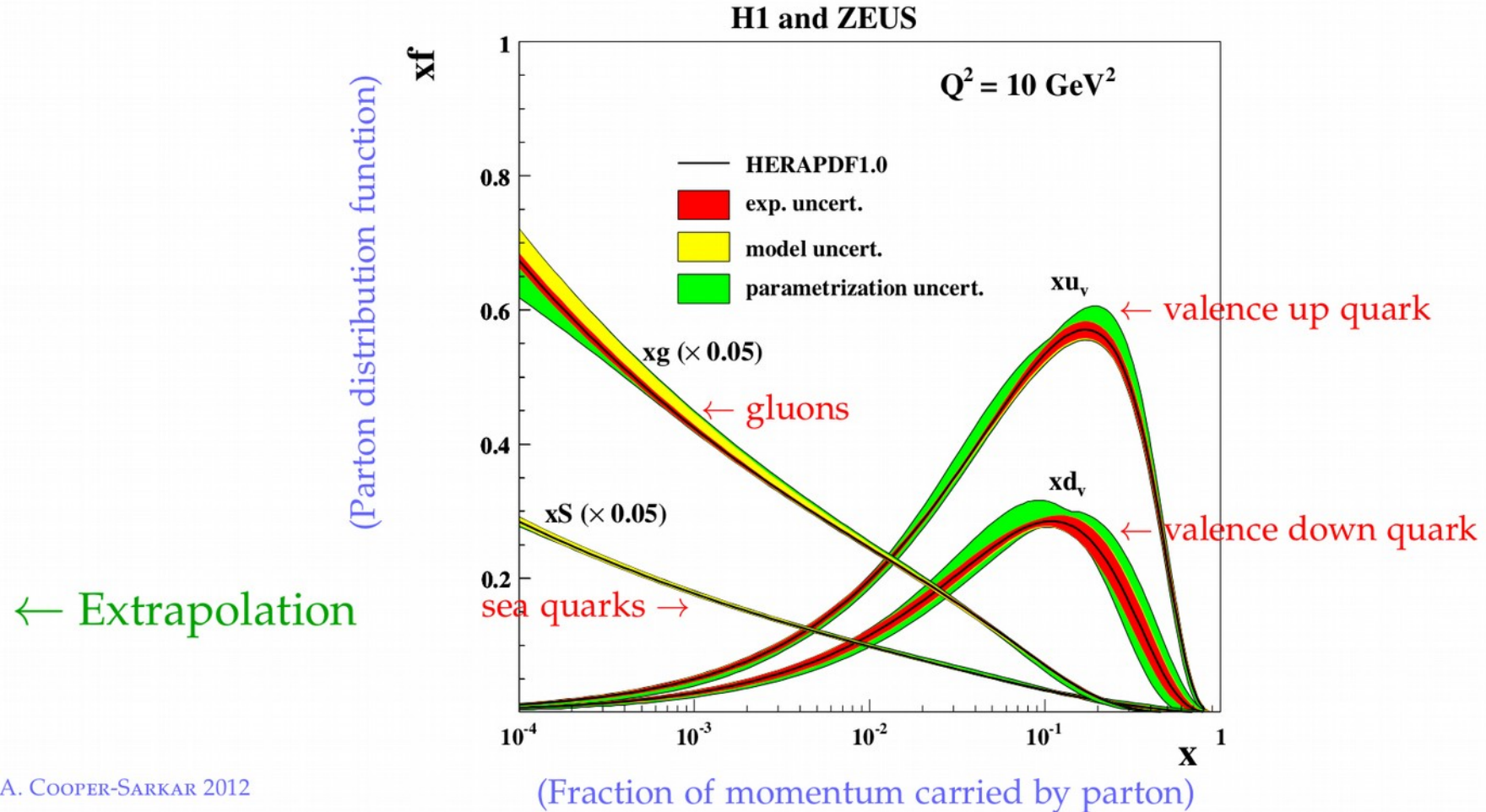


Figure by  
Jakob Van Santen  
ICRC 2017



# Peeking inside a proton



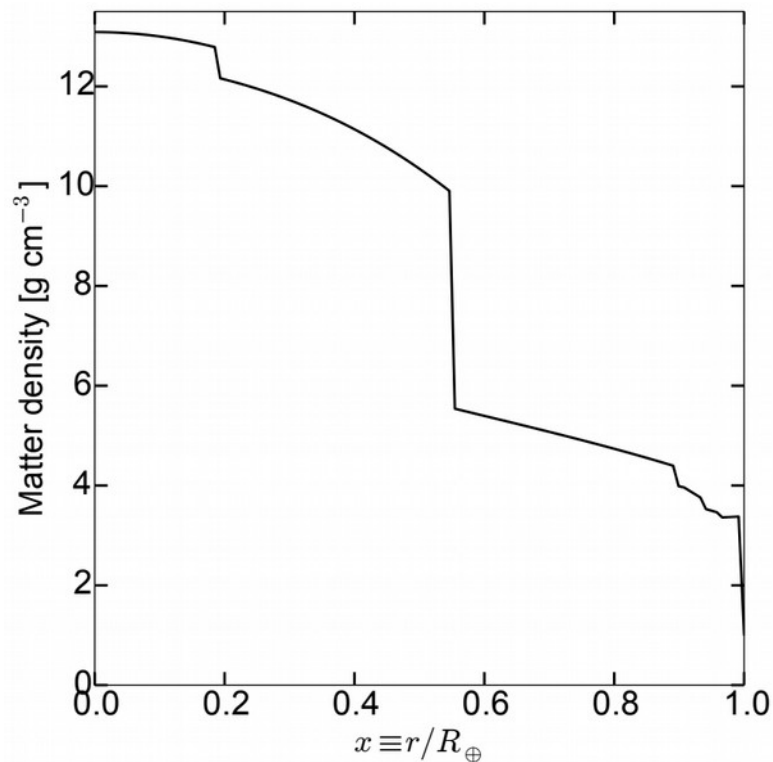
A. COOPER-SARKAR 2012



# A feel for the in-Earth attenuation

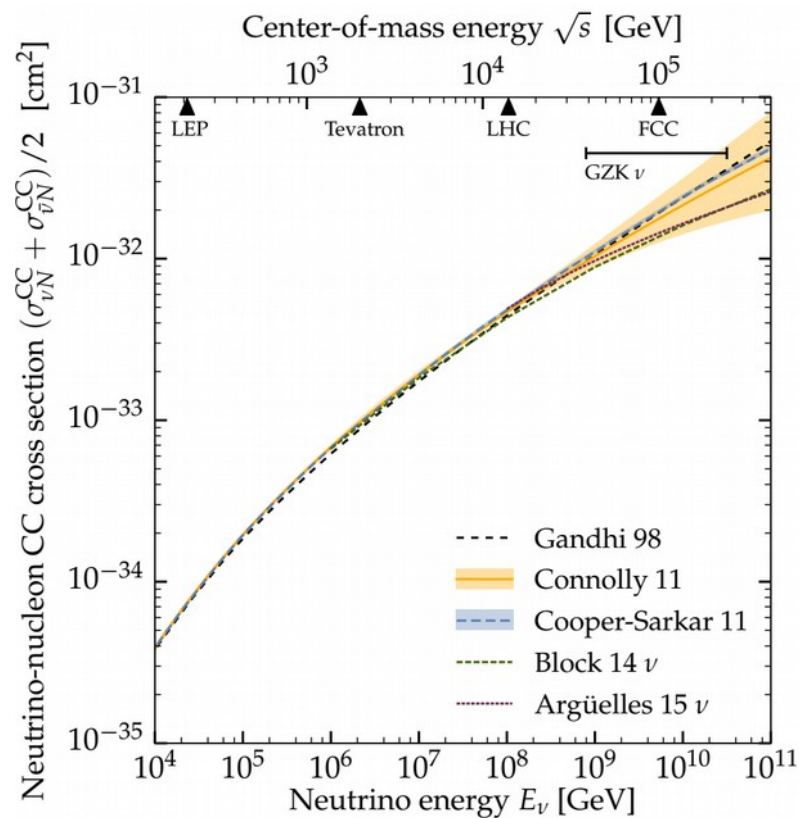
## Earth matter density

(Preliminary Reference Earth Model)

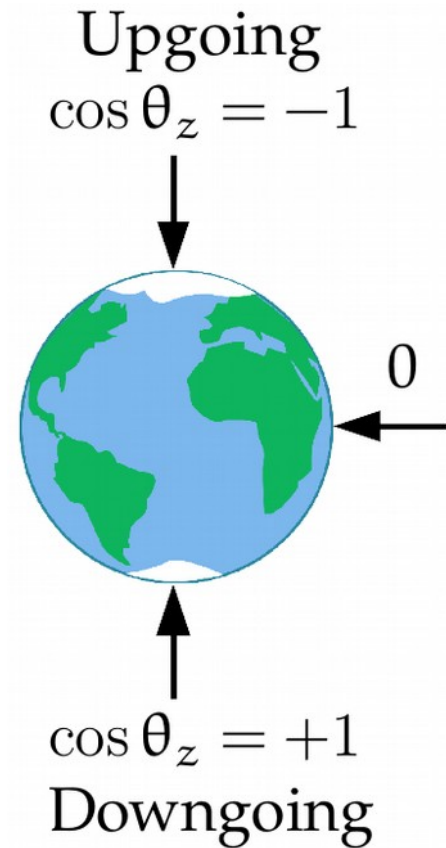
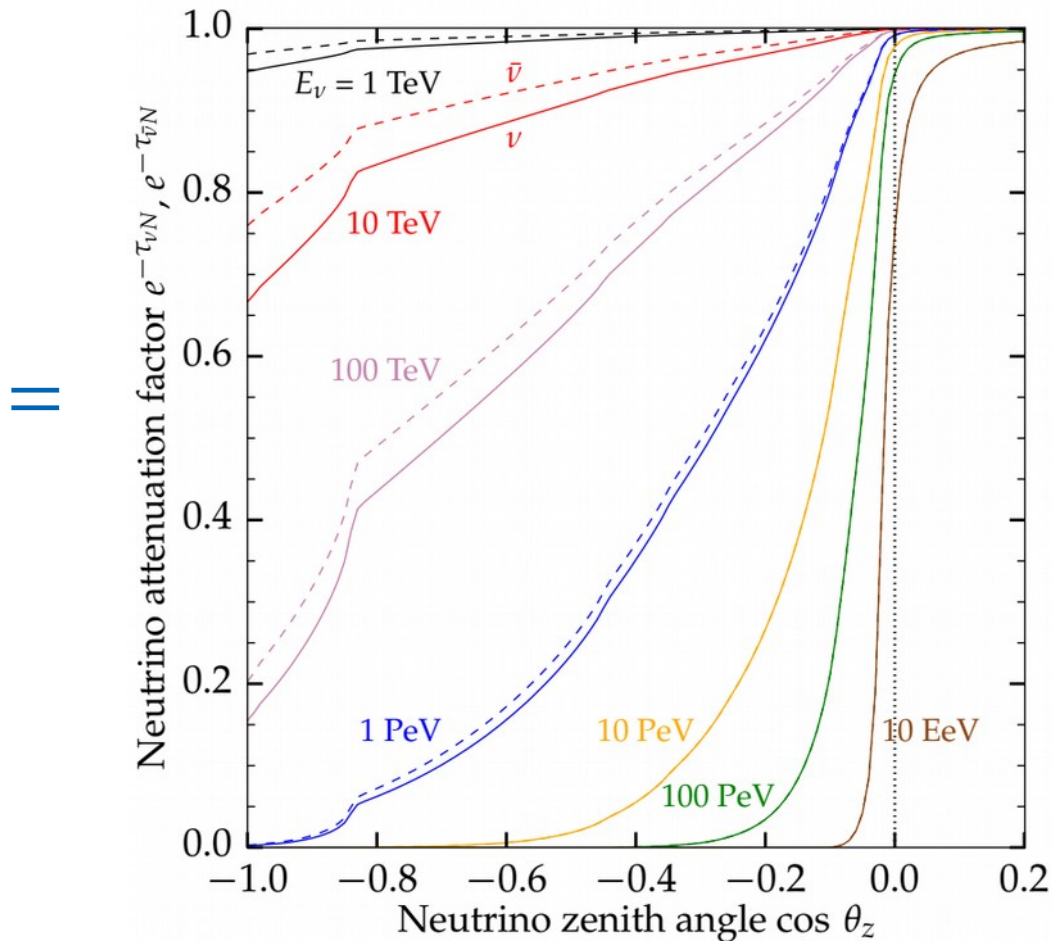


+

## Neutrino-nucleon cross section



# A feel for the in-Earth attenuation



# What goes into the (likelihood) mix?

- ▶ Inside each energy bin, we freely vary
  - ▶  $N_{\text{ast}}$  (showers from astrophysical neutrinos)
  - ▶  $N_{\text{atm}}$  (showers from atmospheric neutrinos)
  - ▶  $\gamma$  (astrophysical spectral index)
  - ▶  $\sigma_{\text{CC}}$  (neutrino-nucleon charged-current cross section)
- ▶ For each combination, we generate the angular and energy shower spectrum...
- ▶ ... and compare it to the observed HESE spectrum via a likelihood
- ▶ Maximum likelihood yields  $\sigma_{\text{CC}}$  (marginalized over nuisance parameters)
- ▶ Bins are independent of each other – there are no (significant) cross-bin correlations

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Including detector resolution  
(10% in energy, 15° in direction)

# Marginalized cross section in each bin

TABLE I. Neutrino-nucleon charged-current inclusive cross sections, averaged between neutrinos ( $\sigma_{\nu N}^{\text{CC}}$ ) and anti-neutrinos ( $\sigma_{\bar{\nu} N}^{\text{CC}}$ ), extracted from 6 years of IceCube HESE showers. To obtain these results, we fixed  $\sigma_{\bar{\nu} N}^{\text{CC}} = \langle \sigma_{\bar{\nu} N}^{\text{CC}} / \sigma_{\nu N}^{\text{CC}} \rangle \cdot \sigma_{\nu N}^{\text{CC}}$  — where  $\langle \sigma_{\bar{\nu} N}^{\text{CC}} / \sigma_{\nu N}^{\text{CC}} \rangle$  is the average ratio of  $\bar{\nu}$  to  $\nu$  cross sections calculated using the standard prediction from Ref. [60](#) — and  $\sigma_{\nu N}^{\text{NC}} = \sigma_{\nu N}^{\text{CC}}/3$ ,  $\sigma_{\bar{\nu} N}^{\text{NC}} = \sigma_{\bar{\nu} N}^{\text{CC}}/3$ . Uncertainties are statistical plus systematic, added in quadrature.

$E_\nu$ [TeV]	$\langle E_\nu \rangle$ [TeV]	$\langle \sigma_{\bar{\nu} N}^{\text{CC}} / \sigma_{\nu N}^{\text{CC}} \rangle$	$\log_{10}[\frac{1}{2}(\sigma_{\nu N}^{\text{CC}} + \sigma_{\bar{\nu} N}^{\text{CC}})/\text{cm}^2]$
18–50	32	0.752	$-34.35 \pm 0.53$
50–100	75	0.825	$-33.80 \pm 0.67$
100–400	250	0.888	$-33.84 \pm 0.67$
400–2004	1202	0.957	$> -33.21 (1\sigma)$

MB & A. Connolly, 1711.11043

# Energy and angular shower spectra

Rate from all flavors, CC + NC:

$$\frac{d^2 N_{\text{sh}}}{dE_{\text{sh}} d \cos \theta_z} = \frac{d^2 N_{\text{sh},e}^{\text{CC}}}{dE_{\text{sh}} d \cos \theta_z} + \text{Br}_{\tau \rightarrow \text{sh}} \frac{d^2 N_{\text{sh},\tau}^{\text{CC}}}{dE_{\text{sh}} d \cos \theta_z} + \sum_{l=e,\mu,\tau} \frac{d^2 N_{\text{sh},l}^{\text{NC}}}{dE_{\text{sh}} d \cos \theta_z}$$

$\text{Br}_{\tau \rightarrow \text{sh}} = 0.83$

Contribution from one flavor CC:

$$\frac{d^2 N_{\text{sh},l}^{\text{CC}}}{dE_{\text{sh}} d \cos \theta_z}(E_{\text{sh}}, \cos \theta_z) \simeq -2\pi \rho_{\text{ice}} N_A V T \left\{ \Phi_l(E_\nu) \sigma_{\nu N}^{\text{CC}}(E_\nu) e^{-\tau_{\nu N}(E_\nu, \theta_z)} + \Phi_{\bar{l}}(E_\nu) \sigma_{\bar{\nu} N}^{\text{CC}}(E_\nu) e^{-\tau_{\bar{\nu} N}(E_\nu, \theta_z)} \right\} \Big|_{E_\nu = E_{\text{sh}}/f_{l,\text{CC}}}$$

Conversion between shower energy and neutrino energy:

$$f_{l,t} \equiv \frac{E_{\text{sh}}}{E_\nu} \simeq \begin{cases} 1 & \text{for } l = e \text{ and } t = \text{CC} \\ [\langle y \rangle + 0.7(1 - \langle y \rangle)] \simeq 0.8 & \text{for } l = \tau \text{ and } t = \text{CC} \\ \langle y \rangle \simeq 0.25 & \text{for } l = e, \mu, \tau \text{ and } t = \text{NC} \end{cases}$$

MB & A. Connolly, 1711.11043



# Detector resolution

Number of contained showers:

$$\frac{d^2 N_{\text{sh}}}{dE_{\text{dep}} d\cos\theta_z} = \int dE_{\text{sh}} \int d\cos\theta'_z \frac{d^2 N_{\text{sh}}}{dE_{\text{sh}} d\cos\theta'_z} R_E(E_{\text{sh}}, E_{\text{dep}}, \sigma_E(E_{\text{sh}})) R_\theta(\cos\theta'_z, \cos\theta_z, \sigma_{\cos\theta_z})$$

