

Ultra-high-energy neutrinos and cosmic rays from gamma-ray bursts: exploring and updating the connections

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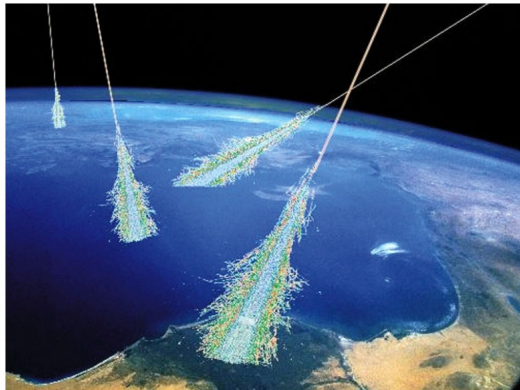
Promotionskolloquium
Würzburg, September 22, 2014



Two of the biggest mysteries –

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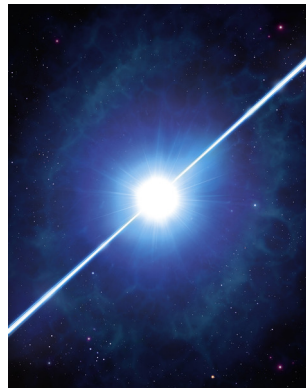
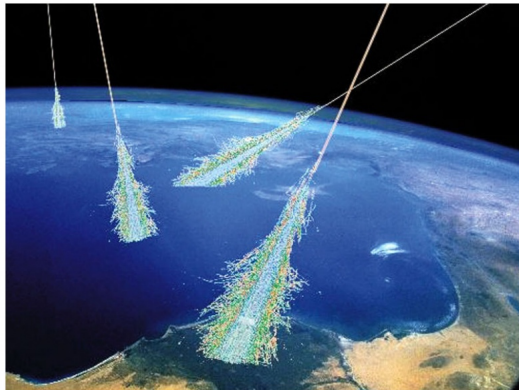
ultra-high-energy cosmic rays (UHECRs)



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gamma-ray bursts (GRBs)



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The mystery

We do not know the origin of UHECRs and GRBs

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GRBs are the sources of the UHECRs
– and neutrinos are the smoking gun

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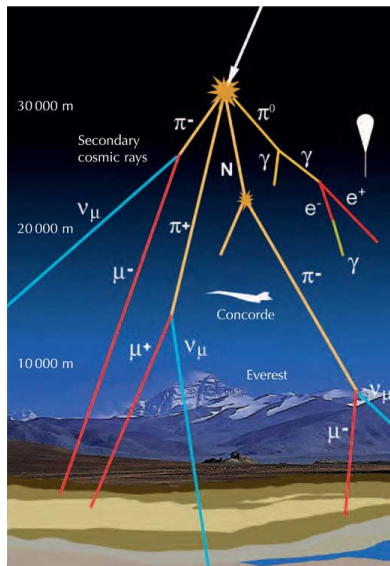
We do not know the origin of UHECRs and GRBs

Our hypothesis

GRBs are the sources of the UHECRs
– and neutrinos are the smoking gun

Our result

It is possible, *and testable*, but the connection between UHECRs, GRBs, and neutrinos is **not** as simple as we thought



1962: discovery of UHECRs at the Volcano Ranch Experiment, New Mexico



$> 10^{18}$ eV – most energetic particles in known Universe

(Fly's Eye experiment, Utah, 1991)

- ▶ a baseball (142 g) travelling at 94 km h^{-1} ; or
- ▶ a football (410 g) travelling at 55 km h^{-1} ,

...but concentrated in a volume of radius 1 fm $\equiv 10^{-15}$ m

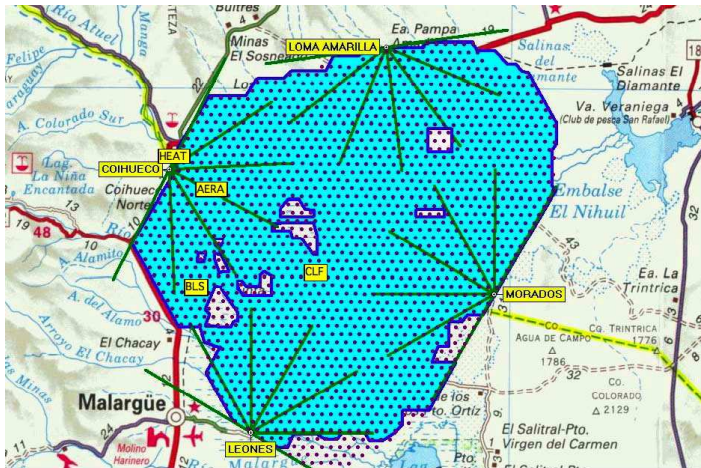
Approximate speed:

$$0.99999999999999999999999951c = (1 - 4.9 \cdot 10^{-24})c$$

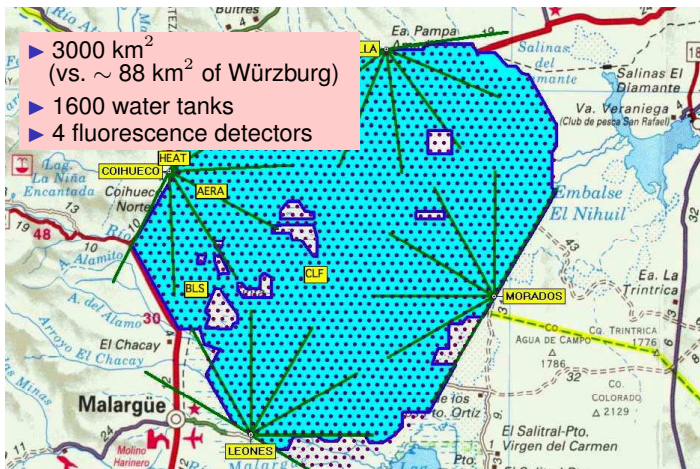
~ 40 million times higher than a 7 TeV proton at the LHC

They are *very* rare: only a few dozen observed so far

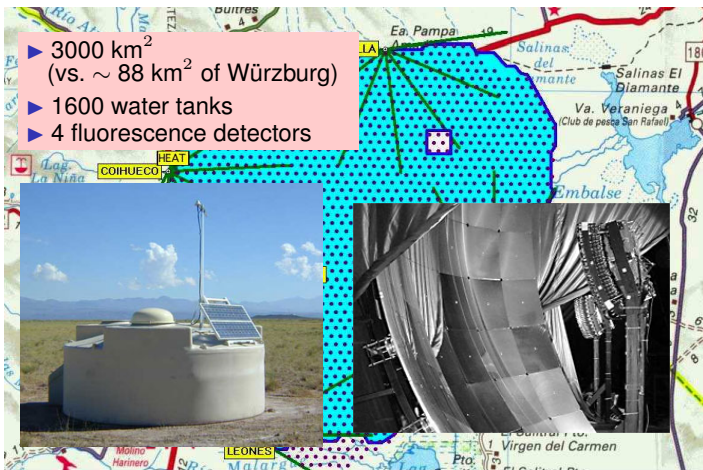
We now have much larger detectors
– *e.g.*, Pierre Auger Observatory, in Argentina



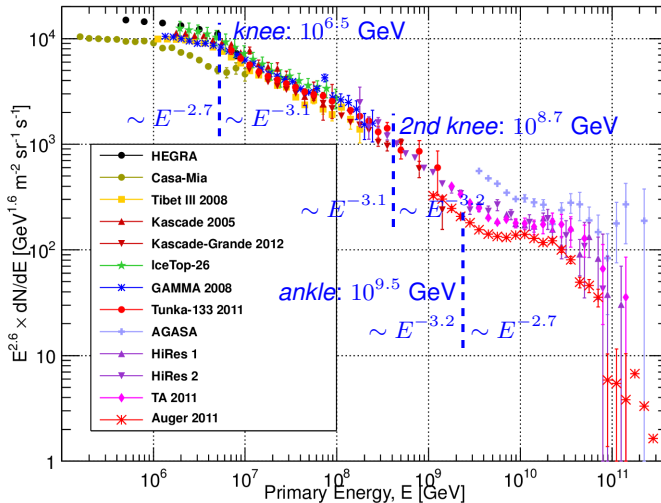
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After 102 years of the discovery of CRs, this is what we know –



THE ASTROPHYSICAL JOURNAL, **182**:L85–L88, 1973 June 1

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OBSERVATIONS OF GAMMA-RAY BURSTS OF COSMIC ORIGIN

RAY W. KLEBESADEL, IAN B. STRONG, AND ROY A. OLSON

University of California, Los Alamos Scientific Laboratory, Los Alamos, New Mexico

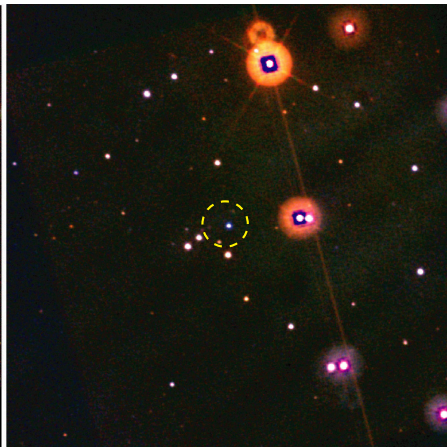
Received 1973 March 16; revised 1973 April 2

ABSTRACT

Sixteen short bursts of photons in the energy range 0.2–1.5 MeV have been observed between 1969 July and 1972 July using widely separated spacecraft. Burst durations ranged from less than 0.1 s to ~ 30 s, and time-integrated flux densities from $\sim 10^{-5}$ ergs cm^{-2} to $\sim 2 \times 10^{-4}$ ergs cm^{-2} in the energy range given. Significant time structure within bursts was observed. Directional information eliminates the Earth and Sun as sources.

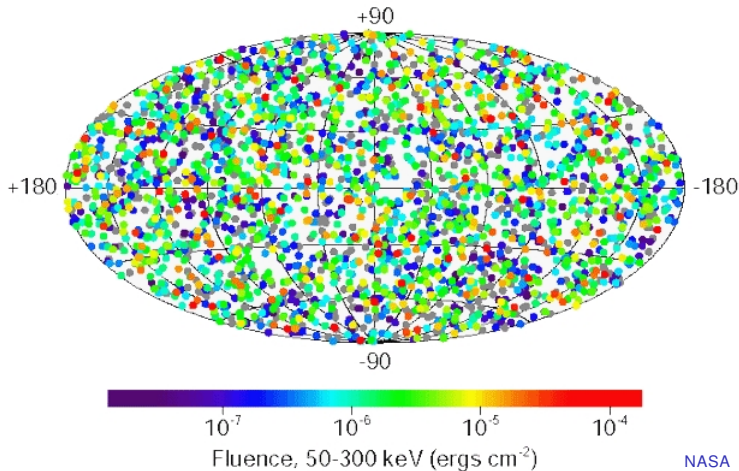
Subject headings: gamma rays — X-rays — variable stars

What does a GRB look like? *e.g.*, GRB060218 seen by *Swift*



SDSS, SWIFT COLLAB., SLOAN FOUNDATION, NSF, NASA

Dedicated missions were flown – *e.g.*, BATSE detected 2704 GRBs between 1991 and 2000



If the sources of UHECRs are extragalactic, they must satisfy:

- ① Sources should produce protons with a local ($z = 0$) energy injection input of $\approx 10^{44} \text{ erg Mpc}^{-3} \text{ yr}^{-1}$
- ② Density of sources should be $n_s > 10^{-4} \text{ Mpc}^{-3}$
- ③ Power output of individual sources should satisfy $L \gtrsim 10^{45.5} \text{ } \Gamma^2 \text{ erg s}^{-1}$
- ④ Plasma flows should be relativistic: $\Gamma \gtrsim 100 (\delta t / 10 \text{ ms})^{-1/4}$

This leaves as candidates:

- ▶ (some) AGN flares
- ▶ GRBs, with typical $L \sim 10^{52} \text{ erg s}^{-1}$, $\Gamma \gtrsim 300$

E. WAXMAN in *Astronomy at the Frontiers of Science*, SPRINGER (2011)

Why is *now* a good time to do this?

better, bigger detectors + loads of data + bright future

UHECRs



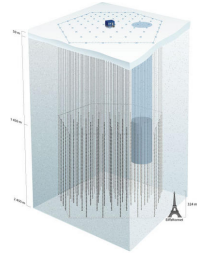
- ▶ Auger: 69 events > 57 EeV
- ▶ Telescope Array: 72 events
- ▶ surface + fluorescence
- ▶ from space: JEM-EUSO (?)
– $\times 10$ event rate

GRBs



- ▶ *Fermi*: ~ 250 GRBs yr^{-1}
in 8 keV – 40 MeV
- ▶ ~ 12 GRBs yr^{-1}
in 20 MeV – 300 GeV
- ▶ different wavelengths:
INTEGRAL, *Swift*
- ▶ 1000's GRBs detected so far

neutrinos

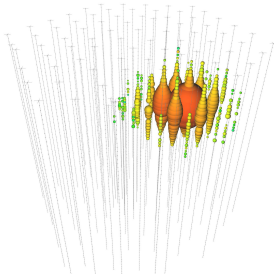


- ▶ IceCube: 1 km³ Antarctic ice
- ▶ detection: νN interactions
- ▶ sensitive to predicted UHE
astrophysical flux
- ▶ see sources after 10-15 yr?

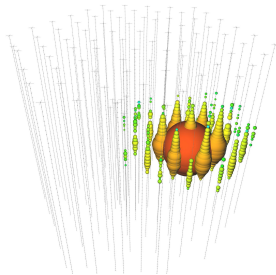
The era of neutrino astronomy has begun!

– IceCube (2010-2013) detected 37 events with 30 TeV – 2 PeV

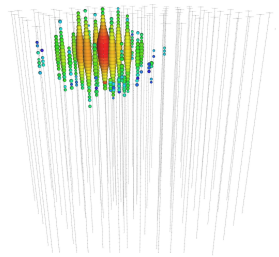
“Bert”, 1.04 PeV



“Ernie”, 1.14 PeV



“Big Bird”, 2 PeV

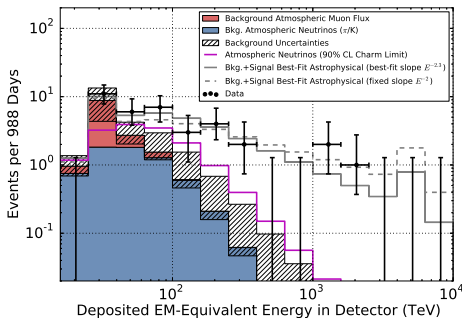


... and 34 more events < 385 TeV



The era of neutrino astronomy has begun!

