Honing in on the flavor composition of high-energy astrophysical neutrinos: the view from theory

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High-energy astrophysical neutrinos: they exist!

The era of neutrino astronomy has begun!

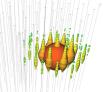
– IceCube (2010-2013) detected 37 events with 30 TeV – 2 PeV

"Bert", 1.04 PeV

"Ernie", 1.14 PeV

"Big Bird", 2 PeV







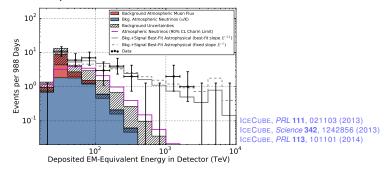
... and 34 more events < 385 TeV



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Diffuse flux compatible with extragalactic origin (Waxman & Bahcall 1997):

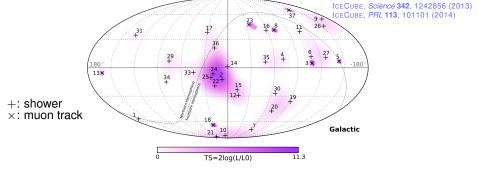
$$E^2\Phi_{\nu} = (0.95 \pm 0.3) \times 10^{-8} \; \text{GeV cm}^{-2} \; \text{s}^{-1} \; \text{sr}^{-1} \; \text{(per flavour)}$$

High-energy astrophysical neutrinos: they exist!

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Arrival directions compatible with an isotropic distribution –



no association with sources found yet

ICECUBE, PRL 111, 021103 (2013)

Flavor composition of neutrinos: an open question

What is the proportion of ν_e , ν_u , ν_τ in the diffuse flux?

Knowing this can reveal two important pieces of information:

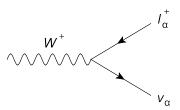
- the physical conditions at the neutrino sources; and
- whether there is new physics, and of what kind

A quick review of neutrino mixing (I)

▶ Two bases:

$$\underbrace{\{\nu_{\textit{e}},\nu_{\mu},\nu_{\tau}\}}_{\text{flavor eigenstates}} \neq \underbrace{\{\nu_{1},\nu_{2},\nu_{3}\}}_{\text{mass eigenstates}}$$

► Flavor eigenstate ν_{α} ($\alpha = e, \mu, \tau$): accompanies the charged anti-lepton I_{α}^{+} that is created in a charged-current weak interaction:



- ▶ Mass eigenstate ν_i (i = 1, 2, 3): has a definite mass
- ▶ Bases connected by a rotation U: $\begin{pmatrix} \nu_e \\ \nu_\mu \\ \nu_\tau \end{pmatrix} = U \begin{pmatrix} \nu_1 \\ \nu_2 \\ \nu_3 \end{pmatrix}$

A quick review of neutrino mixing (II)

▶ *U* is a 3×3 rotation matrix (PMNS matrix):

$$U = \left(egin{array}{ccc} U_{e1} & U_{e2} & U_{e3} \ U_{\mu 1} & U_{\mu 2} & U_{\mu 3} \ U_{\tau 1} & U_{\tau 2} & U_{\tau 3} \ \end{array}
ight)$$

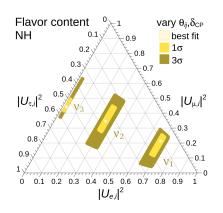
- Parametrise it with three angles and one CP-violating phase
- From solar, atmospheric, reactor, and accelerator experiments:

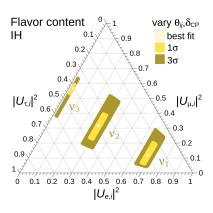
$$\theta_{12}\approx 37^\circ\,,\;\theta_{23}\approx 45^\circ\,,\;\theta_{13}\approx 9^\circ\,,\;\delta_{CP}$$
 unknown

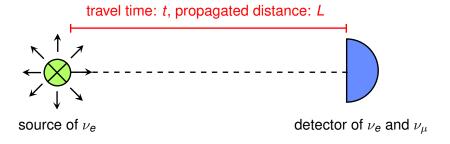
- The mass hierarchy is also unknown:
 - Normal hierarchy (NH): ν₁ is lightest
 - ► Inverted hierarchy (IH): ν₃ is lightest
 - fits to mixing paramters depend on hierarchy assumption