**Energy resolution:** [Palomares-Ruiz, Vincent, Mena *PRD* 2015; Vincent, Palomares-Ruiz, Mena *PRD* 2016; MB, Beacom, Murase, *PRD* 2016]

$$R_E(E_{\text{sh}}, E_{\text{dep}}, \sigma_E(E_{\text{sh}})) = \frac{1}{\sqrt{2\pi\sigma_E^2(E_{\text{sh}})}} \exp\left[-\frac{(E_{\text{sh}} - E_{\text{dep}})^2}{2\sigma_E^2(E_{\text{sh}})}\right] \quad \text{with } \sigma_E(E_{\text{sh}}) = 0.1E_{\text{sh}}$$

IceCube, *JINST* 2014

**Angular resolution:**

$$R_\theta(\cos\theta'_z, \cos\theta_z, \sigma_{\cos\theta_z}) = \frac{1}{\sqrt{2\pi\sigma_{\cos\theta_z}^2}} \exp\left[-\frac{(\cos\theta'_z - \cos\theta_z)^2}{2\sigma_{\cos\theta_z}^2}\right]$$

$$\text{with } \sigma_{\cos\theta_z} \equiv \frac{1}{2} [|\cos(\theta_z + \sigma_{\theta_z}) - \cos\theta_z| + |\cos(\theta_z - \sigma_{\theta_z}) - \cos\theta_z|] \quad \text{and } \sigma_{\theta_z} = 15^\circ$$

MB & A. Connolly, 1711.11043

# Likelihood

In an energy bin containing  $N_{\text{sh}}^{\text{obs}}$  observed showers, the likelihood is

Each energy bin is independent

$$\mathcal{L} = \frac{e^{-(N_{\text{sh}}^{\text{atm}} + N_{\text{sh}}^{\text{ast}})}}{N_{\text{sh}}^{\text{obs}}!} \prod_{i=1}^{N_{\text{sh}}^{\text{obs}}} \mathcal{L}_i$$

Partial likelihood, *i.e.*, relative probability of the  $i$ -th shower being from an atmospheric neutrino or an astrophysical neutrino:

Depends on  $\sigma_{\nu N}$

$$\mathcal{L}_i = N_{\text{sh}}^{\text{atm}} \mathcal{P}_i^{\text{atm}} + N_{\text{sh}}^{\text{ast}} \mathcal{P}_i^{\text{ast}}$$

$$\mathcal{P}_i^{\text{atm}} = \left( \int_{E_{\text{dep}}^{\text{min}}}^{E_{\text{dep}}^{\text{max}}} dE_{\text{dep}} \int_{-1}^1 d \cos \theta_z \frac{d^2 N_{\text{sh}}^{\text{atm}}}{dE_{\text{dep}} d \cos \theta_z} \right)^{-1} \left( \frac{d^2 N_{\text{sh}}^{\text{atm}}}{dE_{\text{dep}} d \cos \theta_z} \Big|_{E_{\text{dep},i}, \cos \theta_{z,i}} \right)$$

PDF for this shower to be made by an atmospheric  $\nu$

$$\mathcal{P}_i^{\text{ast}} = \left( \int_{E_{\text{dep}}^{\text{min}}}^{E_{\text{dep}}^{\text{max}}} dE_{\text{dep}} \int_{-1}^1 d \cos \theta_z \frac{d^2 N_{\text{sh}}^{\text{ast}}}{dE_{\text{dep}} d \cos \theta_z} \right)^{-1} \left( \frac{d^2 N_{\text{sh}}^{\text{ast}}}{dE_{\text{dep}} d \cos \theta_z} \Big|_{E_{\text{dep},i}, \cos \theta_{z,i}} \right)$$

PDF for this shower to be made by an astrophysical  $\nu$

Depends on  $\gamma$  and  $\sigma_{\nu N}$

MB & A. Connolly, 1711.11043

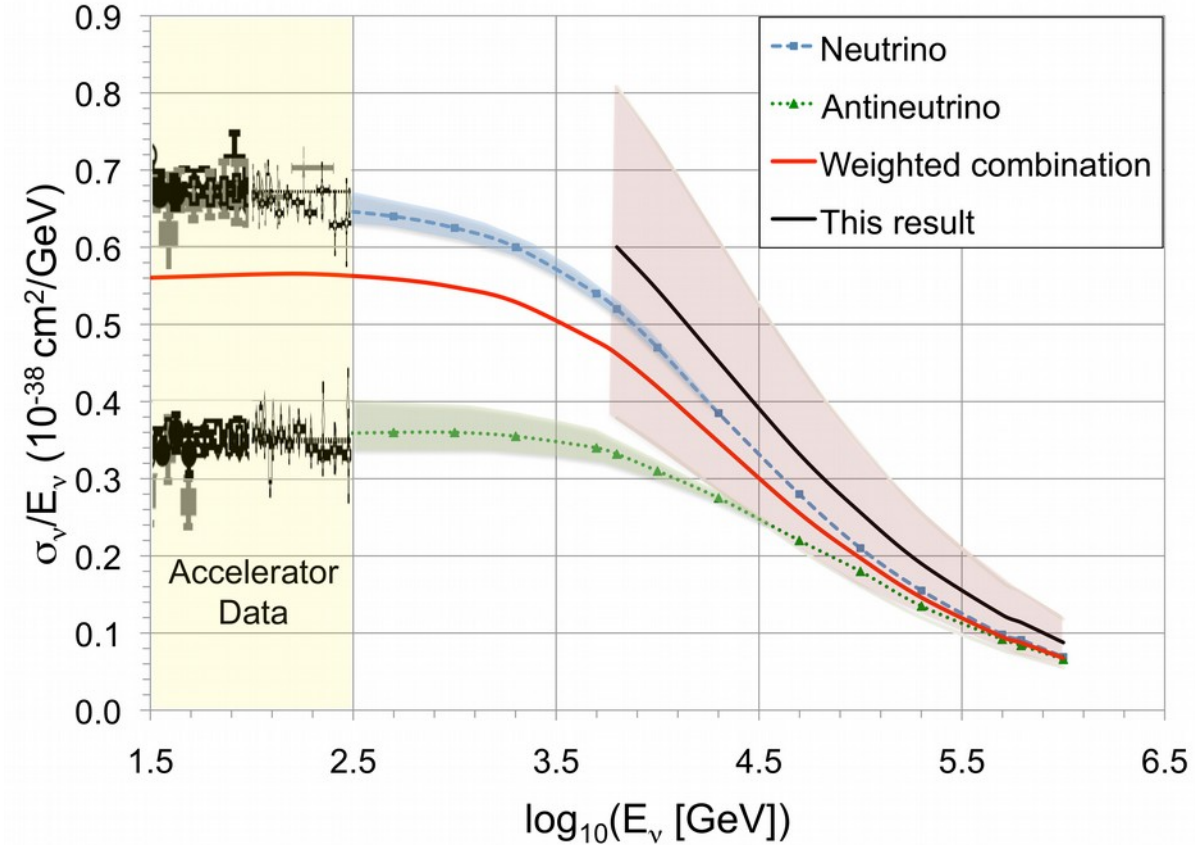
See also: Palomares-Ruiz, Vincent, Mena *PRD* 2015; Vincent, Palomares-Ruiz, Mena *PRD* 2016

# The fine print

- ▶ High-energy  $\nu$ 's: astrophysical (isotropic) + atmospheric (**anisotropic**)
  - We take into account the shape of the atmospheric contribution
- ▶ The shape of the astrophysical  $\nu$  **energy spectrum** is still uncertain
  - We take a  $E^{-\gamma}$  spectrum in *narrow* energy bins
- ▶ **NC showers** are sub-dominant to **CC showers**, but they are indistinguishable
  - Following Standard-Model predictions, we take  $\sigma_{\text{NC}} = \sigma_{\text{CC}}/3$
- ▶ IceCube does not **distinguish  $\nu$  from  $\bar{\nu}$** , and their cross-sections are different
  - We assume equal fluxes, expected from production via pp collisions
  - We assume the avg. ratio  $\langle \sigma_{\bar{\nu}N} / \sigma_{\nu N} \rangle$  in each bin known, from SM predictions
- ▶ The **flavor composition** of astrophysical neutrinos is still uncertain
  - We assume equal flux of each flavor, compatible with theory and observations

# Using through-going muons instead

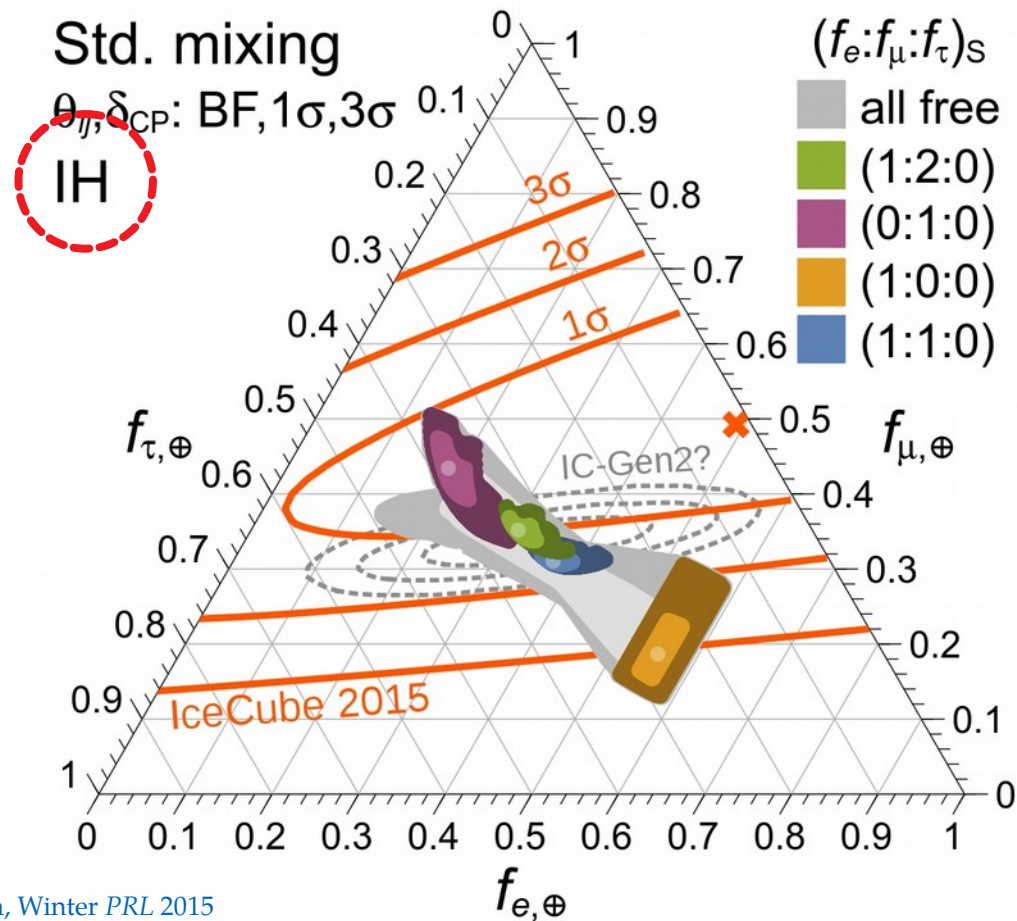
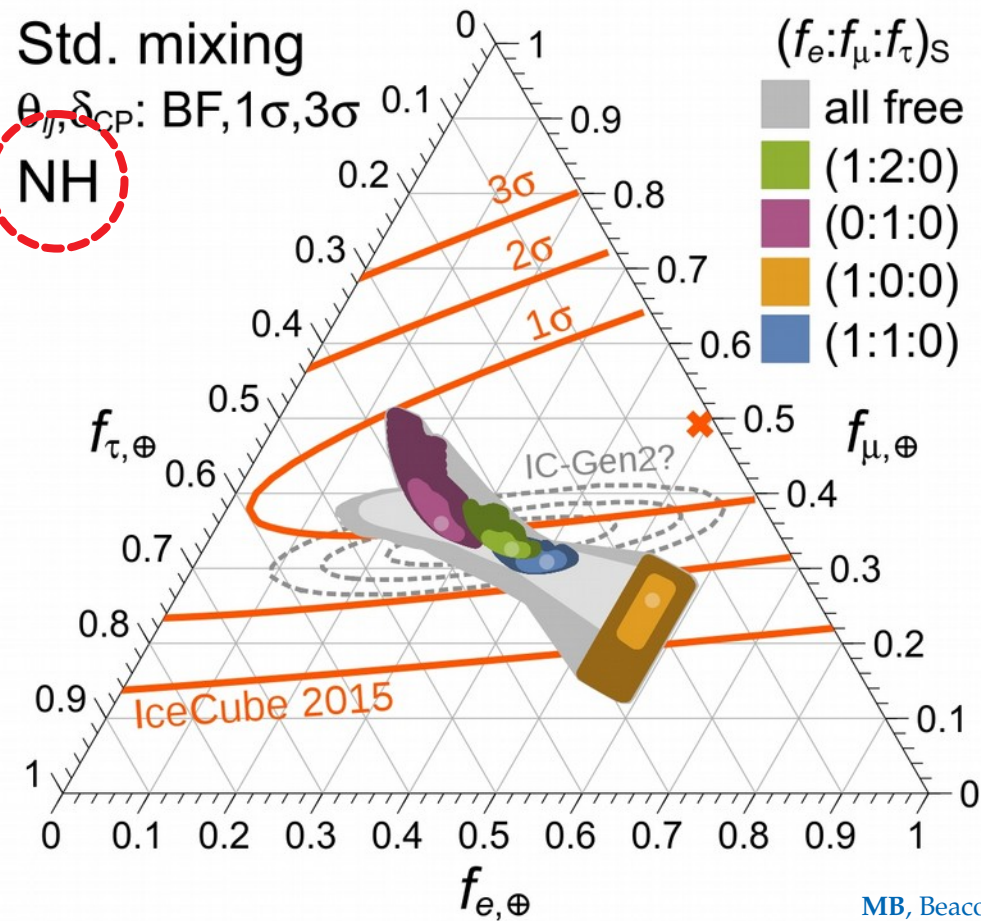
- ▶ Use  $\sim 10^4$  through-going muons
- ▶ Measured:  $dE_\mu/dx$
- ▶ Inferred:  $E_\mu \approx dE_\mu/dx$
- ▶ From simulations (uncertain):  
most likely  $E_\nu$  given  $E_\mu$
- ▶ Fit the ratio  $\sigma_{\text{obs}}/\sigma_{\text{SM}}$   
 $1.30^{+0.21}_{-0.19}(\text{stat.})^{+0.39}_{-0.43}(\text{syst.})$
- ▶ All events grouped in a single  
energy bin 6–980 TeV



*IceCube, Nature 2017*

# Flavor composition – a few source choices

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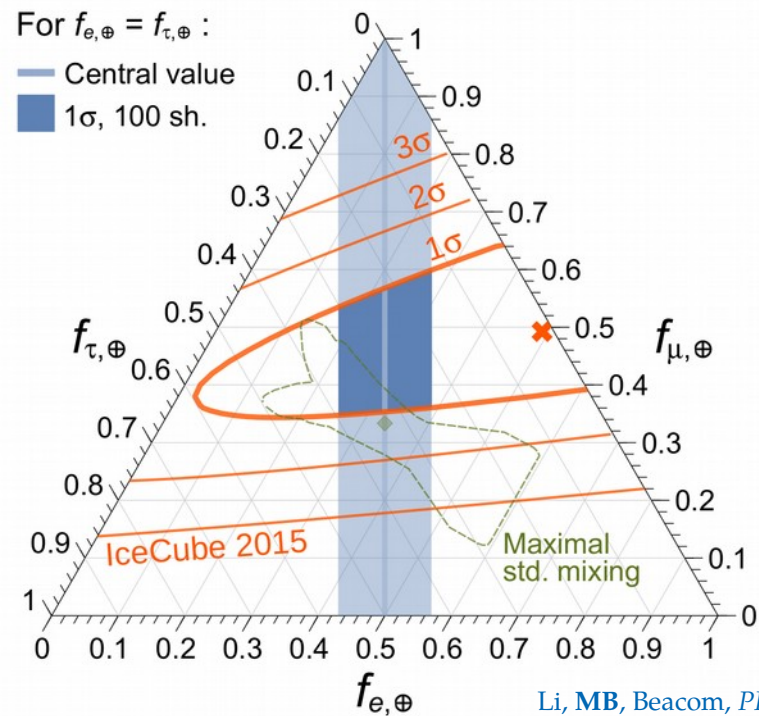
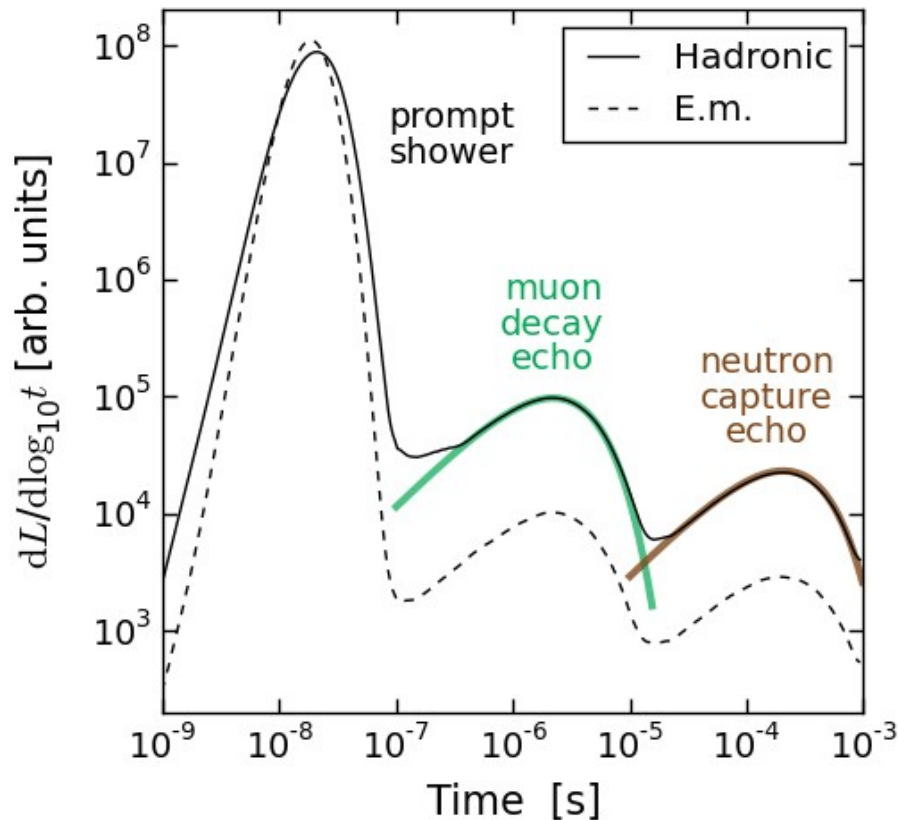