– IceCube (2010-2013) detected 37 events with 30 TeV – 2 PeV



ICECUBE, *PRL* **111**, 021103 (2013)
ICECUBE, *Science* **342**, 1242856 (2013)
ICECUBE, *PRL* **113**, 101101 (2014)

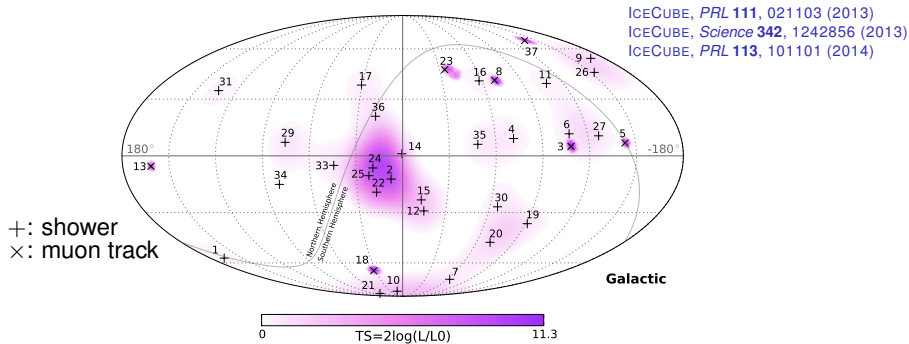
Flux compatible with extragalactic origin (Waxman & Bahcall 1997):

$$E^2 \Phi_\nu = (0.95 \pm 0.3) \times 10^{-8} \text{ GeV cm}^{-2} \text{ s}^{-1} \text{ sr}^{-1} \text{ (per flavour)}$$

The era of neutrino astronomy has begun!

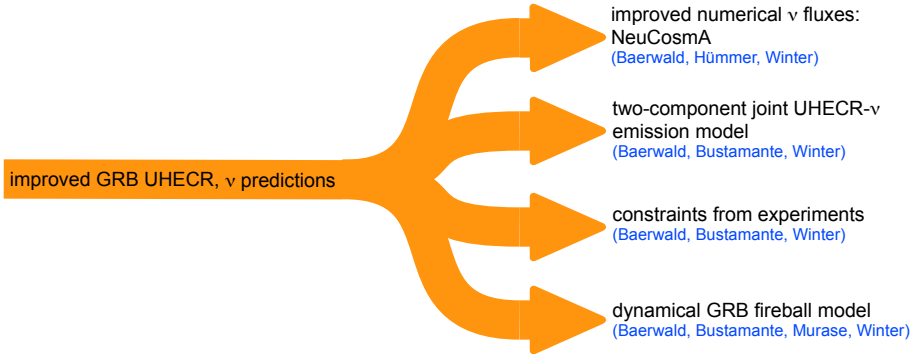
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Arrival directions compatible with an **isotropic** distribution –

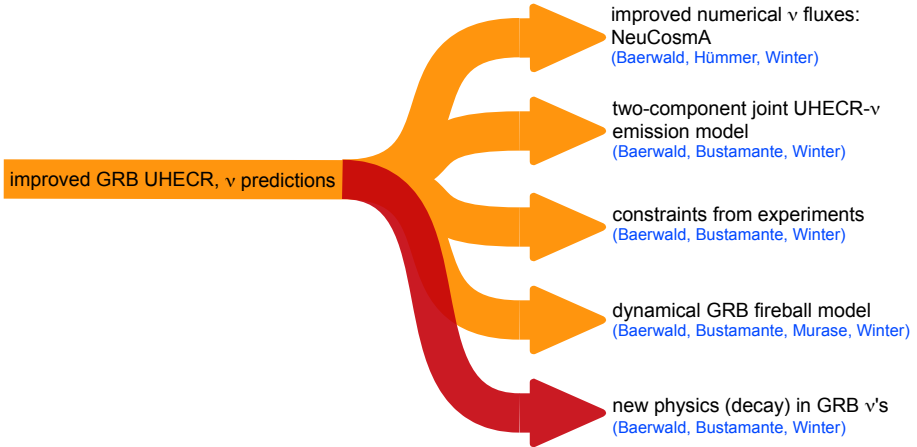


– no association with sources found **yet**

A four-pronged plan of attack –



A **five**-pronged plan of attack –



GRBs are among the best candidate sources for CRs *and* ν 's:

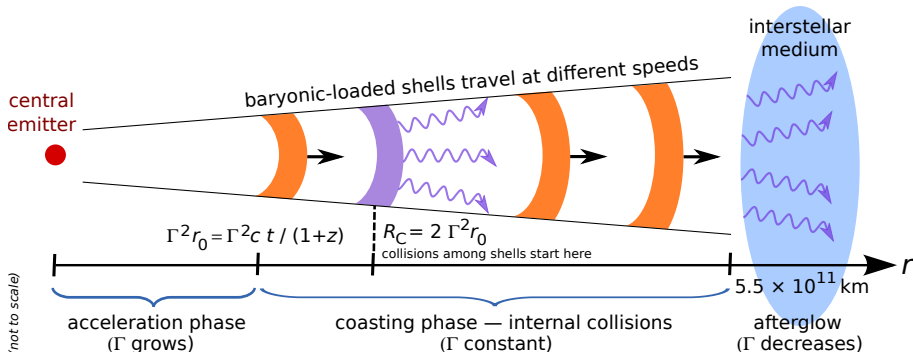
- ▶ radiated energy of $\sim 10^{52} - 10^{53}$ erg
- ▶ intense magnetic fields of $\sim 10^5$ G
- ▶ magnetically-confined p 's shock-accelerated to $\sim 10^{12}$ GeV
- ▶ plus: low backgrounds (for ν 's) due to small time window

Problem: experiments (IceCube, ANTARES) are starting to strongly constrain the simplest joint emission models

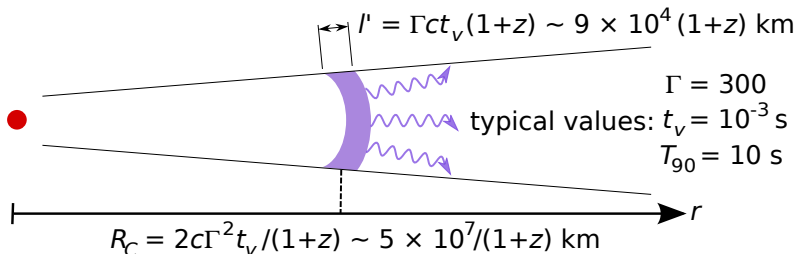
Solution: we need to build more realistic models!

Fireball model: our current paradigm of how a GRB works

- relativistically-expanding blobs of plasma collide with each other and, in the process, emit UHE particles



The **static** fireball picture: all collisions occur at the **same** radius



- ▶ *average* speed Γ inferred from afterglow observations
- ▶ “variability timescale” t_v measured from the light curve
- ▶ redshift z measured for the host galaxy

Static burst: made up of $T_{90}/t_v \sim 100 - 1000$ **identical** collisions

Joint production of UHECRs, ν 's, and γ 's:

power law $\sim E^{-\alpha p}$

broken power law

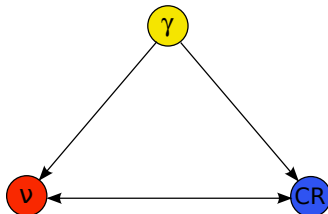
$$p \gamma \rightarrow \Delta^+ (1232) \rightarrow \begin{cases} n\pi^+, & \text{BR} = 1/3 \\ p\pi^0, & \text{BR} = 2/3 \end{cases}$$

$$\pi^+ \rightarrow \mu^+ \nu_\mu \rightarrow \bar{\nu}_\mu e^+ \nu_e \nu_\mu$$

$$\pi^0 \rightarrow \gamma\gamma$$

$$n \text{ (escapes)} \rightarrow p e^- \bar{\nu}_e$$

(Δ^+ : $\sim 50\%$ of all $p\gamma$ interactions)



After propagation, with flavour mixing:

$$\nu_e : \nu_\mu : \nu_\tau : p = 1 : 1 : 1 : 1$$

("one ν_μ per cosmic ray")

CR emission by n escape only is now strongly disfavoured

ICECUBE COLL., *Nature* **484**, 351 (2012)

AHLERS ET AL. *Astropart. Phys.* **35**, 87 (2011)

In a collision, UHE protons, photons, and neutrinos are emitted:

$$\underbrace{N'_p(E'_p)}_{\text{proton density at the source [GeV}^{-1} \text{ cm}^{-3}]}$$

NeuCosmA
 \otimes

$$\underbrace{N'_\gamma(E'_\gamma)}_{\text{photon density at the source}}$$

$$= \underbrace{Q'_\nu(E'_\nu)}_{\text{ejected neutrino spectrum [GeV}^{-1} \text{ cm}^{-3} \text{ s}^{-1]}}$$

- From Fermi shock acceleration: $N'_p(E'_p) \propto E_p'^{-\alpha_p} e^{-E'_p/E'_{p,\max}}$
- Photon density at source has same shape as observed:

$$N'_\gamma(E'_\gamma) = \begin{cases} (E'_\gamma/E'_{\gamma,\text{break}})^{-\alpha_\gamma} & , E'_{\gamma,\min} \leq E'_\gamma < E'_{\gamma,\text{break}} \\ (E'_\gamma/E'_{\gamma,\text{break}})^{-\beta_\gamma} & , E'_\gamma \geq E'_{\gamma,\text{break}} \\ 0 & , \text{otherwise} \end{cases}$$

$$\alpha_\gamma = 1, \beta_\gamma = 2.2, E'_{\gamma,\min} = 0.2 \text{ eV}, E'_{\gamma,\text{break}} = 1 \text{ keV}$$

Normalise the densities at the source – for one collision:

► Photons:

$$\underbrace{\int E'_\gamma N'_\gamma(E'_\gamma) dE'_\gamma}_{\text{total energy density in photons}} = \frac{E_{\gamma\text{-sh}}^{\text{iso}}}{V'_{\text{iso}}}$$

► Protons:

baryonic loading (energy in p 's / energy in e 's + γ 's), e.g., 10

$$\underbrace{\int E'_p N'_p(E'_p) dE'_p}_{\text{total energy density in protons}} = \frac{1}{f_e} \frac{E_{\gamma\text{-sh}}^{\text{iso}}}{V'_{\text{iso}}}$$

NeuCosmA calculates the injected/ejected spectrum of secondaries (π , K , n , ν , etc.):

$$x \equiv E' / E'_p$$

$$y \equiv E'_p E'_\gamma / (m_p c^2)$$

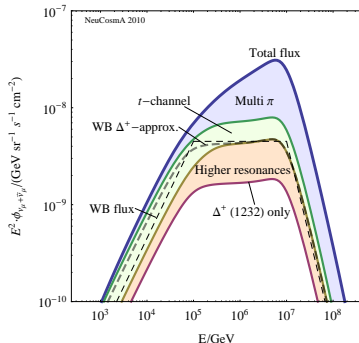
$$Q'(E') = \int_{E'}^{\infty} \frac{dE'_p}{E'_p} N'_p(E'_p) \int_0^{\infty} c dE'_\gamma N'_\gamma(E'_\gamma) R(x, y)$$

response function

R contains cross sections, multiplicities for different channels

What does NeuCosmA include?

- ▶ $p\gamma \rightarrow \Delta^+(1232) \rightarrow \pi^0, \pi^+, \dots$
- ▶ extra K , n , π^- , multi- π production modes
- ▶ synchrotron losses of secondaries
- ▶ adiabatic cooling
- ▶ full photon spectrum
- ▶ neutrino flavour transitions

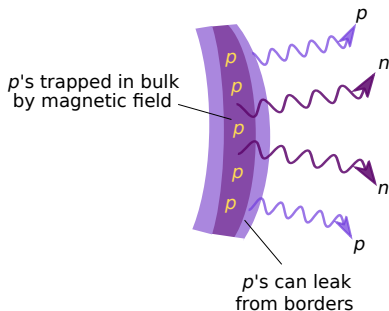


We have improved the model – now UHECRs escape as either:

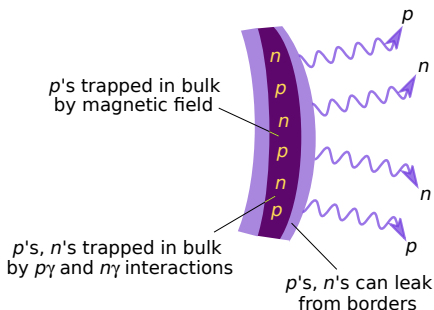
- ▶ **neutrons**, which decay into protons outside the source; or
- ▶ **protons** that leak out without interacting inside the source

Relative contributions determined by $\tau_n \equiv \left(t_{p\gamma}^{-1} / t_{\text{dyn}}^{-1} \right) \Big|_{E'_{p,\text{max}}}$

$\tau_n < 1$
optically **thin** to n escape

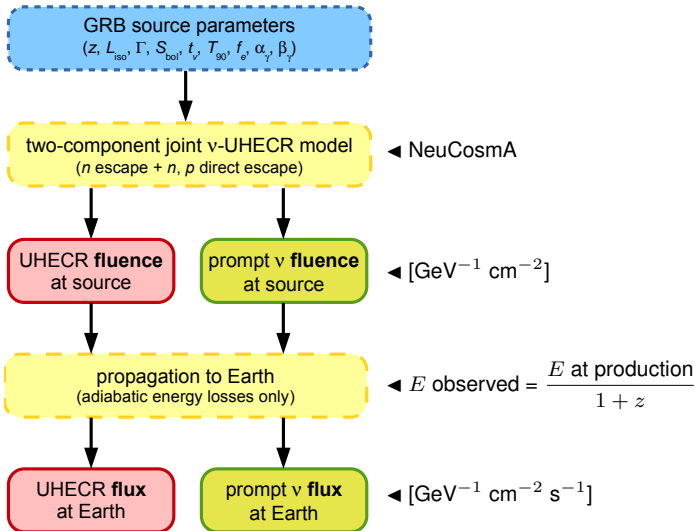


$\tau_n \geq 1$
optically **thick** to n escape



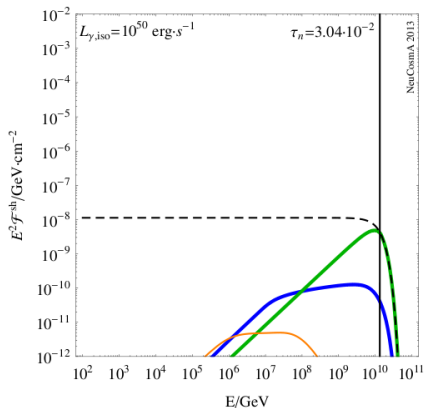
A two-component model of CR emission

Calculation of UHECR and neutrino fluxes from one GRB –

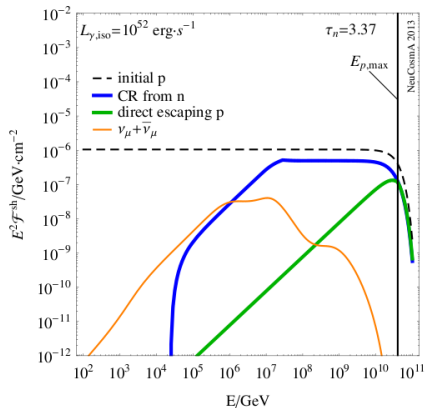


Sample neutrino fluences –

Optically **thin** source



Optically **thick** source

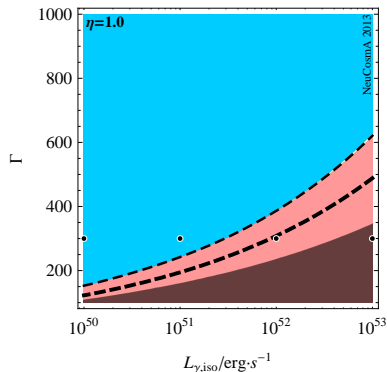
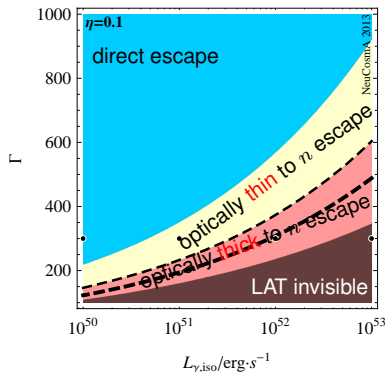