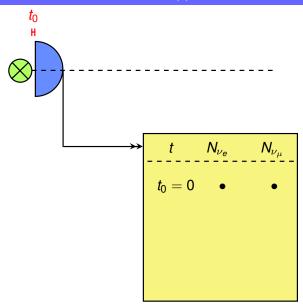
Flavor content of the mass eigenstates ν_1 , ν_2 , ν_3

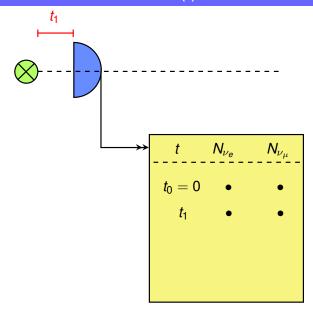
A different way to show this information is via ternary plots:

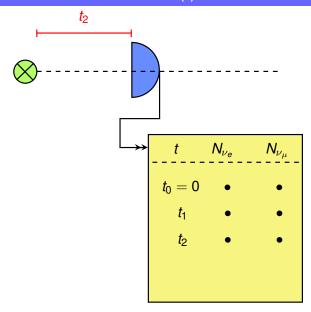


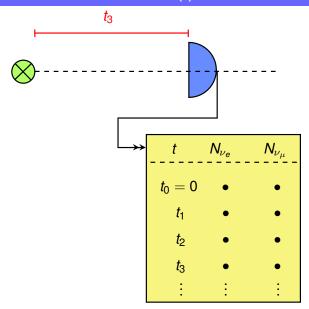




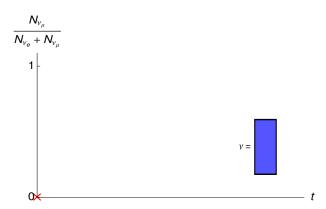


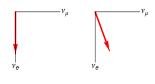


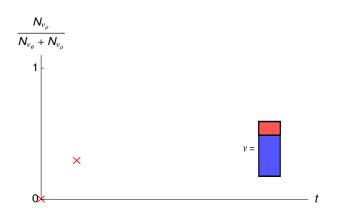




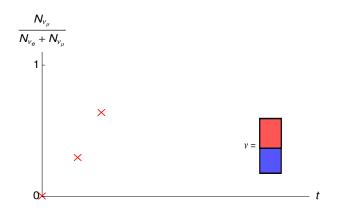


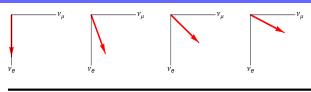




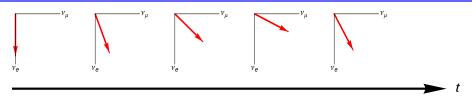




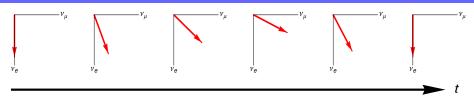


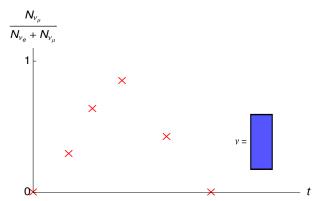


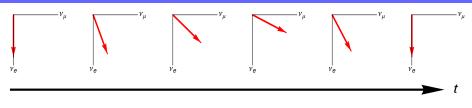


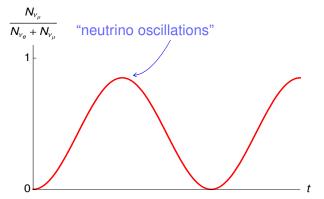












Flavor mixing in high-energy astrophysical neutrinos

A technicality:

$$P_{\overline{\nu}_{\alpha} \to \overline{\nu}_{\beta}} = \delta_{\alpha\beta} - 4\sum_{k>j} \operatorname{Re}\left(J_{\alpha\beta jk}\right) \sin^{2}\left(\frac{\Delta m_{kj}^{2}L}{4E}\right) \pm 2\sum_{k>j} \operatorname{Im}\left(J_{\alpha\beta jk}\right) \sin\left(\frac{\Delta m_{kj}^{2}L}{2E}\right)$$