MB, Beacom, Winter PRL 2015



## Side note: Improving flavor-tagging using *echoes*

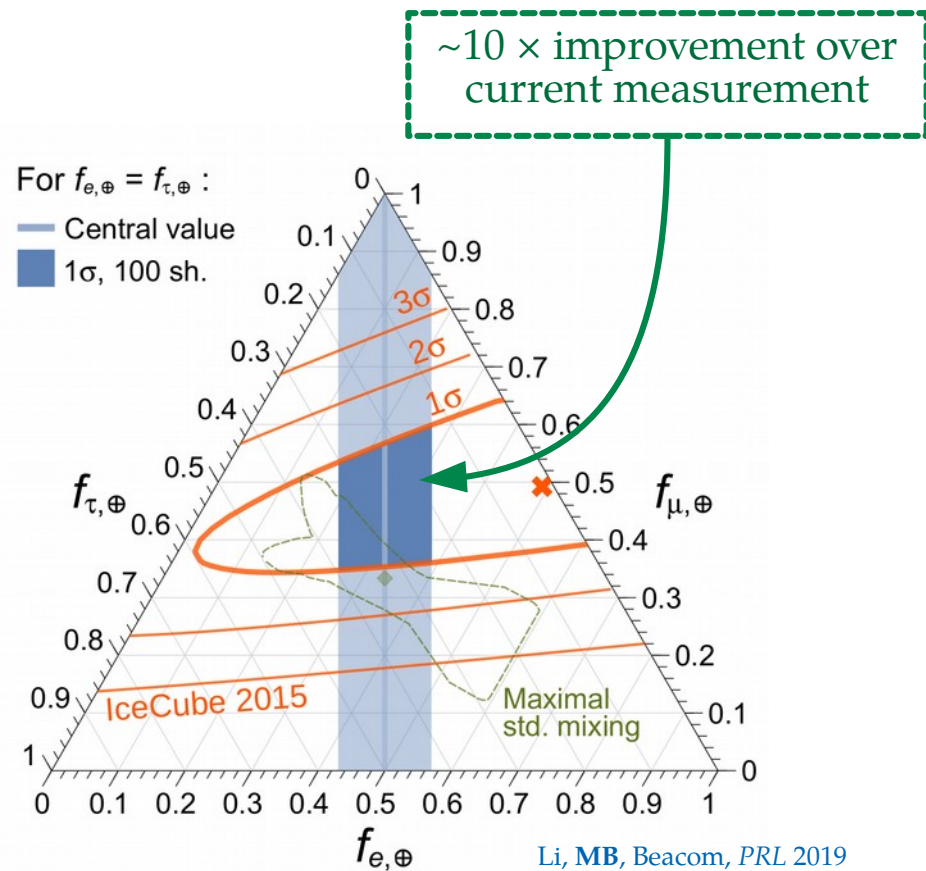
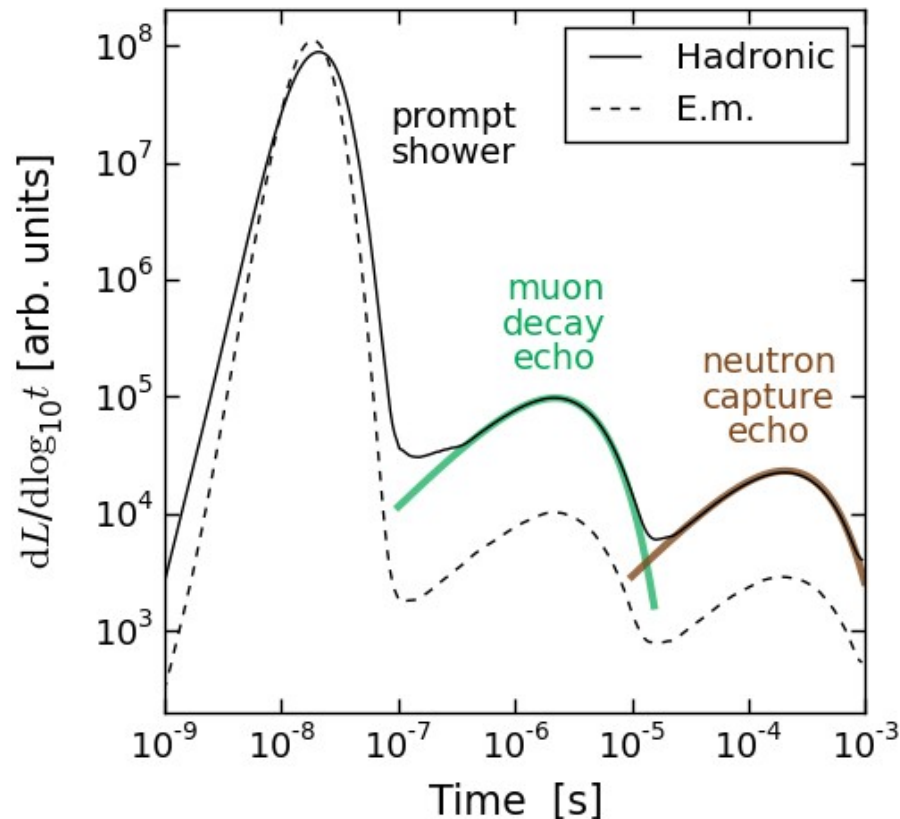
Late-time light (*echoes*) from muon decays and neutron captures can separate showers made by  $\nu_e$  and  $\nu_\tau$  –



Li, MB, Beacom, PRL 2019

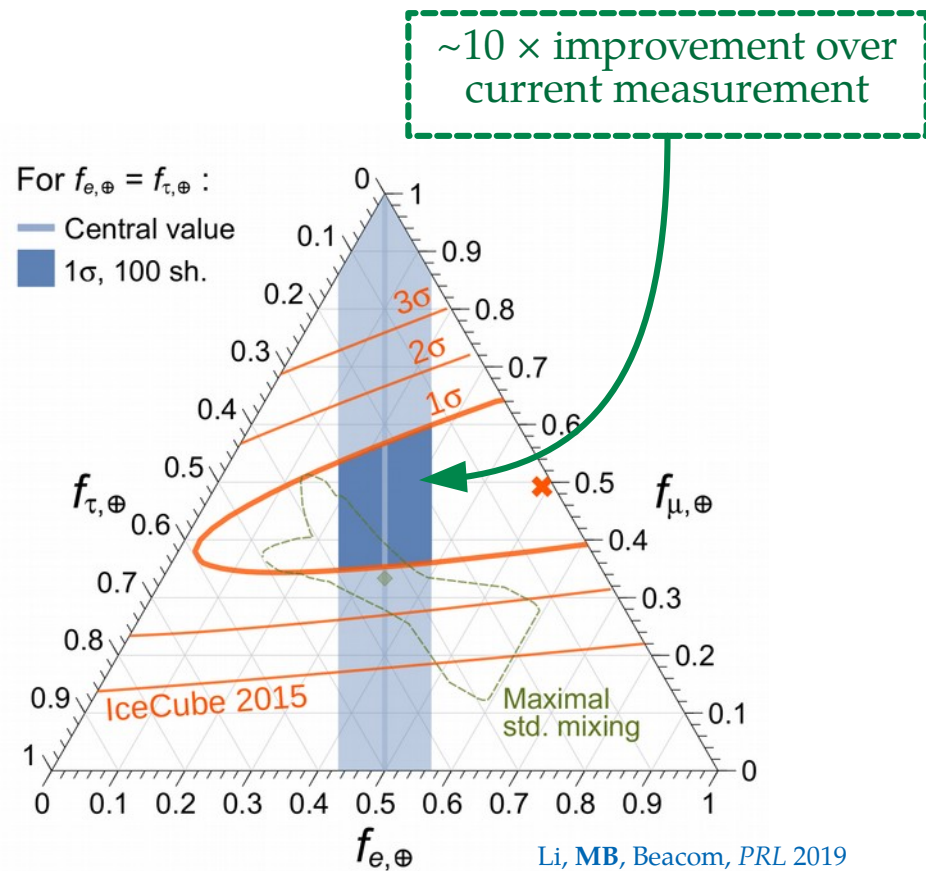
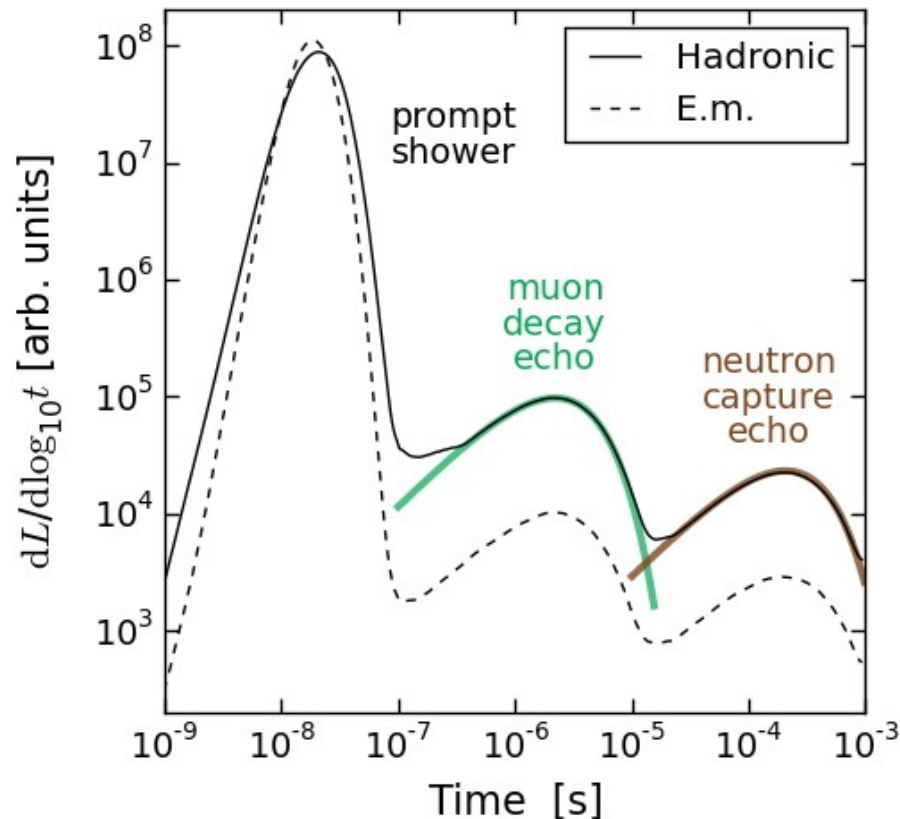
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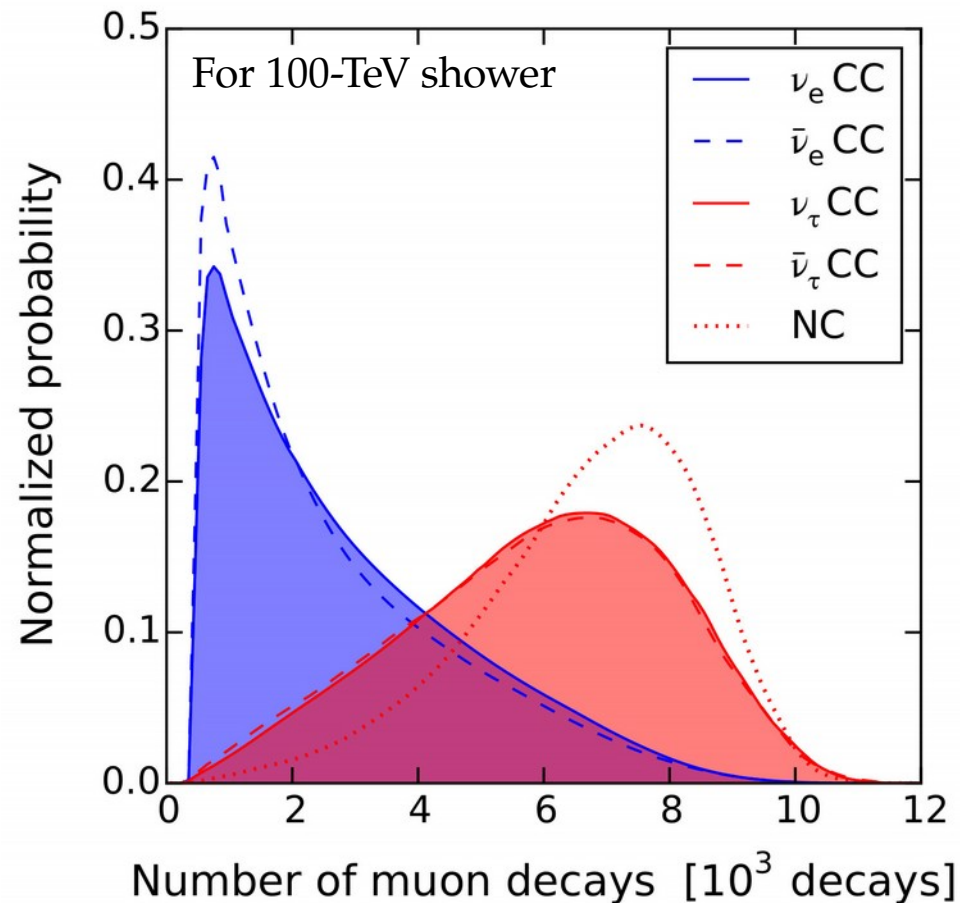
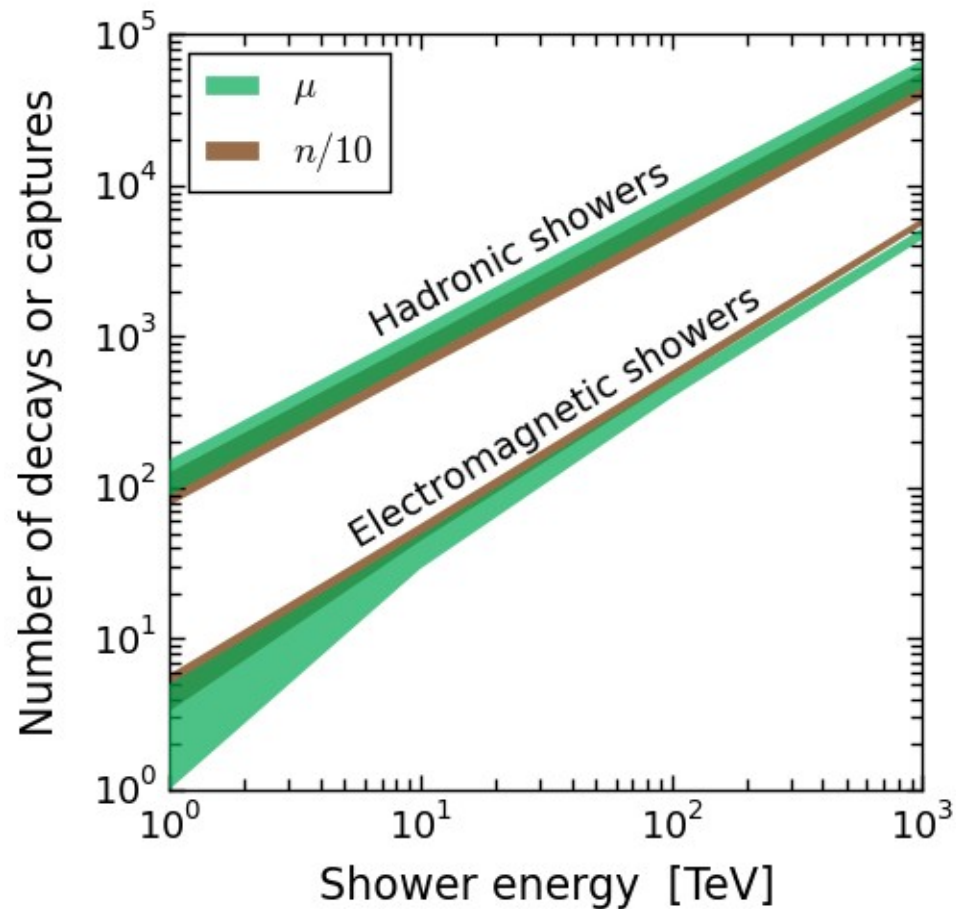