P. BAERWALD, MB, AND W. WINTER, *ApJ* **768**, 186 (2013)

Scan of the GRB emission parameter space –

acceleration efficiency $\longrightarrow \eta = 0.1$

$\eta = 1.0$

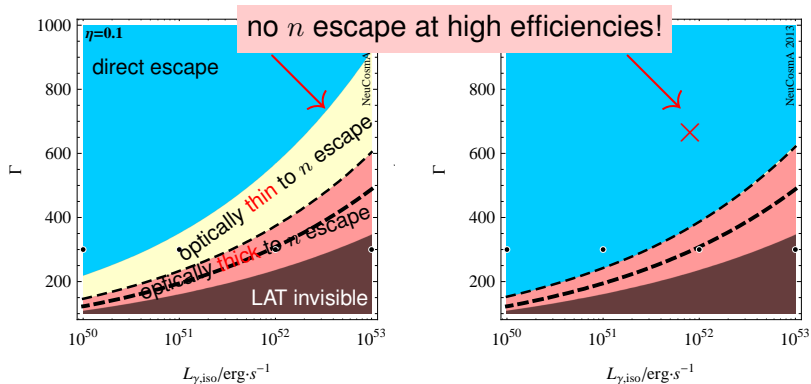


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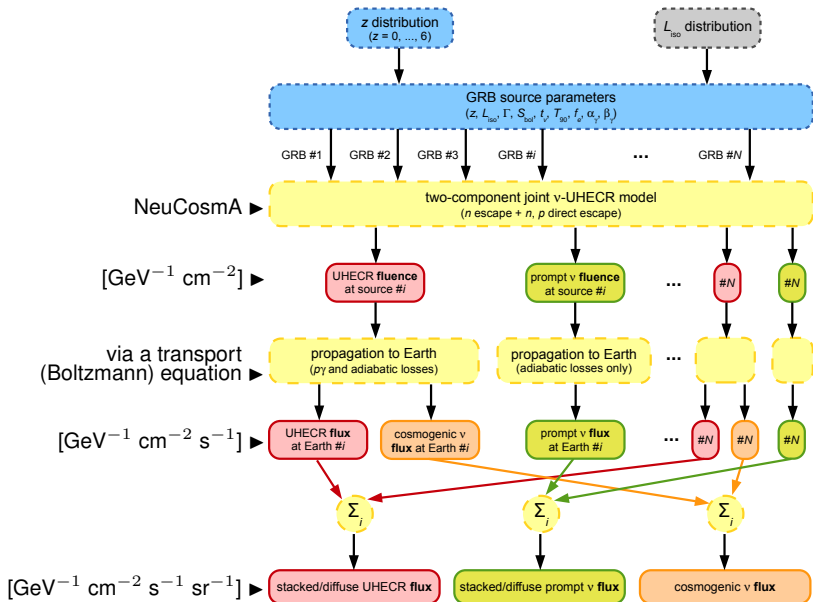
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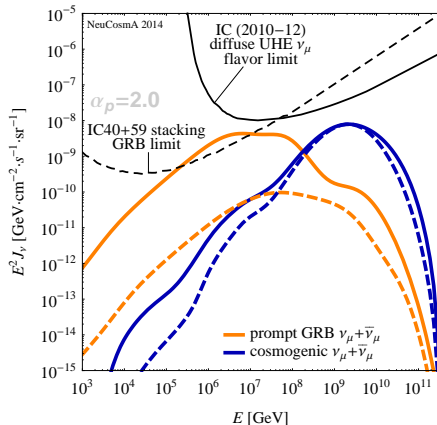
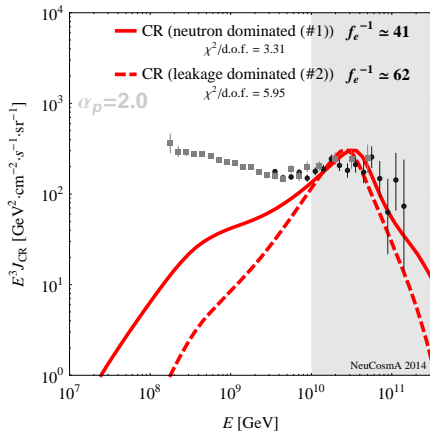


P. BAERWALD, MB, AND W. WINTER, *ApJ* **768**, 186 (2013)

Fluxes from a population of GRBs



Diffuse UHECR and neutrino predictions –



P. BAERWALD, MB, AND W. WINTER, *ApJ* **768**, 186 (2013)

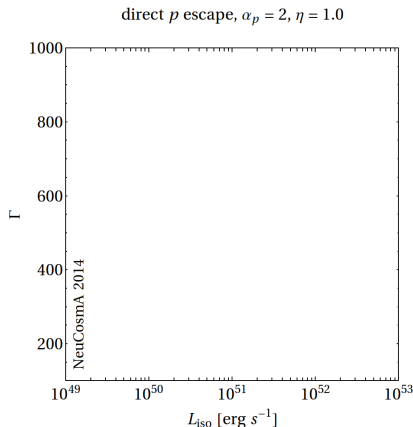
P. BAERWALD, MB, AND W. WINTER, *Astropart. Phys.* **62**, 66 (2015)

See also: H. HE *et al.*, *ApJ* **752**, 29 (2012)

We can already limit the parameter space by using the UHECR observations and ν upper bounds:

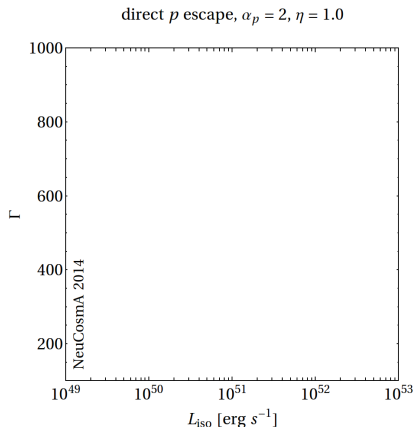
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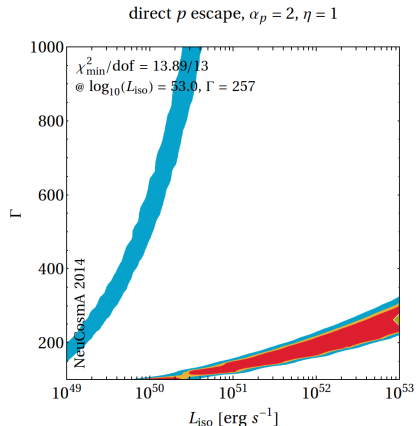
- 1 Generate the UHECR spectrum at every point in parameter space (e.g., in Γ vs. L_{iso})
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P. BAERWALD, MB, AND W. WINTER, *Astropart. Phys.* **62**, 66 (2015)

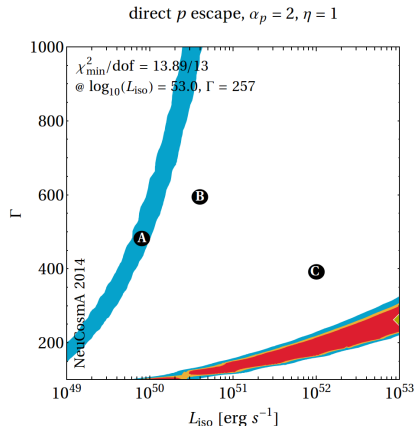
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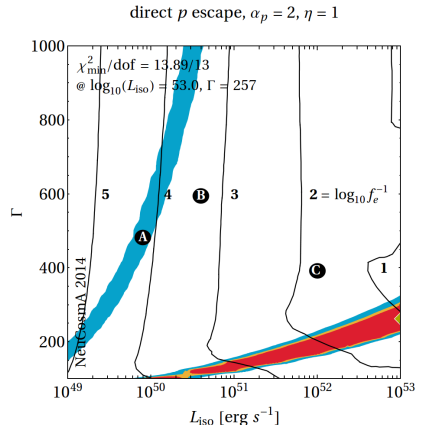
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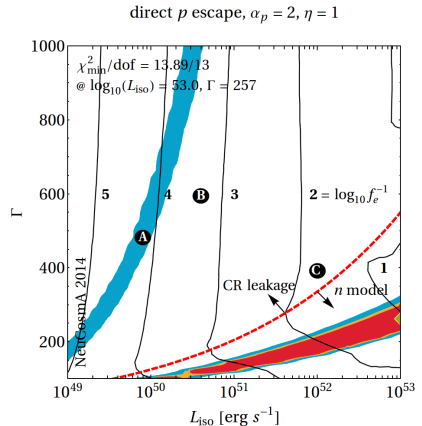
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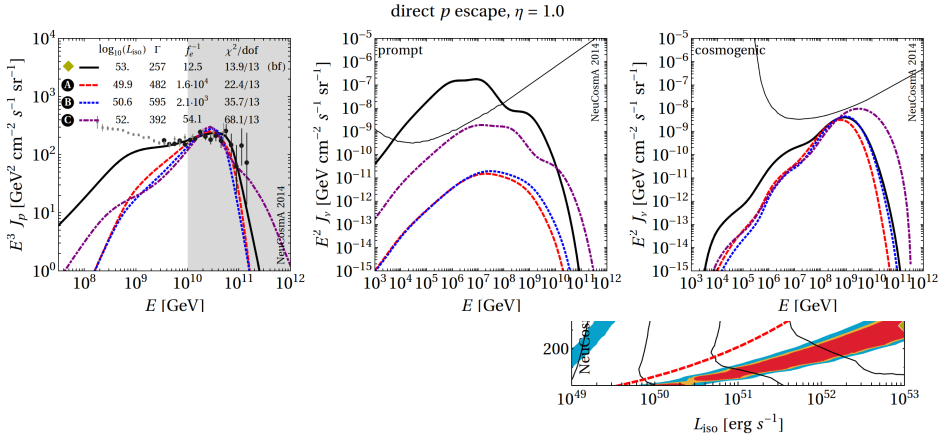
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- 4 Find the baryonic loading (i.e., relative energy of p 's to e 's) at each point
- 5 Identify the region corresponding to pure n escape and to n escape + CR leakage



P. BAERWALD, MB, AND W. WINTER, *Astropart. Phys.* **62**, 66 (2015)

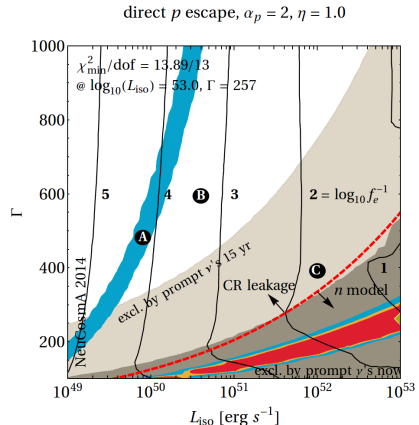
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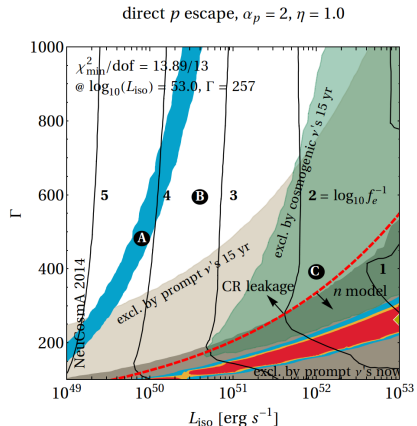
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- 6 Find the region where the number of prompt ν_μ 's is > 2.44 , i.e., the excluded region at 90% C.L.
- 7 After 15 yr of exposure and no detection, cosmogenic neutrinos also exclude



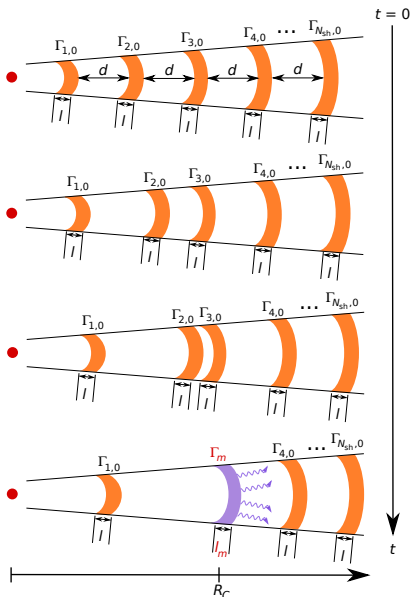
P. BAERWALD, MB, AND W. WINTER, *Astropart. Phys.* **62**, 66 (2015)

We have considered a dynamical fireball instead:

- ▶ the fireball expands with time
- ▶ shells propagate with different speeds
- ▶ they have different masses
- ▶ they collide at different radii (collisions no longer identical)

Why is this important?