- ▶ The Δm_{kj}^2 are very small: $\sim 10^{-4}$, 10^{-3} eV²
- ▶ Therefore, oscillations are very rapid
- They average out after only a few oscillations lengths:

$$\sin^2(\ldots) \to 1/2 \;,\;\; \sin(\ldots) \to 0$$

Hence, for astrophysical neutrinos:

$$P_{\overleftarrow{\nu}_{\alpha} \to \overleftarrow{\nu}_{\beta}} = \sum_{i=1}^{3} |U_{\alpha i}|^{2} |U_{\beta i}|^{2}$$

Flavor ratios

Neutrino production at the source via pion decay:

$$p\gamma o \Delta^+$$
(1232) $o \pi^+ n$ $\pi^+ o \mu^+
u_\mu o e^+
u_e ar{
u}_\mu
u_\mu$

- ▶ Flavor ratios at the source: $(f_e: f_\mu: f_\tau)_S \approx (1/3:2/3:0)$
- At Earth, due to flavor mixing:

$$f_{\alpha,\oplus} = \sum_{\beta} P_{\beta\alpha} f_{\beta,S}$$

$$(1/3:2/3:0)_S \xrightarrow{\text{flavor mixing, NH, best-fit}} (0.36:0.32:0.32)_{\oplus}$$

Other compositions at the source:

```
(0:1:0)_{S} \longrightarrow (0.26:0.36:0.38)_{\oplus} ("muon damped")

(1:0:0)_{S} \longrightarrow (0.55:0.26:0.19)_{\oplus} ("neutron decay")

(1:1:0)_{S} \longrightarrow (0.40:0.31:0.29)_{\oplus} ("charmed decays")
```

How can IceCube identify flavor?

Below $E_{\nu} \sim$ 10 PeV, there are two event topologies:

- ▶ Showers: generated by CC ν_e or ν_τ ; or by NC ν_x
- ▶ Muon tracks: generated by CC ν_{μ}

(Some muon tracks can be mis-reconstructed as showers)

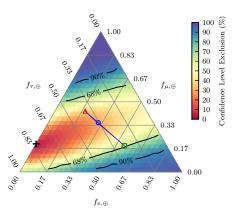
At \gtrsim 10 PeV (no events so far), all of the above, plus:

- ▶ Glashow resonance: CC $\bar{\nu}_e e$ interactions at 6.3 PeV
- ▶ Double bangs: CC $\nu_{\tau} \rightarrow \tau \rightarrow \nu_{\tau}$

Flavor ratios must be inferred from the number of showers and tracks

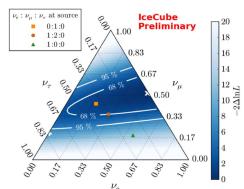
Two IceCube analyses of flavor composition

Using contained events only



Best fit: (0:0.2:0.8)

Using contained events + throughgoing muons

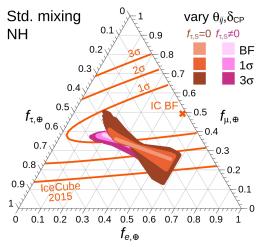


Best fit: (0.49 : 0.51 : 0)_⊕

- Compatible with standard source compositions
- Bounds are weak need more data and better flavor-tagging

Flavor combinations at Earth from flavor mixing

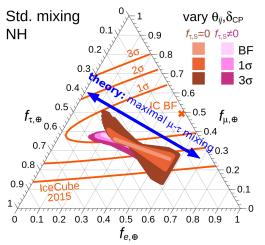
But we do not really know the flavor composition at the source:



Std. mixing can access $only \sim 10\%$ of the possible combinations

Flavor combinations at Earth from flavor mixing

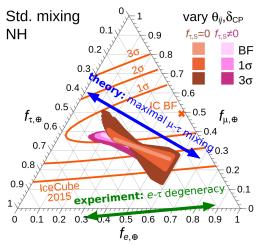
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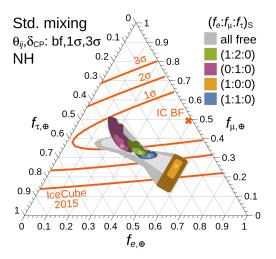
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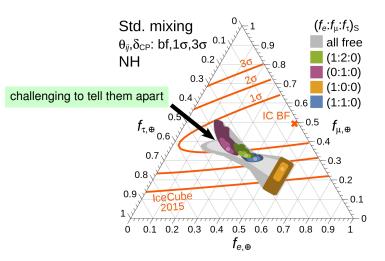
Selected source compositions