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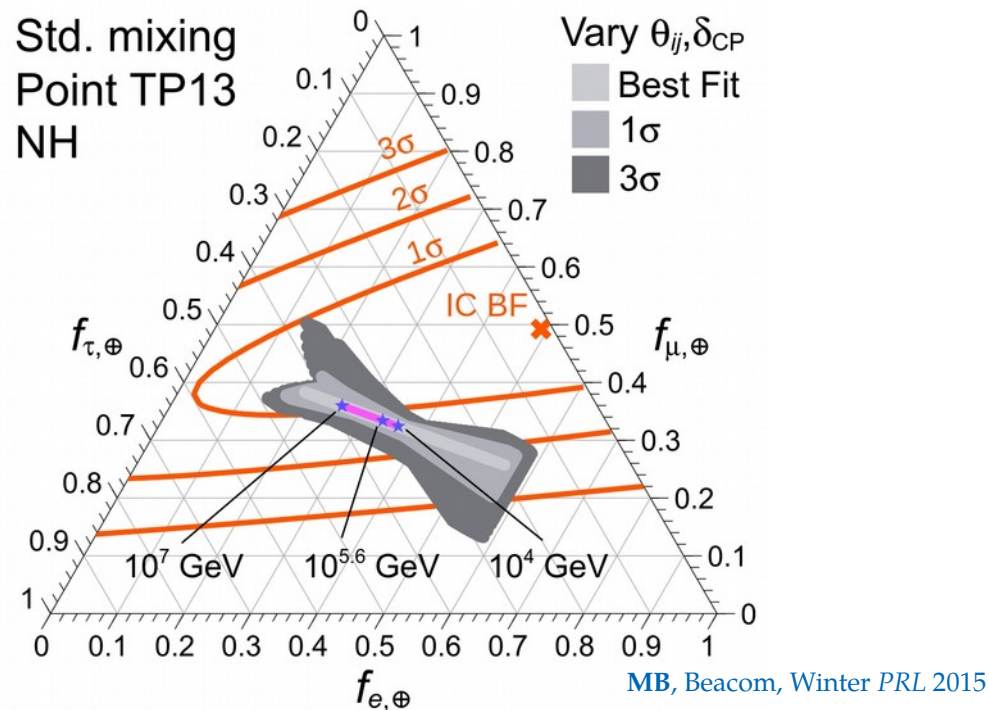
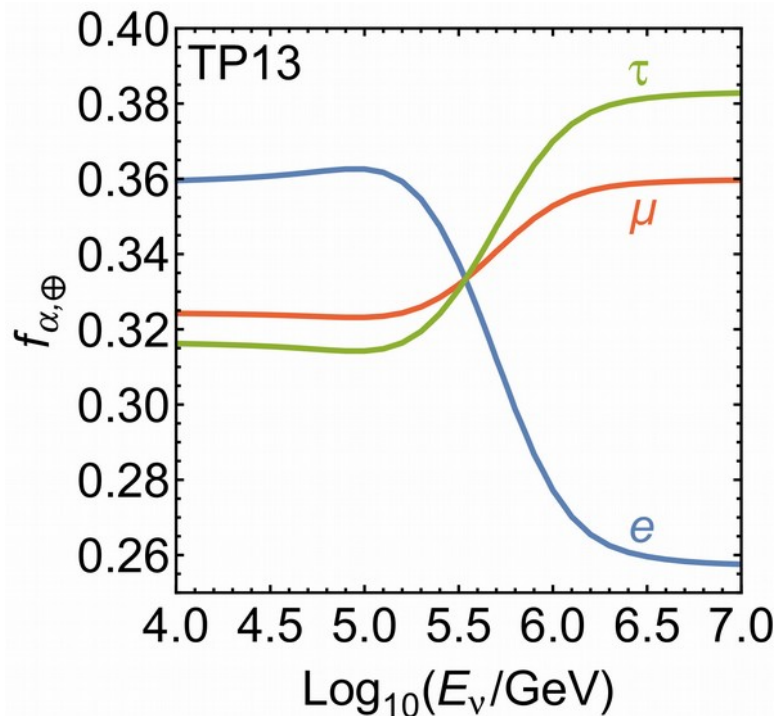
# Hadronic *vs.* electromagnetic showers





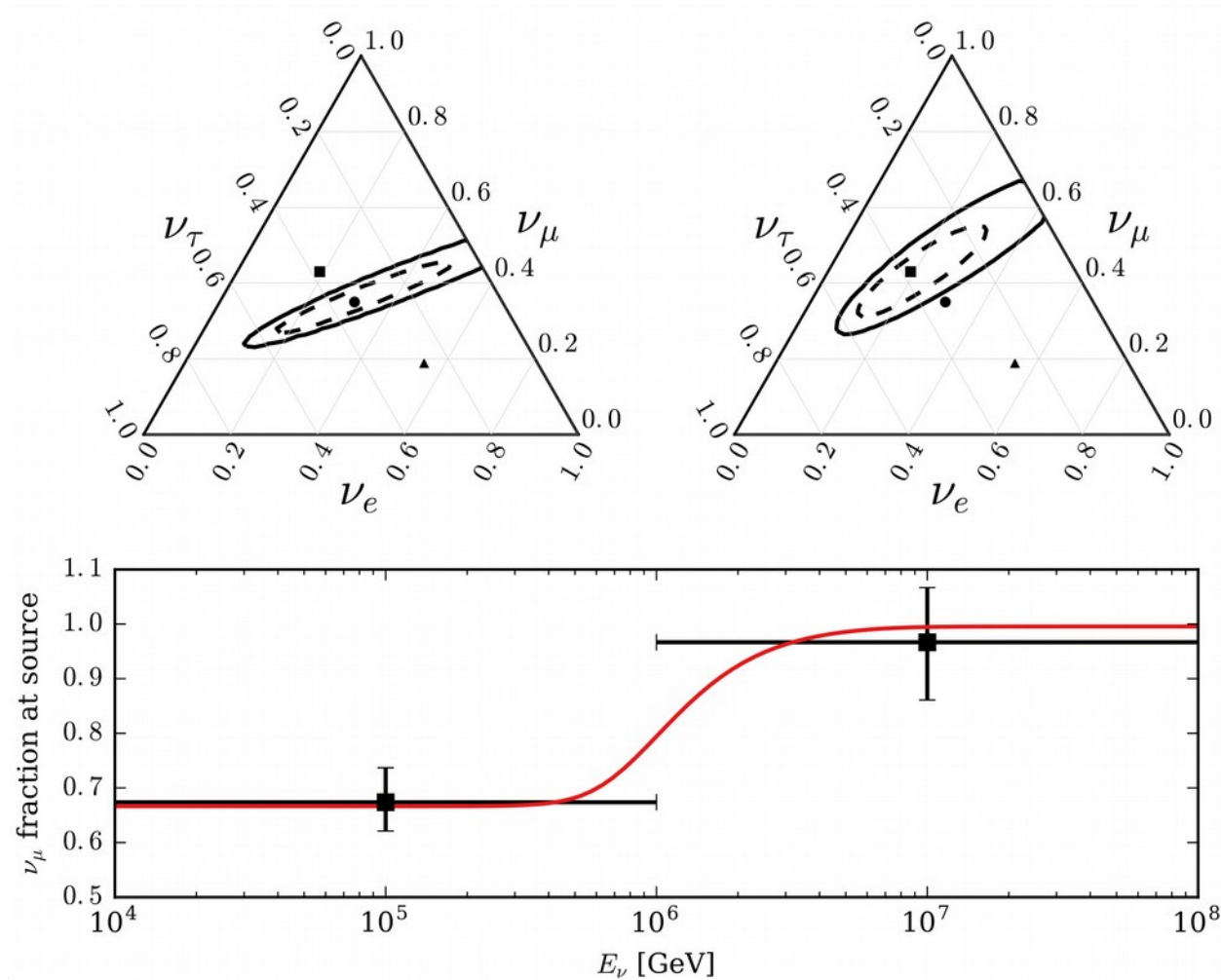
# Energy dependence of the flavor composition?

Different neutrino production channels accessible at different energies –



- ▶ TP13:  $p\gamma$  model, target photons from electron-positron annihilation [Hümmer+, *Astropart. Phys.* 2010]
- ▶ Will be difficult to resolve [Kashti, Waxman, *PRL* 2005; Lipari, Lusignoli, Meloni, *PRD* 2007]

## ... Observable in IceCube-Gen2?



Borrowed from M. Kowalski



# Flavor content of neutrino mass eigenstates

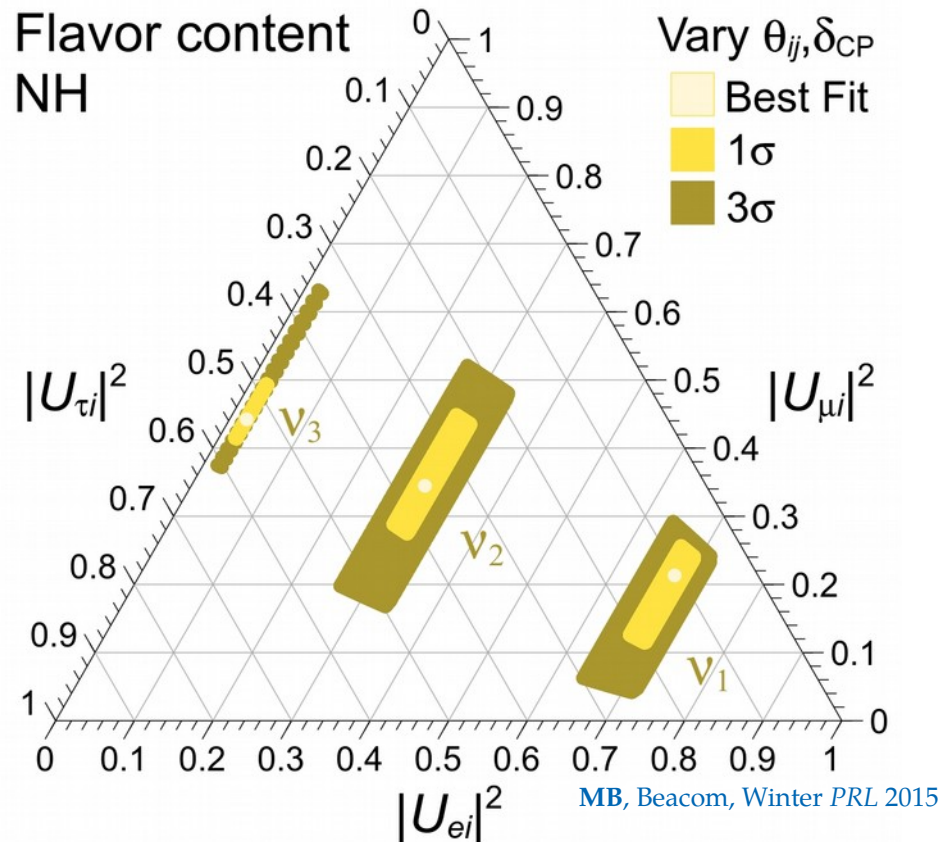
Flavor content for every allowed combination of mixing parameters –

$$|U_{\alpha i}|^2 = |U_{\alpha i}(\theta_{12}, \theta_{23}, \theta_{13}, \delta_{\text{CP}})|^2$$

Known to within 2%

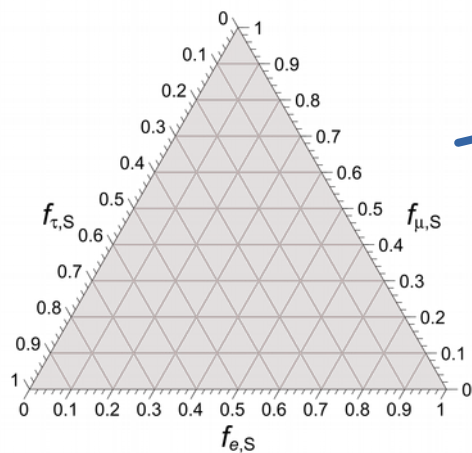
Known to within 8%

Known to within 20% (or worse)



# Measuring the neutrino lifetime

## Sources

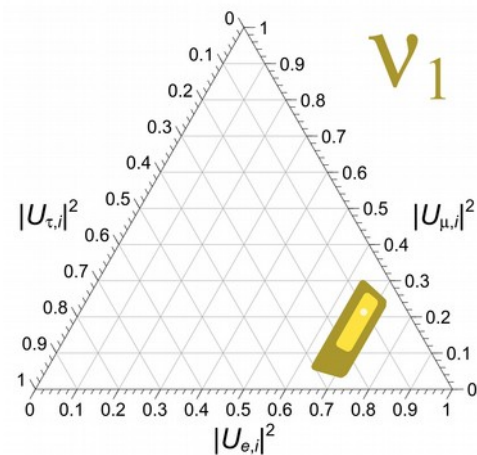


$\nu_2, \nu_3 \rightarrow \nu_1$   
 $\nu_1$  lightest and stable

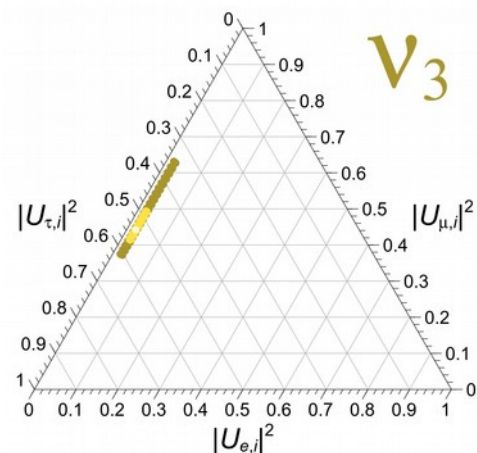
If all unstable  
 neutrinos decay

$\nu_1, \nu_2 \rightarrow \nu_3$   
 $\nu_3$  lightest and stable

## Earth



$$f_{\alpha,\oplus} = |U_{\alpha 1}|^2$$



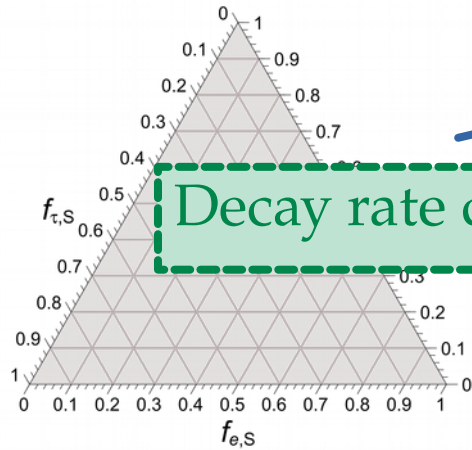
$$f_{\alpha,\oplus} = |U_{\alpha 3}|^2$$

# Measuring the neutrino lifetime

Earth

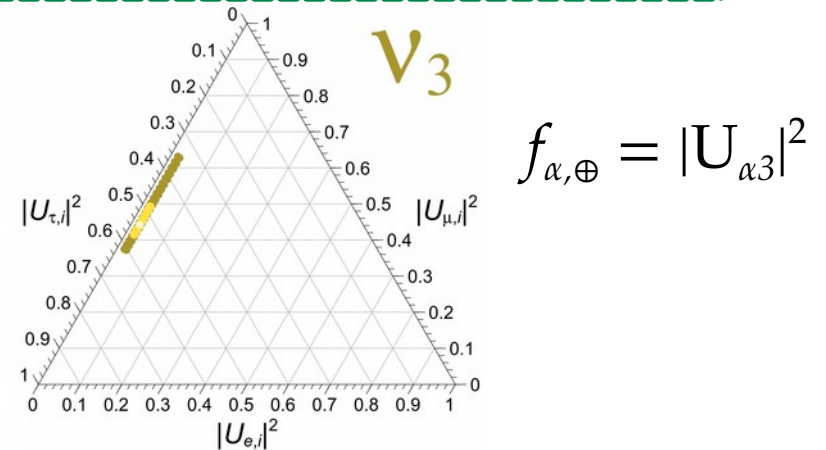
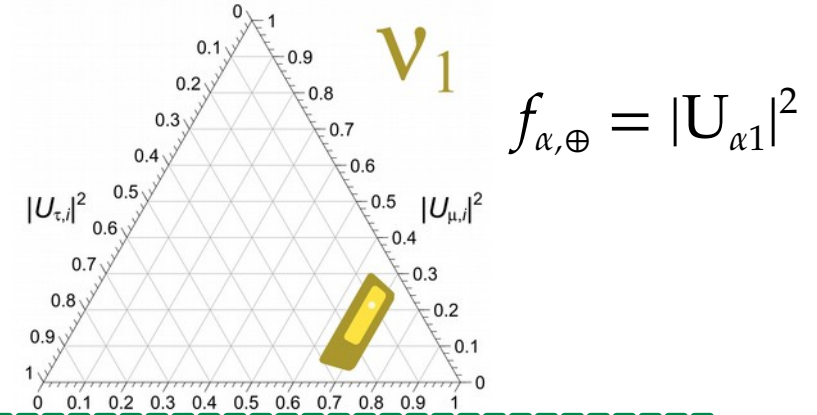
Sources

$\nu_2, \nu_3 \rightarrow \nu_1$   
 $\nu_1$  lightest and stable



Decay rate depends on  $\exp[-t / (\gamma\tau_i)] = \exp[-(L/E) \cdot (m_i/\tau_i)]$