The particle (γ , p) densities fall as the fireball expands – particle production conditions change with time/radius



During propagation:

- ▶ speeds (Γ_k), masses (m_k), widths (l_k) **do not** change (only in collisions)
- ▶ the new, merged shells continue propagating and can collide again

Evolution stops when either:

- ▶ a single shell is left; or
- ▶ all remaining shells have reached the circumburst medium ($\geq 5.5 \times 10^{11}$ km)

final number of collisions

\approx

number of initial shells ($\gtrsim 1000$)

S. KOBAYASHI, T. PIRAN, AND R. SARI, *ApJ* **490**, 92 (1997)
F. DAIGNE AND R. MOCHKOVITCH, *MNRAS* **296**, 275 (1998)

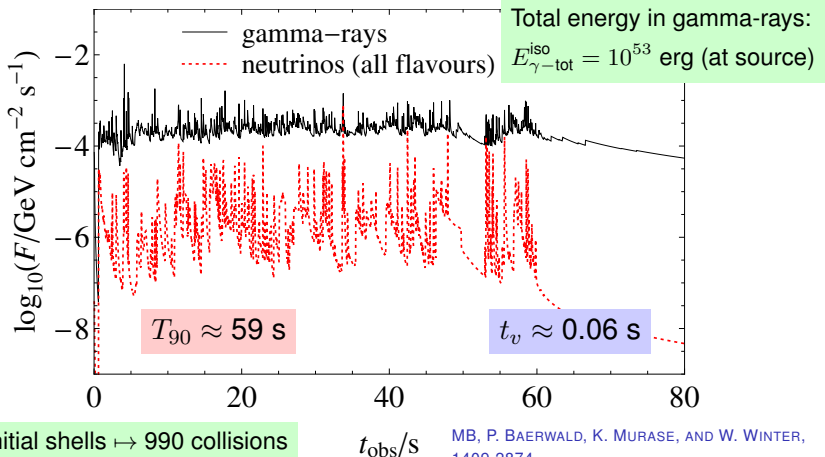
Let's look at a sample animated fireball –



▲ shell has not collided

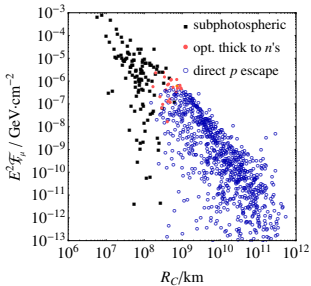
shell has collided many times ▲

- An emission pulse is assigned to each collision
– their superposition yields a **synthetic light curve**:



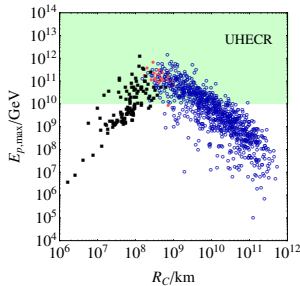
Each collision occurs in a different emission regime –

$\nu_\mu + \bar{\nu}_\mu$ fluence
neutrinos



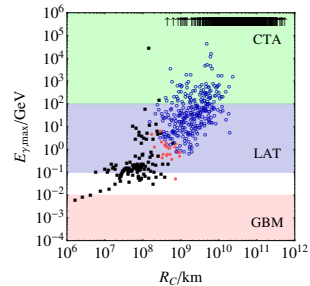
(observer's frame)

maximum p energy
cosmic rays



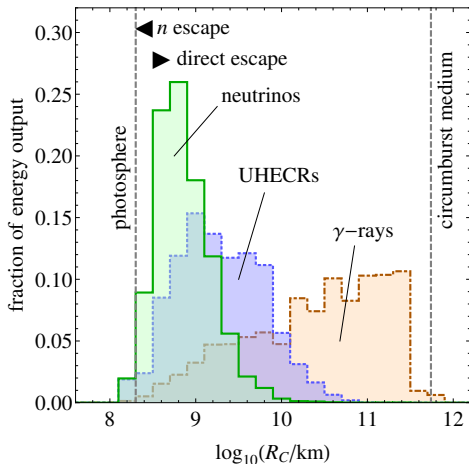
(source frame)

maximum γ energy
gamma-rays



MB, P. BAERWALD, K. MURASE, AND W. WINTER, 1409.2874

Emission of different species peaks at different collision radii –



Why?

As the fireball expands, photon and proton densities fall

Why does it matter?

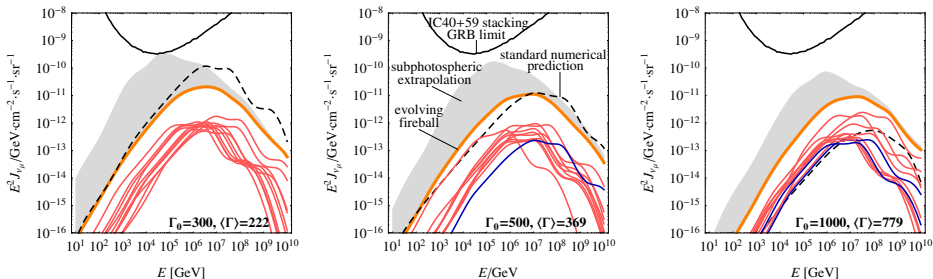
GRB parameters derived from gamma-ray observations might not be adequate to describe ν and UHECR emission

So what?

So the following happens ...

MB, P. BAERWALD, K. MURASE, AND W. WINTER, 1409.2874

Quasi-diffuse neutrino flux, assuming 667 GRBs per year –

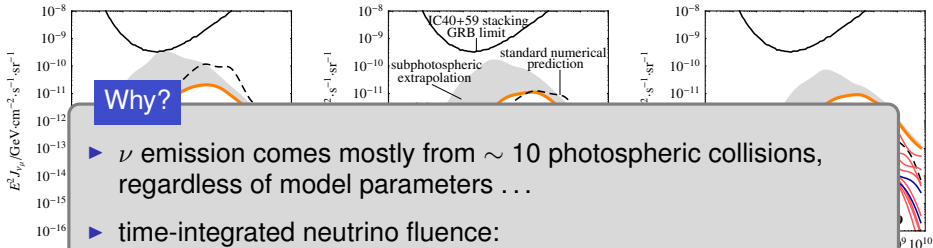


MB, P. BAERWALD, K. MURASE, AND W. WINTER, 1409.2874

we find a minimal ν flux of $\sim 10^{-11} \text{ GeV cm}^{-2} \text{s}^{-1} \text{sr}^{-1}$,
independently of Γ and baryonic loading

in contrast with traditional predictions, with a Γ^{-4} dependence

Quasi-diffuse neutrino flux, assuming 667 GRBs per year –



$$\mathcal{F}_\nu \propto \frac{N_{\text{coll}} (f_{p\gamma} \gtrsim 1)}{N_{\text{coll}}^{\text{tot}}} \times \min [1, f_{p\gamma}^{\text{ph}}] \times \frac{\epsilon_p}{\epsilon_e} \times E_{\gamma-\text{tot}}^{\text{iso}}$$

independently of Γ and baryonic loading

in contrast with traditional predictions, with a Γ^{-4} dependence

We have revised the UHECR and ν predictions from GRBs:

- 1 Refined the ν yields from $p\gamma$ interactions
- 2 Introduced a two-component UHECR- ν production model
 - direct p escape required at high acceleration efficiency
- 3 Constrained the model by using UHECR and neutrino data
 - n escape domination disfavoured by current ν bounds
 - baryonic loading can be inferred from the fits
- 4 Explored a dynamical fireball model
 - different particle species come from different collision radii
 - found a minimal neutrino flux from GRBs

The coming years should provide much more data on the UHE messengers to put the theories to further test



S. LEE AND J. KIRBY, *Fantastic Four* 1 (1961)

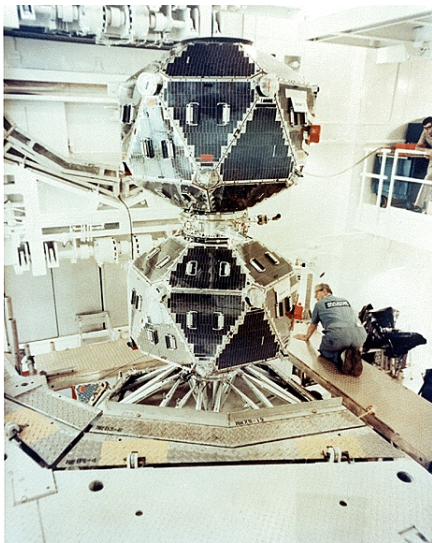
Backup slides

Several ongoing projects, in different stages of progress:

- ▶ **Fireball evolution:** different GRB parameter sets, include nuclei
P. Baerwald (Penn State), MB, K. Murase (IAS Princeton), W. Winter (DESY)
- ▶ **Seesaw and heavy neutrino decay detection in IceCube**
MB, C. de los Heros (Uppsala Univ.), J. Jones (PUCP Lima), P. Ferrario (IFIC Valencia)
- ▶ **Lorentz invariance violation in cosmogenic neutrinos**
MB, P. Mehta (Univ. Delhi), W. Winter (DESY)
- ▶ **Decay of UHE astrophysical neutrinos:** use the latest IceCube data to constrain the ν lifetime (based on [JCAP 1210, 020 \(2012\)](#),
[P. BAERWALD, MB, W. WINTER](#))
MB, K. Murase (IAS Princeton)
- ▶ **Prospects for correlations between UHECRs and neutrinos:** both in position and energy
C. Argüelles (WIPAC Wisconsin), MB, J. Carpio (PUCP Lima), A. Gago (PUCP Lima), J. Salvadó (WIPAC Wisconsin)

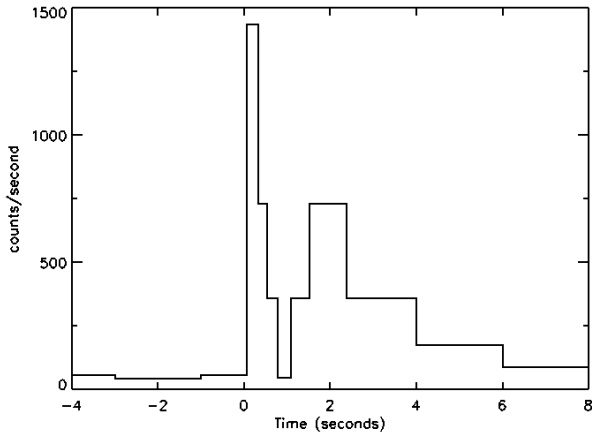
After the 1963 Nuclear Test Ban Treaty, the U.S. launched six pairs of *Vela* satellites:

- ▶ They carried X-ray, gamma-ray, and neutron detectors
- ▶ *Vela* 5a-b had enough spatial resolution to pinpoint the direction of events
- ▶ Intense gamma-ray emission from a nuclear explosion lasts $\lesssim 10^{-6}$ s ...
- ▶ ... however, longer-lasting emissions were detected



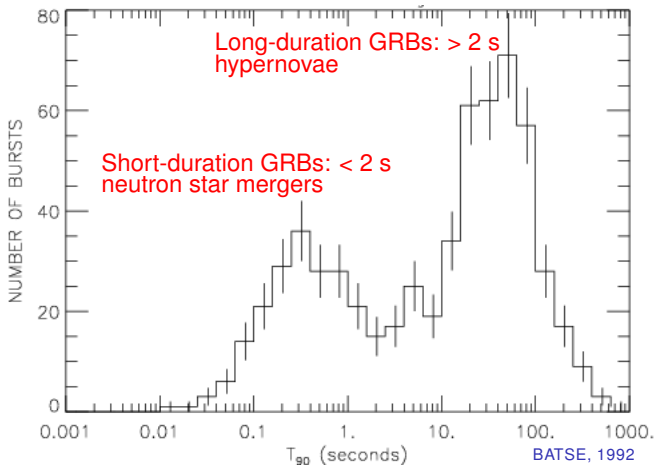
VELA 5A/B SATELLITES (NASA)

First GRB detected: July 2, 1967, 14:19 UTC



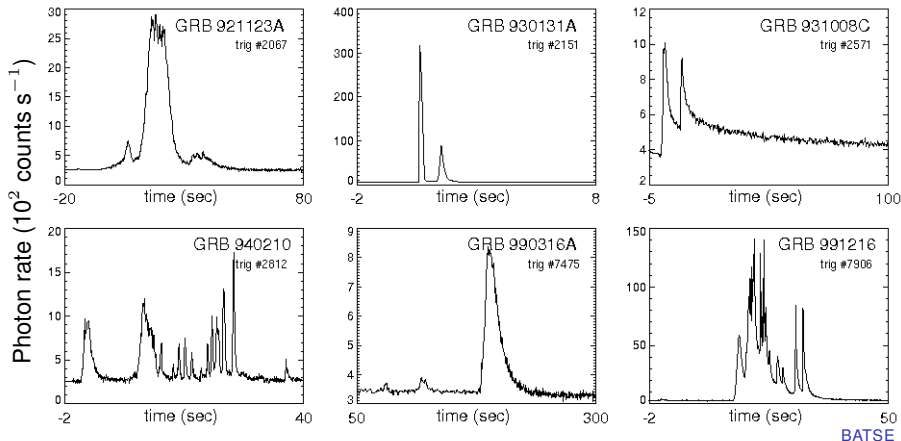
Detected by *Vela* 3, 4a, 4b (found on archival data)

Two populations of GRBs:



T_{90} : time during which 90% of gamma-ray energy is recorded

GRB light curves come in different shapes:



BATSE

variability timescale (width of pulses) $\equiv t_v \approx 1 \text{ ms}$

The neutron model hinges on:

- ① p 's magnetically confined, only n 's escape
- ② p 's interact at most once, n 's do not (*optically thin source*)

However, under the “one ν_μ per CR” hypothesis, GRBs **are disfavoured** to be the sole source of UHECRs (**AHLERS *et al.***).

M. AHLERS, M. GONZÁLEZ-GARCÍA, AND F. HALZEN *Astropart. Phys.* **35**, 87 (2011)

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However, under the “one ν_μ per CR” hypothesis, GRBs **are disfavoured** to be the sole source of UHECRs (**AHLERS *et al.***).

What if ① and ② are violated?