We can look at results for particular choices of ratios at the source:



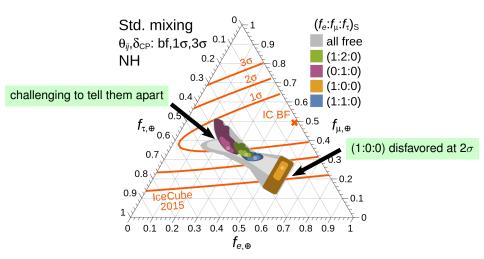
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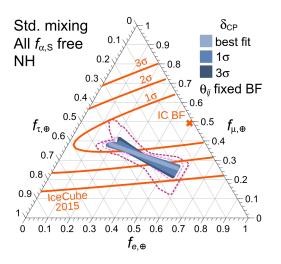
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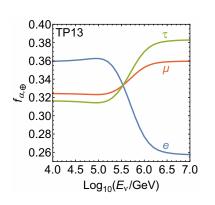
Perfect knowledge of mixing angles

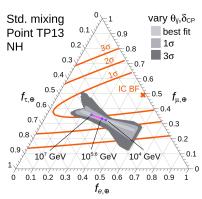
In a few years, we might know all the mixing parameters except δ_{CP} :



Energy dependence of the composition at the source

Different ν production channels are accessible at different energies:

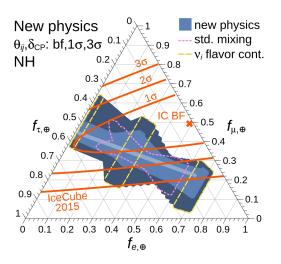




- Equivalent to different sources types contributing to the diffuse flux
- Will be difficult to resolve

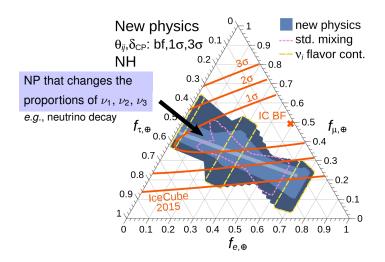
New physics (warning: work in progress)

New physics could modify the flavor ratios at Earth:



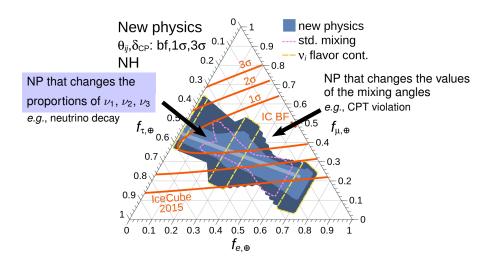
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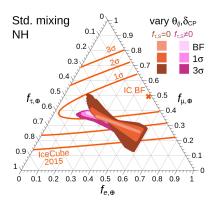


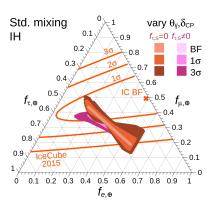
Conclusions ... and the future

- Flavor composition provides information about the sources
- \blacktriangleright Std. mixing can access only \sim 10% of the possible flavor combinations at Earth
- "Milder" new physics can access only 25% of flavor combinations
- It is challenging to think what lies beyond this region
- IceCube searches could use these theoretical considerations to improve constraints

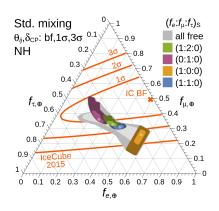
Backup slides

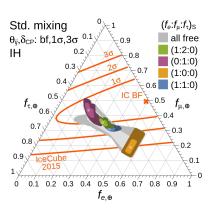
Flavor combinations from flavor mixing: NH vs. IH





Selected source compositions: NH vs. IH





Perfect knowledge of mixing angles: NH vs. IH