$\nu_1, \nu_2 \rightarrow \nu_3$   
 $\nu_3$  lightest and stable



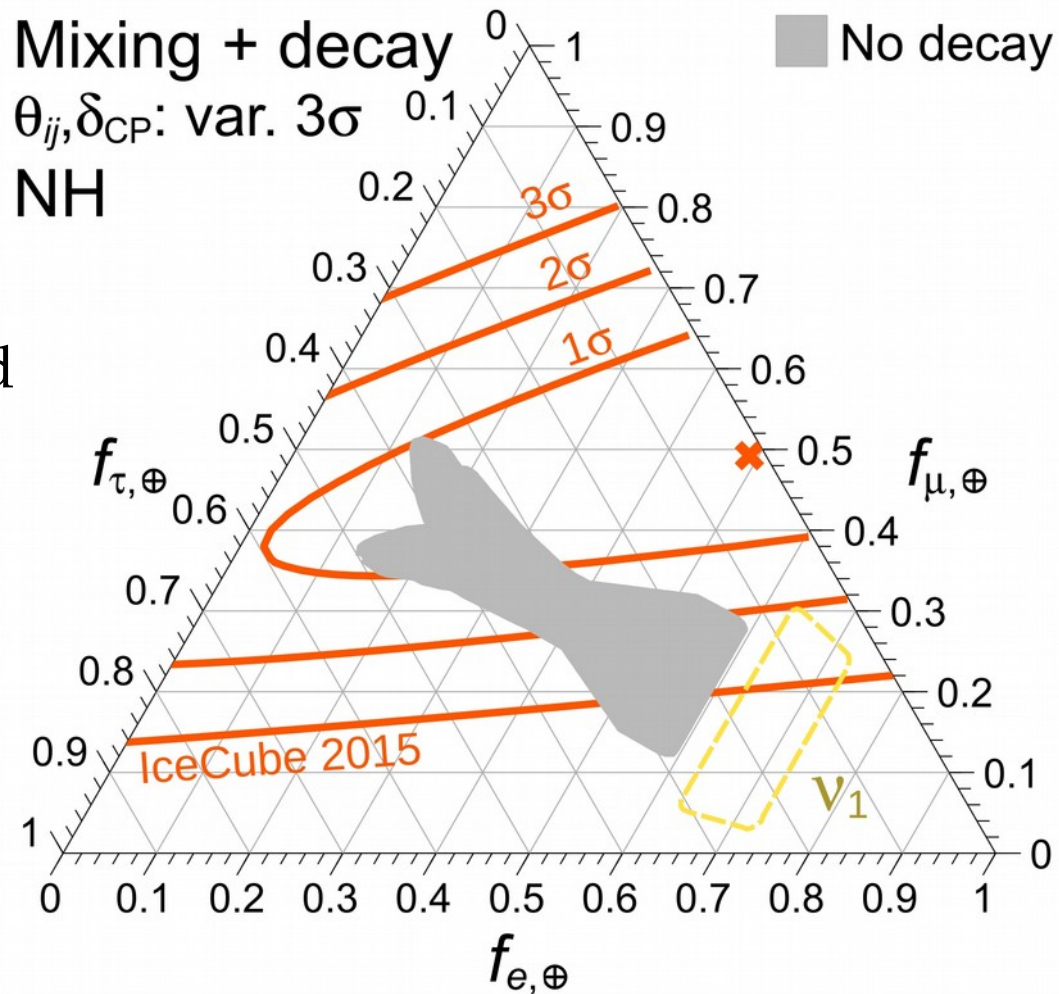
# Measuring the neutrino lifetime

Find the value of  $D$  so that decay is complete, *i.e.*,  $f_{\alpha,\oplus} = |U_{\alpha 1}|^2$ , for

- ▶ Any value of mixing parameters; and
- ▶ Any flavor ratios at the sources

(Assume equal lifetimes of  $\nu_2, \nu_3$ )

MB, Beacom, Murase, *PRD* 2017  
Baerwald, MB, Winter, *JCAP* 2012



# Measuring the neutrino lifetime

Fraction of  $\nu_2, \nu_3$  remaining at Earth

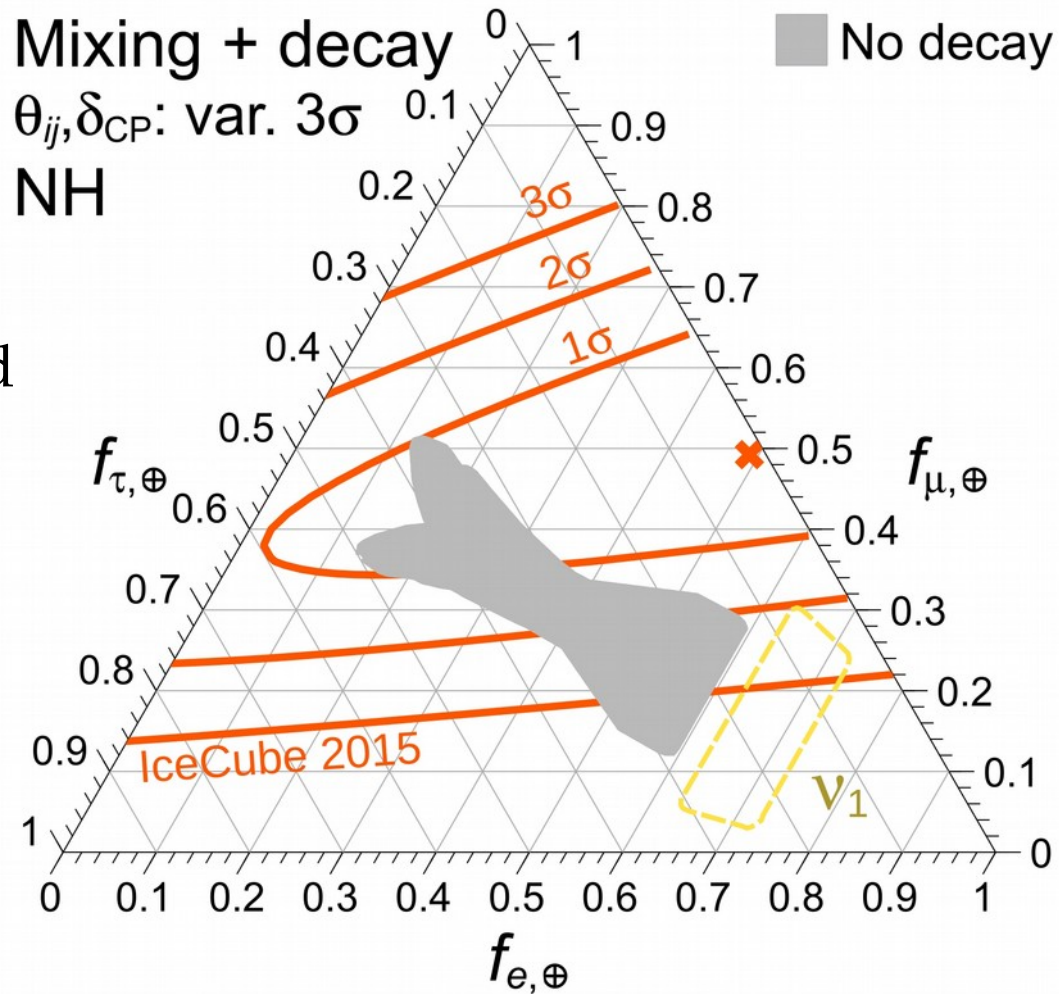


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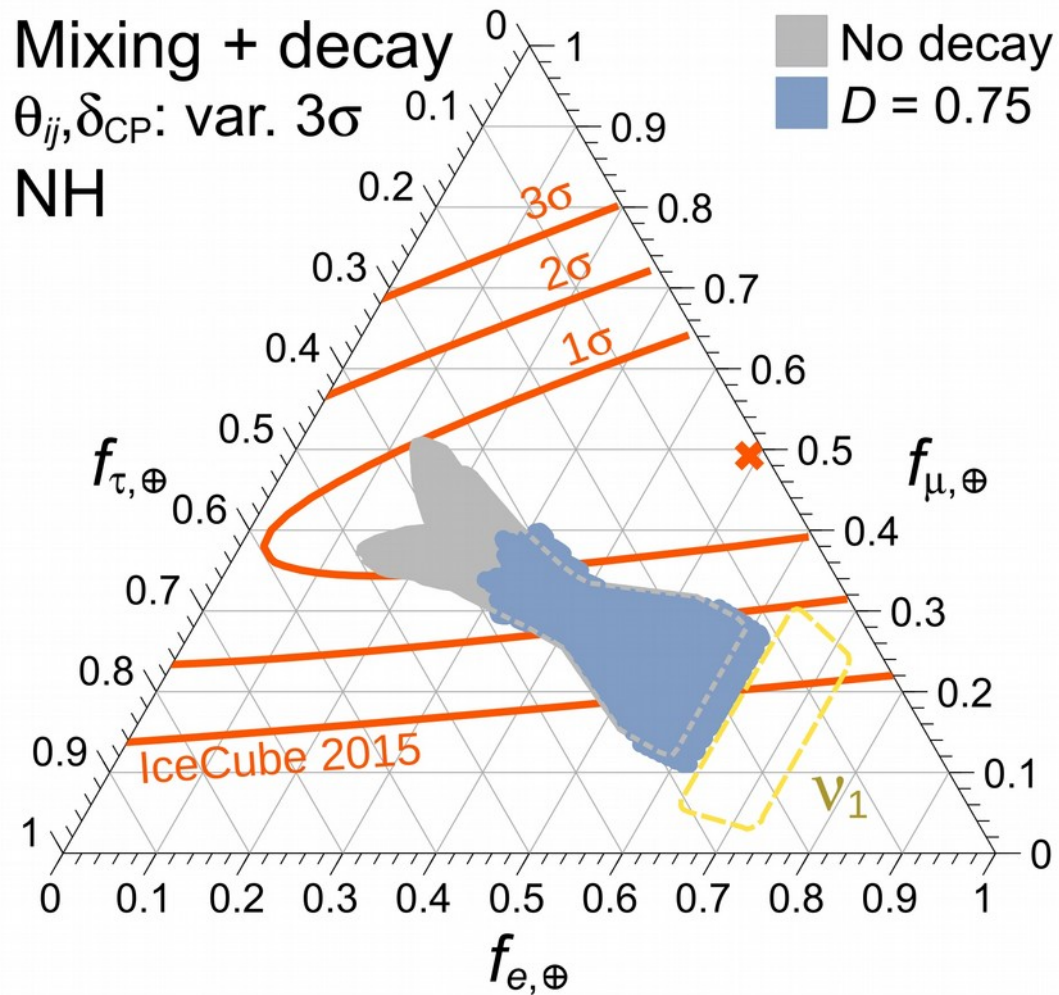


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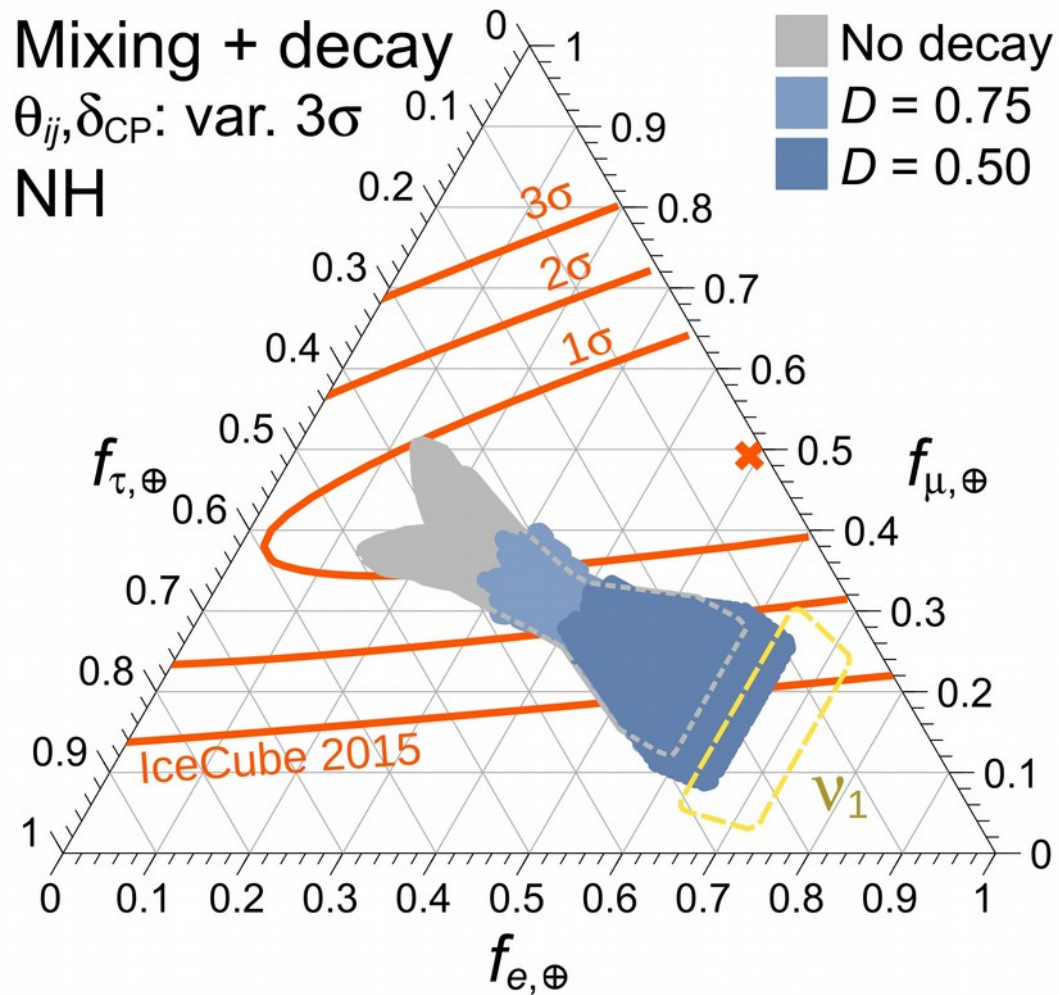


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# Measuring the neutrino lifetime

Fraction of  $\nu_2, \nu_3$  remaining at Earth

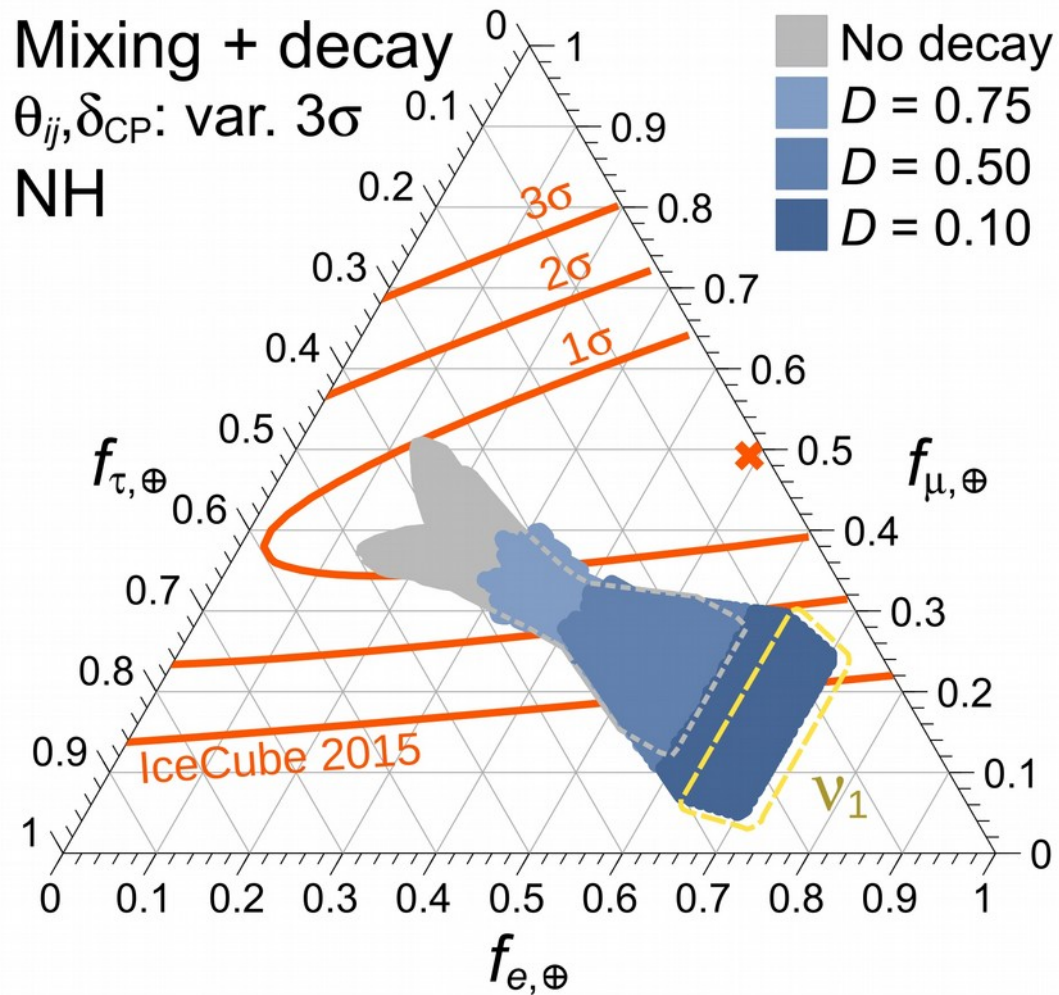


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# Measuring the neutrino lifetime