- ▶ p 's “leak out”, not accompanied by (direct) ν production
- ▶ multiple p interactions enhance the ν flux
- ▶ in *optically thick sources*, only n 's at the borders escape

M. AHLERS, M. GONZÁLEZ-GARCÍA, AND F. HALZEN *Astropart. Phys.* **35**, 87 (2011)

GZK \equiv Greisen-Zatsepin-Kuzmin (1966)

The process $p + \gamma_{\text{CMB}} \rightarrow \Delta^+ (1232) \rightarrow \pi^+ + n$ has a threshold

$$E_{\text{GZK}}^{\text{th}} = \frac{m_{\pi} (m_p + m_{\pi}/2)}{\epsilon_{\text{CMB}}} \approx 6.8 \cdot 10^{10} \left(\frac{\epsilon_{\text{CMB}}}{10^{-3} \text{ eV}} \right) \text{ GeV}$$

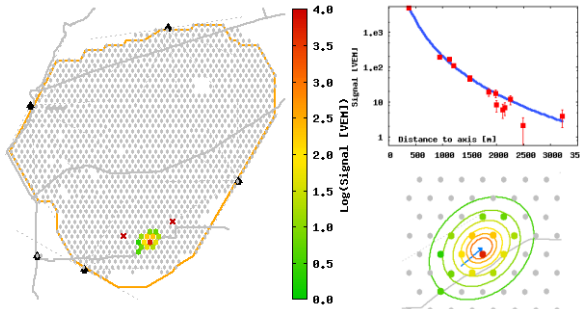
Survival probability of a 10^{11} GeV propagating for a distance d :

$$p(d) \approx \exp \left(\frac{-d}{6.6 \text{ Mpc}} \right) \Rightarrow p(d) < 10^{-4} \text{ for } d = 50 \text{ Mpc}$$

Two conclusions

- ① The maximum CR energy is $\sim 10^{11}$ GeV
- ② UHECRs are created relatively close to us ($\lesssim 50$ Mpc)

This is what a UHE event looks like in Auger:



Idc	10485600
Date	Tue Oct 26 17:39:16 2010
No. of stations	14
Energy	49.7 ± 1.9 EeV
Theta	40.2 ± 0.2 deg
Phi	-139.2 ± 0.2 deg
Curvature	10.9 ± 0.5 km
Core Easting	476053 ± 19 m
Core Northing	6079248 ± 12 m
Reduced χ^2	8.36

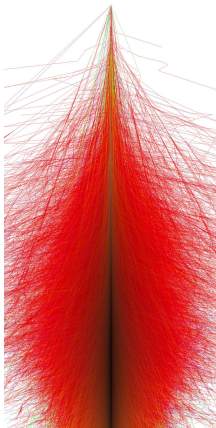
Problem:

So how is the identity of the primary reconstructed from this?

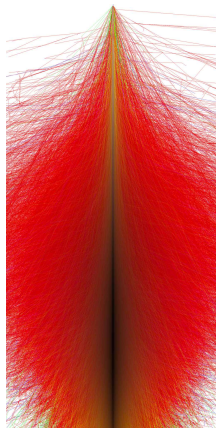
Answer:

use longitudinal air shower development information
from the fluorescence detectors

10^6 GeV proton



10^6 GeV Fe-56 nucleus



VS.

F. SCHMID, UNIV. LEEDS

Number of cascading particles evolves as (Gaisser & Hillas):

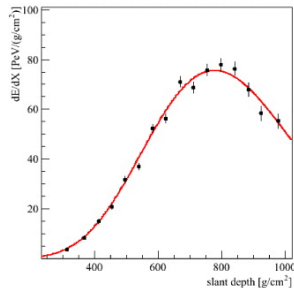
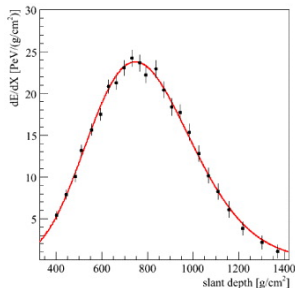
$$N(x) = N_{\max} \left(\frac{x - x_0}{x_{\max} - x_0} \right)^{(x_{\max} - x_0 / \Lambda)} \exp \left(\frac{x_{\max} - x}{\Lambda} \right)$$

x : slant depth, i.e., column density traversed (g cm^{-2})

x_{\max} : depth of shower maximum

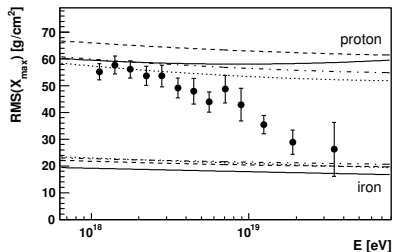
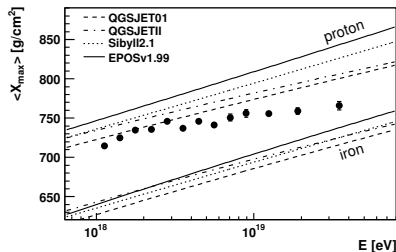
x_0 : related to depth of first interaction in the atmosphere

Using the FDs, measure $N(x)$, x_{\max} for each shower:



$\langle x_{\max} \rangle$: average value of x_{\max} among all showers

Compare these data to the simulated $\langle x_{\max} \rangle$ assuming a proton or Fe primary:



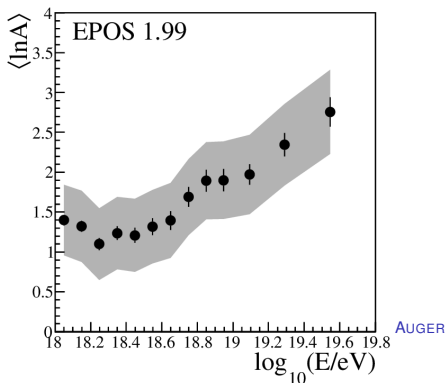
AUGER

There is a tendency towards heavier composition at very high energies

$\langle x_{\max} \rangle$ is related to the average mass number $\langle \ln A \rangle$
(Heitler-Matthews model):

$$\langle x_{\max} \rangle = \alpha (\ln E - \langle \ln A \rangle) + \beta$$

α, β : from hadronic interactions (cross section, multiplicity, etc.)



Two considerations:

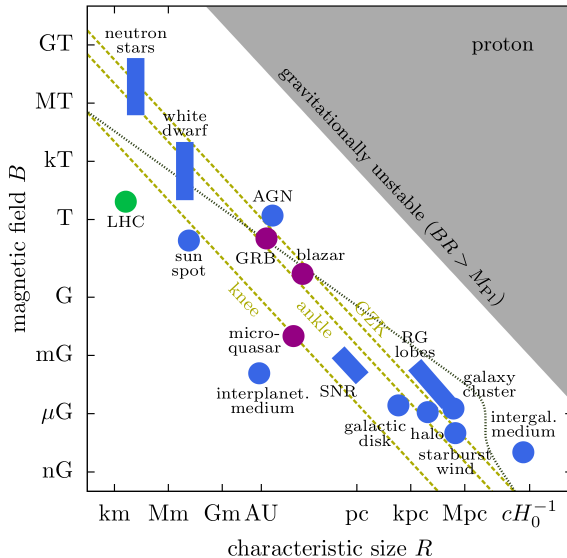
- ① Charged particles (Z) are assumed to be accelerated by intense magnetic fields in astrophysical sources
- ② For the acceleration to be maintained, the gyroradius should be smaller than the size of the acceleration region

$$\text{Larmor radius: } R_L = \frac{1.1}{Z} \left(\frac{E}{\text{EeV}} \right) \left(\frac{B}{\mu\text{G}} \right)^{-1}$$

Hillas criterion: $R_L < R$

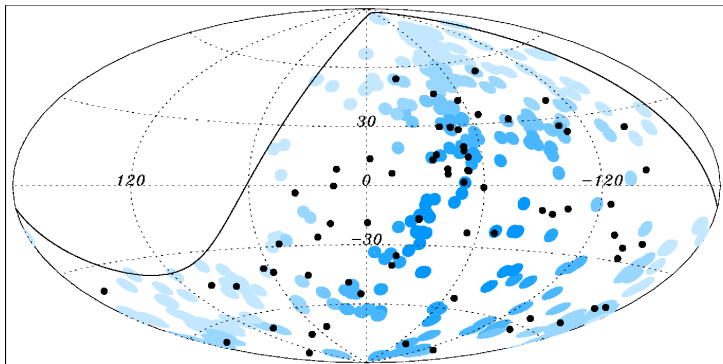
This limits the maximum energy:

$$E_{\text{max}} \simeq Z \left(\frac{B}{\mu\text{G}} \right) \left(\frac{R}{\text{kpc}} \right) \cdot 10^9 \text{ GeV}$$



- ▶ 69 CRs with > 55 EeV observed at Auger
- ▶ Compare arrival directions to positions of 318 known AGN within 75 Mpc

Circles of 3.1° centered around each source



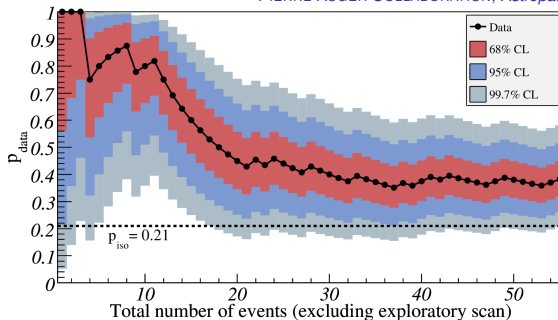
PIERRE AUGER COLLABORATION, *Astropart. Phys.* **34**, 314 (2010)

Degree of correlation: $p_{\text{data}} = k/N$

k : number of UHECRs correlated to sources

N : total number of UHECRs

PIERRE AUGER COLLABORATION, *Astropart. Phys.* **34**, 314 (2010)



Auger found $p_{\text{data}} = 0.38^{+0.07}_{-0.06}$ – inconclusive when compared to the value for an isotropic distribution of sources, $p_{\text{iso}} = 0.21$

Two important points:

- 1 $E'_{p,\max}$ is determined by energy-loss processes:

$$t'_{\text{acc}}(E'_{p,\max}) = \min \left[t'_{\text{dyn}}, t'_{\text{syn}}(E'_{p,\max}), t'_{p\gamma}(E'_{p,\max}) \right]$$

- 2 Photons can be trapped in the source by pair production:

$$\gamma + \gamma \rightarrow e^+ + e^-$$

Photosphere: radius where $\tau_{\gamma\gamma}(E'_\gamma) = 1$ for all E'_γ

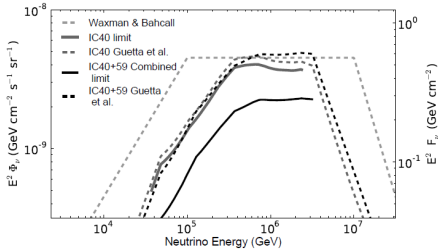
Optical depth:

$$\tau_n = \left. \frac{t_{p\gamma}^{-1}}{t_{\text{dyn}}^{-1}} \right|_{E_{p,\text{max}}} = \begin{cases} \lesssim 1, & \text{optically **thin** source} \\ > 1, & \text{optically **thick** source} \end{cases}$$

Particles can escape from within a shell of thickness λ'_{mfp} :

$$\left. \begin{aligned} \lambda'_{p,\text{mfp}}(E') &= \min [\Delta r', R'_L(E'), ct'_{p\gamma}(E')] \\ \lambda'_{n,\text{mfp}}(E') &= \min [\Delta r', ct'_{p\gamma}(E')] \end{aligned} \right\} f_{\text{esc}} = \frac{\lambda'_{\text{mfp}}}{\Delta r'}$$

fraction of escaping particles



IceCube Collaboration:

- ν flux normalised to GRB γ fluence:

$$\int_0^\infty dE_\nu E_\nu F_\nu(E_\nu) \propto \int_{1 \text{ keV}}^{10 \text{ MeV}} d\varepsilon_\gamma \varepsilon_\gamma F_\gamma(\varepsilon_\gamma)$$

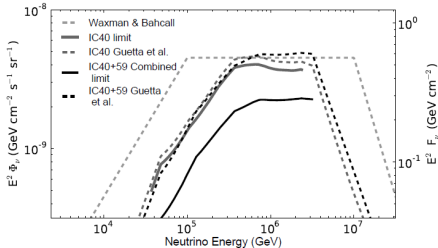
- quasi-diffuse ν flux from 117 GRBs
- **analytical calculation** – in tension with upper bounds

ICECUBE COLL., *Nature* **484**, 351 (2012)

AHLERS ET AL. *Astropart. Phys.* **35**, 87 (2011)

GUETTA ET AL. *Astropart. Phys.* **20**, 429 (2004)

The neutron model under tension?



More detailed particle physics (NeuCosmA):

- ▶ extra multi- π , K , n production modes
- ▶ synchrotron losses of secondaries
- ▶ adiabatic cooling
- ▶ full photon spectrum, etc.

ν flux \sim one order of magnitude lower

BAERWALD, HÜMMER, WINTER, *PRL* **108**, 231101 (2012)

See also: HE, LIU, WANG, *ApJ* **752**, 29 (2012)

IceCube Collaboration:

- ▶ ν flux normalised to GRB γ fluence:

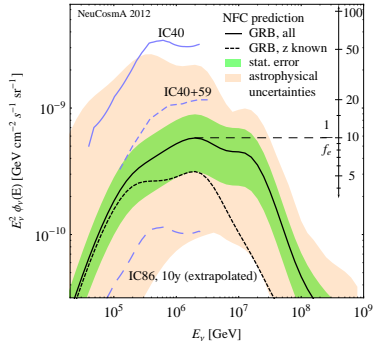
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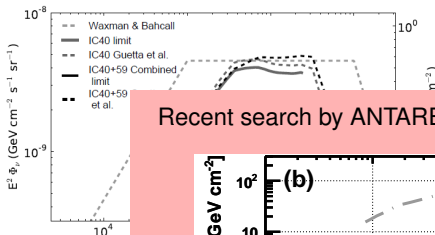
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ICECUBE COLL., *Nature* **484**, 351 (2012)

AHLERS ET AL. *Astropart. Phys.* **35**, 87 (2011)

GUETTA ET AL. *Astropart. Phys.* **20**, 429 (2004)

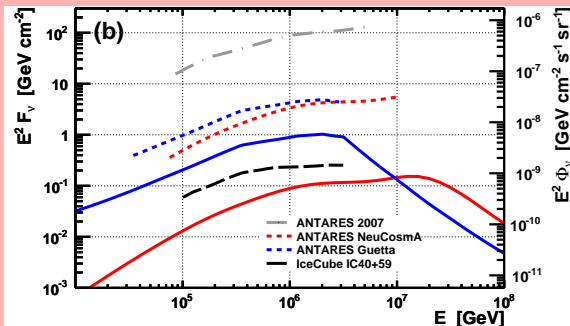




More detailed particle physics (NeuCosmA):

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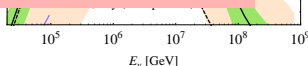
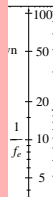
Recent search by ANTARES optimised for NeuCosmA:



ANTARES COLLAB., A & A 559, A9 (2013)

- ▶ IceCube is also revising its GRB predictions

lower
1 (2012)



IceCube Coll.

- ▶ ν flux

$$\int_0^\infty dE_\nu$$

- ▶ quasi-c

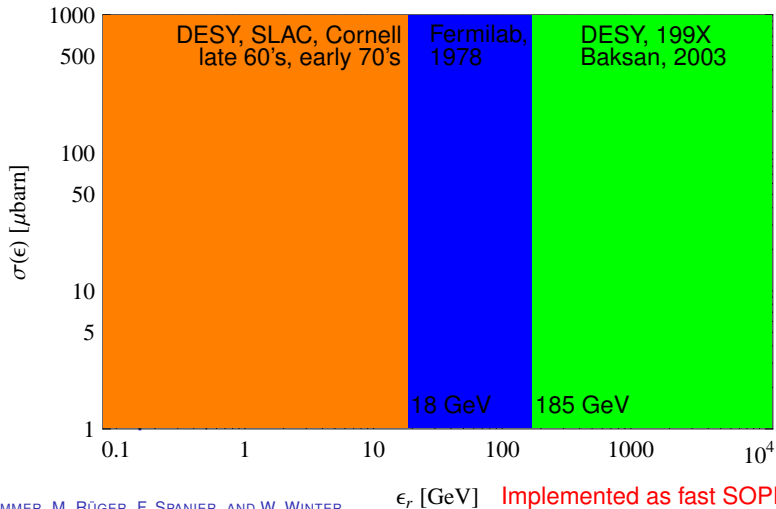
- ▶ analyti

upper l

ICECUBE COLL.,

AHLERS ET AL. *Astropart. Phys.* **35**, 87 (2011)

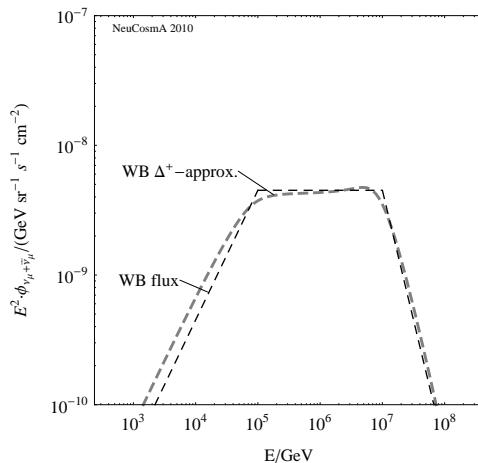
GUETTA ET AL. *Astropart. Phys.* **20**, 429 (2004)



S. HÜMMER, M. RÜGER, F. SPANIER, AND W. WINTER,
Astrophys. J. **721**, 630 (2010)

Implemented as fast SOPHIA-based
parametrisation

- Contributions to the full photohadronic cross section

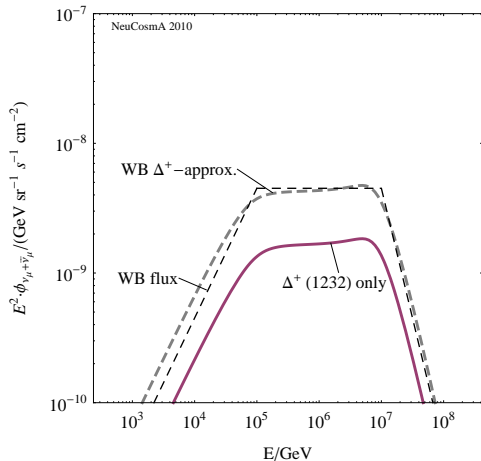


- Contributions to the full photohadronic cross section

Contributions to $(\nu_\mu + \bar{\nu}_\mu)$ flux
from π^\pm decay divided in:

- $\Delta(1232)$ -resonance

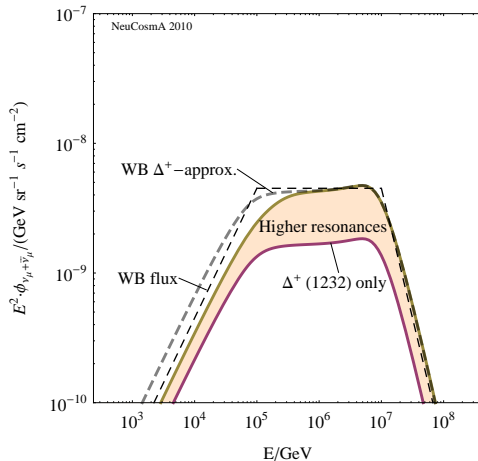
P. BAERWALD, S. HÜMMER, AND W. WINTER,
Phys. Rev. D **D83**, 067303 (2011)



Contributions to $(\nu_\mu + \bar{\nu}_\mu)$ flux
from π^\pm decay divided in:

- ▶ $\Delta(1232)$ -resonance
- ▶ Higher resonances

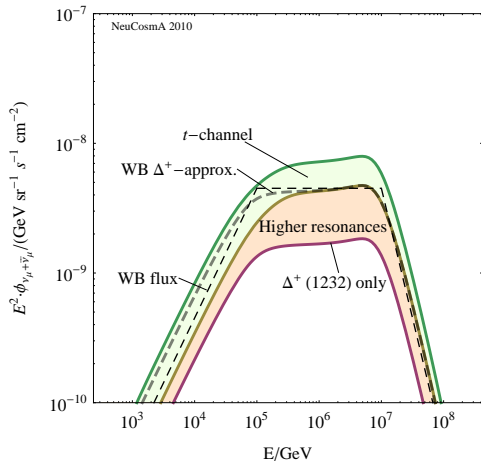
P. BAERWALD, S. HÜMMER, AND W. WINTER,
Phys. Rev. D **83**, 067303 (2011)



Contributions to $(\nu_\mu + \bar{\nu}_\mu)$ flux
from π^\pm decay divided in:

- ▶ $\Delta(1232)$ -resonance
- ▶ Higher resonances
- ▶ t -channel
(direct production)

P. BAERWALD, S. HÜMMER, AND W. WINTER,
Phys. Rev. D **83**, 067303 (2011)

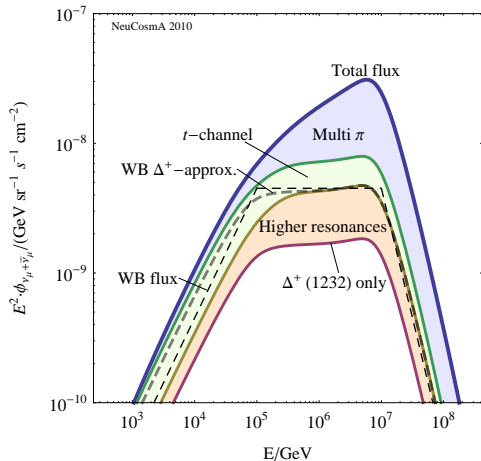


- Contributions to the full photohadronic cross section

Contributions to $(\nu_\mu + \bar{\nu}_\mu)$ flux from π^\pm decay divided in:

- ▶ $\Delta(1232)$ -resonance
- ▶ Higher resonances
- ▶ t -channel (direct production)
- ▶ High energy processes (multiple π)

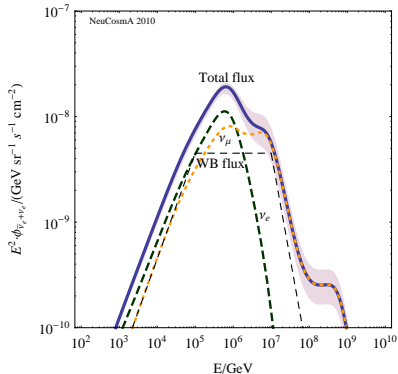
P. BAERWALD, S. HÜMMER, AND W. WINTER,
Phys. Rev. D **83**, 067303 (2011)



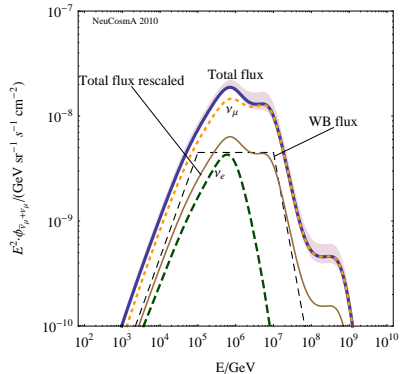
Especially "Multi π " contribution leads to **change of flux shape**; neutrino flux higher by up to a factor of 3 compared to WB treatment

- Neutrino spectra including flavour mixing

Electron neutrino spectrum



Muon neutrino spectrum



P. BAERWALD, S. HÜMMER, AND W. WINTER, *Phys. Rev.* **D83**, 067303 (2011)

Characteristic double peak structure from μ and π decay in both flavours, additional peak from K^+ decay at 10^8 to 10^9 GeV

Corrections to the analytical model:

► **shape revised:**

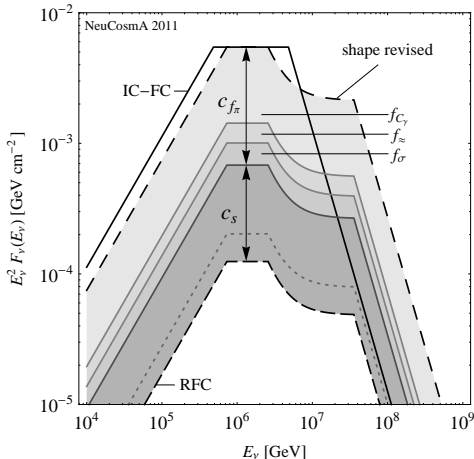
- shift of first break (correction of photohadronic threshold)
- different cooling breaks for μ 's and π 's
- $(1+z)$ correction on the variability scale of the GRB

► **Correction cf_π to π prod. efficiency:**

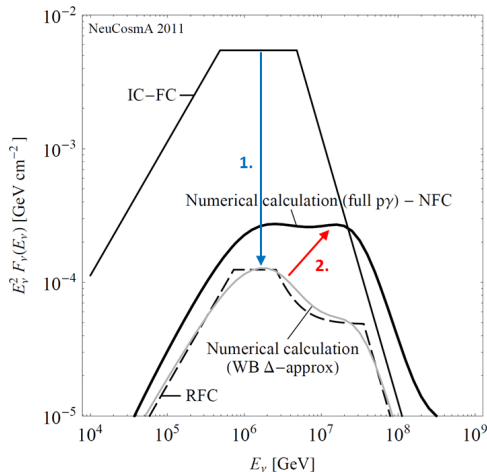
- f_{C_γ} : full spectral shape of photons
- $f_\approx = 0.69$: rounding error in analytical calculation
- $f_\sigma \simeq 2/3$: from neglecting the width of the Δ -resonance

► **Correction c_s :**

- energy losses of secondaries
- energy dependence of the mean free path of protons



S. HÜMMER, P. BAERWALD, AND W. WINTER,
Phys. Rev. Lett. **108**, 231101 (2012)



For example, GRB080603A:

1. Correction to analytical model (IC-FC \rightarrow RFC)
2. Change due to full numerical calculation

IC-FC: IceCube-Fireball Calculation
 RFC: Revised Fireball Calculation
 NFC: Numerical Fireball Calculation

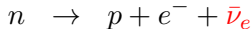
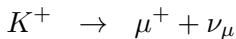
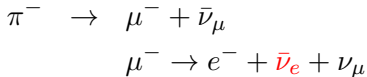
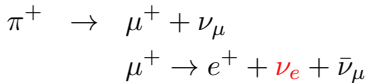
S. HÜMMER, P. BAERWALD, AND W. WINTER, *Phys. Rev. Lett.* **108**, 231101 (2012)

$$\begin{aligned}\pi^+ &\rightarrow \mu^+ + \nu_\mu \\ \mu^+ &\rightarrow e^+ + \nu_e + \bar{\nu}_\mu\end{aligned}$$

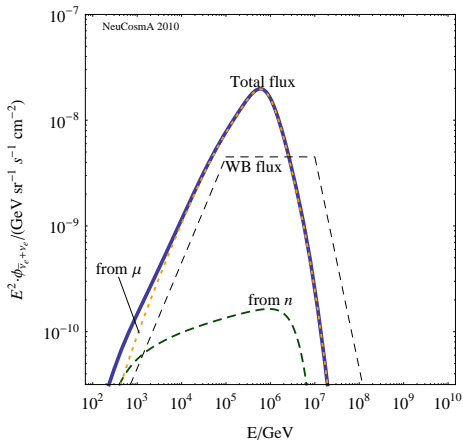
$$\begin{aligned}\pi^- &\rightarrow \mu^- + \bar{\nu}_\mu \\ \mu^- &\rightarrow e^- + \bar{\nu}_e + \nu_\mu\end{aligned}$$

$$K^+ \rightarrow \mu^+ + \nu_\mu$$

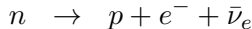
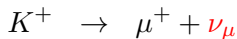
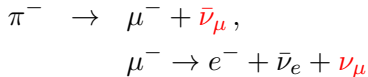
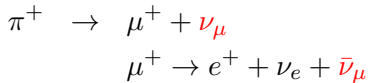
$$n \rightarrow p + e^- + \bar{\nu}_e$$



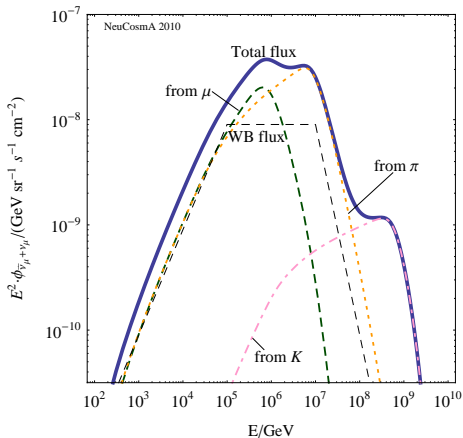
Resulting ν_e flux (at the observer)



P. BAERWALD, S. HÜMMER, AND W. WINTER, *Phys. Rev.* **D83**, 067303 (2011)



Resulting ν_μ flux (at the observer)



P. BAERWALD, S. HÜMMER, AND W. WINTER, *Phys. Rev.* **D83**, 067303 (2011)

- The new prediction of the quasi-diffuse GRB ν flux

- ▶ Same $n = 117$ GRBs, effective area, and parameters as used by the IC-40 analysis

- ▶ Calculate the associated neutrino flux for each burst and the stacked flux $F_\nu(E_\nu)$

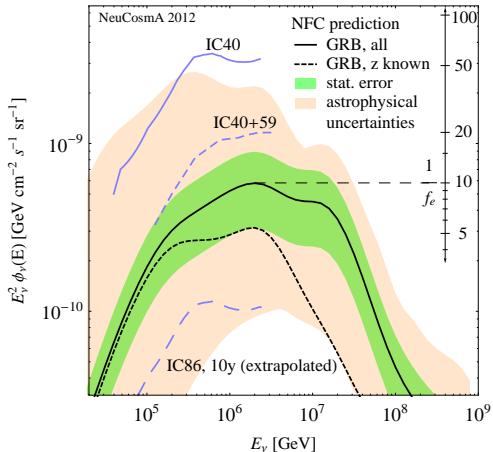
- ▶ Quasidiffuse flux:

$$\phi_\nu(E_\nu) = F_\nu(E_\nu) \frac{1}{4\pi} \frac{1}{n} \frac{667 \text{ bursts}}{\text{yr}}$$

- ▶ **Statistical uncertainty:**
extrapolation of a few bursts to a quasidiffuse flux

- ▶ **Astrophysical uncertainty:**

- ▶ $0.001 \leq t_v [\text{s}] \leq 0.1$
- ▶ $200 \leq \Gamma \leq 500$
- ▶ $1.8 \leq \alpha_p \leq 2.2$
- ▶ $0.1 \leq \epsilon_e/\epsilon_B \leq 10$