Fraction of  $\nu_2, \nu_3$  remaining at Earth

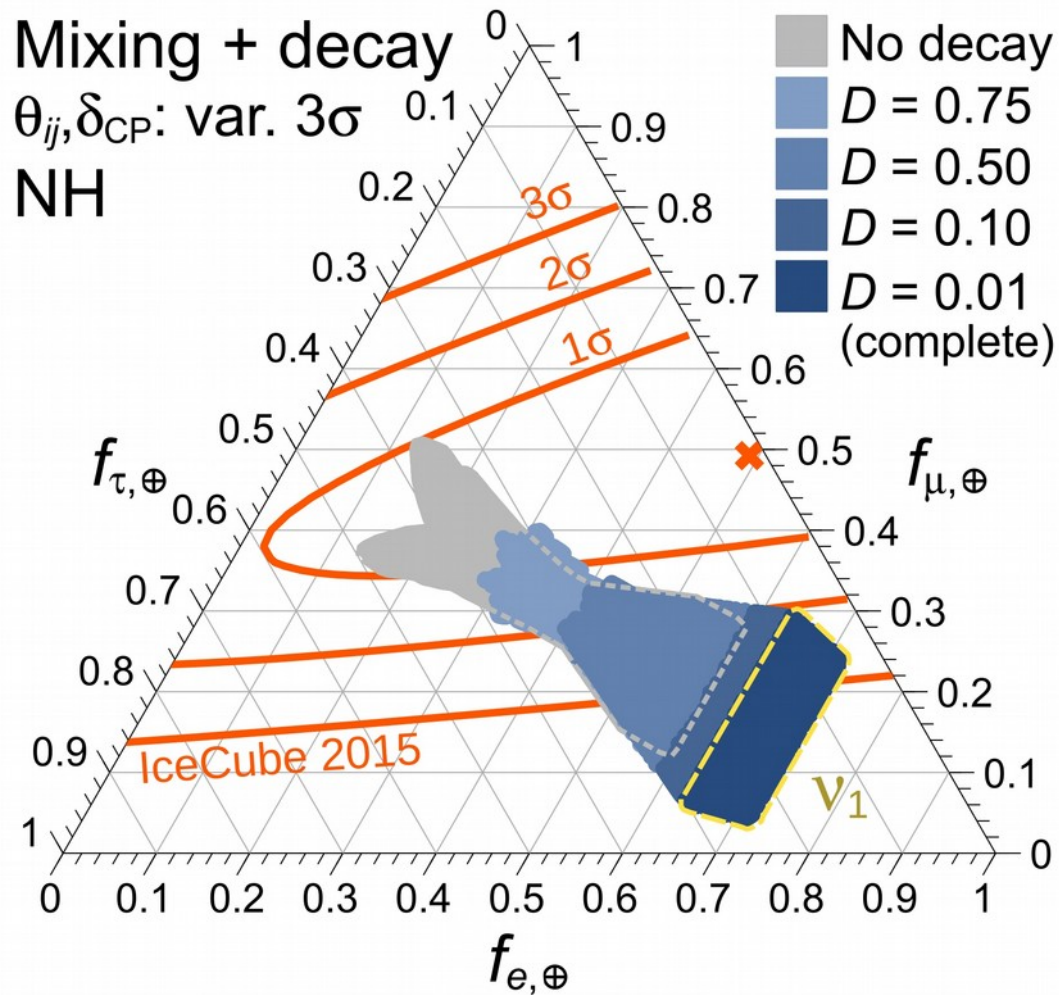


Find the value of  $D$  so that decay is complete, *i.e.*,  $f_{\alpha,\oplus} = |U_{\alpha 1}|^2$ , for

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MB, Beacom, Murase, *PRD* 2017  
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# Measuring the neutrino lifetime

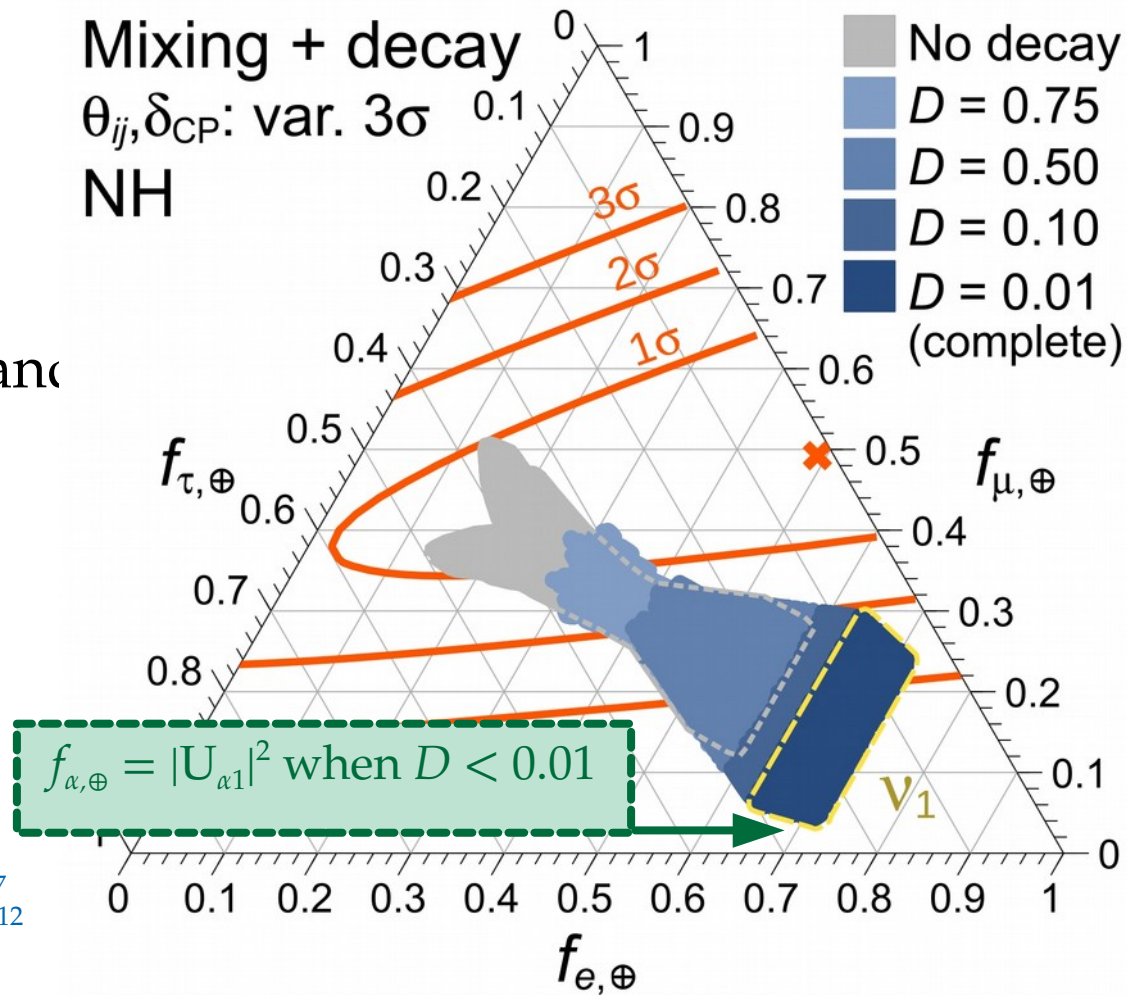
Fraction of  $\nu_2, \nu_3$  remaining at Earth



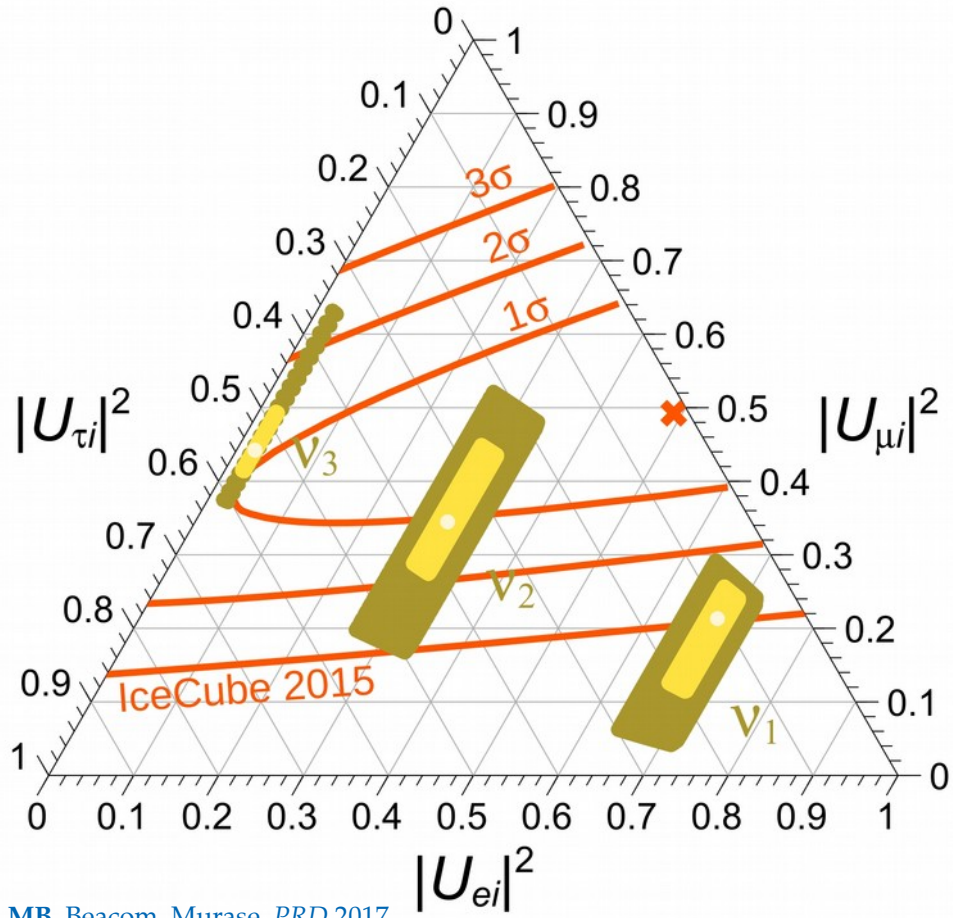
Find the value of  $D$  so that decay is complete, *i.e.*,  $f_{\alpha,\oplus} = |U_{\alpha 1}|^2$ , for

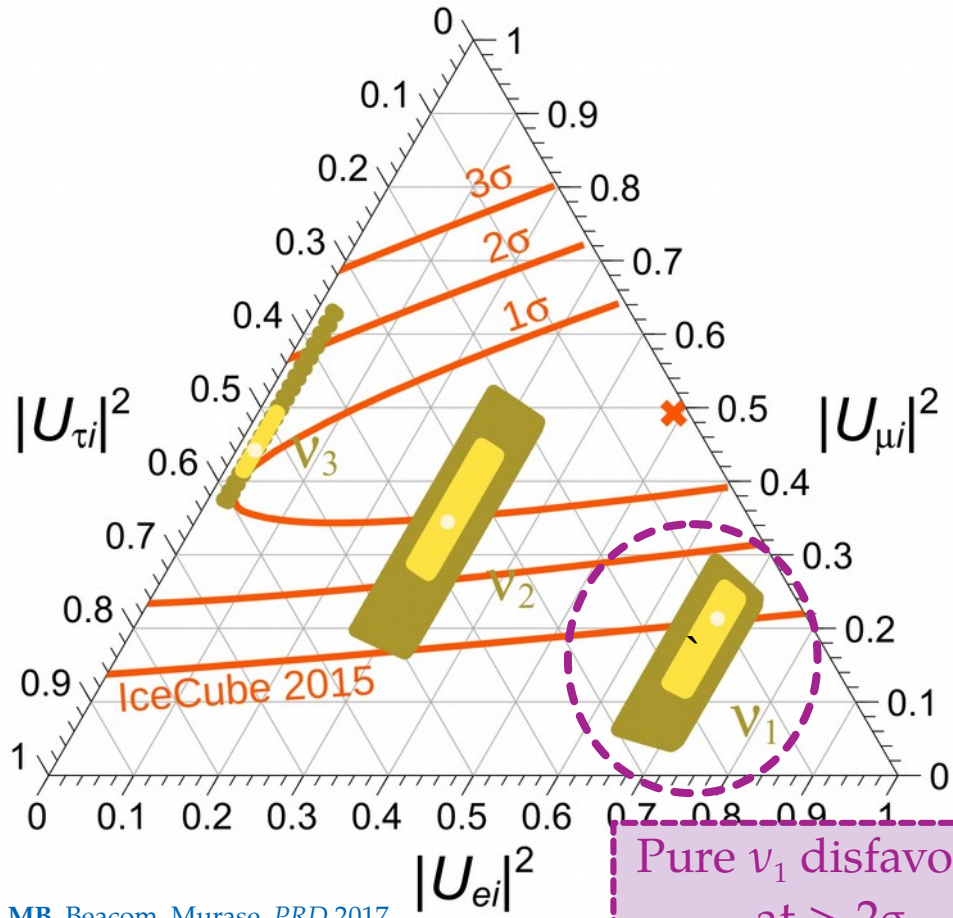
- Any value of mixing parameters; and
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(Assume equal lifetimes of  $\nu_2, \nu_3$ )

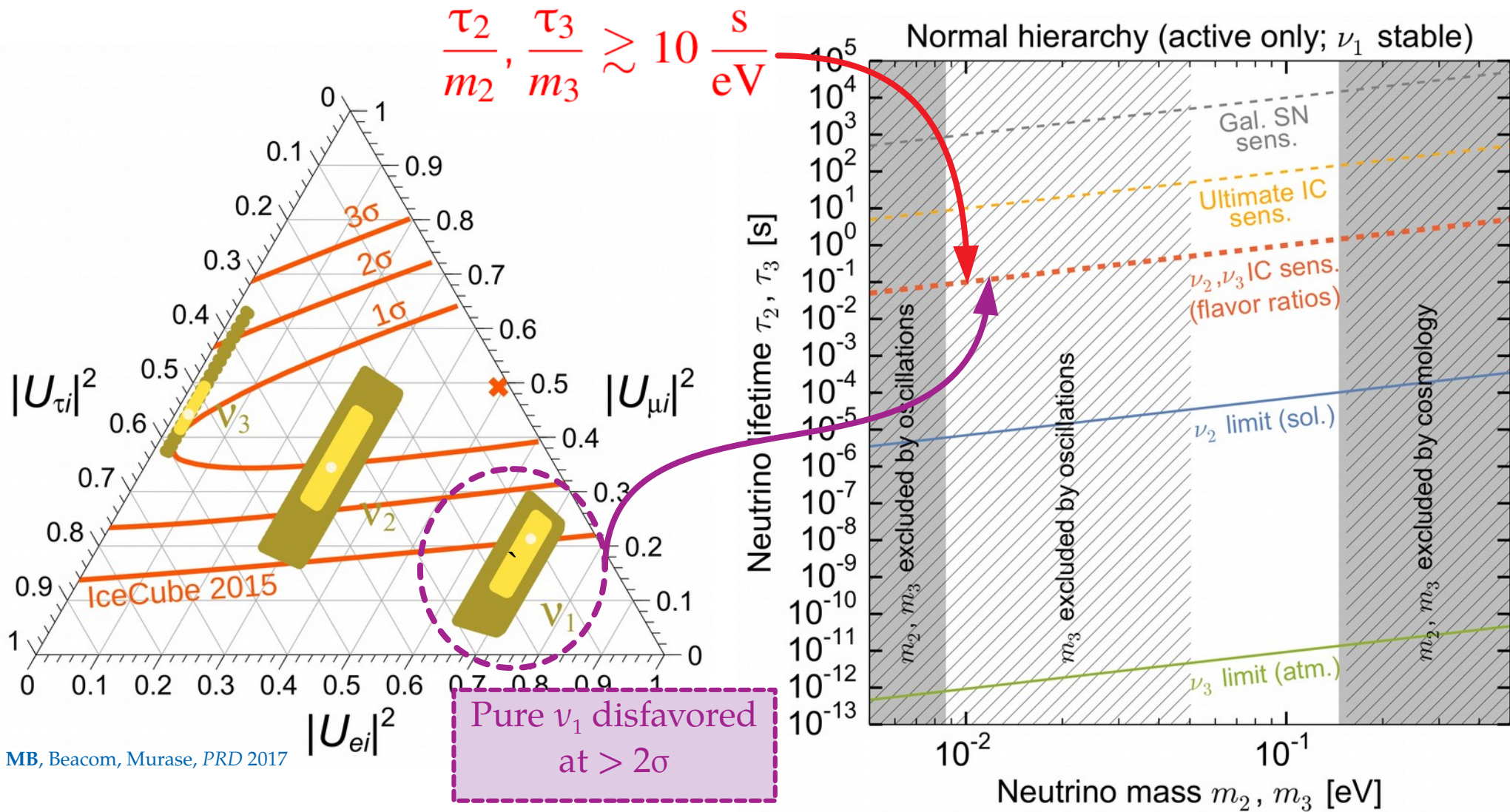






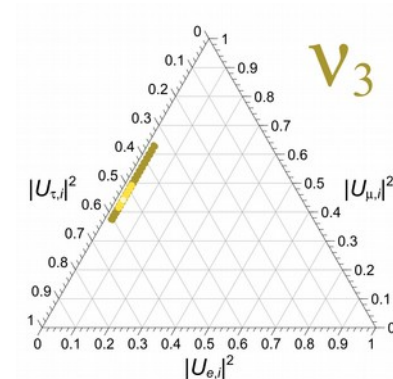
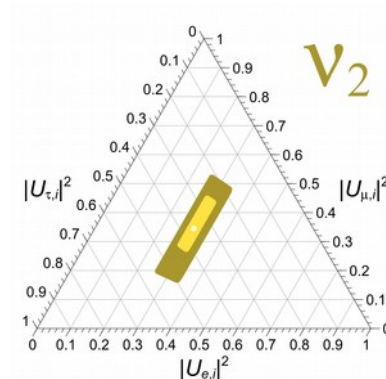
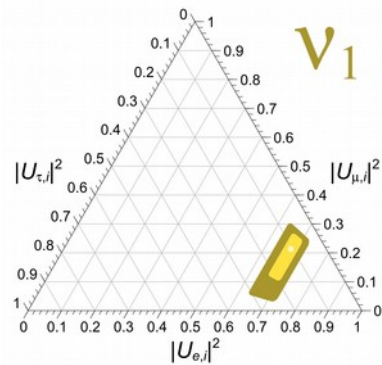






# Two classes of new physics

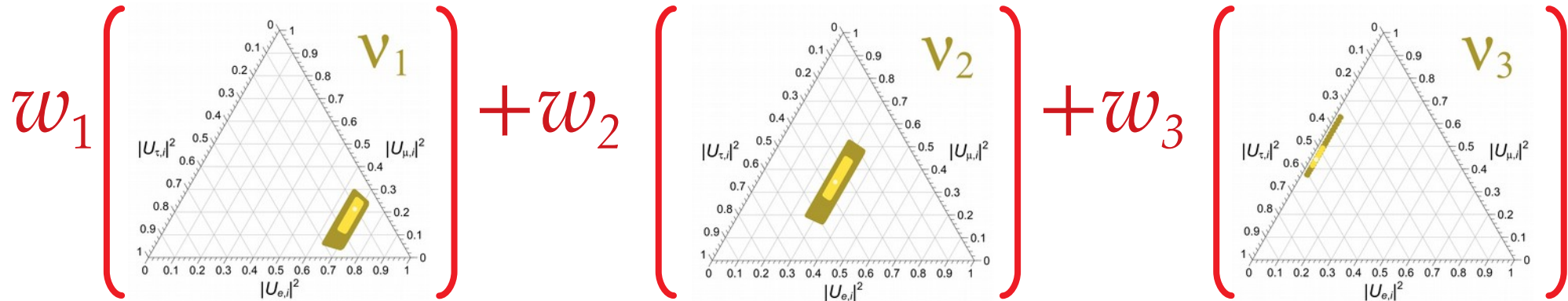
- ▶ Neutrinos propagate as an incoherent mix of  $\nu_1, \nu_2, \nu_3$
- ▶ Each one has a different flavor content:



- ▶ Flavor ratios at Earth are the result of their **combination**
- ▶ New physics may:
  - ▶ Only reweigh the proportion of each  $\nu_i$  reaching Earth (*e.g.*,  $\nu$  decay)
  - ▶ Redefine the propagation states (*e.g.*, Lorentz-invariance violation)

# Two classes of new physics

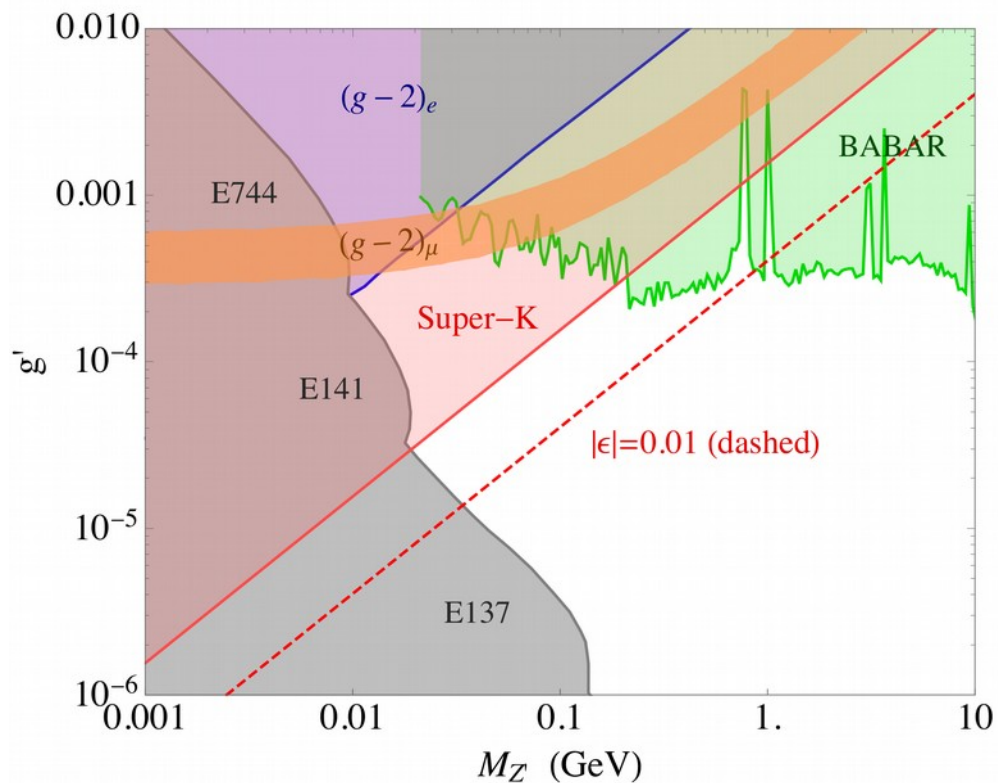
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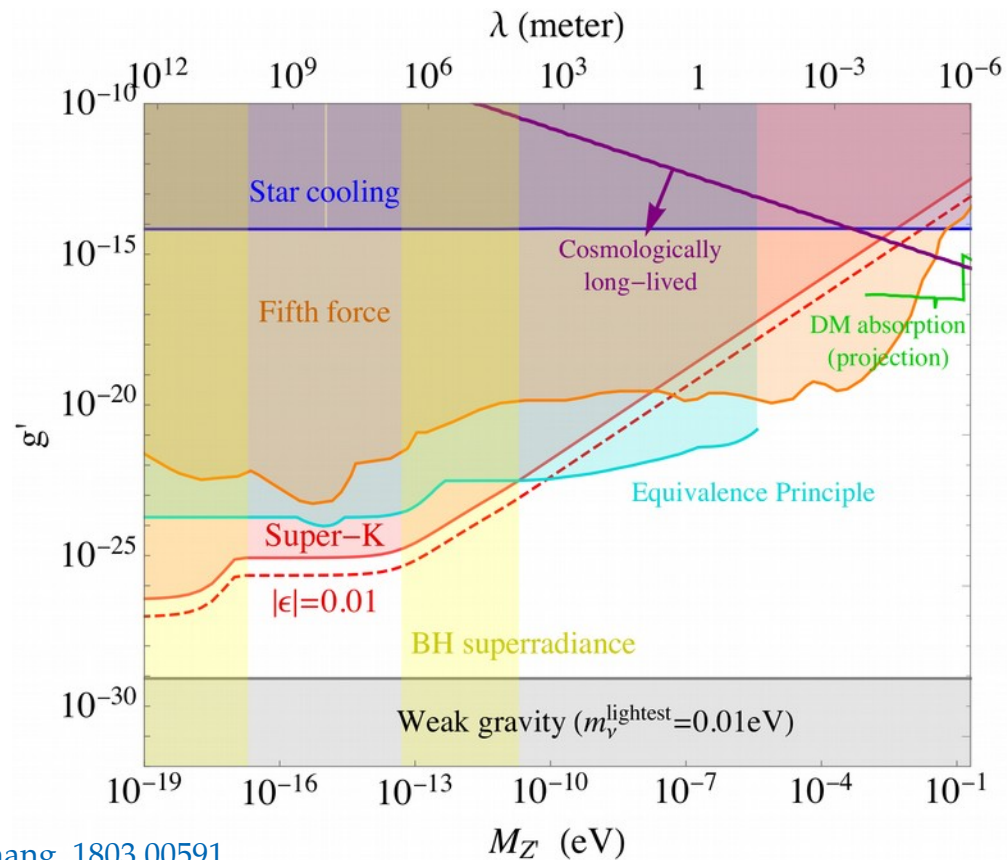
# Current limits on the $Z'$

MeV–GeV masses



M. Wise & Y. Zhang, 1803.00591

Sub-eV masses





# Connecting flavor-ratio predictions to experiment

- 1 Integrate potential in redshift, weighed by source number density  
→ Assume star formation rate

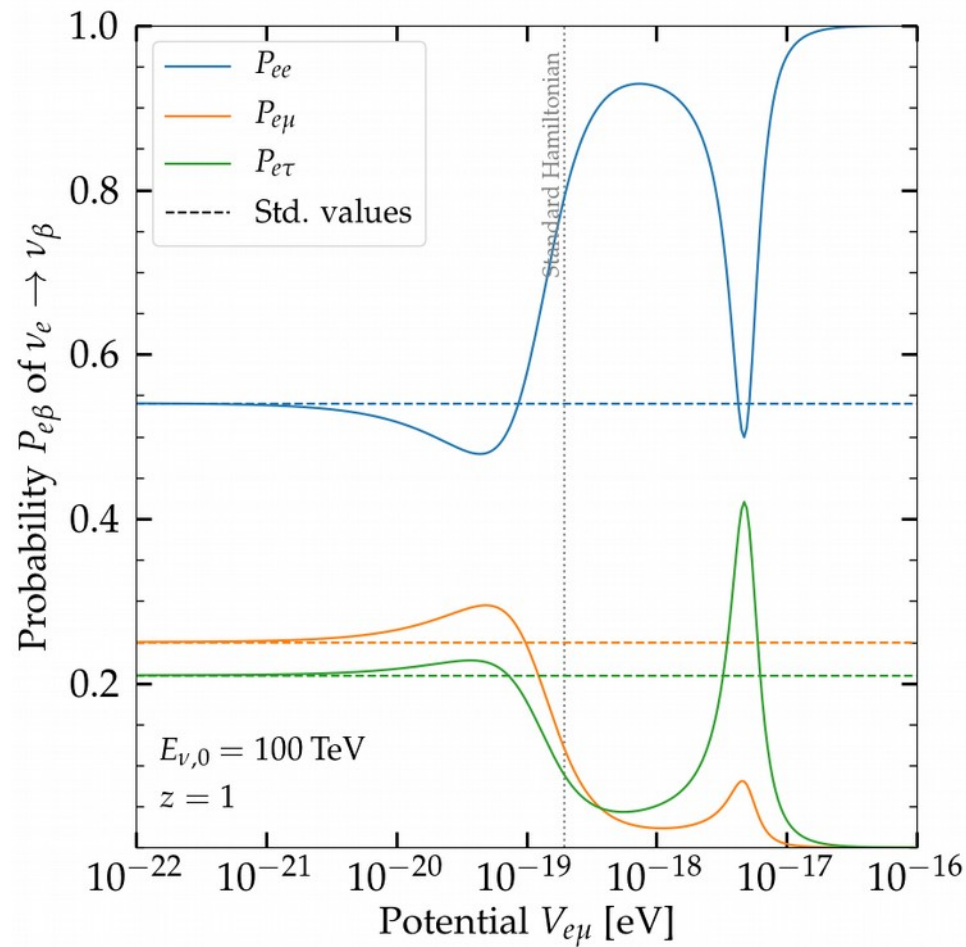
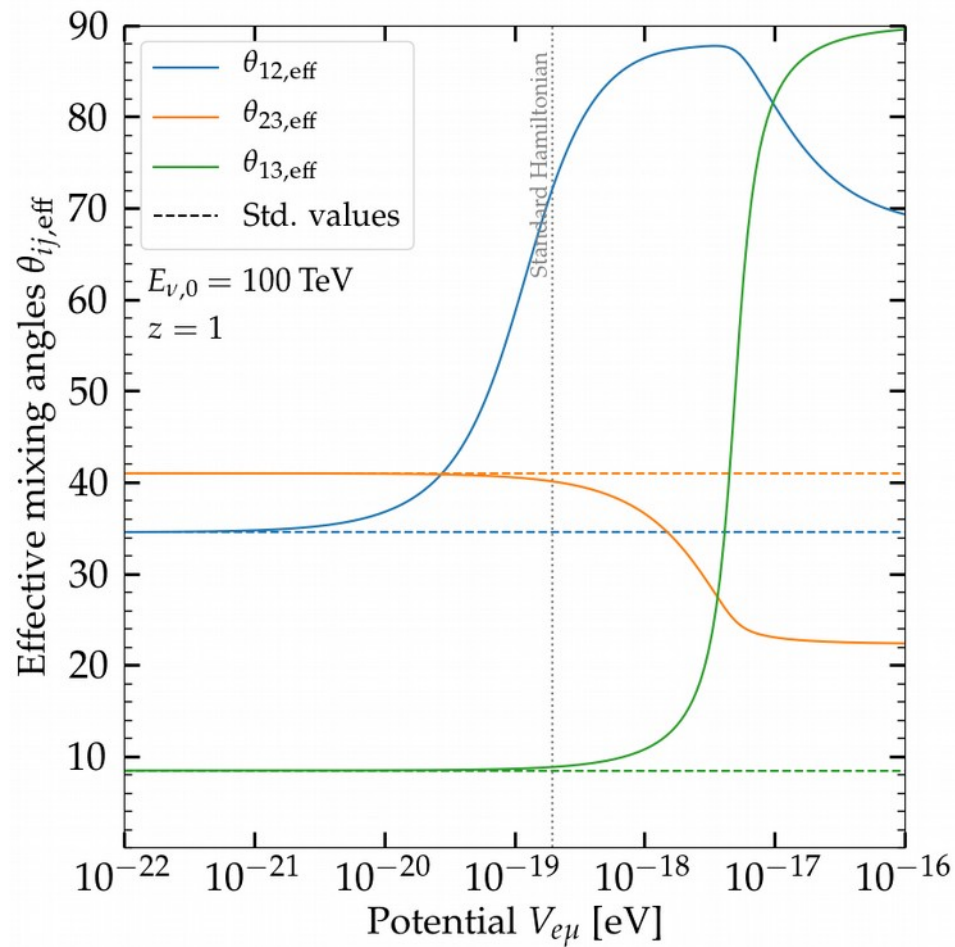
$$\langle V_{e\beta}^{\text{cos}} \rangle \propto \int dz \, \rho_{\text{SFR}}(z) \cdot \frac{dV_c}{dz} \cdot V_{e\beta}^{\text{cos}}(z)$$

Density of cosmological  $e$  grows with  $z$

- 2 Convolve flavor ratios with observed neutrino energy spectrum  
→ Either  $E^{-2.50}$  (combined analysis) or  $E^{-2.13}$  (through-going muons)

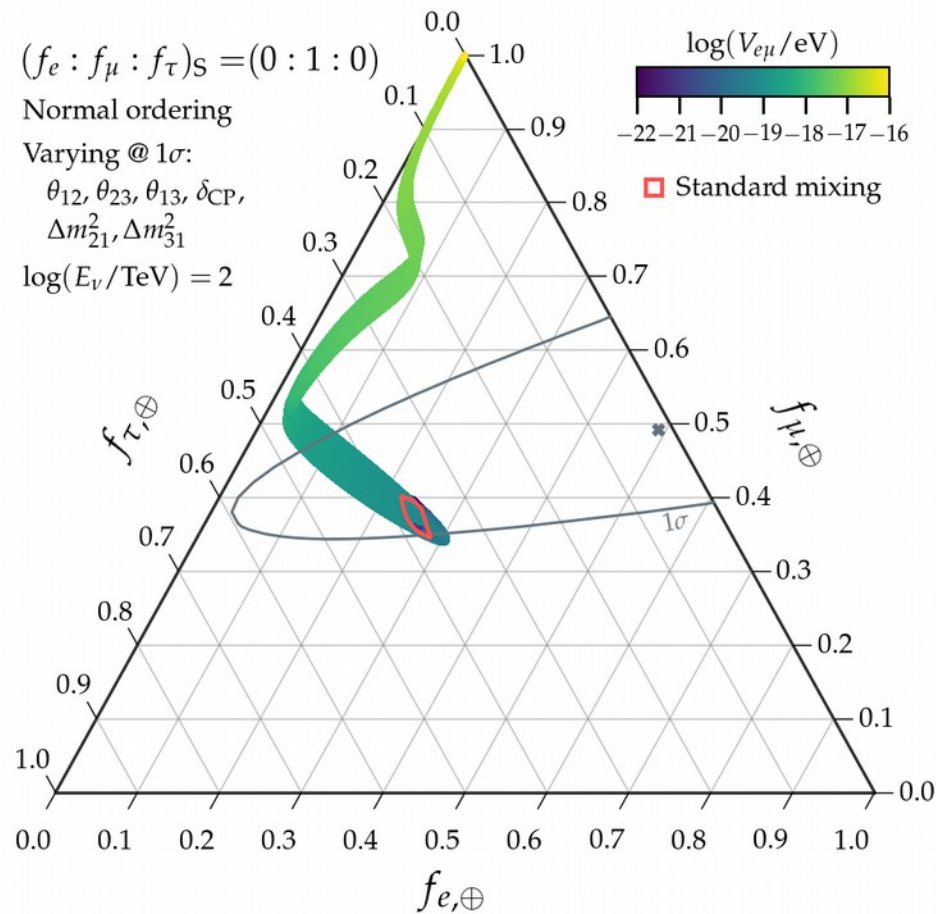
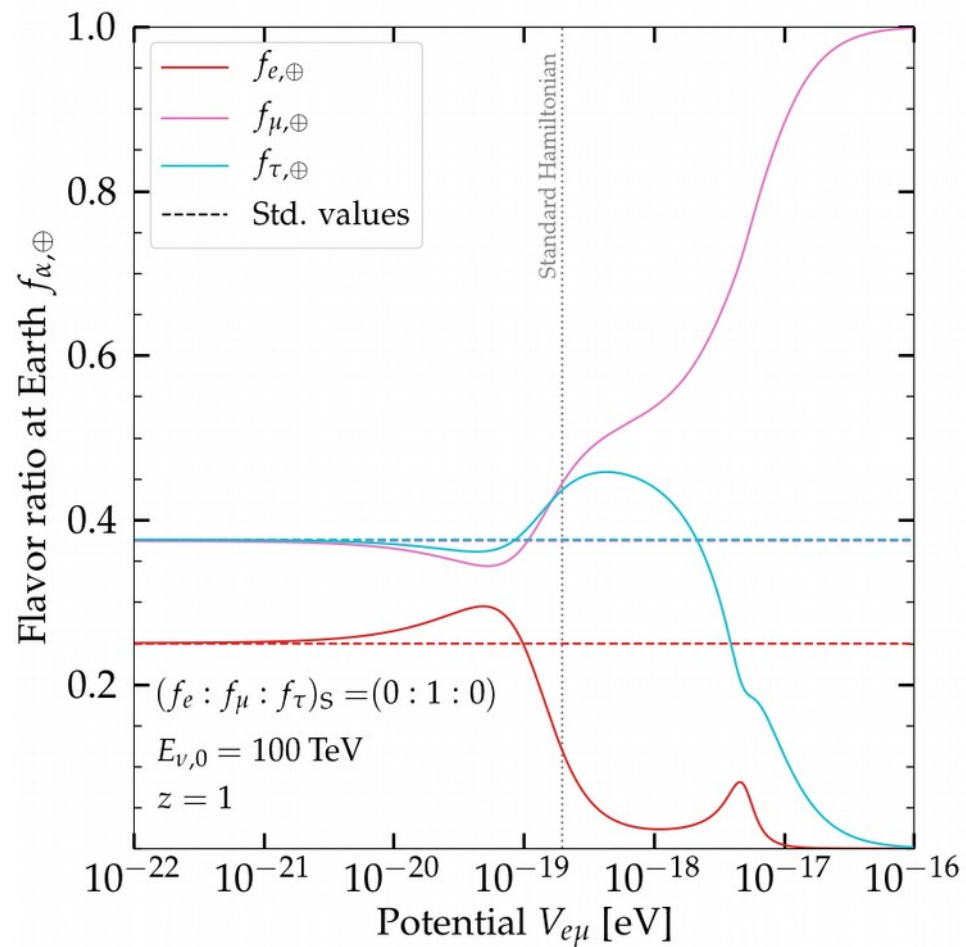
$$\underbrace{\langle \Phi_\alpha \rangle \propto \int dE_\nu \, f_{\alpha,\oplus}(E_\nu) \, E_\nu^{-\gamma}}_{\text{Energy-averaged flux}} \Rightarrow \underbrace{\langle f_{\alpha,\oplus} \rangle \equiv \frac{\langle \Phi_\alpha \rangle}{\sum_{\beta=e,\mu,\tau} \langle \Phi_\beta \rangle}}_{\text{Energy-averaged flavor ratios}}$$

# Resonance due to the $L_e$ - $L_\mu$ symmetry



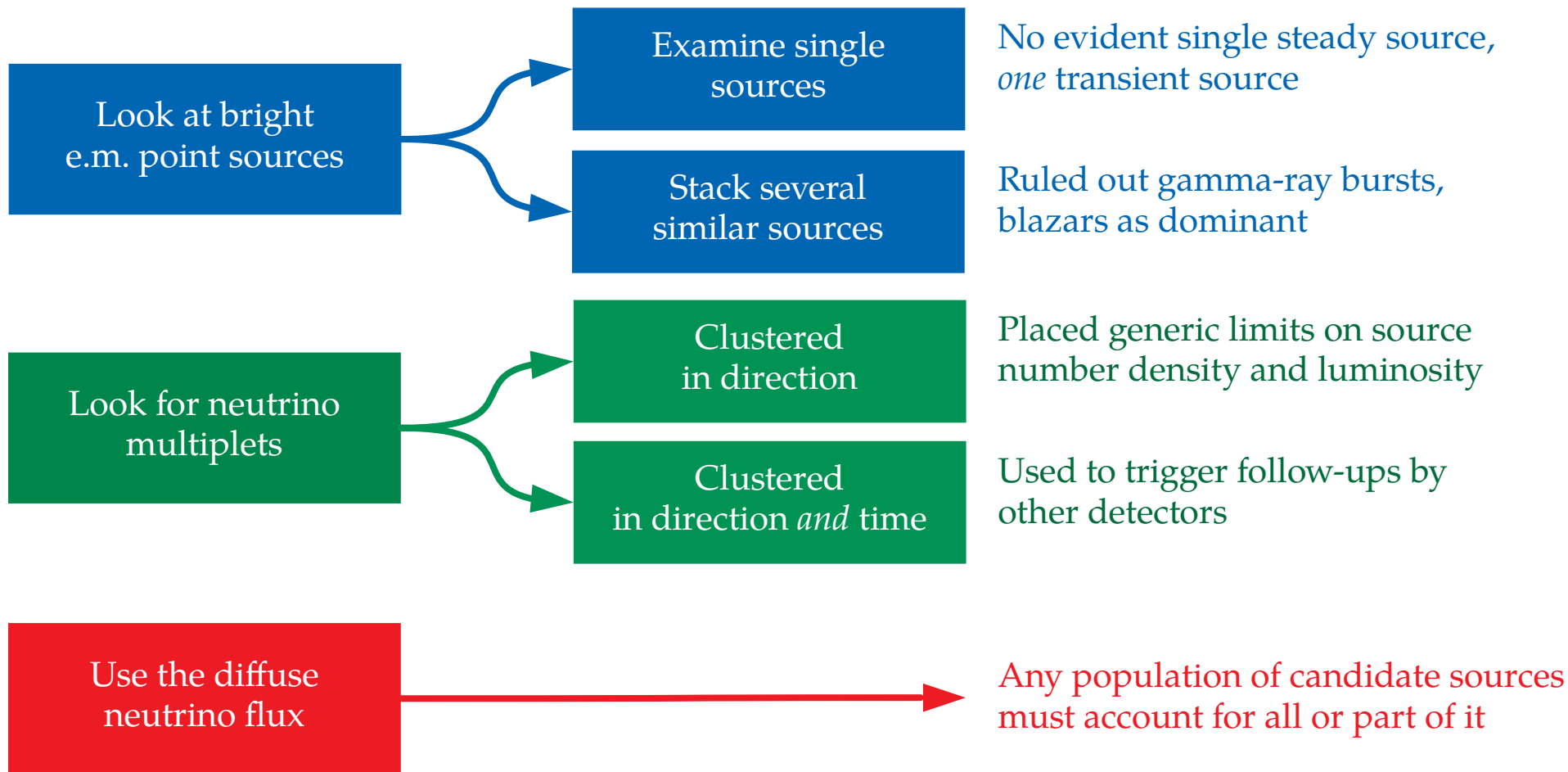


# Resonance due to the $L_e$ - $L_\mu$ symmetry (*cont.*)



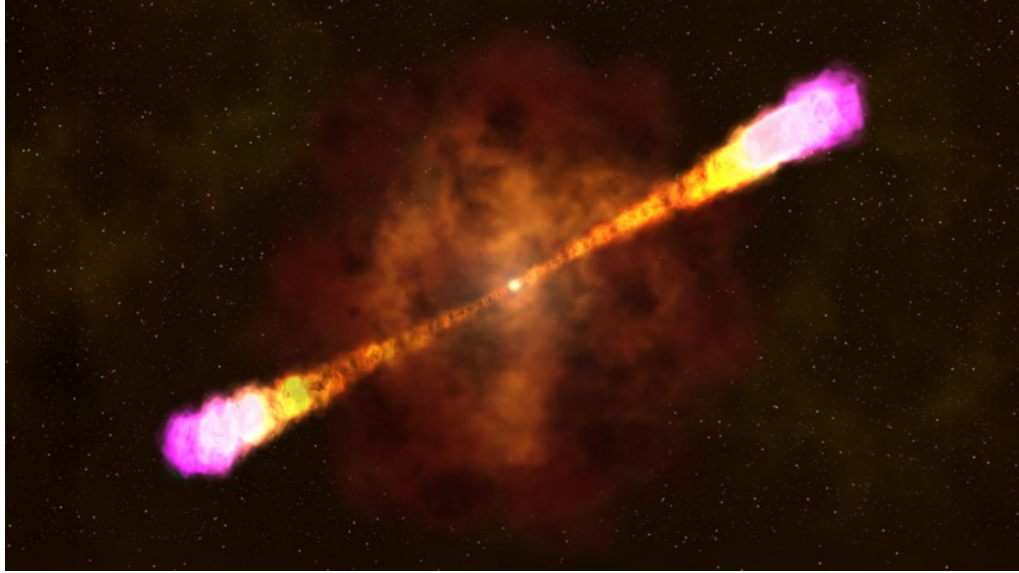
Looking for the sources

# Three Strategies to Reveal Sources Using TeV–PeV $\nu$



# Gamma-ray bursts and blazars – *not* dominant

Gamma-ray bursts

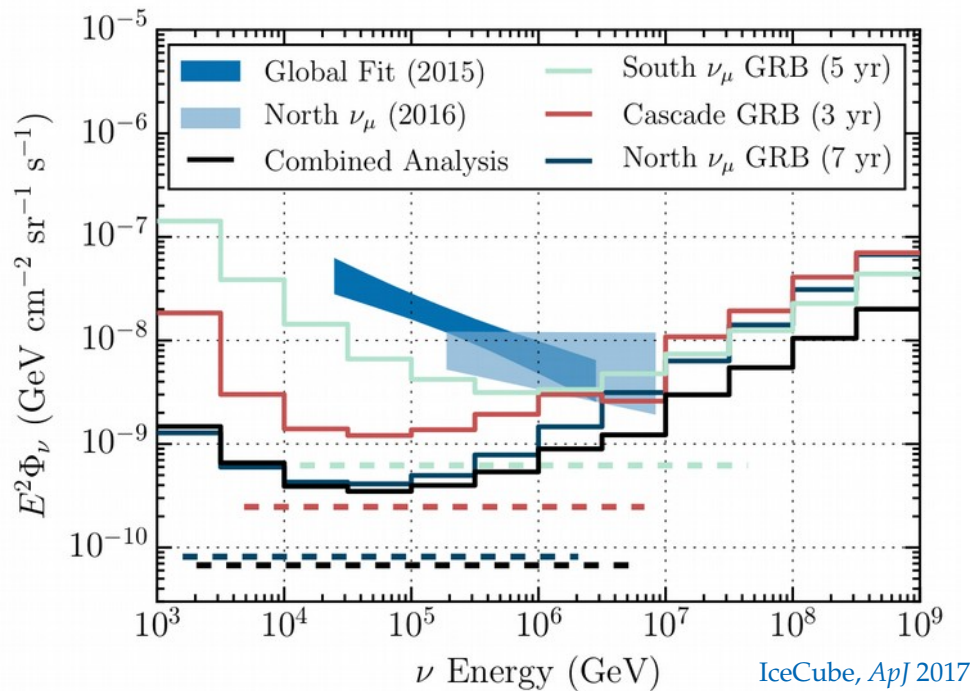


Blazars



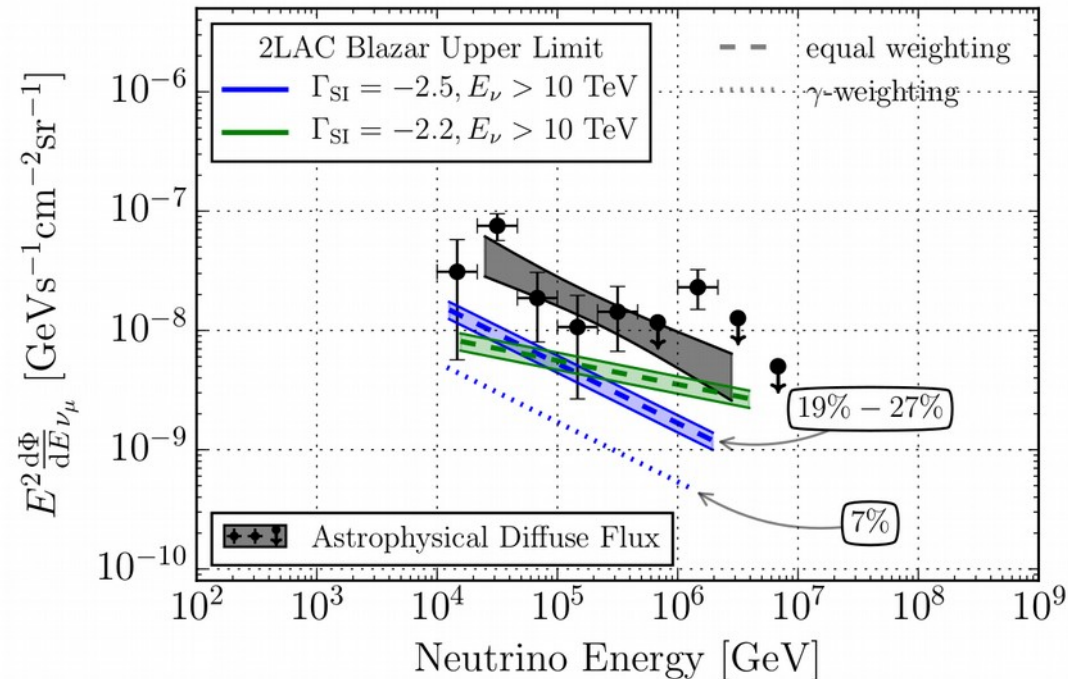
# Gamma-ray bursts and blazars – *not* dominant

## Gamma-ray bursts



1172 GRBs inspected, no correlation found  
< 1% contribution to diffuse flux

## Blazars



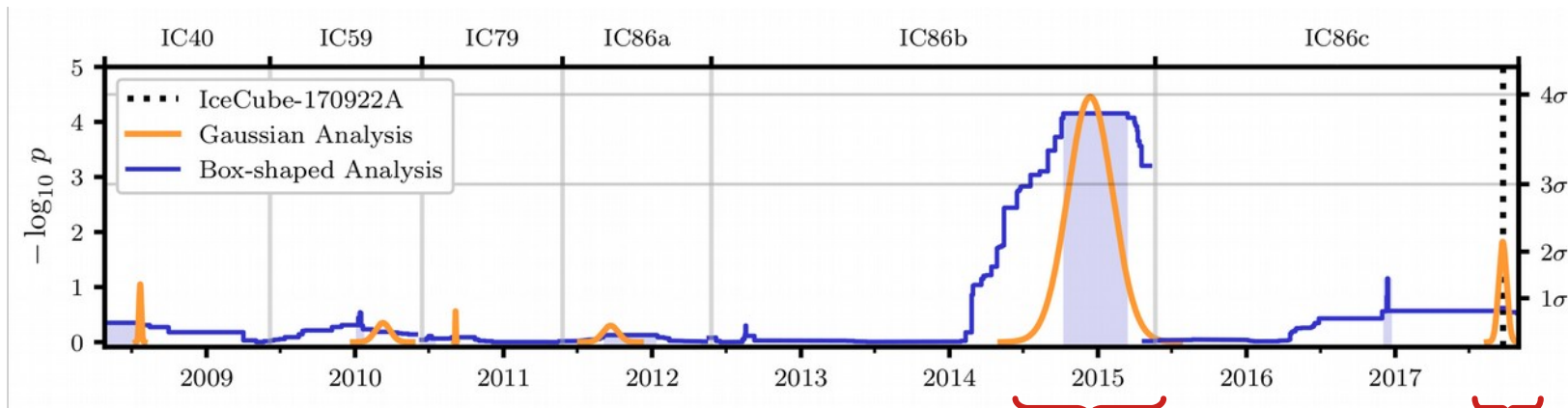
862 blazars inspected, no correlation found  
< 27% contribution to diffuse flux



... but we have seen *one* blazar neutrino flare!

Recent news:  
The starburst Seyfert galaxy NGC 1068 is also a potential neutrino source candidate (1908.05993)

Blazar TXS 0506+056:



Important:

If every blazar produced neutrinos as TXS 0506+056, the diffuse neutrino flux would be 20x higher than observed!

2014–2015:  $13 \pm 5$   $\nu$  flare, no X-ray flare  
3.5 $\sigma$  significance of correlation (post-trial)

2017: one 290-TeV  $\nu$  + X-ray flare  
1.4 $\sigma$  significance of correlation

Combined (pre-trial): 4.1 $\sigma$

Hard fluence:  $E^2 J_{100} = 2.1^{+0.9}_{-0.7} \left( \frac{E}{100 \text{ TeV}} \right)^{-2.1 \pm 0.2} \text{ TeV cm}^{-2}$

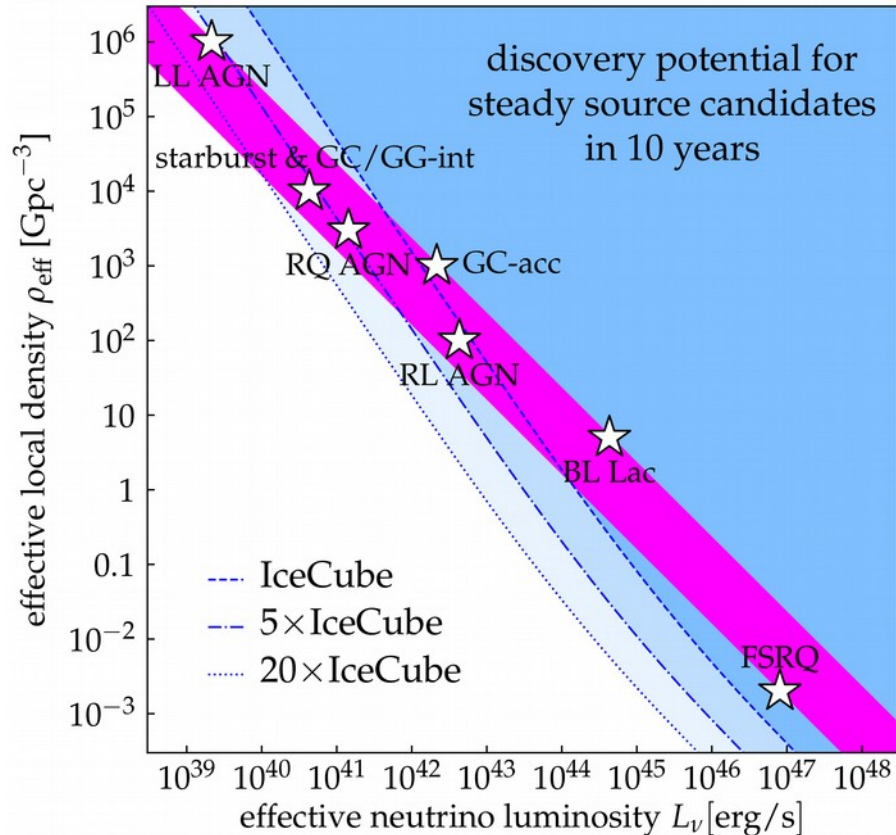
Joint modeling of the two periods is challenging; see ICRC 2019 talk by Walter Winter



# Source discovery potential: today and in the future

Accounts for the observed diffuse  $\nu$  flux (lower/upper edge: rapid/no redshift evolution)

Closest source with  $E^2\Phi_{\nu_\mu+\bar{\nu}_\mu} = 10^{-12} \text{ TeV cm}^{-2} \text{ s}^{-1}$



Closest source with  $E^2F_{\nu_\mu+\bar{\nu}_\mu} = 0.1 \text{ GeV cm}^{-2}$