S. HÜMMER, P. BAERWALD, AND W. WINTER,
Phys. Rev. Lett. **108**, 231101 (2012)

- The new prediction of the quasi-diffuse GRB ν flux

We use a **Boltzmann equation** to transport protons to Earth:

- Comoving number density of protons ($\text{GeV}^{-1} \text{ cm}^{-3}$):

$$Y_p(E, z) = n_p(E, z) / (1 + z)^3,$$

with n_p the real number density

- Transport equation (comoving source frame):

$$\dot{Y}_p = \underbrace{\partial_E (H E Y_p)}_{\text{adiabatic losses}} + \underbrace{\partial_E (b_{e^+e^-} Y_p)}_{\text{pair production losses}} + \underbrace{\partial_E (b_{p\gamma} Y_p)}_{\text{photohadronic losses}} + \underbrace{\mathcal{L}_{\text{CR}}}_{\text{CR injection from sources}}$$

$Q_{\text{CR}}(E) \propto E^{-\alpha_p} e^{-E/E_{p,\text{max}}}$

Expected ν flux from cosmological accelerators (Waxman & Bahcall 1997 & 1998):

$$E^2 \Phi_\nu \sim 10^{-8} \frac{f_\pi}{0.2} \left(\frac{\dot{\epsilon}_{\text{CR}}^{[10^{10}, 10^{12}]}}{10^{44} \text{ erg Mpc}^{-3} \text{ yr}^{-1}} \right) \text{ GeV cm}^{-2} \text{ s}^{-1} \text{ sr}^{-1}$$

Integrated flux above 1 PeV:

$$\Phi_\nu (> 1 \text{ PeV}) \sim \int_{1 \text{ PeV}}^{\infty} \frac{10^{-8}}{E^2} dE \sim 10^{-20} \text{ cm}^{-2} \text{ s}^{-1} \text{ sr}^{-1}$$

Number of events from half of the sky (2π):

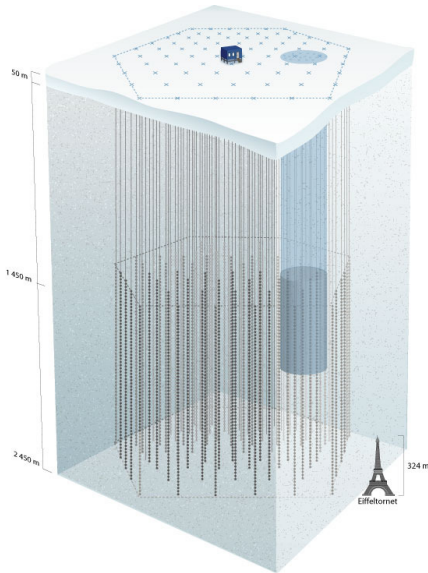
$$N_\nu \simeq 2\pi \cdot \Phi_\nu (> 1 \text{ PeV}) \cdot 1 \text{ yr} \cdot A_{\text{eff}} \approx (2.4 \times 10^{-10} \text{ cm}^{-2}) A_{\text{eff}},$$

where A_{eff} is the effective area of the detector

To detect $N_\nu > 1$ events per year, we need an area of

$$A_{\text{eff}} \gtrsim 0.4 \text{ km}^2$$

Therefore, we need km-scale detectors, like IceCube



IceCube: km³ in-ice South Pole
Čerenkov detector

Neutrinos detected through νN
interactions ($N = n, p$)

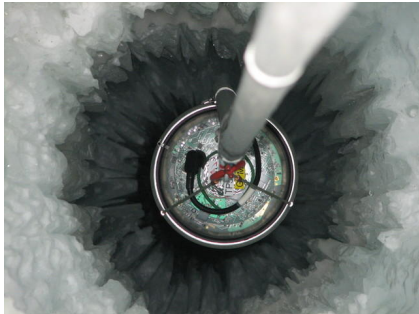
- ▶ **Neutral current:** all flavours
produce hadronic showers
- ▶ **Charged current:** ν_μ 's
leave muon tracks; ν_e/τ
produce showers



IceCube: km³ in-ice South Pole
Čerenkov detector

Neutrinos detected through νN
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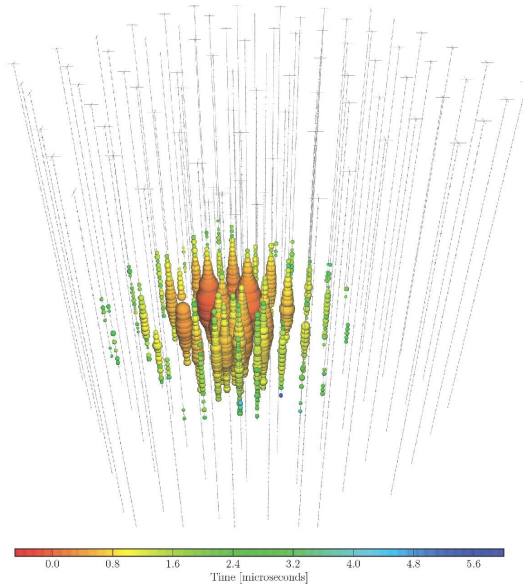
- ▶ **Neutral current:** all flavours
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leave muon tracks; ν_e/τ
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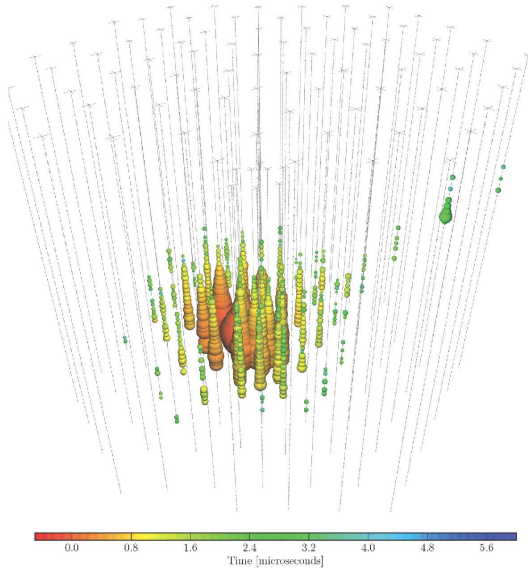


IceCube: km³ in-ice South Pole
Čerenkov detector

Neutrinos detected through νN
interactions ($N = n, p$)

- ▶ **Neutral current:** all flavours
produce hadronic showers
- ▶ **Charged current:** ν_μ 's
leave muon tracks; ν_e/τ
produce showers





We have seen that protons interact with the cosmological photon fields (CMB, etc.), *e.g.*,

$$p + \gamma \rightarrow \Delta^+ \rightarrow \pi^+ + n ,$$

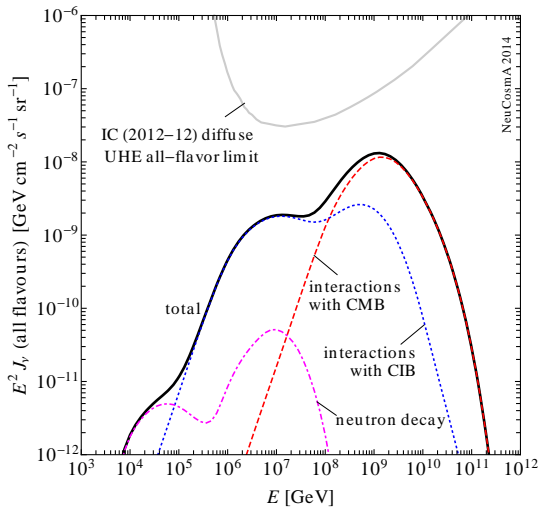
and neutrinos are created in the decays of the secondaries:

$$\pi^+ \rightarrow \mu^+ + \nu_\mu$$

$$\mu^+ \rightarrow \bar{\nu}_\mu + \nu_e + e^+$$

$$n \rightarrow p + e^- + \bar{\nu}_e$$

These are called *cosmogenic neutrinos*



P. BAERWALD, MB, W. WINTER, *Astropart. Phys.* **62**, 66 (2015)

- ▶ Energy loss rate (GeV s^{-1}):

$$b(E) \equiv \frac{dE}{dt}$$

- ▶ For pair production $p\gamma \longrightarrow pe^+e^-$:

$$b_{e^+e^-}(E, z) = -\alpha r_0^2 (m_e c^2)^2 c \int_2^\infty d\xi n_\gamma \left(\frac{\xi m_e c^2}{2\gamma}, z \right) \frac{\phi(\xi)}{\xi^2}$$

- ▶ n_γ : isotropic photon background ($\text{GeV}^{-1} \text{ cm}^{-3}$)
- ▶ ξ : photon energy in units of $m_e c^2$
- ▶ proton energy: $E = \gamma m_p c^2$ ($\gamma \gg 1$)
- ▶ $\phi(\xi)$: (tabulated) integral in energy of outgoing e^-

G. BLUMENTHAL, *Phys. Rev.* **D 1**, 1596 (1970)

H. BETHE, W. HEITLER, *Proc. Roy. Soc.* **A146**, 83 (1934)

Photohadronic interactions – $p\gamma$ interaction rate (s^{-1} per particle):

$$\Gamma_{p\gamma \rightarrow p'b} (E, z) = \frac{1}{2} \frac{m_p^2}{E^2} \int_{\frac{\epsilon_{\text{th}} m_p}{2E}}^{\infty} d\epsilon \frac{n_{\gamma}(\epsilon, z)}{\epsilon^2} \int_{\epsilon_{\text{th}}}^{2E\epsilon/m_p} d\epsilon_r \epsilon_r \sigma_{p\gamma \rightarrow p'b}^{\text{tot}}(\epsilon_r)$$

- 1 For given values of E and z , **NeuCosmA** calculates the cooling rate $t_{p\gamma}^{-1} \equiv -(1/E) b_{p\gamma} (\text{s}^{-1})$ as

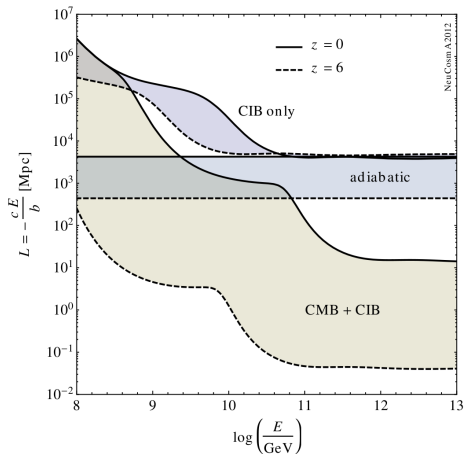
$$t_{p\gamma}^{-1} (E, z) = \sum_i^{\text{all channels}} \Gamma_{p \rightarrow p}^i (E, z) K^i ,$$

with $K^i E$ the loss of energy per interaction

- 2 From this, we calculate back $b_{p\gamma} (\text{GeV s}^{-1}) \dots$
- 3 \dots and the corresponding energy-loss term in the transport equation, $\partial_E (b_{p\gamma} Y_p)$.

S. HÜMMER, M. RÜGER, F. SPANIER, W. WINTER, *Astrophys. J.* **721**, 630 (2010) [1002.1310]

Note that $L_{\text{CIB}} \gg L_{\text{CMB}}$:



Matches, e.g., H. TAKAMI, K. MURASE, S. NAGATAKI, K. SATO, *Astropart. Phys.* **31**, 201 (2009) [0704.0979]

Secondary injection of neutrons, neutrinos ($\text{GeV}^{-1} \text{cm}^{-3} \text{s}^{-1}$)

$$Q'(E') = \int_{E'}^{\infty} \frac{dE'_p}{E'_p} N'_p(E'_p) \int_0^{\infty} c d\varepsilon' N'_\gamma(\varepsilon') R(E', E'_p, \varepsilon')$$

Normalisation to the observed GRB photon flux F_γ

$$\int \varepsilon' N'_\gamma(\varepsilon') d\varepsilon' = \frac{E'_{\text{iso}}}{V'_{\text{iso}}} \propto F_\gamma, \quad \int E'_p N'_p(E'_p) dE'_p = \frac{1}{f_e} \frac{E'_{\text{iso}}}{V'_{\text{iso}}} \propto \frac{F_\gamma}{f_e}$$

Fluence per shell, at Earth ($\text{GeV}^{-1} \text{cm}^{-2}$)

$$\mathcal{F}^{\text{sh}} = t_v V'_{\text{iso}} \frac{(1+z)^2}{4\pi d_L^2} Q'$$

Secondary injection of neutrons, neutrinos ($\text{GeV}^{-1} \text{ cm}^{-3} \text{ s}^{-1}$)

$$Q'(E') = \int_{E'}^{\infty} \frac{dE'_p}{E'_p} N'_p(E'_p) \int_0^{\infty} c d\varepsilon' N'_\gamma(\varepsilon') R(E', E'_p, \varepsilon')$$

► Photon density, shock rest frame ($\text{GeV}^{-1} \text{ cm}^{-3}$):

$$N'_\gamma(\varepsilon') \propto \begin{cases} (\varepsilon')^{-\alpha_\gamma}, & \varepsilon'_{\gamma,\min} = 0.2 \text{ eV} \leq \varepsilon' \leq \varepsilon'_{\gamma,\text{break}} \\ (\varepsilon')^{-\beta_\gamma}, & \varepsilon'_{\gamma,\text{break}} \leq \varepsilon' \leq \varepsilon'_{\gamma,\max} = 300 \times \varepsilon'_{\gamma,\min} \end{cases}$$

$$\varepsilon'_{\gamma,\text{break}} = \mathcal{O}(\text{keV}), \alpha_\gamma \approx 1, \beta_\gamma \approx 2$$

► Proton density:

$$N'_p(E'_p) \propto (E'_p)^{-\alpha_p} \times \exp \left[- (E'_p / E'_{p,\max})^2 \right] \quad (\alpha_p \approx 2)$$

Maximum proton energy limited by energy losses:

$$t'_{\text{acc}}(E'_{p,\max}) = \min [t'_{\text{dyn}}, t'_{\text{syn}}(E'_{p,\max}), t'_{p\gamma}(E'_{p,\max})]$$

Secondary injection of neutrons, neutrinos ($\text{GeV}^{-1} \text{ cm}^{-3} \text{ s}^{-1}$)

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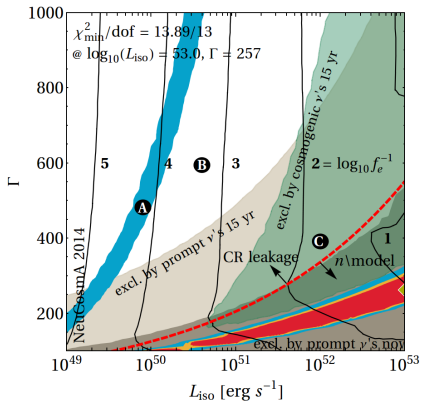
Fluence per shell, at Earth ($\text{GeV}^{-1} \text{cm}^{-2}$)

$$\mathcal{F}^{\text{sh}} = t_v V'_{\text{iso}} \frac{(1+z)^2}{4\pi d_L^2} Q'$$

Constraints: SFR vs. GRB redshift evolution

The exclusion from cosmogenic ν 's grows if the number of GRBs evolves more strongly with redshift:

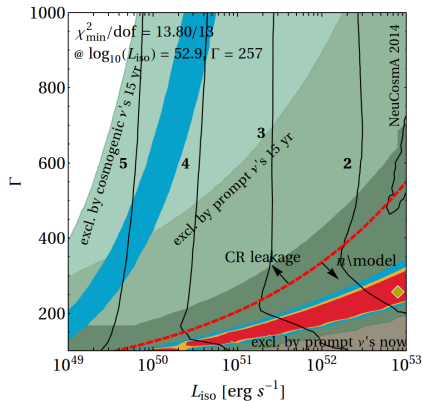
direct p escape, $\eta = 1.0$



$$n_{\text{GRB}}(z) \propto \rho_{\text{SFR}}(z)$$

(star formation rate)

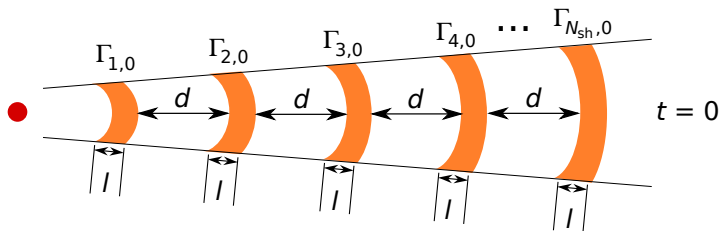
direct p escape, $\eta = 1.0$



$$n_{\text{GRB}}(z) \propto \rho_{\text{SFR}}(z) \times (1+z)^{1.2}$$

P. BAERWALD, MB, AND W. WINTER, *Astropart. Phys.* **62**, 66 (2015)

Initial number of shells: $N_{\text{sh}} \gtrsim 1000$



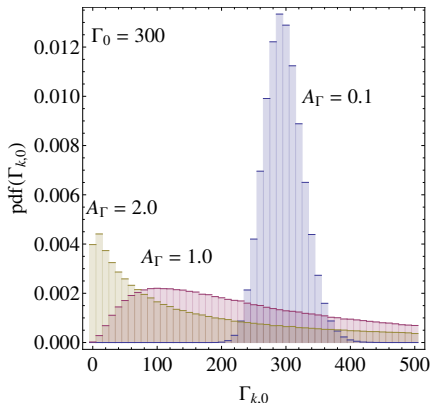
Initial values of shell parameters:

- ▶ Separation between shells: $d = l$
- ▶ Kinetic energy $E_{\text{kin},0}^{\text{iso}}$ equal for all collisions ($\sim 10^{52}$ erg)
- ▶ Speeds $\Gamma_{k,0}$ follow a distribution (see backup)
- ▶ Masses: $m_{k,0} = E_{\text{kin},0}^{\text{iso}} / (\Gamma_{k,0} c^2)$

Distribution of initial shell speeds (Lorentz factors):

$$\ln \left(\frac{\Gamma_{k,0} - 1}{\Gamma_0 - 1} \right) = A_{\Gamma} x$$

x follows a Gaussian distribution, $P(x) dx = dx e^{-x^2/2} / \sqrt{2\pi}$



$$A_{\Gamma} < 1$$

speeds too similar, collisions only at large radii

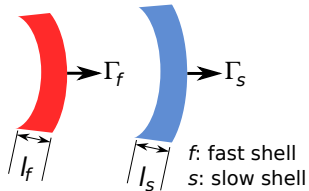
$$A_{\Gamma} \gg 1$$

spread too large, too many collisions at low radii

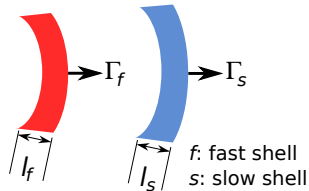
$$A_{\Gamma} \approx 1$$

just right, burst has high efficiency of conversion of kinetic to radiated energy

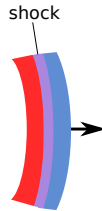
1 Propagation



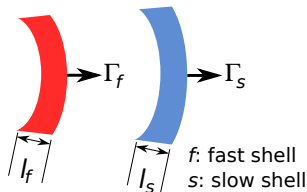
1 Propagation



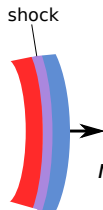
2 Collision



1 Propagation



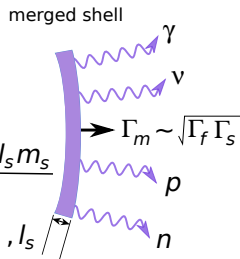
2 Collision



$$m_m = \frac{l_f m_f + l_s m_s}{l_m}$$

$$l_m < l_f, l_s$$

3 Radiation

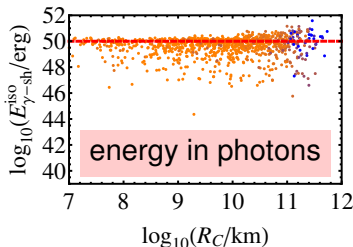
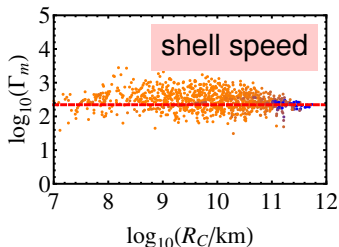
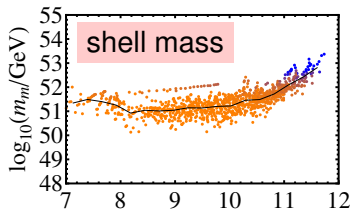
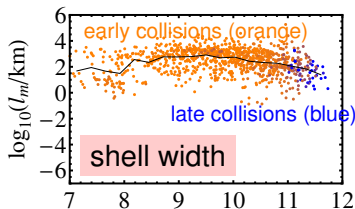


Part of the initial kinetic energy radiated as γ 's, ν 's, p 's, and n 's:

$$E_{\text{coll}}^{\text{iso}} = \left(E_{\text{kin},f}^{\text{iso}} - E_{\text{kin},m}^{\text{iso}} \right) + \left(E_{\text{kin},m}^{\text{iso}} - E_{\text{kin},s}^{\text{iso}} \right)$$

$$\underbrace{E_{\gamma\text{-sh}}^{\text{iso}} \stackrel{1/12}{\equiv} \epsilon_e E_{\text{coll}}^{\text{iso}}}_{\text{energy in photons}} \quad \underbrace{\epsilon_B E_{\text{coll}}^{\text{iso}} \stackrel{1/12}{\equiv}}_{\text{energy in magnetic fields}} \quad \underbrace{\epsilon_p E_{\text{coll}}^{\text{iso}} \stackrel{5/6}{\equiv}}_{\text{energy in baryons}}$$

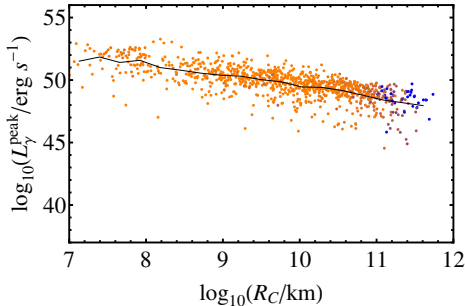
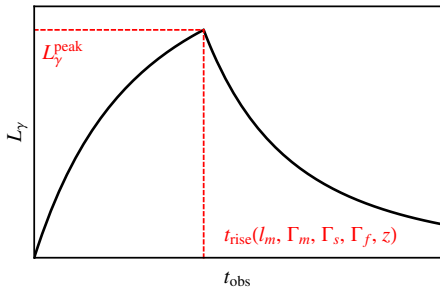
We keep track of collision parameters as the fireball expands:



MB, P. BAERWALD, K. MURASE, AND W. WINTER, 1409.2874

(For this burst: $N_{\text{sh}} = 1000$, $N_{\text{coll}} = 990$, $\Gamma_0 = 300$, $A_{\Gamma} = 1$, $E_{\gamma\text{-tot}}^{\text{iso}} = 10^{53}$ erg)

A fast-rise-exponential-decay (FRED) gamma-ray pulse is emitted in every collision:



$$L_\gamma^{\text{peak}} \sim R_C^{-2}$$

Neutrinos are stable particles ... *are they?*

So far, they seem to be

Bounds on “lifetimes” $\kappa^{-1} \equiv \tau_0/m$ of eigenstates $\nu_{1,2,3}$:

- ▶ $\kappa_1^{-1} \gtrsim 10^5 \text{ s eV}^{-1}$ (from SN 1987A)
- ▶ $\kappa_2^{-1} \gtrsim 10^{-4} \text{ s eV}^{-1}$ (from solar ν 's)
- ▶ $\kappa_3^{-1} \gtrsim 10^{-10} \text{ s eV}^{-1}$ (from atm. and long-baseline)

Very long baselines might reveal their true unstable nature

\Rightarrow cosmological neutrinos

If $\nu_{1,2,3}$ decay, their populations are governed by

$$\frac{dN_i}{dt} = -\lambda_i N_i$$

with the decay rate (s^{-1})

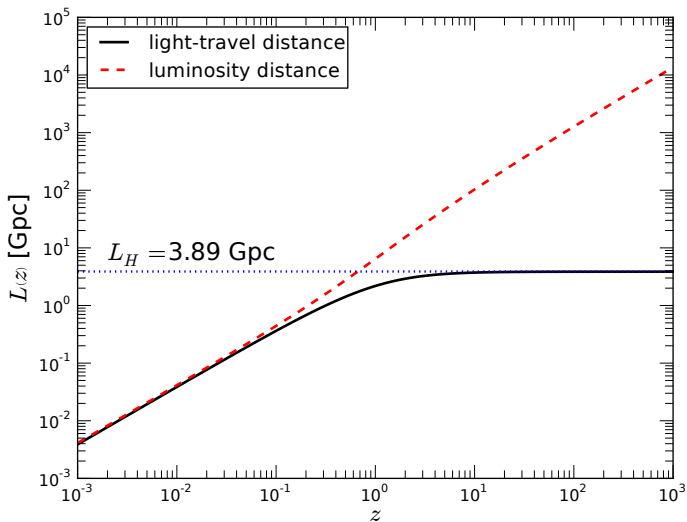
$$\lambda_i \equiv \frac{1}{\tau_i} = \frac{m_i}{\tau_{i,0}} \frac{1}{E} \equiv \frac{\kappa_i}{E}$$

Consider only decay into products invisible to the detector

Neutrinos are ultra-relativistic, so $t \approx L$

— if they are produced at a source with redshift z ,

$$L(z) \equiv \text{light-travel, or lookback distance}$$



$\nu_\alpha \rightarrow \nu_\beta$ flavour-transition probability, oscillations washed out:

$$P_{\alpha\beta} = \sum_{i=1}^3 |U_{\alpha i}|^2 |U_{\beta i}|^2 \quad (\alpha, \beta = e, \mu, \tau)$$

What if neutrinos decay?

$$P_{\alpha\beta}(E_0, z) = \sum_{i=1}^3 |U_{\alpha i}|^2 |U_{\beta i}|^2 \underbrace{\frac{N_i(E_0, z)}{N_i^0(E_0)}}_{D_i(E_0, z) \leq 1}$$

Damping factor $D_i(E_0, z)$ found by solving the decay equation

When solving, take into account:

- ① $L = L(z)$ is the light-travel distance
- ② Cosmological expansion: $E(z) = (1+z)E_0 \Rightarrow \lambda_i(z) = \frac{\kappa_i}{E_0(1+z)}$

The traditional, simplified solution

$$\frac{dN_i}{dt} = -\lambda_i N_i \xrightarrow{\text{assume } \lambda_i \text{ constant}} N_i(t) = N_i^0 e^{-\lambda_i t}$$

Only now introduce the z -dependence of λ_i and L :

$$e^{-\lambda_i t} \longrightarrow D_i(E_0, z) = [\mathcal{Z}_1(z)]^{-\kappa_i L_H/E_0}$$

VS.

The proper solution

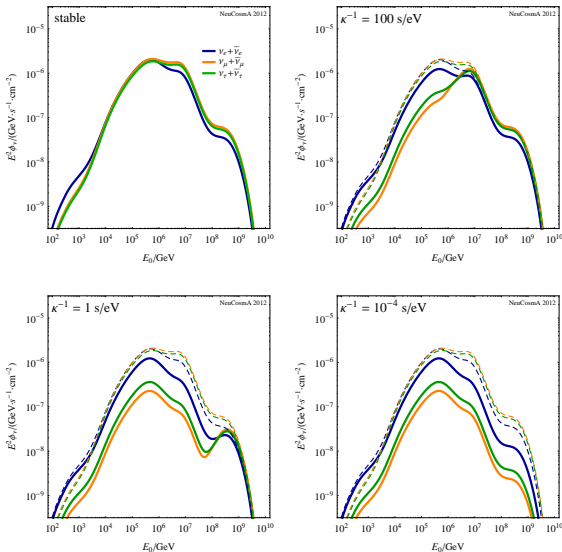
Rewrite the decay equation in terms of z from the start,

$$\frac{dN_i(E_0, z)}{dz} = -\frac{\kappa_i}{E_0} \frac{dL}{dz} \frac{N_i(E_0, z)}{1+z}$$

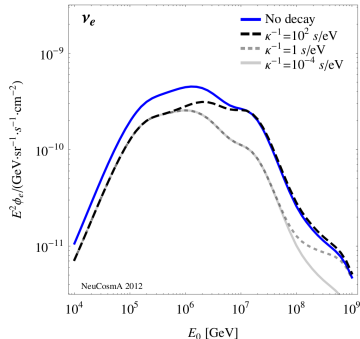
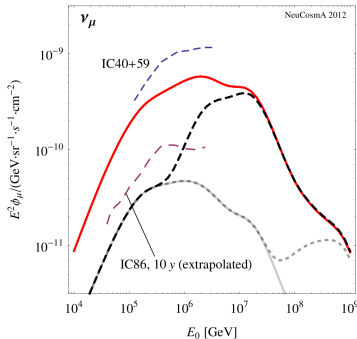
and then solve it:

$$D_i(z) = [\mathcal{Z}_2(z)]^{-\kappa_i L_H/E_0}$$

Now keep ν_1 stable (from SN 1987A) and let $\nu_{2,3}$ decay:



Quasi-diffuse flux (stacking the 117 GRBs from IC-40 analysis):



No neutrinos found because they decay, or because the baryonic loading in GRBs is smaller than anticipated?

No reliable information on astrophysical neutrino sources can be obtained from muon tracks only